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1.1 Installing scikit-learn

Note: If you wish to contribute to the project, it’s recommended you *install the latest development version.*

1.1.1 Installing the latest release

Scikit-learn requires:

- Python (&ge; 2.7 or &ge; 3.3),
- NumPy (&ge; 1.8.2),
- SciPy (&ge; 0.13.3).

If you already have a working installation of numpy and scipy, the easiest way to install scikit-learn is using *pip*

```
pip install -U scikit-learn
```

or *conda:*

```
conda install scikit-learn
```

If you have not installed NumPy or SciPy yet, you can also install these using conda or pip. When using pip, please ensure that *binary wheels* are used, and NumPy and SciPy are not recompiled from source, which can happen when using particular configurations of operating system and hardware (such as Linux on a Raspberry Pi). Building numpy and scipy from source can be complex (especially on Windows) and requires careful configuration to ensure that they link against an optimized implementation of linear algebra routines. Instead, use a third-party distribution as described below.

If you must install scikit-learn and its dependencies with pip, you can install it as *scikit-learn[alldeps]*. The most common use case for this is in a requirements.txt file used as part of an automated build process for a PaaS application or a Docker image. This option is not intended for manual installation from the command line.

1.1.2 Third-party Distributions

If you don’t already have a python installation with numpy and scipy, we recommend to install either via your package manager or via a python bundle. These come with numpy, scipy, scikit-learn, matplotlib and many other helpful
scientific and data processing libraries.
Available options are:

**Canopy and Anaconda for all supported platforms**

Canopy and Anaconda both ship a recent version of scikit-learn, in addition to a large set of scientific python library for Windows, Mac OSX and Linux.

Anaconda offers scikit-learn as part of its free distribution.

```
Warning: To upgrade or uninstall scikit-learn installed with Anaconda or conda you should not use the pip command. Instead:

To upgrade scikit-learn:
conda update scikit-learn

To uninstall scikit-learn:
conda remove scikit-learn

Upgrading with pip install -U scikit-learn or uninstalling pip uninstall scikit-learn is likely to fail to properly remove files installed by the conda command.

pip upgrade and uninstall operations only work on packages installed via pip install.
```

**WinPython for Windows**

The WinPython project distributes scikit-learn as an additional plugin.

For installation instructions for particular operating systems or for compiling the bleeding edge version, see the Advanced installation instructions.

### 1.2 Frequently Asked Questions

Here we try to give some answers to questions that regularly pop up on the mailing list.

#### 1.2.1 What is the project name (a lot of people get it wrong)?

scikit-learn, but not scikit or SciKit nor sci-kit learn. Also not scikits.learn or scikits-learn, which were previously used.

#### 1.2.2 How do you pronounce the project name?

sy-kit learn. sci stands for science!

#### 1.2.3 Why scikit?

There are multiple scikits, which are scientific toolboxes built around SciPy. You can find a list at https://scikits.appspot.com/scikits. Apart from scikit-learn, another popular one is scikit-image.
1.2.4 How can I contribute to scikit-learn?

See Contributing. Before wanting to add a new algorithm, which is usually a major and lengthy undertaking, it is recommended to start with known issues. Please do not contact the contributors of scikit-learn directly regarding contributing to scikit-learn.

1.2.5 What's the best way to get help on scikit-learn usage?

For general machine learning questions, please use Cross Validated with the [machine-learning] tag.

For scikit-learn usage questions, please use Stack Overflow with the [scikit-learn] and [python] tags. You can alternatively use the mailing list.

Please make sure to include a minimal reproduction code snippet (ideally shorter than 10 lines) that highlights your problem on a toy dataset (for instance from sklearn.datasets or randomly generated with functions of numpy.random with a fixed random seed). Please remove any line of code that is not necessary to reproduce your problem.

The problem should be reproducible by simply copy-pasting your code snippet in a Python shell with scikit-learn installed. Do not forget to include the import statements.

More guidance to write good reproduction code snippets can be found at:
http://stackoverflow.com/help/mcve

If your problem raises an exception that you do not understand (even after googling it), please make sure to include the full traceback that you obtain when running the reproduction script.

For bug reports or feature requests, please make use of the issue tracker on GitHub.

There is also a scikit-learn Gitter channel where some users and developers might be found.

Please do not email any authors directly to ask for assistance, report bugs, or for any other issue related to scikit-learn.

1.2.6 How can I create a bunch object?

Don’t make a bunch object! They are not part of the scikit-learn API. Bunch objects are just a way to package some numpy arrays. As a scikit-learn user you only ever need numpy arrays to feed your model with data.

For instance to train a classifier, all you need is a 2D array $X$ for the input variables and a 1D array $y$ for the target variables. The array $X$ holds the features as columns and samples as rows. The array $y$ contains integer values to encode the class membership of each sample in $X$.

1.2.7 How can I load my own datasets into a format usable by scikit-learn?

Generally, scikit-learn works on any numeric data stored as numpy arrays or scipy sparse matrices. Other types that are convertible to numeric arrays such as pandas DataFrame are also acceptable.

For more information on loading your data files into these usable data structures, please refer to loading external datasets.

1.2.8 What are the inclusion criteria for new algorithms?

We only consider well-established algorithms for inclusion. A rule of thumb is at least 3 years since publication, 200+ citations and wide use and usefulness. A technique that provides a clear-cut improvement (e.g. an enhanced data structure or a more efficient approximation technique) on a widely-used method will also be considered for inclusion.
From the algorithms or techniques that meet the above criteria, only those which fit well within the current API of scikit-learn, that is a `fit`, `predict/transform` interface and ordinarily having input/output that is a numpy array or sparse matrix, are accepted.

The contributor should support the importance of the proposed addition with research papers and/or implementations in other similar packages, demonstrate its usefulness via common use-cases/applications and corroborate performance improvements, if any, with benchmarks and/or plots. It is expected that the proposed algorithm should outperform the methods that are already implemented in scikit-learn at least in some areas.

Also note that your implementation need not be in scikit-learn to be used together with scikit-learn tools. You can implement your favorite algorithm in a scikit-learn compatible way, upload it to github and let us know. We will list it under Related Projects.

### 1.2.9 Why are you so selective on what algorithms you include in scikit-learn?

Code is maintenance cost, and we need to balance the amount of code we have with the size of the team (and add to this the fact that complexity scales non linearly with the number of features). The package relies on core developers using their free time to fix bugs, maintain code and review contributions. Any algorithm that is added needs future attention by the developers, at which point the original author might long have lost interest. Also see this thread on the mailing list.

### 1.2.10 Why did you remove HMMs from scikit-learn?

See Will you add graphical models or sequence prediction to scikit-learn?.

### 1.2.11 Will you add graphical models or sequence prediction to scikit-learn?

Not in the foreseeable future. scikit-learn tries to provide a unified API for the basic tasks in machine learning, with pipelines and meta-algorithms like grid search to tie everything together. The required concepts, APIs, algorithms and expertise required for structured learning are different from what scikit-learn has to offer. If we started doing arbitrary structured learning, we’d need to redesign the whole package and the project would likely collapse under its own weight.

There are two project with API similar to scikit-learn that do structured prediction:

- pystruct handles general structured learning (focuses on SSVMs on arbitrary graph structures with approximate inference; defines the notion of sample as an instance of the graph structure)
- seqlearn handles sequences only (focuses on exact inference; has HMMs, but mostly for the sake of completeness; treats a feature vector as a sample and uses an offset encoding for the dependencies between feature vectors)

### 1.2.12 Will you add GPU support?

No, or at least not in the near future. The main reason is that GPU support will introduce many software dependencies and introduce platform specific issues. scikit-learn is designed to be easy to install on a wide variety of platforms. Outside of neural networks, GPUs don’t play a large role in machine learning today, and much larger gains in speed can often be achieved by a careful choice of algorithms.
1.2.13 Do you support PyPy?

In case you didn’t know, PyPy is the new, fast, just-in-time compiling Python implementation. We don’t support it. When the NumPy support in PyPy is complete or near-complete, and SciPy is ported over as well, we can start thinking of a port. We use too much of NumPy to work with a partial implementation.

1.2.14 How do I deal with string data (or trees, graphs...)?

scikit-learn estimators assume you’ll feed them real-valued feature vectors. This assumption is hard-coded in pretty much all of the library. However, you can feed non-numerical inputs to estimators in several ways.

If you have text documents, you can use a term frequency features; see Text feature extraction for the built-in text vectorizers. For more general feature extraction from any kind of data, see Loading features from dicts and Feature hashing.

Another common case is when you have non-numerical data and a custom distance (or similarity) metric on these data. Examples include strings with edit distance (aka. Levenshtein distance; e.g., DNA or RNA sequences). These can be encoded as numbers, but doing so is painful and error-prone. Working with distance metrics on arbitrary data can be done in two ways.

Firstly, many estimators take precomputed distance/similarity matrices, so if the dataset is not too large, you can compute distances for all pairs of inputs. If the dataset is large, you can use feature vectors with only one “feature”, which is an index into a separate data structure, and supply a custom metric function that looks up the actual data in this data structure. E.g., to use DBSCAN with Levenshtein distances:

```python
from leven import levenshtein
from sklearn.cluster import dbscan

data = ["ACCTCTAGAAG", "ACCTACTAGAAGAT", "GAATATTAGGCCGA"]

def lev_metric(x, y):
    i, j = int(x[0]), int(y[0])  # extract indices
    return levenshtein(data[i], data[j])

X = np.arange(len(data)).reshape(-1, 1)

dbscan(X, metric=lev_metric, eps=5, min_samples=2)
```

(This uses the third-party edit distance package leven.)

Similar tricks can be used, with some care, for tree kernels, graph kernels, etc.

1.2.15 Why do I sometime get a crash/freeze with n_jobs > 1 under OSX or Linux?

Several scikit-learn tools such as GridSearchCV and cross_val_score rely internally on Python’s multiprocessing module to parallelize execution onto several Python processes by passing n_jobs > 1 as argument.

The problem is that Python multiprocessing does a fork system call without following it with an exec system call for performance reasons. Many libraries like (some versions of) Accelerate / vecLib under OSX, (some versions of) MKL, the OpenMP runtime of GCC, nvidia’s Cuda (and probably many others), manage their own internal thread pool. Upon a call to fork, the thread pool state in the child process is corrupted: the thread pool believes it has many threads while only the main thread state has been forked. It is possible to change the libraries to make them detect...
when a fork happens and reinitialize the thread pool in that case: we did that for OpenBLAS (merged upstream in master since 0.2.10) and we contributed a patch to GCC’s OpenMP runtime (not yet reviewed).

But in the end the real culprit is Python’s `multiprocessing` that does `fork` without `exec` to reduce the overhead of starting and using new Python processes for parallel computing. Unfortunately this is a violation of the POSIX standard and therefore some software editors like Apple refuse to consider the lack of fork-safety in Accelerate / vecLib as a bug.

In Python 3.4+ it is now possible to configure `multiprocessing` to use the ‘forkserver’ or ‘spawn’ start methods (instead of the default ‘fork’) to manage the process pools. To work around this issue when using scikit-learn, you can set the JOBLIB_START_METHOD environment variable to ‘forkserver’. However the user should be aware that using the ‘forkserver’ method prevents joblib.Parallel to call function interactively defined in a shell session.

If you have custom code that uses `multiprocessing` directly instead of using it via joblib you can enable the ‘forkserver’ mode globally for your program: Insert the following instructions in your main script:

```python
import multiprocessing

# other imports, custom code, load data, define model...

if __name__ == '__main__':
    multiprocessing.set_start_method('forkserver')

    # call scikit-learn utils with n_jobs > 1 here
```

You can find more default on the new start methods in the `multiprocessing` documentation.

### 1.2.16 Why is there no support for deep or reinforcement learning? / Will there be support for deep or reinforcement learning in scikit-learn?

Deep learning and reinforcement learning both require a rich vocabulary to define an architecture, with deep learning additionally requiring GPUs for efficient computing. However, neither of these fit within the design constraints of scikit-learn; as a result, deep learning and reinforcement learning are currently out of scope for what scikit-learn seeks to achieve.

You can find more information about addition of gpu support at [Will you add GPU support?](https://scikit-learn.org/0.20/extras.html).

### 1.2.17 Why is my pull request not getting any attention?

The scikit-learn review process takes a significant amount of time, and contributors should not be discouraged by a lack of activity or review on their pull request. We care a lot about getting things right the first time, as maintenance and later change comes at a high cost. We rarely release any “experimental” code, so all of our contributions will be subject to high use immediately and should be of the highest quality possible initially.

Beyond that, scikit-learn is limited in its reviewing bandwidth; many of the reviewers and core developers are working on scikit-learn on their own time. If a review of your pull request comes slowly, it is likely because the reviewers are busy. We ask for your understanding and request that you not close your pull request or discontinue your work solely because of this reason.

### 1.2.18 How do I set a random_state for an entire execution?

For testing and replicability, it is often important to have the entire execution controlled by a single seed for the pseudo-random number generator used in algorithms that have a randomized component. Scikit-learn does not use its own global random state; whenever a RandomState instance or an integer random seed is not provided as an argument, it
relies on the numpy global random state, which can be set using `numpy.random.seed`. For example, to set an execution’s numpy global random state to 42, one could execute the following in his or her script:

```python
import numpy as np
np.random.seed(42)
```

However, a global random state is prone to modification by other code during execution. Thus, the only way to ensure replicability is to pass `RandomState` instances everywhere and ensure that both estimators and cross-validation splitters have their `random_state` parameter set.

### 1.3 Support

There are several ways to get in touch with the developers.

#### 1.3.1 Mailing List

- The main mailing list is scikit-learn.
- There is also a commit list scikit-learn-commits, where updates to the main repository and test failures get notified.

#### 1.3.2 User questions

- Some scikit-learn developers support users on StackOverflow using the `[scikit-learn]` tag.
- For general theoretical or methodological Machine Learning questions stack exchange is probably a more suitable venue.

In both cases please use a descriptive question in the title field (e.g. no “Please help with scikit-learn!” as this is not a question) and put details on what you tried to achieve, what were the expected results and what you observed instead in the details field.

Code and data snippets are welcome. Minimalistic (up to ~20 lines long) reproduction script very helpful.

Please describe the nature of your data and the how you preprocessed it: what is the number of samples, what is the number and type of features (i.d. categorical or numerical) and for supervised learning tasks, what target are you trying to predict: binary, multiclass (1 out of `n_classes`) or multilabel (`k` out of `n_classes`) classification or continuous variable regression.

#### 1.3.3 Bug tracker

If you think you’ve encountered a bug, please report it to the issue tracker:

https://github.com/scikit-learn/scikit-learn/issues

Don’t forget to include:

- steps (or better script) to reproduce,
- expected outcome,
- observed outcome or python (or gdb) tracebacks
To help developers fix your bug faster, please link to a https://gist.github.com holding a standalone minimalistic python script that reproduces your bug and optionally a minimalistic subsample of your dataset (for instance exported as CSV files using numpy.savetxt).

Note: gists are git cloneable repositories and thus you can use git to push datafiles to them.

1.3.4 IRC

Some developers like to hang out on channel #scikit-learn on irc.freenode.net.

If you do not have an IRC client or are behind a firewall this web client works fine: http://webchat.freenode.net

1.3.5 Documentation resources

This documentation is relative to 0.20.dev0. Documentation for other versions can be found here:

- 0.18
- 0.17
- 0.16
- 0.15

Printable pdf documentation for all versions can be found here.

1.4 Related Projects

Projects implementing the scikit-learn estimator API are encouraged to use the scikit-learn-contrib template which facilitates best practices for testing and documenting estimators. The scikit-learn-contrib GitHub organisation also accepts high-quality contributions of repositories conforming to this template.

Below is a list of sister-projects, extensions and domain specific packages.

1.4.1 Interoperability and framework enhancements

These tools adapt scikit-learn for use with other technologies or otherwise enhance the functionality of scikit-learn’s estimators.

Data formats

- sklearn_pandas bridge for scikit-learn pipelines and pandas data frame with dedicated transformers.

Auto-ML

- auto_ml Automated machine learning for production and analytics, built on scikit-learn and related projects. Trains a pipeline with all the standard machine learning steps. Tuned for prediction speed and ease of transfer to production environments.
- auto-sklearn An automated machine learning toolkit and a drop-in replacement for a scikit-learn estimator
- TPOT An automated machine learning toolkit that optimizes a series of scikit-learn operators to design a machine learning pipeline, including data and feature preprocessors as well as the estimators. Works as a drop-in replacement for a scikit-learn estimator.

Experimentation frameworks

- REP Environment for conducting data-driven research in a consistent and reproducible way
• **ML Frontend** provides dataset management and SVM fitting/prediction through web-based and programmatic interfaces.

• **Scikit-Learn Laboratory** A command-line wrapper around scikit-learn that makes it easy to run machine learning experiments with multiple learners and large feature sets.

• **Xcessiv** is a notebook-like application for quick, scalable, and automated hyperparameter tuning and stacked ensembling. Provides a framework for keeping track of model-hyperparameter combinations.

**Model inspection and visualisation**

• **eli5** A library for debugging/inspecting machine learning models and explaining their predictions.

• **mlxtend** Includes model visualization utilities.

• **scikit-plot** A visualization library for quick and easy generation of common plots in data analysis and machine learning.

• **yellowbrick** A suite of custom matplotlib visualizers for scikit-learn estimators to support visual feature analysis, model selection, evaluation, and diagnostics.

**Model export for production**

• **sklearn-pmml** Serialization of (some) scikit-learn estimators into PMML.

• **sklearn2pmml** Serialization of a wide variety of scikit-learn estimators and transformers into PMML with the help of JPMML-SkLearn library.

• **sklearn-porter** Transpile trained scikit-learn models to C, Java, Javascript and others.

• **sklearn-compiledtrees** Generate a C++ implementation of the predict function for decision trees (and ensembles) trained by sklearn. Useful for latency-sensitive production environments.

### 1.4.2 Other estimators and tasks

Not everything belongs or is mature enough for the central scikit-learn project. The following are projects providing interfaces similar to scikit-learn for additional learning algorithms, infrastructures and tasks.

**Structured learning**

• **Seqlearn** Sequence classification using HMMs or structured perceptron.

• **HMMLearn** Implementation of hidden markov models that was previously part of scikit-learn.

• **PyStruct** General conditional random fields and structured prediction.

• **pomegranate** Probabilistic modelling for Python, with an emphasis on hidden Markov models.

• **sklearn-crfsuite** Linear-chain conditional random fields (CRFsuite wrapper with sklearn-like API).

**Deep neural networks etc.**

• **pylearn2** A deep learning and neural network library build on theano with scikit-learn like interface.

• **sklearn_theano** scikit-learn compatible estimators, transformers, and datasets which use Theano internally.

• **nolearn** A number of wrappers and abstractions around existing neural network libraries.

• **keras** Deep Learning library capable of running on top of either TensorFlow or Theano.

• **lasagne** A lightweight library to build and train neural networks in Theano.

**Broad scope**

• **mlxtend** Includes a number of additional estimators as well as model visualization utilities.

• **sparkit-learn** Scikit-learn API and functionality for PySpark’s distributed modelling.
Other regression and classification

- **xgboost** Optimised gradient boosted decision tree library.
- **ML-Ensemble** Generalized ensemble learning (stacking, blending, subsemble, deep ensembles, etc.).
- **lightning** Fast state-of-the-art linear model solvers (SDCA, AdaGrad, SVRG, SAG, etc.).
- **py-earth** Multivariate adaptive regression splines.
- **Kernel Regression** Implementation of Nadaraya-Watson kernel regression with automatic bandwidth selection.
- **gplearn** Genetic Programming for symbolic regression tasks.
- **multiisotonic** Isotonic regression on multidimensional features.

Decomposition and clustering

- **lda:** Fast implementation of latent Dirichlet allocation in Cython which uses Gibbs sampling to sample from the true posterior distribution. (scikit-learn’s `sklearn.decomposition.LatentDirichletAllocation` implementation uses variational inference to sample from a tractable approximation of a topic model’s posterior distribution.)
- **Sparse Filtering** Unsupervised feature learning based on sparse-filtering.
- **kmodes** k-modes clustering algorithm for categorical data, and several of its variations.
- **hdbscan** HDBSCAN and Robust Single Linkage clustering algorithms for robust variable density clustering.
- **spherecluster** Spherical K-means and mixture of von Mises Fisher clustering routines for data on the unit hypersphere.

Pre-processing

- **categorical-encoding** A library of sklearn compatible categorical variable encoders.
- **imbalanced-learn** Various methods to under- and over-sample datasets.

1.4.3 Statistical learning with Python

Other packages useful for data analysis and machine learning.

- **Pandas** Tools for working with heterogeneous and columnar data, relational queries, time series and basic statistics.
- **theano** A CPU/GPU array processing framework geared towards deep learning research.
- **statsmodels** Estimating and analysing statistical models. More focused on statistical tests and less on prediction than scikit-learn.
- **PyMC** Bayesian statistical models and fitting algorithms.
- **Sacred** Tool to help you configure, organize, log and reproduce experiments.
- **Seaborn** Visualization library based on matplotlib. It provides a high-level interface for drawing attractive statistical graphics.
- **Deep Learning** A curated list of deep learning software libraries.

Domain specific packages

- **scikit-image** Image processing and computer vision in python.
- **Natural language toolkit (nltk)** Natural language processing and some machine learning.
• **gensim** A library for topic modelling, document indexing and similarity retrieval
• **NiLearn** Machine learning for neuro-imaging.
• **AstroML** Machine learning for astronomy.
• **MSMBuilder** Machine learning for protein conformational dynamics time series.

1.4.4 Snippets and tidbits

The wiki has more!

1.5 About us

This is a community effort, and as such many people have contributed to it over the years.

1.5.1 History

This project was started in 2007 as a Google Summer of Code project by David Cournapeau. Later that year, Matthieu Brucher started work on this project as part of his thesis.

In 2010 Fabian Pedregosa, Gael Varoquaux, Alexandre Gramfort and Vincent Michel of INRIA took leadership of the project and made the first public release, February the 1st 2010. Since then, several releases have appeared following a ~3 month cycle, and a thriving international community has been leading the development.

1.5.2 People

The following people have been core contributors to scikit-learn’s development and maintenance:

• Mathieu Blondel
• Matthieu Brucher
• Lars Buitinck
• David Cournapeau
• Noël Dawe
• Vincent Dubourg
• Edouard Duchesnay
• Tom Dupré la Tour
• Alexander Fabisch
• Virgile Fritsch
• Satra Ghosh
• Angel Soler Gollonet
• Chris Filo Gorgolewski
• Alexandre Gramfort
• Olivier Grisel
• Jaques Grobler
• Yaroslav Halchenko
• Brian Holt
• Arnaud Joly
• Thouis (Ray) Jones
• Kyle Kastner
• Manoj Kumar
• Robert Layton
• Wei Li
• Paolo Losi
• Gilles Louppe
• Jan Hendrik Metzen
• Vincent Michel
• Jarrod Millman
• Andreas Müller (release manager)
• Vlad Niculae
• Joel Nothman
• Alexandre Passos
• Fabian Pedregosa
• Peter Prettenhofer
• Bertrand Thirion
• Jake VanderPlas
• Nelle Varoquaux
• Gael Varoquaux
• Ron Weiss

Please do not email the authors directly to ask for assistance or report issues. Instead, please see What’s the best way to ask questions about scikit-learn in the FAQ.

See also:

How you can contribute to the project

1.5.3 Citing scikit-learn

If you use scikit-learn in a scientific publication, we would appreciate citations to the following paper:


Bibtex entry:

```latex
@article{scikit-learn,
  title={Scikit-learn: Machine Learning in {P}ython},
  journal={Journal of Machine Learning Research},
  volume={12},
  pages={2825--2830},
  year={2011}
}
```

If you want to cite scikit-learn for its API or design, you may also want to consider the following paper:

API design for machine learning software: experiences from the scikit-learn project, Buitinck et al., 2013.

Bibtex entry:

```latex
@inproceedings{sklearn_api,
  author = {Lars Buitinck and Gilles Louppe and Mathieu Blondel and Fabian Pedregosa and Andreas Mueller and Olivier Grisel and Vlad Niculae and Peter Prettenhofer and Alexandre Gramfort and Jaques Grobler and Robert Layton and Jake VanderPlas and Arnaud Joly and Brian Holt and Ga"{e}l Varoquaux},
  title = {{API} design for machine learning software: experiences from the scikit-learn
  }
```
1.5.4 Artwork

High quality PNG and SVG logos are available in the doc/logos/ source directory.

1.5.5 Funding

INRIA actively supports this project. It has provided funding for Fabian Pedregosa (2010-2012), Jaques Grobler (2012-2013) and Olivier Grisel (2013-2017) to work on this project full-time. It also hosts coding sprints and other events.

Paris-Saclay Center for Data Science funded one year for a developer to work on the project full-time (2014-2015) and 50% of the time of Guillaume Lemaitre (2016-2017).

NYU Moore-Sloan Data Science Environment funded Andreas Mueller (2014-2016) to work on this project. The Moore-Sloan Data Science Environment also funds several students to work on the project part-time.

Thomas (2017) to work on scikit-learn. Columbia University funds Andreas Müller since 2016. Andreas Müller also received a grant to improve scikit-learn from the Alfred P. Sloan Foundation in 2017. The University of Sydney funds Joel Nothman since July 2017. The following students were sponsored by Google to work on scikit-learn through the Google Summer of Code program.

- 2007 - David Cournapeau
- 2011 - Vlad Niculae
- 2012 - Vlad Niculae, Immanuel Bayer.
- 2013 - Kemal Eren, Nicolas Trésegnie
- 2014 - Hamzeh Alsalhi, Issam Laradji, Maheshakya Wijewardena, Manoj Kumar.
- 2015 - Raghav RV, Wei Xue
- 2016 - Nelson Liu, YenChen Lin

It also provided funding for sprints and events around scikit-learn. If you would like to participate in the next Google Summer of code program, please see this page.

The NeuroDebian project providing Debian packaging and contributions is supported by Dr. James V. Haxby (Dartmouth College).

The PSF helped find and manage funding for our 2011 Granada sprint. More information can be found here tinyclues funded the 2011 international Granada sprint.
Donating to the project

If you are interested in donating to the project or to one of our code-sprints, you can use the *Paypal* button below or the *NumFOCUS Donations Page* (if you use the latter, please indicate that you are donating for the scikit-learn project).

All donations will be handled by *NumFOCUS*, a non-profit-organization which is managed by a board of *SciPy community members*. NumFOCUS’s mission is to foster scientific computing software, in particular in Python. As a fiscal home of scikit-learn, it ensures that money is available when needed to keep the project funded and available while in compliance with tax regulations.

The received donations for the scikit-learn project mostly will go towards covering travel-expenses for code sprints, as well as towards the organization budget of the project\(^1\).

Notes

The 2013 Paris international sprint

Fig. 1.1: IAP VII/19 - DYSCO

*For more information on this sprint, see* [here](#)

\(^1\) Regarding the organization budget in particular, we might use some of the donated funds to pay for other project expenses such as DNS, hosting or continuous integration services.
1.5.6 Infrastructure support

- We would like to thank Rackspace for providing us with a free Rackspace Cloud account to automatically build the documentation and the example gallery from for the development version of scikit-learn using this tool.
- We would also like to thank Shining Panda for free CPU time on their Continuous Integration server.

1.6 Who is using scikit-learn?

1.6.1 Spotify

Scikit-learn provides a toolbox with solid implementations of a bunch of state-of-the-art models and makes it easy to plug them into existing applications. We’ve been using it quite a lot for music recommendations at Spotify and I think it’s the most well-designed ML package I’ve seen so far.

Erik Bernhardsson, Engineering Manager Music Discovery & Machine Learning, Spotify

1.6.2 Inria

At INRIA, we use scikit-learn to support leading-edge basic research in many teams: Parietal for neuroimaging, Lear for computer vision, Visages for medical image analysis, Privatics for security. The project is a fantastic tool to address difficult applications of machine learning in an academic environment as it is performant and versatile, but all easy-to-use and well documented, which makes it well suited to grad students.

Gaël Varoquaux, research at Parietal

1.6.3 betaworks

Betaworks is a NYC-based startup studio that builds new products, grows companies, and invests in others. Over the past 8 years we’ve launched a handful of social data analytics-driven services, such as Bitly, Chartbeat, digg and Scale Model. Consistently the betaworks data science team uses Scikit-learn for a variety of tasks. From exploratory
analysis, to product development, it is an essential part of our toolkit. Recent uses are included in digg’s new video recommender system, and Poncho’s dynamic heuristic subspace clustering.

Gilad Lotan, Chief Data Scientist

1.6.4 Evernote

Building a classifier is typically an iterative process of exploring the data, selecting the features (the attributes of the data believed to be predictive in some way), training the models, and finally evaluating them. For many of these tasks, we relied on the excellent scikit-learn package for Python.

Read more

Mark Ayzenshtat, VP, Augmented Intelligence

1.6.5 Télécom ParisTech

At Telecom ParisTech, scikit-learn is used for hands-on sessions and home assignments in introductory and advanced machine learning courses. The classes are for undergrads and masters students. The great benefit of scikit-learn is its fast learning curve that allows students to quickly start working on interesting and motivating problems.

Alexandre Gramfort, Assistant Professor

1.6.6 Booking.com

At Booking.com, we use machine learning algorithms for many different applications, such as recommending hotels and destinations to our customers, detecting fraudulent reservations, or scheduling our customer service agents. Scikit-learn is one of the tools we use when implementing standard algorithms for prediction tasks. Its API and documentations are excellent and make it easy to use. The scikit-learn developers do a great job of incorporating state of the art implementations and new algorithms into the package. Thus, scikit-learn provides convenient access to a wide spectrum of algorithms, and allows us to readily find the right tool for the right job.

Melanie Mueller, Data Scientist

1.6. Who is using scikit-learn?
1.6.7 AWeber

The scikit-learn toolkit is indispensable for the Data Analysis and Management team at AWeber. It allows us to do AWesome stuff we would not otherwise have the time or resources to accomplish. The documentation is excellent, allowing new engineers to quickly evaluate and apply many different algorithms to our data. The text feature extraction utilities are useful when working with the large volume of email content we have at AWeber. The RandomizedPCA implementation, along with Pipelining and FeatureUnions, allows us to develop complex machine learning algorithms efficiently and reliably.

Anyone interested in learning more about how AWeber deploys scikit-learn in a production environment should check out talks from PyData Boston by AWeber’s Michael Becker available at https://github.com/mdbecker/pydata_2013

Michael Becker, Software Engineer, Data Analysis and Management Ninjas

1.6.8 Yhat

The combination of consistent APIs, thorough documentation, and top notch implementation make scikit-learn our favorite machine learning package in Python. scikit-learn makes doing advanced analysis in Python accessible to anyone. At Yhat, we make it easy to integrate these models into your production applications. Thus eliminating the unnecessary dev time encountered productionizing analytical work.

Greg Lamp, Co-founder Yhat

1.6.9 Rangespan

The Python scikit-learn toolkit is a core tool in the data science group at Rangespan. Its large collection of well documented models and algorithms allow our team of data scientists to prototype fast and quickly iterate to find the right solution to our learning problems. We find that scikit-learn is not only the right tool for prototyping, but its careful and well tested implementation give us the confidence to run scikit-learn models in production.

Jurgen Van Gael, Data Science Director at Rangespan Ltd
1.6.10 Birchbox

At Birchbox, we face a range of machine learning problems typical to E-commerce: product recommendation, user clustering, inventory prediction, trends detection, etc. Scikit-learn lets us experiment with many models, especially in the exploration phase of a new project: the data can be passed around in a consistent way; models are easy to save and reuse; updates keep us informed of new developments from the pattern discovery research community. Scikit-learn is an important tool for our team, built the right way in the right language.

Thierry Bertin-Mahieux, Birchbox, Data Scientist

1.6.11 Bestofmedia Group

Scikit-learn is our #1 toolkit for all things machine learning at Bestofmedia. We use it for a variety of tasks (e.g. spam fighting, ad click prediction, various ranking models) thanks to the varied, state-of-the-art algorithm implementations packaged into it. In the lab it accelerates prototyping of complex pipelines. In production I can say it has proven to be robust and efficient enough to be deployed for business critical components.

Eustache Diemert, Lead Scientist Bestofmedia Group

1.6.12 Change.org
At change.org we automate the use of scikit-learn’s RandomForestClassifier in our production systems to drive email targeting that reaches millions of users across the world each week. In the lab, scikit-learn’s ease-of-use, performance, and overall variety of algorithms implemented has proved invaluable in giving us a single reliable source to turn to for our machine-learning needs.

Vijay Ramesh, Software Engineer in Data/science at Change.org

1.6.13 PHIMECA Engineering

At PHIMECA Engineering, we use scikit-learn estimators as surrogates for expensive-to-evaluate numerical models (mostly but not exclusively finite-element mechanical models) for speeding up the intensive post-processing operations involved in our simulation-based decision making framework. Scikit-learn’s fit/predict API together with its efficient cross-validation tools considerably eases the task of selecting the best-fit estimator. We are also using scikit-learn for illustrating concepts in our training sessions. Trainees are always impressed by the ease-of-use of scikit-learn despite the apparent theoretical complexity of machine learning.

Vincent Dubourg, PHIMECA Engineering, PhD Engineer

1.6.14 HowAboutWe

At HowAboutWe, scikit-learn lets us implement a wide array of machine learning techniques in analysis and in production, despite having a small team. We use scikit-learn’s classification algorithms to predict user behavior, enabling us to (for example) estimate the value of leads from a given traffic source early in the lead’s tenure on our site. Also, our users’ profiles consist of primarily unstructured data (answers to open-ended questions), so we use scikit-learn’s feature extraction and dimensionality reduction tools to translate these unstructured data into inputs for our matchmaking system.

Daniel Weitzenfeld, Senior Data Scientist at HowAboutWe

1.6.15 PeerIndex

At PeerIndex we use scientific methodology to build the Influence Graph - a unique dataset that allows us to identify who’s really influential and in which context. To do this, we have to tackle a range of machine learning and predictive modeling problems. Scikit-learn has emerged as our primary tool for developing prototypes and making quick progress. From predicting missing data and classifying tweets to clustering communities of social media users, scikit-
learn proved useful in a variety of applications. Its very intuitive interface and excellent compatibility with other python tools makes it an indispensable tool in our daily research efforts.

Ferenc Huszar - Senior Data Scientist at Peerindex

### 1.6.16 DataRobot

DataRobot is building next generation predictive analytics software to make data scientists more productive, and scikit-learn is an integral part of our system. The variety of machine learning techniques in combination with the solid implementations that scikit-learn offers makes it a one-stop-shopping library for machine learning in Python. Moreover, its consistent API, well-tested code and permissive licensing allow us to use it in a production environment. Scikit-learn has literally saved us years of work we would have had to do ourselves to bring our product to market.

Jeremy Achin, CEO & Co-founder DataRobot Inc.

### 1.6.17 OkCupid

We’re using scikit-learn at OkCupid to evaluate and improve our matchmaking system. The range of features it has, especially preprocessing utilities, means we can use it for a wide variety of projects, and it’s performant enough to handle the volume of data that we need to sort through. The documentation is really thorough, as well, which makes the library quite easy to use.

David Koh - Senior Data Scientist at OkCupid

### 1.6.18 Lovely

At Lovely, we strive to deliver the best apartment marketplace, with respect to our users and our listings. From understanding user behavior, improving data quality, and detecting fraud, scikit-learn is a regular tool for gathering insights, predictive modeling and improving our product. The easy-to-read documentation and intuitive architecture of the API makes machine learning both explorable and accessible to a wide range of python developers. I’m constantly recommending that more developers and scientists try scikit-learn.

Simon Frid - Data Scientist, Lead at Lovely
1.6.19 Data Publica

Data Publica builds a new predictive sales tool for commercial and marketing teams called C-Radar. We extensively use scikit-learn to build segmentations of customers through clustering, and to predict future customers based on past partnerships success or failure. We also categorize companies using their website communication thanks to scikit-learn and its machine learning algorithm implementations. Eventually, machine learning makes it possible to detect weak signals that traditional tools cannot see. All these complex tasks are performed in an easy and straightforward way thanks to the great quality of the scikit-learn framework.

Guillaume Lebourgeois & Samuel Charron - Data Scientists at Data Publica

1.6.20 Machinalis

Scikit-learn is the cornerstone of all the machine learning projects carried at Machinalis. It has a consistent API, a wide selection of algorithms and lots of auxiliary tools to deal with the boilerplate. We have used it in production environments on a variety of projects including click-through rate prediction, information extraction, and even counting sheep!

In fact, we use it so much that we’ve started to freeze our common use cases into Python packages, some of them open-sourced, like FeatureForge. Scikit-learn in one word: Awesome.

Rafael Carrascosa, Lead developer

1.6.21 solido

Scikit-learn is helping to drive Moore’s Law, via Solido. Solido creates computer-aided design tools used by the majority of top-20 semiconductor companies and fabs, to design the bleeding-edge chips inside smartphones, automobiles, and more. Scikit-learn helps to power Solido’s algorithms for rare-event estimation, worst-case verification, optimization, and more. At Solido, we are particularly fond of scikit-learn’s libraries for Gaussian Process models, large-scale regularized linear regression, and classification. Scikit-learn has increased our productivity, because for many ML problems we no longer need to “roll our own” code. This PyData 2014 talk has details.

Trent McConaghy, founder, Solido Design Automation Inc.
1.6.22 INFONEA

INFONEA

We employ scikit-learn for rapid prototyping and custom-made Data Science solutions within our in-memory based Business Intelligence Software INFONEA®. As a well-documented and comprehensive collection of state-of-the-art algorithms and pipelining methods, scikit-learn enables us to provide flexible and scalable scientific analysis solutions. Thus, scikit-learn is immensely valuable in realizing a powerful integration of Data Science technology within self-service business analytics.

Thorsten Kranz, Data Scientist, Coma Soft AG.

1.6.23 Dataiku

Our software, Data Science Studio (DSS), enables users to create data services that combine ETL with Machine Learning. Our Machine Learning module integrates many scikit-learn algorithms. The scikit-learn library is a perfect integration with DSS because it offers algorithms for virtually all business cases. Our goal is to offer a transparent and flexible tool that makes it easier to optimize time consuming aspects of building a data service, preparing data, and training machine learning algorithms on all types of data.

Florian Douetteau, CEO, Dataiku

1.6.24 Otto Group

Here at Otto Group, one of global Big Five B2C online retailers, we are using scikit-learn in all aspects of our daily work from data exploration to development of machine learning application to the productive deployment of those services. It helps us to tackle machine learning problems ranging from e-commerce to logistics. It consistent APIs enabled us to build the Palladium REST-API framework around it and continuously deliver scikit-learn based services.

Christian Rammig, Head of Data Science, Otto Group

1.6.25 Zopa

At Zopa, the first ever Peer-to-Peer lending platform, we extensively use scikit-learn to run the business and optimize our users’ experience. It powers our Machine Learning models involved in credit risk, fraud risk, marketing, and pricing, and has been used for originating at least 1 billion GBP worth of Zopa loans. It is very well documented, powerful, and simple to use. We are grateful for the capabilities it has provided, and for allowing us to deliver on our mission of making money simple and fair.
1. Release History

1.1. Version 0.20 (under development)

1.1.1. Changed models

The following estimators and functions, when fit with the same data and parameters, may produce different models from the previous version. This often occurs due to changes in the modelling logic (bug fixes or enhancements), or in random sampling procedures.

- *decomposition.IncrementalPCA* in Python 2 (bug fix)
- *isotonic.IsotonicRegression* (bug fix)
- *metrics.roc_auc_score* (bug fix)
- *neural_network.BaseMultilayerPerceptron* (bug fix)
- *neural_network.MLPRegressor* (bug fix)
- *neural_network.MLPClassifier* (bug fix)

Details are listed in the changelog below.

(While we are trying to better inform users by providing this information, we cannot assure that this list is complete.)

2. Changelog

2.1. New features

Classifiers and regressors

- *ensemble.GradientBoostingClassifier* and *ensemble.GradientBoostingRegressor* now support early stopping via *n_iter_no_change*, *validation_fraction* and *tol*. #7071 by Raghav RV

- Added *naive_bayes.ComplementNB*, which implements the Complement Naive Bayes classifier described in Rennie et al. (2003). By Michael A. Alcorn.

Model evaluation

- Added the *metrics.balanced_accuracy* metric and a corresponding 'balanced_accuracy' scorer for binary classification. #8066 by @xyguo and Aman Dalmia.

2.2. Enhancements

Classifiers and regressors

- In *gaussian_process.GaussianProcessRegressor*, method *predict* is faster when using *return_std=True* in particular more when called several times in a row. #9234 by andrewww and Minghui Liu.

- Add *named_estimators_* parameter in *sklearn.ensemble.voting_classifier* to access fitted estimators. #9157 by Herilalaina Rakotorison.
• Add `var_smoothing` parameter in `sklearn.naive_bayes.GaussianNB` to give a precise control over variances calculation. #9681 by Dmitry Mottl.

• Add `n_iter_no_change` parameter in `neural_network.BaseMultilayerPerceptron`, `neural_network.MLPRegressor`, and `neural_network.MLPClassifier` to give control over maximum number of epochs to not meet tol improvement. #9456 by Nicholas Nadeau.

• A parameter `check_inverse` was added to `FunctionTransformer` to ensure that `func` and `inverse_func` are the inverse of each other. #9399 by Guillaume Lemaitre.

Model evaluation and meta-estimators

• A scorer based on `metrics.brier_score_loss` is also available. #9521 by Hanmin Qin.

Metrics

• `metrics.roc_auc_score` now supports binary `y_true` other than `{0, 1}` or `{−1, 1}`. #9828 by Hanmin Qin.

Linear, kernelized and related models

• Deprecate `random_state` parameter in `svm.OneClassSVM` as the underlying implementation is not random. #9497 by Albert Thomas.

Bug fixes

Classifiers and regressors

• Fixed a bug in `isotonic.IsotonicRegression` which incorrectly combined weights when fitting a model to data involving points with identical X values. #9432 by Dallas Card

• Fixed a bug in `neural_network.BaseMultilayerPerceptron`, `neural_network.MLPRegressor`, and `neural_network.MLPClassifier` with new `n_iter_no_change` parameter now at 10 from previously hardcoded 2. #9456 by Nicholas Nadeau.

• Fixed a bug in `neural_network.MLPRegressor` where fitting quit unexpectedly early due to local minima or fluctuations. #9456 by Nicholas Nadeau

• Fixed a bug in `naive_bayes.GaussianNB` which incorrectly raised error for prior list which summed to 1. #10005 by Gaurav Dhingra.

Decomposition, manifold learning and clustering

• Fix for uninformative error in `decomposition.IncrementalPCA`: now an error is raised if the number of components is larger than the chosen batch size. The `n_components=None` case was adapted accordingly. #6452. By Wally Gauze.

• Fixed a bug where the `partial_fit` method of `decomposition.IncrementalPCA` used integer division instead of float division on Python 2 versions. #9492 by James Bourbeau.

• Fixed a bug where the `fit` method of `cluster.affinityPropagation_.AffinityPropagation` stored cluster centers as 3d array instead of 2d array in case of non-convergence. For the same class, fixed undefined and arbitrary behavior in case of training data where all samples had equal similarity. #9612. By Jonatan Samoocha.

• In `decomposition.PCA` selecting a `n_components` parameter greater than the number of samples now raises an error. Similarly, the `n_components=None` case now selects the minimum of `n_samples` and `n_features`. #8484. By Wally Gauze.

• Fixed a bug in `datasets.fetch_kddcup99`, where data were not properly shuffled. #9731 by Nicolas Goix.
• Fixed a bug in \texttt{decomposition.PCA} where users will get unexpected error with large datasets when \texttt{n_components='mle'} on Python 3 versions. \#9886 by Hanmin Qin.

• Fixed a bug when setting parameters on meta-estimator, involving both a wrapped estimator and its parameter. \#9999 by Marcus Voss and Joel Nothman.

Metrics

• Fixed a bug due to floating point error in \texttt{metrics.roc_auc_score} with non-integer sample weights. \#9786 by Hanmin Qin.

API changes summary

Linear, kernelized and related models

• Deprecate random\_state parameter in \texttt{svm.OneClassSVM} as the underlying implementation is not random. \#9497 by Albert Thomas.

Metrics

• Deprecate reorder parameter in \texttt{metrics.auc} as it’s no longer required for \texttt{metrics.roc_auc_score}. Moreover using reorder=True can hide bugs due to floating point error in the input. \#9851 by Hanmin Qin.

Cluster

• Deprecate pooling\_func unused parameter in \texttt{cluster.AgglomerativeClustering}.\#9875 by Kumar Ashutosh.

1.7.2 Version 0.19.1

October 23, 2017

This is a bug-fix release with some minor documentation improvements and enhancements to features released in 0.19.0.

Note there may be minor differences in TSNE output in this release (due to \#9623), in the case where multiple samples have equal distance to some sample.

Changelog

API changes

• Reverted the addition of \texttt{metrics.ndcg\_score} and \texttt{metrics.dcg\_score} which had been merged into version 0.19.0 by error. The implementations were broken and undocumented.

• return\_train\_score which was added to \texttt{model\_selection.GridSearchCV}, \texttt{model\_selection.RandomizedSearchCV} and \texttt{model\_selection.cross\_validate} in version 0.19.0 will be changing its default value from True to False in version 0.21. We found that calculating training score could have a great effect on cross validation runtime in some cases. Users should explicitly set return\_train\_score to False if prediction or scoring functions are slow, resulting in a deleterious effect on CV runtime, or to True if they wish to use the calculated scores. \#9677 by Kumar Ashutosh and Joel Nothman.

• correlation\_models and regression\_models from the legacy gaussian processes implementation have been belatedly deprecated. \#9717 by Kumar Ashutosh.
Bug fixes

- Avoid integer overflows in `metrics.matthews_corrcoef`. #9693 by Sam Steingold.
- Fix ValueError in `preprocessing.LabelEncoder` when using `inverse_transform` on unseen labels. #9816 by Charlie Newey.
- Fixed a bug in the objective function for `manifold.TSNE` (both exact and with the Barnes-Hut approximation) when `n_components >= 3`. #9711 by @goncalo-rodrigues.
- Fix regression in `model_selection.cross_val_predict` where it raised an error with method='predict_proba' for some probabilistic classifiers. #9641 by James Bourbeau.
- Fixed a bug where `datasets.make_classification` modified its input weights. #9865 by Sachin Kelkar.
- `model_selection.StratifiedShuffleSplit` now works with multioutput multiclass or multilabel data with more than 1000 columns. #9922 by Charlie Brummitt.
- Fixed a bug with nested and conditional parameter setting, e.g. setting a pipeline step and its parameter at the same time. #9945 by Andreas Müller and Joel Nothman.

Regressions in 0.19.0 fixed in 0.19.1:

- Fixed a bug where parallelised prediction in random forests was not thread-safe and could (rarely) result in arbitrary errors. #9830 by Joel Nothman.
- Fix regression in `model_selection.cross_val_predict` where it no longer accepted `X` as a list. #9600 by Rasul Kerimov.
- Fixed handling of `cross_val_predict` for binary classification with method='decision_function'. #9593 by Reiichiro Nakano and core devs.
- Fix regression in `pipeline.Pipeline` where it no longer accepted `steps` as a tuple. #9604 by Joris Van den Bossche.
- Fix bug where `n_iter` was not properly deprecated, leaving `n_iter` unavailable for interim use in `linear_model.SGDClassifier`, `linear_model.SGDRegressor`, `linear_model.PassiveAggressiveClassifier`, `linear_model.PassiveAggressiveRegressor` and `linear_model.Perceptron`. #9558 by Andreas Müller.
- Dataset fetchers make sure temporary files are closed before removing them, which caused errors on Windows. #9847 by Joan Massich.
- Fixed a regression in `manifold.TSNE` where it no longer supported metrics other than ‘euclidean’ and ‘precomputed’. #9623 by Oli Blum.

Enhancements

- Our test suite and `utils.estimator_checks.check_estimators` can now be run without Nose installed. #9697 by Joan Massich.
- To improve usability of version 0.19’s `pipeline.Pipeline` caching, `memory` now allows `joblib`. Memory instances. This make use of the new `utils.validation.check_memory` helper. issue:9584 by Kumar Ashutosh
- Some fixes to examples: #9750, #9788, #9815
- Made a FutureWarning in SGD-based estimators less verbose. #9802 by Vrishank Bhardwaj.
1.7.3 Version 0.19

August 12, 2017

Highlights

We are excited to release a number of great new features including `neighbors.LocalOutlierFactor` for anomaly detection, `preprocessing.QuantileTransformer` for robust feature transformation, and the `multioutput.ClassifierChain` meta-estimator to simply account for dependencies between classes in multilabel problems. We have some new algorithms in existing estimators, such as multiplicative update in `decomposition.NMF` and multinomial `linear_model.LogisticRegression` with L1 loss (use `solver='saga'`).

Cross validation is now able to return the results from multiple metric evaluations. The new `model_selection.cross_validate` can return many scores on the test data as well as training set performance and timings, and we have extended the `scoring` and `refit` parameters for grid/randomized search to handle multiple metrics.

You can also learn faster. For instance, the new option to cache transformations in `pipeline.Pipeline` makes grid search over pipelines including slow transformations much more efficient. And you can predict faster: if you’re sure you know what you’re doing, you can turn off validating that the input is finite using `config_context`.

We’ve made some important fixes too. We’ve fixed a longstanding implementation error in `metrics.average_precision_score`, so please be cautious with prior results reported from that function. A number of errors in the `manifold.TSNE` implementation have been fixed, particularly in the default Barnes-Hut approximation. `semi_supervised.LabelSpreading` and `semi_supervised.LabelPropagation` have had substantial fixes. `LabelPropagation` was previously broken. `LabelSpreading` should now correctly respect its alpha parameter.

Changed models

The following estimators and functions, when fit with the same data and parameters, may produce different models from the previous version. This often occurs due to changes in the modelling logic (bug fixes or enhancements), or in random sampling procedures.

- `cluster.KMeans` with sparse X and initial centroids given (bug fix)
- `cross_decomposition.PLSRegression` with scale=True (bug fix)
- `ensemble.GradientBoostingClassifier` and `ensemble.GradientBoostingRegressor` where `min_impurity_split` is used (bug fix)
- gradient boosting loss='quantile' (bug fix)
- `ensemble.IsolationForest` (bug fix)
- `feature_selection.SelectFdr` (bug fix)
- `linear_model.RANSACRegressor` (bug fix)
• linear_model.LassoLars (bug fix)
• linear_model.LassoLarsIC (bug fix)
• manifold.TSNE (bug fix)
• neighbors.NearestCentroid (bug fix)
• semi_supervised.LabelSpreading (bug fix)
• semi_supervised.LabelPropagation (bug fix)
• tree based models where min_weight_fraction_leaf is used (enhancement) Details are listed in the changelog below.

(While we are trying to better inform users by providing this information, we cannot assure that this list is complete.)

Changelog

New features

Classifiers and regressors
• Added multioutput.ClassifierChain for multi-label classification. By Adam Kleczewski.
• Added solver 'saga' that implements the improved version of Stochastic Average Gradient, in linear_model.LogisticRegression and linear_model.Ridge. It allows the use of L1 penalty with multinomial logistic loss, and behaves marginally better than 'sag' during the first epochs of ridge and logistic regression. #8446 by Arthur Mensch.

Other estimators
• Added the neighbors.LocalOutlierFactor class for anomaly detection based on nearest neighbors. #5279 by Nicolas Goix and Alexandre Gramfort.
• Added preprocessing.QuantileTransformer class and preprocessing.quantile_transform function for features normalization based on quantiles. #8363 by Denis Engemann, Guillaume Lemaitre, Olivier Grisel, Raghav RV, Thierry Guillemot, and Gael Varoquaux.
• The new solver 'mu' implements a Multiplicate Update in decomposition.NMF, allowing the optimization of all beta-divergences, including the Frobenius norm, the generalized Kullback-Leibler divergence and the Itakura-Saito divergence. #5295 by Tom Dupre la Tour.

Model selection and evaluation
• model_selection.GridSearchCV and model_selection.RandomizedSearchCV now support simultaneous evaluation of multiple metrics. Refer to the Specifying multiple metrics for evaluation section of the user guide for more information. #7388 by Raghav RV
• Added the model_selection.cross_validate which allows evaluation of multiple metrics. This function returns a dict with more useful information from cross-validation such as the train scores, fit times and score times. Refer to The cross_validate function and multiple metric evaluation section of the userguide for more information. #7388 by Raghav RV
• Added metrics.mean_squared_log_error, which computes the mean square error of the logarithmic transformation of targets, particularly useful for targets with an exponential trend. #7655 by Karan Desai.
• Added metrics.dcg_score and metrics.ndcg_score, which compute Discounted cumulative gain (DCG) and Normalized discounted cumulative gain (NDCG). #7739 by David Gasquez.
• Added the model_selection.RepeatedKFold and model_selection.RepeatedStratifiedKFold. #8120 by Neeraj Gangwar.
Miscellaneous

- Validation that input data contains no NaN or inf can now be suppressed using `config_context`, at your own risk. This will save on runtime, and may be particularly useful for prediction time. #7548 by Joel Nothman.

- Added a test to ensure parameter listing in docstrings match the function/class signature. #9206 by Alexandre Gramfort and Raghav RV.

Enhancements

Trees and ensembles

- The `min_weight_fraction_leaf` constraint in tree construction is now more efficient, taking a fast path to declare a node a leaf if its weight is less than 2 * the minimum. Note that the constructed tree will be different from previous versions where `min_weight_fraction_leaf` is used. #7441 by Nelson Liu.

- `ensemble.GradientBoostingClassifier` and `ensemble.GradientBoostingRegressor` now support sparse input for prediction. #6101 by Ibraim Ganiev.

- `ensemble.VotingClassifier` now allows changing estimators by using `ensemble.VotingClassifier.set_params`. An estimator can also be removed by setting it to `None`. #7674 by Yichuan Liu.

- `tree.export_graphviz` now shows configurable number of decimal places. #8698 by Guillaume Lemaitre.

- Added `flatten_transform` parameter to `ensemble.VotingClassifier` to change output shape of `transform` method to 2 dimensional. #7794 by Ibraim Ganiev and Herilalaina Rakotoarison.

Linear, kernelized and related models

- `linear_model.SGDClassifier`, `linear_model.SGDRegressor`, `linear_model.PassiveAggressiveClassifier`, `linear_model.PassiveAggressiveRegressor` and `linear_model.Perceptron` now expose `max_iter` and `tol` parameters, to handle convergence more precisely. `n_iter` parameter is deprecated, and the fitted estimator exposes a `n_iter_` attribute, with actual number of iterations before convergence. #5036 by Tom Dupre la Tour.

- Added average parameter to perform weight averaging in `linear_model.PassiveAggressiveClassifier`. #4939 by Andrea Esuli.

- `linear_model.RANSACRegressor` no longer throws an error when calling `fit` if no inliers are found in its first iteration. Furthermore, causes of skipped iterations are tracked in newly added attributes, `n_skips_*`. #7914 by Michael Horrell.

- In `gaussian_process.GaussianProcessRegressor`, method `predict` is a lot faster with `return_std=True`. #8591 by Hadrien Bertrand.


- Memory usage enhancements: Prevent cast from float32 to float64 in: `linear_model.MultiTaskElasticNet`, `linear_model.LogisticRegression` when using newton-cg solver; and `linear_model.Ridge` when using svd, sparse_cg, cholesky or lsqr solvers. #8835, #8061 by Joan Massich and Nicolas Cordier and Thierry Guillemot.

Other predictors

- Custom metrics for the `neighbors` binary trees now have fewer constraints: they must take two 1d-arrays and return a float. #6288 by Jake Vanderplas.
- `algorithm='auto` in `neighbors` estimators now chooses the most appropriate algorithm for all input types and metrics. #9145 by Herilalaina Rakotoarison and Reddy Chinthala.

### Decomposition, manifold learning and clustering

- `cluster.MiniBatchKMeans` and `cluster.KMeans` now use significantly less memory when assigning data points to their nearest cluster center. #7721 by Jon Crall.
- `decomposition.PCA`, `decomposition.IncrementalPCA` and `decomposition.TruncatedSVD` now expose the singular values from the underlying SVD. They are stored in the attribute `singular_values_`, like in `decomposition.IncrementalPCA`. #7685 by Tommy Löfstedt
- `decomposition.NMF` now faster when `beta_loss=0`. #9277 by @hongkahjun.
- Memory improvements for method `barnes_hut` in `manifold.TSNE` #7089 by Thomas Moreau and Olivier Grisel.
- Optimization schedule improvements for Barnes-Hut `manifold.TSNE` so the results are closer to the one from the reference implementation lvdmaaten/bhtsne by Thomas Moreau and Olivier Grisel.
- Memory usage enhancements: Prevent cast from float32 to float64 in `decomposition.PCA` and `decomposition.randomized_svd_low_rank`. #9067 by Raghav RV.

### Preprocessing and feature selection

- Added `norm_order` parameter to `feature_selection.SelectFromModel` to enable selection of the norm order when `coef_` is more than 1D. #6181 by Antoine Wendlinger.
- Added ability to use sparse matrices in `feature_selection.f_regression` with `center=True`. #8065 by Daniel LeJeune.
- Small performance improvement to n-gram creation in `feature_extraction.text` by binding methods for loops and special-casing unigrams. #7567 by Jaye Doepke
- Relax assumption on the data for the `kernel_approximation.SkewedChi2Sampler`. Since the Skewed-Chi2 kernel is defined on the open interval $(-\text{skewedness}; +\infty)$, the transform function should not check whether $X < 0$ but whether $X < -\text{self.skewedness}$. #7573 by Romain Brault.
- Made default kernel parameters kernel-dependent in `kernel_approximation.Nystroem`. #5229 by Saurabh Bansod and Andreas Müller.

### Model evaluation and meta-estimators

- `pipeline.Pipeline` is now able to cache transformers within a pipeline by using the `memory` constructor parameter. #7990 by Guillaume Lemaitre.
- `pipeline.Pipeline` steps can now be accessed as attributes of its `named_steps` attribute. #8586 by Herilalaina Rakotoarison.
- Added `sample_weight` parameter to `pipeline.Pipeline.score`. #7723 by Mikhail Korobov.
- Added ability to set `n_jobs` parameter to `pipeline.make_union`. A `TypeError` will be raised for any other kwargs. #8028 by Alexander Booth.
- `model_selection.GridSearchCV`, `model_selection.RandomizedSearchCV` and `model_selection.cross_val_score` now allow estimators with callable kernels which were previously prohibited. #8005 by Andreas Müller.
- `model_selection.cross_val_predict` now returns output of the correct shape for all values of the argument `method`. #7863 by Aman Dalmia.
- Added `shuffle` and `random_state` parameters to shuffle training data before taking prefixes of it based on training sizes in `model_selection.learning_curve`. #7506 by Narine Kokhlikyan.
• `model_selection.StratifiedShuffleSplit` now works with multioutput multiclass (or multilabel) data. #9044 by Vlad Niculae.

• Speed improvements to `model_selection.StratifiedShuffleSplit`. #5991 by Arthur Mensch and Joel Nothman.

• Add `shuffle` parameter to `model_selection.train_test_split`. #8845 by themrmmax


• Add `max_train_size` parameter to `model_selection.TimeSeriesSplit` #8282 by Aman Dalmia.

• More clustering metrics are now available through `metrics.get_scorer` and `scoring` parameters. #8117 by Raghav RV.

• A scorer based on `metrics.explained_variance_score` is also available. #9259 by Hanmin Qin.

**Metrics**

• `metrics.matthews_corrcoef` now support multiclass classification. #8094 by Jon Crall.

• Add `sample_weight` parameter to `metrics.cohen_kappa_score`. #8335 by Victor Poughon.

**Miscellaneous**

• `utils.check_estimator` now attempts to ensure that methods transform, predict, etc. do not set attributes on the estimator. #7533 by Ekaterina Krivich.

• Added type checking to the `accept_sparse` parameter in `utils.validation` methods. This parameter now accepts only boolean, string, or list/tuple of strings. `accept_sparse=None` is deprecated and should be replaced by `accept_sparse=False`. #7880 by Josh Karnofsky.

• Make it possible to load a chunk of an svmlight formatted file by passing a range of bytes to `datasets.load_svmlight_file`. #935 by Olivier Grisel.

• `dummy.DummyClassifier` and `dummy.DummyRegressor` now accept non-finite features. #8931 by @Attractadore.

**Bug fixes**

**Trees and ensembles**

• Fixed a memory leak in trees when using trees with `criterion='mae'`. #8002 by Raghav RV.

• Fixed a bug where `ensemble.IsolationForest` uses an an incorrect formula for the average path length #8549 by Peter Wang.

• Fixed a bug where `ensemble.AdaBoostClassifier` throws a `ZeroDivisionError` while fitting data with single class labels. #7501 by Dominik Krzeminski.

• Fixed a bug in `ensemble.GradientBoostingClassifier` and `ensemble.GradientBoostingRegressor` where a float being compared to 0.0 using `==` caused a divide by zero error. #7970 by He Chen.

• Fix a bug where `ensemble.GradientBoostingClassifier` and `ensemble.GradientBoostingRegressor` ignored the `min_impurity_split` parameter. #8006 by Sebastian Pölsterl.

• Fixed `oob_score` in `ensemble.BaggingClassifier`. #8936 by Michael Lewis

• Fixed excessive memory usage in prediction for random forests estimators. #8672 by Mike Benfield.

• Fixed a bug where `sample_weight` as a list broke random forests in Python 2 #8068 by @xor.
• Fixed a bug where `ensemble.IsolationForest` fails when `max_features` is less than 1. #5732 by Ishank Gulati.

• Fix a bug where gradient boosting with `loss='quantile'` computed negative errors for negative values of `ytrue - ypred` leading to wrong values when calling `__call__`. #8087 by Alexis Mignon.

• Fix a bug where `ensemble.VotingClassifier` raises an error when a numpy array is passed in for weights. #7983 by Vincent Pham.

• Fixed a bug where `tree.export_graphviz` raised an error when the length of features_names does not match n_features in the decision tree. #8512 by Li Li.

Linear, kernelized and related models

• Fixed a bug where `linear_model.RANSACRegressor.fit` may run until `max_iter` if it finds a large inlier group early. #8251 by @aivision2020.

• Fixed a bug where `naive_bayes.MultinomialNB` and `naive_bayes.BernoulliNB` failed when `alpha=0`. #5814 by Yichuan Liu and Herilalaina Rakotarison.

• Fixed a bug where `linear_model.LassoLars` does not give the same result as the LassoLars implementation available in R (lars library). #7849 by Jair Montoya Martinez.

• Fixed a bug in `linear_model.RandomizedLasso`, `linear_model.Lars`, `linear_model.LassoLars`, `linear_model.LarsCV` and `linear_model.LassoLarsCV`, where the parameter `precompute` was not used consistently across classes, and some values proposed in the docstring could raise errors. #5359 by Tom Dupre la Tour.

• Fix inconsistent results between `linear_model.RidgeCV` and `linear_model.Ridge` when using `normalize=True`. #9302 by Alexandre Gramfort.

• Fix a bug where `linear_model.LassoLars.fit` sometimes left `coef_` as a list, rather than an ndarray. #8160 by CJ Carey.

• Fix `linear_model.BayesianRidge.fit` to return ridge parameter `alpha_` and `lambda_` consistent with calculated coefficients `coef_` and `intercept_`. #8224 by Peter Gedeck.

• Fixed a bug in `svm.OneClassSVM` where it returned floats instead of integer classes. #8676 by Vathsala Achar.

• Fix AIC/BIC criterion computation in `linear_model.LassoLarsIC`. #9022 by Alexandre Gramfort and Mehmet Basbug.

• Fixed a memory leak in our LibLinear implementation. #9024 by Sergei Lebedev.

• Fix bug where stratified CV splitters did not work with `linear_model.LassoCV`. #8973 by Paulo Haddad.

• Fixed a bug in `gaussian_process.GaussianProcessRegressor` when the standard deviation and covariance predicted without fit would fail with a meaningless error by default. #6573 by Quazi Marufur Rahman and Manoj Kumar.

Other predictors

• Fix semi_supervised.BaseLabelPropagation to correctly implement LabelPropagation and LabelSpreading as done in the referenced papers. #9239 by Andre Ambrosio Boechat, Utkarsh Upadhyay, and Joel Nothman.

Decomposition, manifold learning and clustering

• Fixed the implementation of `manifold.TSNE`:

  • `early_exageration` parameter had no effect and is now used for the first 250 optimization iterations.

  • Fixed the `AssertionError`: Tree consistency failed exception reported in #8992.
• Improve the learning schedule to match the one from the reference implementation lvdmaaten/bhtsne. by Thomas Moreau and Olivier Grisel.

• Fix a bug in decomposition.LatentDirichletAllocation where the perplexity method was returning incorrect results because the transform method returns normalized document topic distributions as of version 0.18. #7954 by Gary Foreman.

• Fix output shape and bugs with n_jobs > 1 in decomposition.SparseCoder transform and decomposition.sparse_encode for one-dimensional data and one component. This also impacts the output shape of decomposition.DictionaryLearning. #8086 by Andreas Müller.

• Fixed the implementation of explained_variance_ in decomposition.PCA, decomposition.RandomizedPCA and decomposition.IncrementalPCA. #9105 by Hanmin Qin.

• Fixed the implementation of noise_variance_ in decomposition.PCA. #9108 by Hanmin Qin.

• Fixed a bug where cluster.DBSCAN gives incorrect result when input is a precomputed sparse matrix with initial rows all zero. #8306 by Akshay Gupta

• Fix a bug regarding fitting cluster.KMeans with a sparse array X and initial centroids, where X’s means were unnecessarily being subtracted from the centroids. #7872 by Josh Karnofsky.

• Fixes to the input validation in covariance.EllipticEnvelope. #8086 by Andreas Müller.

• Fixed a bug in covariance.MinCovDet where inputting data that produced a singular covariance matrix would cause the helper method _c_step to throw an exception. #3367 by Jeremy Steward

• Fixed a bug in manifold.TSNE affecting convergence of the gradient descent. #8768 by David DeTomaso.

• Fixed a bug in manifold.TSNE where it stored the incorrect kl_divergence_. #6507 by Sebastian Saeger.

• Fixed improper scaling in cross_decomposition.PLSRegression with scale=True. #7819 by jayzed82.

• cluster.bicluster.SpectralCoclustering and cluster.bicluster.SpectralBiclustering fit method conforms with API by accepting y and returning the object. #6126, #7814 by Laurent Direr and Maniteja Nandana.

• Fix bug where mixture sample methods did not return as many samples as requested. #7702 by Levi John Wolf.

• Fixed the shrinkage implementation in neighbors.NearestCentroid. #9219 by Hanmin Qin.

Preprocessing and feature selection

• For sparse matrices, preprocessing.normalize with return_norm=True will now raise a NotImplementedError with ‘l1’ or ‘l2’ norm and with norm ’max’ the norms returned will be the same as for dense matrices. #7771 by Ang Lu.

• Fix a bug where feature_selection.SelectFdr did not exactly implement Benjamini-Hochberg procedure. It formerly may have selected fewer features than it should. #7490 by Peng Meng.

• Fixed a bug where linear_model.RandomizedLasso and linear_model.RandomizedLogisticRegression breaks for sparse input. #8259 by Aman Dalmia.

• Fix a bug where feature_extraction.FeatureHasher mandatorily applied a sparse random projection to the hashed features, preventing the use of feature_extraction.text.HashingVectorizer in a pipeline with feature_extraction.text.TfidfTransformer. #7565 by Roman Yurchak.

• Fix a bug where feature_selection.mutual_info_regression did not correctly use n_neighbors. #8181 by Guillaume Lemaitre.


• Fixed a bug where `model_selection.validation_curve` reused the same estimator for each parameter value. #7365 by Aleksandr Sandrovskii.

• `model_selection.permutation_test_score` now works with Pandas types. #5697 by Stijn Tonk.

• Several fixes to input validation in `multiclass(OutputCodeClassifier` #8086 by Andreas Müller.

• `multiclass.OneVsOneClassifier.partial_fit` now ensures all classes are provided up-front. #6250 by Asish Panda.

• Fix `multioutput.MultiOutputClassifier.predict_proba` to return a list of 2d arrays, rather than a 3d array. In the case where different target columns had different numbers of classes, a `ValueError` would be raised on trying to stack matrices with different dimensions. #8093 by Peter Bull.

• Cross validation now works with Pandas datatypes that have a read-only index. #9507 by Loic Esteve.

Metrics

• `metrics.average_precision_score` no longer linearly interpolates between operating points, and instead weighs precisions by the change in recall since the last operating point, as per the Wikipedia entry. (#7356). By Nick Dingwall and Gael Varoquaux.

• Fix a bug in `metrics.classification._check_targets` which would return `'binary'` if `y_true` and `y_pred` were both `'binary'` but the union of `y_true` and `y_pred` was `'multiclass'`. #8377 by Loic Esteve.

• Fixed an integer overflow bug in `metrics.confusion_matrix` and hence `metrics.cohen_kappa_score`. #8354, #7929 by Joel Nothman and Jon Crall.

• Fixed passing of `gamma` parameter to the `chi2` kernel in `metrics.pairwise.pairwise_kernels` #5211 by Nick Rhinehart, Saurabh Bansod and Andreas Müller.

Miscellaneous

• Fixed a bug when `datasets.make_classification` fails when generating more than 30 features. #8159 by Herilalaina Rakotoarison.

• Fixed a bug where `datasets.make_moons` gives an incorrect result when `n_samples` is odd. #8198 by Josh Levy.

• Some `fetch_` functions in `datasets` were ignoring the `download_if_missing` keyword. #7944 by Ralf Gommers.

• Fix estimators to accept a `sample_weight` parameter of type `pandas.Series` in their `fit` function. #7825 by Kathleen Chen.

• Fix a bug in cases where `numpy.cumsum` may be numerically unstable, raising an exception if instability is identified. #7376 and #7331 by Joel Nothman and @yangarbiter.

• Fix a bug where `base.BaseEstimator.__getstate__` obstructed pickling customizations of child-classes, when used in a multiple inheritance context. #8316 by Holger Peters.

• Update Sphinx-Gallery from 0.1.4 to 0.1.7 for resolving links in documentation build with Sphinx>1.5 #8010, #7986 by Oscar Najera
• Add data_home parameter to sklearn.datasets.fetch_kddcup99. #9289 by Loic Esteve.
• Fix dataset loaders using Python 3 version of makedirs to also work in Python 2. #9284 by Sebastin Santy.
• Several minor issues were fixed with thanks to the alerts of [lgtm.com](http://lgtm.com). #9278 by Jean Helie, among others.

**API changes summary**

**Trees and ensembles**

• Gradient boosting base models are no longer estimators. By Andreas Müller.
• All tree based estimators now accept a min_impurity_decrease parameter in lieu of the min_impurity_split, which is now deprecated. The min_impurity_decrease helps stop splitting the nodes in which the weighted impurity decrease from splitting is no longer at least min_impurity_decrease. #8449 by Raghav RV.

**Linear, kernelized and related models**


**Other predictors**

• neighbors.LSHForest has been deprecated and will be removed in 0.21 due to poor performance. #9078 by Laurent Dierer.
• neighbors.NearestCentroid no longer purports to support metric='precomputed' which now raises an error. #8515 by Sergul Aydore.
• The alpha parameter of semi_supervised.LabelPropagation now has no effect and is deprecated to be removed in 0.21. #9239 by Andre Ambrosio Boechat, Utkarsh Upadhyay, and Joel Nothman.

**Decomposition, manifold learning and clustering**

• Deprecate the doc_topic_distr argument of the perplexity method in decomposition.LatentDirichletAllocation because the user no longer has access to the unnormalized document topic distribution needed for the perplexity calculation. #7954 by Gary Foreman.
• The n_topics parameter of decomposition.LatentDirichletAllocation has been renamed to n_components and will be removed in version 0.21. #8922 by @Attractadore.
• decomposition.SparsePCA.transform's ridge_alpha parameter is deprecated in preference for class parameter. #8137 by Naoya Kanai.
• cluster.DBSCAN now has a metric_params parameter. #8139 by Naoya Kanai.

**Preprocessing and feature selection**

• feature_selection.SelectFromModel now has a partial_fit method only if the underlying estimator does. By Andreas Müller.
• feature_selection.SelectFromModel now validates the threshold parameter and sets the threshold_ attribute during the call to fit, and no longer during the call to transform. By Andreas Müller.
• The non_negative parameter in feature_extraction.FeatureHasher has been deprecated, and replaced with a more principled alternative, alternate_sign. #7565 by Roman Yurchak.
• linear_model.RandomizedLogisticRegression, and linear_model.RandomizedLasso have been deprecated and will be removed in version 0.21. #8995 by Ramana.S.
Model evaluation and meta-estimators

- Deprecate the `fit_params` constructor input to the `model_selection.GridSearchCV` and `model_selection.RandomizedSearchCV` in favor of passing keyword parameters to the `fit` methods of those classes. Data-dependent parameters needed for model training should be passed as keyword arguments to `fit`, and conforming to this convention will allow the hyperparameter selection classes to be used with tools such as `model_selection.cross_val_predict`. #2879 by Stephen Hoover.

- In version 0.21, the default behavior of splitters that use the `test_size` and `train_size` parameter will change, such that specifying `train_size` alone will cause `test_size` to be the remainder. #7459 by Nelson Liu.

- `multiclass.OneVsRestClassifier` now has `partial_fit`, `decision_function` and `predict_proba` methods only when the underlying estimator does. #7812 by Andreas Müller and Mikhail Korobov.

- `multiclass.OneVsRestClassifier` now has a `partial_fit` method only if the underlying estimator does. By Andreas Müller.

- The `decision_function` output shape for binary classification in `multiclass.OneVsRestClassifier` and `multiclass.OneVsOneClassifier` is now `(n_samples,)` to conform to scikit-learn conventions. #9100 by Andreas Müller.

- The `multiclass.MultiOutputClassifier.predict_proba` function used to return a 3d array `(n_samples, n_classes, n_outputs)`. In the case where different target columns had different numbers of classes, a `ValueError` would be raised on trying to stack matrices with different dimensions. This function now returns a list of arrays where the length of the list is `n_outputs`, and each array is `(n_samples, n_classes)` for that particular output. #8093 by Peter Bull.

- Replace attribute `named_steps dict` to `utils.Bunch` in `pipeline.Pipeline` to enable tab completion in interactive environment. In the case conflict value on `named_steps` and `dict` attribute, `dict` behavior will be prioritized. #8481 by Herilalaina Rakotoarison.

Miscellaneous

- Deprecate the `y` parameter in `transform` and `inverse_transform`. The method should not accept `y` parameter, as it’s used at the prediction time. #8174 by Tahar Zanouda, Alexandre Gramfort and Raghav RV.

- SciPy >= 0.13.3 and NumPy >= 1.8.2 are now the minimum supported versions for scikit-learn. The following backported functions in `utils` have been removed or deprecated accordingly. #8854 and #8874 by Naoya Kanai

- The `store_covariances` and `covariances_` parameters of `discriminant_analysis.QuadraticDiscriminantAnalysis` has been renamed to `store_covariance` and `covariance_` to be consistent with the corresponding parameter names of the `discriminant_analysis.LinearDiscriminantAnalysis`. They will be removed in version 0.21. #7998 by Jiacheng

Removed in 0.19:
- `utils.fixes.argpartition`
- `utils.fixes.array_equal`
- `utils.fixes.astype`
- `utils.fixes.bincount`
- `utils.fixes.expit`
- `utils.fixes.frombuffer_empty`
- `utils.fixes.in1d`
- `utils.fixes.norm`
- utils.fixes.rankdata
- utils.fixes.safe_copy

Deprecated in 0.19, to be removed in 0.21:
- utils.arpack.eigs
- utils.arpack.eigsh
- utils.arpack.svds
- utils.extmath.fast_dot
- utils.extmath.logsumexp
- utils.extmath.norm
- utils.extmath.pinvh
- utils.graph.graph_laplacian
- utils.random.choice
- utils.sparsetools.connected_components
- utils.stats.rankdata

- Estimators with both methods decision_function and predict_proba are now required to have a
  monotonic relation between them. The method check_decision_proba_consistency has been added
  in utils.estimator_checks to check their consistency. #7578 by Shubham Bhardwaj

- All checks in utils.estimator_checks, in particular utils.estimator_checks.
  check_estimator now accept estimator instances. Most other checks do not accept estimator classes any
  more. #9019 by Andreas Müller.

- Ensure that estimators’ attributes ending with _ are not set in the constructor but only in the fit method.
  Most notably, ensemble estimators (deriving from ensemble.BaseEnsemble) now only have self.
  estimators_ available after fit. #7464 by Lars Buitinck and Loic Esteve.

Code and Documentation Contributors

Thanks to everyone who has contributed to the maintenance and improvement of the project since version 0.18, in-
cluding:

Joel Nothman, Loic Esteve, Andreas Mueller, Guillaume Lemaitre, Olivier Grisel, Hanmin Qin, Raghav RV, Alexandre
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1.8 Previous Releases

1.8.1 Version 0.18.2

June 20, 2017

Scikit-learn 0.18 is the last major release of scikit-learn to support Python 2.6. Later versions of scikit-learn will require Python 2.7 or above.

Changelog

- Fixes for compatibility with NumPy 1.13.0: #7946 #8355 by Loic Esteve.
- Minor compatibility changes in the examples #9010 #8040 #9149.

Code Contributors

Aman Dalmia, Loic Esteve, Nate Guerin, Sergei Lebedev
1.8.2 Version 0.18.1

November 11, 2016

Changelog

Enhancements

• Improved `sample_without_replacement` speed by utilizing numpy.random.permutation for most cases. As a result, samples may differ in this release for a fixed random state. Affected estimators:
  – `ensemble.BaggingClassifier`
  – `ensemble.BaggingRegressor`
  – `linear_model.RANSACRegressor`
  – `model_selection.RandomizedSearchCV`
  – `random_projection.SparseRandomProjection`

This also affects the `datasets.make_classification` method.

Bug fixes

• Fix issue where `min_grad_norm` and `n_iter_without_progress` parameters were not being utilised by `manifold.TSNE`. #6497 by Sebastian Säger

• Fix bug for svm’s decision values when `decision_function_shape` is `ovr` in `svm.SVC`. `svm.SVC`’s decision_function was incorrect from versions 0.17.0 through 0.18.0. #7724 by Bing Tian Dai

• Attribute `explained_variance_ratio` of `discriminant_analysis.LinearDiscriminantAnalysis` calculated with SVD and Eigen solver are now of the same length. #7632 by JPFrancoia

• Fixes issue in `Univariate feature selection` where score functions were not accepting multi-label targets. #7676 by Mohammed Affan

• Fixed setting parameters when calling `fit` multiple times on `feature_selection.SelectFromModel`. #7756 by Andreas Müller

• Fixes issue in `partial_fit` method of `multiclass.OneVsRestClassifier` when number of classes used in `partial_fit` was less than the total number of classes in the data. #7786 by Srivatsan Ramesh

• Fixes issue in `calibration.CalibratedClassifierCV` where the sum of probabilities of each class for a data was not 1, and `CalibratedClassifierCV` now handles the case where the training set has less number of classes than the total data. #7799 by Srivatsan Ramesh

• Fix a bug where `sklearn.feature_selection.SelectFdr` did not exactly implement Benjamini-Hochberg procedure. It formerly may have selected fewer features than it should. #7490 by Peng Meng.

• `sklearn.manifold.LocallyLinearEmbedding` now correctly handles integer inputs. #6282 by Jake Vanderplas.

• The `min_weight_fraction_leaf` parameter of tree-based classifiers and regressors now assumes uniform sample weights by default if the `sample_weight` argument is not passed to the `fit` function. Previously, the parameter was silently ignored. #7301 by Nelson Liu.

• Numerical issue with `linear_model.RidgeCV` on centered data when `n_features > n_samples`. #6178 by Bertrand Thirion
• Tree splitting criterion classes’ cloning/pickling is now memory safe #7680 by Ibraim Ganiev.
• Fixed a bug where decomposition.NMF sets its n_iters_ attribute in transform(). #7553 by Ekaterina Krivich.
• sklearn.linear_model.LogisticRegressionCV now correctly handles string labels. #5874 by Raghav RV.
• Fixed a bug where sklearn.model_selection.train_test_split raised an error when stratify is a list of string labels. #7593 by Raghav RV.
• Fixed a bug where sklearn.model_selection.GridSearchCV and sklearn.model_selection.RandomizedSearchCV were not pickleable because of a pickling bug in np.ma.MaskedArray. #7594 by Raghav RV.
• All cross-validation utilities in sklearn.model_selection now permit one time cross-validation splitters for the cv parameter. Also non-deterministic cross-validation splitters (where multiple calls to split produce dissimilar splits) can be used as cv parameter. The sklearn.model_selection.GridSearchCV will cross-validate each parameter setting on the split produced by the first split call to the cross-validation splitter. #7660 by Raghav RV.
• Fix bug where preprocessing.MultiLabelBinarizer.fit_transform returned an invalid CSR matrix. #7750 by CJ Carey.
• Fixed a bug where metrics.pairwise.cosine_distances could return a small negative distance. #7732 by Artsion.

API changes summary

Trees and forests

• The min_weight_fraction_leaf parameter of tree-based classifiers and regressors now assumes uniform sample weights by default if the sample_weight argument is not passed to the fit function. Previously, the parameter was silently ignored. #7301 by Nelson Liu.
• Tree splitting criterion classes’ cloning/pickling is now memory safe. #7680 by Ibraim Ganiev.

Linear, kernelized and related models

• Length of explained_variance_ratio of discriminant_analysis.LinearDiscriminantAnalysis changed for both Eigen and SVD solvers. The attribute has now a length of min(n_components, n_classes - 1). #7632 by JPFrancoia
• Numerical issue with linear_model.RidgeCV on centered data when n_features > n_samples. #6178 by Bertrand Thirion

1.8.3 Version 0.18

September 28, 2016

Last release with Python 2.6 support

Scikit-learn 0.18 will be the last version of scikit-learn to support Python 2.6. Later versions of scikit-learn will require Python 2.7 or above.

1.8. Previous Releases
Model Selection Enhancements and API Changes

• The model_selection module

The new module `sklearn.model_selection`, which groups together the functionalities of formerly `sklearn.cross_validation`, `sklearn.grid_search` and `sklearn.learning_curve`, introduces new possibilities such as nested cross-validation and better manipulation of parameter searches with Pandas.

Many things will stay the same but there are some key differences. Read below to know more about the changes.

• Data-independent CV splitters enabling nested cross-validation

The new cross-validation splitters, defined in the `sklearn.model_selection`, are no longer initialized with any data-dependent parameters such as `y`. Instead they expose a `split` method that takes in the data and yields a generator for the different splits.

This change makes it possible to use the cross-validation splitters to perform nested cross-validation, facilitated by `model_selection.GridSearchCV` and `model_selection.RandomizedSearchCV` utilities.

• The enhanced cv_results_ attribute

The new `cv_results_` attribute (of `model_selection.GridSearchCV` and `model_selection.RandomizedSearchCV`) introduced in lieu of the `grid_scores_` attribute is a dict of 1D arrays with elements in each array corresponding to the parameter settings (i.e. search candidates).

The `cv_results_` dict can be easily imported into pandas as a DataFrame for exploring the search results.

The `cv_results_` arrays include scores for each cross-validation split (with keys such as `'split0_test_score'`), as well as their mean (`'mean_test_score'`) and standard deviation (`'std_test_score'`).

The ranks for the search candidates (based on their mean cross-validation score) is available at `cv_results_['rank_test_score']`.

The parameter values for each parameter is stored separately as numpy masked object arrays. The value, for that search candidate, is masked if the corresponding parameter is not applicable. Additionally a list of all the parameter dicts are stored at `cv_results_['params']`.

• Parameters n_folds and n_iter renamed to n_splits

Some parameter names have changed: The `n_folds` parameter in new `model_selection.KFold`, `model_selection.GroupKFold` (see below for the name change), and `model_selection.StratifiedKFold` is now renamed to `n_splits`. The `n_iter` parameter in `model_selection.ShuffleSplit`, the new class `model_selection.GroupShuffleSplit` and `model_selection.StratifiedShuffleSplit` is now renamed to `n_splits`.

• Rename of splitter classes which accepts group labels along with data


Note the change from singular to plural form in `model_selection.LeavePGroupsOut`.

• Fit parameter labels renamed to groups

The `labels` parameter in the split method of the newly renamed splitters `model_selection.GroupKFold`, `model_selection.LeaveOneGroupOut`, `model_selection.LeavePGroupsOut`, `model_selection.GroupShuffleSplit` is renamed to `groups` following the new nomenclature of their class names.
• Parameter n_labels renamed to n_groups

The parameter n_labels in the newly renamed `model_selection.LeavePGroupsOut` is changed to n_groups.

• Training scores and Timing information

`cv_results_` also includes the training scores for each cross-validation split (with keys such as 'split0_train_score'), as well as their mean ('mean_train_score') and standard deviation ('std_train_score'). To avoid the cost of evaluating training score, set `return_train_score=False`.

Additionally the mean and standard deviation of the times taken to split, train and score the model across all the cross-validation splits is available at the key 'mean_time' and 'std_time' respectively.

Changelog

New features

Classifiers and Regressors

• The Gaussian Process module has been reimplemented and now offers classification and regression estimators through `gaussian_process.GaussianProcessClassifier` and `gaussian_process.GaussianProcessRegressor`. Among other things, the new implementation supports kernel engineering, gradient-based hyperparameter optimization or sampling of functions from GP prior and GP posterior. Extensive documentation and examples are provided. By Jan Hendrik Metzen.

• Added new supervised learning algorithm: `Multi-layer Perceptron` #3204 by Issam H. Laradji

• Added `linear_model.HuberRegressor`, a linear model robust to outliers. #5291 by Manoj Kumar.

• Added the `multioutput.MultiOutputRegressor` meta-estimator. It converts single output regressors to multi-output regressors by fitting one regressor per output. By Tim Head.

Other estimators

• New `mixture.GaussianMixture` and `mixture.BayesianGaussianMixture` replace former mixture models, employing faster inference for sounder results. #7295 by Wei Xue and Thierry Guillemot.

• Class `decomposition.RandomizedPCA` is now factored into `decomposition.PCA` and it is available calling with parameter `svd_solver='randomized'`. The default number of n_iter for 'randomized' has changed to 4. The old behavior of PCA is recovered by `svd_solver='full'`. An additional solver calls arpack and performs truncated (non-randomized) SVD. By default, the best solver is selected depending on the size of the input and the number of components requested. #5299 by Giorgio Patrini.

• Added two functions for mutual information estimation: `feature_selection.mutual_info_classif` and `feature_selection.mutual_info_regression`. These functions can be used in `feature_selection.SelectKBest` and `feature_selection.SelectPercentile` as score functions. By Andrea Bravi and Nikolay Mayorov.

• Added the `ensemble.IsolationForest` class for anomaly detection based on random forests. By Nicolas Goix.

• Added `algorithm="elkan"` to `cluster.KMeans` implementing Elkan’s fast K-Means algorithm. By Andreas Müller.

Model selection and evaluation

• Added `metrics.cluster.fowlkes_mallows_score`, the Fowlkes Mallows Index which measures the similarity of two clusterings of a set of points By Arnaud Fouchet and Thierry Guillemot.

1.8. Previous Releases
• Added `metrics.calinski_harabaz_score`, which computes the Calinski and Harabaz score to evaluate the resulting clustering of a set of points. By Arnaud Fouchet and Thierry Guillemot.

• Added new cross-validation splitter `model_selection.TimeSeriesSplit` to handle time series data. #6586 by YenChen Lin

• The cross-validation iterators are replaced by cross-validation splitters available from `sklearn.model_selection`, allowing for nested cross-validation. See Model Selection Enhancements and API Changes for more information. #4294 by Raghav RV.

Enhancements

Trees and ensembles

• Added a new splitting criterion for `tree.DecisionTreeRegressor`, the mean absolute error. This criterion can also be used in `ensemble.ExtraTreesRegressor`, `ensemble.RandomForestRegressor`, and the gradient boosting estimators. #6667 by Nelson Liu.

• Added weighted impurity-based early stopping criterion for decision tree growth. #6954 by Nelson Liu

• The random forest, extra tree and decision tree estimators now has a method `decision_path` which returns the decision path of samples in the tree. By Arnaud Joly.

• A new example has been added unveiling the decision tree structure. By Arnaud Joly.

• Random forest, extra trees, decision trees and gradient boosting estimator accept the parameter `min_samples_split` and `min_samples_leaf` provided as a percentage of the training samples. By yelite and Arnaud Joly.

• Gradient boosting estimators accept the parameter `criterion` to specify to splitting criterion used in built decision trees. #6667 by Nelson Liu.

• The memory footprint is reduced (sometimes greatly) for `ensemble.bagging.BaseBagging` and classes that inherit from it, i.e, `ensemble.BaggingClassifier`, `ensemble.BaggingRegressor`, and `ensemble.IsolationForest`, by dynamically generating attribute `estimators_samples_` only when it is needed. By David Staub.

• Added `n_jobs` and `sample_weight` parameters for `ensemble.VotingClassifier` to fit underlying estimators in parallel. #5805 by Ibraim Ganiev.

Linear, kernelized and related models

• In `linear_model.LogisticRegression`, the SAG solver is now available in the multinomial case. #5251 by Tom Dupre la Tour.

• `linear_model.RANSACRegressor`, `svm.LinearSVC` and `svm.LinearSVR` now support `sample_weight`. By Imaculate.

• Add parameter `loss` to `linear_model.RANSACRegressor` to measure the error on the samples for every trial. By Manoj Kumar.

• Prediction of out-of-sample events with Isotonic Regression (`isotonic.IsotonicRegression`) is now much faster (over 1000x in tests with synthetic data). By Jonathan Arfa.

• Isotonic regression (`isotonic.IsotonicRegression`) now uses a better algorithm to avoid $O(n^2)$ behavior in pathological cases, and is also generally faster (#6691). By Antony Lee.

• `naive_bayes.GaussianNB` now accepts data-independent class-priors through the parameter `priors`. By Guillaume Lemaitre.
• `linear_model.ElasticNet` and `linear_model.Lasso` now works with np.float32 input data without converting it into np.float64. This allows to reduce the memory consumption. #6913 by YenChen Lin.

• `semi_supervised.LabelPropagation` and `semi_supervised.LabelSpreading` now accept arbitrary kernel functions in addition to strings knn and rbf. #5762 by Utkarsh Upadhyay.

Decomposition, manifold learning and clustering

• Added `inverse_transform` function to `decomposition.NMF` to compute data matrix of original shape. By Anish Shah.

• `cluster.KMeans` and `cluster.MiniBatchKMeans` now works with np.float32 and np.float64 input data without converting it. This allows to reduce the memory consumption by using np.float32. #6846 by Sebastian Säger and YenChen Lin.

Preprocessing and feature selection

• `preprocessing.RobustScaler` now accepts quantile_range parameter. #5929 by Konstantin Podshumok.

• `feature_extraction.FeatureHasher` now accepts string values. #6173 by Ryad Zenine and Devashish Deshpande.

• Keyword arguments can now be supplied to `func` in `preprocessing.FunctionTransformer` by means of the `kw_args` parameter. By Brian McFee.

• `feature_selection.SelectKBest` and `feature_selection.SelectPercentile` now accept score functions that take X, y as input and return only the scores. By Nikolay Mayorov.

Model evaluation and meta-estimators

• `multiclass.OneVsOneClassifier` and `multiclass.OneVsRestClassifier` now support partial_fit. By Asish Panda and Philipp Dowling.

• Added support for substituting or disabling `pipeline.Pipeline` and `pipeline.FeatureUnion` components using the `set_params` interface that powers sklearn.grid_search. See Selecting dimensionality reduction with Pipeline and GridSearchCV By Joel Nothman and Robert McGibbon.

• The new `cv_results_` attribute of `model_selection.GridSearchCV` (and `model_selection.RandomizedSearchCV`) can be easily imported into pandas as a DataFrame. Ref Model Selection Enhancements and API Changes for more information. #6697 by Raghav RV.

• Generalization of `model_selection.cross_val_predict`. One can pass method names such as `predict_proba` to be used in the cross validation framework instead of the default `predict`. By Ori Ziv and Sears Merritt.

• The training scores and time taken for training followed by scoring for each search candidate are now available at the `cv_results_` dict. See Model Selection Enhancements and API Changes for more information. #7325 by Eugene Chen and Raghav RV.

Metrics

• Added `labels` flag to `metrics.log_loss` to explicitly provide the labels when the number of classes in `y_true` and `y_pred` differ. #7239 by Hong Guangguo with help from Mads Jensen and Nelson Liu.

• Support sparse contingency matrices in cluster evaluation (metrics.cluster.supervised) to scale to a large number of clusters. #7419 by Gregory Stupp and Joel Nothman.

• Add `sample_weight` parameter to `metrics.matthews_corrcoef`. By Jatin Shah and Raghav RV.

• Speed up `metrics.silhouette_score` by using vectorized operations. By Manoj Kumar.

• Add `sample_weight` parameter to `metrics.confusion_matrix`. By Bernardo Stein.
Miscellaneous

- Added `n_jobs` parameter to `feature_selection.RFECV` to compute the score on the test folds in parallel. By Manoj Kumar.

- Codebase does not contain C/C++ cython generated files: they are generated during build. Distribution packages will still contain generated C/C++ files. By Arthur Mensch.

- Reduce the memory usage for 32-bit float input arrays of `utils.sparse_func.mean_variance_axis` and `utils.sparse_func.incr_mean_variance_axis` by supporting cython fused types. By YenChen Lin.

- The `ignore_warnings` now accept a category argument to ignore only the warnings of a specified type. By Thierry Guillemot.

- Added parameter `return_X_y` and return type `(data, target) : tuple` option to `load_iris dataset #7049, load_breast_cancer dataset #7152, load_digits dataset, load_diabetes dataset, load_linnerud dataset, load_boston dataset #7154 by Manvendra Singh.

- Simplification of the `clone` function, deprecate support for estimators that modify parameters in `__init__`. #5540 by Andreas Müller.

- When unpickling a scikit-learn estimator in a different version than the one the estimator was trained with, a `UserWarning` is raised, see the documentation on model persistence for more details. (#7248) By Andreas Müller.

Bug fixes

Trees and ensembles

- Random forest, extra trees, decision trees and gradient boosting won’t accept anymore `min_samples_split=1` as at least 2 samples are required to split a decision tree node. By Arnaud Joly.

- `ensemble.VotingClassifier` now raises `NotFittedError` if `predict`, `transform` or `predict_proba` are called on the non-fitted estimator. by Sebastian Raschka.

- Fix bug where `ensemble.AdaBoostClassifier` and `ensemble.AdaBoostRegressor` would perform poorly if the `random_state` was fixed (#7411). By Joel Nothman.


Linear, kernelized and related models


- Fix bug in `linear_model.LogisticRegressionCV` where `solver='liblinear'` did not accept `class_weights='balanced'. (#6817). By Tom Dupre la Tour.

- Fix bug in `neighbors.RadiusNeighborsClassifier` where an error occurred when there were outliers being labelled and a weight function specified (#6902). By LeonieBorne.

- Fix `linear_model.ElasticNet` sparse decision function to match output with dense in the multioutput case.

Decomposition, manifold learning and clustering
• `decomposition.RandomizedPCA` default number of `iterated_power` is 4 instead of 3. #5141 by Giorgio Patrini.

• `utils.extmath.randomized_svd` performs 4 power iterations by default, instead or 0. In practice this is enough for obtaining a good approximation of the true eigenvalues/vectors in the presence of noise. When `n_components` is small(< .1 * min(X.shape)) `n_iter` is set to 7, unless the user specifies a higher number. This improves precision with few components. #5299 by Giorgio Patrini.

• Whiten/non-whiten inconsistency between components of `decomposition.PCA` and `decomposition.RandomizedPCA` (now factored into PCA, see the New features) is fixed. `components_` are stored with no whitening. #5299 by Giorgio Patrini.

• Fixed bug in `manifold.spectral_embedding` where diagonal of unnormalized Laplacian matrix was incorrectly set to 1. #4995 by Peter Fischer.


• Attribute `explained_variance_ratio_` calculated with the SVD solver of `discriminant_analysis.LinearDiscriminantAnalysis` now returns correct results. By JPFrancoia

Preprocessing and feature selection

• `preprocessing.data._transform_selected` now always passes a copy of X to transform function when `copy=True` (#7194). By Caio Oliveira.

Model evaluation and meta-estimators

• `model_selection.StratifiedKFold` now raises error if all `n_labels` for individual classes is less than `n_folds`. #6182 by Devashish Deshpande.

• Fixed bug in `model_selection.StratifiedShuffleSplit` where train and test sample could overlap in some edge cases, see #6121 for more details. By Loic Esteve.

• Fix in `sklearn.model_selection.StratifiedShuffleSplit` to return splits of size `train_size` and `test_size` in all cases (#6472). By Andreas Müller.

• Cross-validation of `OneVsOneClassifier` and `OneVsRestClassifier` now works with precomputed kernels. #7350 by Russell Smith.

• Fix incomplete `predict_proba` method delegation from `model_selection.GridSearchCV` to `linear_model.SGDClassifier` (#7159) by Yichuan Liu.

Metrics

• Fix bug in `metrics.silhouette_score` in which clusters of size 1 were incorrectly scored. They should get a score of 0. By Joel Nothman.

• Fix bug in `metrics.silhouette_samples` so that it now works with arbitrary labels, not just those ranging from 0 to `n_clusters` - 1.

• Fix bug where expected and adjusted mutual information were incorrect if cluster contingency cells exceeded $2^{16}$. By Joel Nothman.

• `metrics.pairwise.pairwise_distances` now converts arrays to boolean arrays when required in `scipy.spatial.distance`. #5460 by Tom Dupre la Tour.

• Fix sparse input support in `metrics.silhouette_score` as well as example examples/text/document_clustering.py. By YenChen Lin.

• `metrics.roc_curve` and `metrics.precision_recall_curve` no longer round `y_score` values when creating ROC curves; this was causing problems for users with very small differences in scores (#7353).

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Miscellaneous

- `model_selection.tests._search._check_param_grid` now works correctly with all types that extends/implements `Sequence` (except string), including range (Python 3.x) and xrange (Python 2.x). #7323 by Viacheslav Kovalevskiy.
- `utils.extmath.randomized_range_finder` is more numerically stable when many power iterations are requested, since it applies LU normalization by default. If `n_iter<2` numerical issues are unlikely, thus no normalization is applied. Other normalization options are available: 'none', 'LU' and 'QR'. #5141 by Giorgio Patrini.
- Fix a bug where some formats of `scipy.sparse` matrix, and estimators with them as parameters, could not be passed to `base.clone`. By Loic Estève.
- `datasets.load_svmlight_file` now is able to read long int QID values. #7101 by Ibraim Ganiev.

API changes summary

Linear, kernelized and related models

- `residual_metric` has been deprecated in `linear_model.RANSACRegressor`. Use `loss` instead. By Manoj Kumar.
- Access to public attributes `.X_` and `.y_` has been deprecated in `isotonic.IsotonicRegression`. By Jonathan Arfa.

Decomposition, manifold learning and clustering

- The old `mixture.DPGMM` is deprecated in favor of the new `mixture.BayesianGaussianMixture` (with the parameter `weight_concentration_prior_type='dirichlet_process'`). The new class solves the computational problems of the old class and computes the Gaussian mixture with a Dirichlet process prior faster than before. #7295 by Wei Xue and Thierry Guilleminot.
- The old `mixture.VBGMM` is deprecated in favor of the new `mixture.BayesianGaussianMixture` (with the parameter `weight_concentration_prior_type='dirichlet_distribution'`). The new class solves the computational problems of the old class and computes the Variational Bayesian Gaussian mixture faster than before. #6651 by Wei Xue and Thierry Guilleminot.
- The old `mixture.GMM` is deprecated in favor of the new `mixture.GaussianMixture`. The new class computes the Gaussian mixture faster than before and some of computational problems have been solved. #6666 by Wei Xue and Thierry Guilleminot.

Model evaluation and meta-estimators

- The `sklearn.cross_validation`, `sklearn.grid_search` and `sklearn.learning_curve` have been deprecated and the classes and functions have been reorganized into the `sklearn.model_selection` module. Ref Model Selection Enhancements and API Changes for more information. #4294 by Raghav RV.
- The `grid_scores_` attribute of `model_selection.GridSearchCV` and `model_selection.RandomizedSearchCV` is deprecated in favor of the attribute `cv_results_`. Ref Model Selection Enhancements and API Changes for more information. #6697 by Raghav RV.
- The parameters `n_iter` or `n_folds` in old CV splitters are replaced by the new parameter `n_splits since it can provide a consistent and unambiguous interface to represent the number of train-test splits. #7187 by YenChen Lin.
- `classes` parameter was renamed to `labels` in `metrics.hamming_loss`. #7260 by Sebastián Vanrell.
• The splitter classes LabelKFold, LabelShuffleSplit, LeaveOneLabelOut and LeavePLabelsOut are renamed to `model_selection.GroupKFold`, `model_selection.GroupShuffleSplit`, `model_selection.LeaveOneGroupOut` and `model_selection.LeavePGroupsOut` respectively. Also the parameter `labels` in the split method of the newly renamed splitters `model_selection.LeaveOneGroupOut` and `model_selection.LeavePGroupsOut` is renamed to `groups`. Additionally in `model_selection.LeavePGroupsOut`, the parameter `n_labels` is renamed to `n_groups`. #6660 by Raghav RV.

• Error and loss names for `scoring` parameters are now prefixed by 'neg_', such as `neg_mean_squared_error`. The unprefixed versions are deprecated and will be removed in version 0.20. #7261 by Tim Head.

## Code Contributors

1.8.4 Version 0.17.1

February 18, 2016

Changelog

Bug fixes

- Upgrade vendored joblib to version 0.9.4 that fixes an important bug in joblib.Parallel that can silently yield to wrong results when working on datasets larger than 1MB: https://github.com/joblib/joblib/blob/0.9.4/CHANGES.rst
- Fixed reading of Bunch pickles generated with scikit-learn version <= 0.16. This can affect users who have already downloaded a dataset with scikit-learn 0.16 and are loading it with scikit-learn 0.17. See #6196 for how this affected datasets.fetch_20newsgroups. By Loic Esteve.
- Fixed a bug that prevented using ROC AUC score to perform grid search on several CPU / cores on large arrays. See #6147 By Olivier Grisel.
- Fixed a bug that prevented to properly set the presort parameter in ensemble.GradientBoostingRegressor. See #5857 By Andrew McCulloh.
- Fixed a joblib error when evaluating the perplexity of a decomposition.LatentDirichletAllocation model. See #6258 By Chyi-Kwei Yau.

1.8.5 Version 0.17

November 5, 2015

Changelog

New features

- All the Scaler classes but preprocessing.RobustScaler can be fitted online by calling partial_fit. By Giorgio Patrini.
- The new class ensemble.VotingClassifier implements a “majority rule” / “soft voting” ensemble classifier to combine estimators for classification. By Sebastian Raschka.
- The new class preprocessing.RobustScaler provides an alternative to preprocessing.StandardScaler for feature-wise centering and range normalization that is robust to outliers. By Thomas Unterthiner.
- The new class preprocessing.MaxAbsScaler provides an alternative to preprocessing.MinMaxScaler for feature-wise range normalization when the data is already centered or sparse. By Thomas Unterthiner.
- The new class preprocessing.FunctionTransformer turns a Python function into a Pipeline-compatible transformer object. By Joe Jevnik.
- The new classes cross_validation.LabelKFold and cross_validation.LabelShuffleSplit generate train-test folds, respectively similar to cross_validation.KFold and cross_validation.ShuffleSplit, except that the folds are conditioned on a label array. By Brian McFee, Jean Kossaifi and Gilles Louppe.
• **decomposition.LatentDirichletAllocation** implements the Latent Dirichlet Allocation topic model with online variational inference. By Chyi-Kwei Yau, with code based on an implementation by Matt Hoffman. (#3659)

• The new solver `sag` implements a Stochastic Average Gradient descent and is available in both `linear_model.LogisticRegression` and `linear_model.Ridge`. This solver is very efficient for large datasets. By Danny Sullivan and Tom Dupre la Tour. (#4738)

• The new solver `cd` implements a Coordinate Descent in `decomposition.NMF`. Previous solver based on Projected Gradient is still available setting new parameter `solver` to `pg`, but is deprecated and will be removed in 0.19, along with `decomposition.ProjectedGradientNMF` and parameters `sparseness`, `eta`, `beta` and `nls_max_iter`. New parameters `alpha` and `l1_ratio` control L1 and L2 regularization, and `shuffle` adds a shuffling step in the `cd` solver. By Tom Dupre la Tour and Mathieu Blondel.

**Enhancements**

• **manifold.TSNE** now supports approximate optimization via the Barnes-Hut method, leading to much faster fitting. By Christopher Erick Moody. (#4025)

• **cluster.mean_shift_.MeanShift** now supports parallel execution, as implemented in the `mean_shift` function. By Martino Sorbaro.

• **naive_bayes.GaussianNB** now supports fitting with `sample_weight`. By Jan Hendrik Metzen.

• **dummy.DummyClassifier** now supports a prior fitting strategy. By Arnaud Joly.

• Added a `fit_predict` method for `mixture.GMM` and subclasses. By Cory Lorenz.

• Added the `metrics.label_ranking_loss` metric. By Arnaud Joly.

• Added the `metrics.cohen_kappa_score` metric.

• Added a `warm_start` constructor parameter to the bagging ensemble models to increase the size of the ensemble. By Tim Head.

• Added option to use multi-output regression metrics without averaging. By Konstantin Shmelkov and Michael Eickenberg.

• Added a `stratify` option to `cross_validation.train_test_split` for stratified splitting. By Miroslav Batchkarov.

• The `tree.export_graphviz` function now supports aesthetic improvements for `tree.DecisionTreeClassifier` and `tree.DecisionTreeRegressor`, including options for coloring nodes by their majority class or impurity, showing variable names, and using node proportions instead of raw sample counts. By Trevor Stephens.

• Improved speed of `newton-cg` solver in `linear_model.LogisticRegression`, by avoiding loss computation. By Mathieu Blondel and Tom Dupre la Tour.

• The `class_weight="auto"` heuristic in classifiers supporting `class_weight` was deprecated and replaced by the `class_weight="balanced"` option, which has a simpler formula and interpretation. By Hanna Wallach and Andreas Müller.

• Add `class_weight` parameter to automatically weight samples by class frequency for `linear_model.PassiveAgressiveClassifier`. By Trevor Stephens.

• Added backlinks from the API reference pages to the user guide. By Andreas Müller.

• The `labels` parameter to `sklearn.metrics.f1_score`, `sklearn.metrics.fbeta_score`, `sklearn.metrics.recall_score` and `sklearn.metrics.precision_score` has been ex-
tended. It is now possible to ignore one or more labels, such as where a multiclass problem has a majority class to ignore. By Joel Nothman.

- Provide an option for sparse output from `sklearn.metrics.pairwise.cosine_similarity`. By Jaidev Deshpande.
- Add minmax_scale to provide a function interface for MinMaxScaler. By Thomas Unterthiner.
- `dump_svmlight_file` now handles multi-label datasets. By Chih-Wei Chang.
- RCV1 dataset loader (`sklearn.datasets.fetch_rcv1`). By Tom Dupre la Tour.
- The “Wisconsin Breast Cancer” classical two-class classification dataset is now included in scikit-learn, available with `sklearn.dataset.load_breast_cancer`.
- Upgraded to joblib 0.9.3 to benefit from the new automatic batching of short tasks. This makes it possible for scikit-learn to benefit from parallelism when many very short tasks are executed in parallel, for instance by the `grid_search.GridSearchCV` meta-estimator with `n_jobs > 1` used with a large grid of parameters on a small dataset. By Vlad Niculae, Olivier Grisel and Loïc Estève.
- For more details about changes in joblib 0.9.3 see the release notes: https://github.com/joblib/joblib/blob/master/CHANGES.rst#release-093
- Improved speed (3 times per iteration) of `decomposition.DictLearning` with coordinate descent method from `linear_model.Lasso`. By Arthur Mensch.
- Parallel processing (threaded) for queries of nearest neighbors (using the ball-tree) by Nikolay Mayorov.
- Allow `datasets.make_multilabel_classification` to output a sparse y. By Kashif Rasul.
- `cluster.DBSCAN` now accepts a sparse matrix of precomputed distances, allowing memory-efficient distance precomputation. By Joel Nothman.
- `tree.DecisionTreeClassifier` now exposes an apply method for retrieving the leaf indices samples are predicted as. By Daniel Galvez and Gilles Louppe.
- Speed up decision tree regressors, random forest regressors, extra trees regressors and gradient boosting estimators by computing a proxy of the impurity improvement during the tree growth. The proxy quantity is such that the split that maximizes this value also maximizes the impurity improvement. By Arnaud Joly, Jacob Schreiber and Gilles Louppe.
- Speed up tree based methods by reducing the number of computations needed when computing the impurity measure taking into account linear relationship of the computed statistics. The effect is particularly visible with extra trees and on datasets with categorical or sparse features. By Arnaud Joly.
- `ensemble.GradientBoostingRegressor` and `ensemble.GradientBoostingClassifier` now expose an apply method for retrieving the leaf indices each sample ends up in under each try. By Jacob Schreiber.
- Add sample_weight support to `linear_model.LinearRegression`. By Sonny Hu. (#4881)
- Add n_iter_without_progress to `manifold.TSNE` to control the stopping criterion. By Santi Villalba. (#5186)
- Added optional parameter random_state in `linear_model.Ridge`, to set the seed of the pseudo random generator used in sag solver. By Tom Dupre la Tour.
- Added optional parameter warm_start in `linear_model.LogisticRegression`. If set to True, the solvers lbfgs, newton-cg and sag will be initialized with the coefficients computed in the previous fit. By Tom Dupre la Tour.
• Added `sample_weight` support to `linear_model.LogisticRegression` for the lbfgs, newton-cg, and sag solvers. By Valentin Stolbunov. Support added to the liblinear solver. By Manoj Kumar.

• Added optional parameter `presort` to `ensemble.GradientBoostingRegressor` and `ensemble.GradientBoostingClassifier`, keeping default behavior the same. This allows gradient boosters to turn off presorting when building deep trees or using sparse data. By Jacob Schreiber.

• Altered `metrics.roc_curve` to drop unnecessary thresholds by default. By Graham Clenaghan.

• Added `feature_selection.SelectFromModel` meta-transformer which can be used along with estimators that have `coef_` or `feature_importances_` attribute to select important features of the input data. By Maheshakya Wijewardena, Joel Nothman and Manoj Kumar.

• Added `metrics.pairwise.laplacian_kernel`. By Clyde Fare.

• `covariance.GraphLasso` allows separate control of the convergence criterion for the Elastic-Net subproblem via the `enet_tol` parameter.

• Improved verbosity in `decomposition.DictionaryLearning`.

• `ensemble.RandomForestClassifier` and `ensemble.RandomForestRegressor` no longer explicitly store the samples used in bagging, resulting in a much reduced memory footprint for storing random forest models.

• Added `positive` option to `linear_model.Lars` and `linear_model.lars_path` to force coefficients to be positive. (#5131)

• Added the `X_norm_squared` parameter to `metrics.pairwise.euclidean_distances` to provide precomputed squared norms for `X`.

• Added the `fit_predict` method to `pipeline.Pipeline`.

• Added the `preprocessing.min_max_scale` function.

**Bug fixes**

• Fixed non-determinism in `dummy.DummyClassifier` with sparse multi-label output. By Andreas Müller.

• Fixed the output shape of `linear_model.RANSACRegressor` to `(n_samples, )`. By Andreas Müller.

• Fixed bug in `decomposition.DictLearning` when `n_jobs < 0`. By Andreas Müller.

• Fixed bug where `grid_search.RandomizedSearchCV` could consume a lot of memory for large discrete grids. By Joel Nothman.

• Fixed bug in `linear_model.LogisticRegressionCV` where `penalty` was ignored in the final fit. By Manoj Kumar.

• Fixed bug in `ensemble.forest.ForestClassifier` while computing oob_score and `X` is a sparse.csc_matrix. By Ankur Ankan.

• All regressors now consistently handle and warn when given `y` that is of shape `(n_samples, 1)`. By Andreas Müller and Henry Lin. (#5431)

• Fix in `cluster.KMeans` cluster reassignment for sparse input by Lars Buitinck.

• Fixed a bug in `lda.LDA` that could cause asymmetric covariance matrices when using shrinkage. By Martin Billinger.

• Fixed `cross_validation.cross_val_predict` for estimators with sparse predictions. By Buddha Prakash.

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• Fixed the `predict_proba` method of `linear_model.LogisticRegression` to use soft-max instead of one-vs-rest normalization. By Manoj Kumar. (#5182)

• Fixed the `partial_fit` method of `linear_model.SGDClassifier` when called with `average=True`. By Andrew Lamb. (#5282)

• Dataset fetchers use different filenames under Python 2 and Python 3 to avoid pickling compatibility issues. By Olivier Grisel. (#5355)

• Fixed a bug in `naive_bayes.GaussianNB` which caused classification results to depend on scale. By Jake Vanderplas.

• Fixed temporarily `linear_model.Ridge`, which was incorrect when fitting the intercept in the case of sparse data. The fix automatically changes the solver to 'sag' in this case. #5360 by Tom Dupre la Tour.

• Fixed a performance bug in `decomposition.RandomizedPCA` on data with a large number of features and fewer samples. (#4478) By Andreas Müller, Loic Esteve and Giorgio Patrini.

• Fixed bug in `cross_decomposition.PLS` that yielded unstable and platform dependent output, and failed on `fit_transform`. By Arthur Mensch.

• Fixes to the Bunch class used to store datasets.

• Fixed `ensemble.plot_partial_dependence` ignoring the percentiles parameter.

• Providing a set as vocabulary in `CountVectorizer` no longer leads to inconsistent results when pickling.

• Fixed the conditions on when a precomputed Gram matrix needs to be recomputed in `linear_model.LinearRegression`, `linear_model.OrthogonalMatchingPursuit`, `linear_model.Lasso` and `linear_model.ElasticNet`.

• Fixed inconsistent memory layout in the coordinate descent solver that affected `linear_model.DictionaryLearning` and `covariance.GraphLasso`. (#5337) By Olivier Grisel.

• `manifold.LocallyLinearEmbedding` no longer ignores the `reg` parameter.

• Nearest Neighbor estimators with custom distance metrics can now be pickled. (#4362)

• Fixed a bug in `pipeline.FeatureUnion` where `transformer_weights` were not properly handled when performing grid-searches.

• Fixed a bug in `linear_model.LogisticRegression` and `linear_model.LogisticRegressionCV` when using `class_weight='balanced'` or `'class_weight='auto'`. By Tom Dupre la Tour.

• Fixed bug #5495 when doing OVR(SVC(decision_function_shape="ovr")). Fixed by Elvis Dohmatob.

**API changes summary**

• Attribute `data_min`, `data_max` and `data_range` in `preprocessing.MinMaxScaler` are deprecated and won’t be available from 0.19. Instead, the class now exposes `data_min_`, `data_max_` and `data_range_`. By Giorgio Patrini.

• All Scaler classes now have an `scale_` attribute, the feature-wise rescaling applied by their `transform` methods. The old attribute `std_` in `preprocessing.StandardScaler` is deprecated and superseded by `scale_`; it won’t be available in 0.19. By Giorgio Patrini.

• `svm.SVC` and `svm.NuSVC` now have an `decision_function_shape` parameter to make their decision function of shape `(n_samples, n_classes)` by setting `decision_function_shape='ovr'`. This will be the default behavior starting in 0.19. By Andreas Müller.
• Passing 1D data arrays as input to estimators is now deprecated as it caused confusion in how the array elements should be interpreted as features or as samples. All data arrays are now expected to be explicitly shaped (n_samples, n_features). By Vighnesh Birodkar.

• `lda.LDA` and `qda.QDA` have been moved to `discriminant_analysis.LinearDiscriminantAnalysis` and `discriminant_analysis.QuadraticDiscriminantAnalysis`.

• The `store_covariance` and `tol` parameters have been moved from the `fit` method to the constructor in `discriminant_analysis.LinearDiscriminantAnalysis` and the `store_covariances` and `tol` parameters have been moved from the `fit` method to the constructor in `discriminant_analysis.QuadraticDiscriminantAnalysis`.

• Models inheriting from `_LearntSelectorMixin` will no longer support the `transform` methods. (i.e, RandomForests, GradientBoosting, LogisticRegression, DecisionTrees, SVMs and SGD related models). Wrap these models around the metatransformer `feature_selection.SelectFromModel` to remove features (according to `coefs_ or feature_importances_`) which are below a certain threshold value instead.

• `cluster.KMeans` re-runs cluster-assignments in case of non-convergence, to ensure consistency of `predict(X)` and `labels_`. By Vighnesh Birodkar.

• Classifier and Regressor models are now tagged as such using the `_estimator_type` attribute.

• Cross-validation iterators always provide indices into training and test set, not boolean masks.

• The `decision_function` on all regressors was deprecated and will be removed in 0.19. Use `predict` instead.

• `datasets.load_lfw_pairs` is deprecated and will be removed in 0.19. Use `datasets.fetch_lfw_pairs` instead.

• The deprecated `hmm` module was removed.

• The deprecated Bootstrap cross-validation iterator was removed.

• The deprecated Ward and WardAgglomerative classes have been removed. Use `clustering.AgglomerativeClustering` instead.

• `cross_validation.check_cv` is now a public function.

• The property `residues_` of `linear_model.LinearRegression` is deprecated and will be removed in 0.19.

• The deprecated `n_jobs` parameter of `linear_model.LinearRegression` has been moved to the constructor.

• Removed deprecated `class_weight` parameter from `linear_model.SGDClassifier`'s `fit` method. Use the construction parameter instead.

• The deprecated support for the sequence of sequences (or list of lists) multilabel format was removed. To convert to and from the supported binary indicator matrix format, use `MultiLabelBinarizer`.

• The behavior of calling the `inverse_transform` method of `Pipeline.pipeline` will change in 0.19. It will no longer reshape one-dimensional input to two-dimensional input.

• The deprecated attributes `indicator_matrix_`, `multilabel_` and `classes_` of `preprocessing.LabelBinarizer` were removed.

• Using `gamma=0` in `svm.SVC` and `svm.SVR` to automatically set the gamma to `1. / n_features` is deprecated and will be removed in 0.19. Use `gamma="auto"` instead.
1.8.6 Version 0.16.1

April 14, 2015

Changelog

Bug fixes

- Allow input data larger than block_size in covariance.LedoitWolf by Andreas Müller.
- Fix a bug in isotonic.IsotonicRegression deduplication that caused unstable result in calibration.CalibratedClassifierCV by Jan Hendrik Metzen.
- Fix several stability and convergence issues in cross_decomposition.CCA and cross_decomposition.PLSCanonical by Andreas Müller.
- Fix a bug in cluster.KMeans when precompute_distances=False on fortran-ordered data.
- Fix a speed regression in ensemble.RandomForestClassifier's predict and predict_proba by Andreas Müller.
- Fix a regression where utils.shuffle converted lists and dataframes to arrays, by Olivier Grisel

1.8.7 Version 0.16

March 26, 2015
Highlights

• Speed improvements (notably in `cluster.DBSCAN`), reduced memory requirements, bug-fixes and better default settings.

• Multinomial Logistic regression and a path algorithm in `linear_model.LogisticRegressionCV`.

• Out-of-core learning of PCA via `decomposition.IncrementalPCA`.

• Probability calibration of classifiers using `calibration.CalibratedClassifierCV`.

• `cluster.Birch` clustering method for large-scale datasets.

• Scalable approximate nearest neighbors search with Locality-sensitive hashing forests in `neighbors.LSHForest`.

• Improved error messages and better validation when using malformed input data.

• More robust integration with pandas dataframes.

Changelog

New features

• The new `neighbors.LSHForest` implements locality-sensitive hashing for approximate nearest neighbors search. By Maheshakya Wijewardena.

• Added `svm.LinearSVR`. This class uses the liblinear implementation of Support Vector Regression which is much faster for large sample sizes than `svm.SVR` with linear kernel. By Fabian Pedregosa and Qiang Luo.

• Incremental fit for `GaussianNB`.

• Added `sample_weight` support to `dummy.DummyClassifier` and `dummy.DummyRegressor`. By Arnaud Joly.

• Added the `metrics.label_ranking_average_precision_score` metrics. By Arnaud Joly.

• Add the `metrics.coverage_error` metrics. By Arnaud Joly.

• Added `linear_model.LogisticRegressionCV`. By Manoj Kumar, Fabian Pedregosa, Gael Varoquaux and Alexandre Gramfort.

• Added `warm_start` constructor parameter to make it possible for any trained forest model to grow additional trees incrementally. By Laurent Direr.

• Added `sample_weight` support to `ensemble.GradientBoostingClassifier` and `ensemble.GradientBoostingRegressor`. By Peter Prettenhofer.

• Added `decomposition.IncrementalPCA`, an implementation of the PCA algorithm that supports out-of-core learning with a `partial_fit` method. By Kyle Kastner.

• Averaged SGD for `SGDClassifier` and `SGDRegressor` By Danny Sullivan.

• Added `cross_val_predict` function which computes cross-validated estimates. By Luis Pedro Coelho

• Added `linear_model.TheilSenRegressor`, a robust generalized-median-based estimator. By Florian Wilhelm.

• Added `metrics.median_absolute_error`, a robust metric. By Gael Varoquaux and Florian Wilhelm.

• Add `cluster.Birch`, an online clustering algorithm. By Manoj Kumar, Alexandre Gramfort and Joel Nothman.
• Added shrinkage support to `discriminant_analysis.LinearDiscriminantAnalysis` using two new solvers. By Clemens Brunner and Martin Billinger.

• Added `kernel_ridge.KernelRidge`, an implementation of kernelized ridge regression. By Mathieu Blondel and Jan Hendrik Metzen.

• All solvers in `linear_model.Ridge` now support `sample_weight`. By Mathieu Blondel.

• Added `cross_validation.PredefinedSplit` cross-validation for fixed user-provided cross-validation folds. By Thomas Unterthiner.

• Added `calibration.CalibratedClassifierCV`, an approach for calibrating the predicted probabilities of a classifier. By Alexandre Gramfort, Jan Hendrik Metzen, Mathieu Blondel and Balazs Kegl.

Enhancements

• Add option `return_distance` in `hierarchical.ward_tree` to return distances between nodes for both structured and unstructured versions of the algorithm. By Matteo Visconti di Oleggio Castello. The same option was added in `hierarchical.linkage_tree`. By Manoj Kumar.

• Add support for sample weights in scorer objects. Metrics with sample weight support will automatically benefit from it. By Noel Dawe and Vlad Niculae.

• Added `newton-cg` and `lbfgs` solver support in `linear_model.LogisticRegression`. By Manoj Kumar.

• Add `selection="random"` parameter to implement stochastic coordinate descent for `linear_model.Lasso`, `linear_model.ElasticNet` and related. By Manoj Kumar.

• Add `sample_weight` parameter to `metrics.jaccard_similarity_score` and `metrics.log_loss`. By Jatin Shah.

• Support sparse multilabel indicator representation in `preprocessing.LabelBinarizer` and `multiclass.OneVsRestClassifier` (by Hamzeh Alsalhi with thanks to Rohit Sivaprasad), as well as evaluation metrics (by Joel Nothman).

• Add `sample_weight` parameter to `metrics.jaccard_similarity_score`. By Jatin Shah.

• Add support for multiclass in `metrics.hinge_loss`. Added `labels=None` as optional parameter. By Saurabh Jha.

• Add `sample_weight` parameter to `metrics.hinge_loss`. By Saurabh Jha.

• Add `multi_class="multinomial"` option in `linear_model.LogisticRegression` to implement a Logistic Regression solver that minimizes the cross-entropy or multinomial loss instead of the default One-vs-Rest setting. Supports `lbfgs` and `newton-cg` solvers. By Lars Buitinck and Manoj Kumar. Solver option `newton-cg` by Simon Wu.

• `DictVectorizer` can now perform `fit_transform` on an iterable in a single pass, when giving the option `sort=False`. By Dan Blanchard.

• `GridSearchCV` and `RandomizedSearchCV` can now be configured to work with estimators that may fail and raise errors on individual folds. This option is controlled by the `error_score` parameter. This does not affect errors raised on re-fit. By Michal Romanik.

• Add `digits` parameter to `metrics.classification_report` to allow report to show different precision of floating point numbers. By Ian Gilmore.

• Add a quantile prediction strategy to the `dummy.DummyRegressor`. By Aaron Staple.

• Add `handle_unknown` option to `preprocessing.OneHotEncoder` to handle unknown categorical features more gracefully during transform. By Manoj Kumar.
• Added support for sparse input data to decision trees and their ensembles. By Fares Hedyati and Arnaud Joly.

• Optimized `cluster.AffinityPropagation` by reducing the number of memory allocations of large temporary data-structures. By Antony Lee.

• Parallelization of the computation of feature importances in random forest. By Olivier Grisel and Arnaud Joly.

• Add `n_iter_` attribute to estimators that accept a `max_iter` attribute in their constructor. By Manoj Kumar.

• Added decision function for `multiclass.OneVsOneClassifier` By Raghav RV and Kyle Beauchamp.

• `neighbors.kneighbors_graph` and `radius_neighbors_graph` support non-Euclidean metrics. By Manoj Kumar.

• Parameter `connectivity` in `cluster.AgglomerativeClustering` and family now accept callables that return a connectivity matrix. By Manoj Kumar.

• Sparse support for `paired_distances`. By Joel Nothman.

• `cluster.DBSCAN` now supports sparse input and sample weights and has been optimized: the inner loop has been rewritten in Cython and radius neighbors queries are now computed in batch. By Joel Nothman and Lars Buitinck.

• Add `class_weight` parameter to automatically weight samples by class frequency for `ensemble.RandomForestClassifier`, `tree.DecisionTreeClassifier`, `ensemble.ExtraTreesClassifier` and `tree.ExtraTreeClassifier`. By Trevor Stephens.

• `grid_search.RandomizedSearchCV` now does sampling without replacement if all parameters are given as lists. By Andreas Müller.

• Parallelized calculation of `pairwise_distances` is now supported for scipy metrics and custom callables. By Joel Nothman.

• Allow the fitting and scoring of all clustering algorithms in `pipeline.Pipeline`. By Andreas Müller.

• More robust seeding and improved error messages in `cluster.MeanShift` by Andreas Müller.

• Make the stopping criterion for `mixture.GMM`, `mixture.DPGMM` and `mixture.VBGMM` less dependent on the number of samples by thresholding the average log-likelihood change instead of its sum over all samples. By Hervé Bredin.

• The outcome of `manifold.spectral_embedding` was made deterministic by flipping the sign of eigenvectors. By Hasil Sharma.


• Numerical stability improvements for `preprocessing.StandardScaler` and `preprocessing.scale`. By Nicolas Goix

• `svm.SVC` fitted on sparse input now implements `decision_function`. By Rob Zinkov and Andreas Müller.

• `cross_validation.train_test_split` now preserves the input type, instead of converting to numpy arrays.

**Documentation improvements**

• Added example of using `FeatureUnion` for heterogeneous input. By Matt Terry

• Documentation on scorers was improved, to highlight the handling of loss functions. By Matt Pico.

• A discrepancy between liblinear output and scikit-learn’s wrappers is now noted. By Manoj Kumar.
• Improved documentation generation: examples referring to a class or function are now shown in a gallery on the class/function’s API reference page. By Joel Nothman.

• More explicit documentation of sample generators and of data transformation. By Joel Nothman.

• `sklearn.neighbors.BallTree` and `sklearn.neighbors.KDTree` used to point to empty pages stating that they are aliases of `BinaryTree`. This has been fixed to show the correct class docs. By Manoj Kumar.

• Added silhouette plots for analysis of KMeans clustering using `metrics.silhouette_samples` and `metrics.silhouette_score`. See Selecting the number of clusters with silhouette analysis on KMeans clustering

**Bug fixes**

• Metaestimators now support ducktyping for the presence of `decision_function`, `predict_proba` and other methods. This fixes behavior of `grid_search.GridSearchCV`, `grid_search.RandomizedSearchCV`, `pipeline.Pipeline`, `feature_selection.RFE`, `feature_selection.RFECV` when nested. By Joel Nothman

• The `scoring` attribute of grid-search and cross-validation methods is no longer ignored when a `grid_search.GridSearchCV` is given as a base estimator or the base estimator doesn’t have predict.

• The function `hierarchical.ward_tree` now returns the children in the same order for both the structured and unstructured versions. By Matteo Visconti di Oleggio Castello.

• `feature_selection.RFECV` now correctly handles cases when `step` is not equal to 1. By Nikolay Mayorov

• The `decomposition.PCA` now undoes whitening in its `inverse_transform`. Also, its `components_` now always have unit length. By Michael Eickenberg.

• Fix incomplete download of the dataset when `datasets.download_20newsgroups` is called. By Manoj Kumar.

• Various fixes to the Gaussian processes subpackage by Vincent Dubourg and Jan Hendrik Metzen.

• Calling `partial_fit` with `class_weight='auto'` throws an appropriate error message and suggests a work around. By Danny Sullivan.

• `RBFSampler` with `gamma=g` formerly approximated `rbf_kernel` with `gamma=g/2`.; the definition of `gamma` is now consistent, which may substantially change your results if you use a fixed value. (If you cross-validated over `gamma`, it probably doesn’t matter too much.) By Dougal Sutherland.

• Pipeline object delegate the `classes_attribute` to the underlying estimator. It allows, for instance, to make bagging of a pipeline object. By Arnaud Joly

• `neighbors.NearestCentroid` now uses the median as the centroid when metric is set to `manhattan`. It was using the mean before. By Manoj Kumar

• Fix numerical stability issues in `linear_model.SGDClassifier` and `linear_model.SGDRegressor` by clipping large gradients and ensuring that weight decay rescaling is always positive (for large L2 regularization and large learning rate values). By Olivier Grisel

• When `compute_full_tree` is set to “auto”, the full tree is built when `n_clusters` is high and is early stopped when `n_clusters` is low, while the behavior should be vice-versa in `cluster.AgglomerativeClustering` (and friends). This has been fixed By Manoj Kumar

• Fix lazy centering of data in `linear_model.enet_path` and `linear_model.lasso_path`. It was centered around one. It has been changed to be centered around the origin. By Manoj Kumar
• Fix handling of precomputed affinity matrices in `cluster.AgglomerativeClustering` when using connectivity constraints. By Cathy Deng


• Fixed a crash in `metrics.precision_recall_fscore_support` when using unsorted labels in the multi-label setting. By Andreas Müller.

• Avoid skipping the first nearest neighbor in the methods `radius_neighbors`, `kneighbors`, `kneighbors_graph` and `radius_neighbors_graph` in `sklearn.neighbors.NearestNeighbors` and family, when the query data is not the same as fit data. By Manoj Kumar.

• Fix log-density calculation in the `mixture.GMM` with tied covariance. By Will Dawson

• Fixed a scaling error in `feature_selection.SelectFdr` where a factor `n_features` was missing. By Andrew Tulloch

• Fix zero division in `neighbors.KNeighborsRegressor` and related classes when using distance weighting and having identical data points. By Garret-R.

• Fixed round off errors with non positive-definite covariance matrices in GMM. By Alexis Mignon.

• Fixed a error in the computation of conditional probabilities in `naive_bayes.BernoulliNB`. By Hanna Wallach.

• Make the method `radius_neighbors` of `neighbors.NearestNeighbors` return the samples lying on the boundary for algorithm='brute'. By Yan Yi.

• Flip sign of `dual_coef_` of `svm.SVC` to make it consistent with the documentation and `decision_function`. By Artem Sobolev.

• Fixed handling of ties in `isotonic.IsotonicRegression`. We now use the weighted average of targets (secondary method). By Andreas Müller and Michael Bommarito.

**API changes summary**

• `GridSearchCV` and `cross_val_score` and other meta-estimators don’t convert pandas DataFrames into arrays any more, allowing DataFrame specific operations in custom estimators.

• `multiclass.fit_ovr`, `multiclass.predict_ovr`, `predict_proba_ovr`, `multiclass.fit_ovo`, `multiclass.predict_ovo`, `multiclass.fit_ecoc` and `multiclass.predict_ecoc` are deprecated. Use the underlying estimators instead.

• Nearest neighbors estimators used to take arbitrary keyword arguments and pass these to their distance metric. This will no longer be supported in scikit-learn 0.18; use the `metric_params` argument instead.

• The `predict_proba` method of `multiclass.OneVsRestClassifier` now returns two probabilities per sample in the multiclass case; this is consistent with other estimators and with the method’s documentation, but previous versions accidentally returned only the positive probability. Fixed by Will Lamond and Lars Buitinck.

• Change default value of precompute in `ElasticNet` and `Lasso` to False. Setting precompute to “auto” was found to be slower when n_samples > n_features since the computation of the Gram matrix is computationally expensive and outweighs the benefit of fitting the Gram for just one alpha. `precompute="auto"` is now deprecated and will be removed in 0.18 By Manoj Kumar.

• Expose `positive` option in `linear_model.enet_path` and `linear_model.enet_path` which constrains coefficients to be positive. By Manoj Kumar.
• Users should now supply an explicit `average` parameter to `sklearn.metrics.f1_score`, `sklearn.metrics.fbeta_score`, `sklearn.metrics.recall_score` and `sklearn.metrics.precision_score` when performing multiclass or multilabel (i.e. not binary) classification. By Joel Nothman.

• `scoring` parameter for cross validation now accepts `'f1_micro'`, `'f1_macro'` or `'f1_weighted'`. `'f1'` is now for binary classification only. Similar changes apply to `'precision'` and `'recall'`. By Joel Nothman.

• The `fit_intercept`, `normalize` and `return_models` parameters in `linear_model.enet_path` and `linear_model.lasso_path` have been removed. They were deprecated since 0.14

• From now onwards, all estimators will uniformly raise `NotFittedError` (utils.validation. NotFittedError), when any of the `predict` like methods are called before the model is fit. By Raghav RV.

• Input data validation was refactored for more consistent input validation. The `check_arrays` function was replaced by `check_array` and `check_X_y`. By Andreas Müller.

• Allow `X=None` in the methods `radius_neighbors`, `kneighbors`, `kneighbors_graph` and `radius_neighbors_graph` in `sklearn.neighbors.NearestNeighbors` and family. If set to None, then for every sample this avoids setting the sample itself as the first nearest neighbor. By Manoj Kumar.

• Add parameter `include_self` in `neighbors.kneighbors_graph` and `neighbors.radius_neighbors_graph` which has to be explicitly set by the user. If set to True, then the sample itself is considered as the first nearest neighbor.

• `thresh` parameter is deprecated in favor of new `tol` parameter in `GMM`, `DPGMM` and `VBGMM`. See Enhancements section for details. By Hervé Bredin.

• Estimators will treat input with dtype object as numeric when possible. By Andreas Müller

• Estimators now raise `ValueError` consistently when fitted on empty data (less than 1 sample or less than 1 feature for 2D input). By Olivier Grisel.


• `cluster.DBSCAN` now uses a deterministic initialization. The `random_state` parameter is deprecated. By Erich Schubert.

**Code Contributors**

1.8.8 Version 0.15.2

September 4, 2014

Bug fixes

- Fixed handling of the $p$ parameter of the Minkowski distance that was previously ignored in nearest neighbors models. By Nikolay Mayorov.

- Fixed duplicated alphas in `linear_model.LassoLars` with early stopping on 32 bit Python. By Olivier Grisel and Fabian Pedregosa.

- Fixed the build under Windows when scikit-learn is built with MSVC while NumPy is built with MinGW. By Olivier Grisel and Federico Vaggi.

- Fixed an array index overflow bug in the coordinate descent solver. By Gael Varoquaux.

- Better handling of numpy 1.9 deprecation warnings. By Gael Varoquaux.


- Explicitly close open files to avoid ResourceWarnings under Python 3. By Calvin Giles.

- The `transform` of `discriminant_analysis.LinearDiscriminantAnalysis` now projects the input on the most discriminant directions. By Martin Billinger.

- Fixed potential overflow in `_tree.safe_realloc` by Lars Buitinck.


- `nose` is no-longer a runtime dependency to import `sklearn`, only for running the tests. By Joel Nothman.

- Many documentation and website fixes by Joel Nothman, Lars Buitinck Matt Pico, and others.

1.8.9 Version 0.15.1

August 1, 2014

Bug fixes


- Support unseen labels `preprocessing.LabelBinarizer` to restore the default behavior of 0.14.1 for backward compatibility. By Hamzeh Alsahi.

- Fixed the `cluster.KMeans` stopping criterion that prevented early convergence detection. By Edward Raff and Gael Varoquaux.

- Fixed the behavior of `multiclass.OneVsOneClassifier` in case of ties at the per-class vote level by computing the correct per-class sum of prediction scores. By Andreas Müller.
• Made `cross_validation.cross_val_score` and `grid_search.GridSearchCV` accept Python lists as input data. This is especially useful for cross-validation and model selection of text processing pipelines. By Andreas Müller.

• Fixed data input checks of most estimators to accept input data that implements the NumPy `__array__` protocol. This is the case for for `pandas.Series` and `pandas.DataFrame` in recent versions of pandas. By Gael Varoquaux.

• Fixed a regression for `linear_model.SGDClassifier` with `class_weight="auto"` on data with non-contiguous labels. By Olivier Grisel.

1.8.10 Version 0.15
July 15, 2014

Highlights

• Many speed and memory improvements all across the code
• Huge speed and memory improvements to random forests (and extra trees) that also benefit better from parallel computing.
• Incremental fit to `BernoulliRBM`
• Added `cluster.AgglomerativeClustering` for hierarchical agglomerative clustering with average linkage, complete linkage and ward strategies.
• Added `linear_model.RANSACRegressor` for robust regression models.
• Added dimensionality reduction with `manifold.TSNE` which can be used to visualize high-dimensional data.

Changelog

New features

• Added `ensemble.BaggingClassifier` and `ensemble.BaggingRegressor` meta-estimators for ensembling any kind of base estimator. See the Bagging section of the user guide for details and examples. By Gilles Louppe.
• Added `linear_model.RANSACRegressor` meta-estimator for the robust fitting of regression models. By Johannes Schönberger.
• Added `cluster.AgglomerativeClustering` for hierarchical agglomerative clustering with average linkage, complete linkage and ward strategies, by Nelle Varoquaux and Gael Varoquaux.
• Shorthand constructors `pipeline.make_pipeline` and `pipeline.make_union` were added by Lars Buitinck.
• Shuffle option for `cross_validation.StratifiedKFold`. By Jeffrey Blackburne.
• Incremental learning (partial_fit) for Gaussian Naive Bayes by Imran Haque.
• Added `partial_fit` to `BernoulliRBM` By Danny Sullivan.
• Added `learning_curve` utility to chart performance with respect to training size. See Plotting Learning Curves. By Alexander Fabisch.
• Add positive option in LassoCV and ElasticNetCV. By Brian Wignall and Alexandre Gramfort.

• Added LinearModel.MultiTaskElasticNetCV and LinearModel.MultiTaskLassoCV. By Manoj Kumar.

• Added manifold.TSNE. By Alexander Fabisch.

Enhancements


• Memory improvements of decision trees, by Arnaud Joly.

• Decision trees can now be built in best-first manner by using max_leaf_nodes as the stopping criteria. Refactored the tree code to use either a stack or a priority queue for tree building. By Peter Prettenhofer and Gilles Louppe.

• Decision trees can now be fitted on fortran- and c-style arrays, and non-continuous arrays without the need to make a copy. If the input array has a different dtype than np.float32, a fortran- style copy will be made since fortran-style memory layout has speed advantages. By Peter Prettenhofer and Gilles Louppe.

• Speed improvement of regression trees by optimizing the computation of the mean square error criterion. This lead to speed improvement of the tree, forest and gradient boosting tree modules. By Arnaud Joly.

• The img_to_graph and grid_to_graph functions in sklearn.feature_extraction.image now return np.ndarray instead of np.matrix when return_as=ndarray. See the Notes section for more information on compatibility.

• Changed the internal storage of decision trees to use a struct array. This fixed some small bugs, while improving code and providing a small speed gain. By Joel Nothman.

• Reduce memory usage and overhead when fitting and predicting with forests of randomized trees in parallel with n_jobs ! = 1 by leveraging new threading backend of joblib 0.8 and releasing the GIL in the tree fitting Cython code. By Olivier Grisel and Gilles Louppe.

• Speed improvement of the sklearn.ensemble.gradient_boosting module. By Gilles Louppe and Peter Prettenhofer.

• Various enhancements to the sklearn.ensemble.gradient_boosting module: a warm_start argument to fit additional trees, a max_leaf_nodes argument to fit GBM style trees, a monitor fit argument to inspect the estimator during training, and refactoring of the verbose code. By Peter Prettenhofer.

• Faster sklearn.ensemble.ExtraTrees by caching feature values. By Arnaud Joly.

• Faster depth-based tree building algorithm such as decision tree, random forest, extra trees or gradient tree boosting (with depth based growing strategy) by avoiding trying to split on found constant features in the sample subset. By Arnaud Joly.

• Add min_weight_fraction_leaf pre-pruning parameter to tree-based methods: the minimum weighted fraction of the input samples required to be at a leaf node. By Noel Dawe.

• Added metrics.pairwise_distances_argmin_min, by Philippe Gervais.

• Added predict method to cluster.AffinityPropagation and cluster.MeanShift, by Mathieu Blondel.

• Vector and matrix multiplications have been optimised throughout the library by Denis Engemann, and Alexandre Gramfort. In particular, they should take less memory with older NumPy versions (prior to 1.7.2).

• Precision-recall and ROC examples now use train_test_split, and have more explanation of why these metrics are useful. By Kyle Kastner
• The training algorithm for `decomposition.NMF` is faster for sparse matrices and has much lower memory complexity, meaning it will scale up gracefully to large datasets. By Lars Buitinck.

• Added `svd_method` option with default value to “randomized” to `decomposition.FactorAnalysis` to save memory and significantly speedup computation by Denis Engemann, and Alexandre Gramfort.

• Changed `cross_validation.StratifiedKFold` to try and preserve as much of the original ordering of samples as possible so as not to hide overfitting on datasets with a non-negligible level of samples dependency. By Daniel Nouri and Olivier Grisel.

• Add multi-output support to `gaussian_process.GaussianProcess` by John Novak.

• Support for precomputed distance matrices in nearest neighbor estimators by Robert Layton and Joel Nothman.

• Norm computations optimized for NumPy 1.6 and later versions by Lars Buitinck. In particular, the k-means algorithm no longer needs a temporary data structure the size of its input.

• `dummy.DummyClassifier` can now be used to predict a constant output value. By Manoj Kumar.

• `dummy.DummyRegressor` has now a strategy parameter which allows to predict the mean, the median of the training set or a constant output value. By Maheshakya Wijewardena.

• Multi-label classification output in multilabel indicator format is now supported by `metrics.roc_auc_score` and `metrics.average_precision_score` by Arnaud Joly.

• Significant performance improvements (more than 100x speedup for large problems) in `isotonic.IsotonicRegression` by Andrew Tulloch.

• Speed and memory usage improvements to the SGD algorithm for linear models: it now uses threads, not separate processes, when `n_jobs>1`. By Lars Buitinck.

• Grid search and cross validation allow NaNs in the input arrays so that preprocessors such as `preprocessing.Imputer` can be trained within the cross validation loop, avoiding potentially skewed results.

• Ridge regression can now deal with sample weights in feature space (only sample space until then). By Michael Eickenberg. Both solutions are provided by the Cholesky solver.

• Several classification and regression metrics now support weighted samples with the new `sample_weight` argument: `metrics.accuracy_score`, `metrics.zero_one_loss`, `metrics.precision_score`, `metrics.average_precision_score`, `metrics.f1_score`, `metrics.fbeta_score`, `metrics.recall_score`, `metrics.roc_auc_score`, `metrics.explained_variance_score`, `metrics.mean_squared_error`, `metrics.mean_absolute_error`, `metrics.r2_score`. By Noel Dawe.

• Speed up of the sample generator `datasets.make_multilabel_classification`. By Joel Nothman.

Documentation improvements

• The `Working With Text Data` tutorial has now been worked in to the main documentation’s tutorial section. Includes exercises and skeletons for tutorial presentation. Original tutorial created by several authors including Olivier Grisel, Lars Buitinck and many others. Tutorial integration into the scikit-learn documentation by Jaques Grobler.

• Added `Computational Performance` documentation. Discussion and examples of prediction latency / throughput and different factors that have influence over speed. Additional tips for building faster models and choosing a relevant compromise between speed and predictive power. By Eustache Diemert.
Bug fixes

- Fixed bug in `decomposition.MiniBatchDictionaryLearning`: `partial_fit` was not working properly.
- Fixed bug in `linear_model.stochastic_gradient`: `l1_ratio` was used as `(1.0 - l1_ratio)`.
- Fixed bug in `multiclass.OneVsOneClassifier` with string labels.
- Fixed a bug in `LassoCV` and `ElasticNetCV`: they would not pre-compute the Gram matrix with `precompute=True` or `precompute="auto"` and `n_samples > n_features`. By Manoj Kumar.
- Fixed incorrect estimation of the degrees of freedom in `feature_selection.f_regression` when variates are not centered. By Virgile Fritsch.
- Fixed a race condition in parallel processing with `pre_dispatch != "all"` (for instance, in `cross_val_score`). By Olivier Grisel.
- Raise error in `cluster.FeatureAgglomeration` and `cluster.WardAgglomeration` when no samples are given, rather than returning meaningless clustering.
- Fixed bug in `gradient_boosting.GradientBoostingRegressor` with `loss='huber'`: `gamma` might have not been initialized.
- Fixed feature importances as computed with a forest of randomized trees when fit with `sample_weight != None` and/or with `bootstrap=True`. By Gilles Louppe.

API changes summary

- `sklearn.hmm` is deprecated. Its removal is planned for the 0.17 release.
- Use of `covariance.EllipticEnvelop` has now been removed after deprecation. Please use `covariance.EllipticEnvelope` instead.
- `cluster.Ward` is deprecated. Use `cluster.AgglomerativeClustering` instead.
- `cluster.WardClustering` is deprecated. Use `cluster.AgglomerativeClustering` instead.
- `cross_validation.Bootstrap` is deprecated. `cross_validation.KFold` or `cross_validation.ShuffleSplit` are recommended instead.
- Direct support for the sequence of sequences (or list of lists) multilabel format is deprecated. To convert to and from the supported binary indicator matrix format, use `MultiLabelBinarizer`. By Joel Nothman.
- Add score method to `PCA` following the model of probabilistic PCA and deprecate `ProbabilisticPCA` model whose score implementation is not correct. The computation now also exploits the matrix inversion lemma for faster computation. By Alexandre Gramfort.
- The score method of `FactorAnalysis` now returns the average log-likelihood of the samples. Use `score_samples` to get log-likelihood of each sample. By Alexandre Gramfort.
- Generating boolean masks (the setting `indices=False`) from cross-validation generators is deprecated. Support for masks will be removed in 0.17. The generators have produced arrays of indices by default since 0.10. By Joel Nothman.
- 1-d arrays containing strings with `dtype=object` (as used in Pandas) are now considered valid classification targets. This fixes a regression from version 0.13 in some classifiers. By Joel Nothman.
- Fix wrong `explained_variance_ratio_` attribute in `RandomizedPCA`. By Alexandre Gramfort.
• Fit alphas for each \texttt{l1_ratio} instead of \texttt{mean_l1_ratio} in \texttt{linear_model.ElasticNetCV} and \texttt{linear_model.LassoCV}. This changes the shape of \texttt{alphas} from \texttt{(n_alphas,) to (n\_l1\_ratio, n\_alphas)} if the \texttt{l1\_ratio} provided is a 1-D array like object of length greater than one. By Manoj Kumar.

• Fix \texttt{linear_model.ElasticNetCV} and \texttt{linear_model.LassoCV} when fitting intercept and input data is sparse. The automatic grid of alphas was not computed correctly and the scaling with normalize was wrong. By Manoj Kumar.

• Fix wrong maximal number of features drawn \texttt{(max\_features)} at each split for decision trees, random forests and gradient tree boosting. Previously, the count for the number of drawn features started only after one non constant features in the split. This bug fix will affect computational and generalization performance of those algorithms in the presence of constant features. To get back previous generalization performance, you should modify the value of \texttt{max\_features}. By Arnaud Joly.

• Fix wrong maximal number of features drawn \texttt{(max\_features)} at each split for \texttt{ensemble.ExtraTreesClassifier} and \texttt{ensemble.ExtraTreesRegressor}. Previously, only non constant features in the split was counted as drawn. Now constant features are counted as drawn. Furthermore at least one feature must be non constant in order to make a valid split. This bug fix will affect computational and generalization performance of extra trees in the presence of constant features. To get back previous generalization performance, you should modify the value of \texttt{max\_features}. By Arnaud Joly.

• Fix \texttt{utils.compute_class_weight} when \texttt{class_weight="auto"}. Previously it was broken for input of non-integer \texttt{dtype} and the weighted array that was returned was wrong. By Manoj Kumar.

• Fix \texttt{cross\_validation.Bootstrap} to return \texttt{ValueError} when \texttt{n\_train + n\_test > n}. By Ronald Phlypo.

**People**

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• 312 Olivier Grisel
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• 221 Gael Varoquaux
• 148 Arnaud Joly
• 134 Johannes Schönberger
• 119 Gilles Louppe
• 113 Joel Nothman
• 111 Alexandre Gramfort
• 95 Jaques Grobler
• 89 Denis Engemann
• 83 Peter Prettenhofer
• 83 Alexander Fabisch
• 62 Mathieu Blondel
• 60 Eustache Diemert
• 60 Nelle Varoquaux
• 49 Michael Bommarito
• 45 Manoj-Kumar-S
1.8. Previous Releases

- 28 Kyle Kastner
- 26 Andreas Mueller
- 22 Noel Dawe
- 21 Maheshakya Wijewardena
- 21 Brooke Osborn
- 21 Hamzeh Alsalhi
- 21 Jake VanderPlas
- 21 Philippe Gervais
- 19 Bala Subrahmanyam Varanasi
- 12 Ronald Phlypo
- 10 Mikhail Korobov
- 8 Thomas Unterrhiner
- 8 Jeffrey Blackburne
- 8 eltermann
- 8 bwignall
- 7 Ankit Agrawal
- 7 CJ Carey
- 6 Daniel Nouri
- 6 Chen Liu
- 6 Michael Eickenberg
- 6 ugrurthemaster
- 5 Aaron Schumacher
- 5 Baptiste Lagarde
- 5 Rajat Khanduja
- 5 Robert McGibbon
- 5 Sergio Pascual
- 4 Alexis Metaireau
- 4 Ignacio Rossi
- 4 Virgile Fritsch
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- 3 Andrew Tulloch
• 3 murad
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• 3 Karol Pysniak
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• 3 john collins
• 3 kaushik94
• 3 Erwin Marsi
• 2 csytracy
• 2 LK
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• Joseph Perla
• Joshua Vredevoogd
• José Ricardo
• Julien Miotte
• Kemal Eren
• Kenta Sato
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• Kyle Kelley
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• Laurent Luce
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• Luis Pedro Coelho
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• Craig Thompson
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• Bryan Lunt
• Brian Kearns
• Paul Butler
• Paweł Mandera
• Peter
• Andrew Ash
• Pietro Zambelli
1.8.11 Version 0.14

August 7, 2013

Changelog

- Missing values with sparse and dense matrices can be imputed with the transformer `preprocessing.Imputer` by Nicolas Trésegnie.
- The core implementation of decisions trees has been rewritten from scratch, allowing for faster tree induction and lower memory consumption in all tree-based estimators. By Gilles Louppe.
- Added `ensemble.AdaBoostClassifier` and `ensemble.AdaBoostRegressor`, by Noel Dawe and Gilles Louppe. See the AdaBoost section of the user guide for details and examples.
- Added biclustering algorithms (`sklearn.cluster.bicluster.SpectralCoclustering` and `sklearn.cluster.bicluster.SpectralBiclustering`), data generation methods (`sklearn.datasets.make_biclusters` and `sklearn.datasets.make_checkerboard`), and scoring metrics (`sklearn.metrics.consensus_score`). By Kemal Eren.
- Added Restricted Boltzmann Machines (`neural_network.BernoulliRBM`), by Yann Dauphin.
- Python 3 support by Justin Vincent, Lars Buitinck, Subhodeep Moitra and Olivier Grisel. All tests now pass under Python 3.3.
- Ability to pass one penalty (alpha value) per target in `linear_model.Ridge`, by @eickenberg and Mathieu Blondel.
- Added an interactive version of Andreas Müller’s Machine Learning Cheat Sheet (for scikit-learn) to the documentation. See Choosing the right estimator, by Jaques Grobler.
- `grid_search.GridSearchCV` and `cross_validation.cross_val_score` now support the use of advanced scoring function such as area under the ROC curve and f-beta scores. See The scoring parameter: defining model evaluation rules for details. By Andreas Müller and Lars Buitinck. Passing a function from `sklearn.metrics` as `score_func` is deprecated.
- Multi-label classification output is now supported by `metrics.accuracy_score`, `metrics.zero_one_loss`, `metrics.f1_score`, `metrics.fbeta_score`, `metrics.classification_report`, `metrics.precision_score` and `metrics.recall_score` by Arnaud Joly.
- Two new metrics `metrics.hamming_loss` and `metrics.jaccard_similarity_score` are added with multi-label support by Arnaud Joly.
- Speed and memory usage improvements in `feature_extraction.text.CountVectorizer` and `feature_extraction.text.TfidfVectorizer`, by Jochen Wersdörfer and Roman Sinayev.
- The `min_df` parameter in `feature_extraction.text.CountVectorizer` and `feature_extraction.text.TfidfVectorizer`, which used to be 2, has been reset to 1 to avoid unpleasant surprises (empty vocabularies) for novice users who try it out on tiny document collections. A value of at least 2 is still recommended for practical use.
• **svm.LinearSVC, linear_model.SGDClassifier** and **linear_model.SGDRegressor** now have a **sparsify** method that converts their **coef_** into a sparse matrix, meaning stored models trained using these estimators can be made much more compact.

• **linear_model.SGDClassifier** now produces multiclass probability estimates when trained under log loss or modified Huber loss.

• Hyperlinks to documentation in example code on the website by Martin Luessi.

• Fixed bug in **preprocessing.MinMaxScaler** causing incorrect scaling of the features for non-default **feature_range** settings. By Andreas Müller.

• **max_features** in **tree.DecisionTreeClassifier, tree.DecisionTreeRegressor** and all derived ensemble estimators now supports percentage values. By Gilles Louppe.

• Performance improvements in **isotonic.IsotonicRegression** by Nelle Varoquaux.

• **metrics.accuracy_score** has an option **normalize** to return the fraction or the number of correctly classified sample by Arnaud Joly.

• Added **metrics.log_loss** that computes log loss, aka cross-entropy loss. By Jochen Wersdörfer and Lars Buitinck.

• A bug that caused **ensemble.AdaBoostClassifier**’s to output incorrect probabilities has been fixed.

• Feature selectors now share a mixin providing consistent **transform, inverse_transform** and **get_support** methods. By Joel Nothman.

• A fitted **grid_search.GridSearchCV** or **grid_search.RandomizedSearchCV** can now generally be pickled. By Joel Nothman.

• Refactored and vectorized implementation of **metrics.roc_curve** and **metrics.precision_recall_curve**. By Joel Nothman.

• The new estimator **sklearn.decomposition.TruncatedSVD** performs dimensionality reduction using SVD on sparse matrices, and can be used for latent semantic analysis (LSA). By Lars Buitinck.

• Added self-contained example of out-of-core learning on text data **Out-of-core classification of text documents**. By Eustache Diemert.

• The default number of components for **sklearn.decomposition.RandomizedPCA** is now correctly documented to be **n_features**. This was the default behavior, so programs using it will continue to work as they did.

• **sklearn.cluster.KMeans** now fits several orders of magnitude faster on sparse data (the speedup depends on the sparsity). By Lars Buitinck.

• Reduce memory footprint of FastICA by Denis Engemann and Alexandre Gramfort.

• Verbose output in **sklearn.ensemble.gradient_boosting** now uses a column format and prints progress in decreasing frequency. It also shows the remaining time. By Peter Prettenhofer.

• **sklearn.ensemble.gradient_boosting** provides **out-of-bag improvement oob_improvement_** rather than the OOB score for model selection. An example that shows how to use OOB estimates to select the number of trees was added. By Peter Prettenhofer.

• Most metrics now support string labels for multiclass classification by Arnaud Joly and Lars Buitinck.

• New OrthogonalMatchingPursuitCV class by Alexandre Gramfort and Vlad Niculae.

• Fixed a bug in **sklearn.covariance.GraphLassoCV**: the ‘alphas’ parameter now works as expected when given a list of values. By Philippe Gervais.
• Fixed an important bug in `sklearn.covariance.GraphLassoCV` that prevented all folds provided by a CV object to be used (only the first 3 were used). When providing a CV object, execution time may thus increase significantly compared to the previous version (bug results are correct now). By Philippe Gervais.

• `cross_validation.cross_val_score` and the `grid_search` module is now tested with multi-output data by Arnaud Joly.

• `datasets.make_multilabel_classification` can now return the output in label indicator multi-label format by Arnaud Joly.


• Random state in LibSVM-based estimators (`svm.SVC`, `NuSVC`, `OneClassSVM`, `svm.SVR`, `svm.NuSVR`) can now be controlled. This is useful to ensure consistency in the probability estimates for the classifiers trained with `probability=True`. By Vlad Niculae.

• Out-of-core learning support for discrete naive Bayes classifiers `sklearn.naive_bayes.MultinomialNB` and `sklearn.naive_bayes.BernoulliNB` by adding the `partial_fit` method by Olivier Grisel.

• New website design and navigation by Gilles Louppe, Nelle Varoquaux, Vincent Michel and Andreas Müller.

• Improved documentation on multi-class, multi-label and multi-output classification by Yannick Schwartz and Arnaud Joly.

• Better input and error handling in the `metrics` module by Arnaud Joly and Joel Nothman.

• Speed optimization of the `hmm` module by Mikhail Korobov

• Significant speed improvements for `sklearn.cluster.DBSCAN` by cleverless

**API changes summary**

• The `auc_score` was renamed `roc_auc_score`.

• Testing scikit-learn with `sklearn.test()` is deprecated. Use `nositests sklearn` from the command line.

• Feature importances in `tree.DecisionTreeClassifier`, `tree.DecisionTreeRegressor` and all derived ensemble estimators are now computed on the fly when accessing the `feature_importances_` attribute. Setting `compute_importances=True` is no longer required. By Gilles Louppe.

• `linear_model.lasso_path` and `linear_model.enet_path` can return its results in the same format as that of `linear_model.lars_path`. This is done by setting the `return_models` parameter to `False`. By Jaques Grobler and Alexandre Gramfort

• `grid_search.IterGrid` was renamed to `grid_search.ParameterGrid`.

• Fixed bug in KFold causing imperfect class balance in some cases. By Alexandre Gramfort and Tadej Janež.

• `sklearn.neighbors.BallTree` has been refactored, and a `sklearn.neighbors.KDTree` has been added which shares the same interface. The Ball Tree now works with a wide variety of distance metrics. Both classes have many new methods, including single-tree and dual-tree queries, breadth-first and depth-first searching, and more advanced queries such as kernel density estimation and 2-point correlation functions. By Jake Vanderplas

• Support for scipy.spatial.cKDTree within neighbors queries has been removed, and the functionality replaced with the new `KDTree` class.
• **sklearn.neighbors.KernelDensity** has been added, which performs efficient kernel density estimation with a variety of kernels.

• **sklearn.decomposition.KernelPCA** now always returns output with n_components components, unless the new parameter remove_zero_eig is set to True. This new behavior is consistent with the way kernel PCA was always documented; previously, the removal of components with zero eigenvalues was tacitly performed on all data.

• gcv_mode="auto" no longer tries to perform SVD on a densified sparse matrix in **sklearn.linear_model.RidgeCV**.

• Sparse matrix support in **sklearn.decomposition.RandomizedPCA** is now deprecated in favor of the new **TruncatedSVD**.

• **cross_validation.KFold** and **cross_validation.StratifiedKFold** now enforce n_folds >= 2 otherwise a ValueError is raised. By Olivier Grisel.

• **datasets.load_files**’s charset and charset_errors parameters were renamed encoding and decode_errors.

• Attribute oob_score_ in **sklearn.ensemble.GradientBoostingRegressor** and **sklearn.ensemble.GradientBoostingClassifier** is deprecated and has been replaced by oob_improvement_.

• Attributes in OrthogonalMatchingPursuit have been deprecated (copy_X, Gram, ...) and precompute_gram renamed precompute for consistency. See #2224.

• **sklearn.preprocessing.StandardScaler** now converts integer input to float, and raises a warning. Previously it rounded for dense integer input.

• **sklearn.multiclass.OneVsRestClassifier** now has a decision_function method. This will return the distance of each sample from the decision boundary for each class, as long as the underlying estimators implement the decision_function method. By Kyle Kastner.

• Better input validation, warning on unexpected shapes for y.

**People**

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• 187 Andreas Mueller
• 124 Arnaud Joly
• 112 Jaques Grobler
• 109 Gael Varoquaux
• 107 Olivier Grisel
• 102 Noel Dawe
• 99 Kemal Eren
• 79 Joel Nothman
• 75 Jake VanderPlas
• 73 Nelle Varoquaux
• 71 Vlad Niculae
• 65 Peter Prettenhofer
• 64 Alexandre Gramfort
• 54 Mathieu Blondel
• 38 Nicolas Trésegnie
• 35 eustache
• 27 Denis Engemann
• 25 Yann N. Dauphin
• 19 Justin Vincent
• 17 Robert Layton
• 15 Doug Coleman
• 14 Michael Eickenberg
• 13 Robert Marchman
• 11 Fabian Pedregosa
• 11 Philippe Gervais
• 10 Jim Holmström
• 10 Tadej Janež
• 10 syhw
• 9 Mikhail Korobov
• 9 Steven De Gryze
• 8 sergeyf
• 7 Ben Root
• 7 Hrishikesh Huilgolkar
• 6 Kyle Kastner
• 6 Martin Luessi
• 6 Rob Speer
• 5 Federico Vaggi
• 5 Raul Garreta
• 5 Rob Zinkov
• 4 Ken Geis
• 3 A. Flaxman
• 3 Denton Cockburn
• 3 Dougal Sutherland
• 3 Ian Ozsvald
• 3 Johannes Schönberger
• 3 Robert McGibbon
• 3 Roman Sinayev

1.8. Previous Releases
• 3 Szabo Roland
• 2 Diego Molla
• 2 Imran Haque
• 2 Jochen Wersdörfer
• 2 Sergey Karayev
• 2 Yannick Schwartz
• 2 jameswebber
• 1 Abhijeet Kolhe
• 1 Alexander Fabisch
• 1 Bastiaan van den Berg
• 1 Benjamin Peterson
• 1 Daniel Velkov
• 1 Fazlul Shahriar
• 1 Felix Brockherde
• 1 Félix-Antoine Fortin
• 1 Harikrishnan S
• 1 Jack Hale
• 1 JakeMick
• 1 James McDermott
• 1 John Benediktsson
• 1 John Zwinck
• 1 Joshua Vredevoogd
• 1 Justin Pati
• 1 Kevin Hughes
• 1 Kyle Kelley
• 1 Matthias Ekman
• 1 Miroslav Shubernetskiy
• 1 Naoki Orii
• 1 Norbert Crombach
• 1 Rafael Cunha de Almeida
• 1 Rolando Espinoza La fuente
• 1 Seamus Abshire
• 1 Sergey Feldman
• 1 Sergio Medina
• 1 Stefano Lattarini
• 1 Steve Koch
The 0.13.1 release only fixes some bugs and does not add any new functionality.

Changelog

- Fixed a testing error caused by the function `cross_validation.train_test_split` being interpreted as a test by Yaroslav Halchenko.
- Fixed a bug in the reassignment of small clusters in the `cluster.MiniBatchKMeans` by Gael Varoquaux.
- Fixed default value of `gamma` in `decomposition.KernelPCA` by Lars Buitinck.
- Updated joblib to 0.7.0d by Gael Varoquaux.
- Fixed scaling of the deviance in `ensemble.GradientBoostingClassifier` by Peter Prettenhofer.
- Better tie-breaking in `multiclass.OneVsOneClassifier` by Andreas Müller.
- Other small improvements to tests and documentation.

People

List of contributors for release 0.13.1 by number of commits.

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- 12 Andreas Müller
- 8 Gael Varoquaux
- 5 Robert Marchman
- 3 Peter Prettenhofer
- 2 Hrishikesh Huilgolkar
- 1 Bastiaan van den Berg
- 1 Diego Molla
- 1 Gilles Louppe
- 1 Mathieu Blondel
- 1 Nelle Varoquaux
- 1 Rafael Cunha de Almeida
- 1 Rolando Espinoza La fuente
- 1 Vlad Niculae
- 1 Yaroslav Halchenko
New Estimator Classes


- `decomposition.FactorAnalysis`, a transformer implementing the classical factor analysis, by Christian Osendorfer and Alexandre Gramfort. See Factor Analysis in the user guide.

- `feature_extraction.FeatureHasher`, a transformer implementing the “hashing trick” for fast, low-memory feature extraction from string fields by Lars Buitinck and feature_extraction.text. HashingVectorizer for text documents by Olivier Grisel See Feature hashing and Vectorizing a large text corpus with the hashing trick for the documentation and sample usage.

- `pipeline.FeatureUnion`, a transformer that concatenates results of several other transformers by Andreas Müller. See FeatureUnion: composite feature spaces in the user guide.

- `random_projection.GaussianRandomProjection`, `random_projection.SparseRandomProjection` and the function `random_projection.johnson_lindenstrauss_min_dim`. The first two are transformers implementing Gaussian and sparse random projection matrix by Olivier Grisel and Arnaud Joly. See Random Projection in the user guide.


- `preprocessing.OneHotEncoder`, a transformer that computes binary encodings of categorical features by Andreas Müller. See Encoding categorical features in the user guide.


- `manifold.SpectralEmbedding` and function `manifold.spectral_embedding`, implementing the “laplacian eigenmaps” transformation for non-linear dimensionality reduction by Wei Li. See Spectral Embedding in the user guide.

- `isotonic.IsotonicRegression` by Fabian Pedregosa, Alexandre Gramfort and Nelle Varoquaux,

Changelog

- `metrics.zero_one_loss` (formerly `metrics.zero_one`) now has option for normalized output that reports the fraction of misclassifications, rather than the raw number of misclassifications. By Kyle Beauchamp.

- `tree.DecisionTreeClassifier` and all derived ensemble models now support sample weighting, by Noel Dawe and Gilles Louppe.

- Speedup improvement when using bootstrap samples in forests of randomized trees, by Peter Prettenhofer and Gilles Louppe.

- Partial dependence plots for Gradient Tree Boosting in `ensemble.partial_dependence.partial_dependence` by Peter Prettenhofer. See Partial Dependence Plots for an example.
• The table of contents on the website has now been made expandable by Jaques Grobler.

• `feature_selection.SelectPercentile` now breaks ties deterministically instead of returning all equally ranked features.

• `feature_selection.SelectKBest` and `feature_selection.SelectPercentile` are more numerically stable since they use scores, rather than p-values, to rank results. This means that they might sometimes select different features than they did previously.

• Ridge regression and ridge classification fitting with `sparse_cg` solver no longer has quadratic memory complexity, by Lars Buitinck and Fabian Pedregosa.

• Ridge regression and ridge classification now support a new fast solver called `lsqr`, by Mathieu Blondel.

• Speed up of `metrics.precision_recall_curve` by Conrad Lee.

• Added support for reading/writing svmlight files with pairwise preference attribute (qid in svmlight file format) in `datasets.dump_svmlight_file` and `datasets.load_svmlight_file` by Fabian Pedregosa.

• Faster and more robust `metrics.confusion_matrix` and `Clustering performance evaluation` by Wei Li.

• `cross_validation.cross_val_score` now works with precomputed kernels and affinity matrices, by Andreas Müller.

• LARS algorithm made more numerically stable with heuristics to drop regressors too correlated as well as to stop the path when numerical noise becomes predominant, by Gael Varoquaux.

• Faster implementation of `metrics.precision_recall_curve` by Conrad Lee.

• New kernel `metrics.chi2_kernel` by Andreas Müller, often used in computer vision applications.

• Fix of longstanding bug in `naive_bayes.BernoulliNB` fixed by Shaun Jackman.

• Implemented `predict_proba` in `multiclass.OneVsRestClassifier`, by Andrew Winterman.

• Improve consistency in gradient boosting: estimators `ensemble.GradientBoostingRegressor` and `ensemble.GradientBoostingClassifier` use the estimator `tree.DecisionTreeRegressor` instead of the `tree._tree.Tree` data structure by Arnaud Joly.

• Fixed a floating point exception in the `decision trees` module, by Seberg.

• Fix `metrics.roc_curve` fails when `y_true` has only one class by Wei Li.

• Add the `metrics.mean_absolute_error` function which computes the mean absolute error. The `metrics.mean_squared_error`, `metrics.mean_absolute_error` and `metrics.r2_score` metrics support multioutput by Arnaud Joly.

• Fixed `class_weight` support in `svm.LinearSVC` and `linear_model.LogisticRegression` by Andreas Müller. The meaning of `class_weight` was reversed as erroneously higher weight meant less positives of a given class in earlier releases.

• Improve narrative documentation and consistency in `sklearn.metrics` for regression and classification metrics by Arnaud Joly.

• Fixed a bug in `sklearn.svm.SVC` when using csr-matrices with unsorted indices by Xinfan Meng and Andreas Müller.

• MiniBatchKMeans: Add random reassignment of cluster centers with little observations attached to them, by Gael Varoquaux.

**API changes summary**

• Renamed all occurrences of `n_atoms` to `n_components` for consistency. This applies to `decomposition.DictionaryLearning`, `decomposition`. 81
MiniBatchDictionaryLearning, decomposition.dict_learning, decomposition.dict_learning_online.

- Renamed all occurrences of max_iters to max_iter for consistency. This applies to semi_supervised.LabelPropagation and semi_supervised.label_propagation.LabelSpreading.

- Renamed all occurrences of learn_rate to learning_rate for consistency in ensemble.BaseGradientBoosting and ensemble.GradientBoostingRegressor.

- The module sklearn.linear_model.sparse is gone. Sparse matrix support was already integrated into the “regular” linear models.

- sklearn.metrics.mean_square_error, which incorrectly returned the accumulated error, was removed. Use mean_squared_error instead.

- Passing class_weight parameters to fit methods is no longer supported. Pass them to estimator constructors instead.

- GMMs no longer have decode and rvs methods. Use the score, predict or sample methods instead.

- The solver fit option in Ridge regression and classification is now deprecated and will be removed in v0.14. Use the constructor option instead.

- feature_extraction.text.DictVectorizer now returns sparse matrices in the CSR format, instead of COO.

- Renamed k in cross_validation.KFold and cross_validation.StratifiedKFold to n_folds, renamed n_bootstraps to n_iter in cross_validation.Bootstrap.

- Renamed all occurrences of n_iterations to n_iter for consistency. This applies to cross_validation.ShuffleSplit, cross_validation.StratifiedShuffleSplit, utils.randomized_range_finder and utils.randomized_svd.

- Replaced rho in linear_model.ElasticNet and linear_model.SGDClassifier by l1_ratio. The rho parameter had different meanings; l1_ratio was introduced to avoid confusion. It has the same meaning as previously rho in linear_model.ElasticNet and (1-rho) in linear_model.SGDClassifier.

- linear_model.LassoLars and linear_model.Lars now store a list of paths in the case of multiple targets, rather than an array of paths.

- The attribute gmm of hmm.GMMHMM was renamed to gmm_ to adhere more strictly with the API.

- cluster.spectral_embedding was moved to manifold.spectral_embedding.

- Renamed eig_tol in manifold.spectral_embedding, cluster.SpectralClustering to eigen_tol, renamed mode to eigen_solver.

- Renamed mode in manifold.spectral_embedding and cluster.SpectralClustering to eigen_solver.

- classes_ and n_classes_ attributes of tree.DecisionTreeClassifier and all derived ensemble models are now flat in case of single output problems and nested in case of multi-output problems.


- svm.SVC and svm.NuSVC now provide a classes_ attribute and support arbitrary dtypes for labels y. Also, the dtype returned by predict now reflects the dtype of y during fit (used to be np.float).
• Changed default test_size in `cross_validation.train_test_split` to None, added possibility to infer test_size from train_size in `cross_validation.ShuffleSplit` and `cross_validation.StratifiedShuffleSplit`.

• Renamed function `sklearn.metrics.zero_one` to `sklearn.metrics.zero_one_loss`. Be aware that the default behavior in `sklearn.metrics.zero_one_loss` is different from `sklearn.metrics.zero_one`: normalize=False is changed to normalize=True.

• Renamed function `metrics.zero_one_score` to `metrics.accuracy_score`.

• `datasets.make_circles` now has the same number of inner and outer points.

• In the Naive Bayes classifiers, the class_prior parameter was moved from `fit` to `__init__`.

**People**

List of contributors for release 0.13 by number of commits.

- 364 Andreas Müller
- 143 Arnaud Joly
- 137 Peter Prettenhofer
- 131 Gael Varoquaux
- 117 Mathieu Blondel
- 108 Lars Buitinck
- 106 Wei Li
- 101 Olivier Grisel
- 65 Vlad Niculae
- 54 Gilles Louppe
- 40 Jaques Grobler
- 38 Alexandre Gramfort
- 30 Rob Zinkov
- 19 Aymeric Masurelle
- 18 Andrew Winterman
- 17 Fabian Pedregosa
- 17 Nelle Varoquaux
- 16 Christian Osendorfer
- 14 Daniel Nouri
- 13 Virgile Fritsch
- 13 syhw
- 12 Satrajit Ghosh
- 10 Corey Lynch
- 10 Kyle Beauchamp
- 9 Brian Cheung
• 9 Immanuel Bayer
• 9 mr.Shu
• 8 Conrad Lee
• 8 James Bergstra
• 7 Tadej Janež
• 6 Brian Cajes
• 6 Jake Vanderplas
• 6 Michael
• 6 Noel Dawe
• 6 Tiago Nunes
• 6 cow
• 5 Anze
• 5 Shiqiao Du
• 4 Christian Jauvin
• 4 Jacques Kvam
• 4 Richard T. Guy
• 4 Robert Layton
• 3 Alexandre Abraham
• 3 Doug Coleman
• 3 Scott Dickerson
• 2 ApproximateIdentity
• 2 John Benediktsson
• 2 Mark Veronda
• 2 Matti Lyra
• 2 Mikhail Korobov
• 2 Xinfan Meng
• 1 Alejandro Weinstein
• 1 Alexandre Passos
• 1 Christoph Deil
• 1 Eugene Nizhibitsky
• 1 Kenneth C. Arnold
• 1 Luis Pedro Coelho
• 1 Miroslav Batchkarov
• 1 Pavel
• 1 Sebastian Berg
• 1 Shaun Jackman
1.8.14 Version 0.12.1

October 8, 2012

The 0.12.1 release is a bug-fix release with no additional features, but is instead a set of bug fixes

Changelog

- Improved numerical stability in spectral embedding by Gael Varoquaux
- Doctest under windows 64bit by Gael Varoquaux
- Documentation fixes for elastic net by Andreas Müller and Alexandre Gramfort
- Proper behavior with fortran-ordered NumPy arrays by Gael Varoquaux
- Make GridSearchCV work with non-CSR sparse matrix by Lars Buitinck
- Fix parallel computing in MDS by Gael Varoquaux
- Fix Unicode support in count vectorizer by Andreas Müller
- Fix MinCovDet breaking with X.shape = (3, 1) by Virgile Fritsch
- Fix clone of SGD objects by Peter Prettenhofer
- Stabilize GMM by Virgile Fritsch

People

- 14 Peter Prettenhofer
- 12 Gael Varoquaux
- 10 Andreas Müller
- 5 Lars Buitinck
- 3 Virgile Fritsch
- 1 Alexandre Gramfort
- 1 Gilles Louppe
- 1 Mathieu Blondel

1.8.15 Version 0.12

September 4, 2012
Changelog

- Various speed improvements of the decision trees module, by Gilles Louppe.

- `ensemble.GradientBoostingRegressor` and `ensemble.GradientBoostingClassifier` now support feature subsampling via the `max_features` argument, by Peter Prettenhofer.

- Added Huber and Quantile loss functions to `ensemble.GradientBoostingRegressor`, by Peter Prettenhofer.

- Decision trees and forests of randomized trees now support multi-output classification and regression problems, by Gilles Louppe.

- Added `preprocessing.LabelEncoder`, a simple utility class to normalize labels or transform non-numerical labels, by Mathieu Blondel.

- Added the epsilon-insensitive loss and the ability to make probabilistic predictions with the modified huber loss in Stochastic Gradient Descent, by Mathieu Blondel.

- Added Multi-dimensional Scaling (MDS), by Nelle Varoquaux.

- SVMlight file format loader now detects compressed (gzip/bzip2) files and decompresses them on the fly, by Lars Buitinck.

- SVMlight file format serializer now preserves double precision floating point values, by Olivier Grisel.

- A common testing framework for all estimators was added, by Andreas Müller.

- Understandable error messages for estimators that do not accept sparse input by Gael Varoquaux.

- Speedups in hierarchical clustering by Gael Varoquaux. In particular building the tree now supports early stopping. This is useful when the number of clusters is not small compared to the number of samples.


- Added `metrics.auc_score` and `metrics.average_precision_score` convenience functions by Andreas Müller.

- Improved sparse matrix support in the Feature selection module by Andreas Müller.

- New word boundaries-aware character n-gram analyzer for the Text feature extraction module by @kernc.

- Fixed bug in spectral clustering that led to single point clusters by Andreas Müller.

- In `feature_extraction.text.CountVectorizer`, added an option to ignore infrequent words, `min_df` by Andreas Müller.

- Add support for multiple targets in some linear models (ElasticNet, Lasso and OrthogonalMatchingPursuit) by Vlad Niculae and Alexandre Gramfort.

- Fixes in `decomposition.ProbabilisticPCA` score function by Wei Li.

- Fixed feature importance computation in Gradient Tree Boosting.

API changes summary

- The old `scikits.learn` package has disappeared; all code should import from `sklearn` instead, which was introduced in 0.9.

- In `metrics.roc_curve`, the `thresholds` array is now returned with it's order reversed, in order to keep it consistent with the order of the returned fpr and tpr.

- In `hmm` objects, like `hmm.GaussianHMM`, `hmm.MultinomialHMM`, etc., all parameters must be passed to the object when initialising it and not through `fit`. Now `fit` will only accept the data as an input parameter.
• For all SVM classes, a faulty behavior of gamma was fixed. Previously, the default gamma value was only computed the first time fit was called and then stored. It is now recalculated on every call to fit.

• All Base classes are now abstract meta classes so that they can not be instantiated.

• cluster.ward_tree now also returns the parent array. This is necessary for early-stopping in which case the tree is not completely built.

• In feature_extraction.text.CountVectorizer the parameters min_n and max_n were joined to the parameter n_gram_range to enable grid-searching both at once.

• In feature_extraction.text.CountVectorizer, words that appear only in one document are now ignored by default. To reproduce the previous behavior, set min_df=1.

• Fixed API inconsistency: linear_model.SGDClassifier.predict_proba now returns 2d array when fit on two classes.

• Fixed API inconsistency: discriminant_analysis.QuadraticDiscriminantAnalysis.decision_function and discriminant_analysis.LinearDiscriminantAnalysis.decision_function now return 1d arrays when fit on two classes.

• Grid of alphas used for fitting linear_model.LassoCV and linear_model.ElasticNetCV is now stored in the attribute alphas_ rather than overriding the init parameter alphas.

• Linear models when alpha is estimated by cross-validation store the estimated value in the alpha_ attribute rather than just alpha or best_alpha.


• svm.sparse.SVC and other sparse SVM classes are now deprecated. The all classes in the Support Vector Machines module now automatically select the sparse or dense representation base on the input.

• All clustering algorithms now interpret the array X given to fit as input data, in particular cluster.SpectralClustering and cluster.AffinityPropagation which previously expected affinity matrices.

• For clustering algorithms that take the desired number of clusters as a parameter, this parameter is now called n_clusters.

People

• 267 Andreas Müller
• 94 Gilles Louppe
• 89 Gael Varoquaux
• 79 Peter Prettenhofer
• 60 Mathieu Blondel
• 57 Alexandre Gramfort
• 52 Vlad Niculae
• 45 Lars Buitinck
• 44 Nelle Varoquaux
• 37 Jaques Grobler
• 30 Alexis Mignon
1.8.16 Version 0.11

May 7, 2012

Changelog

Highlights

- Gradient boosted regression trees (Gradient Tree Boosting) for classification and regression by Peter Prettenhofer and Scott White.
- Simple dict-based feature loader with support for categorical variables (feature_extraction.DictVectorizer) by Lars Buitinck.
- Added Matthews correlation coefficient (metrics.matthews_corrcoef) and added macro and micro average options to metrics.precision_score, metrics.recall_score and metrics.f1_score by Satrajit Ghosh.
- Out of Bag Estimates of generalization error for Ensemble methods by Andreas Müller.
- Randomized sparse linear models for feature selection, by Alexandre Gramfort and Gael Varoquaux
- Label Propagation for semi-supervised learning, by Clay Woolam. Note the semi-supervised API is still work in progress, and may change.
- Added BIC/AIC model selection to classical Gaussian mixture models and unified the API with the remainder of scikit-learn, by Bertrand Thirion
- Added sklearn.cross_validation.StratifiedShuffleSplit, which is a sklearn.cross_validation.ShuffleSplit with balanced splits, by Yannick Schwartz.
- sklearn.neighbors.NearestCentroid classifier added, along with a shrink_threshold parameter, which implements shrunken centroid classification, by Robert Layton.

Other changes

- Merged dense and sparse implementations of Stochastic Gradient Descent module and exposed utility extension types for sequential datasets seq_dataset and weight vectors weight_vector by Peter Prettenhofer.
- Added partial_fit (support for online/minibatch learning) and warm_start to the Stochastic Gradient Descent module by Mathieu Blondel.
- Dense and sparse implementations of Support Vector Machines classes and linear_model.LogisticRegression merged by Lars Buitinck.
- Regressors can now be used as base estimator in the Multiclass and multilabel algorithms module by Mathieu Blondel.
- Added n_jobs option to metrics.pairwise.pairwise_distances and metrics.pairwise.pairwise_kernels for parallel computation, by Mathieu Blondel.
- K-means can now be run in parallel, using the n_jobs argument to either K-means or KMeans, by Robert Layton.
- Improved Cross-validation: evaluating estimator performance and Tuning the hyper-parameters of an estimator documentation and introduced the new cross_validation.train_test_split helper function by Olivier Grisel.
• `svm.SVC` members `coef_` and `intercept_` changed sign for consistency with `decision_function`; for `kernel=="linear", coef_` was fixed in the one-vs-one case, by Andreas Müller.

• Performance improvements to efficient leave-one-out cross-validated Ridge regression, esp. for the `n_samples > n_features` case, in `linear_model.RidgeCV`, by Reuben Fletcher-Costin.

• Refactoring and simplification of the `Text feature extraction` API and fixed a bug that caused possible negative IDF, by Olivier Grisel.

• Beam pruning option in `_BaseHMM` module has been removed since it is difficult to Cythonize. If you are interested in contributing a Cython version, you can use the python version in the git history as a reference.

• Classes in `Nearest Neighbors` now support arbitrary Minkowski metric for nearest neighbors searches. The metric can be specified by argument `p`.

**API changes summary**

• `covariance.EllipticEnvelop` is now deprecated - Please use `covariance.EllipticEnvelope` instead.

• `NeighborsClassifier` and `NeighborsRegressor` are gone in the module `Nearest Neighbors`. Use the classes `KNeighborsClassifier`, `RadiusNeighborsClassifier`, `KNeighborsRegressor` and/or `RadiusNeighborsRegressor` instead.

• Sparse classes in the `Stochastic Gradient Descent` module are now deprecated.

• In `mixture.GMM`, `mixture.DPGMM` and `mixture.VBGMM`, parameters must be passed to an object when initialising it and not through `fit`. Now `fit` will only accept the data as an input parameter.

• methods `rvs` and `decode` in GMM module are now deprecated. `sample` and `score` or `predict` should be used instead.

• attribute `_scores` and `_pvalues` in univariate feature selection objects are now deprecated. `scores_` or `pvalues_` should be used instead.

• In `LogisticRegression`, `LinearSVC`, `SVC` and `NuSVC`, the `class_weight` parameter is now an initialization parameter, not a parameter to fit. This makes grid searches over this parameter possible.

• LFW data is now always shape `(n_samples, n_features)` to be consistent with the Olivetti faces dataset. Use images and pairs attribute to access the natural images shapes instead.

• In `svm.LinearSVC`, the meaning of the `multi_class` parameter changed. Options now are 'ovr' and 'crammer_singer', with 'ovr' being the default. This does not change the default behavior but hopefully is less confusing.

• Class `feature_selection.text.Vectorizer` is deprecated and replaced by `feature_selection.text.TfidfVectorizer`.

• The preprocessor / analyzer nested structure for text feature extraction has been removed. All those features are now directly passed as flat constructor arguments to `feature_selection.text.TfidfVectorizer` and `feature_selection.text.CountVectorizer`, in particular the following parameters are now used:

  • `analyzer` can be 'word' or 'char' to switch the default analysis scheme, or use a specific python callable (as previously).

  • `tokenizer` and `preprocessor` have been introduced to make it still possible to customize those steps with the new API.

  • `input` explicitly control how to interpret the sequence passed to `fit` and `predict`: filenames, file objects or direct (byte or Unicode) strings.
• charset decoding is explicit and strict by default.
• the vocabulary, fitted or not is now stored in the vocabulary_ attribute to be consistent with the project conventions.
• Class feature_selection.text.TfidfVectorizer now derives directly from feature_selection.text.CountVectorizer to make grid search trivial.
• methods rvs in _BaseHMM module are now deprecated. sample should be used instead.
• Beam pruning option in _BaseHMM module is removed since it is difficult to be Cythonized. If you are interested, you can look in the history codes by git.
• The SVMlight format loader now supports files with both zero-based and one-based column indices, since both occur “in the wild”.
• Arguments in class ShuffleSplit are now consistent with StratifiedShuffleSplit. Arguments test_fraction and train_fraction are deprecated and renamed to test_size and train_size and can accept both float and int.
• Arguments in class Bootstrap are now consistent with StratifiedShuffleSplit. Arguments n_test and n_train are deprecated and renamed to test_size and train_size and can accept both float and int.
• Argument p added to classes in Nearest Neighbors to specify an arbitrary Minkowski metric for nearest neighbors searches.

People

• 282 Andreas Müller
• 239 Peter Prettenhofer
• 198 Gael Varoquaux
• 129 Olivier Grisel
• 114 Mathieu Blondel
• 103 Clay Woolam
• 96 Lars Buitinck
• 88 Jaques Grobler
• 82 Alexandre Gramfort
• 50 Bertrand Thirion
• 42 Robert Layton
• 28 flyingimmidev
• 26 Jake Vanderplas
• 26 Shiqiao Du
• 21 Satrajit Ghosh
• 17 David Marek
• 17 Gilles Louppe
• 14 Vlad Niculae
• 11 Yannick Schwartz

1.8. Previous Releases
1.8.17 Version 0.10

January 11, 2012
Changelog

• Python 2.5 compatibility was dropped; the minimum Python version needed to use scikit-learn is now 2.6.
• Sparse inverse covariance estimation using the graph Lasso, with associated cross-validated estimator, by Gael Varoquaux
• New Tree module by Brian Holt, Peter Prettenhofer, Satrajit Ghosh and Gilles Louppe. The module comes with complete documentation and examples.
• Fixed a bug in the RFE module by Gilles Louppe (issue #378).
• Fixed a memory leak in Support Vector Machines module by Brian Holt (issue #367).
• Faster tests by Fabian Pedregosa and others.
• Silhouette Coefficient cluster analysis evaluation metric added as sklearn.metrics.silhouette_score by Robert Layton.
• Fixed a bug in K-means in the handling of the n_init parameter: the clustering algorithm used to be run n_init times but the last solution was retained instead of the best solution by Olivier Grisel.
• Minor refactoring in Stochastic Gradient Descent module; consolidated dense and sparse predict methods; Enhanced test time performance by converting model parameters to fortran-style arrays after fitting (only multi-class).
• Adjusted Mutual Information metric added as sklearn.metrics.adjusted_mutual_info_score by Robert Layton.
• Models like SVC/SVR/LinearSVC/LogisticRegression from libsvm/liblinear now support scaling of C regularization parameter by the number of samples by Alexandre Gramfort.
• New Ensemble Methods module by Gilles Louppe and Brian Holt. The module comes with the random forest algorithm and the extra-trees method, along with documentation and examples.
• Novelty and Outlier Detection: outlier and novelty detection, by Virgile Fritsch.
• Kernel Approximation: a transform implementing kernel approximation for fast SGD on non-linear kernels by Andreas Müller.
• Fixed a bug due to atom swapping in Orthogonal Matching Pursuit (OMP) by Vlad Niculae.
• Sparse coding with a precomputed dictionary by Vlad Niculae.
• Mini Batch K-Means performance improvements by Olivier Grisel.
• K-means support for sparse matrices by Mathieu Blondel.
• Improved documentation for developers and for the sklearn.utils module, by Jake Vanderplas.
• Vectorized 20newsgroups dataset loader (sklearn.datasets.fetch_20newsgroups_vectorized) by Mathieu Blondel.
• Multiclass and multilabel algorithms by Lars Buitinck.
• Utilities for fast computation of mean and variance for sparse matrices by Mathieu Blondel.
• Make sklearn.preprocessing.scale and sklearn.preprocessing.Scaler work on sparse matrices by Olivier Grisel
• Feature importances using decision trees and/or forest of trees, by Gilles Louppe.
• Parallel implementation of forests of randomized trees by Gilles Louppe.
• sklearn.cross_validation.ShuffleSplit can subsample the train sets as well as the test sets by Olivier Grisel.
Errors in the build of the documentation fixed by Andreas Müller.

API changes summary

Here are the code migration instructions when upgrading from scikit-learn version 0.9:

- Some estimators that may overwrite their inputs to save memory previously had overwrite_ parameters; these have been replaced with copy_ parameters with exactly the opposite meaning. This particularly affects some of the estimators in linear_model. The default behavior is still to copy everything passed in.

- The SVMlight dataset loader sklearn.datasets.load_svmlight_file no longer supports loading two files at once; use load_svmlight_files instead. Also, the (unused) buffer_mb parameter is gone.

- Sparse estimators in the Stochastic Gradient Descent module use dense parameter vector coef_ instead of sparse_coef_. This significantly improves test time performance.

- The Covariance estimation module now has a robust estimator of covariance, the Minimum Covariance Determinant estimator.

- Cluster evaluation metrics in metrics.cluster have been refactored but the changes are backwards compatible. They have been moved to the metrics.cluster.supervised, along with metrics.cluster.unsupervised which contains the Silhouette Coefficient.

- The permutation_test_score function now behaves the same way as cross_val_score (i.e. uses the mean score across the folds.)

- Cross Validation generators now use integer indices (indices=True) by default instead of boolean masks. This make it more intuitive to use with sparse matrix data.

- The functions used for sparse coding, sparse_encode and sparse_encode_parallel have been combined into sklearn.decomposition.sparse_encode, and the shapes of the arrays have been transposed for consistency with the matrix factorization setting, as opposed to the regression setting.

- Fixed an off-by-one error in the SVMlight/LibSVM file format handling; files generated using sklearn.datasets.dump_svmlight_file should be re-generated. (They should continue to work, but accidentally had one extra column of zeros prepended.)

- BaseDictionaryLearning class replaced by SparseCodingMixin.

- sklearn.utils.extmath.fast_svd has been renamed sklearn.utils.extmath.randomized_svd and the default oversampling is now fixed to 10 additional random vectors instead of doubling the number of components to extract. The new behavior follows the reference paper.

People

The following people contributed to scikit-learn since last release:

- 246 Andreas Müller
- 242 Olivier Grisel
- 220 Gilles Louppe
- 183 Brian Holt
- 166 Gael Varoquaux
- 144 Lars Buitinck
- 73 Vlad Niculae
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1.8.18 Version 0.9

September 21, 2011

scikit-learn 0.9 was released on September 2011, three months after the 0.8 release and includes the new modules *Manifold learning*, *The Dirichlet Process* as well as several new algorithms and documentation improvements.

This release also includes the dictionary-learning work developed by Vlad Niculae as part of the Google Summer of Code program.
Changelog

- New **Manifold learning** module by Jake Vanderplas and Fabian Pedregosa.
- New **Dirichlet Process** Gaussian Mixture Model by Alexandre Passos
- **Nearest Neighbors** module refactoring by Jake Vanderplas: general refactoring, support for sparse matrices in input, speed and documentation improvements. See the next section for a full list of API changes.
- Improvements on the **Feature selection** module by Gilles Louppe: refactoring of the RFE classes, documentation rewrite, increased efficiency and minor API changes.
- **Sparse principal components analysis (SparsePCA and MiniBatchSparsePCA)** by Vlad Niculae, Gael Varoquaux and Alexandre Gramfort
- Printing an estimator now behaves independently of architectures and Python version thanks to Jean Kossaifi.
- **Loader for libsvm/svmlight format** by Mathieu Blondel and Lars Buitinck
- Documentation improvements: thumbnails in example gallery by Fabian Pedregosa.
- Important bugfixes in **Support Vector Machines** module (segfaults, bad performance) by Fabian Pedregosa.
- Added **Multinomial Naive Bayes** and **Bernoulli Naive Bayes** by Lars Buitinck
- Text feature extraction optimizations by Lars Buitinck
- Chi-Square feature selection (**feature_selection.univariate_selection.chi2**) by Lars Buitinck.
- **Sample generators** module refactoring by Gilles Louppe
- **Multiclass and multilabel algorithms** by Mathieu Blondel
- Ball tree rewrite by Jake Vanderplas

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• Implementation of DBSCAN algorithm by Robert Layton
• Kmeans predict and transform by Robert Layton
• Preprocessing module refactoring by Olivier Grisel
• Faster mean shift by Conrad Lee
• New Bootstrap, Random permutations cross-validation a.k.a. Shuffle & Split and various other improvements in cross validation schemes by Olivier Grisel and Gael Varoquaux
• Adjusted Rand index and V-Measure clustering evaluation metrics by Olivier Grisel
• Added Orthogonal Matching Pursuit by Vlad Niculae
• Added 2D-patch extractor utilities in the Feature extraction module by Vlad Niculae
• Implementation of linear_model.LassoLarsCV (cross-validated Lasso solver using the Lars algorithm) and linear_model.LassoLarsIC (BIC/AIC model selection in Lars) by Gael Varoquaux and Alexandre Gramfort
• Scalability improvements to metrics.roc_curve by Olivier Hervieu
• Distance helper functions metrics.pairwise.pairwise_distances and metrics.pairwise.pairwise_kernels by Robert Layton
• Mini-Batch K-Means by Nelle Varoquaux and Peter Prettenhofer.
• Downloading datasets from the mldata.org repository utilities by Pietro Berkes.
• The Olivetti faces dataset by David Warde-Farley.

API changes summary

Here are the code migration instructions when upgrading from scikit-learn version 0.8:

• The scikits.learn package was renamed sklearn. There is still a scikits.learn package alias for backward compatibility.

Third-party projects with a dependency on scikit-learn 0.9+ should upgrade their codebase. For instance, under Linux / MacOSX just run (make a backup first):

```
fine -name "*.py" | xargs sed -i 's/scikits.learn\b/sklearn/g'
```

• Estimators no longer accept model parameters as fit arguments: instead all parameters must be only be passed as constructor arguments or using the now public set_params method inherited from base.BaseEstimator.

Some estimators can still accept keyword arguments on the fit but this is restricted to data-dependent values (e.g. a Gram matrix or an affinity matrix that are precomputed from the X data matrix.

• The cross_val package has been renamed to cross_validation although there is also a cross_val package alias in place for backward compatibility.

Third-party projects with a dependency on scikit-learn 0.9+ should upgrade their codebase. For instance, under Linux / MacOSX just run (make a backup first):

```
fine -name "*.py" | xargs sed -i 's/cross_val\b/cross_validation/g'
```

• The score_func argument of the sklearn.cross_validation.cross_val_score function is now expected to accept y_test and y_predicted as only arguments for classification and regression tasks or X_test for unsupervised estimators.
• The `gamma` parameter for support vector machine algorithms is set to \( \frac{1}{n\_\text{features}} \) by default, instead of \( \frac{1}{n\_\text{samples}} \).

• The `sklearn.hmm` has been marked as orphaned: it will be removed from scikit-learn in version 0.11 unless someone steps up to contribute documentation, examples and fix lurking numerical stability issues.

• `sklearn.neighbors` has been made into a submodule. The two previously available estimators, `NeighborsClassifier` and `NeighborsRegressor` have been marked as deprecated. Their functionality has been divided among five new classes: `NearestNeighbors` for unsupervised neighbors searches, `KNeighborsClassifier` & `RadiusNeighborsClassifier` for supervised classification problems, and `KNeighborsRegressor` & `RadiusNeighborsRegressor` for supervised regression problems.

• `sklearn.ball_tree.BallTree` has been moved to `sklearn.neighbors.BallTree`. Using the former will generate a warning.

• `sklearn.linear_model.LARS()` and related classes (LassoLARS, LassoLARSCV, etc.) have been renamed to `sklearn.linear_model.Lars()`.

• All distance metrics and kernels in `sklearn.metrics.pairwise` now have a Y parameter, which by default is None. If not given, the result is the distance (or kernel similarity) between each sample in Y. If given, the result is the pairwise distance (or kernel similarity) between samples in X to Y.

• `sklearn.metrics.pairwise.l1_distance` is now called `manhattan_distance`, and by default returns the pairwise distance. For the component wise distance, set the parameter `sum_over_features` to `False`.

Backward compatibility package aliases and other deprecated classes and functions will be removed in version 0.11.

**People**

38 people contributed to this release.

• 387 Vlad Niculae
• 320 Olivier Grisel
• 192 Lars Buitinck
• 179 Gael Varoquaux
• 168 Fabian Pedregosa (INRIA, Parietal Team)
• 127 Jake Vanderplas
• 120 Mathieu Blondel
• 85 Alexandre Passos
• 67 Alexandre Gramfort
• 57 Peter Prettenhofer
• 56 Gilles Louppe
• 42 Robert Layton
• 38 Nelle Varoquaux
• 32 Jean Kossaifi
• 30 Conrad Lee
• 22 Pietro Berkes
• 18 andy
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• 17 David Warde-Farley
• 12 Brian Holt
• 11 Robert
• 8 Amit Aides
• 8 Virgile Fritsch
• 7 Yaroslav Halchenko
• 6 Salvatore Masecchia
• 5 Paolo Losi
• 4 Vincent Schut
• 3 Alexis Metaireau
• 3 Bryan Silverthorn
• 3 Andreas Müller
• 2 Minwoo Jake Lee
• 1 Emmanuelle Gouillart
• 1 Keith Goodman
• 1 Lucas Wiman
• 1 Nicolas Pinto
• 1 Thouis (Ray) Jones
• 1 Tim Sheerman-Chase

1.8.19 Version 0.8

May 11, 2011

scikit-learn 0.8 was released on May 2011, one month after the first “international” scikit-learn coding sprint and is marked by the inclusion of important modules: Hierarchical clustering, Cross decomposition, Non-negative matrix factorization (NMF or NNMF), initial support for Python 3 and by important enhancements and bug fixes.

Changelog

Several new modules where introduced during this release:

• New Hierarchical clustering module by Vincent Michel, Bertrand Thirion, Alexandre Gramfort and Gael Varoquaux.
• Kernel PCA implementation by Mathieu Blondel
• The Labeled Faces in the Wild face recognition dataset by Olivier Grisel.
• New Cross decomposition module by Edouard Duchesnay.
• Non-negative matrix factorization (NMF or NNMF) module Vlad Niculae
• Implementation of the Oracle Approximating Shrinkage algorithm by Virgile Fritsch in the Covariance estimation module.

Some other modules benefited from significant improvements or cleanups.
• Initial support for Python 3: builds and imports cleanly, some modules are usable while others have failing tests by Fabian Pedregosa.

• `decomposition.PCA` is now usable from the Pipeline object by Olivier Grisel.

• Guide *How to optimize for speed* by Olivier Grisel.

• Fixes for memory leaks in libsvm bindings, 64-bit safer BallTree by Lars Buitinck.

• bug and style fixing in *K-means* algorithm by Jan Schlüter.

• Add attribute converged to Gaussian Mixture Models by Vincent Schut.

• Implemented `transform`, `predict_log_proba` in `discriminant_analysis.LinearDiscriminantAnalysis` by Mathieu Blondel.

• Refactoring in the *Support Vector Machines* module and bug fixes by Fabian Pedregosa, Gael Varoquaux and Amit Aides.

• Refactored SGD module (removed code duplication, better variable naming), added interface for sample weight by Peter Prettenhofer.

• Wrapped BallTree with Cython by Thouis (Ray) Jones.

• Added function `svm.l1_min_c` by Paolo Losi.

• Typos, doc style, etc. by Yaroslav Halchenko, Gael Varoquaux, Olivier Grisel, Yann Malet, Nicolas Pinto, Lars Buitinck and Fabian Pedregosa.

People

People that made this release possible preceded by number of commits:

• 159 Olivier Grisel

• 96 Gael Varoquaux

• 96 Vlad Niculae

• 94 Fabian Pedregosa

• 36 Alexandre Gramfort

• 32 Paolo Losi

• 31 Edouard Duchesnay

• 30 Mathieu Blondel

• 25 Peter Prettenhofer

• 22 Nicolas Pinto

• **11 Virgile Fritsch**
  – 7 Lars Buitinck
  – 6 Vincent Michel
  – 5 Bertrand Thirion
  – 4 Thouis (Ray) Jones
  – 4 Vincent Schut
  – 3 Jan Schlüter
  – 2 Julien Miotte

1.8. Previous Releases
1.8.20 Version 0.7

March 2, 2011

scikit-learn 0.7 was released in March 2011, roughly three months after the 0.6 release. This release is marked by the speed improvements in existing algorithms like k-Nearest Neighbors and K-Means algorithm and by the inclusion of an efficient algorithm for computing the Ridge Generalized Cross Validation solution. Unlike the preceding release, no new modules where added to this release.

Changelog

• Performance improvements for Gaussian Mixture Model sampling [Jan Schlüter].

• Implementation of efficient leave-one-out cross-validated Ridge in `linear_model.RidgeCV` [Mathieu Blondel]

• Better handling of collinearity and early stopping in `linear_model.lars_path` [Alexandre Gramfort and Fabian Pedregosa].

• Fixes for liblinear ordering of labels and sign of coefficients [Dan Yamins, Paolo Losi, Mathieu Blondel and Fabian Pedregosa].

• Performance improvements for Nearest Neighbors algorithm in high-dimensional spaces [Fabian Pedregosa].

• Performance improvements for `cluster.KMeans` [Gael Varoquaux and James Bergstra].

• Sanity checks for SVM-based classes [Mathieu Blondel].

• Refactoring of `neighbors.NeighborsClassifier` and `neighbors.kneighbors_graph`: added different algorithms for the k-Nearest Neighbor Search and implemented a more stable algorithm for finding barycenter weights. Also added some developer documentation for this module, see `notes_neighbors` for more information [Fabian Pedregosa].

• Documentation improvements: Added `pca.RandomizedPCA` and `linear_model.LogisticRegression` to the class reference. Also added references of matrices used for clustering and other fixes [Gael Varoquaux, Fabian Pedregosa, Mathieu Blondel, Olivier Grisel, Virgile Fritsch, Emmanuelle Gouillart]

• Binded `decision_function` in classes that make use of `liblinear`, dense and sparse variants, like `svm.LinearSVC` or `linear_model.LogisticRegression` [Fabian Pedregosa].

• Performance and API improvements to `metrics.euclidean_distances` and to `pca.RandomizedPCA` [James Bergstra].

• Fix compilation issues under NetBSD [Kamel Ibn Hassen Derouiche]

• Allow input sequences of different lengths in `hmm.GaussianHMM` [Ron Weiss].
• Fix bug in affinity propagation caused by incorrect indexing [Xinfan Meng]

People

People that made this release possible preceded by number of commits:

• 85 Fabian Pedregosa
• 67 Mathieu Blondel
• 20 Alexandre Gramfort
• 19 James Bergstra
• 14 Dan Yamins
• 13 Olivier Grisel
• 12 Gael Varoquaux
• 4 Edouard Duchesnay
• 4 Ron Weiss
• 2 Satrajit Ghosh
• 2 Vincent Dubourg
• 1 Emmanuelle Gouillart
• 1 Kamel Ibn Hassen Derouiche
• 1 Paolo Losi
• 1 VirgileFritsch
• 1 Yaroslav Halchenko
• 1 Xinfan Meng

1.8.21 Version 0.6

December 21, 2010

scikit-learn 0.6 was released on December 2010. It is marked by the inclusion of several new modules and a general renaming of old ones. It is also marked by the inclusion of new example, including applications to real-world datasets.

Changelog

• New stochastic gradient descent module by Peter Prettenhofer. The module comes with complete documentation and examples.

• Improved svm module: memory consumption has been reduced by 50%, heuristic to automatically set class weights, possibility to assign weights to samples (see SVM: Weighted samples for an example).

• New Gaussian Processes module by Vincent Dubourg. This module also has great documentation and some very neat examples. See example_gaussian_process_plot_gp_regression.py or example_gaussian_process_plot_gp_probabilistic_classification_after_regression.py for a taste of what can be done.

• It is now possible to use liblinear's Multi-class SVC (option multi_class in svm.LinearSVC)

• New features and performance improvements of text feature extraction.

1.8. Previous Releases
• Improved sparse matrix support, both in main classes \texttt{(grid\_search.GridSearchCV)} as in modules \texttt{sklearn.svm.sparse} and \texttt{sklearn.linear\_model.sparse}.

• Lots of cool new examples and a new section that uses real-world datasets was created. These include: \textit{Faces recognition example using eigenfaces and SVMs}, \textit{Species distribution modeling}, \textit{Libsvm GUI}, \textit{Wikipedia principal eigenvector} and others.

• Faster \textit{Least Angle Regression} algorithm. It is now 2x faster than the R version on worst case and up to 10x times faster on some cases.

• Faster coordinate descent algorithm. In particular, the full path version of lasso (\texttt{linear\_model.lasso\_path}) is more than 200x times faster than before.

• It is now possible to get probability estimates from a \texttt{linear\_model.LogisticRegression} model.

• module renaming: the glm module has been renamed to linear\_model, the gmm module has been included into the more general mixture model and the sgd module has been included in linear\_model.

• Lots of bug fixes and documentation improvements.

People

People that made this release possible preceded by number of commits:

• 207 Olivier Grisel
• 167 Fabian Pedregosa
• 97 Peter Prettenhofer
• 68 Alexandre Gramfort
• 59 Mathieu Blondel
• 55 Gael Varoquaux
• 33 Vincent Dubourg
• 21 Ron Weiss
• 9 Bertrand Thirion
• 3 Alexandre Passos
• 3 Anne-Laure Fouque
• 2 Ronan Amicel
• 1 Christian Osendorfer

\textbf{1.8.22 Version 0.5}

October 11, 2010

Changelog

New classes

• Support for sparse matrices in some classifiers of modules \texttt{svm} and \texttt{linear\_model} (see \texttt{svm.sparse.SVC}, \texttt{svm.sparse.SVR}, \texttt{svm.sparse.LinearSVC}, \texttt{linear\_model.sparse.Lasso}, \texttt{linear\_model.sparse.ElasticNet})
• New `pipeline.Pipeline` object to compose different estimators.

• Recursive Feature Elimination routines in module `Feature selection`.

• Addition of various classes capable of cross validation in the linear_model module (`linear_model.LassoCV`, `linear_model.ElasticNetCV`, etc.).

• New, more efficient LARS algorithm implementation. The Lasso variant of the algorithm is also implemented. See `linear_model.lars_path`, `linear_model.Lars` and `linear_model.LassoLars`.

• New Hidden Markov Models module (see classes `hmm.GaussianHMM`, `hmm.MultinomialHMM`, etc.).

• New module `feature_extraction` (see class reference)

• New FastICA algorithm in module sklearn.fastica

Documentation

• Improved documentation for many modules, now separating narrative documentation from the class reference. As an example, see documentation for the SVM module and the complete class reference.

Fixes

• API changes: adhere variable names to PEP-8, give more meaningful names.

• Fixes for svm module to run on a shared memory context (multiprocessing).

• It is again possible to generate latex (and thus PDF) from the sphinx docs.

Examples

• new examples using some of the mlcomp datasets: sphx_glr_auto_examples_mlcomp_sparse_document_classification.py (since removed) and Classification of text documents using sparse features

• Many more examples. See here the full list of examples.

External dependencies

• Joblib is now a dependency of this package, although it is shipped with (sklearn.externals.joblib).

Removed modules

• Module ann (Artificial Neural Networks) has been removed from the distribution. Users wanting this sort of algorithms should take a look into pybrain.

Misc

• New sphinx theme for the web page.
Authors

The following is a list of authors for this release, preceded by number of commits:

- 262 Fabian Pedregosa
- 240 Gael Varoquaux
- 149 Alexandre Gramfort
- 116 Olivier Grisel
- 40 Vincent Michel
- 38 Ron Weiss
- 23 Matthieu Perrot
- 10 Bertrand Thirion
- 7 Yaroslav Halchenko
- 9 VirgileFritsch
- 6 Edouard Duchesnay
- 4 Mathieu Blondel
- 1 Ariel Rokem
- 1 Matthieu Brucher

1.8.23 Version 0.4

August 26, 2010

Changelog

Major changes in this release include:

- Coordinate Descent algorithm (Lasso, ElasticNet) refactoring & speed improvements (roughly 100x times faster).
- Coordinate Descent Refactoring (and bug fixing) for consistency with R’s package GLMNET.
- New metrics module.
- New GMM module contributed by Ron Weiss.
- Implementation of the LARS algorithm (without Lasso variant for now).
- feature_selection module redesign.
- Migration to GIT as version control system.
- Removal of obsolete attrselect module.
- Rename of private compiled extensions (added underscore).
- Removal of legacy unmaintained code.
- Documentation improvements (both docstring and rst).
- Improvement of the build system to (optionally) link with MKL. Also, provide a lite BLAS implementation in case no system-wide BLAS is found.
• Lots of new examples.
• Many, many bug fixes …

Authors

The committer list for this release is the following (preceded by number of commits):

• 143 Fabian Pedregosa
• 35 Alexandre Gramfort
• 34 Olivier Grisel
• 11 Gael Varoquaux
• 5 Yaroslav Halchenko
• 2 Vincent Michel
• 1 Chris Filo Gorgolewski

1.8.24 Earlier versions

Earlier versions included contributions by Fred Mailhot, David Cooke, David Huard, Dave Morrill, Ed Schofield, Travis Oliphant, Pearu Peterson.
2.1 An introduction to machine learning with scikit-learn

Section contents

In this section, we introduce the machine learning vocabulary that we use throughout scikit-learn and give a simple learning example.

2.1.1 Machine learning: the problem setting

In general, a learning problem considers a set of n samples of data and then tries to predict properties of unknown data. If each sample is more than a single number and, for instance, a multi-dimensional entry (aka multivariate data), it is said to have several attributes or features.

We can separate learning problems in a few large categories:

- **supervised learning**, in which the data comes with additional attributes that we want to predict (Click here to go to the scikit-learn supervised learning page). This problem can be either:
  
  - **classification**: samples belong to two or more classes and we want to learn from already labeled data how to predict the class of unlabeled data. An example of classification problem would be the handwritten digit recognition example, in which the aim is to assign each input vector to one of a finite number of discrete categories. Another way to think of classification is as a discrete (as opposed to continuous) form of supervised learning where one has a limited number of categories and for each of the n samples provided, one is to try to label them with the correct category or class.

  - **regression**: if the desired output consists of one or more continuous variables, then the task is called regression. An example of a regression problem would be the prediction of the length of a salmon as a function of its age and weight.

- **unsupervised learning**, in which the training data consists of a set of input vectors x without any corresponding target values. The goal in such problems may be to discover groups of similar examples within the data, where it is called clustering, or to determine the distribution of data within the input space, known as density estimation, or to project the data from a high-dimensional space down to two or three dimensions for the purpose of visualization (Click here to go to the Scikit-Learn unsupervised learning page).
Training set and testing set

Machine learning is about learning some properties of a data set and applying them to new data. This is why a common practice in machine learning to evaluate an algorithm is to split the data at hand into two sets, one that we call the training set on which we learn data properties and one that we call the testing set on which we test these properties.

2.1.2 Loading an example dataset

scikit-learn comes with a few standard datasets, for instance the iris and digits datasets for classification and the boston house prices dataset for regression.

In the following, we start a Python interpreter from our shell and then load the iris and digits datasets. Our notational convention is that $ denotes the shell prompt while >>> denotes the Python interpreter prompt:

```
$ python
>>> from sklearn import datasets
>>> iris = datasets.load_iris()
>>> digits = datasets.load_digits()
```

A dataset is a dictionary-like object that holds all the data and some metadata about the data. This data is stored in the .data member, which is a n_samples, n_features array. In the case of supervised problem, one or more response variables are stored in the .target member. More details on the different datasets can be found in the dedicated section.

For instance, in the case of the digits dataset, digits.data gives access to the features that can be used to classify the digits samples:

```
>>> print(digits.data)
[[ 0.  0.  5. ...,  0.  0.  0.]
 [ 0.  0.  0. ..., 10.  0.  0.]
 [ 0.  0.  0. ..., 16.  9.  0.]
 ...,
 [ 0.  0.  1. ...,  6.  0.  0.]
 [ 0.  0.  2. ..., 12.  0.  0.]
 [ 0.  0. 10. ..., 12.  1.  0.]]
```

and digits.target gives the ground truth for the digit dataset, that is the number corresponding to each digit image that we are trying to learn:

```
>>> digits.target
array([0, 1, 2, ..., 8, 9, 8])
```

Shape of the data arrays

The data is always a 2D array, shape (n_samples, n_features), although the original data may have had a different shape. In the case of the digits, each original sample is an image of shape (8, 8) and can be accessed using:

```
>>> digits.images[0]
```

```python
array([[ 0.,  0.,  5., ...,  0.,  0.,  0.],
 [ 0.,  0., 13., 15., 10., 15.,  5.,  0.],
 [ 0.,  3., 15.,  2.,  0., 11.,  8.,  0.],
 [ 0.,  4., 12.,  0.,  0.,  8.,  8.,  0.],
 [ 0.,  5.,  8.,  0.,  0.,  9.,  8.,  0.],
 [ 0.,  4., 11.,  0.,  1., 12.,  7.,  0.],
 [ 0.,  2., 14.,  5., 10., 12.,  0.,  0.],
 [ 0.,  0.,  6., 13., 10.,  0.,  0.,  0.]])
```
The simple example on this dataset illustrates how starting from the original problem one can shape the data for consumption in scikit-learn.

### Loading from external datasets

To load from an external dataset, please refer to loading external datasets.

---

#### 2.1.3 Learning and predicting

In the case of the digits dataset, the task is to predict, given an image, which digit it represents. We are given samples of each of the 10 possible classes (the digits zero through nine) on which we fit an estimator to be able to predict the classes to which unseen samples belong.

In scikit-learn, an estimator for classification is a Python object that implements the methods fit(X, y) and predict(T).

An example of an estimator is the class `sklearn.svm.SVC` that implements support vector classification. The constructor of an estimator takes as arguments the parameters of the model, but for the time being, we will consider the estimator as a black box:

```python
>>> from sklearn import svm

>>> clf = svm.SVC(gamma=0.001, C=100.)
```

### Choosing the parameters of the model

In this example we set the value of `gamma` manually. It is possible to automatically find good values for the parameters by using tools such as grid search and cross validation.

We call our estimator instance `clf`, as it is a classifier. It now must be fitted to the model, that is, it must learn from the model. This is done by passing our training set to the `fit` method. As a training set, let us use all the images of our dataset apart from the last one. We select this training set with the `[:-1]` Python syntax, which produces a new array that contains all but the last entry of `digits.data`:

```python
>>> clf.fit(digits.data[:-1], digits.target[:-1])
SVC(C=100.0, cache_size=200, class_weight=None, coef0=0.0,
   decision_function_shape='ovr', degree=3, gamma=0.001, kernel='rbf',
   max_iter=-1, probability=False, random_state=None, shrinking=True,
   tol=0.001, verbose=False)
```

Now you can predict new values, in particular, we can ask to the classifier what is the digit of our last image in the digits dataset, which we have not used to train the classifier:

```python
>>> clf.predict(digits.data[-1:])
array([8])
```
As you can see, it is a challenging task: the images are of poor resolution. Do you agree with the classifier?

A complete example of this classification problem is available as an example that you can run and study: Recognizing hand-written digits.

### 2.1.4 Model persistence

It is possible to save a model in the scikit by using Python’s built-in persistence model, namely pickle:

```python
>>> from sklearn import svm
>>> from sklearn import datasets
>>> clf = svm.SVC()
>>> iris = datasets.load_iris()
>>> X, y = iris.data, iris.target
>>> clf.fit(X, y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
    decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
    max_iter=-1, probability=False, random_state=None, shrinking=True,
    tol=0.001, verbose=False)
>>> import pickle
>>> s = pickle.dumps(clf)
>>> clf2 = pickle.loads(s)
>>> clf2.predict(X[0:1])
array([0])
>>> y[0]
0
```

In the specific case of the scikit, it may be more interesting to use joblib’s replacement of pickle (joblib.dump & joblib.load), which is more efficient on big data, but can only pickle to the disk and not to a string:

```python
>>> from sklearn.externals import joblib
>>> joblib.dump(clf, 'filename.pkl')
```

Later you can load back the pickled model (possibly in another Python process) with:

```python
>>> clf = joblib.load('filename.pkl')
```

**Note:** joblib.dump and joblib.load functions also accept file-like object instead of filenames. More information on data persistence with Joblib is available [here](#).

Note that pickle has some security and maintainability issues. Please refer to section Model persistence for more detailed information about model persistence with scikit-learn.
2.1.5 Conventions

scikit-learn estimators follow certain rules to make their behavior more predictive.

Type casting

Unless otherwise specified, input will be cast to float64:

```python
>>> import numpy as np
>>> from sklearn import random_projection

>>> rng = np.random.RandomState(0)
>>> X = rng.rand(10, 2000)
>>> X = np.array(X, dtype='float32')
>>> X.dtype
'dtype('float32')

>>> transformer = random_projection.GaussianRandomProjection()
>>> X_new = transformer.fit_transform(X)
>>> X_new.dtype
'dtype('float64')
```

In this example, X is float32, which is cast to float64 by fit_transform(X).

Regression targets are cast to float64, classification targets are maintained:

```python
>>> from sklearn import datasets
>>> from sklearn.svm import SVC

>>> iris = datasets.load_iris()
>>> clf = SVC()
>>> clf.fit(iris.data, iris.target)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
   decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
   max_iter=-1, probability=False, random_state=None, shrinking=True,
   tol=0.001, verbose=False)

>>> list(clf.predict(iris.data[:3]))
[0, 0, 0]

>>> clf.fit(iris.data, iris.target_names[iris.target])
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
   decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
   max_iter=-1, probability=False, random_state=None, shrinking=True,
   tol=0.001, verbose=False)

>>> list(clf.predict(iris.data[:3]))
['setosa', 'setosa', 'setosa']
```

Here, the first predict() returns an integer array, since iris.target (an integer array) was used in fit. The second predict() returns a string array, since iris.target_names was for fitting.

Refitting and updating parameters

Hyper-parameters of an estimator can be updated after it has been constructed via the sklearn.pipeline.Pipeline.set_params method. Calling fit() more than once will overwrite what was learned by any previous fit():

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Here, the default kernel rbf is first changed to linear after the estimator has been constructed via SVC(), and changed back to rbf to refit the estimator and to make a second prediction.

### Multiclass vs. multilabel fitting

When using multiclass classifiers, the learning and prediction task that is performed is dependent on the format of the target data fit upon:

```python
>>> from sklearn.svm import SVC
>>> from sklearn.multiclass import OneVsRestClassifier
>>> from sklearn.preprocessing import LabelBinarizer

>>> X = [[1, 2], [2, 4], [4, 5], [3, 2], [3, 1]]
>>> y = [0, 0, 1, 1, 2]

>>> classif = OneVsRestClassifier(estimator=SVC(random_state=0))
>>> classif.fit(X, y).predict(X)
array([0, 0, 1, 1, 2])
```

In the above case, the classifier is fit on a 1d array of multiclass labels and the predict() method therefore provides corresponding multiclass predictions. It is also possible to fit upon a 2d array of binary label indicators:

```python
>>> y = LabelBinarizer().fit_transform(y)
>>> classif.fit(X, y).predict(X)
array([[0, 0, 0],
       [0, 0, 0],
       [0, 0, 1],
       [0, 0, 0],
       [0, 0, 0]])
```

Here, the classifier is fit() on a 2d binary label representation of y, using the LabelBinarizer. In this case predict() returns a 2d array representing the corresponding multilabel predictions.
Note that the fourth and fifth instances returned all zeroes, indicating that they matched none of the three labels fit upon. With multilabel outputs, it is similarly possible for an instance to be assigned multiple labels:

```python
>> from sklearn.preprocessing import MultiLabelBinarizer
>> y = [[0, 1], [0, 2], [1, 3], [0, 2, 3], [2, 4]]
>> y = MultiLabelBinarizer().fit_transform(y)
>> classif.fit(X, y).predict(X)
array([[1, 1, 0, 0, 0],
       [1, 0, 1, 0, 0],
       [0, 1, 0, 1, 0],
       [1, 0, 1, 1, 0],
       [0, 0, 1, 0, 1]])
```

In this case, the classifier is fit upon instances each assigned multiple labels. The `MultiLabelBinarizer` is used to binarize the 2d array of multilabels to fit upon. As a result, `predict()` returns a 2d array with multiple predicted labels for each instance.

### 2.2 A tutorial on statistical-learning for scientific data processing

#### Statistical learning

Machine learning is a technique with a growing importance, as the size of the datasets experimental sciences are facing is rapidly growing. Problems it tackles range from building a prediction function linking different observations, to classifying observations, or learning the structure in an unlabeled dataset.

This tutorial will explore statistical learning, the use of machine learning techniques with the goal of statistical inference: drawing conclusions on the data at hand.

Scikit-learn is a Python module integrating classic machine learning algorithms in the tightly-knit world of scientific Python packages (NumPy, SciPy, matplotlib).

#### 2.2.1 Statistical learning: the setting and the estimator object in scikit-learn

#### Datasets

Scikit-learn deals with learning information from one or more datasets that are represented as 2D arrays. They can be understood as a list of multi-dimensional observations. We say that the first axis of these arrays is the samples axis, while the second is the features axis.

A simple example shipped with the scikit: iris dataset

```python
>>> from sklearn import datasets
>>> iris = datasets.load_iris()
>>> data = iris.data
>>> data.shape
(150, 4)
```

It is made of 150 observations of irises, each described by 4 features: their sepal and petal length and width, as detailed in `iris.DESCR`.

---

2.2. A tutorial on statistical-learning for scientific data processing 115
When the data is not initially in the \((n_{\text{samples}}, n_{\text{features}})\) shape, it needs to be preprocessed in order to be used by scikit-learn.

An example of reshaping data would be the digits dataset

```python
>>> digits = datasets.load_digits()
>>> digits.images.shape
(1797, 8, 8)
>>> import matplotlib.pyplot as plt
>>> plt.imshow(digits.images[-1], cmap=plt.cm.gray_r)
<matplotlib.image.AxesImage object at ...>
```

To use this dataset with the scikit, we transform each 8x8 image into a feature vector of length 64

```python
>>> data = digits.images.reshape((digits.images.shape[0], -1))
```

Estimators objects

**Fitting data**: the main API implemented by scikit-learn is that of the estimator. An estimator is any object that learns from data; it may be a classification, regression or clustering algorithm or a transformer that extracts/filters useful features from raw data.

All estimator objects expose a `fit` method that takes a dataset (usually a 2-d array):

```python
>>> estimator.fit(data)
```

**Estimator parameters**: All the parameters of an estimator can be set when it is instantiated or by modifying the corresponding attribute:

```python
>>> estimator = Estimator(param1=1, param2=2)
>>> estimator.param1
1
```

**Estimated parameters**: When data is fitted with an estimator, parameters are estimated from the data at hand. All the estimated parameters are attributes of the estimator object ending by an underscore:

```python
>>> estimator.estimated_param_
```
2.2.2 Supervised learning: predicting an output variable from high-dimensional observations

The problem solved in supervised learning

Supervised learning consists in learning the link between two datasets: the observed data \( X \) and an external variable \( y \) that we are trying to predict, usually called “target” or “labels”. Most often, \( y \) is a 1D array of length \( n_{\text{samples}} \).

All supervised estimators in scikit-learn implement a \texttt{fit(X, y)} method to fit the model and a \texttt{predict(X)} method that, given unlabeled observations \( X \), returns the predicted labels \( y \).

Vocabulary: classification and regression

If the prediction task is to classify the observations in a set of finite labels, in other words to “name” the objects observed, the task is said to be a classification task. On the other hand, if the goal is to predict a continuous target variable, it is said to be a regression task.

When doing classification in scikit-learn, \( y \) is a vector of integers or strings.

Note: See the Introduction to machine learning with scikit-learn Tutorial for a quick run-through on the basic machine learning vocabulary used within scikit-learn.

Nearest neighbor and the curse of dimensionality

Classifying irises:
The iris dataset is a classification task consisting in identifying 3 different types of irises (Setosa, Versicolour, and Virginica) from their petal and sepal length and width:

```python
>>> import numpy as np
>>> from sklearn import datasets
>>> iris = datasets.load_iris()
>>> iris_X = iris.data
>>> iris_y = iris.target
>>> np.unique(iris_y)
array([0, 1, 2])
```

### k-Nearest neighbors classifier

The simplest possible classifier is the nearest neighbor: given a new observation $X_{test}$, find in the training set (i.e. the data used to train the estimator) the observation with the closest feature vector. (Please see the Nearest Neighbors section of the online Scikit-learn documentation for more information about this type of classifier.)

### Training set and testing set

While experimenting with any learning algorithm, it is important not to test the prediction of an estimator on the data used to fit the estimator as this would not be evaluating the performance of the estimator on new data. This is why datasets are often split into train and test data.
KNN (k nearest neighbors) classification example:

```python
>>> # Split iris data in train and test data
>>> # A random permutation, to split the data randomly
>>> np.random.seed(0)
>>> indices = np.random.permutation(len(iris_X))
>>> iris_X_train = iris_X[indices[:-10]]
>>> iris_y_train = iris_y[indices[:-10]]
>>> iris_X_test = iris_X[indices[-10:]]
>>> iris_y_test = iris_y[indices[-10:]]
>>> # Create and fit a nearest-neighbor classifier
>>> from sklearn.neighbors import KNeighborsClassifier
>>> knn = KNeighborsClassifier()
>>> knn.fit(iris_X_train, iris_y_train)
KNeighborsClassifier(algorithm='auto', leaf_size=30, metric='minkowski',
                    metric_params=None, n_jobs=1, n_neighbors=5, p=2,
                    weights='uniform')
>>> knn.predict(iris_X_test)
array([1, 2, 1, 0, 0, 2, 1, 2, 0, 0])
>>> iris_y_test
array([1, 1, 1, 0, 0, 2, 1, 2, 0])
```

The curse of dimensionality

For an estimator to be effective, you need the distance between neighboring points to be less than some value $d$, which depends on the problem. In one dimension, this requires on average $n \sim 1/d$ points. In the context of the above $k$-NN example, if the data is described by just one feature with values ranging from 0 to 1 and with $n$ training observations, then new data will be no further away than $1/n$. Therefore, the nearest neighbor decision rule will be efficient as soon as $1/n$ is small compared to the scale of between-class feature variations.

If the number of features is $p$, you now require $n \sim 1/d^p$ points. Let’s say that we require 10 points in one dimension: now $10^p$ points are required in $p$ dimensions to pave the $[0, 1]$ space. As $p$ becomes large, the number of training points required for a good estimator grows exponentially.

For example, if each point is just a single number (8 bytes), then an effective $k$-NN estimator in a paltry $p \sim 20$ dimensions would require more training data than the current estimated size of the entire internet (±1000 Exabytes or
This is called the curse of dimensionality and is a core problem that machine learning addresses.

**Linear model: from regression to sparsity**

### Diabetes dataset

The diabetes dataset consists of 10 physiological variables (age, sex, weight, blood pressure) measure on 442 patients, and an indication of disease progression after one year:

```python
>>> diabetes = datasets.load_diabetes()
>>> diabetes_X_train = diabetes.data[:-20]
>>> diabetes_X_test = diabetes.data[-20:]
>>> diabetes_y_train = diabetes.target[:-20]
>>> diabetes_y_test = diabetes.target[-20:]
```

The task at hand is to predict disease progression from physiological variables.

### Linear regression

*LinearRegression*, in its simplest form, fits a linear model to the data set by adjusting a set of parameters in order to make the sum of the squared residuals of the model as small as possible.

\[
    y = X\beta + \epsilon
\]

- \(X\): data
- \(y\): target variable
- \(\beta\): Coefficients
- \(\epsilon\): Observation noise

```python
>>> from sklearn import linear_model
>>> regr = linear_model.LinearRegression()
>>> regr.fit(diabetes_X_train, diabetes_y_train)
LinearRegression(copy_X=True, fit_intercept=True, n_jobs=1, normalize=False)
>>> print(regr.coef_)
[ 0.30349955 -237.63931533 510.53060544 327.73698041 -814.13170937
  492.81458798 102.84845219 184.60648906 743.51961675 76.09517222]
```

```python
>>> # The mean square error
>>> np.mean((regr.predict(diabetes_X_test)-diabetes_y_test)**2)
2004.56760268...
```
Shrinkage

If there are few data points per dimension, noise in the observations induces high variance:

A solution in high-dimensional statistical learning is to shrink the regression coefficients to zero: any two randomly chosen set of observations are likely to be uncorrelated. This is called *Ridge* regression:
This is an example of **bias/variance tradeoff**: the larger the ridge alpha parameter, the higher the bias and the lower the variance.

We can choose alpha to minimize left out error, this time using the diabetes dataset rather than our synthetic data:

```python
>>> alphas = np.logspace(-4, -1, 6)
>>> from __future__ import print_function
>>> print([regr.set_params(alpha=alpha).fit(diabetes_X_train, diabetes_y_train,...
...     ).score(diabetes_X_test, diabetes_y_test) for alpha in alphas])
[0.5851110683883..., 0.5852073015444..., 0.5854677540698..., 0.5855512036503..., 0.
˓→5830717085554..., 0.57058999437...]
```

**Note:** Capturing in the fitted parameters noise that prevents the model to generalize to new data is called overfitting. The bias introduced by the ridge regression is called a **regularization**.

### Sparsity

Fitting only features 1 and 2
Note: A representation of the full diabetes dataset would involve 11 dimensions (10 feature dimensions and one of the target variable). It is hard to develop an intuition on such representation, but it may be useful to keep in mind that it would be a fairly empty space.

We can see that, although feature 2 has a strong coefficient on the full model, it conveys little information on \( y \) when considered with feature 1.

To improve the conditioning of the problem (i.e. mitigating the *The curse of dimensionality*), it would be interesting to select only the informative features and set non-informative ones, like feature 2 to 0. Ridge regression will decrease their contribution, but not set them to zero. Another penalization approach, called Lasso (least absolute shrinkage and selection operator), can set some coefficients to zero. Such methods are called sparse method and sparsity can be seen as an application of Occam’s razor: *prefer simpler models*.

```python
generate code here
```
Different algorithms for the same problem

Different algorithms can be used to solve the same mathematical problem. For instance the Lasso object in scikit-learn solves the lasso regression problem using a coordinate descent method, that is efficient on large datasets. However, scikit-learn also provides the LassoLars object using the LARS algorithm, which is very efficient for problems in which the weight vector estimated is very sparse (i.e. problems with very few observations).

Classification

For classification, as in the labeling iris task, linear regression is not the right approach as it will give too much weight to data far from the decision frontier. A linear approach is to fit a sigmoid function or logistic function:

\[ y = \text{sigmoid}(X\beta - \text{offset}) + \epsilon = \frac{1}{1 + \exp(-X\beta + \text{offset})} + \epsilon \]

```python
>>> logistic = linear_model.LogisticRegression(C=1e5)
>>> logistic.fit(iris_X_train, iris_y_train)
LogisticRegression(C=100000.0, class_weight=None, dual=False,
                   fit_intercept=True, intercept_scaling=1, max_iter=100,
                   multi_class='ovr', n_jobs=1, penalty='l2', random_state=None,
                   solver='liblinear', tol=0.0001, verbose=0, warm_start=False)
```

This is known as LogisticRegression.
Multiclass classification

If you have several classes to predict, an option often used is to fit one-versus-all classifiers and then use a voting heuristic for the final decision.

Shrinkage and sparsity with logistic regression

The $C$ parameter controls the amount of regularization in the `LogisticRegression` object: a large value for $C$ results in less regularization. `penalty="l2"` gives Shrinkage (i.e. non-sparse coefficients), while `penalty="l1"` gives Sparsity.

Exercise

Try classifying the digits dataset with nearest neighbors and a linear model. Leave out the last 10% and test prediction performance on these observations.

```python
from sklearn import datasets, neighbors, linear_model
digits = datasets.load_digits()
X_digits = digits.data
y_digits = digits.target
```

Solution: `../../auto_examples/exercises/plot_digits_classification_exercise.py`

Support vector machines (SVMs)

Linear SVMs

Support Vector Machines belong to the discriminant model family: they try to find a combination of samples to build a plane maximizing the margin between the two classes. Regularization is set by the $C$ parameter: a small value for $C$ means the margin is calculated using many or all of the observations around the separating line (more regularization); a large value for $C$ means the margin is calculated on observations close to the separating line (less regularization).
Example:

- Plot different SVM classifiers in the iris dataset

SVMs can be used in regression — SVR (Support Vector Regression) —, or in classification — SVC (Support Vector Classification).

```python
>>> from sklearn import svm
>>> svc = svm.SVC(kernel='linear')
>>> svc.fit(iris_X_train, iris_y_train)
```

SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
   decision_function_shape='ovr', degree=3, gamma='auto', kernel='linear',
   max_iter=-1, probability=False, random_state=None, shrinking=True,
   tol=0.001, verbose=False)

Warning: Normalizing data

For many estimators, including the SVMs, having datasets with unit standard deviation for each feature is important to get good prediction.

Using kernels

Classes are not always linearly separable in feature space. The solution is to build a decision function that is not linear but may be polynomial instead. This is done using the kernel trick that can be seen as creating a decision energy by positioning kernels on observations:

<table>
<thead>
<tr>
<th>Linear kernel</th>
<th>Polynomial kernel</th>
</tr>
</thead>
<tbody>
<tr>
<td><img src="image" alt="Linear kernel" /></td>
<td><img src="image" alt="Polynomial kernel" /></td>
</tr>
</tbody>
</table>

```python
>>> svc = svm.SVC(kernel='linear')
>>> svc = svm.SVC(kernel='poly',
...               degree=3)
>>> # degree: polynomial degree
```
RBF kernel (Radial Basis Function)

```python
>>> svc = svm.SVC(kernel='rbf')
>>> # gamma: inverse of size of
>>> # radial kernel
```

Interactive example

See the *SVM GUI* to download `svm_gui.py`; add data points of both classes with right and left button, fit the model and change parameters and data.
Exercise

Try classifying classes 1 and 2 from the iris dataset with SVMs, with the 2 first features. Leave out 10% of each class and test prediction performance on these observations.

Warning: the classes are ordered, do not leave out the last 10%, you would be testing on only one class.

Hint: You can use the \texttt{decision\_function} method on a grid to get intuitions.

```python
iris = datasets.load_iris()
X = iris.data
y = iris.target
X = X[y != 0, :2]
y = y[y != 0]
Solution: ../../auto_examples/exercises/plot_iris_exercise.py
```

2.2.3 Model selection: choosing estimators and their parameters

Score, and cross-validated scores

As we have seen, every estimator exposes a \texttt{score} method that can judge the quality of the fit (or the prediction) on new data. Bigger is better.

```python
>>> from sklearn import datasets, svm
>>> digits = datasets.load_digits()
>>> X_digits = digits.data
>>> y_digits = digits.target
>>> svc = svm.SVC(C=1, kernel='linear')
>>> svc.fit(X_digits[:-100], y_digits[:-100]).score(X_digits[-100:], y_digits[-100:]),
0.97999999999999998
```

To get a better measure of prediction accuracy (which we can use as a proxy for goodness of fit of the model), we can successively split the data in folds that we use for training and testing:

```python
>>> import numpy as np
>>> X_folds = np.array_split(X_digits, 3)
>>> y_folds = np.array_split(y_digits, 3)
>>> scores = list()
>>> for k in range(3):
...     # We use 'list' to copy, in order to 'pop' later on
...     X_train = list(X_folds)
...     X_test = X_train.pop(k)
...     X_train = np.concatenate(X_train)
...     y_train = list(y_folds)
...     y_test = y_train.pop(k)
...     y_train = np.concatenate(y_train)
...     scores.append(svc.fit(X_train, y_train).score(X_test, y_test))
>>> print(scores)
[0.93489148580968284, 0.95659432387312182, 0.93989983305509184]
```

This is called a \texttt{KFold} cross-validation.
Cross-validation generators

Scikit-learn has a collection of classes which can be used to generate lists of train/test indices for popular cross-validation strategies.

They expose a `split` method which accepts the input dataset to be split and yields the train/test set indices for each iteration of the chosen cross-validation strategy.

This example shows an example usage of the `split` method.

```python
>>> from sklearn.model_selection import KFold, cross_val_score
>>> X = ["a", "a", "b", "c", "c", "c"]
>>> k_fold = KFold(n_splits=3)
>>> for train_indices, test_indices in k_fold.split(X):
...     print('Train: %s | test: %s' % (train_indices, test_indices))
Train: [2 3 4 5] | test: [0 1]
Train: [0 1 4 5] | test: [2 3]
Train: [0 1 2 3] | test: [4 5]
```

The cross-validation can then be performed easily:

```python
>>> [svc.fit(X_digits[train], y_digits[train]).score(X_digits[test], y_digits[test])
...     for train, test in k_fold.split(X_digits)]
[0.93489148580968284, 0.95659432387312182, 0.93989983305509184]
```

The cross-validation score can be directly calculated using the `cross_val_score` helper. Given an estimator, the cross-validation object and the input dataset, the `cross_val_score` splits the data repeatedly into a training and a testing set, trains the estimator using the training set and computes the scores based on the testing set for each iteration of cross-validation.

By default the estimator's `score` method is used to compute the individual scores.

Refer the `metrics module` to learn more on the available scoring methods.

```python
>>> cross_val_score(svc, X_digits, y_digits, cv=k_fold, n_jobs=-1)
array([0.93489149, 0.95659432, 0.93989983])
```

`n_jobs=-1` means that the computation will be dispatched on all the CPUs of the computer.

Alternatively, the `scoring` argument can be provided to specify an alternative scoring method.

```python
>>> cross_val_score(svc, X_digits, y_digits, cv=k_fold,
...                 scoring='precision_macro')
array([0.93969761, 0.95911415, 0.94041254])
```

Cross-validation generators

- **KFold** *(n_splits, shuffle, random_state)*
  - Splits it into K folds, trains on K-1 and then tests on the left-out.
- **StratifiedKFold** *(n_splits, shuffle, random_state)*
  - Same as K-Fold but preserves the class distribution within each fold.
- **GroupKFold** *(n_splits)*
  - Ensures that the same group is not in both testing and training sets.

- **ShuffleSplit** *(n_splits, test_size, train_size, random_state)*
  - Generates train/test indices based on random permutation.
- **StratifiedShuffleSplit**
  - Same as shuffle split but preserves the class distribution within each iteration.
- **GroupShuffleSplit**
  - Ensures that the same group is not in both testing and training sets.
Exercise

On the digits dataset, plot the cross-validation score of a `SVC` estimator with a linear kernel as a function of parameter $C$ (use a logarithmic grid of points, from 1 to 10).

```python
import numpy as np
from sklearn.model_selection import cross_val_score
from sklearn import datasets, svm

digits = datasets.load_digits()
X = digits.data
y = digits.target

svc = svm.SVC(kernel='linear')
C_s = np.logspace(-10, 0, 10)
```

Solution: *Cross-validation on Digits Dataset Exercise*

Grid-search and cross-validated estimators

Grid-search

scikit-learn provides an object that, given data, computes the score during the fit of an estimator on a parameter grid and chooses the parameters to maximize the cross-validation score. This object takes an estimator during the construction and exposes an estimator API:

```python
>>> from sklearn.model_selection import GridSearchCV, cross_val_score
>>> Cs = np.logspace(-6, -1, 10)
```
By default, the `GridSearchCV` uses a 3-fold cross-validation. However, if it detects that a classifier is passed, rather than a regressor, it uses a stratified 3-fold.

### Nested cross-validation

```python
>>> cross_val_score(clf, X_digits, y_digits)
... array([ 0.938..., 0.963..., 0.944...])
```

Two cross-validation loops are performed in parallel: one by the `GridSearchCV` estimator to set gamma and the other one by `cross_val_score` to measure the prediction performance of the estimator. The resulting scores are unbiased estimates of the prediction score on new data.

**Warning:** You cannot nest objects with parallel computing (n_jobs different than 1).

### Cross-validated estimators

Cross-validation to set a parameter can be done more efficiently on an algorithm-by-algorithm basis. This is why, for certain estimators, scikit-learn exposes `Cross-validation: evaluating estimator performance` estimators that set their parameter automatically by cross-validation:

```python
>>> from sklearn import linear_model, datasets
>>> lasso = linear_model.LassoCV()
>>> diabetes = datasets.load_diabetes()
>>> X_diabetes = diabetes.data
>>> y_diabetes = diabetes.target
>>> lasso.fit(X_diabetes, y_diabetes)
LassoCV(alphas=None, copy_X=True, cv=None, eps=0.001, fit_intercept=True,
       max_iter=1000, n_alphas=100, n_jobs=1, normalize=False, positive=False,
       precompute='auto', random_state=None, selection='cyclic', tol=0.0001,
       verbose=False)
>>> # The estimator chose automatically its lambda:
>>> lasso.alpha_
0.01229...
```

These estimators are called similarly to their counterparts, with ‘CV’ appended to their name.
Exercise

On the diabetes dataset, find the optimal regularization parameter alpha.

**Bonus:** How much can you trust the selection of alpha?

```python
from sklearn import datasets
from sklearn.linear_model import LassoCV
from sklearn.linear_model import Lasso
from sklearn.model_selection import KFold
from sklearn.model_selection import GridSearchCV

diabetes = datasets.load_diabetes()
```

**Solution:** Cross-validation on diabetes Dataset Exercise

### 2.2.4 Unsupervised learning: seeking representations of the data

#### Clustering: grouping observations together

**The problem solved in clustering**

Given the iris dataset, if we knew that there were 3 types of iris, but did not have access to a taxonomist to label them: we could try a clustering task: split the observations into well-separated group called clusters.

#### K-means clustering

Note that there exist a lot of different clustering criteria and associated algorithms. The simplest clustering algorithm is K-means.

```python
>>> from sklearn import cluster, datasets
>>> iris = datasets.load_iris()
>>> X_iris = iris.data
>>> y_iris = iris.target

>>> k_means = cluster.KMeans(n_clusters=3)
>>> k_means.fit(X_iris)
KMeans(algorithm='auto', copy_x=True, init='k-means++', ...

>>> print(k_means.labels_[:10])
```

---

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Warning: There is absolutely no guarantee of recovering a ground truth. First, choosing the right number of clusters is hard. Second, the algorithm is sensitive to initialization, and can fall into local minima, although scikit-learn employs several tricks to mitigate this issue.

Application example: vector quantization

Clustering in general and KMeans, in particular, can be seen as a way of choosing a small number of exemplars to compress the information. The problem is sometimes known as vector quantization. For instance, this can be used to posterize an image:

```python
>>> import scipy as sp
>>> try:
...     face = sp.face(gray=True)
... except AttributeError:
...     from scipy import misc
...     face = misc.face(gray=True)

>>> X = face.reshape((-1, 1))  # We need an (n_sample, n_feature) array
>>> k_means = cluster.KMeans(n_clusters=5, n_init=1)
>>> k_means.fit(X)

>>> values = k_means.cluster_centers_.squeeze()
>>> labels = k_means.labels_
>>> face_compressed = np.choose(labels, values)
>>> face_compressed.shape = face.shape
```
Hierarchical agglomerative clustering: Ward

A Hierarchical clustering method is a type of cluster analysis that aims to build a hierarchy of clusters. In general, the various approaches of this technique are either:

- **Agglomerative** - bottom-up approaches: each observation starts in its own cluster, and clusters are iteratively merged in such a way to minimize a linkage criterion. This approach is particularly interesting when the clusters of interest are made of only a few observations. When the number of clusters is large, it is much more computationally efficient than k-means.

- **Divisive** - top-down approaches: all observations start in one cluster, which is iteratively split as one moves down the hierarchy. For estimating large numbers of clusters, this approach is both slow (due to all observations starting as one cluster, which it splits recursively) and statistically ill-posed.

Connectivity-constrained clustering

With agglomerative clustering, it is possible to specify which samples can be clustered together by giving a connectivity graph. Graphs in the scikit are represented by their adjacency matrix. Often, a sparse matrix is used. This can be useful, for instance, to retrieve connected regions (sometimes also referred to as connected components) when clustering an image:

```python
import matplotlib.pyplot as plt
from sklearn.feature_extraction.image import grid_to_graph
from sklearn.cluster import AgglomerativeClustering

# Generate data
try:
    # SciPy >= 0.16 have face in misc
    from scipy.misc import face
    face = face(gray=True)
except ImportError:
    face = sp.face(gray=True)

# Resize it to 10% of the original size to speed up the processing
face = sp.misc.imresize(face, 0.10) / 255.

X = np.reshape(face, (-1, 1))

# Define the structure A of the data. Pixels connected to their neighbors.
connectivity = grid_to_graph(*face.shape)
```
Feature agglomeration

We have seen that sparsity could be used to mitigate the curse of dimensionality, i.e. an insufficient amount of observations compared to the number of features. Another approach is to merge together similar features: feature agglomeration. This approach can be implemented by clustering in the feature direction, in other words clustering the transposed data.

```python
>>> digits = datasets.load_digits()
>>> images = digits.images
>>> X = np.reshape(images, (len(images), -1))
>>> connectivity = grid_to_graph(*images[0].shape)

>>> agglo = cluster.FeatureAgglomeration(connectivity=connectivity,
... n_clusters=32)

>>> agglo.fit(X)

>>> X_reduced = agglo.transform(X)

>>> X_approx = agglo.inverse_transform(X_reduced)

>>> images_approx = np.reshape(X_approx, images.shape)
```

transform and inverse_transform methods

Some estimators expose a `transform` method, for instance to reduce the dimensionality of the dataset.

Decompositions: from a signal to components and loadings

Components and loadings

If X is our multivariate data, then the problem that we are trying to solve is to rewrite it on a different observational basis: we want to learn loadings L and a set of components C such that $X = L \cdot C$. Different criteria exist to choose the components.
Principal component analysis: PCA

 Principal component analysis (PCA) selects the successive components that explain the maximum variance in the signal.

The point cloud spanned by the observations above is very flat in one direction: one of the three univariate features can almost be exactly computed using the other two. PCA finds the directions in which the data is not flat.

When used to transform data, PCA can reduce the dimensionality of the data by projecting on a principal subspace.

```python
>>> # Create a signal with only 2 useful dimensions
>>> x1 = np.random.normal(size=100)
>>> x2 = np.random.normal(size=100)
>>> x3 = x1 + x2
>>> X = np.c_[x1, x2, x3]

>>> from sklearn import decomposition
>>> pca = decomposition.PCA()
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=None, random_state=None, svd_solver='auto', tol=0.0, whiten=False)
>>> print(pca.explained_variance_)
[ 2.18565811e+00 1.19346747e+00 8.43026679e-32]

>>> # As we can see, only the 2 first components are useful
>>> pca.n_components = 2
>>> X_reduced = pca.fit_transform(X)
>>> X_reduced.shape
(100, 2)
```

Independent Component Analysis: ICA

 Independent component analysis (ICA) selects components so that the distribution of their loadings carries a maximum amount of independent information. It is able to recover non-Gaussian independent signals:
```python
# Generate sample data
import numpy as np
from scipy import signal

time = np.linspace(0, 10, 2000)
s1 = np.sin(2 * time)  # Signal 1: sinusoidal signal
s2 = np.sign(np.sin(3 * time))  # Signal 2: square signal
s3 = signal.sawtooth(2 * np.pi * time)  # Signal 3: saw tooth signal
S = np.c_[s1, s2, s3]
S += 0.2 * np.random.normal(size=S.shape)  # Add noise
S /= S.std(axis=0)  # Standardize data

# Mix data
A = np.array([[1, 1, 1], [0.5, 2, 1], [1.5, 1, 2]])  # Mixing matrix
X = np.dot(S, A.T)  # Generate observations

# Compute ICA
ica = decomposition.FastICA()
S_ = ica.fit_transform(X)  # Get the estimated sources
A_ = ica.mixing_.T
np.allclose(X, np.dot(S_, A_) + ica.mean_)
```

2.2. A tutorial on statistical-learning for scientific data processing
2.2.5 Putting it all together

Pipelining

We have seen that some estimators can transform data and that some estimators can predict variables. We can also create combined estimators:

```python
import numpy as np
import matplotlib.pyplot as plt

from sklearn import linear_model, decomposition, datasets
from sklearn.pipeline import Pipeline
from sklearn.model_selection import GridSearchCV

logistic = linear_model.LogisticRegression()
pca = decomposition.PCA()
pipe = Pipeline(steps=[('pca', pca), ('logistic', logistic)])
digits = datasets.load_digits()
X_digits = digits.data
y_digits = digits.target

# Plot the PCA spectrum
pca.fit(X_digits)
plt.figure(1, figsize=(4, 3))
plt.clf()
plt.axes([.2, .2, .7, .7])
plt.plot(pca.explained_variance_, linewidth=2)
plt.axis('tight')
plt.xlabel('n_components')
plt.ylabel('explained_variance_')

# Prediction
n_components = [20, 40, 64]
Cs = np.logspace(-4, 4, 3)
estimator = GridSearchCV(pipe,
                        dict(pca__n_components=n_components,
                             logistic__C=Cs))
estimator.fit(X_digits, y_digits)
plt.axvline(estimator.best_estimator_.named_steps['pca'].n_components,
            linestyle=':', label='n_components chosen')
```

![Plot of PCA spectrum](image)
Face recognition with eigenfaces

The dataset used in this example is a preprocessed excerpt of the “Labeled Faces in the Wild”, also known as LFW:


------
Faces recognition example using eigenfaces and SVMs

The dataset used in this example is a preprocessed excerpt of the "Labeled Faces in the Wild", aka LFW:


.. _LFW: http://vis-www.cs.umass.edu/lfw/

Expected results for the top 5 most represented people in the dataset:

+-----------------+-----------+-----------+-----------+-----+
| Precision        | Recall    | F1-score  | Support  |
| Ariel Sharon     | 0.67      | 0.92      | 0.77      | 13  |
| Colin Powell     | 0.75      | 0.78      | 0.76      | 60  |
| Donald Rumsfeld  | 0.78      | 0.67      | 0.72      | 27  |
| George W Bush    | 0.86      | 0.86      | 0.86      | 146 |
| Gerhard Schroeder| 0.76      | 0.76      | 0.76      | 25  |
| Hugo Chavez      | 0.67      | 0.67      | 0.67      | 15  |
| Tony Blair       | 0.81      | 0.69      | 0.75      | 36  |
| Avg / Total      | 0.80      | 0.80      | 0.80      | 322 |

------


from sklearn.decomposition import PCA
from sklearn.svm import SVC

print(__doc__)

# Display progress logs on stdout
logging.basicConfig(level=logging.INFO, format='%(asctime)s %(message)s')
# Download the data, if not already on disk and load it as numpy arrays

```python
lfw_people = fetch_lfw_people(min_faces_per_person=70, resize=0.4)
```

# Introspect the images arrays to find the shapes (for plotting)

```python
n_samples, h, w = lfw_people.images.shape
```

# For machine learning we use the 2 data directly (as relative pixel positions info is ignored by this model)

```python
X = lfw_people.data
n_features = X.shape[1]
```

# The label to predict is the id of the person

```python
y = lfw_people.target
target_names = lfw_people.target_names
n_classes = target_names.shape[0]
```

```python
print("Total dataset size:")
print("n_samples: %d" % n_samples)
print("n_features: %d" % n_features)
print("n_classes: %d" % n_classes)
```

# Split into a training set and a test set using a stratified k fold

```python
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.25, random_state=42)
```

# Compute a PCA (eigenfaces) on the face dataset (treated as unlabeled dataset): unsupervised feature extraction / dimensionality reduction

```python
n_components = 150
```

```python
print("Extracting the top %d eigenfaces from %d faces" % (n_components, X_train.shape[0]))
t0 = time()
pca = PCA(n_components=n_components, svd_solver='randomized', whiten=True).fit(X_train)
print("done in %0.3fs" % (time() - t0))
eigenfaces = pca.components_.reshape((n_components, h, w))
```

```python
print("Projecting the input data on the eigenfaces orthonormal basis")
t0 = time()
X_train_pca = pca.transform(X_train)
X_test_pca = pca.transform(X_test)
print("done in %0.3fs" % (time() - t0))
```

# Train a SVM classification model
Fitting the classifier to the training set

t0 = time()
param_grid = 

'gamma': [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.1],

clf = GridSearchCV(SVC(kernel='rbf', class_weight='balanced'), param_grid)
clf = clf.fit(X_train_pca, y_train)
print("done in %0.3fs" % (time() - t0))
print("Best estimator found by grid search:")
print(clf.best_estimator_)
Expected results for the top 5 most represented people in the dataset:

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>Gerhard_Schroeder</td>
<td>0.91</td>
<td>0.75</td>
<td>0.82</td>
<td>28</td>
</tr>
<tr>
<td>Donald_Rumsfeld</td>
<td>0.84</td>
<td>0.82</td>
<td>0.83</td>
<td>33</td>
</tr>
<tr>
<td>Tony_Blair</td>
<td>0.65</td>
<td>0.82</td>
<td>0.73</td>
<td>34</td>
</tr>
<tr>
<td>Colin_Powell</td>
<td>0.78</td>
<td>0.88</td>
<td>0.83</td>
<td>58</td>
</tr>
<tr>
<td>George_W_Bush</td>
<td>0.93</td>
<td>0.86</td>
<td>0.90</td>
<td>129</td>
</tr>
<tr>
<td>avg / total</td>
<td>0.86</td>
<td>0.84</td>
<td>0.85</td>
<td>282</td>
</tr>
</tbody>
</table>

Open problem: Stock Market Structure

Can we predict the variation in stock prices for Google over a given time frame?

Learning a graph structure

2.2.6 Finding help

The project mailing list

If you encounter a bug with scikit-learn or something that needs clarification in the docstring or the online documentation, please feel free to ask on the Mailing List

Q&A communities with Machine Learning practitioners

Quora.com Quora has a topic for Machine Learning related questions that also features some interesting discussions: https://www.quora.com/topic/Machine-Learning
The Stack Exchange family of sites hosts multiple subdomains for Machine Learning questions.

- _'An excellent free online course for Machine Learning taught by Professor Andrew Ng of Stanford': [https://www.coursera.org/learn/machine-learning](https://www.coursera.org/learn/machine-learning)
- _'Another excellent free online course that takes a more general approach to Artificial Intelligence': [https://www.udacity.com/course/intro-to-artificial-intelligence--cs271](https://www.udacity.com/course/intro-to-artificial-intelligence--cs271)

## 2.3 Working With Text Data

The goal of this guide is to explore some of the main scikit-learn tools on a single practical task: analysing a collection of text documents (newsgroups posts) on twenty different topics.

In this section we will see how to:

- load the file contents and the categories
- extract feature vectors suitable for machine learning
- train a linear model to perform categorization
- use a grid search strategy to find a good configuration of both the feature extraction components and the classifier

### 2.3.1 Tutorial setup

To get started with this tutorial, you firstly must have the scikit-learn and all of its required dependencies installed. Please refer to the installation instructions page for more information and for per-system instructions.

The source of this tutorial can be found within your scikit-learn folder:

```
scikit-learn/doc/tutorial/text_analytics/
```

The tutorial folder, should contain the following folders:

- *.rst files - the source of the tutorial document written with sphinx
- data - folder to put the datasets used during the tutorial
- skeletons - sample incomplete scripts for the exercises
- solutions - solutions of the exercises

You can already copy the skeletons into a new folder somewhere on your hard-drive named sklearn_tut_workspace where you will edit your own files for the exercises while keeping the original skeletons intact:

```
% cp -r skeletons work_directory/sklearn_tut_workspace
```

Machine Learning algorithms need data. Go to each $TUTORIAL_HOME/data sub-folder and run the fetch_data.py script from there (after having read them first).

For instance:

```
% cd $TUTORIAL_HOME/data/languages
% less fetch_data.py
% python fetch_data.py
```
2.3.2 Loading the 20 newsgroups dataset

The dataset is called “Twenty Newsgroups”. Here is the official description, quoted from the website:

The 20 Newsgroups data set is a collection of approximately 20,000 newsgroup documents, partitioned (nearly) evenly across 20 different newsgroups. To the best of our knowledge, it was originally collected by Ken Lang, probably for his paper “Newsweeder: Learning to filter netnews,” though he does not explicitly mention this collection. The 20 newsgroups collection has become a popular data set for experiments in text applications of machine learning techniques, such as text classification and text clustering.

In the following we will use the built-in dataset loader for 20 newsgroups from scikit-learn. Alternatively, it is possible to download the dataset manually from the web-site and use the `sklearn.datasets.load_files` function by pointing it to the `20news-bydate-train` subfolder of the uncompressed archive folder.

In order to get faster execution times for this first example we will work on a partial dataset with only 4 categories out of the 20 available in the dataset:

```python
>>> categories = ['alt.atheism', 'soc.religion.christian',
                 'comp.graphics', 'sci.med']
```

We can now load the list of files matching those categories as follows:

```python
>>> from sklearn.datasets import fetch_20newsgroups
>>> twenty_train = fetch_20newsgroups(subset='train',
                         categories=categories, shuffle=True, random_state=42)
```

The returned dataset is a scikit-learn “bunch”: a simple holder object with fields that can be both accessed as python dict keys or object attributes for convenience, for instance the `target_names` holds the list of the requested category names:

```python
>>> twenty_train.target_names
['alt.atheism', 'comp.graphics', 'sci.med', 'soc.religion.christian']
```

The files themselves are loaded in memory in the `data` attribute. For reference the filenames are also available:

```python
>>> len(twenty_train.data) 2257
>>> len(twenty_train.filenames) 2257
```

Let’s print the first lines of the first loaded file:

```python
>>> print("\n".join(twenty_train.data[0].split("\n")[:3]))
From: sd345@city.ac.uk (Michael Collier)
Subject: Converting images to HP LaserJet III?
Nntp-Posting-Host: hampton
```

```python
>>> print(twenty_train.target_names[twenty_train.target[0]])
com.graphics
```

Supervised learning algorithms will require a category label for each document in the training set. In this case the category is the name of the newsgroup which also happens to be the name of the folder holding the individual documents.

For speed and space efficiency reasons scikit-learn loads the target attribute as an array of integers that corresponds to the index of the category name in the `target_names` list. The category integer id of each sample is stored in the `target` attribute:
It is possible to get back the category names as follows:

```python
>>> for t in twenty_train.target[:10]:
    ...   print(twenty_train.target_names[t])
...  comp.graphics
  comp.graphics
  soc.religion.christian
  soc.religion.christian
  soc.religion.christian
  soc.religion.christian
  sci.med
  sci.med
  sci.med
```

You can notice that the samples have been shuffled randomly (with a fixed RNG seed): this is useful if you select only the first samples to quickly train a model and get a first idea of the results before re-training on the complete dataset later.

### 2.3.3 Extracting features from text files

In order to perform machine learning on text documents, we first need to turn the text content into numerical feature vectors.

#### Bags of words

The most intuitive way to do so is the bags of words representation:

1. assign a fixed integer id to each word occurring in any document of the training set (for instance by building a dictionary from words to integer indices).
2. for each document #i, count the number of occurrences of each word w and store it in $X[i, j]$ as the value of feature #j where $j$ is the index of word $w$ in the dictionary

The bags of words representation implies that $n\_features$ is the number of distinct words in the corpus: this number is typically larger than 100,000.

If $n\_samples == 10000$, storing $X$ as a numpy array of type float32 would require $10000 \times 100000 \times 4$ bytes = **4GB in RAM** which is barely manageable on today’s computers.

Fortunately, **most values in X will be zeros** since for a given document less than a couple thousands of distinct words will be used. For this reason we say that bags of words are typically **high-dimensional sparse datasets**. We can save a lot of memory by only storing the non-zero parts of the feature vectors in memory.

**scipy.sparse** matrices are data structures that do exactly this, and **scikit-learn** has built-in support for these structures.

#### Tokenizing text with scikit-learn

Text preprocessing, tokenizing and filtering of stopwords are included in a high level component that is able to build a dictionary of features and transform documents to feature vectors:
CountVectorizer supports counts of N-grams of words or consecutive characters. Once fitted, the vectorizer has built a dictionary of feature indices:

```python
>>> count_vect.vocabulary_.get(u'algorithm')
4690
```

The index value of a word in the vocabulary is linked to its frequency in the whole training corpus.

**From occurrences to frequencies**

Occurrence count is a good start but there is an issue: longer documents will have higher average count values than shorter documents, even though they might talk about the same topics.

To avoid these potential discrepancies it suffices to divide the number of occurrences of each word in a document by the total number of words in the document: these new features are called \( tf \) for Term Frequencies.

Another refinement on top of \( tf \) is to downscale weights for words that occur in many documents in the corpus and are therefore less informative than those that occur only in a smaller portion of the corpus.

This downsizing is called \( tf–idf \) for “Term Frequency times Inverse Document Frequency”.

Both \( tf \) and \( tf–idf \) can be computed as follows:

```python
>>> from sklearn.feature_extraction.text import TfidfTransformer
>>> tf_transformer = TfidfTransformer(use_idf=False).fit(X_train_counts)
>>> X_train_tf = tf_transformer.transform(X_train_counts)
>>> X_train_tf.shape
(2257, 35788)
```

In the above example-code, we firstly use the \texttt{fit}(...) method to fit our estimator to the data and secondly the \texttt{transform}(...) method to transform our count-matrix to a \texttt{tf-idf} representation. These two steps can be combined to achieve the same end result faster by skipping redundant processing. This is done through using the \texttt{fit_transform}(...) method as shown below, and as mentioned in the note in the previous section:

```python
>>> tfidf_transformer = TfidfTransformer()
>>> X_train_tfidf = tfidf_transformer.fit_transform(X_train_counts)
>>> X_train_tfidf.shape
(2257, 35788)
```

### 2.3.4 Training a classifier

Now that we have our features, we can train a classifier to try to predict the category of a post. Let’s start with a \textit{naïve} Bayes classifier, which provides a nice baseline for this task. \texttt{scikit-learn} includes several variants of this classifier; the one most suitable for word counts is the multinomial variant:

```python
>>> from sklearn.naive_bayes import MultinomialNB
>>> clf = MultinomialNB().fit(X_train_tfidf, twenty_train.target)
```
To try to predict the outcome on a new document we need to extract the features using almost the same feature extracting chain as before. The difference is that we call `transform` instead of `fit_transform` on the transformers, since they have already been fit to the training set:

```python
>>> docs_new = ['God is love', 'OpenGL on the GPU is fast']
>>> X_new_counts = count_vect.transform(docs_new)
>>> X_new_tfidf = tfidf_transformer.transform(X_new_counts)

>>> predicted = clf.predict(X_new_tfidf)
>>> for doc, category in zip(docs_new, predicted):
...     print(' %r => %s' % (doc, twenty_train.target_names[category]))
...     ...

'God is love' => soc.religion.christian
'OpenGL on the GPU is fast' => comp.graphics
```

### 2.3.5 Building a pipeline

In order to make the vectorizer => transformer => classifier easier to work with, scikit-learn provides a `Pipeline` class that behaves like a compound classifier:

```python
>>> from sklearn.pipeline import Pipeline

>>> text_clf = Pipeline([('vect', CountVectorizer()),
... ('tfidf', TfidfTransformer()),
... ('clf', MultinomialNB()),
... ])
```

The names `vect`, `tfidf` and `clf` (classifier) are arbitrary. We shall see their use in the section on grid search, below.

We can now train the model with a single command:

```python
>>> text_clf.fit(twenty_train.data, twenty_train.target)
```

### 2.3.6 Evaluation of the performance on the test set

Evaluating the predictive accuracy of the model is equally easy:

```python
>>> import numpy as np

>>> twenty_test = fetch_20newsgroups(subset='test',
...     categories=categories, shuffle=True, random_state=42)

>>> docs_test = twenty_test.data
>>> predicted = text_clf.predict(docs_test)
>>> np.mean(predicted == twenty_test.target)

0.834...
```

I.e., we achieved 83.4% accuracy. Let’s see if we can do better with a linear support vector machine (SVM), which is widely regarded as one of the best text classification algorithms (although it’s also a bit slower than naïve Bayes). We can change the learner by just plugging a different classifier object into our pipeline:

```python
>>> from sklearn.linear_model import SGDClassifier

>>> text_clf = Pipeline([('vect', CountVectorizer()),
... ('tfidf', TfidfTransformer()),
... ('clf', SGDClassifier(loss='hinge', penalty='l2',
...                        alpha=1e-3, random_state=42,
...                        max_iter=5, tol=None)),
... ])
```
```python
>>> text_clf.fit(twenty_train.data, twenty_train.target)
Pipeline(...)
>>> predicted = text_clf.predict(docs_test)
>>> np.mean(predicted == twenty_test.target)
0.912...
```

scikit-learn further provides utilities for more detailed performance analysis of the results:

```python
>>> from sklearn import metrics

>>> print(metrics.classification_report(twenty_test.target, predicted, ...
... target_names=twenty_test.target_names))

precision    recall    f1-score   support

alt.atheism   0.95      0.81      0.87      319
comp.graphics 0.88      0.97      0.92      389
sci.med       0.94      0.90      0.92      396
soc.religion.christian 0.90      0.95      0.93      398
avg / total  0.92      0.91      0.91      1502
```

```python
>>> metrics.confusion_matrix(twenty_test.target, predicted)
array([[258, 11, 15, 35],
       [ 4, 379, 3,  3],
       [ 5,  33, 355, 3],
       [ 5, 10,  4, 379]])
```

As expected the confusion matrix shows that posts from the newsgroups on atheism and christian are more often confused for one another than with computer graphics.

### 2.3.7 Parameter tuning using grid search

We’ve already encountered some parameters such as `use_idf` in the TfidfTransformer. Classifiers tend to have many parameters as well; e.g., MultinomialNB includes a smoothing parameter `alpha` and SGDClassifier has a penalty parameter `alpha` and configurable loss and penalty terms in the objective function (see the module documentation, or use the Python `help` function, to get a description of these).

Instead of tweaking the parameters of the various components of the chain, it is possible to run an exhaustive search of the best parameters on a grid of possible values. We try out all classifiers on either words or bigrams, with or without idf, and with a penalty parameter of either 0.01 or 0.001 for the linear SVM:

```python
>>> from sklearn.model_selection import GridSearchCV
>>> parameters = {'vect__ngram_range': [(1, 1), (1, 2)],
...                'tfidf__use_idf': (True, False),
...                'clf__alpha': [1e-2, 1e-3],
...                }
```

Obviously, such an exhaustive search can be expensive. If we have multiple CPU cores at our disposal, we can tell the grid searcher to try these eight parameter combinations in parallel with the `n_jobs` parameter. If we give this parameter a value of -1, grid search will detect how many cores are installed and uses them all:

```python
>>> gs_clf = GridSearchCV(text_clf, parameters, n_jobs=-1)
```
The grid search instance behaves like a normal scikit-learn model. Let’s perform the search on a smaller subset of the training data to speed up the computation:

```python
>>> gs_clf = gs_clf.fit(twenty_train.data[:400], twenty_train.target[:400])
```

The result of calling `fit` on a GridSearchCV object is a classifier that we can use to predict:

```python
>>> twenty_train.target_names[gs_clf.predict(['God is love'])[0]]
'soc.religion.christian'
```

The object’s `best_score_` and `best_params_` attributes store the best mean score and the parameters setting corresponding to that score:

```python
>>> gs_clf.best_score_
0.900...
>>> for param_name in sorted(parameters.keys()):
...     print("$s: $r" % (param_name, gs_clf.best_params_[param_name]))
...     clf__alpha: 0.001
tfidf__use_idf: True
vect__ngram_range: (1, 1)
```

A more detailed summary of the search is available at `gs_clf.cv_results_`. The `cv_results_` parameter can be easily imported into pandas as a DataFrame for further inspection.

**Exercises**

To do the exercises, copy the content of the ‘skeletons’ folder as a new folder named ‘workspace’:

```
% cp -r skeletons workspace
```

You can then edit the content of the workspace without fear of losing the original exercise instructions.

Then fire an ipython shell and run the work-in-progress script with:

```
[1] %run workspace/exercise_XX_script.py arg1 arg2 arg3
```

If an exception is triggered, use `%debug` to fire-up a post mortem ipdb session.

Refine the implementation and iterate until the exercise is solved.

For each exercise, the skeleton file provides all the necessary import statements, boilerplate code to load the data and sample code to evaluate the predictive accuracy of the model.

### 2.3.8 Exercise 1: Language identification

- Write a text classification pipeline using a custom preprocessor and CharNGramAnalyzer using data from Wikipedia articles as training set.
- Evaluate the performance on some held out test set.

ipython command line:

```
%run workspace/exercise_01_language_train_model.py data/languages/paragraphs/
```
2.3.9 Exercise 2: Sentiment Analysis on movie reviews

- Write a text classification pipeline to classify movie reviews as either positive or negative.
- Find a good set of parameters using grid search.
- Evaluate the performance on a held out test set.

ipython command line:

```
%run workspace/exercise_02_sentiment.py data/movie_reviews/txt_sentoken/
```

2.3.10 Exercise 3: CLI text classification utility

Using the results of the previous exercises and the `cPickle` module of the standard library, write a command line utility that detects the language of some text provided on `stdin` and estimate the polarity (positive or negative) if the text is written in English.

Bonus point if the utility is able to give a confidence level for its predictions.

2.3.11 Where to from here

Here are a few suggestions to help further your scikit-learn intuition upon the completion of this tutorial:

- Try playing around with the analyzer and token normalisation under `CountVectorizer`.
- If you don’t have labels, try using `Clustering` on your problem.
- If you have multiple labels per document, e.g. categories, have a look at the `Multiclass and multilabel section`.
- Try using `Truncated SVD` for latent semantic analysis.
- Have a look at using `Out-of-core Classification` to learn from data that would not fit into the computer main memory.
- Have a look at the `Hashing Vectorizer` as a memory efficient alternative to `CountVectorizer`.

2.4 Choosing the right estimator

Often the hardest part of solving a machine learning problem can be finding the right estimator for the job.

Different estimators are better suited for different types of data and different problems.

The flowchart below is designed to give users a bit of a rough guide on how to approach problems with regard to which estimators to try on your data.

Click on any estimator in the chart below to see its documentation.

2.5 External Resources, Videos and Talks

For written tutorials, see the `Tutorial section` of the documentation.
2.5.1 New to Scientific Python?

For those that are still new to the scientific Python ecosystem, we highly recommend the Python Scientific Lecture Notes. This will help you find your footing a bit and will definitely improve your scikit-learn experience. A basic understanding of NumPy arrays is recommended to make the most of scikit-learn.

2.5.2 External Tutorials

There are several online tutorials available which are geared toward specific subject areas:

- Machine Learning for NeuroImaging in Python
- Machine Learning for Astronomical Data Analysis

2.5.3 Videos

- An introduction to scikit-learn Part I and Part II at Scipy 2013 by Gael Varoquaux, Jake Vanderplas and Olivier Grisel. Notebooks on github.
- Introduction to scikit-learn by Gael Varoquaux at ICML 2010
  A three minute video from a very early stage of the scikit, explaining the basic idea and approach we are following.
- Introduction to statistical learning with scikit-learn by Gael Varoquaux at SciPy 2011
  An extensive tutorial, consisting of four sessions of one hour. The tutorial covers the basics of machine learning, many algorithms and how to apply them using scikit-learn. The material corresponding is now in the scikit-learn documentation section A tutorial on statistical-learning for scientific data processing.
- Statistical Learning for Text Classification with scikit-learn and NLTK (and slides) by Olivier Grisel at PyCon 2011
  Thirty minute introduction to text classification. Explains how to use NLTK and scikit-learn to solve real-world text classification tasks and compares against cloud-based solutions.
- Introduction to Interactive Predictive Analytics in Python with scikit-learn by Olivier Grisel at PyCon 2012
  3-hours long introduction to prediction tasks using scikit-learn.
- scikit-learn - Machine Learning in Python by Jake Vanderplas at the 2012 PyData workshop at Google
  Interactive demonstration of some scikit-learn features. 75 minutes.
- scikit-learn tutorial by Jake Vanderplas at PyData NYC 2012
  Presentation using the online tutorial, 45 minutes.

Note: Doctest Mode

The code-examples in the above tutorials are written in a python-console format. If you wish to easily execute these examples in IPython, use:
in the IPython-console. You can then simply copy and paste the examples directly into IPython without having to worry about removing the >>> manually.
3.1 Supervised learning

3.1.1 Generalized Linear Models

The following are a set of methods intended for regression in which the target value is expected to be a linear combination of the input variables. In mathematical notion, if \( \hat{y} \) is the predicted value.

\[
\hat{y}(w, x) = w_0 + w_1 x_1 + ... + w_p x_p
\]

Across the module, we designate the vector \( w = (w_1, ..., w_p) \) as \texttt{coef\_} and \( w_0 \) as \texttt{intercept\_}.

To perform classification with generalized linear models, see \textit{Logistic regression}.

**Ordinary Least Squares**

\texttt{LinearRegression} fits a linear model with coefficients \( w = (w_1, ..., w_p) \) to minimize the residual sum of squares between the observed responses in the dataset, and the responses predicted by the linear approximation. Mathematically it solves a problem of the form:

\[
\min_w \|Xw - y\|^2_2
\]

\texttt{LinearRegression} will take in its \texttt{fit} method arrays \( X, y \) and will store the coefficients \( w \) of the linear model in its \texttt{coef\_} member:
However, coefficient estimates for Ordinary Least Squares rely on the independence of the model terms. When terms are correlated and the columns of the design matrix $X$ have an approximate linear dependence, the design matrix becomes close to singular and as a result, the least-squares estimate becomes highly sensitive to random errors in the observed response, producing a large variance. This situation of multicollinearity can arise, for example, when data are collected without an experimental design.

Examples:
- Linear Regression Example

**Ordinary Least Squares Complexity**

This method computes the least squares solution using a singular value decomposition of X. If X is a matrix of size (n, p) this method has a cost of $O(np^2)$, assuming that $n \geq p$.

**Ridge Regression**

*Ridge* regression addresses some of the problems of *Ordinary Least Squares* by imposing a penalty on the size of coefficients. The ridge coefficients minimize a penalized residual sum of squares,

$$
\min_w \|Xw - y\|^2 + \alpha \|w\|^2
$$

Here, $\alpha \geq 0$ is a complexity parameter that controls the amount of shrinkage: the larger the value of $\alpha$, the greater the amount of shrinkage and thus the coefficients become more robust to collinearity.

As with other linear models, *Ridge* will take in its `fit` method arrays X, y and will store the coefficients $w$ of the linear model in its `coef_` member.
from sklearn import linear_model
reg = linear_model.Ridge(alpha = .5)
reg.fit ([[0, 0], [0, 0], [1, 1]], [0, .1, 1])

Ridge(alpha=0.5, copy_X=True, fit_intercept=True, max_iter=None,
      normalize=False, random_state=None, solver='auto', tol=0.001)

reg.coef_
array([ 0.34545455, 0.34545455])

reg.intercept_
0.13636...

Examples:

- Plot Ridge coefficients as a function of the regularization
- Classification of text documents using sparse features

Ridge Complexity

This method has the same order of complexity than an Ordinary Least Squares.

Setting the regularization parameter: generalized Cross-Validation

RidgeCV implements ridge regression with built-in cross-validation of the alpha parameter. The object works in the same way as GridSearchCV except that it defaults to Generalized Cross-Validation (GCV), an efficient form of leave-one-out cross-validation:

from sklearn import linear_model
reg = linear_model.RidgeCV(alphas=[0.1, 1.0, 10.0])
reg.fit ([[0, 0], [0, 0], [1, 1]], [0, .1, 1])

RidgeCV(alphas=[0.1, 1.0, 10.0], cv=None, fit_intercept=True, scoring=None,
        normalize=False)

reg.alpha_
0.1

References

- “Notes on Regularized Least Squares”, Rifkin & Lippert (technical report, course slides).

Lasso

The Lasso is a linear model that estimates sparse coefficients. It is useful in some contexts due to its tendency to prefer solutions with fewer parameter values, effectively reducing the number of variables upon which the given solution is dependent. For this reason, the Lasso and its variants are fundamental to the field of compressed sensing. Under certain conditions, it can recover the exact set of non-zero weights (see Compressive sensing: tomography reconstruction with L1 prior (Lasso)).

Mathematically, it consists of a linear model trained with $\ell_1$ prior as regularizer. The objective function to minimize
The lasso estimate thus solves the minimization of the least-squares penalty with $\alpha \|w\|_1$ added, where $\alpha$ is a constant and $\|w\|_1$ is the $\ell_1$-norm of the parameter vector.

The implementation in the class `Lasso` uses coordinate descent as the algorithm to fit the coefficients. See `Least Angle Regression` for another implementation:

```python
>>> from sklearn import linear_model
>>> reg = linear_model.Lasso(alpha = 0.1)
>>> reg.fit([[0, 0], [1, 1]], [0, 1])
Lasso(alpha=0.1, copy_X=True, fit_intercept=True, max_iter=1000,
     normalize=False, positive=False, precompute=False, random_state=None,
     selection='cyclic', tol=0.0001, warm_start=False)
>>> reg.predict([[1, 1]])
array([ 0.8])
```

Also useful for lower-level tasks is the function `lasso_path` that computes the coefficients along the full path of possible values.

**Examples:**

- [Lasso and Elastic Net for Sparse Signals](#)
- [Compressive sensing: tomography reconstruction with L1 prior (Lasso)](#)

**Note: Feature selection with Lasso**

As the Lasso regression yields sparse models, it can thus be used to perform feature selection, as detailed in [L1-based feature selection](#).

**Setting regularization parameter**

The alpha parameter controls the degree of sparsity of the coefficients estimated.

**Using cross-validation**

scikit-learn exposes objects that set the Lasso alpha parameter by cross-validation: `LassoCV` and `LassoLarsCV`. `LassoLarsCV` is based on the `Least Angle Regression` algorithm explained below.

For high-dimensional datasets with many collinear regressors, `LassoCV` is most often preferable. However, `LassoLarsCV` has the advantage of exploring more relevant values of alpha parameter, and if the number of samples is very small compared to the number of features, it is often faster than `LassoCV`. 
Information-criteria based model selection

Alternatively, the estimator LassoLarsIC proposes to use the Akaike information criterion (AIC) and the Bayes Information criterion (BIC). It is a computationally cheaper alternative to find the optimal value of alpha as the regularization path is computed only once instead of k+1 times when using k-fold cross-validation. However, such criteria needs a proper estimation of the degrees of freedom of the solution, are derived for large samples (asymptotic results) and assume the model is correct, i.e. that the data are actually generated by this model. They also tend to break when the problem is badly conditioned (more features than samples).

Examples:

- Lasso model selection: Cross-Validation / AIC / BIC

Comparison with the regularization parameter of SVM

The equivalence between alpha and the regularization parameter of SVM, C is given by $\alpha = 1 / C$ or $\alpha = 1 / (n_{\text{samples}} \times C)$, depending on the estimator and the exact objective function optimized by the model.
**Multi-task Lasso**

The `MultiTaskLasso` is a linear model that estimates sparse coefficients for multiple regression problems jointly: \( y \) is a 2D array, of shape \((n_{samples}, n_{tasks})\). The constraint is that the selected features are the same for all the regression problems, also called tasks.

The following figure compares the location of the non-zeros in \( W \) obtained with a simple Lasso or a MultiTaskLasso. The Lasso estimates yields scattered non-zeros while the non-zeros of the MultiTaskLasso are full columns.

Fitting a time-series model, imposing that any active feature be active at all times.

**Examples:**

- *Joint feature selection with multi-task Lasso*

Mathematically, it consists of a linear model trained with a mixed \( \ell_1 \ell_2 \) prior as regularizer. The objective function to minimize is:

\[
\min_w \frac{1}{2n_{samples}} ||XW - Y||_{Fro}^2 + \alpha||W||_{21}
\]

where \( \text{Fro} \) indicates the Frobenius norm:

\[
||A||_{\text{Fro}} = \sqrt{\sum_{ij} a_{ij}^2}
\]
and $\ell_1 \ell_2$ reads:

$$||A||_{21} = \sum_i \sqrt{\sum_j a_{ij}^2}$$

The implementation in the class `MultiTaskLasso` uses coordinate descent as the algorithm to fit the coefficients.

**Elastic Net**

`ElasticNet` is a linear regression model trained with L1 and L2 prior as regularizer. This combination allows for learning a sparse model where few of the weights are non-zero like `Lasso`, while still maintaining the regularization properties of `Ridge`. We control the convex combination of L1 and L2 using the `l1_ratio` parameter.

Elastic-net is useful when there are multiple features which are correlated with one another. Lasso is likely to pick one of these at random, while elastic-net is likely to pick both.

A practical advantage of trading-off between Lasso and Ridge is it allows Elastic-Net to inherit some of Ridge’s stability under rotation.

The objective function to minimize is in this case:

$$\min_w \frac{1}{2n_{\text{samples}}} ||X_w - y||_2^2 + \alpha \rho ||w||_1 + \frac{\alpha(1 - \rho)}{2} ||w||_2^2$$

The class `ElasticNetCV` can be used to set the parameters `alpha` ($\alpha$) and `l1_ratio` ($\rho$) by cross-validation.

**Examples:**

- `Lasso and Elastic Net for Sparse Signals`
- `Lasso and Elastic Net`

**Multi-task Elastic Net**

The `MultiTaskElasticNet` is an elastic-net model that estimates sparse coefficients for multiple regression problems jointly: $Y$ is a 2D array, of shape `(n_samples, n_tasks)`. The constraint is that the selected features are the same for all the regression problems, also called tasks.
Mathematically, it consists of a linear model trained with a mixed $\ell_1 \ell_2$ prior and $\ell_2$ prior as regularizer. The objective function to minimize is:

$$
\min_W \frac{1}{2n_{\text{samples}}} \|XW - Y\|_F^2 + \alpha_\rho \|W\|_{21} + \frac{\alpha (1-\rho)}{2} \|W\|_F^2
$$

The implementation in the class `MultiTaskElasticNet` uses coordinate descent as the algorithm to fit the coefficients.

The class `MultiTaskElasticNetCV` can be used to set the parameters `alpha ($\alpha$)` and `l1_ratio ($\rho$)` by cross-validation.

### Least Angle Regression

Least-angle regression (LARS) is a regression algorithm for high-dimensional data, developed by Bradley Efron, Trevor Hastie, Iain Johnstone and Robert Tibshirani. LARS is similar to forward stepwise regression. At each step, it finds the predictor most correlated with the response. When there are multiple predictors having equal correlation, instead of continuing along the same predictor, it proceeds in a direction equiangular between the predictors.

The advantages of LARS are:

- It is numerically efficient in contexts where $p >> n$ (i.e., when the number of dimensions is significantly greater than the number of points)
- It is computationally just as fast as forward selection and has the same order of complexity as an ordinary least squares.
- It produces a full piecewise linear solution path, which is useful in cross-validation or similar attempts to tune the model.
- If two variables are almost equally correlated with the response, then their coefficients should increase at approximately the same rate. The algorithm thus behaves as intuition would expect, and also is more stable.
- It is easily modified to produce solutions for other estimators, like the Lasso.

The disadvantages of the LARS method include:

- Because LARS is based upon an iterative refitting of the residuals, it would appear to be especially sensitive to the effects of noise. This problem is discussed in detail by Weisberg in the discussion section of the Efron et al. (2004) Annals of Statistics article.

The LARS model can be used using estimator `Lars`, or its low-level implementation `lars_path`.

### LARS Lasso

`LassoLars` is a lasso model implemented using the LARS algorithm, and unlike the implementation based on coordinate descent, this yields the exact solution, which is piecewise linear as a function of the norm of its coefficients.

```python
>>> from sklearn import linear_model
>>> reg = linear_model.LassoLars(alpha=.1)
>>> reg.fit([[0, 0], [1, 1]], [0, 1])
LassoLars(alpha=0.1, copy_X=True, eps=..., fit_intercept=True,
    fit_path=True, max_iter=500, normalize=True, positive=False,
    precompute='auto', verbose=False)
>>> reg.coef_
array([ 0.717157..., 0. ])
```
Examples:

- Lasso path using LARS

The Lars algorithm provides the full path of the coefficients along the regularization parameter almost for free, thus a common operation consist of retrieving the path with function `lars_path`

Mathematical formulation

The algorithm is similar to forward stepwise regression, but instead of including variables at each step, the estimated parameters are increased in a direction equiangular to each one’s correlations with the residual.

Instead of giving a vector result, the LARS solution consists of a curve denoting the solution for each value of the L1 norm of the parameter vector. The full coefficients path is stored in the array `coef_path_`, which has size `(n_features, max_features+1)`. The first column is always zero.

References:

- Original Algorithm is detailed in the paper Least Angle Regression by Hastie et al.

Orthogonal Matching Pursuit (OMP)

`OrthogonalMatchingPursuit` and `orthogonal_mp` implements the OMP algorithm for approximating the fit of a linear model with constraints imposed on the number of non-zero coefficients (ie. the L0 pseudo-norm).

Being a forward feature selection method like Least Angle Regression, orthogonal matching pursuit can approximate the optimum solution vector with a fixed number of non-zero elements:

\[
\text{arg min} \ | | y - X\gamma | |^2_2 \text{ subject to } | |\gamma| |_0 \leq n_{\text{nonzero coefs}}
\]

Alternatively, orthogonal matching pursuit can target a specific error instead of a specific number of non-zero coefficients. This can be expressed as:

\[
\text{arg min} \ | |\gamma| |_0 \text{ subject to } | | y - X\gamma | |^2_2 \leq \text{tol}
\]
OMP is based on a greedy algorithm that includes at each step the atom most highly correlated with the current residual. It is similar to the simpler matching pursuit (MP) method, but better in that at each iteration, the residual is recomputed using an orthogonal projection on the space of the previously chosen dictionary elements.

Examples:
- Orthogonal Matching Pursuit

References:

Bayesian Regression

Bayesian regression techniques can be used to include regularization parameters in the estimation procedure: the regularization parameter is not set in a hard sense but tuned to the data at hand. This can be done by introducing uninformative priors over the hyper parameters of the model. The $\ell_2$ regularization used in Ridge Regression is equivalent to finding a maximum a posteriori estimation under a Gaussian prior over the parameters $w$ with precision $\lambda^{-1}$. Instead of setting lambda manually, it is possible to treat it as a random variable to be estimated from the data.

To obtain a fully probabilistic model, the output $y$ is assumed to be Gaussian distributed around $Xw$:

$$p(y|X, w, \alpha) = \mathcal{N}(y|Xw, \alpha)$$

Alpha is again treated as a random variable that is to be estimated from the data.

The advantages of Bayesian Regression are:
- It adapts to the data at hand.
- It can be used to include regularization parameters in the estimation procedure.

The disadvantages of Bayesian regression include:
- Inference of the model can be time consuming.

References
- A good introduction to Bayesian methods is given in C. Bishop: Pattern Recognition and Machine Learning
- Original Algorithm is detailed in the book Bayesian learning for neural networks by Radford M. Neal

Bayesian Ridge Regression

BayesianRidge estimates a probabilistic model of the regression problem as described above. The prior for the parameter $w$ is given by a spherical Gaussian:

$$p(w|\lambda) = \mathcal{N}(w|0, \lambda^{-1}I_p)$$
The priors over $\alpha$ and $\lambda$ are chosen to be gamma distributions, the conjugate prior for the precision of the Gaussian.

The resulting model is called Bayesian Ridge Regression, and is similar to the classical Ridge. The parameters $w$, $\alpha$ and $\lambda$ are estimated jointly during the fit of the model. The remaining hyperparameters are the parameters of the gamma priors over $\alpha$ and $\lambda$. These are usually chosen to be non-informative. The parameters are estimated by maximizing the marginal log likelihood.

By default $\alpha_1 = \alpha_2 = \lambda_1 = \lambda_2 = 10^{-6}$.

Bayesian Ridge Regression is used for regression:

```python
>>> from sklearn import linear_model
>>> X = [[0., 0.], [1., 1.], [2., 2.], [3., 3.]]
>>> Y = [0., 1., 2., 3.]
>>> reg = linear_model.BayesianRidge()
>>> reg.fit(X, Y)
BayesianRidge(alpha_1=1e-06, alpha_2=1e-06, compute_score=False, copy_X=True,
            fit_intercept=True, lambda_1=1e-06, lambda_2=1e-06, n_iter=300,
            normalize=False, tol=0.001, verbose=False)
```

After being fitted, the model can then be used to predict new values:

```python
>>> reg.predict ([[1, 0.]])
array([0.50000013])
```

The weights $w$ of the model can be access:

```python
>>> reg.coef_
array([0.49999993, 0.49999993])
```

Due to the Bayesian framework, the weights found are slightly different to the ones found by Ordinary Least Squares. However, Bayesian Ridge Regression is more robust to ill-posed problem.

**Examples:**

- Bayesian Ridge Regression
Automatic Relevance Determination - ARD

ARDRegression is very similar to Bayesian Ridge Regression, but can lead to sparser weights $w^{12}$. ARDRegression poses a different prior over $w$, by dropping the assumption of the Gaussian being spherical. Instead, the distribution over $w$ is assumed to be an axis-parallel, elliptical Gaussian distribution. This means each weight $w_i$ is drawn from a Gaussian distribution, centered on zero and with a precision $\lambda_i$:

$$p(w|\lambda) = \mathcal{N}(w|0, A^{-1})$$

with $\text{diag}(A) = \lambda = \{\lambda_1, ..., \lambda_p\}$. In contrast to Bayesian Ridge Regression, each coordinate of $w_i$ has its own standard deviation $\lambda_i$. The prior over all $\lambda_i$ is chosen to be the same gamma distribution given by hyperparameters $\lambda_1$ and $\lambda_2$.

ARD is also known in the literature as Sparse Bayesian Learning and Relevance Vector Machine$^{14}$.

Examples:

- Automatic Relevance Determination Regression (ARD)

References:

1 Christopher M. Bishop: Pattern Recognition and Machine Learning, Chapter 7.2.1
2 David Wipf and Srikantan Nagarajan: A new view of automatic relevance determination
3 Michael E. Tipping: Sparse Bayesian Learning and the Relevance Vector Machine
4 Tristan Fletcher: Relevance Vector Machines explained
Logistic regression

Logistic regression, despite its name, is a linear model for classification rather than regression. Logistic regression is also known in the literature as logit regression, maximum-entropy classification (MaxEnt) or the log-linear classifier. In this model, the probabilities describing the possible outcomes of a single trial are modeled using a logistic function.

The implementation of logistic regression in scikit-learn can be accessed from class `LogisticRegression`. This implementation can fit binary, One-vs- Rest, or multinomial logistic regression with optional L2 or L1 regularization.

As an optimization problem, binary class L2 penalized logistic regression minimizes the following cost function:

$$
\min_{w,c} \frac{1}{2} w^T w + C \sum_{i=1}^{n} \log(\exp(-y_i (X_i^T w + c)) + 1).
$$

Similarly, L1 regularized logistic regression solves the following optimization problem

$$
\min_{w,c} \|w\|_1 + C \sum_{i=1}^{n} \log(\exp(-y_i (X_i^T w + c)) + 1).
$$

The solvers implemented in the class `LogisticRegression` are “liblinear”, “newton-cg”, “lbfgs”, “sag” and “saga”:

The solver “liblinear” uses a coordinate descent (CD) algorithm, and relies on the excellent C++ LIBLINEAR library, which is shipped with scikit-learn. However, the CD algorithm implemented in liblinear cannot learn a true multinomial (multiclass) model; instead, the optimization problem is decomposed in a “one-vs-rest” fashion so separate binary classifiers are trained for all classes. This happens under the hood, so `LogisticRegression` instances using this solver behave as multiclass classifiers. For L1 penalization `sklearn.svm.l1_min_c` allows to calculate the lower bound for C in order to get a non “null” (all feature weights to zero) model.

The “lbfgs”, “sag” and “newton-cg” solvers only support L2 penalization and are found to converge faster for some high dimensional data. Setting `multi_class` to “multinomial” with these solvers learns a true multinomial logistic regression model\(^5\), which means that its probability estimates should be better calibrated than the default “one-vs-rest” setting.

The “sag” solver uses a Stochastic Average Gradient descent\(^6\). It is faster than other solvers for large datasets, when both the number of samples and the number of features are large.

The “saga” solver\(^7\) is a variant of “sag” that also supports the non-smooth `penalty="l1"` option. This is therefore the solver of choice for sparse multinomial logistic regression.

In a nutshell, one may choose the solver with the following rules:

<table>
<thead>
<tr>
<th>Case</th>
<th>Solver</th>
</tr>
</thead>
<tbody>
<tr>
<td>L1 penalty</td>
<td>“liblinear” or “saga”</td>
</tr>
<tr>
<td>Multinomial loss</td>
<td>“lbfgs”, “sag”, “saga” or “newton-cg”</td>
</tr>
<tr>
<td>Very Large dataset (n_{samples})</td>
<td>“sag” or “saga”</td>
</tr>
</tbody>
</table>

The “saga” solver is often the best choice. The “liblinear” solver is used by default for historical reasons.

For large dataset, you may also consider using `SGDClassifier` with ‘log’ loss.

---

\(^5\) Christopher M. Bishop: Pattern Recognition and Machine Learning, Chapter 4.3.4

\(^6\) Mark Schmidt, Nicolas Le Roux, and Francis Bach: Minimizing Finite Sums with the Stochastic Average Gradient.

\(^7\) Aaron Defazio, Francis Bach, Simon Lacoste-Julien: SAGA: A Fast Incremental Gradient Method With Support for Non-Strongly Convex Composite Objectives.
Differences from liblinear:

There might be a difference in the scores obtained between `LogisticRegression` with `solver=liblinear` or LinearSVC and the external liblinear library directly, when `fit_intercept=False` and the fit `coef_` (or) the data to be predicted are zeroes. This is because for the sample(s) with `decision_function` zero, `LogisticRegression` and LinearSVC predict the negative class, while liblinear predicts the positive class. Note that a model with `fit_intercept=False` and having many samples with `decision_function` zero, is likely to be a underfit, bad model and you are advised to set `fit_intercept=True` and increase the intercept scaling.

Note: Feature selection with sparse logistic regression

A logistic regression with L1 penalty yields sparse models, and can thus be used to perform feature selection, as detailed in *L1-based feature selection*.

`LogisticRegressionCV` implements Logistic Regression with builtin cross-validation to find out the optimal C parameter. “newton-cg”, “sag”, “saga” and “lbfgs” solvers are found to be faster for high-dimensional dense data, due to warm-starting. For the multiclass case, if `multi_class` option is set to “ovo”, an optimal C is obtained for each class and if the `multi_class` option is set to “multinomial”, an optimal C is obtained by minimizing the cross-entropy loss.

References:

**Stochastic Gradient Descent - SGD**

Stochastic gradient descent is a simple yet very efficient approach to fit linear models. It is particularly useful when the number of samples (and the number of features) is very large. The `partial_fit` method allows only/out-of-core learning.

The classes `SGDClassifier` and `SGDRegressor` provide functionality to fit linear models for classification and regression using different (convex) loss functions and different penalties. E.g., with `loss="log"`, `SGDClassifier` fits a logistic regression model, while with `loss="hinge"` it fits a linear support vector machine (SVM).
Perceptron

The Perceptron is another simple algorithm suitable for large scale learning. By default:

- It does not require a learning rate.
- It is not regularized (penalized).
- It updates its model only on mistakes.

The last characteristic implies that the Perceptron is slightly faster to train than SGD with the hinge loss and that the resulting models are sparser.

Passive Aggressive Algorithms

The passive-aggressive algorithms are a family of algorithms for large-scale learning. They are similar to the Perceptron in that they do not require a learning rate. However, contrary to the Perceptron, they include a regularization parameter $C$.

For classification, PassiveAggressiveClassifier can be used with loss='hinge' (PA-I) or loss='squared_hinge' (PA-II). For regression, PassiveAggressiveRegressor can be used with loss='epsilon_insensitive' (PA-I) or loss='squared_epsilon_insensitive' (PA-II).

References:


Robustness regression: outliers and modeling errors

Robust regression is interested in fitting a regression model in the presence of corrupt data: either outliers, or error in the model.

![Robustness Regression Graph](image)

Different scenario and useful concepts

There are different things to keep in mind when dealing with data corrupted by outliers:
• Outliers in X or in y?

The number of outlying points matters, but also how much they are outliers.

An important notion of robust fitting is that of breakdown point: the fraction of data that can be outlying for the fit to start missing the inlying data.

Note that in general, robust fitting in high-dimensional setting (large n_features) is very hard. The robust models here will probably not work in these settings.

Trade-offs: which estimator?

Scikit-learn provides 3 robust regression estimators: RANSAC, Theil Sen and HuberRegressor

- HuberRegressor should be faster than RANSAC and Theil Sen unless the number of samples are very large, i.e n_samples >> n_features. This is because RANSAC and Theil Sen fit on smaller subsets of the data. However, both Theil Sen and RANSAC are unlikely to be as robust as HuberRegressor for the default parameters.
- **RANSAC** is faster than *Theil Sen* and scales much better with the number of samples.
- **RANSAC** will deal better with large outliers in the y direction (most common situation).
- *Theil Sen* will cope better with medium-size outliers in the X direction, but this property will disappear in large dimensional settings.

When in doubt, use **RANSAC**

### RANSAC: RANdom SAmple Consensus

RANSAC (RANdom SAmple Consensus) fits a model from random subsets of inliers from the complete data set. RANSAC is a non-deterministic algorithm producing only a reasonable result with a certain probability, which is dependent on the number of iterations (see *max_trials* parameter). It is typically used for linear and non-linear regression problems and is especially popular in the fields of photogrammetric computer vision.

The algorithm splits the complete input sample data into a set of inliers, which may be subject to noise, and outliers, which are e.g. caused by erroneous measurements or invalid hypotheses about the data. The resulting model is then estimated only from the determined inliers.

![Example graph showing linear regression](image)

#### Details of the algorithm

Each iteration performs the following steps:

1. Select *min_samples* random samples from the original data and check whether the set of data is valid (see *is_data_valid*).
2. Fit a model to the random subset (*base_estimator.fit*) and check whether the estimated model is valid (see *is_model_valid*).
3. Classify all data as inliers or outliers by calculating the residuals to the estimated model (*base_estimator.predict(X) - y*) - all data samples with absolute residuals smaller than the *residual_threshold* are considered as inliers.
4. Save fitted model as best model if number of inlier samples is maximal. In case the current estimated model has the same number of inliers, it is only considered as the best model if it has better score.
These steps are performed either a maximum number of times (max_trials) or until one of the special stop criteria are met (see stop_n_inliers and stop_score). The final model is estimated using all inlier samples (consensus set) of the previously determined best model.

The is_data_valid and is_model_valid functions allow to identify and reject degenerate combinations of random sub-samples. If the estimated model is not needed for identifying degenerate cases, is_data_valid should be used as it is called prior to fitting the model and thus leading to better computational performance.

**Examples:**

- Robust linear model estimation using RANSAC
- Robust linear estimator fitting

**References:**


**Theil-Sen estimator: generalized-median-based estimator**

The TheilSenRegressor estimator uses a generalization of the median in multiple dimensions. It is thus robust to multivariate outliers. Note however that the robustness of the estimator decreases quickly with the dimensionality of the problem. It looses its robustness properties and becomes no better than an ordinary least squares in high dimension.

**Examples:**

- Theil-Sen Regression
- Robust linear estimator fitting

**References:**

- https://en.wikipedia.org/wiki/Theil%E2%80%93Sen_estimator

**Theoretical considerations**

TheilSenRegressor is comparable to the **Ordinary Least Squares (OLS)** in terms of asymptotic efficiency and as an unbiased estimator. In contrast to OLS, Theil-Sen is a non-parametric method which means it makes no assumption about the underlying distribution of the data. Since Theil-Sen is a median-based estimator, it is more robust against corrupted data aka outliers. In univariate setting, Theil-Sen has a breakdown point of about 29.3% in case of a simple linear regression which means that it can tolerate arbitrary corrupted data of up to 29.3%.
The implementation of \texttt{TheilSenRegressor} in scikit-learn follows a generalization to a multivariate linear regression model\textsuperscript{8} using the spatial median which is a generalization of the median to multiple dimensions\textsuperscript{9}.

In terms of time and space complexity, Theil-Sen scales according to

\[
\binom{n_{\text{samples}}}{n_{\text{subsamples}}}
\]

which makes it infeasible to be applied exhaustively to problems with a large number of samples and features. Therefore, the magnitude of a subpopulation can be chosen to limit the time and space complexity by considering only a random subset of all possible combinations.

\begin{itemize}
  \item \textbf{Theil-Sen Regression}
\end{itemize}

\begin{itemize}
  \item \textbf{References:}
\end{itemize}

**Huber Regression**

The \texttt{HuberRegressor} is different to \texttt{Ridge} because it applies a linear loss to samples that are classified as outliers. A sample is classified as an inlier if the absolute error of that sample is lesser than a certain threshold. It differs from \texttt{TheilSenRegressor} and \texttt{RANSACRegressor} because it does not ignore the effect of the outliers but gives a lesser weight to them.

The loss function that \texttt{HuberRegressor} minimizes is given by

\[
\min_{w,\sigma} \sum_{i=1}^{n} \left( \sigma + H_{m} \left( \frac{x_{i}w - y_{i}}{\sigma} \right) \sigma \right) + \alpha||w||^2
\]

\textsuperscript{8} Xin Dang, Hanxian Peng, Xueqin Wang and Heping Zhang: Theil-Sen Estimators in a Multiple Linear Regression Model.

\textsuperscript{9} 20. Kärkkäinen and S. Åyrämö: On Computation of Spatial Median for Robust Data Mining.

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where

\[
H_m(z) = \begin{cases} 
  z^2, & \text{if } |z| < \epsilon, \\
  2|z| - \epsilon^2, & \text{otherwise}
\end{cases}
\]

It is advised to set the parameter `epsilon` to 1.35 to achieve 95% statistical efficiency.

**Notes**

The `HuberRegressor` differs from using `SGDRegressor` with loss set to `huber` in the following ways.

- `HuberRegressor` is scaling invariant. Once `epsilon` is set, scaling `X` and `y` down or up by different values would produce the same robustness to outliers as before, as compared to `SGDRegressor` where `epsilon` has to be set again when `X` and `y` are scaled.

- `HuberRegressor` should be more efficient to use on data with small number of samples while `SGDRegressor` needs a number of passes on the training data to produce the same robustness.

**Examples:**

- `HuberRegressor vs Ridge on dataset with strong outliers`

**References:**

- Peter J. Huber, Elvezio M. Ronchetti: Robust Statistics, Concomitant scale estimates, pg 172

Also, this estimator is different from the R implementation of Robust Regression (http://www.ats.ucla.edu/stat/r/dae/rreg.htm) because the R implementation does a weighted least squares implementation with weights given to each sample on the basis of how much the residual is greater than a certain threshold.

**Polynomial regression: extending linear models with basis functions**

One common pattern within machine learning is to use linear models trained on nonlinear functions of the data. This approach maintains the generally fast performance of linear methods, while allowing them to fit a much wider range of data.
For example, a simple linear regression can be extended by constructing **polynomial features** from the coefficients. In the standard linear regression case, you might have a model that looks like this for two-dimensional data:

\[
\hat{y}(w, x) = w_0 + w_1 x_1 + w_2 x_2
\]

If we want to fit a paraboloid to the data instead of a plane, we can combine the features in second-order polynomials, so that the model looks like this:

\[
\hat{y}(w, x) = w_0 + w_1 x_1 + w_2 x_2 + w_3 x_1 x_2 + w_4 x_1^2 + w_5 x_2^2
\]

The (sometimes surprising) observation is that this is **still a linear model**: to see this, imagine creating a new variable

\[
z = [x_1, x_2, x_1 x_2, x_1^2, x_2^2]
\]

With this re-labeling of the data, our problem can be written

\[
\hat{y}(w, x) = w_0 + w_1 z_1 + w_2 z_2 + w_3 z_3 + w_4 z_4 + w_5 z_5
\]

We see that the resulting polynomial regression is in the same class of linear models we’d considered above (i.e. the model is linear in \(w\)) and can be solved by the same techniques. By considering linear fits within a higher-dimensional space built with these basis functions, the model has the flexibility to fit a much broader range of data.

Here is an example of applying this idea to one-dimensional data, using polynomial features of varying degrees:

This figure is created using the `PolynomialFeatures` preprocessor. This preprocessor transforms an input data matrix into a new data matrix of a given degree. It can be used as follows:

```python
>>> from sklearn.preprocessing import PolynomialFeatures
>>> import numpy as np

>>> X = np.arange(6).reshape(3, 2)
>>> poly = PolynomialFeatures(degree=2)
>>> poly.fit_transform(X)
```

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The features of $X$ have been transformed from $[x_1, x_2]$ to $[1, x_1, x_2, x_1^2, x_1x_2, x_2^2]$, and can now be used within any linear model.

This sort of preprocessing can be streamlined with the `Pipeline` tools. A single object representing a simple polynomial regression can be created and used as follows:

```python
>>> from sklearn.preprocessing import PolynomialFeatures
>>> from sklearn.linear_model import LinearRegression
>>> from sklearn.pipeline import Pipeline
>>> import numpy as np

>>> model = Pipeline([('poly', PolynomialFeatures(degree=3)), ...
                      ('linear', LinearRegression(fit_intercept=False))])

>>> # fit to an order-3 polynomial data
>>> x = np.arange(5)
>>> y = 3 - 2 * x + x ** 2 - x ** 3
>>> model = model.fit(x[:, np.newaxis], y)
>>> model.named_steps['linear'].coef_
array([ 3., -2., 1., -1.])
```

The linear model trained on polynomial features is able to exactly recover the input polynomial coefficients.

In some cases it’s not necessary to include higher powers of any single feature, but only the so-called interaction features that multiply together at most $d$ distinct features. These can be gotten from `PolynomialFeatures` with the setting `interaction_only=True`.

For example, when dealing with boolean features, $x_i^n = x_i$ for all $n$ and is therefore useless; but $x_ix_j$ represents the conjunction of two booleans. This way, we can solve the XOR problem with a linear classifier:

```python
>>> from sklearn.linear_model import Perceptron
>>> from sklearn.preprocessing import PolynomialFeatures
>>> import numpy as np

>>> X = np.array([[0, 0], [0, 1], [1, 0], [1, 1]])
>>> y = X[:, 0] ^ X[:, 1]
>>> y
array([0, 1, 1, 0])
>>> X = PolynomialFeatures(interaction_only=True).fit_transform(X).astype(int)
>>> X
array([[1, 0, 0, 0],
       [1, 0, 1, 0],
       [1, 1, 0, 0],
       [1, 1, 1, 1]])
>>> clf = Perceptron(fit_intercept=False, max_iter=10, tol=None, ...
                    shuffle=False).fit(X, y)

And the classifier “predictions” are perfect:

```python
>>> clf.predict(X)
array([0, 1, 1, 0])
>>> clf.score(X, y)
1.0
```

### 3.1.2 Linear and Quadratic Discriminant Analysis

Linear Discriminant Analysis ([discriminant_analysis.LinearDiscriminantAnalysis](#)) and Quadratic Discriminant Analysis ([discriminant_analysis.QuadraticDiscriminantAnalysis](#)) are two classic classifiers, with, as their names suggest, a linear and a quadratic decision surface, respectively.
These classifiers are attractive because they have closed-form solutions that can be easily computed, are inherently multiclass, have proven to work well in practice and have no hyperparameters to tune.

The plot shows decision boundaries for Linear Discriminant Analysis and Quadratic Discriminant Analysis. The bottom row demonstrates that Linear Discriminant Analysis can only learn linear boundaries, while Quadratic Discriminant Analysis can learn quadratic boundaries and is therefore more flexible.

**Examples:**

*Linear and Quadratic Discriminant Analysis with covariance ellipsoid*: Comparison of LDA and QDA on synthetic data.

**Dimensionality reduction using Linear Discriminant Analysis**

discriminant_analysis.LinearDiscriminantAnalysis can be used to perform supervised dimensionality reduction, by projecting the input data to a linear subspace consisting of the directions which maximize the separation between classes (in a precise sense discussed in the mathematics section below). The dimension of the output is necessarily less than the number of classes, so this is a in general a rather strong dimensionality reduction, and only makes senses in a multiclass setting.

This is implemented in discriminant_analysis.LinearDiscriminantAnalysis.transform. The desired dimensionality can be set using the n_components constructor parameter. This parameter has no influence on discriminant_analysis.LinearDiscriminantAnalysis.fit or discriminant_analysis.LinearDiscriminantAnalysis.predict.

**Examples:**
Mathematical formulation of the LDA and QDA classifiers

Both LDA and QDA can be derived from simple probabilistic models which model the class conditional distribution of the data \( P(X|y = k) \) for each class \( k \). Predictions can then be obtained by using Bayes’ rule:

\[
P(y = k|X) = \frac{P(X|y = k)P(y = k)}{P(X)} = \frac{P(X|y = k)P(y = k)}{\sum_l P(X|y = l) \cdot P(y = l)}
\]

and we select the class \( k \) which maximizes this conditional probability.

More specifically, for linear and quadratic discriminant analysis, \( P(X|y) \) is modelled as a multivariate Gaussian distribution with density:

\[
p(X|y = k) = \frac{1}{(2\pi)^{n/2} |\Sigma_k|^{1/2}} \exp \left( -\frac{1}{2} (X - \mu_k)^T \Sigma_k^{-1} (X - \mu_k) \right)
\]

To use this model as a classifier, we just need to estimate from the training data the class priors \( P(y = k) \) (by the proportion of instances of class \( k \)), the class means \( \mu_k \) (by the empirical sample class means) and the covariance matrices (either by the empirical sample class covariance matrices, or by a regularized estimator: see the section on shrinkage below).

In the case of LDA, the Gaussians for each class are assumed to share the same covariance matrix: \( \Sigma_k = \Sigma \) for all \( k \). This leads to linear decision surfaces between, as can be seen by comparing the log-probability ratios \( \log[P(y = k|X)/P(y = l|X)] \):

\[
\log \left( \frac{P(y = k|X)}{P(y = l|X)} \right) = 0 \iff (\mu_k - \mu_l)^T \Sigma^{-1} (X - \mu_k) = 0
\]

In the case of QDA, there are no assumptions on the covariance matrices \( \Sigma_k \) of the Gaussians, leading to quadratic decision surfaces. See\(^3\) for more details.

**Note: Relation with Gaussian Naive Bayes**

If in the QDA model one assumes that the covariance matrices are diagonal, then the inputs are assumed to be conditionally independent in each class, and the resulting classifier is equivalent to the Gaussian Naive Bayes classifier `naive_bayes.GaussianNB`.

Mathematical formulation of LDA dimensionality reduction

To understand the use of LDA in dimensionality reduction, it is useful to start with a geometric reformulation of the LDA classification rule explained above. We write \( K \) for the total number of target classes. Since in LDA we assume that all classes have the same estimated covariance \( \Sigma \), we can rescale the data so that this covariance is the identity:

\[
X^* = D^{-1/2} U^T X \quad \text{with} \quad \Sigma = U D U^T
\]

Then one can show that to classify a data point after scaling is equivalent to finding the estimated class mean \( \mu_k^* \) which is closest to the data point in the Euclidean distance. But this can be done just as well after projecting on the \( K - 1 \) affine subspace \( \mathcal{H}_K \) generated by all the \( \mu_k^* \) for all classes. This shows that, implicit in the LDA classifier, there is a dimensionality reduction by linear projection onto a \( K - 1 \) dimensional space.

We can reduce the dimension even more, to a chosen $L$, by projecting onto the linear subspace $H_L$ which maximize the variance of the $\mu^*_k$ after projection (in effect, we are doing a form of PCA for the transformed class means $\mu^*_k$). This $L$ corresponds to the $n\_components$ parameter used in the `discriminant_analysis.LinearDiscriminantAnalysis.transform` method. See\(^3\) for more details.

**Shrinkage**

Shrinkage is a tool to improve estimation of covariance matrices in situations where the number of training samples is small compared to the number of features. In this scenario, the empirical sample covariance is a poor estimator. Shrinkage LDA can be used by setting the `shrinkage` parameter of the `discriminant_analysis.LinearDiscriminantAnalysis` class to ‘auto’. This automatically determines the optimal shrinkage parameter in an analytic way following the lemma introduced by Ledoit and Wolf\(^4\). Note that currently shrinkage only works when setting the `solver` parameter to ‘lsqr’ or ‘eigen’.

The `shrinkage` parameter can also be manually set between 0 and 1. In particular, a value of 0 corresponds to no shrinkage (which means the empirical covariance matrix will be used) and a value of 1 corresponds to complete shrinkage (which means that the diagonal matrix of variances will be used as an estimate for the covariance matrix). Setting this parameter to a value between these two extrema will estimate a shrunk version of the covariance matrix.

![Linear Discriminant Analysis with shrinkage vs. Linear Discriminant Analysis](image)

**Estimation algorithms**

The default solver is ‘svd’. It can perform both classification and transform, and it does not rely on the calculation of the covariance matrix. This can be an advantage in situations where the number of features is large. However, the ‘svd’ solver cannot be used with shrinkage.

The ‘lsqr’ solver is an efficient algorithm that only works for classification. It supports shrinkage.

The ‘eigen’ solver is based on the optimization of the between class scatter to within class scatter ratio. It can be used for both classification and transform, and it supports shrinkage. However, the ‘eigen’ solver needs to compute the covariance matrix, so it might not be suitable for situations with a high number of features.

Examples:

*Normal and Shrinkage Linear Discriminant Analysis for classification*: Comparison of LDA classifiers with and without shrinkage.

References:

3.1.3 Kernel ridge regression

Kernel ridge regression (KRR) \[M2012\] combines *Ridge Regression* (linear least squares with l2-norm regularization) with the kernel trick. It thus learns a linear function in the space induced by the respective kernel and the data. For non-linear kernels, this corresponds to a non-linear function in the original space.

The form of the model learned by *KernelRidge* is identical to support vector regression (SVR). However, different loss functions are used: KRR uses squared error loss while support vector regression uses \(\epsilon\)-insensitive loss, both combined with l2 regularization. In contrast to SVR, fitting *KernelRidge* can be done in closed-form and is typically faster for medium-sized datasets. On the other hand, the learned model is non-sparse and thus slower than SVR, which learns a sparse model for \(\epsilon > 0\), at prediction-time.

The following figure compares *KernelRidge* and SVR on an artificial dataset, which consists of a sinusoidal target function and strong noise added to every fifth datapoint. The learned model of *KernelRidge* and SVR is plotted, where both complexity/regularization and bandwidth of the RBF kernel have been optimized using grid-search. The learned functions are very similar; however, fitting *KernelRidge* is approx. seven times faster than fitting SVR (both with grid-search). However, prediction of 100000 target values is more than three times faster with SVR since it has learned a sparse model using only approx. 1/3 of the 100 training datapoints as support vectors.

The next figure compares the time for fitting and prediction of *KernelRidge* and SVR for different sizes of the training set. Fitting *KernelRidge* is faster than SVR for medium-sized training sets (less than 1000 samples); however, for larger training sets SVR scales better. With regard to prediction time, SVR is faster than *KernelRidge* for all sizes of the training set because of the learned sparse solution. Note that the degree of sparsity and thus the prediction time depends on the parameters \(\epsilon\) and \(C\) of the SVR; \(\epsilon = 0\) would correspond to a dense model.

References:

3.1.4 Support Vector Machines

Support vector machines (SVMs) are a set of supervised learning methods used for *classification*, *regression* and *outliers detection*.

The advantages of support vector machines are:

- Effective in high dimensional spaces.
- Still effective in cases where number of dimensions is greater than the number of samples.
- Uses a subset of training points in the decision function (called support vectors), so it is also memory efficient.
- Versatile: different *Kernel functions* can be specified for the decision function. Common kernels are provided, but it is also possible to specify custom kernels.

The disadvantages of support vector machines include:
SVR versus Kernel Ridge

- SVR (fit: 0.871s, predict: 0.151s)
- KRR (fit: 0.402s, predict: 0.384s)
- SVR support vectors
- data

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Execution Time

- KRR (train)
- KRR (test)
- SVR (train)
- SVR (test)

Time (seconds)

Train size

10^1  10^2  10^3  10^4
- If the number of features is much greater than the number of samples, avoid over-fitting in choosing Kernel functions and regularization term is crucial.
- SVMs do not directly provide probability estimates, these are calculated using an expensive five-fold cross-validation (see Scores and probabilities, below).

The support vector machines in scikit-learn support both dense (numpy.ndarray and convertible to that by numpy.asarray) and sparse (any scipy.sparse) sample vectors as input. However, to use an SVM to make predictions for sparse data, it must have been fit on such data. For optimal performance, use C-ordered numpy.ndarray (dense) or scipy.sparse.csr_matrix (sparse) with dtype=float64.

Classification

SVC, NuSVC and LinearSVC are classes capable of performing multi-class classification on a dataset.

SVC and NuSVC are similar methods, but accept slightly different sets of parameters and have different mathematical formulations (see section Mathematical formulation). On the other hand, LinearSVC is another implementation of Support Vector Classification for the case of a linear kernel. Note that LinearSVC does not accept keyword kernel, as this is assumed to be linear. It also lacks some of the members of SVC and NuSVC, like support_.

As other classifiers, SVC, NuSVC and LinearSVC take as input two arrays: an array X of size [n_samples, n_features] holding the training samples, and an array y of class labels (strings or integers), size [n_samples]:

```python
>>> from sklearn import svm
>>> X = [[0, 0], [1, 1]]
```
```python
>>> y = [0, 1]
>>> clf = svm.SVC()
>>> clf.fit(X, y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
    decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
    max_iter=-1, probability=False, random_state=None, shrinking=True,
    tol=0.001, verbose=False)
After being fitted, the model can then be used to predict new values:
```  
```python
>>> clf.predict([[2., 2.]])
array([1])
```  
SVMs decision function depends on some subset of the training data, called the support vectors. Some properties of these support vectors can be found in members support_vectors_, support_ and n_support:
```python
>>> # get support vectors
>>> clf.support_vectors_
array([[ 0., 0.],
        [ 1., 1.]])
>>> # get indices of support vectors
>>> clf.support_
array([0, 1]...)
>>> # get number of support vectors for each class
>>> clf.n_support_
array([1, 1]...)

Multi-class classification

SVC and NuSVC implement the “one-against-one” approach (Knerr et al., 1990) for multi-class classification. If n_class is the number of classes, then n_class * (n_class - 1) / 2 classifiers are constructed and each one trains data from two classes. To provide a consistent interface with other classifiers, the decision_function_shape option allows to aggregate the results of the “one-against-one” classifiers to a decision function of shape (n_samples, n_classes):
```python
>>> X = [[0], [1], [2], [3]]
>>> Y = [0, 1, 2, 3]
>>> clf = svm.SVC(decision_function_shape='ovo')
>>> clf.fit(X, Y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
    decision_function_shape='ovo', degree=3, gamma='auto', kernel='rbf',
    max_iter=-1, probability=False, random_state=None, shrinking=True,
    tol=0.001, verbose=False)
>>> dec = clf.decision_function([[1]])
>>> dec.shape[1]  # 4 classes: 4*3/2 = 6
6
>>> clf.decision_function_shape = "ovr"
>>> dec = clf.decision_function([[1]])
>>> dec.shape[1]  # 4 classes
4
On the other hand, LinearSVC implements “one-vs-the-rest” multi-class strategy, thus training n_class models. If there are only two classes, only one model is trained:
>>> lin_clf = svm.LinearSVC()
>>> lin_clf.fit(X, Y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
         intercept_scaling=1, loss='squared_hinge', max_iter=1000,
         multi_class='ovr', penalty='l2', random_state=None, tol=0.0001,
         verbose=0)
>>> dec = lin_clf.decision_function([[1]])
>>> dec.shape[1]
4

See Mathematical formulation for a complete description of the decision function.

Note that the LinearSVC also implements an alternative multi-class strategy, the so-called multi-class SVM formulated by Crammer and Singer, by using the option multi_class='crammer_singer'. This method is consistent, which is not true for one-vs-rest classification. In practice, one-vs-rest classification is usually preferred, since the results are mostly similar, but the runtime is significantly less.

For “one-vs-rest” LinearSVC the attributes coef_ and intercept_ have the shape [n_class, n_features] and [n_class] respectively. Each row of the coefficients corresponds to one of the n_class many “one-vs-rest” classifiers and similar for the intercepts, in the order of the “one” class.

In the case of “one-vs-one” SVC, the layout of the attributes is a little more involved. In the case of having a linear kernel, The layout of coef_ and intercept_ is similar to the one described for LinearSVC described above, except that the shape of coef_is [n_class * (n_class - 1) / 2, n_features], corresponding to as many binary classifiers. The order for classes 0 to n is “0 vs 1”, “0 vs 2”, . . . “0 vs n”, “1 vs 2”, “1 vs 3”, “1 vs n”, . . . “n-1 vs n”.

The shape of dual_coef__ is [n_class-1, n_SV] with a somewhat hard to grasp layout. The columns correspond to the support vectors involved in any of the n_class * (n_class - 1) / 2 “one-vs-one” classifiers. Each of the support vectors is used in n_class - 1 classifiers. The n_class - 1 entries in each row correspond to the dual coefficients for these classifiers.

This might be made more clear by an example:

Consider a three class problem with class 0 having three support vectors $v^0_0$, $v^1_0$, $v^2_0$ and class 1 and 2 having two support vectors $v^0_1$, $v^1_1$ and $v^0_2$, $v^1_2$ respectively. For each support vector $v^i_j$, there are two dual coefficients. Let’s call the coefficient of support vector $v^i_j$ in the classifier between classes $i$ and $k$ $\alpha^i_{j,k}$. Then dual_coef__ looks like this:

| $\alpha^0_{0,0}$ | $\alpha^0_{0,2}$ | Coefficients for SVs of class 0 |
| $\alpha^0_{0,1}$ | $\alpha^0_{1,2}$ | $\alpha^0_{2,2}$ |
| $\alpha^1_{0,0}$ | $\alpha^1_{0,1}$ | Coefficients for SVs of class 1 |
| $\alpha^1_{0,2}$ | $\alpha^1_{1,2}$ | $\alpha^1_{2,2}$ |
| $\alpha^2_{0,0}$ | $\alpha^2_{0,1}$ | Coefficients for SVs of class 2 |
| $\alpha^2_{0,2}$ | $\alpha^2_{1,2}$ |

Scores and probabilities

The decision_function method of SVC and NuSVC gives per-class scores for each sample (or a single score per sample in the binary case). When the constructor option probability is set to True, class membership probability estimates (from the methods predict_proba and predict_log_proba) are enabled. In the binary case, the probabilities are calibrated using Platt scaling: logistic regression on the SVM’s scores, fit by an additional cross-validation on the training data. In the multiclass case, this is extended as per Wu et al. (2004).

 Needless to say, the cross-validation involved in Platt scaling is an expensive operation for large datasets. In addition, the probability estimates may be inconsistent with the scores, in the sense that the “argmax” of the scores may not be
the argmax of the probabilities. (E.g., in binary classification, a sample may be labeled by `predict` as belonging to a class that has probability <½ according to `predict_proba`.) Platt’s method is also known to have theoretical issues. If confidence scores are required, but these do not have to be probabilities, then it is advisable to set `probability=False` and use `decision_function` instead of `predict_proba`.

**References:**

- Platt “Probabilistic outputs for SVMs and comparisons to regularized likelihood methods”.

**Unbalanced problems**

In problems where it is desired to give more importance to certain classes or certain individual samples keywords `class_weight` and `sample_weight` can be used.

*SVC* (but not *NuSVC*) implement a keyword `class_weight` in the `fit` method. It’s a dictionary of the form `{class_label : value}`, where value is a floating point number > 0 that sets the parameter $C$ of class `class_label` to $C \times$ value.

*SVC, NuSVC, SVR, NuSVR* and *OneClassSVM* implement also weights for individual samples in method `fit` through keyword `sample_weight`. Similar to `class_weight`, these set the parameter $C$ for the i-th example to $C \times$ sample_weight[i].

**Examples:**

- *Plot different SVM classifiers in the iris dataset.*
Regression

The method of Support Vector Classification can be extended to solve regression problems. This method is called Support Vector Regression.

The model produced by support vector classification (as described above) depends only on a subset of the training data, because the cost function for building the model does not care about training points that lie beyond the margin. Analogously, the model produced by Support Vector Regression depends only on a subset of the training data, because the cost function for building the model ignores any training data close to the model prediction.

There are three different implementations of Support Vector Regression: SVR, NuSVR and LinearSVR. LinearSVR provides a faster implementation than SVR but only considers linear kernels, while NuSVR implements a slightly different formulation than SVR and LinearSVR. See Implementation details for further details.

As with classification classes, the fit method will take as argument vectors $X$, $y$, only that in this case $y$ is expected to have floating point values instead of integer values:

```python
>>> from sklearn import svm

>>> X = [[0, 0], [2, 2]]
>>> y = [0.5, 2.5]
>>> clf = svm.SVR()

>>> clf.fit(X, y)
SVR(C=1.0, cache_size=200, coef0=0.0, degree=3, epsilon=0.1, gamma='auto',
    kernel='rbf', max_iter=-1, shrinking=True, tol=0.001, verbose=False)

>>> clf.predict([[1, 1]])
array([ 1.5])
```
Examples:

- Support Vector Regression (SVR) using linear and non-linear kernels

Density estimation, novelty detection

One-class SVM is used for novelty detection, that is, given a set of samples, it will detect the soft boundary of that set so as to classify new points as belonging to that set or not. The class that implements this is called `OneClassSVM`.

In this case, as it is a type of unsupervised learning, the fit method will only take as input an array X, as there are no class labels.

See, section Novelty and Outlier Detection for more details on this usage.

Complexity

Support Vector Machines are powerful tools, but their compute and storage requirements increase rapidly with the number of training vectors. The core of an SVM is a quadratic programming problem (QP), separating support vectors from the rest of the training data. The QP solver used by this `libsvm`-based implementation scales between $O(n_{features} \times n_{samples}^2)$ and $O(n_{features} \times n_{samples}^3)$ depending on how efficiently the `libsvm` cache is used in practice (dataset dependent). If the data is very sparse $n_{features}$ should be replaced by the average number of non-zero features in a sample vector.
Also note that for the linear case, the algorithm used in `LinearSVC` by the liblinear implementation is much more efficient than its libsvm-based `SVC` counterpart and can scale almost linearly to millions of samples and/or features.

**Tips on Practical Use**

- **Avoiding data copy**: For `SVC`, `SVR`, `NuSVC` and `NuSVR`, if the data passed to certain methods is not C-ordered contiguous, and double precision, it will be copied before calling the underlying C implementation. You can check whether a given numpy array is C-contiguous by inspecting its `flags` attribute. For `LinearSVC` (and `LogisticRegression`) any input passed as a numpy array will be copied and converted to the liblinear internal sparse data representation (double precision floats and int32 indices of non-zero components). If you want to fit a large-scale linear classifier without copying a dense numpy C-contiguous double precision array as input we suggest to use the `SGDClassifier` class instead. The objective function can be configured to be almost the same as the `LinearSVC` model.

- **Kernel cache size**: For `SVC`, `SVR`, `NuSVC` and `NuSVR`, the size of the kernel cache has a strong impact on run times for larger problems. If you have enough RAM available, it is recommended to set `cache_size` to a higher value than the default of 200(MB), such as 500(MB) or 1000(MB).

- **Setting C**: `C` is 1 by default and it’s a reasonable default choice. If you have a lot of noisy observations you should decrease it. It corresponds to regularize more the estimation.

- **Support Vector Machine algorithms are not scale invariant, so it is highly recommended to scale your data.** For example, scale each attribute on the input vector X to [0,1] or [-1,1], or standardize it to have mean 0 and variance 1. Note that the same scaling must be applied to the test vector to obtain meaningful results. See section Preprocessing data for more details on scaling and normalization.

- **Parameter nu in `NuSVC/OneClassSVM/NuSVR` approximates the fraction of training errors and support vectors.**

- **In `SVC`, if data for classification are unbalanced (e.g. many positive and few negative), set `class_weight='balanced'` and/or try different penalty parameters C.**

- **Randomness of the underlying implementations**: The underlying implementations of `SVC` and `NuSVC` use a random number generator only to shuffle the data for probability estimation (when `probability` is set to `True`). This randomness can be controlled with the `random_state` parameter. If `probability` is set to `False` these estimators are not random and `random_state` has no effect on the results. The underlying `OneClassSVM` implementation is similar to the ones of `SVC` and `NuSVC`. As no probability estimation is provided for `OneClassSVM`, it is not random.

The underlying `LinearSVC` implementation uses a random number generator to select features when fitting the model with a dual coordinate descent (i.e when `dual` is set to `True`). It is thus not uncommon, to have slightly different results for the same input data. If that happens, try with a smaller `tol` parameter. This randomness can also be controlled with the `random_state` parameter. When `dual` is set to `False` the underlying implementation of `LinearSVC` is not random and `random_state` has no effect on the results.

- **Using L1 penalization as provided by `LinearSVC(loss='l2', penalty='l1', dual=False)` yields a sparse solution, i.e. only a subset of feature weights is different from zero and contribute to the decision function. Increasing `C` yields a more complex model (more feature are selected). The `C` value that yields a “null” model (all weights equal to zero) can be calculated using `l1_min_c`.**

**Kernel functions**

The `kernel function` can be any of the following:

- **linear**: $\langle x, x' \rangle$.  
- **polynomial**: $(\gamma \langle x, x' \rangle + r)^d$. $d$ is specified by keyword `degree`, $r$ by `coef0`.  

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• rbf: \( \exp(-\gamma \|x - x'\|²) \). \( \gamma \) is specified by keyword \texttt{gamma}, must be greater than 0.

• sigmoid \( \tanh(\gamma \langle x, x' \rangle + r) \), where \( r \) is specified by \texttt{coef0}.

Different kernels are specified by keyword \texttt{kernel} at initialization:

```python
>>> linear_svc = svm.SVC(kernel='linear')
>>> linear_svc.kernel
'linear'
>>> rbf_svc = svm.SVC(kernel='rbf')
>>> rbf_svc.kernel
'rbf'
```

**Custom Kernels**

You can define your own kernels by either giving the kernel as a python function or by precomputing the Gram matrix. Classifiers with custom kernels behave the same way as any other classifiers, except that:

- Field \texttt{support_vectors_} is now empty, only indices of support vectors are stored in \texttt{support_}
- A reference (and not a copy) of the first argument in the \texttt{fit()} method is stored for future reference. If that array changes between the use of \texttt{fit()} and \texttt{predict()} you will have unexpected results.

**Using Python functions as kernels**

You can also use your own defined kernels by passing a function to the keyword \texttt{kernel} in the constructor.

Your kernel must take as arguments two matrices of shape \((n\_samples\_1, n\_features),(n\_samples\_2, n\_features)\) and return a kernel matrix of shape \((n\_samples\_1, n\_samples\_2)\).

The following code defines a linear kernel and creates a classifier instance that will use that kernel:

```python
>>> import numpy as np
>>> from sklearn import svm
>>> def my_kernel(X, Y):
...     return np.dot(X, Y.T)
...
>>> clf = svm.SVC(kernel=my_kernel)
```

**Examples:**

- \( SVM \) with custom kernel.

**Using the Gram matrix**

Set \texttt{kernel='precomputed'} and pass the Gram matrix instead of \( X \) in the \texttt{fit} method. At the moment, the kernel values between all training vectors and the test vectors must be provided.

```python
>>> import numpy as np
>>> from sklearn import svm
>>> X = np.array([[0, 0], [1, 1]])
>>> y = [0, 1]
>>> clf = svm.SVC(kernel='precomputed')
```
Parameters of the RBF Kernel

When training an SVM with the Radial Basis Function (RBF) kernel, two parameters must be considered: \(C\) and \(\gamma\). The parameter \(C\), common to all SVM kernels, trades off misclassification of training examples against simplicity of the decision surface. A low \(C\) makes the decision surface smooth, while a high \(C\) aims at classifying all training examples correctly. \(\gamma\) defines how much influence a single training example has. The larger \(\gamma\) is, the closer other examples must be to be affected.

Proper choice of \(C\) and \(\gamma\) is critical to the SVM’s performance. One is advised to use `sklearn.model_selection.GridSearchCV` with \(C\) and \(\gamma\) spaced exponentially far apart to choose good values.

Examples:

- **RBF SVM parameters**

Mathematical formulation

A support vector machine constructs a hyper-plane or set of hyper-planes in a high or infinite dimensional space, which can be used for classification, regression or other tasks. Intuitively, a good separation is achieved by the hyper-plane that has the largest distance to the nearest training data points of any class (so-called functional margin), since in general the larger the margin the lower the generalization error of the classifier.

**SVC**

Given training vectors \(x_i \in \mathbb{R}^p, i=1,\ldots, n\), in two classes, and a vector \(y \in \{1, -1\}^n\), SVC solves the following primal problem:

\[
\min_{w,b,\zeta} \frac{1}{2} w^T w + C \sum_{i=1}^{n} \zeta_i \\
\text{subject to } y_i(w^T \phi(x_i) + b) \geq 1 - \zeta_i, \\
\zeta_i \geq 0, i = 1, \ldots, n
\]

Its dual is

\[
\min_{\alpha} \frac{1}{2} \alpha^T Q \alpha - c^T \alpha \\
\text{subject to } y^T \alpha = 0 \\
0 \leq \alpha_i \leq C, i = 1, \ldots, n
\]
where \( e \) is the vector of all ones, \( C > 0 \) is the upper bound, \( Q \) is an \( n \) by \( n \) positive semidefinite matrix, \( Q_{ij} \equiv y_i y_j K(x_i,x_j) \), where \( K(x_i,x_j) = \phi(x_i)^T \phi(x_j) \) is the kernel. Here training vectors are implicitly mapped into a higher (maybe infinite) dimensional space by the function \( \phi \).

The decision function is:

\[
\text{sgn}\left( \sum_{i=1}^{n} y_i \alpha_i K(x_i, x) + \rho \right)
\]

Note: While SVM models derived from libsvm and liblinear use \( C \) as regularization parameter, most other estimators use alpha. The exact equivalence between the amount of regularization of two models depends on the exact objective function optimized by the model. For example, when the estimator used is sklearn.linear_model.Ridge regression, the relation between them is given as \( C = \frac{1}{\alpha \text{alpha}} \).

This parameters can be accessed through the members dual_coef_ which holds the product \( y_i \alpha_i \), support_vectors_ which holds the support vectors, and intercept_ which holds the independent term \( \rho \).

References:


NuSVC

We introduce a new parameter \( \nu \) which controls the number of support vectors and training errors. The parameter \( \nu \in (0, 1] \) is an upper bound on the fraction of training errors and a lower bound of the fraction of support vectors.
It can be shown that the $\nu$-SVC formulation is a reparameterization of the $C$-SVC and therefore mathematically equivalent.

**SVR**

Given training vectors $x_i \in \mathbb{R}^p$, $i=1, \ldots, n$, and a vector $y \in \mathbb{R}^n$, $\varepsilon$-SVR solves the following primal problem:

$$
\min_{w, b, \zeta, \zeta^*} \frac{1}{2} w^T w + C \sum_{i=1}^{n} (\zeta_i + \zeta_i^*)
$$

subject to

$$
y_i - w^T \phi(x_i) - b \leq \varepsilon + \zeta_i,
$$

$$
w^T \phi(x_i) + b - y_i \leq \varepsilon + \zeta_i^*,
$$

$$
\zeta_i, \zeta_i^* \geq 0, i = 1, \ldots, n
$$

Its dual is

$$
\min_{\alpha, \alpha^*} \frac{1}{2} (\alpha - \alpha^*)^T Q (\alpha - \alpha^*) + \varepsilon e^T (\alpha + \alpha^*) - y^T (\alpha - \alpha^*)
$$

subject to $e^T (\alpha - \alpha^*) = 0$

$$
0 \leq \alpha_i, \alpha_i^* \leq C, i = 1, \ldots, n
$$

where $e$ is the vector of all ones, $C > 0$ is the upper bound, $Q$ is an $n$ by $n$ positive semidefinite matrix, $Q_{ij} = K(x_i, x_j) = \phi(x_i)^T \phi(x_j)$ is the kernel. Here training vectors are implicitly mapped into a higher (maybe infinite) dimensional space by the function $\phi$.

The decision function is:

$$
\sum_{i=1}^{n} (\alpha_i - \alpha_i^*) K(x_i, x) + \rho
$$

These parameters can be accessed through the members `dual_coef_` which holds the difference $\alpha_i - \alpha_i^*$, `support_vectors_` which holds the support vectors, and `intercept_` which holds the independent term $\rho$.

**References:**


**Implementation details**

Internally, we use `libsvm` and `liblinear` to handle all computations. These libraries are wrapped using C and Cython.

**References:**

For a description of the implementation and details of the algorithms used, please refer to

- LIBSVM: A Library for Support Vector Machines.
- LIBLINEAR – A Library for Large Linear Classification.
3.1.5 Stochastic Gradient Descent

Stochastic Gradient Descent (SGD) is a simple yet very efficient approach to discriminative learning of linear classifiers under convex loss functions such as (linear) Support Vector Machines and Logistic Regression. Even though SGD has been around in the machine learning community for a long time, it has received a considerable amount of attention just recently in the context of large-scale learning.

SGD has been successfully applied to large-scale and sparse machine learning problems often encountered in text classification and natural language processing. Given that the data is sparse, the classifiers in this module easily scale to problems with more than $10^5$ training examples and more than $10^5$ features.

The advantages of Stochastic Gradient Descent are:

- Efficiency.
- Ease of implementation (lots of opportunities for code tuning).

The disadvantages of Stochastic Gradient Descent include:

- SGD requires a number of hyperparameters such as the regularization parameter and the number of iterations.
- SGD is sensitive to feature scaling.

Classification

**Warning:** Make sure you permute (shuffle) your training data before fitting the model or use `shuffle=True` to shuffle after each iteration.

The class `SGDClassifier` implements a plain stochastic gradient descent learning routine which supports different loss functions and penalties for classification.
As other classifiers, SGD has to be fitted with two arrays: an array X of size [n_samples, n_features] holding the training samples, and an array Y of size [n_samples] holding the target values (class labels) for the training samples:

```python
>>> from sklearn.linear_model import SGDClassifier
>>> X = [[0., 0.], [1., 1.]]
>>> y = [0, 1]
>>> clf = SGDClassifier(loss="hinge", penalty="l2", max_iter=5)
>>> clf.fit(X, y)
SGDClassifier(alpha=0.0001, average=False, class_weight=None, epsilon=0.1, eta0=0.0, fit_intercept=True, l1_ratio=0.15, learning_rate='optimal', loss='hinge', max_iter=5, n_iter=None, n_jobs=1, penalty='l2', power_t=0.5, random_state=None, shuffle=True, tol=None, verbose=0, warm_start=False)
```

After being fitted, the model can then be used to predict new values:

```python
>>> clf.predict([[2., 2.]])
array([1])
```

SGD fits a linear model to the training data. The member `coef_` holds the model parameters:

```python
>>> clf.coef_
array([[ 9.9..., 9.9...]])
```

Member `intercept_` holds the intercept (aka offset or bias):

```python
>>> clf.intercept_
array([-9.9...])
```

Whether or not the model should use an intercept, i.e. a biased hyperplane, is controlled by the parameter `fit_intercept`.

To get the signed distance to the hyperplane use `SGDClassifier.decision_function`:

```python
>>> clf.decision_function([[2., 2.]])
array([ 29.6...])
```

The concrete loss function can be set via the `loss` parameter. `SGDClassifier` supports the following loss functions:

- `loss="hinge"`: (soft-margin) linear Support Vector Machine,
- `loss="modified_huber"`: smoothed hinge loss,
- `loss="log"`: logistic regression,
- and all regression losses below.

The first two loss functions are lazy, they only update the model parameters if an example violates the margin constraint, which makes training very efficient and may result in sparser models, even when L2 penalty is used.

Using `loss="log"` or `loss="modified_huber"` enables the `predict_proba` method, which gives a vector of probability estimates $P(y|x)$ per sample $x$:

```python
>>> clf = SGDClassifier(loss="log", max_iter=5).fit(X, y)
>>> clf.predict_proba([[1., 1.]])
array([[ 0.00..., 0.99...]])
```

The concrete penalty can be set via the `penalty` parameter. SGD supports the following penalties:

- `penalty="l2"`: L2 norm penalty on `coef_`.
• **penalty="l1"**: L1 norm penalty on \( \text{coef}_\text{.} \).
• **penalty="elasticnet"**: Convex combination of L2 and L1: \((1 - l1\_\text{ratio}) \times \text{L2} + l1\_\text{ratio} \times \text{L1.}\)

The default setting is **penalty="l2"**. The L1 penalty leads to sparse solutions, driving most coefficients to zero. The Elastic Net solves some deficiencies of the L1 penalty in the presence of highly correlated attributes. The parameter **l1\_\text{ratio}** controls the convex combination of L1 and L2 penalty.

**SGDClassifier** supports multi-class classification by combining multiple binary classifiers in a “one versus all” (OVA) scheme. For each of the \( K \) classes, a binary classifier is learned that discriminates between that and all other \( K - 1 \) classes. At testing time, we compute the confidence score (i.e. the signed distances to the hyperplane) for each classifier and choose the class with the highest confidence. The Figure below illustrates the OVA approach on the iris dataset. The dashed lines represent the three OVA classifiers; the background colors show the decision surface induced by the three classifiers.

In the case of multi-class classification **coef\_** is a two-dimensionally array of shape=[\( n\_\text{classes}, n\_\text{features} \)] and **intercept\_** is a one dimensional array of shape=[\( n\_\text{classes} \)]. The i-th row of **coef\_** holds the weight vector of the OVA classifier for the i-th class; classes are indexed in ascending order (see attribute **classes\_**). Note that, in principle, since they allow to create a probability model, **loss="log"** and **loss="modified\_huber"** are more suitable for one-vs-all classification.

**SGDClassifier** supports both weighted classes and weighted instances via the fit parameters **class\_weight** and **sample\_weight**. See the examples below and the doc string of **SGDClassifier.fit** for further information.

**Examples:**

- **SGD**: Maximum margin separating hyperplane,
- **Plot multi-class SGD on the iris dataset**
- **SGD**: Weighted samples
SGDClassifier supports averaged SGD (ASGD). Averaging can be enabled by setting `average=True`. ASGD works by averaging the coefficients of the plain SGD over each iteration over a sample. When using ASGD the learning rate can be larger and even constant leading on some datasets to a speed up in training time.

For classification with a logistic loss, another variant of SGD with an averaging strategy is available with Stochastic Average Gradient (SAG) algorithm, available as a solver in LogisticRegression.

Regression

The class SGDRegressor implements a plain stochastic gradient descent learning routine which supports different loss functions and penalties to fit linear regression models. SGDRegressor is well suited for regression problems with a large number of training samples (> 10.000), for other problems we recommend Ridge, Lasso, or ElasticNet.

The concrete loss function can be set via the loss parameter. SGDRegressor supports the following loss functions:

- `loss="squared_loss"`: Ordinary least squares,
- `loss="huber"`: Huber loss for robust regression,
- `loss="epsilon_insensitive"`: linear Support Vector Regression.

The Huber and epsilon-insensitive loss functions can be used for robust regression. The width of the insensitive region has to be specified via the parameter epsilon. This parameter depends on the scale of the target variables.

SGDRegressor supports averaged SGD as SGDClassifier. Averaging can be enabled by setting `average=True`.

For regression with a squared loss and a l2 penalty, another variant of SGD with an averaging strategy is available with Stochastic Average Gradient (SAG) algorithm, available as a solver in Ridge.

Stochastic Gradient Descent for sparse data

**Note:** The sparse implementation produces slightly different results than the dense implementation due to a shrunk learning rate for the intercept.

There is built-in support for sparse data given in any matrix in a format supported by scipy.sparse. For maximum efficiency, however, use the CSR matrix format as defined in scipy.sparse.csr_matrix.

Examples:

- Classification of text documents using sparse features

Complexity

The major advantage of SGD is its efficiency, which is basically linear in the number of training examples. If X is a matrix of size (n, p) training has a cost of $O(knp)$, where k is the number of iterations (epochs) and $\bar{p}$ is the average number of non-zero attributes per sample.
Recent theoretical results, however, show that the runtime to get some desired optimization accuracy does not increase as the training set size increases.

**Tips on Practical Use**

- Stochastic Gradient Descent is sensitive to feature scaling, so it is highly recommended to scale your data. For example, scale each attribute on the input vector X to [0,1] or [-1,+1], or standardize it to have mean 0 and variance 1. Note that the same scaling must be applied to the test vector to obtain meaningful results. This can be easily done using `StandardScaler`:

```python
from sklearn.preprocessing import StandardScaler
scaler = StandardScaler()
scaler.fit(X_train)  # Don't cheat - fit only on training data
X_train = scaler.transform(X_train)
X_test = scaler.transform(X_test)  # apply same transformation to test data
```

If your attributes have an intrinsic scale (e.g. word frequencies or indicator features) scaling is not needed.

- Finding a reasonable regularization term $\alpha$ is best done using `GridSearchCV`, usually in the range $10^{-\text{np.arange}(1,7)}$.

- Empirically, we found that SGD converges after observing approx. $10^6$ training samples. Thus, a reasonable first guess for the number of iterations is $n_{\text{iter}} = \text{np.ceil}(10^6 / n)$, where $n$ is the size of the training set.

- If you apply SGD to features extracted using PCA we found that it is often wise to scale the feature values by some constant $c$ such that the average L2 norm of the training data equals one.

- We found that Averaged SGD works best with a larger number of features and a higher `eta0`

**References:**


**Mathematical formulation**

Given a set of training examples $(x_1, y_1, \ldots, (x_n, y_n)$ where $x_i \in \mathbb{R}^m$ and $y_i \in \{-1, 1\}$, our goal is to learn a linear scoring function $f(x) = w^T x + b$ with model parameters $w \in \mathbb{R}^m$ and intercept $b \in \mathbb{R}$. In order to make predictions, we simply look at the sign of $f(x)$. A common choice to find the model parameters is by minimizing the regularized training error given by

$$E(w, b) = \frac{1}{n} \sum_{i=1}^{n} L(y_i, f(x_i)) + \alpha R(w)$$

where $L$ is a loss function that measures model (mis)fit and $R$ is a regularization term (aka penalty) that penalizes model complexity; $\alpha > 0$ is a non-negative hyperparameter.

Different choices for $L$ entail different classifiers such as

- Hinge: (soft-margin) Support Vector Machines.
- Log: Logistic Regression.
- Least-Squares: Ridge Regression.
- Epsilon-Insensitive: (soft-margin) Support Vector Regression.
All of the above loss functions can be regarded as an upper bound on the misclassification error (Zero-one loss) as shown in the Figure below.

Popular choices for the regularization term $R$ include:

- L2 norm: $R(w) := \frac{1}{2} \sum_{i=1}^{n} w_i^2$.
- L1 norm: $R(w) := \sum_{i=1}^{n} |w_i|$, which leads to sparse solutions.
- Elastic Net: $R(w) := \rho \frac{1}{2} \sum_{i=1}^{n} w_i^2 + (1 - \rho) \sum_{i=1}^{n} |w_i|$, a convex combination of L2 and L1, where $\rho$ is given by $1 - \text{l1_ratio}$.

The Figure below shows the contours of the different regularization terms in the parameter space when $R(w) = 1$.

**SGD**

Stochastic gradient descent is an optimization method for unconstrained optimization problems. In contrast to (batch) gradient descent, SGD approximates the true gradient of $E(w, b)$ by considering a single training example at a time.

The class `SGDClassifier` implements a first-order SGD learning routine. The algorithm iterates over the training examples and for each example updates the model parameters according to the update rule given by

$$w \leftarrow w - \eta(\alpha \frac{\partial R(w)}{\partial w} + \frac{\partial L(w^T x_i + b, y_i)}{\partial w})$$

where $\eta$ is the learning rate which controls the step-size in the parameter space. The intercept $b$ is updated similarly but without regularization.

The learning rate $\eta$ can be either constant or gradually decaying. For classification, the default learning rate schedule (`learning_rate='optimal'`) is given by

$$\eta(t) = \frac{1}{\alpha(t_0 + t)}$$
where \( t \) is the time step (there are a total of \( n_{\text{samples}} \times n_{\text{iter}} \) time steps), \( t_0 \) is determined based on a heuristic proposed by Léon Bottou such that the expected initial updates are comparable with the expected size of the weights (this assuming that the norm of the training samples is approx. 1). The exact definition can be found in \_init\_t in BaseSGD.

For regression the default learning rate schedule is inverse scaling (\texttt{learning\_rate='invscaling'}, given by

\[
\eta(t) = \frac{\eta_0}{t^{\text{power}_t}}
\]

where \( \eta_0 \) and \( \text{power}_t \) are hyperparameters chosen by the user via \texttt{eta0} and \texttt{power_t}, resp.

For a constant learning rate use \texttt{learning\_rate='constant'} and use \texttt{eta0} to specify the learning rate.

The model parameters can be accessed through the members \texttt{coef\_} and \texttt{intercept\_}:

- Member \texttt{coef\_} holds the weights \( w \)
- Member \texttt{intercept\_} holds \( b \)

References:
- “Towards Optimal One Pass Large Scale Learning with Averaged Stochastic Gradient Descent” Xu, Wei

Implementation details

The implementation of SGD is influenced by the Stochastic Gradient SVM of Léon Bottou. Similar to SvmSGD, the weight vector is represented as the product of a scalar and a vector which allows an efficient weight update in
the case of L2 regularization. In the case of sparse feature vectors, the intercept is updated with a smaller learning rate (multiplied by 0.01) to account for the fact that it is updated more frequently. Training examples are picked up sequentially and the learning rate is lowered after each observed example. We adopted the learning rate schedule from Shalev-Shwartz et al. 2007. For multi-class classification, a “one versus all” approach is used. We use the truncated gradient algorithm proposed by Tsuruoka et al. 2009 for L1 regularization (and the Elastic Net). The code is written in Cython.

References:

- “Pegasos: Primal estimated sub-gradient solver for svm” S. Shalev-Shwartz, Y. Singer, N. Srebro - In Proceedings of ICML ‘07.

3.1.6 Nearest Neighbors

`sklearn.neighbors` provides functionality for unsupervised and supervised neighbors-based learning methods. Unsupervised nearest neighbors is the foundation of many other learning methods, notably manifold learning and spectral clustering. Supervised neighbors-based learning comes in two flavors: classification for data with discrete labels, and regression for data with continuous labels.

The principle behind nearest neighbor methods is to find a predefined number of training samples closest in distance to the new point, and predict the label from these. The number of samples can be a user-defined constant (k-nearest neighbor learning), or vary based on the local density of points (radius-based neighbor learning). The distance can, in general, be any metric measure: standard Euclidean distance is the most common choice. Neighbors-based methods are known as non-generalizing machine learning methods, since they simply “remember” all of its training data (possibly transformed into a fast indexing structure such as a Ball Tree or KD Tree).

Despite its simplicity, nearest neighbors has been successful in a large number of classification and regression problems, including handwritten digits or satellite image scenes. Being a non-parametric method, it is often successful in classification situations where the decision boundary is very irregular.

The classes in `sklearn.neighbors` can handle either Numpy arrays or `scipy.sparse` matrices as input. For dense matrices, a large number of possible distance metrics are supported. For sparse matrices, arbitrary Minkowski metrics are supported for searches.

There are many learning routines which rely on nearest neighbors at their core. One example is kernel density estimation, discussed in the density estimation section.

Unsupervised Nearest Neighbors

`NearestNeighbors` implements unsupervised nearest neighbors learning. It acts as a uniform interface to three different nearest neighbors algorithms: `BallTree`, `KDTree`, and a brute-force algorithm based on routines in `sklearn.metrics.pairwise`. The choice of neighbors search algorithm is controlled through the keyword 'algorithm', which must be one of ['auto', 'ball_tree', 'kd_tree', 'brute']. When the default value 'auto' is passed, the algorithm attempts to determine the best approach from the training data. For a discussion of the strengths and weaknesses of each option, see Nearest Neighbor Algorithms.
Finding the Nearest Neighbors

For the simple task of finding the nearest neighbors between two sets of data, the unsupervised algorithms within `sklearn.neighbors` can be used:

```python
>>> from sklearn.neighbors import NearestNeighbors
>>> import numpy as np

>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])

>>> nbrs = NearestNeighbors(n_neighbors=2, algorithm='ball_tree').fit(X)

>>> distances, indices = nbrs.kneighbors(X)

>>> indices
array([[0, 1],
       [1, 0],
       [2, 1],
       [3, 4],
       [4, 3],
       [5, 4]])

>>> distances
array([[0., 1.],
       [0., 1.],
       [0., 1.41421356],
       [0., 1.],
       [0., 1.],
       [0., 1.41421356]])

Because the query set matches the training set, the nearest neighbor of each point is the point itself, at a distance of zero.

It is also possible to efficiently produce a sparse graph showing the connections between neighboring points:

```python
>>> nbrs.kneighbors_graph(X).toarray()
```

```
array([[1., 1., 0., 0., 0., 0.],
       [1., 1., 0., 0., 0., 0.],
       [0., 1., 0., 0., 0., 0.],
       [0., 0., 1., 1., 0., 0.],
       [0., 0., 0., 1., 1., 0.],
       [0., 0., 0., 0., 1., 1.]])
```

Our dataset is structured such that points nearby in index order are nearby in parameter space, leading to an approximately block-diagonal matrix of K-nearest neighbors. Such a sparse graph is useful in a variety of circumstances which make use of spatial relationships between points for unsupervised learning; in particular, see `sklearn.manifold.Isomap`, `sklearn.manifold.LocallyLinearEmbedding`, and `sklearn.cluster.SpectralClustering`.

KDTree and BallTree Classes

Alternatively, one can use the `KDTree` or `BallTree` classes directly to find nearest neighbors. This is the functionality wrapped by the `NearestNeighbors` class used above. The Ball Tree and KD Tree have the same interface; we’ll show an example of using the KD Tree here:
Refer to the `KDTree` and `BallTree` class documentation for more information on the options available for neighbors searches, including specification of query strategies, of various distance metrics, etc. For a list of available metrics, see the documentation of the `DistanceMetric` class.

### Nearest Neighbors Classification

Neighbors-based classification is a type of instance-based learning or non-generalizing learning: it does not attempt to construct a general internal model, but simply stores instances of the training data. Classification is computed from a simple majority vote of the nearest neighbors of each point: a query point is assigned the data class which has the most representatives within the nearest neighbors of the point.

scikit-learn implements two different nearest neighbors classifiers: `KNeighborsClassifier` implements learning based on the $k$ nearest neighbors of each query point, where $k$ is an integer value specified by the user. `RadiusNeighborsClassifier` implements learning based on the number of neighbors within a fixed radius $r$ of each training point, where $r$ is a floating-point value specified by the user.

The $k$-neighbors classification in `KNeighborsClassifier` is the more commonly used of the two techniques. The optimal choice of the value $k$ is highly data-dependent: in general a larger $k$ suppresses the effects of noise, but makes the classification boundaries less distinct.

In cases where the data is not uniformly sampled, radius-based neighbors classification in `RadiusNeighborsClassifier` can be a better choice. The user specifies a fixed radius $r$, such that points in sparser neighborhoods use fewer nearest neighbors for the classification. For high-dimensional parameter spaces, this method becomes less effective due to the so-called “curse of dimensionality”.

The basic nearest neighbors classification uses uniform weights: that is, the value assigned to a query point is computed from a simple majority vote of the nearest neighbors. Under some circumstances, it is better to weight the neighbors such that nearer neighbors contribute more to the fit. This can be accomplished through the `weights` keyword. The default value, `weights = 'uniform'`, assigns uniform weights to each neighbor. `weights = 'distance'` assigns weights proportional to the inverse of the distance from the query point. Alternatively, a user-defined function of the distance can be supplied which is used to compute the weights.
Examples:

- Nearest Neighbors Classification: an example of classification using nearest neighbors.

Nearest Neighbors Regression

Neighbors-based regression can be used in cases where the data labels are continuous rather than discrete variables. The label assigned to a query point is computed based on the mean of the labels of its nearest neighbors.

scikit-learn implements two different neighbors regressors: `KNeighborsRegressor` implements learning based on the $k$ nearest neighbors of each query point, where $k$ is an integer value specified by the user. `RadiusNeighborsRegressor` implements learning based on the neighbors within a fixed radius $r$ of the query point, where $r$ is a floating-point value specified by the user.

The basic nearest neighbors regression uses uniform weights: that is, each point in the local neighborhood contributes uniformly to the classification of a query point. Under some circumstances, it can be advantageous to weight points such that nearby points contribute more to the regression than faraway points. This can be accomplished through the `weights` keyword. The default value, `weights = 'uniform'`, assigns equal weights to all points. `weights = 'distance'` assigns weights proportional to the inverse of the distance from the query point. Alternatively, a user-defined function of the distance can be supplied, which will be used to compute the weights.

The use of multi-output nearest neighbors for regression is demonstrated in `Face completion with a multi-output estimators`. In this example, the inputs X are the pixels of the upper half of faces and the outputs Y are the pixels of the lower half of those faces.

Examples:

- Nearest Neighbors regression: an example of regression using nearest neighbors.
- Face completion with a multi-output estimators: an example of multi-output regression using nearest neighbors.
Nearest Neighbor Algorithms

Brute Force

Fast computation of nearest neighbors is an active area of research in machine learning. The most naive neighbor search implementation involves the brute-force computation of distances between all pairs of points in the dataset: for \( N \) samples in \( D \) dimensions, this approach scales as \( O[N^2] \). Efficient brute-force neighbors searches can be very competitive for small data samples. However, as the number of samples \( N \) grows, the brute-force approach quickly becomes infeasible. In the classes within \texttt{sklearn.neighbors}, brute-force neighbors searches are specified using the keyword \texttt{algorithm = 'brute'}, and are computed using the routines available in \texttt{sklearn.metrics.pairwise}.

K-D Tree

To address the computational inefficiencies of the brute-force approach, a variety of tree-based data structures have been invented. In general, these structures attempt to reduce the required number of distance calculations by efficiently encoding aggregate distance information for the sample. The basic idea is that if point \( A \) is very distant from point \( B \), and point \( B \) is very close to point \( C \), then we know that points \( A \) and \( C \) are very distant, \textit{without having to explicitly calculate their distance}. In this way, the computational cost of a nearest neighbors search can be reduced to \( O[D \log(N)] \) or better. This is a significant improvement over brute-force for large \( N \).

An early approach to taking advantage of this aggregate information was the \textit{KD tree} data structure (short for \textit{K-dimensional tree}), which generalizes two-dimensional \textit{Quad-trees} and 3-dimensional \textit{Oct-trees} to an arbitrary number of dimensions. The KD tree is a binary tree structure which recursively partitions the parameter space along the data axes, dividing it into nested orthotropic regions into which data points are filed. The construction of a KD tree is very fast: because partitioning is performed only along the data axes, no \( D \)-dimensional distances need to be computed. Once constructed, the nearest neighbor of a query point can be determined with only \( O[\log(N)] \) distance computations. Though the KD tree approach is very fast for low-dimensional (\( D < 20 \)) neighbors searches, it becomes inefficient as \( D \) grows very large: this is one manifestation of the so-called “curse of dimensionality”. In scikit-learn, KD tree
Face completion with multi-output estimators

true faces  Extra trees  K-nn  Linear regression  Ridge
neighbors searches are specified using the keyword `algorithm = 'kd_tree'`, and are computed using the class `KDTree`.

**References:**

- “Multidimensional binary search trees used for associative searching”, Bentley, J.L., Communications of the ACM (1975)

**Ball Tree**

To address the inefficiencies of KD Trees in higher dimensions, the ball tree data structure was developed. Where KD trees partition data along Cartesian axes, ball trees partition data in a series of nesting hyper-spheres. This makes tree construction more costly than that of the KD tree, but results in a data structure which can be very efficient on highly-structured data, even in very high dimensions.

A ball tree recursively divides the data into nodes defined by a centroid $C$ and radius $r$, such that each point in the node lies within the hyper-sphere defined by $r$ and $C$. The number of candidate points for a neighbor search is reduced through use of the triangle inequality:

$$|x + y| \leq |x| + |y|$$

With this setup, a single distance calculation between a test point and the centroid is sufficient to determine a lower and upper bound on the distance to all points within the node. Because of the spherical geometry of the ball tree nodes, it can out-perform a KD-tree in high dimensions, though the actual performance is highly dependent on the structure of the training data. In scikit-learn, ball-tree-based neighbors searches are specified using the keyword `algorithm = 'ball_tree'`, and are computed using the class `sklearn.neighbors.BallTree`. Alternatively, the user can work with the `BallTree` class directly.

**References:**


**Choice of Nearest Neighbors Algorithm**

The optimal algorithm for a given dataset is a complicated choice, and depends on a number of factors:

- number of samples $N$ (i.e. `n_samples`) and dimensionality $D$ (i.e. `n_features`).
  - **Brute force** query time grows as $O[DN]$
  - **Ball tree** query time grows as approximately $O[D \log(N)]$
  - **KD tree** query time changes with $D$ in a way that is difficult to precisely characterise. For small $D$ (less than 20 or so) the cost is approximately $O[D \log(N)]$, and the KD tree query can be very efficient. For larger $D$, the cost increases to nearly $O[DN]$, and the overhead due to the tree structure can lead to queries which are slower than brute force.

For small data sets ($N$ less than 30 or so), $\log(N)$ is comparable to $N$, and brute force algorithms can be more efficient than a tree-based approach. Both `KDTree` and `BallTree` address this through providing a `leaf size` parameter: this controls the number of samples at which a query switches to brute-force. This allows both algorithms to approach the efficiency of a brute-force computation for small $N$. 

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• data structure: *intrinsic dimensionality* of the data and/or *sparsity* of the data. Intrinsic dimensionality refers to the dimension $d \leq D$ of a manifold on which the data lies, which can be linearly or non-linearly embedded in the parameter space. Sparsity refers to the degree to which the data fills the parameter space (this is to be distinguished from the concept as used in “sparse” matrices. The data matrix may have no zero entries, but the structure can still be “sparse” in this sense).

  – *Brute force* query time is unchanged by data structure.

  – *Ball tree* and *KD tree* query times can be greatly influenced by data structure. In general, sparser data with a smaller intrinsic dimensionality leads to faster query times. Because the KD tree internal representation is aligned with the parameter axes, it will not generally show as much improvement as ball tree for arbitrarily structured data.

Datasets used in machine learning tend to be very structured, and are very well-suited for tree-based queries.

• number of neighbors $k$ requested for a query point.

  – *Brute force* query time is largely unaffected by the value of $k$

  – *Ball tree* and *KD tree* query time will become slower as $k$ increases. This is due to two effects: first, a larger $k$ leads to the necessity to search a larger portion of the parameter space. Second, using $k > 1$ requires internal queueing of results as the tree is traversed.

As $k$ becomes large compared to $N$, the ability to prune branches in a tree-based query is reduced. In this situation, Brute force queries can be more efficient.

• number of query points. Both the ball tree and the KD Tree require a construction phase. The cost of this construction becomes negligible when amortized over many queries. If only a small number of queries will be performed, however, the construction can make up a significant fraction of the total cost. If very few query points will be required, brute force is better than a tree-based method.

Currently, `algorithm = 'auto'` selects 'kd_tree' if $k < N/2$ and the 'effective_metric_' is in the 'VALID_METRICS' list of 'kd_tree'. It selects 'ball_tree' if $k < N/2$ and the 'effective_metric_' is in the 'VALID_METRICS' list of 'ball_tree'. It selects 'brute' if $k < N/2$ and the 'effective_metric_' is not in the 'VALID_METRICS' list of 'kd_tree' or 'ball_tree'. It selects 'brute' if $k \geq N/2$. This choice is based on the assumption that the number of query points is at least the same order as the number of training points, and that `leaf_size` is close to its default value of 30.

**Effect of leaf_size**

As noted above, for small sample sizes a brute force search can be more efficient than a tree-based query. This fact is accounted for in the ball tree and KD tree by internally switching to brute force searches within leaf nodes. The level of this switch can be specified with the parameter `leaf_size`. This parameter choice has many effects:

**construction time** A larger `leaf_size` leads to a faster tree construction time, because fewer nodes need to be created

**query time** Both a large or small `leaf_size` can lead to suboptimal query cost. For `leaf_size` approaching 1, the overhead involved in traversing nodes can significantly slow query times. For `leaf_size` approaching the size of the training set, queries become essentially brute force. A good compromise between these is `leaf_size = 30`, the default value of the parameter.

**memory** As `leaf_size` increases, the memory required to store a tree structure decreases. This is especially important in the case of ball tree, which stores a $D$-dimensional centroid for each node. The required storage space for BallTree is approximately $1 / \text{leaf_size}$ times the size of the training set.

`leaf_size` is not referenced for brute force queries.
Nearest Centroid Classifier

The `NearestCentroid` classifier is a simple algorithm that represents each class by the centroid of its members. In effect, this makes it similar to the label updating phase of the `sklearn.KMeans` algorithm. It also has no parameters to choose, making it a good baseline classifier. It does, however, suffer on non-convex classes, as well as when classes have drastically different variances, as equal variance in all dimensions is assumed. See Linear Discriminant Analysis (```sklearn.discriminant_analysis.LinearDiscriminantAnalysis```)) and Quadratic Discriminant Analysis (```sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis```)) for more complex methods that do not make this assumption. Usage of the default `NearestCentroid` is simple:

```python
>>> from sklearn.neighbors.nearest_centroid import NearestCentroid
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])
>>> clf = NearestCentroid()
>>> clf.fit(X, y)
NearestCentroid(metric='euclidean', shrink_threshold=None)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

Nearest Shrunken Centroid

The `NearestCentroid` classifier has a `shrink_threshold` parameter, which implements the nearest shrunken centroid classifier. In effect, the value of each feature for each centroid is divided by the within-class variance of that feature. The feature values are then reduced by `shrink_threshold`. Most notably, if a particular feature value crosses zero, it is set to zero. In effect, this removes the feature from affecting the classification. This is useful, for example, for removing noisy features.

In the example below, using a small shrink threshold increases the accuracy of the model from 0.81 to 0.82.

Examples:

- **Nearest Centroid Classification**: an example of classification using nearest centroid with different shrink thresholds.
3.1.7 Gaussian Processes

Gaussian Processes (GP) are a generic supervised learning method designed to solve regression and probabilistic classification problems.

The advantages of Gaussian processes are:

- The prediction interpolates the observations (at least for regular kernels).
- The prediction is probabilistic (Gaussian) so that one can compute empirical confidence intervals and decide based on those if one should refit (online fitting, adaptive fitting) the prediction in some region of interest.
- Versatile: different kernels can be specified. Common kernels are provided, but it is also possible to specify custom kernels.

The disadvantages of Gaussian processes include:

- They are not sparse, i.e., they use the whole samples/features information to perform the prediction.
- They lose efficiency in high dimensional spaces – namely when the number of features exceeds a few dozens.

GPR with noise-level estimation

This example illustrates that GPR with a sum-kernel including a WhiteKernel can estimate the noise level of data. An illustration of the log-marginal-likelihood (LML) landscape shows that there exist two local maxima of LML.

The first corresponds to a model with a high noise level and a large length scale, which explains all variations in the data by noise.
Initial: $1 * RBF(\text{length \_scale}=100) + \text{WhiteKernel}(\text{noise \_level}=1)$
Minimum: $0.00316 * RBF(\text{length \_scale}=109) + \text{WhiteKernel}(\text{noise \_level}=0.6)$
Log-Marginal-Likelihood: $-23.872337362$
Initial: $1^2 \times \text{RBF(length scale=1)} + \text{WhiteKernel(noise level=1e-05)}$

Optimum: $0.64^2 \times \text{RBF(length scale=0.365)} + \text{WhiteKernel(noise level=0.29)}$

Log-Marginal-Likelihood: -21.8050908902
The second one has a smaller noise level and shorter length scale, which explains most of the variation by the noise-free functional relationship. The second model has a higher likelihood; however, depending on the initial value for the hyperparameters, the gradient-based optimization might also converge to the high-noise solution. It is thus important to repeat the optimization several times for different initializations.

**Comparison of GPR and Kernel Ridge Regression**

Both kernel ridge regression (KRR) and GPR learn a target function by employing internally the “kernel trick”. KRR learns a linear function in the space induced by the respective kernel which corresponds to a non-linear function in the original space. The linear function in the kernel space is chosen based on the mean-squared error loss with ridge regularization. GPR uses the kernel to define the covariance of a prior distribution over the target functions and uses the observed training data to define a likelihood function. Based on Bayes theorem, a (Gaussian) posterior distribution over target functions is defined, whose mean is used for prediction.

A major difference is that GPR can choose the kernel’s hyperparameters based on gradient-ascent on the marginal likelihood function while KRR needs to perform a grid search on a cross-validated loss function (mean-squared error loss). A further difference is that GPR learns a generative, probabilistic model of the target function and can thus provide meaningful confidence intervals and posterior samples along with the predictions while KRR only provides predictions.

The following figure illustrates both methods on an artificial dataset, which consists of a sinusoidal target function and strong noise. The figure compares the learned model of KRR and GPR based on a ExpSineSquared kernel, which is suited for learning periodic functions. The kernel’s hyperparameters control the smoothness (length_scale)
and periodicity of the kernel (periodicity). Moreover, the noise level of the data is learned explicitly by GPR by an additional WhiteKernel component in the kernel and by the regularization parameter alpha of KRR.

The figure shows that both methods learn reasonable models of the target function. GPR correctly identifies the periodicity of the function to be roughly $2 \pi$ (6.28), while KRR chooses the doubled periodicity $4 \pi$. Besides that, GPR provides reasonable confidence bounds on the prediction which are not available for KRR. A major difference between the two methods is the time required for fitting and predicting: while fitting KRR is fast in principle, the grid-search for hyperparameter optimization scales exponentially with the number of hyperparameters (“curse of dimensionality”). The gradient-based optimization of the parameters in GPR does not suffer from this exponential scaling and is thus considerably faster on this example with 3-dimensional hyperparameter space. The time for predicting is similar; however, generating the variance of the predictive distribution of GPR takes considerably longer than just predicting the mean.

**GPR on Mauna Loa CO2 data**

This example is based on Section 5.4.3 of [RW2006]. It illustrates an example of complex kernel engineering and hyperparameter optimization using gradient ascent on the log-marginal-likelihood. The data consists of the monthly average atmospheric CO2 concentrations (in parts per million by volume (ppmv)) collected at the Mauna Loa Observatory in Hawaii, between 1958 and 1997. The objective is to model the CO2 concentration as a function of the time $t$.

The kernel is composed of several terms that are responsible for explaining different properties of the signal:

- a long term, smooth rising trend is to be explained by an RBF kernel. The RBF kernel with a large length-scale enforces this component to be smooth; it is not enforced that the trend is rising which leaves this choice to the GP. The specific length-scale and the amplitude are free hyperparameters.

- a seasonal component, which is to be explained by the periodic ExpSineSquared kernel with a fixed periodicity of 1 year. The length-scale of this periodic component, controlling its smoothness, is a free parameter. In order to allow decaying away from exact periodicity, the product with an RBF kernel is taken. The length-scale of this RBF component controls the decay time and is a further free parameter.

- smaller, medium term irregularities are to be explained by a RationalQuadratic kernel component, whose length-scale and alpha parameter, which determines the diffuseness of the length-scales, are to be determined. Ac-
According to [RW2006], these irregularities can better be explained by a RationalQuadratic than an RBF kernel component, probably because it can accommodate several length-scales.

- a “noise” term, consisting of an RBF kernel contribution, which shall explain the correlated noise components such as local weather phenomena, and a WhiteKernel contribution for the white noise. The relative amplitudes and the RBF’s length scale are further free parameters.

Maximizing the log-marginal-likelihood after subtracting the target’s mean yields the following kernel with an LML of -83.214:

\[
34.4 \times 2 \times \text{RBF}(\text{length\_scale}=41.8) + 3.27 \times 2 \times \text{RBF}(\text{length\_scale}=180) \times \text{ExpSineSquared}(\text{length\_scale}=1.44, \text{periodicity}=1) + 0.446 \times 2 \times \text{RationalQuadratic}(\alpha=17.7, \text{length\_scale}=0.957) + 0.197 \times 2 \times \text{RBF}(\text{length\_scale}=0.138) + \text{WhiteKernel}(\text{noise\_level}=0.0336)
\]

Thus, most of the target signal (34.4ppm) is explained by a long-term rising trend (length-scale 41.8 years). The periodic component has an amplitude of 3.27ppm, a decay time of 180 years and a length-scale of 1.44. The long decay time indicates that we have a locally very close to periodic seasonal component. The correlated noise has an amplitude of 0.197ppm with a length scale of 0.138 years and a white-noise contribution of 0.197ppm. Thus, the overall noise level is very small, indicating that the data can be very well explained by the model. The figure shows also that the model makes very confident predictions until around 2015.
Gaussian Process Classification (GPC)

The `GaussianProcessClassifier` implements Gaussian processes (GP) for classification purposes, more specifically for probabilistic classification, where test predictions take the form of class probabilities. GaussianProcessClassifier places a GP prior on a latent function $f$, which is then squashed through a link function to obtain the probabilistic classification. The latent function $f$ is a so-called nuisance function, whose values are not observed and are not relevant by themselves. Its purpose is to allow a convenient formulation of the model, and $f$ is removed (integrated out) during prediction. GaussianProcessClassifier implements the logistic link function, for which the integral cannot be computed analytically but is easily approximated in the binary case.

In contrast to the regression setting, the posterior of the latent function $f$ is not Gaussian even for a GP prior since a Gaussian likelihood is inappropriate for discrete class labels. Rather, a non-Gaussian likelihood corresponding to the logistic link function (logit) is used. GaussianProcessClassifier approximates the non-Gaussian posterior with a Gaussian based on the Laplace approximation. More details can be found in Chapter 3 of [RW2006].

The GP prior mean is assumed to be zero. The prior’s covariance is specified by a passing a `kernel` object. The hyperparameters of the kernel are optimized during fitting of GaussianProcessRegressor by maximizing the log-marginal-likelihood (LML) based on the passed `optimizer`. As the LML may have multiple local optima, the optimizer can be started repeatedly by specifying `n_restarts_optimizer`. The first run is always conducted starting from the initial hyperparameter values of the kernel; subsequent runs are conducted from hyperparameter values that have been chosen randomly from the range of allowed values. If the initial hyperparameters should be kept fixed, `None` can be passed as optimizer.

`GaussianProcessClassifier` supports multi-class classification by performing either one-versus-rest or one-versus-one based training and prediction. In one-versus-rest, one binary Gaussian process classifier is fitted for each class, which is trained to separate this class from the rest. In “one_vs_one”, one binary Gaussian process classifier is fitted for each pair of classes, which is trained to separate these two classes. The predictions of these binary predictors are combined into multi-class predictions. See the section on multi-class classification for more details.

In the case of Gaussian process classification, “one_vs_one” might be computationally cheaper since it has to solve many problems involving only a subset of the whole training set rather than fewer problems on the whole dataset. Since Gaussian process classification scales cubically with the size of the dataset, this might be considerably faster. However, note that “one_vs_one” does not support predicting probability estimates but only plain predictions. Moreover, note that `GaussianProcessClassifier` does not (yet) implement a true multi-class Laplace approximation internally, but as discussed above is based on solving several binary classification tasks internally, which are combined using one-versus-rest or one-versus-one.

**GPC examples**

**Probabilistic predictions with GPC**

This example illustrates the predicted probability of GPC for an RBF kernel with different choices of the hyperparameters. The first figure shows the predicted probability of GPC with arbitrarily chosen hyperparameters and with the hyperparameters corresponding to the maximum log-marginal-likelihood (LML).

While the hyperparameters chosen by optimizing LML have a considerable larger LML, they perform slightly worse according to the log-loss on test data. The figure shows that this is because they exhibit a steep change of the class probabilities at the class boundaries (which is good) but have predicted probabilities close to 0.5 far away from the class boundaries (which is bad) This undesirable effect is caused by the Laplace approximation used internally by GPC.

The second figure shows the log-marginal-likelihood for different choices of the kernel’s hyperparameters, highlighting the two choices of the hyperparameters used in the first figure by black dots.
Illustration of GPC on the XOR dataset

This example illustrates GPC on XOR data. Compared are a stationary, isotropic kernel (RBF) and a non-stationary kernel (DotProduct). On this particular dataset, the DotProduct kernel obtains considerably better results because the class-boundaries are linear and coincide with the coordinate axes. In practice, however, stationary kernels such as RBF often obtain better results.

Gaussian process classification (GPC) on iris dataset

This example illustrates the predicted probability of GPC for an isotropic and anisotropic RBF kernel on a two-dimensional version for the iris-dataset. This illustrates the applicability of GPC to non-binary classification. The anisotropic RBF kernel obtains slightly higher log-marginal-likelihood by assigning different length-scales to the two feature dimensions.

Kernels for Gaussian Processes

Kernels (also called “covariance functions” in the context of GPs) are a crucial ingredient of GPs which determine the shape of prior and posterior of the GP. They encode the assumptions on the function being learned by defining the “similarity” of two datapoints combined with the assumption that similar datapoints should have similar target values. Two categories of kernels can be distinguished: stationary kernels depend only on the distance of two datapoints and not on their absolute values \( k(x_i, x_j) = k(d(x_i, x_j)) \) and are thus invariant to translations in the input space, while non-stationary kernels depend also on the specific values of the datapoints. Stationary kernels can further be subdivided into isotropic and anisotropic kernels, where isotropic kernels are also invariant to rotations in the input space. For more details, we refer to Chapter 4 of [RW2006].

Gaussian Process Kernel API

The main usage of a Kernel is to compute the GP’s covariance between datapoints. For this, the method __call__ of the kernel can be called. This method can either be used to compute the “auto-covariance” of all pairs of datapoints
in a 2d array X, or the “cross-covariance” of all combinations of datapoints of a 2d array X with datapoints in a 2d array Y. The following identity holds true for all kernels k (except for the WhiteKernel): k(X) == K(X, Y=X)

If only the diagonal of the auto-covariance is being used, the method diag() of a kernel can be called, which is more computationally efficient than the equivalent call to __call__: np.diag(k(X, X)) == k.diag(X)

Kernels are parameterized by a vector θ of hyperparameters. These hyperparameters can for instance control length-scales or periodicity of a kernel (see below). All kernels support computing analytic gradients of of the kernel’s auto-covariance with respect to θ via setting eval_gradient=True in the __call__ method. This gradient is used by the Gaussian process (both regressor and classifier) in computing the gradient of the log-marginal-likelihood, which in turn is used to determine the value of θ, which maximizes the log-marginal-likelihood, via gradient ascent. For each hyperparameter, the initial value and the bounds need to be specified when creating an instance of the kernel. The current value of θ can be get and set via the property theta of the kernel object. Moreover, the bounds of the hyperparameters can be accessed by the property bounds of the kernel. Note that both properties (theta and bounds) return log-transformed values of the internally used values since those are typically more amenable to gradient-based optimization. The specification of each hyperparameter is stored in the form of an instance of Hyperparameter in the respective kernel. Note that a kernel using a hyperparameter with name “x” must have the attributes self.x and self.x_bounds.

The abstract base class for all kernels is Kernel. Kernel implements a similar interface as Estimator, providing the methods get_params(), set_params(), and clone(). This allows setting kernel values also via meta-estimators such as Pipeline or GridSearch. Note that due to the nested structure of kernels (by applying kernel operators, see below), the names of kernel parameters might become relatively complicated. In general, for a binary kernel operator, parameters of the left operand are prefixed with k1__ and parameters of the right operand with k2__.

An additional convenience method is clone_with_theta(theta), which returns a cloned version of the kernel but with the hyperparameters set to theta. An illustrative example:

```python
>>> from sklearn.gaussian_process.kernels import ConstantKernel, RBF
>>> kernel = ConstantKernel(constant_value=1.0, constant_value_bounds=(0.0, 10.0)) *
|   | RBF(length_scale=0.5, length_scale_bounds=(0.0, 10.0)) + RBF(length_scale=2.0,
|   | length_scale_bounds=(0.0, 10.0))
>>> for hyperparameter in kernel.hyperparameters: print(hyperparameter)
Hyperparameter(name='k1__k1__constant_value', value_type='numeric', bounds=array([[ 0., 10.]]), n_elements=1, fixed=False)
Hyperparameter(name='k1__k2__length_scale', value_type='numeric', bounds=array([[ 0., 10.]]), n_elements=1, fixed=False)
```
Hyperparameter(name='k2__length_scale', value_type='numeric', bounds=array([[ 0., -10.]]), n_elements=1, fixed=False)

```python
>>> params = kernel.get_params()

>>> for key in sorted(params): print("%s : %s" % (key, params[key]))
  k1 : 1**2 * RBF(length_scale=0.5)
  k1__k1 : 1**2
  k1__k1__constant_value : 1.0
  k1__k1__constant_value_bounds : (0.0, 10.0)
  k1__k2 : RBF(length_scale=0.5)
  k1__k2__length_scale : 0.5
  k1__k2__length_scale_bounds : (0.0, 10.0)
  k2 : RBF(length_scale=2)
  k2__length_scale : 2.0
  k2__length_scale_bounds : (0.0, 10.0)
```

```python
>>> print(kernel.theta)  # Note: log-transformed
[ 0.  -0.69314718  0.69314718]
```

```python
>>> print(kernel.bounds)  # Note: log-transformed
[[ -inf  2.30258509]
 [ -inf  2.30258509]
 [ -inf  2.30258509]]
```

All Gaussian process kernels are interoperable with `sklearn.metrics.pairwise` and vice versa: instances of subclasses of `Kernel` can be passed as `metric` to `pairwise_kernels`` from `sklearn.metrics.pairwise`. Moreover, kernel functions from pairwise can be used as GP kernels by using the wrapper class `PairwiseKernel`. The only caveat is that the gradient of the hyperparameters is not analytic but numeric and all those kernels support only isotropic distances. The parameter `gamma` is considered to be a hyperparameter and may be optimized. The other kernel parameters are set directly at initialization and are kept fixed.

### Basic kernels

The `ConstantKernel` kernel can be used as part of a `Product` kernel where it scales the magnitude of the other factor (kernel) or as part of a `Sum` kernel, where it modifies the mean of the Gaussian process. It depends on a parameter `constant_value`. It is defined as:

\[
k(x_i, x_j) = constant_value \forall x_1, x_2
\]

The main use-case of the `WhiteKernel` kernel is as part of a sum-kernel where it explains the noise-component of the signal. Tuning its parameter `noise_level` corresponds to estimating the noise-level. It is defined as:

\[
k(x_i, x_j) = noise_level \text{ if } x_i == x_j \text{ else } 0
\]

### Kernel operators

Kernel operators take one or two base kernels and combine them into a new kernel. The `Sum` kernel takes two kernels \( k_1 \) and \( k_2 \) and combines them via \( k_{\text{sum}}(X, Y) = k_1(X, Y) + k_2(X, Y) \). The `Product` kernel takes two kernels \( k_1 \) and \( k_2 \) and combines them via \( k_{\text{product}}(X, Y) = k_1(X, Y) * k_2(X, Y) \). The `Exponentiation` kernel takes one base kernel and a scalar parameter `exponent` and combines them via \( k_{\text{exp}}(X, Y) = k(X, Y)^{\text{exponent}} \).

### Radial-basis function (RBF) kernel

The `RBF` kernel is a stationary kernel. It is also known as the “squared exponential” kernel. It is parameterized by a length-scale parameter \( l > 0 \), which can either be a scalar (isotropic variant of the kernel) or a vector with the same...
number of dimensions as the inputs \( x \) (anisotropic variant of the kernel). The kernel is given by:

\[
k(x_i, x_j) = \exp \left( -\frac{1}{2} d(x_i/l, x_j/l)^2 \right)
\]

This kernel is infinitely differentiable, which implies that GPs with this kernel as covariance function have mean square derivatives of all orders, and are thus very smooth. The prior and posterior of a GP resulting from an RBF kernel are shown in the following figure:

**Matérn kernel**

The Matérn kernel is a stationary kernel and a generalization of the RBF kernel. It has an additional parameter \( \nu \) which controls the smoothness of the resulting function. It is parameterized by a length-scale parameter \( l > 0 \), which
can either be a scalar (isotropic variant of the kernel) or a vector with the same number of dimensions as the inputs \( x \) (anisotropic variant of the kernel). The kernel is given by:

\[
k(x_i, x_j) = \sigma^2 \frac{1}{\Gamma(\nu)2^{\nu-1}} \left(\gamma \sqrt{2\nu d(x_i/l, x_j/l)}\right)^\nu K_\nu \left(\gamma \sqrt{2\nu d(x_i/l, x_j/l)}\right),
\]

As \( \nu \to \infty \), the Matérn kernel converges to the RBF kernel. When \( \nu = 1/2 \), the Matérn kernel becomes identical to the absolute exponential kernel, i.e.,

\[
k(x_i, x_j) = \sigma^2 \exp \left(-\gamma d(x_i/l, x_j/l)\right) \quad \nu = \frac{1}{2}
\]

In particular, \( \nu = 3/2 \):

\[
k(x_i, x_j) = \sigma^2 \left(1 + \gamma \sqrt{3} d(x_i/l, x_j/l)\right) \exp \left(-\gamma \sqrt{3} d(x_i/l, x_j/l)\right) \quad \nu = \frac{3}{2}
\]

and \( \nu = 5/2 \):

\[
k(x_i, x_j) = \sigma^2 \left(1 + \gamma \sqrt{5} d(x_i/l, x_j/l) + \frac{5}{3} \gamma^2 d(x_i/l, x_j/l)^2\right) \exp \left(-\gamma \sqrt{5} d(x_i/l, x_j/l)\right) \quad \nu = \frac{5}{2}
\]

are popular choices for learning functions that are not infinitely differentiable (as assumed by the RBF kernel) but at least once (\( \nu = 3/2 \)) or twice differentiable (\( \nu = 5/2 \)).

The flexibility of controlling the smoothness of the learned function via \( \nu \) allows adapting to the properties of the true underlying functional relation. The prior and posterior of a GP resulting from a Matérn kernel are shown in the following figure:

See [RW2006], pp84 for further details regarding the different variants of the Matérn kernel.

### Rational quadratic kernel

The *RationalQuadratic* kernel can be seen as a scale mixture (an infinite sum) of RBF kernels with different characteristic length-scales. It is parameterized by a length-scale parameter \( l > 0 \) and a scale mixture parameter \( \alpha > 0 \). Only the isotropic variant where \( l \) is a scalar is supported at the moment. The kernel is given by:

\[
k(x_i, x_j) = \left(1 + \frac{d(x_i, x_j)^2}{2\alpha l^2}\right)^{-\alpha}
\]

The prior and posterior of a GP resulting from an RBF kernel are shown in the following figure:

### Exp-Sine-Squared kernel

The *ExpSineSquared* kernel allows modeling periodic functions. It is parameterized by a length-scale parameter \( l > 0 \) and a periodicity parameter \( p > 0 \). Only the isotropic variant where \( l \) is a scalar is supported at the moment. The kernel is given by:

\[
k(x_i, x_j) = \exp \left(-2 \left(\sin(\pi/p * d(x_i, x_j)/l)\right)^2\right)
\]

The prior and posterior of a GP resulting from an ExpSineSquared kernel are shown in the following figure:

3.1. Supervised learning
3.1. Supervised learning
Prior (kernel: $1^{\times2} \times \text{ExpSineSquared}(\text{length\_scale}=1, \text{periodicity}=3)$)

Posterior (kernel: $0.799^{\times2} \times \text{ExpSineSquared}(\text{length\_scale}=0.791, \text{periodicity}=2.87)$)
Log-Likelihood: 3.394
Dot-Product kernel

The DotProduct kernel is non-stationary and can be obtained from linear regression by putting $N(0, 1)$ priors on the coefficients of $x_d(d = 1, ..., D)$ and a prior of $N(0, \sigma_b^2)$ on the bias. The DotProduct kernel is invariant to a rotation of the coordinates about the origin, but not translations. It is parameterized by a parameter $\sigma_b^2$. For $\sigma_b^2 = 0$, the kernel is called the homogeneous linear kernel, otherwise it is inhomogeneous. The kernel is given by

$$k(x_i, x_j) = \sigma_b^2 + x_i \cdot x_j$$

The DotProduct kernel is commonly combined with exponentiation. An example with exponent 2 is shown in the following figure:
References

3.1.8 Cross decomposition

The cross decomposition module contains two main families of algorithms: the partial least squares (PLS) and the canonical correlation analysis (CCA).

These families of algorithms are useful to find linear relations between two multivariate datasets: the $X$ and $Y$ arguments of the `fit` method are 2D arrays.

Cross decomposition algorithms find the fundamental relations between two matrices ($X$ and $Y$). They are latent variable approaches to modeling the covariance structures in these two spaces. They will try to find the multidimensional direction in the $X$ space that explains the maximum multidimensional variance direction in the $Y$ space. PLS-regression is particularly suited when the matrix of predictors has more variables than observations, and when there is multicollinearity among $X$ values. By contrast, standard regression will fail in these cases.

Classes included in this module are `PLSRegression`, `PLSCanonical`, `CCA`, and `PLSSVD`.

Reference:

- JA Wegelin *A survey of Partial Least Squares (PLS) methods, with emphasis on the two-block case*

Examples:
3.1.9 Naive Bayes

Naive Bayes methods are a set of supervised learning algorithms based on applying Bayes’ theorem with the “naive” assumption of independence between every pair of features. Given a class variable $y$ and a dependent feature vector $x_1$ through $x_n$, Bayes’ theorem states the following relationship:

$$P(y \mid x_1, \ldots, x_n) = \frac{P(y)P(x_1, \ldots, x_n \mid y)}{P(x_1, \ldots, x_n)}$$

Using the naive independence assumption that

$$P(x_i \mid y, x_1, \ldots, x_{i-1}, x_{i+1}, \ldots, x_n) = P(x_i \mid y),$$

for all $i$, this relationship is simplified to

$$P(y \mid x_1, \ldots, x_n) = \frac{P(y) \prod_{i=1}^{n} P(x_i \mid y)}{P(x_1, \ldots, x_n)}$$

Since $P(x_1, \ldots, x_n)$ is constant given the input, we can use the following classification rule:

$$P(y \mid x_1, \ldots, x_n) \propto P(y) \prod_{i=1}^{n} P(x_i \mid y)$$

$$\downarrow$$

$$\hat{y} = \arg \max_y P(y) \prod_{i=1}^{n} P(x_i \mid y),$$

and we can use Maximum A Posteriori (MAP) estimation to estimate $P(y)$ and $P(x_i \mid y)$; the former is then the relative frequency of class $y$ in the training set.

The different naive Bayes classifiers differ mainly by the assumptions they make regarding the distribution of $P(x_i \mid y)$.

In spite of their apparently over-simplified assumptions, naive Bayes classifiers have worked quite well in many real-world situations, famously document classification and spam filtering. They require a small amount of training data to estimate the necessary parameters. (For theoretical reasons why naive Bayes works well, and on which types of data it does, see the references below.)

Naive Bayes learners and classifiers can be extremely fast compared to more sophisticated methods. The decoupling of the class conditional feature distributions means that each distribution can be independently estimated as a one dimensional distribution. This in turn helps to alleviate problems stemming from the curse of dimensionality.

On the flip side, although naive Bayes is known as a decent classifier, it is known to be a bad estimator, so the probability outputs from predict_proba are not to be taken too seriously.

References:

Gaussian Naive Bayes

**GaussianNB** implements the Gaussian Naive Bayes algorithm for classification. The likelihood of the features is assumed to be Gaussian:

\[
P(x_i \mid y) = \frac{1}{\sqrt{2\pi\sigma_y^2}} \exp\left(-\frac{(x_i - \mu_y)^2}{2\sigma_y^2}\right)
\]

The parameters \(\sigma_y\) and \(\mu_y\) are estimated using maximum likelihood.

```python
>>> from sklearn import datasets
>>> iris = datasets.load_iris()
>>> from sklearn.naive_bayes import GaussianNB
>>> gnb = GaussianNB()
>>> y_pred = gnb.fit(iris.data, iris.target).predict(iris.data)
>>> print("Number of mislabeled points out of a total %d points : %d"
      ... % (iris.data.shape[0],(iris.target != y_pred).sum()))
Number of mislabeled points out of a total 150 points : 6
```

Multinomial Naive Bayes

**MultinomialNB** implements the naive Bayes algorithm for multinomially distributed data, and is one of the two classic naive Bayes variants used in text classification (where the data are typically represented as word vector counts, although tf-idf vectors are also known to work well in practice). The distribution is parametrized by vectors \(\theta_y = (\theta_{yi}, \ldots, \theta_{yn})\) for each class \(y\), where \(n\) is the number of features (in text classification, the size of the vocabulary) and \(\theta_{yi}\) is the probability \(P(x_i \mid y)\) of feature \(i\) appearing in a sample belonging to class \(y\).

The parameters \(\theta_y\) is estimated by a smoothed version of maximum likelihood, i.e. relative frequency counting:

\[
\hat{\theta}_{yi} = \frac{N_{yi} + \alpha}{N_y + \alpha n}
\]

where \(N_{yi} = \sum_{x \in T} x_i\) is the number of times feature \(i\) appears in a sample of class \(y\) in the training set \(T\), and \(N_y = \sum_{i=1}^{\left|T\right|} N_{yi}\) is the total count of all features for class \(y\).

The smoothing priors \(\alpha \geq 0\) accounts for features not present in the learning samples and prevents zero probabilities in further computations. Setting \(\alpha = 1\) is called Laplace smoothing, while \(\alpha < 1\) is called Lidstone smoothing.

Complement Naive Bayes

**ComplementNB** implements the complement naive Bayes (CNB) algorithm. CNB is an adaptation of the standard multinomial naive Bayes (MNB) algorithm that is particularly suited for imbalanced data sets. Specifically, CNB uses statistics from the complement of each class to compute the model’s weights. The inventors of CNB show empirically that the parameter estimates for CNB are more stable than those for MNB. Further, CNB regularly outperforms MNB (often by a considerable margin) on text classification tasks. The procedure for calculating the weights is as follows:

\[
\hat{\theta}_{ci} = \frac{\alpha_i + \sum_{j:y_j \neq c} d_{ij}}{\alpha + \sum_{j:y_j \neq c} \sum_k d_{kj}}
\]

\[
w_{ci} = \log \hat{\theta}_{ci}
\]

\[
w_{ci} = \frac{w_{ci}}{\sum_j |w_{cj}|}
\]
where the summations are over all documents \( j \) not in class \( c \), \( \alpha_i \) is a smoothing hyperparameter like that found in MNB, and \( \alpha = \sum \alpha_i \). The second normalization addresses the tendency for longer documents to dominate parameter estimates in MNB. The classification rule is:

\[
\hat{c} = \arg \min_c \sum_i t_i w_{ci}
\]

i.e., a document is assigned to the class that is the poorest complement match.

References:


Bernoulli Naive Bayes

`BernoulliNB` implements the naive Bayes training and classification algorithms for data that is distributed according to multivariate Bernoulli distributions; i.e., there may be multiple features but each one is assumed to be a binary-valued (Bernoulli, boolean) variable. Therefore, this class requires samples to be represented as binary-valued feature vectors; if handed any other kind of data, a `BernoulliNB` instance may binarize its input (depending on the `binarize` parameter).

The decision rule for Bernoulli naive Bayes is based on

\[
P(x_i \mid y) = P(i \mid y)x_i + (1 - P(i \mid y))(1 - x_i)
\]

which differs from multinomial NB’s rule in that it explicitly penalizes the non-occurrence of a feature \( i \) that is an indicator for class \( y \), where the multinomial variant would simply ignore a non-occurring feature.

In the case of text classification, word occurrence vectors (rather than word count vectors) may be used to train and use this classifier. `BernoulliNB` might perform better on some datasets, especially those with shorter documents. It is advisable to evaluate both models, if time permits.

References:


Out-of-core naive Bayes model fitting

Naive Bayes models can be used to tackle large scale classification problems for which the full training set might not fit in memory. To handle this case, `MultinomialNB`, `BernoulliNB`, and `GaussianNB` expose a `partial_fit` method that can be used incrementally as done with other classifiers as demonstrated in Out-of-core classification of text documents. All naive Bayes classifiers support sample weighting.

Contrary to the `fit` method, the first call to `partial_fit` needs to be passed the list of all the expected class labels.

For an overview of available strategies in scikit-learn, see also the out-of-core learning documentation.
3.1.10 Decision Trees

Decision Trees (DTs) are a non-parametric supervised learning method used for classification and regression. The goal is to create a model that predicts the value of a target variable by learning simple decision rules inferred from the data features.

For instance, in the example below, decision trees learn from data to approximate a sine curve with a set of if-then-else decision rules. The deeper the tree, the more complex the decision rules and the fitter the model.

Some advantages of decision trees are:

- Simple to understand and to interpret. Trees can be visualised.
- Requires little data preparation. Other techniques often require data normalisation, dummy variables need to be created and blank values to be removed. Note however that this module does not support missing values.
- The cost of using the tree (i.e., predicting data) is logarithmic in the number of data points used to train the tree.
- Able to handle both numerical and categorical data. Other techniques are usually specialised in analysing datasets that have only one type of variable. See algorithms for more information.
- Able to handle multi-output problems.
- Uses a white box model. If a given situation is observable in a model, the explanation for the condition is easily explained by boolean logic. By contrast, in a black box model (e.g., in an artificial neural network), results may be more difficult to interpret.
- Possible to validate a model using statistical tests. That makes it possible to account for the reliability of the model.
• Performs well even if its assumptions are somewhat violated by the true model from which the data were generated.

The disadvantages of decision trees include:

• Decision-tree learners can create over-complex trees that do not generalise the data well. This is called overfitting. Mechanisms such as pruning (not currently supported), setting the minimum number of samples required at a leaf node or setting the maximum depth of the tree are necessary to avoid this problem.

• Decision trees can be unstable because small variations in the data might result in a completely different tree being generated. This problem is mitigated by using decision trees within an ensemble.

• The problem of learning an optimal decision tree is known to be NP-complete under several aspects of optimality and even for simple concepts. Consequently, practical decision-tree learning algorithms are based on heuristic algorithms such as the greedy algorithm where locally optimal decisions are made at each node. Such algorithms cannot guarantee to return the globally optimal decision tree. This can be mitigated by training multiple trees in an ensemble learner, where the features and samples are randomly sampled with replacement.

• There are concepts that are hard to learn because decision trees do not express them easily, such as XOR, parity or multiplexer problems.

• Decision tree learners create biased trees if some classes dominate. It is therefore recommended to balance the dataset prior to fitting with the decision tree.

**Classification**

*DecisionTreeClassifier* is a class capable of performing multi-class classification on a dataset.

As with other classifiers, *DecisionTreeClassifier* takes as input two arrays: an array X, sparse or dense, of size \([n\text{\_samples}, n\text{\_features}]\) holding the training samples, and an array Y of integer values, size \([n\text{\_samples}]\), holding the class labels for the training samples:

```python
>>> from sklearn import tree
>>> X = [[0, 0], [1, 1]]
>>> Y = [0, 1]
>>> clf = tree.DecisionTreeClassifier()
>>> clf = clf.fit(X, Y)
```

After being fitted, the model can then be used to predict the class of samples:

```python
>>> clf.predict([[2., 2.]])
array([1])
```

Alternatively, the probability of each class can be predicted, which is the fraction of training samples of the same class in a leaf:

```python
>>> clf.predict_proba([[2., 2.]])
array([[0., 1.]])
```

*DecisionTreeClassifier* is capable of both binary (where the labels are \([-1, 1]\)) classification and multiclass (where the labels are \([0, ..., K-1]\)) classification.

Using the Iris dataset, we can construct a tree as follows:

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn import tree
>>> iris = load_iris()
>>> clf = tree.DecisionTreeClassifier()
>>> clf = clf.fit(iris.data, iris.target)
```
Once trained, we can export the tree in Graphviz format using the `export_graphviz` exporter. If you use the conda package manager, the graphviz binaries and the python package can be installed with

    conda install python-graphviz

Alternatively binaries for graphviz can be downloaded from the graphviz project homepage, and the Python wrapper installed from pypi with `pip install graphviz`.

Below is an example graphviz export of the above tree trained on the entire iris dataset; the results are saved in an output file `iris.pdf`:

```python
>>> import graphviz

>>> dot_data = tree.export_graphviz(clf, out_file=None)
>>> graph = graphviz.Source(dot_data)
>>> graph.render("iris")
```

The `export_graphviz` exporter also supports a variety of aesthetic options, including coloring nodes by their class (or value for regression) and using explicit variable and class names if desired. Jupyter notebooks also render these plots inline automatically:

```python
>>> dot_data = tree.export_graphviz(clf, out_file=None,
                                          feature_names=iris.feature_names,
                                          class_names=iris.target_names,
                                          filled=True, rounded=True,
                                          special_characters=True)
>>> graph = graphviz.Source(dot_data)
>>> graph
```

After being fitted, the model can then be used to predict the class of samples:

```python
>>> clf.predict(iris.data[:1,:])
array([0])
```

Alternatively, the probability of each class can be predicted, which is the fraction of training samples of the same class in a leaf:

```python
>>> clf.predict_proba(iris.data[:1,:])
array([[1., 0., 0.]])
```

**Examples:**

- *Plot the decision surface of a decision tree on the iris dataset*

### Regression

Decision trees can also be applied to regression problems, using the `DecisionTreeRegressor` class.

As in the classification setting, the fit method will take as argument arrays X and y, only that in this case y is expected to have floating point values instead of integer values:

```python
>>> from sklearn import tree
>>> X = [[0, 0], [2, 2]]
>>> y = [0.5, 2.5]
>>> clf = tree.DecisionTreeRegressor()
>>> clf = clf.fit(X, y)
```
3.1. Supervised learning

3.1.1. Decision trees

Decision surface of a decision tree using paired features

- **petal length (cm) ≤ 2.45**
  - gini = 0.6667
  - samples = 150
  - value = [50, 50, 50]
  - class = setosa

- **petal width (cm) ≤ 1.75**
  - gini = 0.5
  - samples = 100
  - value = [50, 50, 50]
  - class = setosa

- **petal length (cm) ≤ 4.95**
  - gini = 0.168
  - samples = 54
  - value = [49, 5, 0]
  - class = versicolor

- **petal length (cm) ≤ 4.85**
  - gini = 0.0425
  - samples = 46
  - value = [0, 1, 45]
  - class = virginica

- **petal width (cm) ≤ 1.65**
  - gini = 0.0408
  - samples = 48
  - value = [47, 1, 0]
  - class = versicolor

- **petal width (cm) ≤ 1.55**
  - gini = 0.4444
  - samples = 6
  - value = [1, 2, 3]
  - class = virginica

- **sepal length (cm) ≤ 6.95**
  - gini = 0.4444
  - samples = 3
  - value = [1, 2, 0]
  - class = versicolor

- **sepal length (cm) ≤ 5.95**
  - gini = 0.4444
  - samples = 3
  - value = [0, 2, 1]
  - class = virginica

- **sepal length (cm) ≤ 5.85**
  - gini = 0.0
  - samples = 43
  - value = [0, 0, 43]
  - class = virginica

- **sepal length (cm) ≤ 5.75**
  - gini = 0.0
  - samples = 2
  - value = [0, 2, 0]
  - class = virginica

- **sepal length (cm) ≤ 5.65**
  - gini = 0.0
  - samples = 1
  - value = [0, 1, 0]
  - class = versicolor

- **sepal length (cm) ≤ 5.55**
  - gini = 0.0
  - samples = 2
  - value = [0, 0, 2]
  - class = virginica

- **sepal length (cm) ≤ 5.45**
  - gini = 0.0
  - samples = 1
  - value = [0, 0, 1]
  - class = versicolor
A multi-output problem is a supervised learning problem with several outputs to predict, that is when Y is a 2d array of size \([n_{\text{samples}}, n_{\text{outputs}}]\).

When there is no correlation between the outputs, a very simple way to solve this kind of problem is to build \(n\) independent models, i.e. one for each output, and then to use those models to independently predict each one of the \(n\) outputs. However, because it is likely that the output values related to the same input are themselves correlated, an often better way is to build a single model capable of predicting simultaneously all \(n\) outputs. First, it requires lower training time since only a single estimator is built. Second, the generalization accuracy of the resulting estimator may often be increased.

With regard to decision trees, this strategy can readily be used to support multi-output problems. This requires the following changes:

- Store \(n\) output values in leaves, instead of 1;
- Use splitting criteria that compute the average reduction across all \(n\) outputs.

This module offers support for multi-output problems by implementing this strategy in both `DecisionTreeClassifier` and `DecisionTreeRegressor`. If a decision tree is fit on an output array \(Y\) of size \([n_{\text{samples}}, n_{\text{outputs}}]\) then the resulting estimator will:
• Output n_output values upon predict;
• Output a list of n_output arrays of class probabilities upon predict_proba.

The use of multi-output trees for regression is demonstrated in **Multi-output Decision Tree Regression**. In this example, the input X is a single real value and the outputs Y are the sine and cosine of X.

![Multi-output Decision Tree Regression](image)

The use of multi-output trees for classification is demonstrated in **Face completion with a multi-output estimators**. In this example, the inputs X are the pixels of the upper half of faces and the outputs Y are the pixels of the lower half of those faces.

**Examples:**

• **Multi-output Decision Tree Regression**
• **Face completion with a multi-output estimators**

**References:**

• M. Dumont et al, Fast multi-class image annotation with random subwindows and multiple output randomized trees, International Conference on Computer Vision Theory and Applications 2009

**Complexity**

In general, the run time cost to construct a balanced binary tree is \(O(n_{\text{samples}} n_{\text{features}} \log(n_{\text{samples}}))\) and query time \(O(\log(n_{\text{samples}}))\). Although the tree construction algorithm attempts to generate balanced trees, they will not always be balanced. Assuming that the subtrees remain approximately balanced, the cost at each node consists of searching through \(O(n_{\text{features}})\) to find the feature that offers the largest reduction in entropy. This has a cost of
Face completion with multi-output estimators

true faces    Extra trees    K-nn    Linear regression    Ridge
Scikit-learn offers a more efficient implementation for the construction of decision trees. A naive implementation (as above) would recompute the class label histograms (for classification) or the means (for regression) at each new split point along a given feature. Presorting the feature over all relevant samples, and retaining a running label count, will reduce the complexity at each node to \( O(n_{\text{features}} \log(n_{\text{samples}})) \), which results in a total cost of \( O(n_{\text{features}} n_{\text{samples}} \log(n_{\text{samples}})) \). This is an option for all tree-based algorithms. By default it is turned on for gradient boosting, where in general it makes training faster, but turned off for all other algorithms as it tends to slow down training when training deep trees.

**Tips on practical use**

- Decision trees tend to overfit on data with a large number of features. Getting the right ratio of samples to number of features is important, since a tree with few samples in high dimensional space is very likely to overfit.
- Consider performing dimensionality reduction (PCA, ICA, or Feature selection) beforehand to give your tree a better chance of finding features that are discriminative.
- Visualise your tree as you are training by using the `export` function. Use `max_depth=3` as an initial tree depth to get a feel for how the tree is fitting to your data, and then increase the depth.
- Remember that the number of samples required to populate the tree doubles for each additional level the tree grows to. Use `max_depth` to control the size of the tree to prevent overfitting.
- Use `min_samples_split` or `min_samples_leaf` to control the number of samples at a leaf node. A very small number will usually mean the tree will overfit, whereas a large number will prevent the tree from learning the data. Try `min_samples_leaf=5` as an initial value. If the sample size varies greatly, a float number can be used as percentage in these two parameters. The main difference between the two is that `min_samples_leaf` guarantees a minimum number of samples in a leaf, while `min_samples_split` can create arbitrary small leaves, though `min_samples_split` is more common in the literature.
- Balance your dataset before training to prevent the tree from being biased toward the classes that are dominant. Class balancing can be done by sampling an equal number of samples from each class, or preferably by normalizing the sum of the sample weights (`sample_weight`) for each class to the same value. Also note that weight-based pre-pruning criteria, such as `min_weight_fraction_leaf`, will then be less biased toward dominant classes than criteria that are not aware of the sample weights, like `min_samples_leaf`.
- If the samples are weighted, it will be easier to optimize the tree structure using weight-based pre-pruning criterion such as `min_weight_fraction_leaf`, which ensure that leaf nodes contain at least a fraction of the overall sum of the sample weights.
- All decision trees use `np.float32` arrays internally. If training data is not in this format, a copy of the dataset will be made.
- If the input matrix X is very sparse, it is recommended to convert to sparse `csc_matrix` before calling fit and sparse `csr_matrix` before calling predict. Training time can be orders of magnitude faster for a sparse matrix input compared to a dense matrix when features have zero values in most of the samples.

**Tree algorithms: ID3, C4.5, C5.0 and CART**

What are all the various decision tree algorithms and how do they differ from each other? Which one is implemented in scikit-learn?

**ID3** (Iterative Dichotomiser 3) was developed in 1986 by Ross Quinlan. The algorithm creates a multiway tree, finding for each node (i.e. in a greedy manner) the categorical feature that will yield the largest information gain for categorical
targets. Trees are grown to their maximum size and then a pruning step is usually applied to improve the ability of the
tree to generalise to unseen data.

C4.5 is the successor to ID3 and removed the restriction that features must be categorical by dynamically defining
a discrete attribute (based on numerical variables) that partitions the continuous attribute value into a discrete set of
intervals. C4.5 converts the trained trees (i.e. the output of the ID3 algorithm) into sets of if-then rules. These accuracy
each rule is then evaluated to determine the order in which they should be applied. Pruning is done by removing a
rule’s precondition if the accuracy of the rule improves without it.

C5.0 is Quinlan’s latest version release under a proprietary license. It uses less memory and builds smaller rulesets
than C4.5 while being more accurate.

CART (Classification and Regression Trees) is very similar to C4.5, but it differs in that it supports numerical target
variables (regression) and does not compute rule sets. CART constructs binary trees using the feature and threshold
that yield the largest information gain at each node.

scikit-learn uses an optimised version of the CART algorithm.

Mathematical formulation

Given training vectors \( x_i \in \mathbb{R}^n \), i=1,…, 1 and a label vector \( y \in \mathbb{R}^l \), a decision tree recursively partitions the space
such that the samples with the same labels are grouped together.

Let the data at node \( m \) be represented by \( Q \). For each candidate split \( \theta = (j, t_m) \) consisting of a feature \( j \) and threshold
\( t_m \), partition the data into \( Q_{left}(\theta) \) and \( Q_{right}(\theta) \) subsets

\[
Q_{left}(\theta) = (x, y)|x \leq t_m \\
Q_{right}(\theta) = Q \setminus Q_{left}(\theta)
\]

The impurity at \( m \) is computed using an impurity function \( H() \), the choice of which depends on the task being solved
(classification or regression)

\[
G(Q, \theta) = \frac{n_{left}}{N_m} H(Q_{left}(\theta)) + \frac{n_{right}}{N_m} H(Q_{right}(\theta))
\]

Select the parameters that minimises the impurity

\[
\theta^* = \arg\min_{\theta} G(Q, \theta)
\]

Recurse for subsets \( Q_{left}(\theta^*) \) and \( Q_{right}(\theta^*) \) until the maximum allowable depth is reached, \( N_m < \min_{\text{samples}} \) or
\( N_m = 1 \).

Classification criteria

If a target is a classification outcome taking on values 0,1,…,K-1, for node \( m \), representing a region \( R_m \) with \( N_m \)
observations, let

\[
p_{mk} = 1/N_m \sum_{x_i \in R_m} I(y_i = k)
\]

be the proportion of class k observations in node \( m \)

Common measures of impurity are Gini

\[
H(X_m) = \sum_k p_{mk}(1 - p_{mk})
\]
Cross-Entropy

\[ H(X_m) = - \sum_k p_{mk} \log(p_{mk}) \]

and Misclassification

\[ H(X_m) = 1 - \max(p_{mk}) \]

where \( X_m \) is the training data in node \( m \)

**Regression criteria**

If the target is a continuous value, then for node \( m \), representing a region \( R_m \) with \( N_m \) observations, common criteria to minimise as for determining locations for future splits are Mean Squared Error, which minimizes the L2 error using mean values at terminal nodes, and Mean Absolute Error, which minimizes the L1 error using median values at terminal nodes.

Mean Squared Error:

\[ c_m = \frac{1}{N_m} \sum_{i \in N_m} y_i \]

\[ H(X_m) = \frac{1}{N_m} \sum_{i \in N_m} (y_i - c_m)^2 \]

Mean Absolute Error:

\[ \bar{y}_m = \frac{1}{N_m} \sum_{i \in N_m} y_i \]

\[ H(X_m) = \frac{1}{N_m} \sum_{i \in N_m} |y_i - \bar{y}_m| \]

where \( X_m \) is the training data in node \( m \)

**References:**

- https://en.wikipedia.org/wiki/Predictive_analytics

### 3.1.11 Ensemble methods

The goal of **ensemble methods** is to combine the predictions of several base estimators built with a given learning algorithm in order to improve generalizability / robustness over a single estimator.

Two families of ensemble methods are usually distinguished:
In averaging methods, the driving principle is to build several estimators independently and then to average their predictions. On average, the combined estimator is usually better than any of the single base estimator because its variance is reduced.

Examples: Bagging methods, Forests of randomized trees, ...

By contrast, in boosting methods, base estimators are built sequentially and one tries to reduce the bias of the combined estimator. The motivation is to combine several weak models to produce a powerful ensemble.

Examples: AdaBoost, Gradient Tree Boosting, ...

Bagging meta-estimator

In ensemble algorithms, bagging methods form a class of algorithms which build several instances of a black-box estimator on random subsets of the original training set and then aggregate their individual predictions to form a final prediction. These methods are used as a way to reduce the variance of a base estimator (e.g., a decision tree), by introducing randomization into its construction procedure and then making an ensemble out of it. In many cases, bagging methods constitute a very simple way to improve with respect to a single model, without making it necessary to adapt the underlying base algorithm. As they provide a way to reduce overfitting, bagging methods work best with strong and complex models (e.g., fully developed decision trees), in contrast with boosting methods which usually work best with weak models (e.g., shallow decision trees).

Bagging methods come in many flavours but mostly differ from each other by the way they draw random subsets of the training set:

- When random subsets of the dataset are drawn as random subsets of the samples, then this algorithm is known as Pasting [B1999].
- When samples are drawn with replacement, then the method is known as Bagging [B1996].
- When random subsets of the dataset are drawn as random subsets of the features, then the method is known as Random Subspaces [H1998].
- Finally, when base estimators are built on subsets of both samples and features, then the method is known as Random Patches [LG2012].

In scikit-learn, bagging methods are offered as a unified BaggingClassifier meta-estimator (resp. BaggingRegressor), taking as input a user-specified base estimator along with parameters specifying the strategy to draw random subsets. In particular, max_samples and max_features control the size of the subsets (in terms of samples and features), while bootstrap and bootstrap_features control whether samples and features are drawn with or without replacement. When using a subset of the available samples the generalization accuracy can be estimated with the out-of-bag samples by setting oob_score=True. As an example, the snippet below illustrates how to instantiate a bagging ensemble of KNeighborsClassifier base estimators, each built on random subsets of 50% of the samples and 50% of the features.

```python
>>> from sklearn.ensemble import BaggingClassifier
>>> from sklearn.neighbors import KNeighborsClassifier
>>> bagging = BaggingClassifier(KNeighborsClassifier(),
... max_samples=0.5, max_features=0.5)
```

Examples:

- Single estimator versus bagging: bias-variance decomposition
Forests of randomized trees

The sklearn.ensemble module includes two averaging algorithms based on randomized decision trees: the RandomForest algorithm and the Extra-Trees method. Both algorithms are perturb-and-combine techniques [B1998] specifically designed for trees. This means a diverse set of classifiers is created by introducing randomness in the classifier construction. The prediction of the ensemble is given as the averaged prediction of the individual classifiers.

As other classifiers, forest classifiers have to be fitted with two arrays: a sparse or dense array X of size [n_samples, n_features] holding the training samples, and an array Y of size [n_samples] holding the target values (class labels) for the training samples:

```python
>>> from sklearn.ensemble import RandomForestClassifier
>>> X = [[0, 0], [1, 1]]
>>> Y = [0, 1]
>>> clf = RandomForestClassifier(n_estimators=10)
>>> clf = clf.fit(X, Y)
```

Like decision trees, forests of trees also extend to multi-output problems (if Y is an array of size [n_samples, n_outputs]).

Random Forests

In random forests (see RandomForestClassifier and RandomForestRegressor classes), each tree in the ensemble is built from a sample drawn with replacement (i.e., a bootstrap sample) from the training set. In addition, when splitting a node during the construction of the tree, the split that is chosen is no longer the best split among all features. Instead, the split that is picked is the best split among a random subset of the features. As a result of this randomness, the bias of the forest usually slightly increases (with respect to the bias of a single non-random tree) but, due to averaging, its variance also decreases, usually more than compensating for the increase in bias, hence yielding an overall better model.

In contrast to the original publication [B2001], the scikit-learn implementation combines classifiers by averaging their probabilistic prediction, instead of letting each classifier vote for a single class.

Extremely Randomized Trees

In extremely randomized trees (see ExtraTreesClassifier and ExtraTreesRegressor classes), randomness goes one step further in the way splits are computed. As in random forests, a random subset of candidate features is used, but instead of looking for the most discriminative thresholds, thresholds are drawn at random for each candidate feature and the best of these randomly-generated thresholds is picked as the splitting rule. This usually allows to reduce the variance of the model a bit more, at the expense of a slightly greater increase in bias:

```python
>>> from sklearn.model_selection import cross_val_score
>>> from sklearn.datasets import make_blobs
>>> from sklearn.ensemble import RandomForestClassifier
>>> from sklearn.ensemble import ExtraTreesClassifier
>>> from sklearn.tree import DecisionTreeClassifier

>>> X, y = make_blobs(n_samples=10000, n_features=10, centers=100, ...
...                      random_state=0)
```
```python
>>> clf = DecisionTreeClassifier(max_depth=None, min_samples_split=2, random_state=0)
>>> scores = cross_val_score(clf, X, y)
>>> scores.mean()
0.97...

>>> clf = RandomForestClassifier(n_estimators=10, max_depth=None, min_samples_split=2, random_state=0)
>>> scores = cross_val_score(clf, X, y)
>>> scores.mean()
0.999...

>>> clf = ExtraTreesClassifier(n_estimators=10, max_depth=None, min_samples_split=2, random_state=0)
>>> scores = cross_val_score(clf, X, y)
>>> scores.mean() > 0.999
True
```

Parameters

The main parameters to adjust when using these methods is `n_estimators` and `max_features`. The former is the number of trees in the forest. The larger the better, but also the longer it will take to compute. In addition, note that results will stop getting significantly better beyond a critical number of trees. The latter is the size of the random subsets of features to consider when splitting a node. The lower the greater the reduction of variance, but also the greater the increase in bias. Empirical good default values are `max_features=n_features` for regression problems, and `max_features=sqrt(n_features)` for classification tasks (where `n_features` is the number of features in the data). Good results are often achieved when setting `max_depth=None` in combination with `min_samples_split=2` (i.e., when fully developing the trees). Bear in mind though that these values are usually not optimal, and might result in models that consume a lot of RAM. The best parameter values should always be cross-validated. In addition, note that in random forests, bootstrap samples are used by default (bootstrap=True)
while the default strategy for extra-trees is to use the whole dataset (bootstrap=False). When using bootstrap sampling the generalization accuracy can be estimated on the left out or out-of-bag samples. This can be enabled by setting oob_score=True.

Note: The size of the model with the default parameters is $O(M \times N \times \log(N))$, where $M$ is the number of trees and $N$ is the number of samples. In order to reduce the size of the model, you can change these parameters: min_samples_split, min_samples_leaf, max_leaf_nodes and max_depth.

Parallelization

Finally, this module also features the parallel construction of the trees and the parallel computation of the predictions through the n_jobs parameter. If n_jobs=k then computations are partitioned into k jobs, and run on k cores of the machine. If n_jobs=-1 then all cores available on the machine are used. Note that because of inter-process communication overhead, the speedup might not be linear (i.e., using k jobs will unfortunately not be k times as fast). Significant speedup can still be achieved though when building a large number of trees, or when building a single tree requires a fair amount of time (e.g., on large datasets).

Examples:

• Plot the decision surfaces of ensembles of trees on the iris dataset
• Pixel importances with a parallel forest of trees
• Face completion with a multi-output estimators

References


Feature importance evaluation

The relative rank (i.e. depth) of a feature used as a decision node in a tree can be used to assess the relative importance of that feature with respect to the predictability of the target variable. Features used at the top of the tree contribute to the final prediction decision of a larger fraction of the input samples. The expected fraction of the samples they contribute to can thus be used as an estimate of the relative importance of the features.

By averaging those expected activity rates over several randomized trees one can reduce the variance of such an estimate and use it for feature selection.

The following example shows a color-coded representation of the relative importances of each individual pixel for a face recognition task using a ExtraTreesClassifier model.

In practice those estimates are stored as an attribute named feature_importances_ on the fitted model. This is an array with shape (n_features,) whose values are positive and sum to 1.0. The higher the value, the more important is the contribution of the matching feature to the prediction function.

Examples:

• Pixel importances with a parallel forest of trees
Totally Random Trees Embedding

RandomTreesEmbedding implements an unsupervised transformation of the data. Using a forest of completely random trees, RandomTreesEmbedding encodes the data by the indices of the leaves a data point ends up in. This index is then encoded in a one-of-K manner, leading to a high dimensional, sparse binary coding. This coding can be computed very efficiently and can then be used as a basis for other learning tasks. The size and sparsity of the code can be influenced by choosing the number of trees and the maximum depth per tree. For each tree in the ensemble, the coding contains one entry of one. The size of the coding is at most \( n_{\text{estimators}} \times 2^{\text{max\_depth}} \), the maximum number of leaves in the forest.

As neighboring data points are more likely to lie within the same leaf of a tree, the transformation performs an implicit, non-parametric density estimation.

Examples:

- Hashing feature transformation using Totally Random Trees
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap... compares non-linear dimensionality reduction techniques on handwritten digits.
- Feature transformations with ensembles of trees compares supervised and unsupervised tree based feature transformations.

See also:

Manifold learning techniques can also be useful to derive non-linear representations of feature space, also these approaches focus also on dimensionality reduction.
AdaBoost

The module `sklearn.ensemble` includes the popular boosting algorithm AdaBoost, introduced in 1995 by Freund and Schapire [FS1995].

The core principle of AdaBoost is to fit a sequence of weak learners (i.e., models that are only slightly better than random guessing, such as small decision trees) on repeatedly modified versions of the data. The predictions from all of them are then combined through a weighted majority vote (or sum) to produce the final prediction. The data modifications at each so-called boosting iteration consist of applying weights $w_1, w_2, ..., w_N$ to each of the training samples. Initially, those weights are all set to $w_i = 1/N$, so that the first step simply trains a weak learner on the original data. For each successive iteration, the sample weights are individually modified and the learning algorithm is reapplied to the reweighted data. At a given step, those training examples that were incorrectly predicted by the boosted model induced at the previous step have their weights increased, whereas the weights are decreased for those that were predicted correctly. As iterations proceed, examples that are difficult to predict receive ever-increasing influence. Each subsequent weak learner is thereby forced to concentrate on the examples that are missed by the previous ones in the sequence [HTF].

AdaBoost can be used both for classification and regression problems:

- For multi-class classification, `AdaBoostClassifier` implements AdaBoost-SAMME and AdaBoost-SAMME.R [ZZRH2009].
- For regression, `AdaBoostRegressor` implements AdaBoost.R2 [D1997].

Usage

The following example shows how to fit an AdaBoost classifier with 100 weak learners:

```python
>>> from sklearn.model_selection import cross_val_score
>>> from sklearn.datasets import load_iris
>>> from sklearn.ensemble import AdaBoostClassifier
```
>> iris = load_iris()
>> clf = AdaBoostClassifier(n_estimators=100)
>> scores = cross_val_score(clf, iris.data, iris.target)
>> scores.mean()
0.9...

The number of weak learners is controlled by the parameter `n_estimators`. The `learning_rate` parameter controls the contribution of the weak learners in the final combination. By default, weak learners are decision stumps. Different weak learners can be specified through the `base_estimator` parameter. The main parameters to tune to obtain good results are `n_estimators` and the complexity of the base estimators (e.g., its depth `max_depth` or minimum required number of samples at a leaf `min_samples_leaf` in case of decision trees).

### Examples:

- **Discrete versus Real AdaBoost** compares the classification error of a decision stump, decision tree, and a boosted decision stump using AdaBoost-SAMME and AdaBoost-SAMME.R.
- **Two-class AdaBoost** shows the decision boundary and decision function values for a non-linearly separable two-class problem using AdaBoost-SAMME.
- **Decision Tree Regression with AdaBoost** demonstrates regression with the AdaBoost.R2 algorithm.

### References

Gradient Tree Boosting

Gradient Tree Boosting or Gradient Boosted Regression Trees (GBRT) is a generalization of boosting to arbitrary differentiable loss functions. GBRT is an accurate and effective off-the-shelf procedure that can be used for both regression and classification problems. Gradient Tree Boosting models are used in a variety of areas including Web search ranking and ecology.

The advantages of GBRT are:

- Natural handling of data of mixed type (= heterogeneous features)
- Predictive power
- Robustness to outliers in output space (via robust loss functions)

The disadvantages of GBRT are:

- Scalability, due to the sequential nature of boosting it can hardly be parallelized.

The module `sklearn.ensemble` provides methods for both classification and regression via gradient boosted regression trees.

### Classification

`GradientBoostingClassifier` supports both binary and multi-class classification. The following example shows how to fit a gradient boosting classifier with 100 decision stumps as weak learners:
```python
>>> from sklearn.datasets import make_hastie_10_2
>>> from sklearn.ensemble import GradientBoostingClassifier

>>> X, y = make_hastie_10_2(random_state=0)
>>> X_train, X_test = X[:2000], X[2000:]
>>> y_train, y_test = y[:2000], y[2000:]

>>> clf = GradientBoostingClassifier(n_estimators=100, learning_rate=1.0,
...     max_depth=1, random_state=0).fit(X_train, y_train)
>>> clf.score(X_test, y_test)
0.913...
```

The number of weak learners (i.e. regression trees) is controlled by the parameter `n_estimators`. The size of each tree can be controlled either by setting the tree depth via `max_depth` or by setting the number of leaf nodes via `max_leaf_nodes`. The learning_rate is a hyper-parameter in the range (0.0, 1.0] that controls overfitting via shrinkage.

**Note:** Classification with more than 2 classes requires the induction of `n_classes` regression trees at each iteration, thus, the total number of induced trees equals `n_classes * n_estimators`. For datasets with a large number of classes we strongly recommend to use `RandomForestClassifier` as an alternative to `GradientBoostingClassifier`.

## Regression

`GradientBoostingRegressor` supports a number of different loss functions for regression which can be specified via the argument `loss`; the default loss function for regression is least squares (`'ls'`).

```python
>>> from sklearn.metrics import mean_squared_error
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.ensemble import GradientBoostingRegressor

>>> X, y = make_friedman1(n_samples=1200, random_state=0, noise=1.0)
>>> X_train, X_test = X[:200], X[200:]
>>> y_train, y_test = y[:200], y[200:]

>>> est = GradientBoostingRegressor(n_estimators=100, learning_rate=0.1,
...     max_depth=1, random_state=0, loss='ls').fit(X_train, y_train)
>>> mean_squared_error(y_test, est.predict(X_test))
5.00...
```

The figure below shows the results of applying `GradientBoostingRegressor` with least squares loss and 500 base learners to the Boston house price dataset (`sklearn.datasets.load_boston`). The plot on the left shows the train and test error at each iteration. The train error at each iteration is stored in the `train_score_` attribute of the gradient boosting model. The test error at each iterations can be obtained via the `staged_predict` method which returns a generator that yields the predictions at each stage. Plots like these can be used to determine the optimal number of trees (i.e. `n_estimators`) by early stopping. The plot on the right shows the feature importances which can be obtained via the `feature_importances_` property.

**Examples:**
- Gradient Boosting regression
Fitting additional weak-learners

Both :class:`GradientBoostingRegressor` and :class:`GradientBoostingClassifier` support :obj:`warm_start=True` which allows you to add more estimators to an already fitted model.

```python
def
>>> est.set_params(n_estimators=200, warm_start=True) # set warm_start and new nr of trees
>>> est.fit(X_train, y_train) # fit additional 100 trees to est
>>> mean_squared_error(y_test, est.predict(X_test))
3.84...
```

Controlling the tree size

The size of the regression tree base learners defines the level of variable interactions that can be captured by the gradient boosting model. In general, a tree of depth $h$ can capture interactions of order $h$. There are two ways in which the size of the individual regression trees can be controlled.

If you specify :obj:`max_depth=h` then complete binary trees of depth $h$ will be grown. Such trees will have (at most) $2^h$ leaf nodes and $2^h - 1$ split nodes.

Alternatively, you can control the tree size by specifying the number of leaf nodes via the parameter :obj:`max_leaf_nodes`. In this case, trees will be grown using best-first search where nodes with the highest improvement in impurity will be expanded first. A tree with :obj:`max_leaf_nodes=k` has $k - 1$ split nodes and thus can model interactions of up to order $\max\_\text{leaf}\_\text{nodes} - 1$.

We found that :obj:`max_leaf_nodes=k` gives comparable results to :obj:`max_depth=k-1` but is significantly faster to train at the expense of a slightly higher training error. The parameter :obj:`max_leaf_nodes` corresponds to the variable $J$ in the chapter on gradient boosting in [F2001] and is related to the parameter :obj:`interaction.depth` in R’s gbm package where :obj:`max_leaf_nodes == interaction.depth + 1`. 
Mathematical formulation

GBRT considers additive models of the following form:

\[ F(x) = \sum_{m=1}^{M} \gamma_m h_m(x) \]

where \( h_m(x) \) are the basis functions which are usually called weak learners in the context of boosting. Gradient Tree Boosting uses decision trees of fixed size as weak learners. Decision trees have a number of abilities that make them valuable for boosting, namely the ability to handle data of mixed type and the ability to model complex functions.

Similar to other boosting algorithms GBRT builds the additive model in a forward stagewise fashion:

\[ F_m(x) = F_{m-1}(x) + \gamma_m h_m(x) \]

At each stage the decision tree \( h_m(x) \) is chosen to minimize the loss function \( L \) given the current model \( F_{m-1} \) and its fit \( F_{m-1}(x_i) \)

\[ F_m(x) = F_{m-1}(x) + \arg \min_h \sum_{i=1}^{n} L(y_i, F_{m-1}(x_i) + h(x)) \]

The initial model \( F_0 \) is problem specific, for least-squares regression one usually chooses the mean of the target values.

**Note:** The initial model can also be specified via the init argument. The passed object has to implement fit and predict.

Gradient Boosting attempts to solve this minimization problem numerically via steepest descent: The steepest descent direction is the negative gradient of the loss function evaluated at the current model \( F_{m-1} \) which can be calculated for any differentiable loss function:

\[ F_m(x) = F_{m-1}(x) - \gamma_m \sum_{i=1}^{n} \nabla_{F} L(y_i, F_{m-1}(x_i)) \]

Where the step length \( \gamma_m \) is chosen using line search:

\[ \gamma_m = \arg \min_{\gamma} \sum_{i=1}^{n} L(y_i, F_{m-1}(x_i) - \gamma \frac{\partial L(y_i, F_{m-1}(x_i))}{\partial F_{m-1}(x_i)}) \]

The algorithms for regression and classification only differ in the concrete loss function used.
**Loss Functions**

The following loss functions are supported and can be specified using the parameter `loss`:

- **Regression**
  - Least squares (`'ls'`): The natural choice for regression due to its superior computational properties. The initial model is given by the mean of the target values.
  - Least absolute deviation (`'lad'`): A robust loss function for regression. The initial model is given by the median of the target values.
  - Huber (`'huber'`): Another robust loss function that combines least squares and least absolute deviation; use `alpha` to control the sensitivity with regards to outliers (see [F2001] for more details).
  - Quantile (`'quantile'`): A loss function for quantile regression. Use $0 < \alpha < 1$ to specify the quantile. This loss function can be used to create prediction intervals (see Prediction Intervals for Gradient Boosting Regression).

- **Classification**
  - Binomial deviance (`'deviance'`): The negative binomial log-likelihood loss function for binary classification (provides probability estimates). The initial model is given by the log odds-ratio.
  - Multinomial deviance (`'deviance'`): The negative multinomial log-likelihood loss function for multi-class classification with `n_classes` mutually exclusive classes. It provides probability estimates. The initial model is given by the prior probability of each class. At each iteration `n_classes` regression trees have to be constructed which makes GBRT rather inefficient for data sets with a large number of classes.
  - Exponential loss (`'exponential'`): The same loss function as `AdaBoostClassifier`. Less robust to mislabeled examples than `deviance`; can only be used for binary classification.

**Regularization**

**Shrinkage**

[F2001] proposed a simple regularization strategy that scales the contribution of each weak learner by a factor $\nu$:

$$F_m(x) = F_{m-1}(x) + \nu \gamma_m h_m(x)$$

The parameter $\nu$ is also called the **learning rate** because it scales the step length the gradient descent procedure; it can be set via the `learning_rate` parameter.

The parameter `learning_rate` strongly interacts with the parameter `n_estimators`, the number of weak learners to fit. Smaller values of `learning_rate` require larger numbers of weak learners to maintain a constant training error. Empirical evidence suggests that small values of `learning_rate` favor better test error. [HTF2009] recommend to set the learning rate to a small constant (e.g. `learning_rate <= 0.1`) and choose `n_estimators` by early stopping. For a more detailed discussion of the interaction between `learning_rate` and `n_estimators` see [R2007].

**Subsampling**

[F1999] proposed stochastic gradient boosting, which combines gradient boosting with bootstrap averaging (bagging). At each iteration the base classifier is trained on a fraction `subsample` of the available training data. The subsample is drawn without replacement. A typical value of `subsample` is 0.5.
The figure below illustrates the effect of shrinkage and subsampling on the goodness-of-fit of the model. We can clearly see that shrinkage outperforms no-shrinkage. Subsampling with shrinkage can further increase the accuracy of the model. Subsampling without shrinkage, on the other hand, does poorly.

Another strategy to reduce the variance is by subsampling the features analogous to the random splits in RandomForestClassifier. The number of subsampled features can be controlled via the max_features parameter.

Note: Using a small max_features value can significantly decrease the runtime.

Stochastic gradient boosting allows to compute out-of-bag estimates of the test deviance by computing the improvement in deviance on the examples that are not included in the bootstrap sample (i.e. the out-of-bag examples). The improvements are stored in the attribute oob_improvement_. oob_improvement_[i] holds the improvement in terms of the loss on the OOB samples if you add the i-th stage to the current predictions. Out-of-bag estimates can be used for model selection, for example to determine the optimal number of iterations. OOB estimates are usually very pessimistic thus we recommend to use cross-validation instead and only use OOB if cross-validation is too time consuming.

Examples:

- Gradient Boosting regularization
- Gradient Boosting Out-of-Bag estimates
- OOB Errors for Random Forests
Interpretation

Individual decision trees can be interpreted easily by simply visualizing the tree structure. Gradient boosting models, however, comprise hundreds of regression trees thus they cannot be easily interpreted by visual inspection of the individual trees. Fortunately, a number of techniques have been proposed to summarize and interpret gradient boosting models.

Feature importance

Often features do not contribute equally to predict the target response; in many situations the majority of the features are in fact irrelevant. When interpreting a model, the first question usually is: what are those important features and how do they contributing in predicting the target response?

Individual decision trees intrinsically perform feature selection by selecting appropriate split points. This information can be used to measure the importance of each feature; the basic idea is: the more often a feature is used in the split points of a tree the more important that feature is. This notion of importance can be extended to decision tree ensembles by simply averaging the feature importance of each tree (see Feature importance evaluation for more details).

The feature importance scores of a fit gradient boosting model can be accessed via the feature_importances_ property:

```
>>> from sklearn.datasets import make_hastie_10_2
>>> from sklearn.ensemble import GradientBoostingClassifier

>>> X, y = make_hastie_10_2(random_state=0)
>>> clf = GradientBoostingClassifier(n_estimators=100, learning_rate=1.0,
... max_depth=1, random_state=0).fit(X, y)
>>> clf.feature_importances_
array([ 0.11, 0.1 , 0.11, ...])
```

Examples:

- Gradient Boosting regression

Partial dependence

Partial dependence plots (PDP) show the dependence between the target response and a set of ‘target’ features, marginalizing over the values of all other features (the ‘complement’ features). Intuitively, we can interpret the partial dependence as the expected target response\(^1\) as a function of the ‘target’ features\(^2\).

Due to the limits of human perception the size of the target feature set must be small (usually, one or two) thus the target features are usually chosen among the most important features.

The Figure below shows four one-way and one two-way partial dependence plots for the California housing dataset:

One-way PDPs tell us about the interaction between the target response and the target feature (e.g. linear, non-linear). The upper left plot in the above Figure shows the effect of the median income in a district on the median house price; we can clearly see a linear relationship among them.

PDPs with two target features show the interactions among the two features. For example, the two-variable PDP in the above Figure shows the dependence of median house price on joint values of house age and avg. occupants per

---

\(^1\) For classification with loss='deviance' the target response is logit(p).

\(^2\) More precisely its the expectation of the target response after accounting for the initial model; partial dependence plots do not include the init model.
household. We can clearly see an interaction between the two features: For an avg. occupancy greater than two, the house price is nearly independent of the house age, whereas for values less than two there is a strong dependence on age.

The module `partial_dependence` provides a convenience function `plot_partial_dependence` to create one-way and two-way partial dependence plots. In the below example we show how to create a grid of partial dependence plots: two one-way PDPs for the features 0 and 1 and a two-way PDP between the two features:

```python
>>> from sklearn.datasets import make_hastie_10_2
>>> from sklearn.ensemble import GradientBoostingClassifier
>>> from sklearn.ensemble.partial_dependence import plot_partial_dependence

>>> X, y = make_hastie_10_2(random_state=0)
>>> clf = GradientBoostingClassifier(n_estimators=100, learning_rate=1.0,
... max_depth=1, random_state=0).fit(X, y)
>>> features = [0, 1, (0, 1)]
>>> fig, axs = plot_partial_dependence(clf, X, features)
```

For multi-class models, you need to set the class label for which the PDPs should be created via the `label` argument:

```python
>>> from sklearn.datasets import load_iris
>>> iris = load_iris()
>>> mc_clf = GradientBoostingClassifier(n_estimators=10,
... max_depth=1).fit(iris.data, iris.target)
>>> features = [3, 2, (3, 2)]
>>> fig, axs = plot_partial_dependence(mc_clf, X, features, label=0)
```

If you need the raw values of the partial dependence function rather than the plots you can use the `partial_dependence` function:

```python
>>> from sklearn.ensemble.partial_dependence import partial_dependence

>>> pdp, axes = partial_dependence(clf, [0], X=X)
>>> pdp
```

3.1. Supervised learning
axes

>>> axes
[array([-1.62497054, -1.59201391, ...

The function requires either the argument `grid` which specifies the values of the target features on which the partial dependence function should be evaluated or the argument `X` which is a convenience mode for automatically creating `grid` from the training data. If `X` is given, the `axes` value returned by the function gives the axis for each target feature.

For each value of the ‘target’ features in the `grid` the partial dependence function need to marginalize the predictions of a tree over all possible values of the ‘complement’ features. In decision trees this function can be evaluated efficiently without reference to the training data. For each grid point a weighted tree traversal is performed: if a split node involves a ‘target’ feature, the corresponding left or right branch is followed, otherwise both branches are followed, each branch is weighted by the fraction of training samples that entered that branch. Finally, the partial dependence is given by a weighted average of all visited leaves. For tree ensembles the results of each individual tree are again averaged.

Examples:

- Partial Dependence Plots

References

Voting Classifier

The idea behind the `VotingClassifier` is to combine conceptually different machine learning classifiers and use a majority vote or the average predicted probabilities (soft vote) to predict the class labels. Such a classifier can be useful for a set of equally well performing model in order to balance out their individual weaknesses.

Majority Class Labels (Majority/Hard Voting)

In majority voting, the predicted class label for a particular sample is the class label that represents the majority (mode) of the class labels predicted by each individual classifier.

E.g., if the prediction for a given sample is

- classifier 1 -> class 1
- classifier 2 -> class 1
- classifier 3 -> class 2

the `VotingClassifier` (with `voting='hard'`) would classify the sample as “class 1” based on the majority class label. In the cases of a tie, the `VotingClassifier` will select the class based on the ascending sort order. E.g., in the following scenario

- classifier 1 -> class 2
- classifier 2 -> class 1

the class label 1 will be assigned to the sample.
Usage

The following example shows how to fit the majority rule classifier:

```python
>>> from sklearn import datasets
>>> from sklearn.model_selection import cross_val_score
>>> from sklearn.linear_model import LogisticRegression
>>> from sklearn.naive_bayes import GaussianNB
>>> from sklearn.ensemble import RandomForestClassifier
>>> from sklearn.ensemble import VotingClassifier

>>> iris = datasets.load_iris()
>>> X, y = iris.data[:, 1:3], iris.target

>>> clf1 = LogisticRegression(random_state=1)
>>> clf2 = RandomForestClassifier(random_state=1)
>>> clf3 = GaussianNB()

>>> eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)], voting='hard')

>>> for clf, label in zip([clf1, clf2, clf3, eclf], ['Logistic Regression', 'Random Forest', 'naive Bayes', 'Ensemble']):
...     scores = cross_val_score(clf, X, y, cv=5, scoring='accuracy')
...     print("Accuracy: %0.2f (+/- %0.2f) [%s]" % (scores.mean(), scores.std(), label))

Accuracy: 0.90 (+/- 0.05) [Logistic Regression]
Accuracy: 0.93 (+/- 0.05) [Random Forest]
Accuracy: 0.91 (+/- 0.04) [naive Bayes]
Accuracy: 0.95 (+/- 0.05) [Ensemble]
```

**Weighted Average Probabilities (Soft Voting)**

In contrast to majority voting (hard voting), soft voting returns the class label as argmax of the sum of predicted probabilities.

Specific weights can be assigned to each classifier via the `weights` parameter. When weights are provided, the predicted class probabilities for each classifier are collected, multiplied by the classifier weight, and averaged. The final class label is then derived from the class label with the highest average probability.

To illustrate this with a simple example, let’s assume we have 3 classifiers and a 3-class classification problems where we assign equal weights to all classifiers: w1=1, w2=1, w3=1.

The weighted average probabilities for a sample would then be calculated as follows:

```
<table>
<thead>
<tr>
<th>classifier</th>
<th>class 1</th>
<th>class 2</th>
<th>class 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>classifier 1</td>
<td>w1 * 0.2</td>
<td>w1 * 0.5</td>
<td>w1 * 0.3</td>
</tr>
<tr>
<td>classifier 2</td>
<td>w2 * 0.6</td>
<td>w2 * 0.3</td>
<td>w2 * 0.1</td>
</tr>
<tr>
<td>classifier 3</td>
<td>w3 * 0.3</td>
<td>w3 * 0.4</td>
<td>w3 * 0.3</td>
</tr>
<tr>
<td>weighted average</td>
<td>0.37</td>
<td>0.4</td>
<td>0.23</td>
</tr>
</tbody>
</table>
```

Here, the predicted class label is 2, since it has the highest average probability.

The following example illustrates how the decision regions may change when a soft `VotingClassifier` is used based on an linear Support Vector Machine, a Decision Tree, and a K-nearest neighbor classifier:
Using the VotingClassifier with GridSearch

The VotingClassifier can also be used together with GridSearch in order to tune the hyperparameters of the individual estimators:

```python
>>> from sklearn.model_selection import GridSearchCV
>>> clf1 = LogisticRegression(random_state=1)
>>> clf2 = RandomForestClassifier(random_state=1)
>>> clf3 = GaussianNB()
>>> eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
                          voting='soft')
>>> params = {'lr__C': [1.0, 100.0], 'rf__n_estimators': [20, 200],}
>>> grid = GridSearchCV(estimator=eclf, param_grid=params, cv=5)
>>> grid = grid.fit(iris.data, iris.target)
```

Usage

In order to predict the class labels based on the predicted class-probabilities (scikit-learn estimators in the VotingClassifier must support predict_proba method):

```python
>>> eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
                          voting='soft')
```

Optionally, weights can be provided for the individual classifiers:

```python
>>> eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
                          voting='soft', weights=[2, 5, 1])
```
3.1. Supervised learning
3.1.12 Multiclass and multilabel algorithms

Warning: All classifiers in scikit-learn do multiclass classification out-of-the-box. You don’t need to use the sklearn.multiclass module unless you want to experiment with different multiclass strategies.

The sklearn.multiclass module implements meta-estimators to solve multiclass and multilabel classification problems by decomposing such problems into binary classification problems. Multitarget regression is also supported.

- **Multiclass classification** means a classification task with more than two classes; e.g., classify a set of images of fruits which may be oranges, apples, or pears. Multiclass classification makes the assumption that each sample is assigned to one and only one label: a fruit can be either an apple or a pear but not both at the same time.

- **Multilabel classification** assigns to each sample a set of target labels. This can be thought as predicting properties of a data-point that are not mutually exclusive, such as topics that are relevant for a document. A text might be about any of religion, politics, finance or education at the same time or none of these.

- **Multilabel classification** assigns each sample a set of target values. This can be thought of as predicting several properties for each data-point, such as wind direction and magnitude at a certain location.

- **Multilabel-multiclass classification** and **multi-task classification** means that a single estimator has to handle several joint classification tasks. This is both a generalization of the multi-label classification task, which only considers binary classification, as well as a generalization of the multi-class classification task. The output format is a 2d numpy array or sparse matrix.

The set of labels can be different for each output variable. For instance, a sample could be assigned “pear” for an output variable that takes possible values in a finite set of species such as “pear”, “apple”; and “blue” or “green” for a second output variable that takes possible values in a finite set of colors such as “green”, “red”, “blue”, “yellow”...

This means that any classifiers handling multi-output multiclass or multi-task classification tasks, support the multi-label classification task as a special case. Multi-task classification is similar to the multi-output classification task with different model formulations. For more information, see the relevant estimator documentation.

All scikit-learn classifiers are capable of multiclass classification, but the meta-estimators offered by sklearn.multiclass permit changing the way they handle more than two classes because this may have an effect on classifier performance (either in terms of generalization error or required computational resources).

Below is a summary of the classifiers supported by scikit-learn grouped by strategy; you don’t need the meta-estimators in this class if you’re using one of these, unless you want custom multiclass behavior:

- **Inherently multiclass:**
  - sklearn.naive_bayes.BernoulliNB
  - sklearn.tree.DecisionTreeClassifier
  - sklearn.tree.ExtraTreeClassifier
  - sklearn.ensemble.ExtraTreesClassifier
  - sklearn.naive_bayes.GaussianNB
  - sklearn.neighbors.KNeighborsClassifier
  - sklearn.semi_supervised.LabelPropagation
  - sklearn.semi_supervised.LabelSpreading
  - sklearn.discriminant_analysis.LinearDiscriminantAnalysis
- `sklearn.svm.LinearSVC` (setting `multi_class=’crammer_singer’`)
- `sklearn.linear_model.LogisticRegression` (setting `multi_class=’multinomial’`)
- `sklearn.linear_model.LogisticRegressionCV` (setting `multi_class=’multinomial’`)
- `sklearn.neural_network.MLPClassifier`
- `sklearn.neighbors.NearestCentroid`
- `sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis`
- `sklearn.neighbors.RadiusNeighborsClassifier`
- `sklearn.ensemble.RandomForestClassifier`
- `sklearn.linear_model.RidgeClassifier`
- `sklearn.linear_model.RidgeClassifierCV`

**Multiclass as One-Vs-One:**
- `sklearn.svm.NuSVC`
- `sklearn.svm.SVC`
- `sklearn.gaussian_process.GaussianProcessClassifier` (setting `multi_class = ‘one_vs_one’`)

**Multiclass as One-Vs-All:**
- `sklearn.ensemble.GradientBoostingClassifier`
- `sklearn.gaussian_process.GaussianProcessClassifier` (setting `multi_class = ‘one_vs_rest’`)
- `sklearn.svm.LinearSVC` (setting `multi_class=’ovr’`)
- `sklearn.linear_model.LogisticRegression` (setting `multi_class=’ovr’`)
- `sklearn.linear_model.LogisticRegressionCV` (setting `multi_class=’ovr’`)
- `sklearn.linear_model.SGDClassifier`
- `sklearn.linear_model.Perceptron`
- `sklearn.linear_model.PassiveAggressiveClassifier`

**Support multilabel:**
- `sklearn.tree.DecisionTreeClassifier`
- `sklearn.tree.ExtraTreeClassifier`
- `sklearn.ensemble.ExtraTreesClassifier`
- `sklearn.neighbors.KNeighborsClassifier`
- `sklearn.neural_network.MLPClassifier`
- `sklearn.neighbors.RadiusNeighborsClassifier`
- `sklearn.ensemble.RandomForestClassifier`
- `sklearn.linear_model.RidgeClassifierCV`

**Support multiclass-multioutput:**
- `sklearn.tree.DecisionTreeClassifier`
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– sklearn.ensemble.ExtraTreesClassifier
– sklearn.neighbors.KNeighborsClassifier
– sklearn.neighbors.RadiusNeighborsClassifier
– sklearn.ensemble.RandomForestClassifier
Warning: At present, no metric in sklearn.metrics supports the multioutput-multiclass classification task.

Multilabel classification format
In multilabel learning, the joint set of binary classification tasks is expressed with label binary indicator array: each
sample is one row of a 2d array of shape (n_samples, n_classes) with binary values: the one, i.e. the non zero elements,
corresponds to the subset of labels. An array such as np.array([[1, 0, 0], [0, 1, 1], [0, 0, 0]])
represents label 0 in the first sample, labels 1 and 2 in the second sample, and no labels in the third sample.
Producing multilabel data as a list of sets of labels may be more intuitive. The MultiLabelBinarizer transformer
can be used to convert between a collection of collections of labels and the indicator format.
>>> from sklearn.preprocessing import MultiLabelBinarizer
>>> y = [[2, 3, 4], [2], [0, 1, 3], [0, 1, 2, 3, 4], [0, 1, 2]]
>>> MultiLabelBinarizer().fit_transform(y)
array([[0, 0, 1, 1, 1],
[0, 0, 1, 0, 0],
[1, 1, 0, 1, 0],
[1, 1, 1, 1, 1],
[1, 1, 1, 0, 0]])

One-Vs-The-Rest
This strategy, also known as one-vs-all, is implemented in OneVsRestClassifier. The strategy consists in
fitting one classifier per class. For each classifier, the class is fitted against all the other classes. In addition to its
computational efficiency (only n_classes classifiers are needed), one advantage of this approach is its interpretability.
Since each class is represented by one and only one classifier, it is possible to gain knowledge about the class by
inspecting its corresponding classifier. This is the most commonly used strategy and is a fair default choice.
Multiclass learning
Below is an example of multiclass learning using OvR:
>>> from sklearn import datasets
>>> from sklearn.multiclass import OneVsRestClassifier
>>> from sklearn.svm import LinearSVC
>>> iris = datasets.load_iris()
>>> X, y = iris.data, iris.target
>>> OneVsRestClassifier(LinearSVC(random_state=0)).fit(X,
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
0, 0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 1,
1, 1, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2,
2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 1, 2, 2,
2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2])

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y).predict(X)
0, 0, 0, 0, 0,
0, 0, 0, 0, 0,
1, 1, 1, 1, 1,
1, 1, 1, 1, 1,
2, 2, 2, 2, 2,
2, 1, 2, 2, 2,

0,
0,
1,
1,
2,
2,

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Multilabel learning

OneVsRestClassifier also supports multilabel classification. To use this feature, feed the classifier an indicator matrix, in which cell [i, j] indicates the presence of label j in sample i.

Examples:

- Multilabel classification

One-Vs-One

OneVsOneClassifier constructs one classifier per pair of classes. At prediction time, the class which received the most votes is selected. In the event of a tie (among two classes with an equal number of votes), it selects the class with the highest aggregate classification confidence by summing over the pair-wise classification confidence levels computed by the underlying binary classifiers.

Since it requires to fit $n_{\text{classes}} \ast (n_{\text{classes}} - 1) / 2$ classifiers, this method is usually slower than one-vs-the-rest, due to its $O(n_{\text{classes}}^2)$ complexity. However, this method may be advantageous for algorithms such as kernel algorithms which don’t scale well with $n_{\text{samples}}$. This is because each individual learning problem only involves a small subset of the data whereas, with one-vs-the-rest, the complete dataset is used $n_{\text{classes}}$ times.
Multiclass learning

Below is an example of multiclass learning using OvO:

```python
>>> from sklearn import datasets
>>> from sklearn.multiclass import OneVsOneClassifier
>>> from sklearn.svm import LinearSVC

>>> iris = datasets.load_iris()

>>> X, y = iris.data, iris.target

>>> OneVsOneClassifier(LinearSVC(random_state=0)).fit(X, y).predict(X)
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
       0, 0, 0, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
       1, 2, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
       1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
       1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
       2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2])
```

References:


Error-Correcting Output-Codes

Output-code based strategies are fairly different from one-vs-the-rest and one-vs-one. With these strategies, each class is represented in a Euclidean space, where each dimension can only be 0 or 1. Another way to put it is that each class is represented by a binary code (an array of 0 and 1). The matrix which keeps track of the location/code of each class is called the code book. The code size is the dimensionality of the aforementioned space. Intuitively, each class should be represented by a code as unique as possible and a good code book should be designed to optimize classification accuracy. In this implementation, we simply use a randomly-generated code book as advocated in\(^3\) although more elaborate methods may be added in the future.

At fitting time, one binary classifier per bit in the code book is fitted. At prediction time, the classifiers are used to project new points in the class space and the class closest to the points is chosen.

In `OutputCodeClassifier`, the `code_size` attribute allows the user to control the number of classifiers which will be used. It is a percentage of the total number of classes.

A number between 0 and 1 will require fewer classifiers than one-vs-the-rest. In theory, \(\log_2(n_{\text{classes}}) / n_{\text{classes}}\) is sufficient to represent each class unambiguously. However, in practice, it may not lead to good accuracy since \(\log_2(n_{\text{classes}})\) is much smaller than \(n_{\text{classes}}\).

A number greater than 1 will require more classifiers than one-vs-the-rest. In this case, some classifiers will in theory correct for the mistakes made by other classifiers, hence the name “error-correcting”. In practice, however, this may not happen as classifier mistakes will typically be correlated. The error-correcting output codes have a similar effect to bagging.

Multiclass learning

Below is an example of multiclass learning using Output-Codes:

```python
>>> from sklearn import datasets
>>> from sklearn.multiclass import OutputCodeClassifier
>>> from sklearn.svm import LinearSVC

>>> iris = datasets.load_iris()
>>> X, y = iris.data, iris.target

>>> clf = OutputCodeClassifier(LinearSVC(random_state=0),
                             code_size=2, random_state=0)

>>> clf.fit(X, y).predict(X)
array([0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
      0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0, 0,
      1, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 1, 1, 1, 1, 1,
      2, 1, 1, 1, 1, 2, 1, 1, 1, 1, 1, 1, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
      2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
      2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2,
      2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2, 2]
```

References:


Multioutput regression

Multioutput regression support can be added to any regressor with `MultiOutputRegressor`. This strategy consists of fitting one regressor per target. Since each target is represented by exactly one regressor it is possible to gain knowledge about the target by inspecting its corresponding regressor. As `MultiOutputRegressor` fits one regressor per target it can not take advantage of correlations between targets.

Below is an example of multioutput regression:

```python
>>> from sklearn.datasets import make_regression
>>> from sklearn.multioutput import MultiOutputRegressor

>>> X, y = make_regression(n_samples=10, n_targets=3, random_state=1)

>>> MultiOutputRegressor(GradientBoostingRegressor(random_state=0)).fit(X, y).predict(X)
array([[-154.75474165, -147.03498585, -50.03812219],
      [  7.12165031,  5.12914884, -81.46081961],
      [ 123.92529176,  21.25719016,  -7.84253],
      [ 122.25193977,  -85.16443186, 107.12274212],
      [ -30.170388,  -94.80956739,  12.16979946],
      [ 140.72667194, 176.50941682,  -17.50447799],
      [ 149.37967282, -81.15699552,  -5.72850319]])
```

Multioutput classification

Multioutput classification support can be added to any classifier with `MultiOutputClassifier`. This strategy consists of fitting one classifier per target. This allows multiple target variable classifications. The purpose of this class
is to extend estimators to be able to estimate a series of target functions \((f_1,f_2,f_3,\ldots,f_n)\) that are trained on a single \(X\) predictor matrix to predict a series of responses \((y_1,y_2,y_3,\ldots,y_n)\).

Below is an example of multioutput classification:

```python
>>> from sklearn.datasets import make_classification
>>> from sklearn.multioutput import MultiOutputClassifier
>>> from sklearn.ensemble import RandomForestClassifier
>>> from sklearn.utils import shuffle
>>> import numpy as np

>>> X, y1 = make_classification(n_samples=10, n_features=100, n_informative=30, n_classes=3, random_state=1)
>>> y2 = shuffle(y1, random_state=1)
>>> y3 = shuffle(y1, random_state=2)
>>> Y = np.vstack((y1, y2, y3)).T
>>> n_samples, n_features = X.shape  # 10,100
>>> n_outputs = Y.shape[1]  # 3
>>> n_classes = 3
>>> forest = RandomForestClassifier(n_estimators=100, random_state=1)
>>> multi_target_forest = MultiOutputClassifier(forest, n_jobs=-1)
>>> multi_target_forest.fit(X, Y).predict(X)
array([[2, 2, 0],
       [1, 2, 1],
       [2, 1, 0],
       [0, 0, 2],
       [0, 2, 1],
       [0, 0, 2],
       [1, 1, 0],
       [1, 1, 1],
       [0, 0, 2],
       [2, 0, 0]])
```

### Classifier Chain

Classifier chains (see `ClassifierChain`) are a way of combining a number of binary classifiers into a single multi-label model that is capable of exploiting correlations among targets.

For a multi-label classification problem with \(N\) classes, \(N\) binary classifiers are assigned an integer between 0 and \(N-1\). These integers define the order of models in the chain. Each classifier is then fit on the available training data plus the true labels of the classes whose models were assigned a lower number.

When predicting, the true labels will not be available. Instead the predictions of each model are passed on to the subsequent models in the chain to be used as features.

Clearly the order of the chain is important. The first model in the chain has no information about the other labels while the last model in the chain has features indicating the presence of all of the other labels. In general one does not know the optimal ordering of the models in the chain so typically many randomly ordered chains are fit and their predictions are averaged together.

### References:

3.1.13 Feature selection

The classes in the sklearn.feature_selection module can be used for feature selection/dimensionality reduction on sample sets, either to improve estimators’ accuracy scores or to boost their performance on very high-dimensional datasets.

Removing features with low variance

VarianceThreshold is a simple baseline approach to feature selection. It removes all features whose variance doesn’t meet some threshold. By default, it removes all zero-variance features, i.e. features that have the same value in all samples.

As an example, suppose that we have a dataset with boolean features, and we want to remove all features that are either one or zero (on or off) in more than 80% of the samples. Boolean features are Bernoulli random variables, and the variance of such variables is given by

\[ \text{Var}[X] = p(1 - p) \]

so we can select using the threshold \(.8 \times (1 - .8)\):

```python
>>> from sklearn.feature_selection import VarianceThreshold
>>> X = [[0, 0, 1], [0, 1, 0], [1, 0, 0], [0, 1, 1], [0, 1, 0], [0, 1, 1]]
>>> sel = VarianceThreshold(threshold=(.8 * (1 - .8)))
>>> sel.fit_transform(X)
array([[0, 1],
       [1, 0],
       [0, 0],
       [1, 1],
       [1, 0],
       [1, 1]])
```

As expected, VarianceThreshold has removed the first column, which has a probability \(p = 5/6 > .8\) of containing a zero.

Univariate feature selection

Univariate feature selection works by selecting the best features based on univariate statistical tests. It can be seen as a preprocessing step to an estimator. Scikit-learn exposes feature selection routines as objects that implement the transform method:

- SelectKBest removes all but the \(k\) highest scoring features
- SelectPercentile removes all but a user-specified highest scoring percentage of features
- using common univariate statistical tests for each feature: false positive rate SelectFpr, false discovery rate SelectFdr, or family wise error SelectFwe.
- GenericUnivariateSelect allows to perform univariate feature selection with a configurable strategy. This allows to select the best univariate selection strategy with hyper-parameter search estimator.

For instance, we can perform a \(\chi^2\) test to the samples to retrieve only the two best features as follows:

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn.feature_selection import SelectKBest
>>> from sklearn.feature_selection import chi2
>>> iris = load_iris()
>>> X, y = iris.data, iris.target
```
These objects take as input a scoring function that returns univariate scores and p-values (or only scores for `SelectKBest` and `SelectPercentile`):

- For regression: `f_regression`, `mutual_info_regression`
- For classification: `chi2`, `f_classif`, `mutual_info_classif`

The methods based on F-test estimate the degree of linear dependency between two random variables. On the other hand, mutual information methods can capture any kind of statistical dependency, but being nonparametric, they require more samples for accurate estimation.

Feature selection with sparse data

If you use sparse data (i.e. data represented as sparse matrices), `chi2`, `mutual_info_regression`, `mutual_info_classif` will deal with the data without making it dense.

Warning: Beware not to use a regression scoring function with a classification problem, you will get useless results.

Examples:

- **Univariate Feature Selection**
- **Comparison of F-test and mutual information**

Recursive feature elimination

Given an external estimator that assigns weights to features (e.g., the coefficients of a linear model), recursive feature elimination (`RFE`) is to select features by recursively considering smaller and smaller sets of features. First, the estimator is trained on the initial set of features and the importance of each feature is obtained either through a `coef_` attribute or through a `feature_importances_` attribute. Then, the least important features are pruned from current set of features. That procedure is recursively repeated on the pruned set until the desired number of features to select is eventually reached.

`RFECV` performs RFE in a cross-validation loop to find the optimal number of features.

Examples:

- **Recursive feature elimination**: A recursive feature elimination example showing the relevance of pixels in a digit classification task.
- **Recursive feature elimination with cross-validation**: A recursive feature elimination example with automatic tuning of the number of features selected with cross-validation.
Feature selection using SelectFromModel

SelectFromModel is a meta-transformer that can be used along with any estimator that has a coef_ or feature_importances_ attribute after fitting. The features are considered unimportant and removed, if the corresponding coef_ or feature_importances_ values are below the provided threshold parameter. Apart from specifying the threshold numerically, there are built-in heuristics for finding a threshold using a string argument. Available heuristics are “mean”, “median” and float multiples of these like “0.1*mean”.

For examples on how it is to be used refer to the sections below.

Examples

• Feature selection using SelectFromModel and LassoCV: Selecting the two most important features from the Boston dataset without knowing the threshold beforehand.

L1-based feature selection

Linear models penalized with the L1 norm have sparse solutions: many of their estimated coefficients are zero. When the goal is to reduce the dimensionality of the data to use with another classifier, they can be used along with feature_selection.SelectFromModel to select the non-zero coefficients. In particular, sparse estimators useful for this purpose are the linear_model.Lasso for regression, and of linear_model.LogisticRegression and svm.LinearSVC for classification:

```python
>>> from sklearn.svm import LinearSVC
>>> from sklearn.datasets import load_iris
>>> from sklearn.feature_selection import SelectFromModel

>>> iris = load_iris()
>>> X, y = iris.data, iris.target
>>> X.shape
(150, 4)
>>> lsvc = LinearSVC(C=0.01, penalty="l1", dual=False).fit(X, y)
>>> model = SelectFromModel(lsvc, prefit=True)
>>> X_new = model.transform(X)
>>> X_new.shape
(150, 3)
```

With SVMs and logistic-regression, the parameter C controls the sparsity: the smaller C the fewer features selected. With Lasso, the higher the alpha parameter, the fewer features selected.

Examples:

• Classification of text documents using sparse features: Comparison of different algorithms for document classification including L1-based feature selection.

L1-recovery and compressive sensing

For a good choice of alpha, the Lasso can fully recover the exact set of non-zero variables using only few observations, provided certain specific conditions are met. In particular, the number of samples should be “sufficiently large”, or L1 models will perform at random, where “sufficiently large” depends on the number of non-zero coefficients, the logarithm of the number of features, the amount of noise, the smallest absolute value of non-zero
coefficients, and the structure of the design matrix $X$. In addition, the design matrix must display certain specific properties, such as not being too correlated.

There is no general rule to select an alpha parameter for recovery of non-zero coefficients. It can be set by cross-validation (LassoCV or LassoLarsCV), though this may lead to under-penalized models: including a small number of non-relevant variables is not detrimental to prediction score. BIC (LassoLarsIC) tends, on the opposite, to set high values of alpha.


### Tree-based feature selection

Tree-based estimators (see the sklearn.tree module and forest of trees in the sklearn.ensemble module) can be used to compute feature importances, which in turn can be used to discard irrelevant features (when coupled with the sklearn.feature_selection.SelectFromModel meta-transformer):

```python
>>> from sklearn.ensemble import ExtraTreesClassifier
>>> from sklearn.datasets import load_iris
>>> iris = load_iris()
>>> X, y = iris.data, iris.target
>>> X.shape
(150, 4)
>>> clf = ExtraTreesClassifier()
>>> clf = clf.fit(X, y)
>>> clf.feature_importances_
array([0.04..., 0.05..., 0.4..., 0.4...])
>>> model = SelectFromModel(clf, prefit=True)
>>> X_new = model.transform(X)
>>> X_new.shape
(150, 2)
```

**Examples:**

- *Feature importances with forests of trees*: example on synthetic data showing the recovery of the actually meaningful features.
- *Pixel importances with a parallel forest of trees*: example on face recognition data.

### Feature selection as part of a pipeline

Feature selection is usually used as a pre-processing step before doing the actual learning. The recommended way to do this in scikit-learn is to use a sklearn.pipeline.Pipeline:

```python
clf = Pipeline([  
    ('feature_selection', SelectFromModel(LinearSVC(penalty="l1"))),
    ('classification', RandomForestClassifier())
])
clf.fit(X, y)
```

In this snippet we make use of a sklearn.svm.LinearSVC coupled with sklearn.feature_selection.SelectFromModel to evaluate feature importances and select the most relevant features. Then, a sklearn.
ensemble.RandomForestClassifier is trained on the transformed output, i.e., using only relevant features. You can perform similar operations with the other feature selection methods and also classifiers that provide a way to evaluate feature importances of course. See the sklearn.pipeline.Pipeline examples for more details.

### 3.1.14 Semi-Supervised

Semi-supervised learning is a situation in which in your training data some of the samples are not labeled. The semi-supervised estimators in sklearn.semi_supervised are able to make use of this additional unlabeled data to better capture the shape of the underlying data distribution and generalize better to new samples. These algorithms can perform well when we have a very small amount of labeled points and a large amount of unlabeled points.

#### Unlabeled entries in y

It is important to assign an identifier to unlabeled points along with the labeled data when training the model with the fit method. The identifier that this implementation uses is the integer value −1.

#### Label Propagation

Label propagation denotes a few variations of semi-supervised graph inference algorithms.

**A few features available in this model:**

- Can be used for classification and regression tasks
- Kernel methods to project data into alternate dimensional spaces

scikit-learn provides two label propagation models: LabelPropagation and LabelSpreading. Both work by constructing a similarity graph over all items in the input dataset.

---

**Fig. 3.1:** An illustration of label-propagation: the structure of unlabeled observations is consistent with the class structure, and thus the class label can be propagated to the unlabeled observations of the training set.

LabelPropagation and LabelSpreading differ in modifications to the similarity matrix that graph and the clamping effect on the label distributions. Clamping allows the algorithm to change the weight of the true ground labeled data to some degree. The LabelPropagation algorithm performs hard clamping of input labels, which means \( \alpha = 0 \). This clamping factor can be relaxed, to say \( \alpha = 0.2 \), which means that we will always retain 80 percent of our original label distribution, but the algorithm gets to change its confidence of the distribution within 20 percent.
LabelPropagation uses the raw similarity matrix constructed from the data with no modifications. In contrast, LabelSpreading minimizes a loss function that has regularization properties, as such it is often more robust to noise. The algorithm iterates on a modified version of the original graph and normalizes the edge weights by computing the normalized graph Laplacian matrix. This procedure is also used in Spectral clustering.

Label propagation models have two built-in kernel methods. Choice of kernel effects both scalability and performance of the algorithms. The following are available:

- rbf ($\exp(-\gamma |x - y|^2), \gamma > 0$). $\gamma$ is specified by keyword gamma.
- knn ($\mathbb{1}[x' \in kNN(x)]$). $k$ is specified by keyword n_neighbors.

The RBF kernel will produce a fully connected graph which is represented in memory by a dense matrix. This matrix may be very large and combined with the cost of performing a full matrix multiplication calculation for each iteration of the algorithm can lead to prohibitively long running times. On the other hand, the KNN kernel will produce a much more memory-friendly sparse matrix which can drastically reduce running times.

### Examples

- Decision boundary of label propagation versus SVM on the Iris dataset
- Label Propagation learning a complex structure
- Label Propagation digits active learning

### References


### 3.1.15 Isotonic regression

The class IsotonicRegression fits a non-decreasing function to data. It solves the following problem:

\[
\minimize \sum_i w_i (y_i - \hat{y}_i)^2 \\
\text{subject to } \hat{y}_{\text{min}} = \hat{y}_1 \leq \hat{y}_2 \ldots \leq \hat{y}_n = \hat{y}_{\text{max}}
\]

where each $w_i$ is strictly positive and each $y_i$ is an arbitrary real number. It yields the vector which is composed of non-decreasing elements the closest in terms of mean squared error. In practice this list of elements forms a function that is piecewise linear.

### 3.1.16 Probability calibration

When performing classification you often want not only to predict the class label, but also obtain a probability of the respective label. This probability gives you some kind of confidence on the prediction. Some models can give you poor estimates of the class probabilities and some even do not support probability prediction. The calibration module allows you to better calibrate the probabilities of a given model, or to add support for probability prediction.

Well calibrated classifiers are probabilistic classifiers for which the output of the predict_proba method can be directly interpreted as a confidence level. For instance, a well calibrated (binary) classifier should classify the samples such that among the samples to which it gave a predict_proba value close to 0.8, approximately 80% actually belong to the
positive class. The following plot compares how well the probabilistic predictions of different classifiers are calibrated:

LogisticRegression returns well calibrated predictions by default as it directly optimizes log-loss. In contrast, the other methods return biased probabilities; with different biases per method:

- **GaussianNB** tends to push probabilities to 0 or 1 (note the counts in the histograms). This is mainly because it makes the assumption that features are conditionally independent given the class, which is not the case in this dataset which contains 2 redundant features.

- **RandomForestClassifier** shows the opposite behavior: the histograms show peaks at approximately 0.2 and 0.9 probability, while probabilities close to 0 or 1 are very rare. An explanation for this is given by Niculescu-Mizil and Caruana\(^4\): “Methods such as bagging and random forests that average predictions from a

---

\(^4\) Predicting Good Probabilities with Supervised Learning, A. Niculescu-Mizil & R. Caruana, ICML 2005
base set of models can have difficulty making predictions near 0 and 1 because variance in the underlying base models will bias predictions that should be near zero or one away from these values. Because predictions are restricted to the interval [0,1], errors caused by variance tend to be one-sided near zero and one. For example, if a model should predict \( p = 0 \) for a case, the only way bagging can achieve this is if all bagged trees predict zero. If we add noise to the trees that bagging is averaging over, this noise will cause some trees to predict values larger than 0 for this case, thus moving the average prediction of the bagged ensemble away from 0. We observe this effect most strongly with random forests because the base-level trees trained with random forests have relatively high variance due to feature subsetting. As a result, the calibration curve also referred to as the reliability diagram (Wilks 1995) shows a characteristic sigmoid shape, indicating that the classifier could trust its “intuition” more and return probabilities closer to 0 or 1 typically.

- Linear Support Vector Classification (LinearSVC) shows an even more sigmoid curve as the RandomForest-Classifier, which is typical for maximum-margin methods (compare Niculescu-Mizil and Caruana), which focus on hard samples that are close to the decision boundary (the support vectors).

Two approaches for performing calibration of probabilistic predictions are provided: a parametric approach based on Platt’s sigmoid model and a non-parametric approach based on isotonic regression (sklearn.isotonic). Probability calibration should be done on new data not used for model fitting. The class CalibratedClassifierCV uses a cross-validation generator and estimates for each split the model parameter on the train samples and the calibration of the test samples. The probabilities predicted for the folds are then averaged. Already fitted classifiers can be calibrated by CalibratedClassifierCV via the parameter cv="prefit". In this case, the user has to take care manually that data for model fitting and calibration are disjoint.

The following images demonstrate the benefit of probability calibration. The first image present a dataset with 2 classes and 3 blobs of data. The blob in the middle contains random samples of each class. The probability for the samples in this blob should be 0.5.

The following image shows on the data above the estimated probability using a Gaussian naive Bayes classifier without calibration, with a sigmoid calibration and with a non-parametric isotonic calibration. One can observe that the non-parametric model provides the most accurate probability estimates for samples in the middle, i.e., 0.5.

The following experiment is performed on an artificial dataset for binary classification with 100.000 samples (1.000 of them are used for model fitting) with 20 features. Of the 20 features, only 2 are informative and 10 are redundant. The figure shows the estimated probabilities obtained with logistic regression, a linear support-vector classifier (SVC), and linear SVC with both isotonic calibration and sigmoid calibration. The calibration performance is evaluated with Brier score brier_score_loss, reported in the legend (the smaller the better).

One can observe here that logistic regression is well calibrated as its curve is nearly diagonal. Linear SVC’s calibration curve or reliability diagram has a sigmoid curve, which is typical for an under-confident classifier. In the case of LinearSVC, this is caused by the margin property of the hinge loss, which lets the model focus on hard samples that are close to the decision boundary (the support vectors). Both kinds of calibration can fix this issue and yield nearly identical results. The next figure shows the calibration curve of Gaussian naive Bayes on the same data, with both kinds of calibration and also without calibration.

One can see that Gaussian naive Bayes performs very badly but does so in an other way than linear SVC: While linear SVC exhibited a sigmoid calibration curve, Gaussian naive Bayes’ calibration curve has a transposed-sigmoid shape. This is typical for an over-confident classifier. In this case, the classifier’s overconfidence is caused by the redundant features which violate the naive Bayes assumption of feature-independence.

Calibration of the probabilities of Gaussian naive Bayes with isotonic regression can fix this issue as can be seen from the nearly diagonal calibration curve. Sigmoid calibration also improves the brier score slightly, albeit not as strongly as the non-parametric isotonic calibration. This is an intrinsic limitation of sigmoid calibration, whose parametric form assumes a sigmoid rather than a transposed-sigmoid curve. The non-parametric isotonic calibration model, however, makes no such strong assumptions and can deal with either shape, provided that there is sufficient calibration data. In general, sigmoid calibration is preferable in cases where the calibration curve is sigmoid and where there is limited

\footnote{On the combination of forecast probabilities for consecutive precipitation periods. Wea. Forecasting, 5, 640–650., Wilks, D. S., 1990a}
Data

- Class 0
- Class 1
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calibration data, while isotonic calibration is preferable for non-sigmoid calibration curves and in situations where large amounts of data are available for calibration.

CalibratedClassifierCV can also deal with classification tasks that involve more than two classes if the base estimator can do so. In this case, the classifier is calibrated first for each class separately in an one-vs-rest fashion. When predicting probabilities for unseen data, the calibrated probabilities for each class are predicted separately. As those probabilities do not necessarily sum to one, a postprocessing is performed to normalize them.

The next image illustrates how sigmoid calibration changes predicted probabilities for a 3-class classification problem. Illustrated is the standard 2-simplex, where the three corners correspond to the three classes. Arrows point from the probability vectors predicted by an uncalibrated classifier to the probability vectors predicted by the same classifier after sigmoid calibration on a hold-out validation set. Colors indicate the true class of an instance (red: class 1, green: class 2, blue: class 3).

The base classifier is a random forest classifier with 25 base estimators (trees). If this classifier is trained on all 800 training datapoints, it is overly confident in its predictions and thus incurs a large log-loss. Calibrating an identical classifier, which was trained on 600 datapoints, with method=’sigmoid’ on the remaining 200 datapoints reduces the confidence of the predictions, i.e., moves the probability vectors from the edges of the simplex towards the center:

This calibration results in a lower log-loss. Note that an alternative would have been to increase the number of base estimators which would have resulted in a similar decrease in log-loss.

References:
Illustration of sigmoid calibrator
3.1.17 Neural network models (supervised)

Warning: This implementation is not intended for large-scale applications. In particular, scikit-learn offers no GPU support. For much faster, GPU-based implementations, as well as frameworks offering much more flexibility to build deep learning architectures, see Related Projects.

Multi-layer Perceptron

Multi-layer Perceptron (MLP) is a supervised learning algorithm that learns a function $f(\cdot) : R^m \rightarrow R^o$ by training on a dataset, where $m$ is the number of dimensions for input and $o$ is the number of dimensions for output. Given a set of features $X = x_1, x_2, ..., x_m$ and a target $y$, it can learn a non-linear function approximator for either classification or regression. It is different from logistic regression, in that between the input and the output layer, there can be one or more non-linear layers, called hidden layers. Figure 1 shows a one hidden layer MLP with scalar output.

![Figure 1: One hidden layer MLP.](image)

The leftmost layer, known as the input layer, consists of a set of neurons $\{x_i | x_1, x_2, ..., x_m\}$ representing the input features. Each neuron in the hidden layer transforms the values from the previous layer with a weighted linear summation $w_1x_1 + w_2x_2 + ... + w_mx_m$, followed by a non-linear activation function $g(\cdot) : R \rightarrow R$ - like the hyperbolic tan function. The output layer receives the values from the last hidden layer and transforms them into output values.

The module contains the public attributes `coefs_` and `intercepts_`. `coefs_` is a list of weight matrices, where weight matrix at index $i$ represents the weights between layer $i$ and layer $i+1$. `intercepts_` is a list of bias vectors, where the vector at index $i$ represents the bias values added to layer $i+1$.

The advantages of Multi-layer Perceptron are:
• Capability to learn non-linear models.
• Capability to learn models in real-time (on-line learning) using `partial_fit`.

The disadvantages of Multi-layer Perceptron (MLP) include:

• MLP with hidden layers have a non-convex loss function where there exists more than one local minimum. Therefore different random weight initializations can lead to different validation accuracy.
• MLP requires tuning a number of hyperparameters such as the number of hidden neurons, layers, and iterations.
• MLP is sensitive to feature scaling.

Please see *Tips on Practical Use* section that addresses some of these disadvantages.

**Classification**

Class `MLPClassifier` implements a multi-layer perceptron (MLP) algorithm that trains using Backpropagation.
MLP trains on two arrays: array X of size (n_samples, n_features), which holds the training samples represented as floating point feature vectors; and array y of size (n_samples,), which holds the target values (class labels) for the training samples:

```python
>>> from sklearn.neural_network import MLPClassifier
>>> X = [[0., 0.], [1., 1.]]
>>> y = [0, 1]
>>> clf = MLPClassifier(solver='lbfgs', alpha=1e-5,
                          hidden_layer_sizes=(5, 2), random_state=1)
...                          ...
>>> clf.fit(X, y)
MLPClassifier(activation='relu', alpha=1e-05, batch_size='auto',
              beta_1=0.9, beta_2=0.999, early_stopping=False,
              epsilon=1e-08, hidden_layer_sizes=(5, 2),
              learning_rate='constant', learning_rate_init=0.001,
              max_iter=200, momentum=0.9, n_iter_no_change=10,
              nesterovs_momentum=True, power_t=0.5, random_state=1,
              shuffle=True, solver='lbfgs', tol=0.0001,
              validation_fraction=0.1, verbose=False, warm_start=False)
```

After fitting (training), the model can predict labels for new samples:

```python
>>> clf.predict([[2., 2.], [-1., -2.]])
array([1, 0])
```

MLP can fit a non-linear model to the training data. `clf.coefs_` contains the weight matrices that constitute the model parameters:

```python
>>> [coef.shape for coef in clf.coefs_]
[(2, 5), (5, 2), (2, 1)]
```

Currently, `MLPClassifier` supports only the Cross-Entropy loss function, which allows probability estimates by running the `predict_proba` method.
MLP trains using Backpropagation. More precisely, it trains using some form of gradient descent and the gradients are calculated using Backpropagation. For classification, it minimizes the Cross-Entropy loss function, giving a vector of probability estimates $P(y|x)$ per sample $x$:

```python
>>> clf.predict_proba([[2., 2.], [1., 2.]])
array([[ 1.967...e-04, 9.998...-01],
       [ 1.967...e-04, 9.998...-01]])
```
MLPClassifier supports multi-class classification by applying Softmax as the output function.

Further, the model supports multi-label classification in which a sample can belong to more than one class. For each class, the raw output passes through the logistic function. Values larger or equal to 0.5 are rounded to 1, otherwise to 0. For a predicted output of a sample, the indices where the value is 1 represents the assigned classes of that sample:

```python
>>> X = [[0., 0.], [1., 1.]]
>>> y = [[0, 1], [1, 1]]
>>> clf = MLPClassifier(solver='lbfgs', alpha=1e-5,
...                     hidden_layer_sizes=(15,), random_state=1)
... >>> clf.fit(X, y)
MLPClassifier(activation='relu', alpha=1e-05, batch_size='auto',
              beta_1=0.9, beta_2=0.999, early_stopping=False,
              epsilon=1e-08, hidden_layer_sizes=(15,),
              learning_rate='constant', learning_rate_init=0.001,
              max_iter=200, momentum=0.9, n_iter_no_change=10,
              nesterovs_momentum=True, power_t=0.5, random_state=1,
              shuffle=True, solver='lbfgs', tol=0.0001,
              validation_fraction=0.1, verbose=False, warm_start=False)
>>> clf.predict([[1., 2.]])
array([[1, 1]])
>>> clf.predict([[0., 0.]])
array([[0, 1]])
```

See the examples below and the doc string of MLPClassifier.fit for further information.

Examples:
- Compare Stochastic learning strategies for MLPClassifier
- Visualization of MLP weights on MNIST

Regression

Class MLPRegressor implements a multi-layer perceptron (MLP) that trains using backpropagation with no activation function in the output layer, which can also be seen as using the identity function as activation function. Therefore, it uses the square error as the loss function, and the output is a set of continuous values.

MLPRegressor also supports multi-output regression, in which a sample can have more than one target.

Regularization

Both MLPRegressor and MLPClassifier use parameter alpha for regularization (L2 regularization) term which helps in avoiding overfitting by penalizing weights with large magnitudes. Following plot displays varying decision function with value of alpha.

See the examples below for further information.

Examples:
- Varying regularization in Multi-layer Perceptron
Algorithms

MLP trains using Stochastic Gradient Descent, Adam, or L-BFGS. Stochastic Gradient Descent (SGD) updates parameters using the gradient of the loss function with respect to a parameter that needs adaptation, i.e.

\[ w \leftarrow w - \eta \left( \frac{\partial R(w)}{\partial w} + \frac{\partial \text{Loss}}{\partial w} \right) \]

where \( \eta \) is the learning rate which controls the step-size in the parameter space search. Loss \( \text{Loss} \) is the loss function used for the network.

More details can be found in the documentation of SGD.

Adam is similar to SGD in a sense that it is a stochastic optimizer, but it can automatically adjust the amount to update parameters based on adaptive estimates of lower-order moments.

With SGD or Adam, training supports online and mini-batch learning.

L-BFGS is a solver that approximates the Hessian matrix which represents the second-order partial derivative of a function. Further it approximates the inverse of the Hessian matrix to perform parameter updates. The implementation uses the Scipy version of L-BFGS.

If the selected solver is ‘L-BFGS’, training does not support online nor mini-batch learning.

Complexity

Suppose there are \( n \) training samples, \( m \) features, \( k \) hidden layers, each containing \( h \) neurons - for simplicity, and \( o \) output neurons. The time complexity of backpropagation is \( O(n \cdot m \cdot h^k \cdot o \cdot i) \), where \( i \) is the number of iterations. Since backpropagation has a high time complexity, it is advisable to start with smaller number of hidden neurons and few hidden layers for training.
Mathematical formulation

Given a set of training examples \((x_1, y_1), (x_2, y_2), \ldots, (x_n, y_n)\) where \(x_i \in \mathbb{R}^n\) and \(y_i \in \{0, 1\}\), a one hidden layer one hidden neuron MLP learns the function \(f(x) = W_2 g(W_1^T x + b_1) + b_2\) where \(W_1 \in \mathbb{R}^{m \times n}\) and \(W_2, b_1, b_2 \in \mathbb{R}\) are model parameters. \(W_1, W_2\) represent the weights of the input layer and hidden layer, respectively; and \(b_1, b_2\) represent the bias added to the hidden layer and the output layer, respectively. \(g(\cdot) : \mathbb{R} \rightarrow \mathbb{R}\) is the activation function, set by default as the hyperbolic tan. It is given as,

\[
g(z) = \frac{e^z - e^{-z}}{e^z + e^{-z}}
\]

For binary classification, \(f(x)\) passes through the logistic function \(g(z) = 1/(1+e^{-z})\) to obtain output values between zero and one. A threshold, set to 0.5, would assign samples of outputs larger or equal 0.5 to the positive class, and the rest to the negative class.

If there are more than two classes, \(f(x)\) itself would be a vector of size (n_classes,). Instead of passing through logistic function, it passes through the softmax function, which is written as,

\[
\text{softmax}(z)_i = \frac{\exp(z_i)}{\sum_{k=1}^{K} \exp(z_k)}
\]

where \(z_i\) represents the \(i\)th element of the input to softmax, which corresponds to class \(i\), and \(K\) is the number of classes. The result is a vector containing the probabilities that sample \(x\) belong to each class. The output is the class with the highest probability.

In regression, the output remains as \(f(x)\); therefore, output activation function is just the identity function.

MLP uses different loss functions depending on the problem type. The loss function for classification is Cross-Entropy, which in binary case is given as,

\[
\text{Loss}(\hat{y}, y, W) = -y \ln \hat{y} - (1 - y) \ln (1 - \hat{y}) + \alpha ||W||^2_2
\]

where \(\alpha ||W||^2_2\) is an L2-regularization term (aka penalty) that penalizes complex models; and \(\alpha > 0\) is a non-negative hyperparameter that controls the magnitude of the penalty.

For regression, MLP uses the Square Error loss function; written as,

\[
\text{Loss}(\hat{y}, y, W) = \frac{1}{2} ||\hat{y} - y||^2_2 + \frac{\alpha}{2} ||W||^2_2
\]

Starting from initial random weights, multi-layer perceptron (MLP) minimizes the loss function by repeatedly updating these weights. After computing the loss, a backward pass propagates it from the output layer to the previous layers, providing each weight parameter with an update value meant to decrease the loss.

In gradient descent, the gradient \(\nabla \text{Loss}_W\) of the loss with respect to the weights is computed and deducted from \(W\). More formally, this is expressed as,

\[
W^{i+1} = W^i - \epsilon \nabla \text{Loss}_W^i
\]

where \(i\) is the iteration step, and \(\epsilon\) is the learning rate with a value larger than 0.

The algorithm stops when it reaches a preset maximum number of iterations; or when the improvement in loss is below a certain, small number.

Tips on Practical Use

- Multi-layer Perceptron is sensitive to feature scaling, so it is highly recommended to scale your data. For example, scale each attribute on the input vector \(X\) to [0, 1] or [-1, +1], or standardize it to have mean 0 and variance 1. Note that you must apply the same scaling to the test set for meaningful results. You can use \texttt{StandardScaler} for standardization.
An alternative and recommended approach is to use `StandardScaler` in a Pipeline

- Finding a reasonable regularization parameter $\alpha$ is best done using `GridSearchCV`, usually in the range $10.0 \times \text{np.arange}(1, 7)$.

- Empirically, we observed that `L-BFGS` converges faster and with better solutions on small datasets. For relatively large datasets, however, `Adam` is very robust. It usually converges quickly and gives pretty good performance. `SGD` with momentum or nesterov’s momentum, on the other hand, can perform better than those two algorithms if learning rate is correctly tuned.

**More control with warm_start**

If you want more control over stopping criteria or learning rate in SGD, or want to do additional monitoring, using `warm_start=True` and `max_iter=1` and iterating yourself can be helpful:

```python
>>> X = [[0., 0.], [1., 1.]]
>>> y = [0, 1]
>>> clf = MLPClassifier(hidden_layer_sizes=(15,), random_state=1, max_iter=1, warm_start=True)
>>> for i in range(10):
...     clf.fit(X, y)
...     # additional monitoring / inspection
```

**References:**

- “Backpropagation” Andrew Ng, Jiquan Ngiam, Chuan Yu Foo, Yifan Mai, Caroline Suen - Website, 2011.

# 3.2 Unsupervised learning

## 3.2.1 Gaussian mixture models

`sklearn.mixture` is a package which enables one to learn Gaussian Mixture Models (diagonal, spherical, tied and full covariance matrices supported), sample them, and estimate them from data. Facilities to help determine the appropriate number of components are also provided.
A Gaussian mixture model is a probabilistic model that assumes all the data points are generated from a mixture of a finite number of Gaussian distributions with unknown parameters. One can think of mixture models as generalizing k-means clustering to incorporate information about the covariance structure of the data as well as the centers of the latent Gaussians.

Scikit-learn implements different classes to estimate Gaussian mixture models, that correspond to different estimation strategies, detailed below.

### Gaussian Mixture

The `GaussianMixture` object implements the expectation-maximization (EM) algorithm for fitting mixture-of-Gaussian models. It can also draw confidence ellipsoids for multivariate models, and compute the Bayesian Information Criterion to assess the number of clusters in the data. A `GaussianMixture.fit` method is provided that learns a Gaussian Mixture Model from train data. Given test data, it can assign to each sample the Gaussian it mostly probably belong to using the `GaussianMixture.predict` method.

The `GaussianMixture` comes with different options to constrain the covariance of the difference classes estimated: spherical, diagonal, tied or full covariance.

#### Examples:

- See *GMM covariances* for an example of using the Gaussian mixture as clustering on the iris dataset.
- See *Density Estimation for a Gaussian mixture* for an example on plotting the density estimation.

### Pros and cons of class `GaussianMixture`

#### Pros

- **Speed** It is the fastest algorithm for learning mixture models
- **Agnostic** As this algorithm maximizes only the likelihood, it will not bias the means towards zero, or bias the cluster sizes to have specific structures that might or might not apply.
Cons

**Singularities** When one has insufficiently many points per mixture, estimating the covariance matrices becomes difficult, and the algorithm is known to diverge and find solutions with infinite likelihood unless one regularizes the covariances artificially.

**Number of components** This algorithm will always use all the components it has access to, needing held-out data or information theoretical criteria to decide how many components to use in the absence of external cues.

**Selecting the number of components in a classical Gaussian Mixture Model**

The BIC criterion can be used to select the number of components in a Gaussian Mixture in an efficient way. In theory, it recovers the true number of components only in the asymptotic regime (i.e. if much data is available and assuming that the data was actually generated i.i.d. from a mixture of Gaussian distribution). Note that using a **Variational Bayesian Gaussian mixture** avoids the specification of the number of components for a Gaussian mixture model.

**Examples:**

- See *Gaussian Mixture Model Selection* for an example of model selection performed with classical Gaussian mixture.
Estimation algorithm Expectation-maximization

The main difficulty in learning Gaussian mixture models from unlabeled data is that it is one usually doesn’t know which points came from which latent component (if one has access to this information it gets very easy to fit a separate Gaussian distribution to each set of points). **Expectation-maximization** is a well-founded statistical algorithm to get around this problem by an iterative process. First one assumes random components (randomly centered on data points, learned from k-means, or even just normally distributed around the origin) and computes for each point a probability of being generated by each component of the model. Then, one tweaks the parameters to maximize the likelihood of the data given those assignments. Repeating this process is guaranteed to always converge to a local optimum.

Variational Bayesian Gaussian Mixture

The `BayesianGaussianMixture` object implements a variant of the Gaussian mixture model with variational inference algorithms. The API is similar as the one defined by `GaussianMixture`.

Estimation algorithm: variational inference

Variational inference is an extension of expectation-maximization that maximizes a lower bound on model evidence (including priors) instead of data likelihood. The principle behind variational methods is the same as expectation-maximization (that is both are iterative algorithms that alternate between finding the probabilities for each point to be generated by each mixture and fitting the mixture to these assigned points), but variational methods add regularization by integrating information from prior distributions. This avoids the singularities often found in expectation-maximization solutions but introduces some subtle biases to the model. Inference is often notably slower, but not usually as much so as to render usage unpractical.

Due to its Bayesian nature, the variational algorithm needs more hyper-parameters than expectation-maximization, the most important of these being the concentration parameter `weight_concentration_prior`. Specifying a low value for the concentration prior will make the model put most of the weight on few components set the remaining components weights very close to zero. High values of the concentration prior will allow a larger number of components to be active in the mixture.

The parameters implementation of the `BayesianGaussianMixture` class proposes two types of prior for the weights distribution: a finite mixture model with Dirichlet distribution and an infinite mixture model with the Dirichlet Process. In practice Dirichlet Process inference algorithm is approximated and uses a truncated distribution with a fixed maximum number of components (called the Stick-breaking representation). The number of components actually used almost always depends on the data.
The next figure compares the results obtained for the different type of the weight concentration prior (parameter `weight_concentration_prior_type`) for different values of `weight_concentration_prior`. Here, we can see the value of the `weight_concentration_prior` parameter has a strong impact on the effective number of active components obtained. We can also notice that large values for the concentration weight prior lead to more uniform weights when the type of prior is ‘dirichlet_distribution’ while this is not necessarily the case for the ‘dirichlet_process’ type (used by default).

The examples below compare Gaussian mixture models with a fixed number of components, to the variational Gaus-
sian mixture models with a Dirichlet process prior. Here, a classical Gaussian mixture is fitted with 5 components on a dataset composed of 2 clusters. We can see that the variational Gaussian mixture with a Dirichlet process prior is able to limit itself to only 2 components whereas the Gaussian mixture fits the data with a fixed number of components that has to be set a priori by the user. In this case the user has selected n_components=5 which does not match the true generative distribution of this toy dataset. Note that with very little observations, the variational Gaussian mixture models with a Dirichlet process prior can take a conservative stand, and fit only one component.

On the following figure we are fitting a dataset not well-depicted by a Gaussian mixture. Adjusting the weight_concentration_prior, parameter of the class:BayesianGaussianMixture controls the number of components used to fit this data. We also present on the last two plots a random sampling generated from the two resulting mixtures.

Examples:

- See Gaussian Mixture Model Ellipsoids for an example on plotting the confidence ellipsoids for both GaussianMixture and BayesianGaussianMixture.
- Gaussian Mixture Model Sine Curve shows using GaussianMixture and BayesianGaussianMixture to fit a sine wave.
- See Concentration Prior Type Analysis of Variation Bayesian Gaussian Mixture for an example plotting the confidence ellipsoids for the BayesianGaussianMixture with different weight_concentration_prior_type for different values of the parameter weight_concentration_prior.

Pros and cons of variational inference with BayesianGaussianMixture

Pros

Automatic selection when weight_concentration_prior is small enough and n_components is larger than what is found necessary by the model, the Variational Bayesian
3.2. Unsupervised learning

Expectation-maximization

Bayesian Gaussian mixture models with a Dirichlet process prior for $\gamma_0 = 0.01$.

Bayesian Gaussian mixture models with a Dirichlet process prior for $\gamma_0 = 100$

Gaussian mixture with a Dirichlet process prior for $\gamma_0 = 0.01$ sampled with 2000 samples.

Gaussian mixture with a Dirichlet process prior for $\gamma_0 = 100$ sampled with 2000 samples.
mixture model has a natural tendency to set some mixture weights values close to zero. This makes it possible to let the model choose a suitable number of effective components automatically. Only an upper bound of this number needs to be provided. Note however that the “ideal” number of active components is very application specific and is typically ill-defined in a data exploration setting.

**Less sensitivity to the number of parameters** unlike finite models, which will almost always use all components as much as they can, and hence will produce wildly different solutions for different numbers of components, the variational inference with a Dirichlet process prior (weight_concentration_prior_type='dirichlet_process') won’t change much with changes to the parameters, leading to more stability and less tuning.

**Regularization** due to the incorporation of prior information, variational solutions have less pathological special cases than expectation-maximization solutions.

**Cons**

**Speed** the extra parametrization necessary for variational inference make inference slower, although not by much.

**Hyperparameters** this algorithm needs an extra hyperparameter that might need experimental tuning via cross-validation.

**Bias** there are many implicit biases in the inference algorithms (and also in the Dirichlet process if used), and whenever there is a mismatch between these biases and the data it might be possible to fit better models using a finite mixture.

**The Dirichlet Process**

Here we describe variational inference algorithms on Dirichlet process mixture. The Dirichlet process is a prior probability distribution on *clusterings with an infinite, unbounded, number of partitions*. Variational techniques let us incorporate this prior structure on Gaussian mixture models at almost no penalty in inference time, comparing with a finite Gaussian mixture model.

An important question is how can the Dirichlet process use an infinite, unbounded number of clusters and still be consistent. While a full explanation doesn’t fit this manual, one can think of its stick breaking process analogy to help understanding it. The stick breaking process is a generative story for the Dirichlet process. We start with a unit-length stick and in each step we break off a portion of the remaining stick. Each time, we associate the length of the piece of the stick to the proportion of points that falls into a group of the mixture. At the end, to represent the infinite mixture, we associate the last remaining piece of the stick to the proportion of points that don’t fall into all the other groups. The length of each piece is random variable with probability proportional to the concentration parameter. Smaller value of the concentration will divide the unit-length into larger pieces of the stick (defining more concentrated distribution). Larger concentration values will create smaller pieces of the stick (increasing the number of components with non zero weights).

Variational inference techniques for the Dirichlet process still work with a finite approximation to this infinite mixture model, but instead of having to specify a priori how many components one wants to use, one just specifies the concentration parameter and an upper bound on the number of mixture components (this upper bound, assuming it is higher than the “true” number of components, affects only algorithmic complexity, not the actual number of components used).

**3.2.2 Manifold learning**

Look for the bare necessities
The simple bare necessities
Forget about your worries and your strife
I mean the bare necessities
Old Mother Nature’s recipes
That bring the bare necessities of life

– Baloo’s song [The Jungle Book]

Manifold learning is an approach to non-linear dimensionality reduction. Algorithms for this task are based on the idea that the dimensionality of many data sets is only artificially high.

**Introduction**

High-dimensional datasets can be very difficult to visualize. While data in two or three dimensions can be plotted to show the inherent structure of the data, equivalent high-dimensional plots are much less intuitive. To aid visualization of the structure of a dataset, the dimension must be reduced in some way.

The simplest way to accomplish this dimensionality reduction is by taking a random projection of the data. Though this allows some degree of visualization of the data structure, the randomness of the choice leaves much to be desired. In a random projection, it is likely that the more interesting structure within the data will be lost.
To address this concern, a number of supervised and unsupervised linear dimensionality reduction frameworks have been designed, such as Principal Component Analysis (PCA), Independent Component Analysis, Linear Discriminant Analysis, and others. These algorithms define specific rubrics to choose an “interesting” linear projection of the data. These methods can be powerful, but often miss important non-linear structure in the data.

Manifold Learning can be thought of as an attempt to generalize linear frameworks like PCA to be sensitive to non-linear structure in data. Though supervised variants exist, the typical manifold learning problem is unsupervised: it learns the high-dimensional structure of the data from the data itself, without the use of predetermined classifications.

Examples:

- See [Manifold learning on handwritten digits: Locally Linear Embedding, Isomap…](#) for an example of dimensionality reduction on handwritten digits.
- See [Comparison of Manifold Learning methods](#) for an example of dimensionality reduction on a toy “S-curve” dataset.

The manifold learning implementations available in scikit-learn are summarized below

### Isomap

One of the earliest approaches to manifold learning is the Isomap algorithm, short for Isometric Mapping. Isomap can be viewed as an extension of Multi-dimensional Scaling (MDS) or Kernel PCA. Isomap seeks a lower-dimensional
embedding which maintains geodesic distances between all points. Isomap can be performed with the object `Isomap`.

Complexity

The Isomap algorithm comprises three stages:

1. **Nearest neighbor search.** Isomap uses `sklearn.neighbors.BallTree` for efficient neighbor search. The cost is approximately $O[D \log(k)N \log(N)]$, for $k$ nearest neighbors of $N$ points in $D$ dimensions.

2. **Shortest-path graph search.** The most efficient known algorithms for this are Dijkstra’s Algorithm, which is approximately $O[N^2(k + \log(N))]$, or the Floyd-Warshall algorithm, which is $O[N^3]$. The algorithm can be selected by the user with the `path_method` keyword of `Isomap`. If unspecified, the code attempts to choose the best algorithm for the input data.

3. **Partial eigenvalue decomposition.** The embedding is encoded in the eigenvectors corresponding to the $d$ largest eigenvalues of the $N \times N$ isomap kernel. For a dense solver, the cost is approximately $O[dN^2]$. This cost can often be improved using the ARPACK solver. The eigensolver can be specified by the user with the `path_method` keyword of `Isomap`. If unspecified, the code attempts to choose the best algorithm for the input data.

The overall complexity of Isomap is $O[D \log(k)N \log(N)] + O[N^2(k + \log(N))] + O[dN^2]$.

- $N$ : number of training data points
- $D$ : input dimension
- $k$ : number of nearest neighbors
- $d$ : output dimension

References:

- “A global geometric framework for nonlinear dimensionality reduction” Tenenbaum, J.B.; De Silva, V.; & Langford, J.C. Science 290 (5500)
Locally Linear Embedding

Locally linear embedding (LLE) seeks a lower-dimensional projection of the data which preserves distances within local neighborhoods. It can be thought of as a series of local Principal Component Analyses which are globally compared to find the best non-linear embedding.

Locally linear embedding can be performed with function `locally_linear_embedding` or its object-oriented counterpart `LocallyLinearEmbedding`.

**Complexity**

The standard LLE algorithm comprises three stages:

1. **Nearest Neighbors Search.** See discussion under Isomap above.

2. **Weight Matrix Construction.** $O[DNk^3]$. The construction of the LLE weight matrix involves the solution of a $k \times k$ linear equation for each of the $N$ local neighborhoods.

3. **Partial Eigenvalue Decomposition.** See discussion under Isomap above.

The overall complexity of standard LLE is $O[D\log(k)N\log(N)] + O[DNk^3] + O[dN^2]$.

- $N$: number of training data points
- $D$: input dimension
- $k$: number of nearest neighbors
- $d$: output dimension

**References:**


**Modified Locally Linear Embedding**

One well-known issue with LLE is the regularization problem. When the number of neighbors is greater than the number of input dimensions, the matrix defining each local neighborhood is rank-deficient. To address this, standard
LLE applies an arbitrary regularization parameter $r$, which is chosen relative to the trace of the local weight matrix. Though it can be shown formally that as $r \to 0$, the solution converges to the desired embedding, there is no guarantee that the optimal solution will be found for $r > 0$. This problem manifests itself in embeddings which distort the underlying geometry of the manifold.

One method to address the regularization problem is to use multiple weight vectors in each neighborhood. This is the essence of modified locally linear embedding (MLLE). MLLE can be performed with function `locally_linear_embedding` or its object-oriented counterpart `LocallyLinearEmbedding`, with the keyword `method = 'modified'`. It requires $n_{neighbors} > n_{components}$.

![Modified Locally Linear Embedding of the digits (time 1.21s)](image)

**Complexity**

The MLLE algorithm comprises three stages:

1. **Nearest Neighbors Search.** Same as standard LLE

2. **Weight Matrix Construction.** Approximately $O[DNk^3] + O[N(k - D)k^2]$. The first term is exactly equivalent to that of standard LLE. The second term has to do with constructing the weight matrix from multiple weights. In practice, the added cost of constructing the MLLE weight matrix is relatively small compared to the cost of steps 1 and 3.

3. **Partial Eigenvalue Decomposition.** Same as standard LLE

The overall complexity of MLLE is $O[D \log(k)N \log(N)] + O[DNk^3] + O[N(k - D)k^2] + O[dN^2]$.

- $N$: number of training data points
- $D$: input dimension
- $k$: number of nearest neighbors
- $d$: output dimension

**References:**

- “MLLE: Modified Locally Linear Embedding Using Multiple Weights” Zhang, Z. & Wang, J.
Hessian Eigenmapping

Hessian Eigenmapping (also known as Hessian-based LLE: HLLE) is another method of solving the regularization problem of LLE. It revolves around a hessian-based quadratic form at each neighborhood which is used to recover the locally linear structure. Though other implementations note its poor scaling with data size, sklearn implements some algorithmic improvements which make its cost comparable to that of other LLE variants for small output dimension. HLLE can be performed with function `locally_linear_embedding` or its object-oriented counterpart `LocallyLinearEmbedding`, with the keyword `method = 'hessian'`. It requires `n_neighbors > n_components * (n_components + 3) / 2`.

**Complexity**

The HLLE algorithm comprises three stages:

1. **Nearest Neighbors Search.** Same as standard LLE

2. **Weight Matrix Construction.** Approximately $O[D N k^3] + O[N d^6]$. The first term reflects a similar cost to that of standard LLE. The second term comes from a QR decomposition of the local hessian estimator.

3. **Partial Eigenvalue Decomposition.** Same as standard LLE


- $N$ : number of training data points
- $D$ : input dimension
- $k$ : number of nearest neighbors
- $d$ : output dimension

**References:**

Spectral Embedding

Spectral Embedding is an approach to calculating a non-linear embedding. Scikit-learn implements Laplacian Eigenmaps, which finds a low dimensional representation of the data using a spectral decomposition of the graph Laplacian. The graph generated can be considered as a discrete approximation of the low dimensional manifold in the high dimensional space. Minimization of a cost function based on the graph ensures that points close to each other on the manifold are mapped close to each other in the low dimensional space, preserving local distances. Spectral embedding can be performed with the function `spectral_embedding` or its object-oriented counterpart `SpectralEmbedding`.

Complexity

The Spectral Embedding (Laplacian Eigenmaps) algorithm comprises three stages:

1. **Weighted Graph Construction.** Transform the raw input data into graph representation using affinity (adjacency) matrix representation.
2. **Graph Laplacian Construction.** Unnormalized Graph Laplacian is constructed as \( L = D - A \) for and normalized one as \( L = D^{-\frac{1}{2}}(D - A)D^{-\frac{1}{2}} \).
3. **Partial Eigenvalue Decomposition.** Eigenvalue decomposition is done on graph Laplacian

The overall complexity of spectral embedding is \( O[D \log(k)N \log(N)] + O[DNk^3] + O[dN^2] \).

- \( N \): number of training data points
- \( D \): input dimension
- \( k \): number of nearest neighbors
- \( d \): output dimension

References:

- “Laplacian Eigenmaps for Dimensionality Reduction and Data Representation” M. Belkin, P. Niyogi, Neural Computation, June 2003; 15 (6):1373-1396

Local Tangent Space Alignment

Though not technically a variant of LLE, Local tangent space alignment (LTSA) is algorithmically similar enough to LLE that it can be put in this category. Rather than focusing on preserving neighborhood distances as in LLE, LTSA seeks to characterize the local geometry at each neighborhood via its tangent space, and performs a global optimization to align these local tangent spaces to learn the embedding. LTSA can be performed with function `locally_linear_embedding` or its object-oriented counterpart `LocallyLinearEmbedding`, with the keyword `method = 'ltsa'`.

Complexity

The LTSA algorithm comprises three stages:

1. **Nearest Neighbors Search.** Same as standard LLE
2. **Weight Matrix Construction.** Approximately \( O[DNk^3] + O[k^2d] \). The first term reflects a similar cost to that of standard LLE.
3. **Partial Eigenvalue Decomposition.** Same as standard LLE
The overall complexity of standard LTSA is \(O[D \log(k) N \log(N)] + O[DNk^3] + O[k^2d] + O[dN^2]\).

- \(N\): number of training data points
- \(D\): input dimension
- \(k\): number of nearest neighbors
- \(d\): output dimension

### Multi-dimensional Scaling (MDS)

Multi-dimensional scaling (MDS) seeks a low-dimensional representation of the data in which the distances respect well the distances in the original high-dimensional space.

In general, is a technique used for analyzing similarity or dissimilarity data. MDS attempts to model similarity or dissimilarity data as distances in a geometric spaces. The data can be ratings of similarity between objects, interaction frequencies of molecules, or trade indices between countries.

There exists two types of MDS algorithm: metric and non metric. In the scikit-learn, the class MDS implements both. In Metric MDS, the input similarity matrix arises from a metric (and thus respects the triangular inequality), the distances between output two points are then set to be as close as possible to the similarity or dissimilarity data. In the non-metric version, the algorithms will try to preserve the order of the distances, and hence seek for a monotonic relationship between the distances in the embedded space and the similarities/dissimilarities.

Let \(S\) be the similarity matrix, and \(X\) the coordinates of the \(n\) input points. Disparities \(\hat{d}_{ij}\) are transformation of the similarities chosen in some optimal ways. The objective, called the stress, is then defined by \(\sum_{i<j} d_{ij}(X) - \hat{d}_{ij}(X)\)

### Metric MDS

The simplest metric MDS model, called absolute MDS, disparities are defined by \(\hat{d}_{ij} = S_{ij}\). With absolute MDS, the value \(S_{ij}\) should then correspond exactly to the distance between point \(i\) and \(j\) in the embedding point.

References:

Most commonly, disparities are set to $\hat{d}_{ij} = b S_{ij}$.

**Nonmetric MDS**

Non metric MDS focuses on the ordination of the data. If $S_{ij} < S_{kl}$, then the embedding should enforce $d_{ij} < d_{jk}$. A simple algorithm to enforce that is to use a monotonic regression of $d_{ij}$ on $S_{ij}$, yielding disparities $\hat{d}_{ij}$ in the same order as $S_{ij}$.

A trivial solution to this problem is to set all the points on the origin. In order to avoid that, the disparities $\hat{d}_{ij}$ are normalized.

References:

- “Nonmetric multidimensional scaling: a numerical method” Kruskal, J. Psychometrika, 29 (1964)
t-distributed Stochastic Neighbor Embedding (t-SNE)

t-SNE (TSNE) converts affinities of data points to probabilities. The affinities in the original space are represented by Gaussian joint probabilities and the affinities in the embedded space are represented by Student’s t-distributions. This allows t-SNE to be particularly sensitive to local structure and has a few other advantages over existing techniques:

- Revealing the structure at many scales on a single map
- Revealing data that lie in multiple, different, manifolds or clusters
- Reducing the tendency to crowd points together at the center

While Isomap, LLE and variants are best suited to unfold a single continuous low dimensional manifold, t-SNE will focus on the local structure of the data and will tend to extract clustered local groups of samples as highlighted on the S-curve example. This ability to group samples based on the local structure might be beneficial to visually disentangle a dataset that comprises several manifolds at once as is the case in the digits dataset.

The Kullback-Leibler (KL) divergence of the joint probabilities in the original space and the embedded space will be minimized by gradient descent. Note that the KL divergence is not convex, i.e. multiple restarts with different initializations will end up in local minima of the KL divergence. Hence, it is sometimes useful to try different seeds and select the embedding with the least KL divergence.

The disadvantages to using t-SNE are roughly:

- t-SNE is computationally expensive, and can take several hours on million-sample datasets where PCA will finish in seconds or minutes
- The Barnes-Hut t-SNE method is limited to two or three dimensional embeddings.
- The algorithm is stochastic and multiple restarts with different seeds can yield different embeddings. However, it is perfectly legitimate to pick the embedding with the least error.
- Global structure is not explicitly preserved. This is problem is mitigated by initializing points with PCA (using init='pca').
Optimizing t-SNE

The main purpose of t-SNE is visualization of high-dimensional data. Hence, it works best when the data will be embedded on two or three dimensions.

Optimizing the KL divergence can be a little bit tricky sometimes. There are five parameters that control the optimization of t-SNE and therefore possibly the quality of the resulting embedding:

- perplexity
- early exaggeration factor
- learning rate
- maximum number of iterations
- angle (not used in the exact method)

The perplexity is defined as $k = 2^S$ where $S$ is the Shannon entropy of the conditional probability distribution. The perplexity of a $k$-sided die is $k$, so that $k$ is effectively the number of nearest neighbors t-SNE considers when generating the conditional probabilities. Larger perplexities lead to more nearest neighbors and less sensitive to small structure. Conversely a lower perplexity considers a smaller number of neighbors, and thus ignores more global information in favour of the local neighborhood. As dataset sizes get larger more points will be required to get a reasonable sample of the local neighborhood, and hence larger perplexities may be required. Similarly noisier datasets will require larger perplexity values to encompass enough local neighbors to see beyond the background noise.

The maximum number of iterations is usually high enough and does not need any tuning. The optimization consists of two phases: the early exaggeration phase and the final optimization. During early exaggeration the joint probabilities in the original space will be artificially increased by multiplication with a given factor. Larger factors result in larger gaps between natural clusters in the data. If the factor is too high, the KL divergence could increase during this phase. Usually it does not have to be tuned. A critical parameter is the learning rate. If it is too low gradient descent will get stuck in a bad local minimum. If it is too high the KL divergence will increase during optimization. More tips can be found in Laurens van der Maaten’s FAQ (see references). The last parameter, angle, is a tradeoff between performance and accuracy. Larger angles imply that we can approximate larger regions by a single point, leading to better speed but less accurate results.

“How to Use t-SNE Effectively” provides a good discussion of the effects of the various parameters, as well as interactive plots to explore the effects of different parameters.

Barnes-Hut t-SNE

The Barnes-Hut t-SNE that has been implemented here is usually much slower than other manifold learning algorithms. The optimization is quite difficult and the computation of the gradient is $O(dN \log(N))$, where $d$ is the number of output dimensions and $N$ is the number of samples. The Barnes-Hut method improves on the exact method where t-SNE complexity is $O(dN^2)$, but has several other notable differences:

- The Barnes-Hut implementation only works when the target dimensionality is 3 or less. The 2D case is typical when building visualizations.
- Barnes-Hut only works with dense input data. Sparse data matrices can only be embedded with the exact method or can be approximated by a dense low rank projection for instance using `sklearn.decomposition.TruncatedSVD`
- Barnes-Hut is an approximation of the exact method. The approximation is parameterized with the angle parameter, therefore the angle parameter is unused when method=“exact”
- Barnes-Hut is significantly more scalable. Barnes-Hut can be used to embed hundred of thousands of data points while the exact method can handle thousands of samples before becoming computationally intractable
For visualization purpose (which is the main use case of t-SNE), using the Barnes-Hut method is strongly recommended. The exact t-SNE method is useful for checking the theoretically properties of the embedding possibly in higher dimensional space but limit to small datasets due to computational constraints.

Also note that the digits labels roughly match the natural grouping found by t-SNE while the linear 2D projection of the PCA model yields a representation where label regions largely overlap. This is a strong clue that this data can be well separated by non linear methods that focus on the local structure (e.g. an SVM with a Gaussian RBF kernel). However, failing to visualize well separated homogeneously labeled groups with t-SNE in 2D does not necessarily imply that the data cannot be correctly classified by a supervised model. It might be the case that 2 dimensions are not low enough to accurately represents the internal structure of the data.

References:

- “t-Distributed Stochastic Neighbor Embedding” van der Maaten, L.J.P.

Tips on practical use

- Make sure the same scale is used over all features. Because manifold learning methods are based on a nearest-neighbor search, the algorithm may perform poorly otherwise. See StandardScaler for convenient ways of scaling heterogeneous data.

- The reconstruction error computed by each routine can be used to choose the optimal output dimension. For a \(d\)-dimensional manifold embedded in a \(D\)-dimensional parameter space, the reconstruction error will decrease as \(n\_components\) is increased until \(n\_components == d\).

- Note that noisy data can “short-circuit” the manifold, in essence acting as a bridge between parts of the manifold that would otherwise be well-separated. Manifold learning on noisy and/or incomplete data is an active area of research.

- Certain input configurations can lead to singular weight matrices, for example when more than two points in the dataset are identical, or when the data is split into disjointed groups. In this case, \(solver='arpack'\) will fail to find the null space. The easiest way to address this is to use \(solver='dense'\) which will work on a singular matrix, though it may be very slow depending on the number of input points. Alternatively, one can attempt to understand the source of the singularity: if it is due to disjoint sets, increasing \(n\_neighbors\) may help. If it is due to identical points in the dataset, removing these points may help.

See also:

Totally Random Trees Embedding can also be useful to derive non-linear representations of feature space, also it does not perform dimensionality reduction.

### 3.2.3 Clustering

Clustering of unlabeled data can be performed with the module sklearn.cluster.

Each clustering algorithm comes in two variants: a class, that implements the fit method to learn the clusters on train data, and a function, that, given train data, returns an array of integer labels corresponding to the different clusters. For the class, the labels over the training data can be found in the labels_ attribute.
Input data

One important thing to note is that the algorithms implemented in this module can take different kinds of matrix as input. All the methods accept standard data matrices of shape \([n\_samples, n\_features]\). These can be obtained from the classes in the \texttt{sklearn.feature_extraction} module. For \texttt{AffinityPropagation}, \texttt{SpectralClustering} and \texttt{DBSCAN} one can also input similarity matrices of shape \([n\_samples, n\_samples]\). These can be obtained from the functions in the \texttt{sklearn.metrics.pairwise} module.

Overview of clustering methods

![Comparison of clustering algorithms](image)

Fig. 3.4: A comparison of the clustering algorithms in scikit-learn
<table>
<thead>
<tr>
<th>Method name</th>
<th>Parameters</th>
<th>Scalability</th>
<th>Usecase</th>
<th>Geometry used</th>
</tr>
</thead>
<tbody>
<tr>
<td>K-Means</td>
<td>number of clusters</td>
<td>Very large n_samples, medium n_clusters with <strong>MiniBatch code</strong></td>
<td>General-purpose, even cluster size, flat geometry, not too many clusters</td>
<td>Distances between points</td>
</tr>
<tr>
<td>Affinity propagation</td>
<td>damping, sample preference</td>
<td>Not scalable with n_samples</td>
<td>Many clusters, uneven cluster size, non-flat geometry</td>
<td>Graph distance (e.g. nearest-neighbor graph)</td>
</tr>
<tr>
<td>Mean-shift</td>
<td>bandwidth</td>
<td>Not scalable with n_samples</td>
<td>Many clusters, uneven cluster size, non-flat geometry</td>
<td>Distances between points</td>
</tr>
<tr>
<td>Spectral clustering</td>
<td>number of clusters</td>
<td>Medium n_samples, small n_clusters</td>
<td>Few clusters, even cluster size, non-flat geometry</td>
<td>Graph distance (e.g. nearest-neighbor graph)</td>
</tr>
<tr>
<td>Ward hierarchical clustering</td>
<td>number of clusters</td>
<td>Large n_samples and n_clusters</td>
<td>Many clusters, possibly connectivity constraints</td>
<td>Distances between points</td>
</tr>
<tr>
<td>Agglomerative clustering</td>
<td>number of clusters, linkage type, distance</td>
<td>Large n_samples and n_clusters</td>
<td>Many clusters, possibly connectivity constraints, non Euclidean distances</td>
<td>Any pairwise distance</td>
</tr>
<tr>
<td>DBSCAN</td>
<td>neighborhood size</td>
<td>Very large n_samples, medium n_clusters</td>
<td>Non-flat geometry, uneven cluster sizes</td>
<td>Distances between nearest points</td>
</tr>
<tr>
<td>Gaussian mixtures</td>
<td>many</td>
<td>Not scalable</td>
<td>Flat geometry, good for density estimation</td>
<td>Mahalanobis distances to centers</td>
</tr>
<tr>
<td>Birch</td>
<td>branching factor, threshold, optional global clusterer.</td>
<td>Large n_clusters and n_samples</td>
<td>Large dataset, outlier removal, data reduction.</td>
<td>Euclidean distance between points</td>
</tr>
</tbody>
</table>

Non-flat geometry clustering is useful when the clusters have a specific shape, i.e. a non-flat manifold, and the standard euclidean distance is not the right metric. This case arises in the two top rows of the figure above.

Gaussian mixture models, useful for clustering, are described in another chapter of the documentation dedicated to mixture models. KMeans can be seen as a special case of Gaussian mixture model with equal covariance per component.

**K-means**

The **KMeans** algorithm clusters data by trying to separate samples in n groups of equal variance, minimizing a criterion known as the **inertia** or within-cluster sum-of-squares. This algorithm requires the number of clusters to be specified. It scales well to large number of samples and has been used across a large range of application areas in many different fields.

The k-means algorithm divides a set of \( N \) samples \( X \) into \( K \) disjoint clusters \( C \), each described by the mean \( \mu_j \) of the samples in the cluster. The means are commonly called the cluster “centroids”; note that they are not, in general, points from \( X \), although they live in the same space. The K-means algorithm aims to choose centroids that minimise the **inertia**, or within-cluster sum of squared criterion:

\[
\sum_{i=0}^{n} \min_{\mu_j \in C}(||x_j - \mu_i||^2)
\]
Inertia, or the within-cluster sum of squares criterion, can be recognized as a measure of how internally coherent clusters are. It suffers from various drawbacks:

- Inertia makes the assumption that clusters are convex and isotropic, which is not always the case. It responds poorly to elongated clusters, or manifolds with irregular shapes.
- Inertia is not a normalized metric: we just know that lower values are better and zero is optimal. But in very high-dimensional spaces, Euclidean distances tend to become inflated (this is an instance of the so-called “curse of dimensionality”). Running a dimensionality reduction algorithm such as PCA prior to k-means clustering can alleviate this problem and speed up the computations.

K-means is often referred to as Lloyd’s algorithm. In basic terms, the algorithm has three steps. The first step chooses the initial centroids, with the most basic method being to choose \( k \) samples from the dataset \( X \). After initialization, K-means consists of looping between the two other steps. The first step assigns each sample to its nearest centroid. The second step creates new centroids by taking the mean value of all of the samples assigned to each previous centroid. The difference between the old and the new centroids are computed and the algorithm repeats these last two steps until this value is less than a threshold. In other words, it repeats until the centroids do not move significantly.
K-means is equivalent to the expectation-maximization algorithm with a small, all-equal, diagonal covariance matrix.

The algorithm can also be understood through the concept of Voronoi diagrams. First the Voronoi diagram of the points is calculated using the current centroids. Each segment in the Voronoi diagram becomes a separate cluster. Secondly, the centroids are updated to the mean of each segment. The algorithm then repeats this until a stopping criterion is fulfilled. Usually, the algorithm stops when the relative decrease in the objective function between iterations is less than the given tolerance value. This is not the case in this implementation: iteration stops when centroids move less than the tolerance.

Given enough time, K-means will always converge, however this may be to a local minimum. This is highly dependent on the initialization of the centroids. As a result, the computation is often done several times, with different initializations of the centroids. One method to help address this issue is the k-means++ initialization scheme, which has been implemented in scikit-learn (use the `init='k-means++'` parameter). This initializes the centroids to be (generally) distant from each other, leading to provably better results than random initialization, as shown in the reference.

A parameter can be given to allow K-means to be run in parallel, called `n_jobs`. Giving this parameter a positive value uses that many processors (default: 1). A value of -1 uses all available processors, with -2 using one less, and so on. Parallelization generally speeds up computation at the cost of memory (in this case, multiple copies of centroids need to be stored, one for each job).

**Warning:** The parallel version of K-Means is broken on OS X when `numpy` uses the `Accelerate` Framework. This is expected behavior: `Accelerate` can be called after a fork but you need to `execv` the subprocess with the Python binary (which multiprocessing does not do under posix).

K-means can be used for vector quantization. This is achieved using the transform method of a trained model of `KMeans`.

**Examples:**

- *Demonstration of k-means assumptions:* Demonstrating when k-means performs intuitively and when it does not
- *A demo of K-Means clustering on the handwritten digits data:* Clustering handwritten digits

**References:**

Mini Batch K-Means

The MiniBatchKMeans is a variant of the KMeans algorithm which uses mini-batches to reduce the computation time, while still attempting to optimise the same objective function. Mini-batches are subsets of the input data, randomly sampled in each training iteration. These mini-batches drastically reduce the amount of computation required to converge to a local solution. In contrast to other algorithms that reduce the convergence time of k-means, mini-batch k-means produces results that are generally only slightly worse than the standard algorithm.

The algorithm iterates between two major steps, similar to vanilla k-means. In the first step, \( b \) samples are drawn randomly from the dataset, to form a mini-batch. These are then assigned to the nearest centroid. In the second step, the centroids are updated. In contrast to k-means, this is done on a per-sample basis. For each sample in the mini-batch, the assigned centroid is updated by taking the streaming average of the sample and all previous samples assigned to that centroid. This has the effect of decreasing the rate of change for a centroid over time. These steps are performed until convergence or a predetermined number of iterations is reached.

MiniBatchKMeans converges faster than KMeans, but the quality of the results is reduced. In practice this difference in quality can be quite small, as shown in the example and cited reference.

Examples:

- Comparison of the K-Means and MiniBatchKMeans clustering algorithms: Comparison of KMeans and MiniBatchKMeans
- Clustering text documents using k-means: Document clustering using sparse MiniBatchKMeans
- Online learning of a dictionary of parts of faces

References:


Affinity Propagation

AffinityPropagation creates clusters by sending messages between pairs of samples until convergence. A dataset is then described using a small number of exemplars, which are identified as those most representative of other
samples. The messages sent between pairs represent the suitability for one sample to be the exemplar of the other, which is updated in response to the values from other pairs. This updating happens iteratively until convergence, at which point the final exemplars are chosen, and hence the final clustering is given.

Affinity Propagation can be interesting as it chooses the number of clusters based on the data provided. For this purpose, the two important parameters are the preference, which controls how many exemplars are used, and the damping factor which damps the responsibility and availability messages to avoid numerical oscillations when updating these messages.

The main drawback of Affinity Propagation is its complexity. The algorithm has a time complexity of the order $O(N^2T)$, where $N$ is the number of samples and $T$ is the number of iterations until convergence. Further, the memory complexity is of the order $O(N^2)$ if a dense similarity matrix is used, but reducible if a sparse similarity matrix is used. This makes Affinity Propagation most appropriate for small to medium sized datasets.

**Examples:**

- **Demo of affinity propagation clustering algorithm**: Affinity Propagation on a synthetic 2D datasets with 3 classes.
- **Visualizing the stock market structure** Affinity Propagation on Financial time series to find groups of companies

**Algorithm description:** The messages sent between points belong to one of two categories. The first is the responsibility $r(i, k)$, which is the accumulated evidence that sample $k$ should be the exemplar for sample $i$. The second is the availability $a(i, k)$ which is the accumulated evidence that sample $i$ should choose sample $k$ to be its exemplar, and considers the values for all other samples that $k$ should be an exemplar. In this way, exemplars are chosen by samples if they are (1) similar enough to many samples and (2) chosen by many samples to be representative of themselves.

More formally, the responsibility of a sample $k$ to be the exemplar of sample $i$ is given by:

$$r(i, k) \leftarrow s(i, k) - \max[a(i, k') + s(i, k') \forall k' \neq k]$$

Where $s(i, k)$ is the similarity between samples $i$ and $k$. The availability of sample $k$ to be the exemplar of sample $i$ is given by:

$$a(i, k) \leftarrow \min[0, r(k, k) + \sum_{i' \text{ s.t. } i' \notin \{i, k\}} r(i', k)]$$

To begin with, all values for $r$ and $a$ are set to zero, and the calculation of each iterates until convergence. As discussed above, in order to avoid numerical oscillations when updating the messages, the damping factor $\lambda$ is introduced to
iteration process:

\[ r_{t+1}(i, k) = \lambda \cdot r_t(i, k) + (1 - \lambda) \cdot r_{t+1}(i, k) \]
\[ a_{t+1}(i, k) = \lambda \cdot a_t(i, k) + (1 - \lambda) \cdot a_{t+1}(i, k) \]

where \( t \) indicates the iteration times.

**Mean Shift**

**MeanShift** clustering aims to discover **blobs** in a smooth density of samples. It is a centroid based algorithm, which works by updating candidates for centroids to be the mean of the points within a given region. These candidates are then filtered in a post-processing stage to eliminate near-duplicates to form the final set of centroids.

Given a candidate centroid \( x_i \) for iteration \( t \), the candidate is updated according to the following equation:

\[ x_{i}^{t+1} = x_i^t + m(x_i^t) \]

Where \( N(x_i) \) is the neighborhood of samples within a given distance around \( x_i \) and \( m \) is the **mean shift** vector that is computed for each centroid that points towards a region of the maximum increase in the density of points. This is computed using the following equation, effectively updating a centroid to be the mean of the samples within its neighborhood:

\[ m(x_i) = \frac{\sum_{x_j \in N(x_i)} K(x_j - x_i)x_j}{\sum_{x_j \in N(x_i)} K(x_j - x_i)} \]

The algorithm automatically sets the number of clusters, instead of relying on a parameter **bandwidth**, which dictates the size of the region to search through. This parameter can be set manually, but can be estimated using the provided **estimate_bandwidth** function, which is called if the bandwidth is not set.

The algorithm is not highly scalable, as it requires multiple nearest neighbor searches during the execution of the algorithm. The algorithm is guaranteed to converge, however the algorithm will stop iterating when the change in centroids is small.

Labelling a new sample is performed by finding the nearest centroid for a given sample.

**Examples:**

- A demo of the mean-shift clustering algorithm: Mean Shift clustering on a synthetic 2D datasets with 3 classes.
References:


Spectral clustering

SpectralClustering does a low-dimension embedding of the affinity matrix between samples, followed by a KMeans in the low dimensional space. It is especially efficient if the affinity matrix is sparse and the pyamg module is installed. SpectralClustering requires the number of clusters to be specified. It works well for a small number of clusters but is not advised when using many clusters.

For two clusters, it solves a convex relaxation of the normalised cuts problem on the similarity graph: cutting the graph in two so that the weight of the edges cut is small compared to the weights of the edges inside each cluster. This criteria is especially interesting when working on images: graph vertices are pixels, and edges of the similarity graph are a function of the gradient of the image.

**Warning:** Transforming distance to well-behaved similarities

Note that if the values of your similarity matrix are not well distributed, e.g. with negative values or with a distance matrix rather than a similarity, the spectral problem will be singular and the problem not solvable. In which case it is advised to apply a transformation to the entries of the matrix. For instance, in the case of a signed distance matrix, is common to apply a heat kernel:

```
similarity = np.exp(-beta * distance / distance.std())
```

See the examples for such an application.

Examples:

• *Spectral clustering for image segmentation:* Segmenting objects from a noisy background using spectral clustering.

• *Segmenting the picture of a raccoon face in regions:* Spectral clustering to split the image of the raccoon face in regions.
Different label assignment strategies

Different label assignment strategies can be used, corresponding to the `assign_labels` parameter of `SpectralClustering`. The "kmeans" strategy can match finer details of the data, but it can be more unstable. In particular, unless you control the `random_state`, it may not be reproducible from run-to-run, as it depends on a random initialization. On the other hand, the "discretize" strategy is 100% reproducible, but it tends to create parcels of fairly even and geometrical shape.

```python
assign_labels="kmeans"
assign_labels="discretize"
```

![Spectral clustering: kmeans, 6.68s](image1)
![Spectral clustering: discretize, 5.83s](image2)

References:

- “Normalized cuts and image segmentation” Jianbo Shi, Jitendra Malik, 2000
- “On Spectral Clustering: Analysis and an algorithm” Andrew Y. Ng, Michael I. Jordan, Yair Weiss, 2001

Hierarchical clustering

Hierarchical clustering is a general family of clustering algorithms that build nested clusters by merging or splitting them successively. This hierarchy of clusters is represented as a tree (or dendrogram). The root of the tree is the unique cluster that gathers all the samples, the leaves being the clusters with only one sample. See the Wikipedia page for more details.

The `AgglomerativeClustering` object performs a hierarchical clustering using a bottom up approach: each observation starts in its own cluster, and clusters are successively merged together. The linkage criteria determines the metric used for the merge strategy:

- **Ward** minimizes the sum of squared differences within all clusters. It is a variance-minimizing approach and in this sense is similar to the k-means objective function but tackled with an agglomerative hierarchical approach.
- **Maximum** or **complete linkage** minimizes the maximum distance between observations of pairs of clusters.
- **Average linkage** minimizes the average of the distances between all observations of pairs of clusters.

*AgglomerativeClustering* can also scale to large number of samples when it is used jointly with a connectivity matrix, but is computationally expensive when no connectivity constraints are added between samples: it considers at each step all the possible merges.

**FeatureAgglomeration**

The *FeatureAgglomeration* uses agglomerative clustering to group together features that look very similar, thus decreasing the number of features. It is a dimensionality reduction tool, see *Unsupervised dimensionality reduction*.

### Different linkage type: Ward, complete and average linkage

*AgglomerativeClustering* supports Ward, average, and complete linkage strategies.

![Agglomerative Clustering on a 2D embedding of digits](image)

Agglomerative cluster has a “rich get richer” behavior that leads to uneven cluster sizes. In this regard, complete linkage is the worst strategy, and Ward gives the most regular sizes. However, the affinity (or distance used in clustering) cannot be varied with Ward, thus for non Euclidean metrics, average linkage is a good alternative.

**Examples:**

- *Various Agglomerative Clustering on a 2D embedding of digits*: exploration of the different linkage strategies in a real dataset.

### Adding connectivity constraints

An interesting aspect of *AgglomerativeClustering* is that connectivity constraints can be added to this algorithm (only adjacent clusters can be merged together), through a connectivity matrix that defines for each sample the neighboring samples following a given structure of the data. For instance, in the swiss-roll example below, the connectivity constraints forbid the merging of points that are not adjacent on the swiss roll, and thus avoid forming clusters that extend across overlapping folds of the roll.
These constraints are useful to impose a certain local structure, but they also make the algorithm faster, especially when the number of the samples is high.

The connectivity constraints are imposed via an connectivity matrix: a scipy sparse matrix that has elements only at the intersection of a row and a column with indices of the dataset that should be connected. This matrix can be constructed from a-priori information: for instance, you may wish to cluster web pages by only merging pages with a link pointing from one to another. It can also be learned from the data, for instance using `sklearn.neighbors.kneighbors_graph` to restrict merging to nearest neighbors as in this example, or using `sklearn.feature_extraction.image.grid_to_graph` to enable only merging of neighboring pixels on an image, as in the raccoon face example.

Examples:

- A demo of structured Ward hierarchical clustering on a raccoon face image: Ward clustering to split the image of a raccoon face in regions.
- Hierarchical clustering: structured vs unstructured ward: Example of Ward algorithm on a swiss-roll, comparison of structured approaches versus unstructured approaches.
- Feature agglomeration vs. univariate selection: Example of dimensionality reduction with feature agglomeration based on Ward hierarchical clustering.
- Agglomerative clustering with and without structure

Warning: Connectivity constraints with average and complete linkage

Connectivity constraints and complete or average linkage can enhance the ‘rich getting richer’ aspect of agglomerative clustering, particularly so if they are built with `sklearn.neighbors.kneighbors_graph`. In the limit of a small number of clusters, they tend to give a few macroscopically occupied clusters and almost empty ones. (see the discussion in Agglomerative clustering with and without structure).
Varying the metric

Average and complete linkage can be used with a variety of distances (or affinities), in particular Euclidean distance ($l_2$), Manhattan distance (or Cityblock, or $l_1$), cosine distance, or any precomputed affinity matrix.

- $l_1$ distance is often good for sparse features, or sparse noise: i.e. many of the features are zero, as in text mining using occurrences of rare words.
- cosine distance is interesting because it is invariant to global scalings of the signal.

The guidelines for choosing a metric is to use one that maximizes the distance between samples in different classes, and minimizes that within each class.

Examples:

- Agglomerative clustering with different metrics

**DBSCAN**

The **DBSCAN** algorithm views clusters as areas of high density separated by areas of low density. Due to this rather generic view, clusters found by DBSCAN can be any shape, as opposed to k-means which assumes that clusters are convex shaped. The central component to the DBSCAN is the concept of core samples, which are samples that are in areas of high density. A cluster is therefore a set of core samples, each close to each other (measured by some distance measure) and a set of non-core samples that are close to a core sample (but are not themselves core samples). There are two parameters to the algorithm, min_samples and eps, which define formally what we mean when we say dense. Higher min_samples or lower eps indicate higher density necessary to form a cluster.

More formally, we define a core sample as being a sample in the dataset such that there exist min_samples other samples within a distance of eps, which are defined as neighbors of the core sample. This tells us that the core sample is in a dense area of the vector space. A cluster is a set of core samples that can be built by recursively taking a core sample, finding all of its neighbors that are core samples, finding all of their neighbors that are core samples, and so on. A cluster also has a set of non-core samples, which are samples that are neighbors of a core sample in the cluster but are not themselves core samples. Intuitively, these samples are on the fringes of a cluster.
Any core sample is part of a cluster, by definition. Any sample that is not a core sample, and is at least $\epsilon$ in distance from any core sample, is considered an outlier by the algorithm.

In the figure below, the color indicates cluster membership, with large circles indicating core samples found by the algorithm. Smaller circles are non-core samples that are still part of a cluster. Moreover, the outliers are indicated by black points below.

Examples:

- Demo of DBSCAN clustering algorithm

Implementation

The DBSCAN algorithm is deterministic, always generating the same clusters when given the same data in the same order. However, the results can differ when data is provided in a different order. First, even though the core samples will always be assigned to the same clusters, the labels of those clusters will depend on the order in which those samples are encountered in the data. Second and more importantly, the clusters to which non-core samples are assigned can differ depending on the data order. This would happen when a non-core sample has a distance lower than $\epsilon$ to two core samples in different clusters. By the triangular inequality, those two core samples must be more distant than $\epsilon$ from each other, or they would be in the same cluster. The non-core sample is assigned to whichever cluster is generated first in a pass through the data, and so the results will depend on the data ordering.

The current implementation uses ball trees and kd-trees to determine the neighborhood of points, which avoids calculating the full distance matrix (as was done in scikit-learn versions before 0.14). The possibility to use custom metrics is retained; for details, see NearestNeighbors.

Memory consumption for large sample sizes

This implementation is by default not memory efficient because it constructs a full pairwise similarity matrix in the case where kd-trees or ball-trees cannot be used (e.g. with sparse matrices). This matrix will consume $n^2$ floats. A couple of mechanisms for getting around this are:

- A sparse radius neighborhood graph (where missing entries are presumed to be out of $\epsilon$) can be precomputed in a memory-efficient way and dbscan can be run over this with metric='precomputed'.
- The dataset can be compressed, either by removing exact duplicates if these occur in your data, or by using BIRCH. Then you only have a relatively small number of representatives for a large number of points. You
can then provide a `sample_weight` when fitting DBSCAN.

References:


Birch

The Birch builds a tree called the Characteristic Feature Tree (CFT) for the given data. The data is essentially lossy compressed to a set of Characteristic Feature nodes (CF Nodes). The CF Nodes have a number of subclusters called Characteristic Feature subclusters (CF Subclusters) and these CF Subclusters located in the non-terminal CF Nodes can have CF Nodes as children.

The CF Subclusters hold the necessary information for clustering which prevents the need to hold the entire input data in memory. This information includes:

- Number of samples in a subcluster.
- Linear Sum - A n-dimensional vector holding the sum of all samples
- Squared Sum - Sum of the squared L2 norm of all samples.
- Centroids - To avoid recalculation linear sum / n_samples.
- Squared norm of the centroids.

The Birch algorithm has two parameters, the threshold and the branching factor. The branching factor limits the number of subclusters in a node and the threshold limits the distance between the entering sample and the existing subclusters.

This algorithm can be viewed as an instance or data reduction method, since it reduces the input data to a set of subclusters which are obtained directly from the leaves of the CFT. This reduced data can be further processed by feeding it into a global clusterer. This global clusterer can be set by `n_clusters`. If `n_clusters` is set to None, the subclusters from the leaves are directly read off, otherwise a global clustering step labels these subclusters into global clusters (labels) and the samples are mapped to the global label of the nearest subcluster.

Algorithm description:

- A new sample is inserted into the root of the CF Tree which is a CF Node. It is then merged with the subcluster of the root, that has the smallest radius after merging, constrained by the threshold and branching factor conditions. If the subcluster has any child node, then this is done repeatedly till it reaches a leaf. After finding the nearest subcluster in the leaf, the properties of this subcluster and the parent subclusters are recursively updated.

- If the radius of the subcluster obtained by merging the new sample and the nearest subcluster is greater than the square of the threshold and if the number of subclusters is greater than the branching factor, then a space is temporarily allocated to this new sample. The two farthest subclusters are taken and the subclusters are divided into two groups on the basis of the distance between these subclusters.

- If this split node has a parent subcluster and there is room for a new subcluster, then the parent is split into two. If there is no room, then this node is again split into two and the process is continued recursively, till it reaches the root.

Birch or MiniBatchKMeans?

- Birch does not scale very well to high dimensional data. As a rule of thumb if `n_features` is greater than twenty, it is generally better to use MiniBatchKMeans.
• If the number of instances of data needs to be reduced, or if one wants a large number of subclusters either as a preprocessing step or otherwise, Birch is more useful than MiniBatchKMeans.

**How to use partial_fit?**

To avoid the computation of global clustering, for every call of `partial_fit` the user is advised

1. To set `n_clusters=None` initially
2. Train all data by multiple calls to `partial_fit`.
3. Set `n_clusters` to a required value using `brc.set_params(n_clusters=n_clusters)`.
4. Call `partial_fit` finally with no arguments, i.e. `brc.partial_fit()` which performs the global clustering.

References:

• Roberto Perdisci JBirch - Java implementation of BIRCH clustering algorithm https://code.google.com/archive/p/jbirch

**Clustering performance evaluation**

Evaluating the performance of a clustering algorithm is not as trivial as counting the number of errors or the precision and recall of a supervised classification algorithm. In particular any evaluation metric should not take the absolute values of the cluster labels into account but rather if this clustering define separations of the data similar to some ground truth set of classes or satisfying some assumption such that members belong to the same class are more similar that members of different classes according to some similarity metric.

**Adjusted Rand index**

Given the knowledge of the ground truth class assignments `labels_true` and our clustering algorithm assignments of the same samples `labels_pred`, the *adjusted Rand index* is a function that measures the *similarity* of the two assignments, ignoring permutations and with *chance normalization*:

```python
>>> from sklearn import metrics
>>> labels_true = [0, 0, 0, 1, 1, 1]
>>> labels_pred = [0, 0, 1, 1, 2, 2]
```
metrics.adjusted_rand_score(labels_true, labels_pred)
0.24...

One can permute 0 and 1 in the predicted labels, rename 2 to 3, and get the same score:

labels_pred = [1, 1, 0, 0, 3, 3]
metrics.adjusted_rand_score(labels_true, labels_pred)
0.24...

Furthermore, adjusted_rand_score is symmetric: swapping the argument does not change the score. It can thus be used as a consensus measure:

metrics.adjusted_rand_score(labels_pred, labels_true)
0.24...

Perfect labeling is scored 1.0:

labels_pred = labels_true[:]
metrics.adjusted_rand_score(labels_true, labels_pred)
1.0

Bad (e.g. independent labelings) have negative or close to 0.0 scores:

labels_true = [0, 1, 2, 0, 3, 4, 5, 1]
labels_pred = [1, 1, 0, 0, 2, 2, 2, 2]
metrics.adjusted_rand_score(labels_true, labels_pred)
-0.12...

Advantages

• Random (uniform) label assignments have a ARI score close to 0.0 for any value of n_clusters and n_samples (which is not the case for raw Rand index or the V-measure for instance).
• Bounded range [-1, 1]: negative values are bad (independent labelings), similar clusterings have a positive ARI, 1.0 is the perfect match score.
• No assumption is made on the cluster structure: can be used to compare clustering algorithms such as k-means which assumes isotropic blob shapes with results of spectral clustering algorithms which can find cluster with “folded” shapes.

Drawbacks

• Contrary to inertia, ARI requires knowledge of the ground truth classes while is almost never available in practice or requires manual assignment by human annotators (as in the supervised learning setting).

However ARI can also be useful in a purely unsupervised setting as a building block for a Consensus Index that can be used for clustering model selection (TODO).

Examples:

• Adjustment for chance in clustering performance evaluation: Analysis of the impact of the dataset size on the value of clustering measures for random assignments.
Mathematical formulation

If C is a ground truth class assignment and K the clustering, let us define a and b as:

- \( a \), the number of pairs of elements that are in the same set in C and in the same set in K
- \( b \), the number of pairs of elements that are in different sets in C and in different sets in K

The raw (unadjusted) Rand index is then given by:

\[
RI = \frac{a + b}{C_2^{n_{\text{samples}}}}
\]

Where \( C_2^{n_{\text{samples}}} \) is the total number of possible pairs in the dataset (without ordering).

However the RI score does not guarantee that random label assignments will get a value close to zero (esp. if the number of clusters is in the same order of magnitude as the number of samples).

To counter this effect we can discount the expected RI \( E[RI] \) of random labelings by defining the adjusted Rand index as follows:

\[
ARI = \frac{RI - E[RI]}{\max(RI) - E[RI]}
\]

References

- Comparing Partitions L. Hubert and P. Arabie, Journal of Classification 1985
- Wikipedia entry for the adjusted Rand index

Mutual Information based scores

Given the knowledge of the ground truth class assignments \( \text{labels\_true} \) and our clustering algorithm assignments of the same samples \( \text{labels\_pred} \), the Mutual Information is a function that measures the agreement of the two assignments, ignoring permutations. Two different normalized versions of this measure are available, Normalized Mutual Information(NMI) and Adjusted Mutual Information(AMI). NMI is often used in the literature while AMI was proposed more recently and is normalized against chance:

```python
>>> from sklearn import metrics
>>> labels_true = [0, 0, 0, 1, 1, 1]
>>> labels_pred = [0, 0, 1, 1, 2, 2]

>>> metrics.adjusted_mutual_info_score(labels_true, labels_pred)
0.22504...
```

One can permute 0 and 1 in the predicted labels, rename 2 to 3 and get the same score:

```python
>>> labels_pred = [1, 1, 0, 0, 3, 3]
>>> metrics.adjusted_mutual_info_score(labels_true, labels_pred)
0.22504...
```

All, \( \text{mutual\_info\_score}, \text{adjusted\_mutual\_info\_score} \) and \( \text{normalized\_mutual\_info\_score} \) are symmetric: swapping the argument does not change the score. Thus they can be used as a consensus measure:

```python
>>> metrics.adjusted_mutual_info_score(labels_pred, labels_true)
0.22504...
```
Perfect labeling is scored 1.0:

```python
>>> labels_pred = labels_true[:]
>>> metrics.adjusted_mutual_info_score(labels_true, labels_pred)
1.0

>>> metrics.normalized_mutual_info_score(labels_true, labels_pred)
1.0
```

This is not true for `mutual_info_score`, which is therefore harder to judge:

```python
>>> metrics.mutual_info_score(labels_true, labels_pred)
0.69...
```

Bad (e.g. independent labelings) have non-positive scores:

```python
>>> labels_true = [0, 1, 2, 0, 3, 4, 5, 1]
>>> labels_pred = [1, 1, 0, 0, 2, 2, 2, 2]
>>> metrics.adjusted_mutual_info_score(labels_true, labels_pred)
-0.10526...
```

**Advantages**

- **Random (uniform) label assignments have a AMI score close to 0.0** for any value of `n_clusters` and `n_samples` (which is not the case for raw Mutual Information or the V-measure for instance).
- **Bounded range [0, 1]**: Values close to zero indicate two label assignments that are largely independent, while values close to one indicate significant agreement. Further, values of exactly 0 indicate purely independent label assignments and a AMI of exactly 1 indicates that the two label assignments are equal (with or without permutation).
- **No assumption is made on the cluster structure**: can be used to compare clustering algorithms such as k-means which assumes isotropic blob shapes with results of spectral clustering algorithms which can find cluster with “folded” shapes.

**Drawbacks**

- Contrary to inertia, **MI-based measures require the knowledge of the ground truth classes** while almost never available in practice or requires manual assignment by human annotators (as in the supervised learning setting).

  However MI-based measures can also be useful in purely unsupervised setting as a building block for a Consensus Index that can be used for clustering model selection.
- **NMI and MI are not adjusted against chance**.

**Examples:**

- **Adjustment for chance in clustering performance evaluation**: Analysis of the impact of the dataset size on the value of clustering measures for random assignments. This example also includes the Adjusted Rand Index.
Mathematical formulation

Assume two label assignments (of the same N objects), $U$ and $V$. Their entropy is the amount of uncertainty for a partition set, defined by:

$$H(U) = -\sum_{i=1}^{\left|U\right|} P(i) \log(P(i))$$

where $P(i) = |U_i|/N$ is the probability that an object picked at random from $U$ falls into class $U_i$. Likewise for $V$:

$$H(V) = -\sum_{j=1}^{\left|V\right|} P'(j) \log(P'(j))$$

With $P'(j) = |V_j|/N$. The mutual information (MI) between $U$ and $V$ is calculated by:

$$\text{MI}(U, V) = \sum_{i=1}^{\left|U\right|} \sum_{j=1}^{\left|V\right|} P(i,j) \log \left( \frac{P(i,j)}{P(i)P'(j)} \right)$$

where $P(i, j) = |U_i \cap V_j|/N$ is the probability that an object picked at random falls into both classes $U_i$ and $V_j$.

It also can be expressed in set cardinality formulation:

$$\text{MI}(U, V) = \sum_{i=1}^{\left|U\right|} \sum_{j=1}^{\left|V\right|} \frac{|U_i \cap V_j|}{N} \log \left( \frac{N|U_i \cap V_j|}{|U_i||V_j|} \right)$$

The normalized mutual information is defined as

$$\text{NMI}(U, V) = \frac{\text{MI}(U, V)}{\sqrt{H(U)H(V)}}$$

This value of the mutual information and also the normalized variant is not adjusted for chance and will tend to increase as the number of different labels (clusters) increases, regardless of the actual amount of “mutual information” between the label assignments.

The expected value for the mutual information can be calculated using the following equation, from Vinh, Epps, and Bailey, (2009). In this equation, $a_i = |U_i|$ (the number of elements in $U_i$) and $b_j = |V_j|$ (the number of elements in $V_j$).

$$E[\text{MI}(U, V)] = \sum_{i=1}^{\left|U\right|} \sum_{j=1}^{\left|V\right|} \min(a_i, b_j) \frac{n_{ij}}{N} \log \left( \frac{N n_{ij}}{a_i b_j} \right) \frac{a_i!b_j!(N - a_i)!(N - b_j)!}{N!n_{ij}!(a_i - n_{ij})!(b_j - n_{ij})!(N - a_i - b_j + n_{ij})!}$$

Using the expected value, the adjusted mutual information can then be calculated using a similar form to that of the adjusted Rand index:

$$\text{AMI} = \frac{\text{MI} - E[\text{MI}]}{\max(H(U), H(V)) - E[\text{MI}]}$$

References

Homogeneity, completeness and V-measure

Given the knowledge of the ground truth class assignments of the samples, it is possible to define some intuitive metric using conditional entropy analysis.

In particular Rosenberg and Hirschberg (2007) define the following two desirable objectives for any cluster assignment:

- **homogeneity**: each cluster contains only members of a single class.
- **completeness**: all members of a given class are assigned to the same cluster.

We can turn those concept as scores `homogeneity_score` and `completeness_score`. Both are bounded below by 0.0 and above by 1.0 (higher is better):

```python
>>> from sklearn import metrics

>>> labels_true = [0, 0, 0, 1, 1, 1]
>>> labels_pred = [0, 0, 1, 1, 2, 2]

>>> metrics.homogeneity_score(labels_true, labels_pred)
0.66...

>>> metrics.completeness_score(labels_true, labels_pred)
0.42...
```

Their harmonic mean called **V-measure** is computed by `v_measure_score`:

```python
>>> metrics.v_measure_score(labels_true, labels_pred)
0.51...
```

The V-measure is actually equivalent to the mutual information (NMI) discussed above normalized by the sum of the label entropies [B2011].

Homogeneity, completeness and V-measure can be computed at once using `homogeneity_completeness_v_measure` as follows:

```python
>>> metrics.homogeneity_completeness_v_measure(labels_true, labels_pred)
...(0.66..., 0.42..., 0.51...)
```

The following clustering assignment is slightly better, since it is homogeneous but not complete:

```python
>>> labels_pred = [0, 0, 0, 1, 2, 2]
...
>>> metrics.homogeneity_completeness_v_measure(labels_true, labels_pred)
...(1.0, 0.68..., 0.81...)
```
Note: \( v\_measure\_score \) is symmetric: it can be used to evaluate the agreement of two independent assignments on the same dataset.

This is not the case for \( completeness\_score \) and \( homogeneity\_score \): both are bound by the relationship:

\[
\text{homogeneity\_score}(a, b) = \text{completeness\_score}(b, a)
\]

**Advantages**

- **Bounded scores**: 0.0 is as bad as it can be, 1.0 is a perfect score.
- Intuitive interpretation: clustering with bad V-measure can be qualitatively analyzed in terms of homogeneity and completeness to better feel what ‘kind’ of mistakes is done by the assignment.
- **No assumption is made on the cluster structure**: can be used to compare clustering algorithms such as k-means which assumes isotropic blob shapes with results of spectral clustering algorithms which can find cluster with “folded” shapes.

**Drawbacks**

- The previously introduced metrics are **not normalized with regards to random labeling**: this means that depending on the number of samples, clusters and ground truth classes, a completely random labeling will not always yield the same values for homogeneity, completeness and hence v-measure. In particular **random labeling won’t yield zero scores especially when the number of clusters is large**.

  This problem can safely be ignored when the number of samples is more than a thousand and the number of clusters is less than 10. **For smaller sample sizes or larger number of clusters it is safer to use an adjusted index such as the Adjusted Rand Index (ARI).**

- These metrics **require the knowledge of the ground truth classes** while almost never available in practice or requires manual assignment by human annotators (as in the supervised learning setting).

**Examples:**

- **Adjustment for chance in clustering performance evaluation**: Analysis of the impact of the dataset size on the value of clustering measures for random assignments.

**Mathematical formulation**

Homogeneity and completeness scores are formally given by:

\[
h = 1 - \frac{H(C|K)}{H(C)}
\]

\[
c = 1 - \frac{H(K|C)}{H(K)}
\]

where \( H(C|K) \) is the **conditional entropy of the classes given the cluster assignments** and is given by:

\[
H(C|K) = - \sum_{c=1}^{C} \sum_{k=1}^{K} \frac{n_{c,k}}{n} \log \left( \frac{n_{c,k}}{n_k} \right)
\]
Clustering measures for 2 random uniform labelings with equal number of clusters

Score value

Number of clusters (Number of samples is fixed to 100)
and $H(C)$ is the **entropy of the classes** and is given by:

$$H(C) = -\sum_{c=1}^{|C|} \frac{n_c}{n} \cdot \log \left( \frac{n_c}{n} \right)$$

with $n$ the total number of samples, $n_c$ and $n_k$ the number of samples respectively belonging to class $c$ and cluster $k$, and finally $n_{c,k}$ the number of samples from class $c$ assigned to cluster $k$.

The **conditional entropy of clusters given class** $H(K|C)$ and the **entropy of clusters** $H(K)$ are defined in a symmetric manner.

Rosenberg and Hirschberg further define **V-measure** as the **harmonic mean of homogeneity and completeness**:

$$v = \frac{2 \cdot h \cdot c}{h + c}$$

**References**

- **V-Measure: A conditional entropy-based external cluster evaluation measure** Andrew Rosenberg and Julia Hirschberg, 2007

**Fowlkes-Mallows scores**

The Fowlkes-Mallows index (*sklearn.metrics.fowlkes_mallows_score*) can be used when the ground truth class assignments of the samples is known. The Fowlkes-Mallows score FMI is defined as the geometric mean of the pairwise precision and recall:

$$\text{FMI} = \frac{\text{TP}}{\sqrt{(\text{TP} + \text{FP}) (\text{TP} + \text{FN})}}$$

Where TP is the number of **True Positive** (i.e. the number of pair of points that belong to the same clusters in both the true labels and the predicted labels), FP is the number of **False Positive** (i.e. the number of pair of points that belong to the same clusters in the true labels and not in the predicted labels) and FN is the number of **False Negative** (i.e. the number of pair of points that belongs in the same clusters in the predicted labels and not in the true labels).

The score ranges from 0 to 1. A high value indicates a good similarity between two clusters.

```python
>>> from sklearn import metrics

>>> labels_true = [0, 0, 0, 1, 1, 1]
>>> labels_pred = [0, 0, 1, 1, 2, 2]

>>> metrics.fowlkes_mallows_score(labels_true, labels_pred)
0.47140...
```

One can permute 0 and 1 in the predicted labels, rename 2 to 3 and get the same score:

```python
>>> labels_pred = [1, 1, 0, 0, 3, 3]

>>> metrics.fowlkes_mallows_score(labels_true, labels_pred)
0.47140...
```

Perfect labeling is scored 1.0:
```python
>>> labels_pred = labels_true[:]
>>> metrics.fowlkes_mallows_score(labels_true, labels_pred)
1.0
```

Bad (e.g. independent labelings) have zero scores:

```python
>>> labels_true = [0, 1, 2, 0, 3, 4, 5, 1]
>>> labels_pred = [1, 1, 0, 0, 2, 2, 2, 2]
>>> metrics.fowlkes_mallows_score(labels_true, labels_pred)
0.0
```

Advantages

- **Random (uniform) label assignments have a FMI score close to 0.0** for any value of n_clusters and n_samples (which is not the case for raw Mutual Information or the V-measure for instance).
- **Bounded range [0, 1]**: Values close to zero indicate two label assignments that are largely independent, while values close to one indicate significant agreement. Further, values of exactly 0 indicate purely independent label assignments and a AMI of exactly 1 indicates that the two label assignments are equal (with or without permutation).
- **No assumption is made on the cluster structure**: can be used to compare clustering algorithms such as k-means which assumes isotropic blob shapes with results of spectral clustering algorithms which can find cluster with “folded” shapes.

Drawbacks

- Contrary to inertia, **FMI-based measures require the knowledge of the ground truth classes** while almost never available in practice or requires manual assignment by human annotators (as in the supervised learning setting).

References

- Wikipedia entry for the Fowlkes-Mallows Index

Silhouette Coefficient

If the ground truth labels are not known, evaluation must be performed using the model itself. The Silhouette Coefficient (sklearn.metrics.silhouette_score) is an example of such an evaluation, where a higher Silhouette Coefficient score relates to a model with better defined clusters. The Silhouette Coefficient is defined for each sample and is composed of two scores:

- **a**: The mean distance between a sample and all other points in the same class.
- **b**: The mean distance between a sample and all other points in the next nearest cluster.

The Silhouette Coefficient \( s \) for a single sample is then given as:

\[
s = \frac{b - a}{\max(a, b)}
\]
The Silhouette Coefficient for a set of samples is given as the mean of the Silhouette Coefficient for each sample.

```python
>>> from sklearn import metrics
>>> from sklearn.metrics import pairwise_distances
>>> from sklearn import datasets

>>> dataset = datasets.load_iris()
>>> X = dataset.data
>>> y = dataset.target
```

In normal usage, the Silhouette Coefficient is applied to the results of a cluster analysis.

```python
>>> import numpy as np
>>> from sklearn.cluster import KMeans

>>> kmeans_model = KMeans(n_clusters=3, random_state=1).fit(X)
>>> labels = kmeans_model.labels_
>>> metrics.silhouette_score(X, labels, metric='euclidean')
... 0.55...
```

### References


### Advantages

- The score is bounded between -1 for incorrect clustering and +1 for highly dense clustering. Scores around zero indicate overlapping clusters.
- The score is higher when clusters are dense and well separated, which relates to a standard concept of a cluster.

### Drawbacks

- The Silhouette Coefficient is generally higher for convex clusters than other concepts of clusters, such as density based clusters like those obtained through DBSCAN.

### Examples:

- Selecting the number of clusters with silhouette analysis on KMeans clustering: In this example the silhouette analysis is used to choose an optimal value for n_clusters.

### Calinski-Harabaz Index

If the ground truth labels are not known, the Calinski-Harabaz index (sklearn.metrics.calinski_harabaz_score) can be used to evaluate the model, where a higher Calinski-Harabaz score relates to a model with better defined clusters.
For $k$ clusters, the Calinski-Harabaz score $s$ is given as the ratio of the between-clusters dispersion mean and the within-cluster dispersion:

$$ s(k) = \frac{\text{Tr}(B_k)}{\text{Tr}(W_k)} \times \frac{N - k}{k - 1} $$

where $B_K$ is the between group dispersion matrix and $W_K$ is the within-cluster dispersion matrix defined by:

$$ W_k = \sum_{q=1}^{k} \sum_{x \in C_q} (x - c_q)(x - c_q)^T $$

$$ B_k = \sum_{q} n_q(c_q - c)(c_q - c)^T $$

with $N$ be the number of points in our data, $C_q$ be the set of points in cluster $q$, $c_q$ be the center of cluster $q$, $c$ be the center of $E$, $n_q$ be the number of points in cluster $q$.

In normal usage, the Calinski-Harabaz index is applied to the results of a cluster analysis.

```python
>>> from sklearn import metrics
>>> from sklearn.metrics import pairwise_distances
>>> from sklearn import datasets
>>> dataset = datasets.load_iris()
>>> X = dataset.data
>>> y = dataset.target
>>> from sklearn.cluster import KMeans
>>> kmeans_model = KMeans(n_clusters=3, random_state=1).fit(X)
>>> labels = kmeans_model.labels_
>>> metrics.calinski_harabaz_score(X, labels)
560.39...
```

**Advantages**

- The score is higher when clusters are dense and well separated, which relates to a standard concept of a cluster.
- The score is fast to compute

**Drawbacks**

- The Calinski-Harabaz index is generally higher for convex clusters than other concepts of clusters, such as density based clusters like those obtained through DBSCAN.

**References**

3.2.4 Biclustering

Biclustering can be performed with the module `sklearn.cluster.bicluster`. Biclustering algorithms simultaneously cluster rows and columns of a data matrix. These clusters of rows and columns are known as biclusters. Each determines a submatrix of the original data matrix with some desired properties.

For instance, given a matrix of shape `(10, 10)`, one possible bicluster with three rows and two columns induces a submatrix of shape `(3, 2):

```python
>>> import numpy as np

>>> data = np.arange(100).reshape(10, 10)

>>> rows = np.array([0, 2, 3])[:, np.newaxis]

>>> columns = np.array([1, 2])

>>> data[rows, columns]

array([[1, 2],
        [21, 22],
        [31, 32]])
```

For visualization purposes, given a bicluster, the rows and columns of the data matrix may be rearranged to make the bicluster contiguous.

Algorithms differ in how they define biclusters. Some of the common types include:

- constant values, constant rows, or constant columns
- unusually high or low values
- submatrices with low variance
- correlated rows or columns

Algorithms also differ in how rows and columns may be assigned to biclusters, which leads to different bicluster structures. Block diagonal or checkerboard structures occur when rows and columns are divided into partitions.

If each row and each column belongs to exactly one bicluster, then rearranging the rows and columns of the data matrix reveals the biclusters on the diagonal. Here is an example of this structure where biclusters have higher average values than the other rows and columns:

![Fig. 3.5: An example of biclusters formed by partitioning rows and columns.](image)

In the checkerboard case, each row belongs to all column clusters, and each column belongs to all row clusters. Here is an example of this structure where the variance of the values within each bicluster is small:
Fig. 3.6: An example of checkerboard biclusters.

After fitting a model, row and column cluster membership can be found in the `rows_` and `columns_` attributes. `rows_[i]` is a binary vector with nonzero entries corresponding to rows that belong to bicluster `i`. Similarly, `columns_[i]` indicates which columns belong to bicluster `i`.

Some models also have `row_labels_` and `column_labels_` attributes. These models partition the rows and columns, such as in the block diagonal and checkerboard bicluster structures.

**Note:** Biclustering has many other names in different fields including co-clustering, two-mode clustering, two-way clustering, block clustering, coupled two-way clustering, etc. The names of some algorithms, such as the Spectral Co-Clustering algorithm, reflect these alternate names.

**Spectral Co-Clustering**

The `SpectralCoclustering` algorithm finds biclusters with values higher than those in the corresponding other rows and columns. Each row and each column belongs to exactly one bicluster, so rearranging the rows and columns to make partitions contiguous reveals these high values along the diagonal:

**Note:** The algorithm treats the input data matrix as a bipartite graph: the rows and columns of the matrix correspond to the two sets of vertices, and each entry corresponds to an edge between a row and a column. The algorithm approximates the normalized cut of this graph to find heavy subgraphs.

**Mathematical formulation**

An approximate solution to the optimal normalized cut may be found via the generalized eigenvalue decomposition of the Laplacian of the graph. Usually this would mean working directly with the Laplacian matrix. If the original data matrix `A` has shape `m × n`, the Laplacian matrix for the corresponding bipartite graph has shape `(m + n) × (m + n)`. However, in this case it is possible to work directly with `A`, which is smaller and more efficient.

The input matrix `A` is preprocessed as follows:

\[ A_n = R^{-1/2} A C^{-1/2} \]
Where $R$ is the diagonal matrix with entry $i$ equal to $\sum_j A_{ij}$ and $C$ is the diagonal matrix with entry $j$ equal to $\sum_i A_{ij}$.

The singular value decomposition, $A_n = U \Sigma V^\top$, provides the partitions of the rows and columns of $A$. A subset of the left singular vectors gives the row partitions, and a subset of the right singular vectors gives the column partitions.

The $\ell = \lceil \log_2 k \rceil$ singular vectors, starting from the second, provide the desired partitioning information. They are used to form the matrix $Z$:

$$Z = \begin{bmatrix} R^{-1/2}U \\ C^{-1/2}V \end{bmatrix}$$

where the columns of $U$ are $u_2, \ldots, u_{\ell+1}$, and similarly for $V$.

Then the rows of $Z$ are clustered using $k$-means. The first $n_{\text{rows}}$ labels provide the row partitioning, and the remaining $n_{\text{columns}}$ labels provide the column partitioning.

### Examples:

- **A demo of the Spectral Co-Clustering algorithm**: A simple example showing how to generate a data matrix with biclusters and apply this method to it.
- **Biclustering documents with the Spectral Co-clustering algorithm**: An example of finding biclusters in the twenty newsgroup dataset.

### References:


## Spectral Biclustering

The **SpectralBiclustering** algorithm assumes that the input data matrix has a hidden checkerboard structure. The rows and columns of a matrix with this structure may be partitioned so that the entries of any bicluster in the Cartesian product of row clusters and column clusters are approximately constant. For instance, if there are two row partitions and three column partitions, each row will belong to three biclusters, and each column will belong to two biclusters.

The algorithm partitions the rows and columns of a matrix so that a corresponding blockwise-constant checkerboard matrix provides a good approximation to the original matrix.

### Mathematical formulation

The input matrix $A$ is first normalized to make the checkerboard pattern more obvious. There are three possible methods:

1. **Independent row and column normalization**, as in Spectral Co-Clustering. This method makes the rows sum to a constant and the columns sum to a different constant.
2. **Bistochastization**: repeated row and column normalization until convergence. This method makes both rows and columns sum to the same constant.
3. **Log normalization**: the log of the data matrix is computed: $L = \log A$. Then the column mean $\overline{L}_j$, row mean $\overline{L}_i$, and overall mean $\overline{L}$ of $L$ are computed. The final matrix is computed according to the formula...
\[ K_{ij} = L_{ij} - L_{i \cdot} - L_{\cdot j} + L_{\cdot \cdot} \]

After normalizing, the first few singular vectors are computed, just as in the Spectral Co-Clustering algorithm.

If log normalization was used, all the singular vectors are meaningful. However, if independent normalization or bistochastization were used, the first singular vectors, \( u_1 \) and \( v_1 \), are discarded. From now on, the “first” singular vectors refers to \( u_2 \ldots u_{p+1} \) and \( v_2 \ldots v_{p+1} \) except in the case of log normalization.

Given these singular vectors, they are ranked according to which can be best approximated by a piecewise-constant vector. The approximations for each vector are found using one-dimensional k-means and scored using the Euclidean distance. Some subset of the best left and right singular vector are selected. Next, the data is projected to this best subset of singular vectors and clustered.

For instance, if \( p \) singular vectors were calculated, the \( q \) best are found as described, where \( q < p \). Let \( U \) be the matrix with columns the \( q \) best left singular vectors, and similarly \( V \) for the right. To partition the rows, the rows of \( A \) are projected to a \( q \) dimensional space: \( A \ast V \). Treating the \( m \) rows of this \( m \times q \) matrix as samples and clustering using k-means yields the row labels. Similarly, projecting the columns to \( A^T \ast U \) and clustering this \( n \times q \) matrix yields the column labels.

### Examples:
- **A demo of the Spectral Biclustering algorithm**: a simple example showing how to generate a checkerboard matrix and bicluster it.

### References:

### Biclustering evaluation

There are two ways of evaluating a biclustering result: internal and external. Internal measures, such as cluster stability, rely only on the data and the result themselves. Currently there are no internal bicluster measures in scikit-learn. External measures refer to an external source of information, such as the true solution. When working with real data the true solution is usually unknown, but biclustering artificial data may be useful for evaluating algorithms precisely because the true solution is known.

To compare a set of found biclusters to the set of true biclusters, two similarity measures are needed: a similarity measure for individual biclusters, and a way to combine these individual similarities into an overall score.

To compare individual biclusters, several measures have been used. For now, only the Jaccard index is implemented:

\[
J(A, B) = \frac{|A \cap B|}{|A| + |B| - |A \cap B|}
\]

where \( A \) and \( B \) are biclusters, \( |A \cap B| \) is the number of elements in their intersection. The Jaccard index achieves its minimum of 0 when the biclusters to not overlap at all and its maximum of 1 when they are identical.

Several methods have been developed to compare two sets of biclusters. For now, only `consensus_score` (Hochreiter et al., 2010) is available:

1. Compute bicluster similarities for pairs of biclusters, one in each set, using the Jaccard index or a similar measure.
2. Assign biclusters from one set to another in a one-to-one fashion to maximize the sum of their similarities. This step is performed using the Hungarian algorithm.
3. The final sum of similarities is divided by the size of the larger set.

The minimum consensus score, 0, occurs when all pairs of biclusters are totally dissimilar. The maximum score, 1, occurs when both sets are identical.

References:

- Hochreiter, Bodenhofer, et. al., 2010. FABIA: factor analysis for bicluster acquisition.

### 3.2.5 Decomposing signals in components (matrix factorization problems)

#### Principal component analysis (PCA)

##### Exact PCA and probabilistic interpretation

PCA is used to decompose a multivariate dataset in a set of successive orthogonal components that explain a maximum amount of the variance. In scikit-learn, PCA is implemented as a *transformer* object that learns \( n \) components in its *fit* method, and can be used on new data to project it on these components.

The optional parameter `whiten=True` makes it possible to project the data onto the singular space while scaling each component to unit variance. This is often useful if the models down-stream make strong assumptions on the isotropy of the signal: this is for example the case for Support Vector Machines with the RBF kernel and the K-Means clustering algorithm.

Below is an example of the iris dataset, which is comprised of 4 features, projected on the 2 dimensions that explain most variance:

![PCA of IRIS dataset](image)

The PCA object also provides a probabilistic interpretation of the PCA that can give a likelihood of data based on the amount of variance it explains. As such it implements a *score* method that can be used in cross-validation:
Incremental PCA

The `PCA` object is very useful, but has certain limitations for large datasets. The biggest limitation is that `PCA` only supports batch processing, which means all of the data to be processed must fit in main memory. The `IncrementalPCA` object uses a different form of processing and allows for partial computations which almost exactly match the results of `PCA` while processing the data in a minibatch fashion. `IncrementalPCA` makes it possible to implement out-of-core Principal Component Analysis either by:

- Using its `partial_fit` method on chunks of data fetched sequentially from the local hard drive or a network database.
- Calling its `fit` method on a memory mapped file using `numpy.memmap`.

`IncrementalPCA` only stores estimates of component and noise variances, in order update `explained_variance_ratio_` incrementally. This is why memory usage depends on the number of samples per batch, rather than the number of samples to be processed in the dataset.

Examples:

- `Incremental PCA`
Incremental PCA of iris dataset
Mean absolute unsigned error 0.002308
PCA using randomized SVD

It is often interesting to project data to a lower-dimensional space that preserves most of the variance, by dropping the singular vector of components associated with lower singular values.

For instance, if we work with 64x64 pixel gray-level pictures for face recognition, the dimensionality of the data is 4096 and it is slow to train an RBF support vector machine on such wide data. Furthermore we know that the intrinsic dimensionality of the data is much lower than 4096 since all pictures of human faces look somewhat alike. The samples lie on a manifold of much lower dimension (say around 200 for instance). The PCA algorithm can be used to linearly transform the data while both reducing the dimensionality and preserve most of the explained variance at the same time.

The class `PCA` used with the optional parameter `svd_solver='randomized'` is very useful in that case: since we are going to drop most of the singular vectors it is much more efficient to limit the computation to an approximated estimate of the singular vectors we will keep to actually perform the transform.

For instance, the following shows 16 sample portraits (centered around 0.0) from the Olivetti dataset. On the right hand side are the first 16 singular vectors reshaped as portraits. Since we only require the top 16 singular vectors of a dataset with size $n_{\text{samples}} = 400$ and $n_{\text{features}} = 64 \times 64 = 4096$, the computation time is less than 1s:

![First centered Olivetti faces](image)

Note: with the optional parameter `svd_solver='randomized'`, we also need to give `PCA` the size of the lower-dimensional space `n_components` as a mandatory input parameter.
If we note $n_{\text{max}} = \max(n_{\text{samples}}, n_{\text{features}})$ and $n_{\text{min}} = \min(n_{\text{samples}}, n_{\text{features}})$, the time complexity of the randomized PCA is $O(n_{\text{max}}^2 \cdot n_{\text{components}})$ instead of $O(n_{\text{max}} \cdot n_{\text{min}})$ for the exact method implemented in PCA.

The memory footprint of randomized PCA is also proportional to $2 \cdot n_{\text{max}} \cdot n_{\text{components}}$ instead of $n_{\text{max}} \cdot n_{\text{min}}$ for the exact method.

Note: the implementation of `inverse_transform` in PCA with `svd_solver='randomized'` is not the exact inverse transform of `transform` even when `whiten=False` (default).

Examples:

- Faces recognition example using eigenfaces and SVMs
- Faces dataset decompositions

References:

- “Finding structure with randomness: Stochastic algorithms for constructing approximate matrix decompositions” Halko, et al., 2009

Kernel PCA

KernelPCA is an extension of PCA which achieves non-linear dimensionality reduction through the use of kernels (see Pairwise metrics, Affinities and Kernels). It has many applications including denoising, compression and structured prediction (kernel dependency estimation). KernelPCA supports both transform and inverse_transform.
Examples:

- **Kernel PCA**

**Sparse principal components analysis (SparsePCA and MiniBatchSparsePCA)**

*SparsePCA* is a variant of PCA, with the goal of extracting the set of sparse components that best reconstruct the data.

Mini-batch sparse PCA (*MiniBatchSparsePCA*) is a variant of *SparsePCA* that is faster but less accurate. The increased speed is reached by iterating over small chunks of the set of features, for a given number of iterations.

Principal component analysis (PCA) has the disadvantage that the components extracted by this method have exclusively dense expressions, i.e. they have non-zero coefficients when expressed as linear combinations of the original variables. This can make interpretation difficult. In many cases, the real underlying components can be more naturally imagined as sparse vectors; for example in face recognition, components might naturally map to parts of faces.

Sparse principal components yields a more parsimonious, interpretable representation, clearly emphasizing which of the original features contribute to the differences between samples.

The following example illustrates 16 components extracted using sparse PCA from the Olivetti faces dataset. It can be seen how the regularization term induces many zeros. Furthermore, the natural structure of the data causes the non-zero coefficients to be vertically adjacent. The model does not enforce this mathematically: each component is a vector $h \in \mathbb{R}^{4096}$, and there is no notion of vertical adjacency except during the human-friendly visualization as 64x64 pixel images. The fact that the components shown below appear local is the effect of the inherent structure of the data, which makes such local patterns minimize reconstruction error. There exist sparsity-inducing norms that take into account adjacency and different kinds of structure; see [Jen09] for a review of such methods. For more details on how to use Sparse PCA, see the Examples section, below.

![genfaces - PCA using randomized SVD - Train time 0.1](image)
Note that there are many different formulations for the Sparse PCA problem. The one implemented here is based on [Mrl09]. The optimization problem solved is a PCA problem (dictionary learning) with an $\ell_1$ penalty on the components:

$$
(U^*, V^*) = \arg \min_{U,V} \frac{1}{2} \|X - UV\|_2^2 + \alpha \|V\|_1
$$

subject to $\|U_k\|_2 = 1$ for all $0 \leq k < n_{\text{components}}$

The sparsity-inducing $\ell_1$ norm also prevents learning components from noise when few training samples are available. The degree of penalization (and thus sparsity) can be adjusted through the hyperparameter $\alpha$. Small values lead to a gently regularized factorization, while larger values shrink many coefficients to zero.

**Note:** While in the spirit of an online algorithm, the class `MiniBatchSparsePCA` does not implement `partial_fit` because the algorithm is online along the features direction, not the samples direction.

**Examples:**

- *Faces dataset decompositions*

**References:**

**Truncated singular value decomposition and latent semantic analysis**

`TruncatedSVD` implements a variant of singular value decomposition (SVD) that only computes the $k$ largest singular values, where $k$ is a user-specified parameter.

When truncated SVD is applied to term-document matrices (as returned by `CountVectorizer` or `TfidfVectorizer`), this transformation is known as latent semantic analysis (LSA), because it transforms such matrices to a “semantic” space of low dimensionality. In particular, LSA is known to combat the effects of synonymy and polysemy (both of which roughly mean there are multiple meanings per word), which cause term-document matrices to be overly sparse and exhibit poor similarity under measures such as cosine similarity.
Mathematically, truncated SVD applied to training samples $X$ produces a low-rank approximation $X$:

$$X \approx X_k = U_k \Sigma_k V_k^T$$

After this operation, $U_k \Sigma_k^T$ is the transformed training set with $k$ features (called $\text{n\_components}$ in the API).

To also transform a test set $X$, we multiply it with $V_k$:

$$X' = XV_k$$

**Note:** Most treatments of LSA in the natural language processing (NLP) and information retrieval (IR) literature swap the axes of the matrix $X$ so that it has shape $\text{n\_features} \times \text{n\_samples}$. We present LSA in a different way that matches the scikit-learn API better, but the singular values found are the same.

TruncatedSVD is very similar to PCA, but differs in that it works on sample matrices $X$ directly instead of their covariance matrices. When the columnwise (per-feature) means of $X$ are subtracted from the feature values, truncated SVD on the resulting matrix is equivalent to PCA. In practical terms, this means that the TruncatedSVD transformer accepts scipy.sparse matrices without the need to densify them, as densifying may fill up memory even for medium-sized document collections.

While the TruncatedSVD transformer works with any (sparse) feature matrix, using it on tf–idf matrices is recommended over raw frequency counts in an LSA/document processing setting. In particular, sublinear scaling and inverse document frequency should be turned on (sublinear_tf=True, use_idf=True) to bring the feature values closer to a Gaussian distribution, compensating for LSA’s erroneous assumptions about textual data.

**Examples:**

- Clustering text documents using k-means

**References:**

- Christopher D. Manning, Prabhakar Raghavan and Hinrich Schütze (2008), *Introduction to Information Retrieval*, Cambridge University Press, chapter 18: Matrix decompositions & latent semantic indexing

**Dictionary Learning**

**Sparse coding with a precomputed dictionary**

The *SparseCoder* object is an estimator that can be used to transform signals into sparse linear combination of atoms from a fixed, precomputed dictionary such as a discrete wavelet basis. This object therefore does not implement a `fit` method. The transformation amounts to a sparse coding problem: finding a representation of the data as a linear combination of as few dictionary atoms as possible. All variations of dictionary learning implement the following transform methods, controllable via the `transform_method` initialization parameter:

- Orthogonal matching pursuit (*Orthogonal Matching Pursuit (OMP)*)
• Least-angle regression (Least Angle Regression)
• Lasso computed by least-angle regression
• Lasso using coordinate descent (Lasso)
• Thresholding

Thresholding is very fast but it does not yield accurate reconstructions. They have been shown useful in literature for classification tasks. For image reconstruction tasks, orthogonal matching pursuit yields the most accurate, unbiased reconstruction.

The dictionary learning objects offer, via the split_code parameter, the possibility to separate the positive and negative values in the results of sparse coding. This is useful when dictionary learning is used for extracting features that will be used for supervised learning, because it allows the learning algorithm to assign different weights to negative loadings of a particular atom, from to the corresponding positive loading.

The split code for a single sample has length $2 \times n_{\text{components}}$ and is constructed using the following rule: First, the regular code of length $n_{\text{components}}$ is computed. Then, the first $n_{\text{components}}$ entries of the split_code are filled with the positive part of the regular code vector. The second half of the split code is filled with the negative part of the code vector, only with a positive sign. Therefore, the split_code is non-negative.

Examples:

• Sparse coding with a precomputed dictionary

**Generic dictionary learning**

Dictionary learning (DictionaryLearning) is a matrix factorization problem that amounts to finding a (usually overcomplete) dictionary that will perform good at sparsely encoding the fitted data.

Representing data as sparse combinations of atoms from an overcomplete dictionary is suggested to be the way the mammal primary visual cortex works. Consequently, dictionary learning applied on image patches has been shown to give good results in image processing tasks such as image completion, inpainting and denoising, as well as for supervised recognition tasks.

Dictionary learning is an optimization problem solved by alternatively updating the sparse code, as a solution to multiple Lasso problems, considering the dictionary fixed, and then updating the dictionary to best fit the sparse code.

\[
(U^*, V^*) = \arg \min_{U,V} \frac{1}{2} ||X - UV||^2_2 + \alpha ||U||_1 \\
\text{subject to } ||V_k||_2 = 1 \text{ for all } 0 \leq k < n_{\text{atoms}}
\]
After using such a procedure to fit the dictionary, the transform is simply a sparse coding step that shares the same implementation with all dictionary learning objects (see *Sparse coding with a precomputed dictionary*).

The following image shows how a dictionary learned from 4x4 pixel image patches extracted from part of the image of a raccoon face looks like.
Examples:

- Image denoising using dictionary learning

References:


Mini-batch dictionary learning

*MiniBatchDictionaryLearning* implements a faster, but less accurate version of the dictionary learning algorithm that is better suited for large datasets.

By default, *MiniBatchDictionaryLearning* divides the data into mini-batches and optimizes in an online manner by cycling over the mini-batches for the specified number of iterations. However, at the moment it does not implement a stopping condition.

The estimator also implements *partial_fit*, which updates the dictionary by iterating only once over a mini-batch. This can be used for online learning when the data is not readily available from the start, or for when the data does not fit into the memory.

![Patches of faces](image)

Train time 3.6s on 3200 patches

Clustering for dictionary learning

Note that when using dictionary learning to extract a representation (e.g. for sparse coding) clustering can be a good proxy to learn the dictionary. For instance the *MiniBatchKMeans* estimator is computationally efficient and implements on-line learning with a *partial_fit* method.

Example: *Online learning of a dictionary of parts of faces*

Factor Analysis

In unsupervised learning we only have a dataset $X = \{x_1, x_2, \ldots, x_n\}$. How can this dataset be described mathematically? A very simple *continuous latent variable* model for $X$ is

$$x_i = Wh_i + \mu + \epsilon$$

The vector $h_i$ is called “latent” because it is unobserved. $\epsilon$ is considered a noise term distributed according to a Gaussian with mean 0 and covariance $\Psi$ (i.e. $\epsilon \sim \mathcal{N}(0, \Psi)$), $\mu$ is some arbitrary offset vector. Such a model is called
“generative” as it describes how $x_i$ is generated from $h_i$. If we use all the $x_i$’s as columns to form a matrix $X$ and all the $h_i$’s as columns of a matrix $H$ then we can write (with suitably defined $M$ and $E$):

$$X = WH + M + E$$

In other words, we decomposed matrix $X$.

If $h_i$ is given, the above equation automatically implies the following probabilistic interpretation:

$$p(x_i|h_i) = \mathcal{N}(Wh_i + \mu, \Psi)$$

For a complete probabilistic model we also need a prior distribution for the latent variable $h$. The most straightforward assumption (based on the nice properties of the Gaussian distribution) is $h \sim \mathcal{N}(0, I)$. This yields a Gaussian as the marginal distribution of $x$:

$$p(x) = \mathcal{N}(\mu, WW^T + \Psi)$$

Now, without any further assumptions the idea of having a latent variable $h$ would be superfluous – $x$ can be completely modelled with a mean and a covariance. We need to impose some more specific structure on one of these two parameters. A simple additional assumption regards the structure of the error covariance $\Psi$:

- $\Psi = \sigma^2 I$: This assumption leads to the probabilistic model of PCA.
- $\Psi = \text{diag}(\psi_1, \psi_2, \ldots, \psi_n)$: This model is called FactorAnalysis, a classical statistical model. The matrix $W$ is sometimes called the “factor loading matrix”.

Both models essentially estimate a Gaussian with a low-rank covariance matrix. Because both models are probabilistic they can be integrated in more complex models, e.g. Mixture of Factor Analysers. One gets very different models (e.g. FastICA) if non-Gaussian priors on the latent variables are assumed.

Factor analysis can produce similar components (the columns of its loading matrix) to PCA. However, one can not make any general statements about these components (e.g. whether they are orthogonal):

```
genfaces - PCA using randomized SVD - Train time 0.1:
```

![Faces decomposed using PCA](image)
The main advantage for Factor Analysis (over PCA) is that it can model the variance in every direction of the input space independently (heteroscedastic noise):

![Factor Analysis components - FA - Train time 0.1s](image)

This allows better model selection than probabilistic PCA in the presence of heteroscedastic noise:

![Pixelwise variance](image)

---

**Examples:**

- *Model selection with Probabilistic PCA and Factor Analysis (FA)*

---

**Independent component analysis (ICA)**

Independent component analysis separates a multivariate signal into additive subcomponents that are maximally independent. It is implemented in scikit-learn using the FastICA algorithm. Typically, ICA is not used for reducing dimensionality but for separating superimposed signals. Since the ICA model does not include a noise term, for the model to be correct, whitening must be applied. This can be done internally using the whiten argument or manually using one of the PCA variants.

It is classically used to separate mixed signals (a problem known as *blind source separation*), as in the example below:

ICA can also be used as yet another non linear decomposition that finds components with some sparsity:
Examples:

- **Blind source separation using FastICA**
- **FastICA on 2D point clouds**
- **Faces dataset decompositions**

Non-negative matrix factorization (NMF or NNMF)

**NMF with the Frobenius norm**

NMF\(^1\) is an alternative approach to decomposition that assumes that the data and the components are non-negative. NMF can be plugged in instead of PCA or its variants, in the cases where the data matrix does not contain negative values. It finds a decomposition of samples \(X\) into two matrices \(W\) and \(H\) of non-negative elements, by optimizing the distance \(d\) between \(X\) and the matrix product \(WH\). The most widely used distance function is the squared Frobenius distance.

\(^1\) “Learning the parts of objects by non-negative matrix factorization” D. Lee, S. Seung. 1999
norm, which is an obvious extension of the Euclidean norm to matrices:

\[ d_{\text{Fro}}(X, Y) = \frac{1}{2} ||X - Y||_{\text{Fro}} = \frac{1}{2} \sum_{i,j} (X_{ij} - Y_{ij})^2 \]

Unlike PCA, the representation of a vector is obtained in an additive fashion, by superimposing the components, without subtracting. Such additive models are efficient for representing images and text.

It has been observed in [Hoyer, 2004] that, when carefully constrained, NMF can produce a parts-based representation of the dataset, resulting in interpretable models. The following example displays 16 sparse components found by NMF from the images in the Olivetti faces dataset, in comparison with the PCA eigenfaces.

The \textit{init} attribute determines the initialization method applied, which has a great impact on the performance of the method. NMF implements the method Nonnegative Double Singular Value Decomposition. NNDSVD is based on two SVD processes, one approximating the data matrix, the other approximating positive sections of the resulting partial SVD factors utilizing an algebraic property of unit rank matrices. The basic NNDSVD algorithm is better fit for sparse factorization. Its variants NNDSVDa (in which all zeros are set equal to the mean of all elements of the data), and NNDSVDar (in which the zeros are set to random perturbations less than the mean of the data divided by 100) are recommended in the dense case.

---

2 “Non-negative Matrix Factorization with Sparseness Constraints” P. Hoyer, 2004
4 “SVD based initialization: A head start for nonnegative matrix factorization” C. Boutsidis, E. Gallopoulos, 2008
Note that the Multiplicative Update (‘mu’) solver cannot update zeros present in the initialization, so it leads to poorer results when used jointly with the basic NNDSVD algorithm which introduces a lot of zeros; in this case, NNDSVDa or NNDSVDar should be preferred.

**NMF** can also be initialized with correctly scaled random non-negative matrices by setting `init="random"`. An integer seed or a `RandomState` can also be passed to `random_state` to control reproducibility.

In **NMF**, L1 and L2 priors can be added to the loss function in order to regularize the model. The L2 prior uses the Frobenius norm, while the L1 prior uses an elementwise L1 norm. As in ElasticNet, we control the combination of L1 and L2 with the `l1_ratio` \((\beta)\) parameter, and the intensity of the regularization with the `alpha` \((\alpha)\) parameter. Then the priors terms are:

\[
\alpha \beta ||W||_1 + \alpha \rho ||H||_1 + \frac{\alpha (1 - \rho)}{2} ||W||_\text{Fro}^2 + \frac{\alpha (1 - \rho)}{2} ||H||_\text{Fro}^2
\]

and the regularized objective function is:

\[
d_{\text{Fro}}(X, WH) + \alpha \rho ||W||_1 + \alpha \rho ||H||_1 + \frac{\alpha (1 - \rho)}{2} ||W||_\text{Fro}^2 + \frac{\alpha (1 - \rho)}{2} ||H||_\text{Fro}^2
\]

**NMF** regularizes both W and H. The public function `non_negative_factorization` allows a finer control through the `regularization` attribute, and may regularize only W, only H, or both.

**NMF with a beta-divergence**

As described previously, the most widely used distance function is the squared Frobenius norm, which is an obvious extension of the Euclidean norm to matrices:

\[
d_{\text{Fro}}(X, Y) = \frac{1}{2} \|X - Y\|_\text{Fro}^2 = \frac{1}{2} \sum_{i,j} (X_{ij} - Y_{ij})^2
\]

Other distance functions can be used in NMF as, for example, the (generalized) Kullback-Leibler (KL) divergence, also referred as I-divergence:

\[
d_{\text{KL}}(X, Y) = \sum_{i,j} (X_{ij} \log(\frac{X_{ij}}{Y_{ij}}) - X_{ij} + Y_{ij})
\]

Or, the Itakura-Saito (IS) divergence:

\[
d_{\text{IS}}(X, Y) = \sum_{i,j} \frac{X_{ij}}{Y_{ij}} - \log(\frac{X_{ij}}{Y_{ij}}) - 1
\]

These three distances are special cases of the beta-divergence family, with \(\beta = 2, 1, 0\) respectively\(^6\). The beta-divergence are defined by:

\[
d_{\beta}(X, Y) = \sum_{i,j} \frac{1}{\beta(\beta - 1)} (X_{ij}^\beta + (\beta - 1) Y_{ij}^{\beta} - \beta X_{ij} Y_{ij}^{\beta - 1})
\]

Note that this definition is not valid if \(\beta \in (0; 1)\), yet it can be continuously extended to the definitions of \(d_{KL}\) and \(d_{IS}\) respectively.

\(^6\) “Algorithms for nonnegative matrix factorization with the beta-divergence” C. Fevotte, J. Idier, 2011

\(^5\) “Fast local algorithms for large scale nonnegative matrix and tensor factorizations.” A. Cichocki, P. Anh-Huy, 2009
significantly faster than for other values of $\beta$. Note also that with a negative (or 0, i.e. ‘itakura-saito’) $\beta$, the input matrix cannot contain zero values.

The ‘cd’ solver can only optimize the Frobenius norm. Due to the underlying non-convexity of NMF, the different solvers may converge to different minima, even when optimizing the same distance function.

NMF is best used with the `fit_transform` method, which returns the matrix $W$. The matrix $H$ is stored into the fitted model in the `components_` attribute; the method `transform` will decompose a new matrix $X_{\text{new}}$ based on these stored components:

```python
>>> import numpy as np
>>> X = np.array([[1, 1], [2, 1], [3, 1.2], [4, 1], [5, 0.8], [6, 1]])
>>> from sklearn.decomposition import NMF
>>> model = NMF(n_components=2, init='random', random_state=0)
>>> W = model.fit_transform(X)
>>> H = model.components_
>>> X_new = np.array([[1, 0], [1, 6.1], [1, 0], [1, 4], [3.2, 1], [0, 4]])
>>> W_new = model.transform(X_new)
```

Examples:

- Faces dataset decompositions
- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Beta-divergence loss functions

References:
Latent Dirichlet Allocation (LDA)

Latent Dirichlet Allocation is a generative probabilistic model for collections of discrete dataset such as text corpora. It is also a topic model that is used for discovering abstract topics from a collection of documents.

The graphical model of LDA is a three-level Bayesian model:

When modeling text corpora, the model assumes the following generative process for a corpus with $D$ documents and $K$ topics:

1. For each topic $k$, draw $\beta_k \sim \text{Dirichlet}(\eta)$, $k = 1...K$
2. For each document $d$, draw $\theta_d \sim \text{Dirichlet}(\alpha)$, $d = 1...D$
3. For each word $i$ in document $d$:
   1. Draw a topic index $z_{di} \sim \text{Multinomial}(\theta_d)$
   2. Draw the observed word $w_{ij} \sim \text{Multinomial}(\beta_{z_{di}})$

For parameter estimation, the posterior distribution is:

$$p(z, \theta, \beta|w, \alpha, \eta) = \frac{p(z, \theta, \beta|\alpha, \eta)}{p(w|\alpha, \eta)}$$

Since the posterior is intractable, variational Bayesian method uses a simpler distribution $q(z, \theta, \beta|\lambda, \phi, \gamma)$ to approximate it, and those variational parameters $\lambda, \phi, \gamma$ are optimized to maximize the Evidence Lower Bound (ELBO):

$$\log P(w|\alpha, \eta) \geq L(w, \phi, \gamma, \lambda) \overset{\Delta}{=} E_q[\log p(w, z, \theta, \beta|\alpha, \eta)] - E_q[\log q(z, \theta, \beta)]$$

Maximizing ELBO is equivalent to minimizing the Kullback-Leibler(KL) divergence between $q(z, \theta, \beta)$ and the true posterior $p(z, \theta, \beta|w, \alpha, \eta)$.

`LatentDirichletAllocation` implements online variational Bayes algorithm and supports both online and batch update method. While batch method updates variational variables after each full pass through the data, online method updates variational variables from mini-batch data points.

**Note:** Although online method is guaranteed to converge to a local optimum point, the quality of the optimum point and the speed of convergence may depend on mini-batch size and attributes related to learning rate setting.
When \texttt{LatentDirichletAllocation} is applied on a “document-term” matrix, the matrix will be decomposed into a “topic-term” matrix and a “document-topic” matrix. While “topic-term” matrix is stored as \texttt{components_} in the model, “document-topic” matrix can be calculated from \texttt{transform} method. \texttt{LatentDirichletAllocation} also implements \texttt{partial_fit} method. This is used when data can be fetched sequentially.

\textbf{Examples:}
- \textit{Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation}

\textbf{References:}

\subsection{3.2.6 Covariance estimation}

Many statistical problems require at some point the estimation of a population’s covariance matrix, which can be seen as an estimation of data set scatter plot shape. Most of the time, such an estimation has to be done on a sample whose properties (size, structure, homogeneity) has a large influence on the estimation’s quality. The \texttt{sklearn.covariance} package aims at providing tools affording an accurate estimation of a population’s covariance matrix under various settings.

We assume that the observations are independent and identically distributed (i.i.d.).

\textbf{Empirical covariance}

The covariance matrix of a data set is known to be well approximated with the classical maximum likelihood estimator (or “empirical covariance”), provided the number of observations is large enough compared to the number of features (the variables describing the observations). More precisely, the Maximum Likelihood Estimator of a sample is an unbiased estimator of the corresponding population covariance matrix.

The empirical covariance matrix of a sample can be computed using the \texttt{empirical_covariance} function of the package, or by fitting an \texttt{EmpiricalCovariance} object to the data sample with the \texttt{EmpiricalCovariance.fit} method. Be careful that depending whether the data are centered or not, the result will be different, so one may want to use the \texttt{assume_centered} parameter accurately. More precisely if one uses \texttt{assume_centered=False}, then the test set is supposed to have the same mean vector as the training set. If not so, both should be centered by the user, and \texttt{assume_centered=True} should be used.

\textbf{Examples:}
- See \textit{Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood} for an example on how to fit an \texttt{EmpiricalCovariance} object to data.

3.2. Unsupervised learning
Shrunk Covariance

Basic shrinkage

Despite being an unbiased estimator of the covariance matrix, the Maximum Likelihood Estimator is not a good estimator of the eigenvalues of the covariance matrix, so the precision matrix obtained from its inversion is not accurate. Sometimes, it even occurs that the empirical covariance matrix cannot be inverted for numerical reasons. To avoid such an inversion problem, a transformation of the empirical covariance matrix has been introduced: the shrinkage.

In the scikit-learn, this transformation (with a user-defined shrinkage coefficient) can be directly applied to a pre-computed covariance with the `shrunk_covariance` method. Also, a shrunk estimator of the covariance can be fitted to data with a `ShrunkCovariance` object and its `ShrunkCovariance.fit` method. Again, depending whether the data are centered or not, the result will be different, so one may want to use the `assume_centered` parameter accurately.

Mathematically, this shrinkage consists in reducing the ratio between the smallest and the largest eigenvalue of the empirical covariance matrix. It can be done by simply shifting every eigenvalue according to a given offset, which is equivalent of finding the l2-penalized Maximum Likelihood Estimator of the covariance matrix. In practice, shrinkage boils down to a simple a convex transformation: \( \Sigma_{\text{shrunk}} = (1 - \alpha)\Sigma + \alpha \frac{Tr^\Sigma}{p} \text{Id}. \)

Choosing the amount of shrinkage, \( \alpha \) amounts to setting a bias/variance trade-off, and is discussed below.

Examples:

- See Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood for an example on how to fit a `ShrunkCovariance` object to data.

Ledoit-Wolf shrinkage

In their 2004 paper\(^1\), O. Ledoit and M. Wolf propose a formula so as to compute the optimal shrinkage coefficient \( \alpha \) that minimizes the Mean Squared Error between the estimated and the real covariance matrix.

The Ledoit-Wolf estimator of the covariance matrix can be computed on a sample with the `ledoit_wolf` function of the `sklearn.covariance` package, or it can be otherwise obtained by fitting a `LedoitWolf` object to the same sample.

Note: Case when population covariance matrix is isotropic

It is important to note that when the number of samples is much larger than the number of features, one would expect that no shrinkage would be necessary. The intuition behind this is that if the population covariance is full rank, when the number of sample grows, the sample covariance will also become positive definite. As a result, no shrinkage would necessary and the method should automatically do this.

This, however, is not the case in the Ledoit-Wolf procedure when the population covariance happens to be a multiple of the identity matrix. In this case, the Ledoit-Wolf shrinkage estimate approaches 1 as the number of samples increases. This indicates that the optimal estimate of the covariance matrix in the Ledoit-Wolf sense is multiple of the identity. Since the population covariance is already a multiple of the identity matrix, the Ledoit-Wolf solution is indeed a reasonable estimate.

---

Examples:

- See *Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood* for an example on how to fit a *LedoitWolf* object to data and for visualizing the performances of the Ledoit-Wolf estimator in terms of likelihood.

References:

**Oracle Approximating Shrinkage**

Under the assumption that the data are Gaussian distributed, Chen et al.\(^2\) derived a formula aimed at choosing a shrinkage coefficient that yields a smaller Mean Squared Error than the one given by Ledoit and Wolf’s formula. The resulting estimator is known as the Oracle Shrinkage Approximating estimator of the covariance.

The OAS estimator of the covariance matrix can be computed on a sample with the *oas* function of the *sklearn.covariance* package, or it can be otherwise obtained by fitting an *OAS* object to the same sample.

![Regularized covariance: likelihood and shrinkage coefficient](image)

Fig. 3.7: Bias-variance trade-off when setting the shrinkage: comparing the choices of Ledoit-Wolf and OAS estimators

References:

Examples:

- See *Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood* for an example on how to fit an *OAS* object to data.

Sparse inverse covariance

The matrix inverse of the covariance matrix, often called the precision matrix, is proportional to the partial correlation matrix. It gives the partial independence relationship. In other words, if two features are independent conditionally on the others, the corresponding coefficient in the precision matrix will be zero. This is why it makes sense to estimate a sparse precision matrix: by learning independence relations from the data, the estimation of the covariance matrix is better conditioned. This is known as covariance selection.

In the small-samples situation, in which \( n_{samples} \) is on the order of \( n_{features} \) or smaller, sparse inverse covariance estimators tend to work better than shrunk covariance estimators. However, in the opposite situation, or for very correlated data, they can be numerically unstable. In addition, unlike shrinkage estimators, sparse estimators are able to recover off-diagonal structure.

The GraphLasso estimator uses an l1 penalty to enforce sparsity on the precision matrix: the higher its alpha parameter, the more sparse the precision matrix. The corresponding GraphLassoCV object uses cross-validation to automatically set the alpha parameter.

Note: Structure recovery

Recovering a graphical structure from correlations in the data is a challenging thing. If you are interested in such recovery keep in mind that:

- Recovery is easier from a correlation matrix than a covariance matrix: standardize your observations before running GraphLasso
- If the underlying graph has nodes with much more connections than the average node, the algorithm will miss some of these connections.
Fig. 3.8: A comparison of maximum likelihood, shrinkage and sparse estimates of the covariance and precision matrix in the very small samples settings.

- If your number of observations is not large compared to the number of edges in your underlying graph, you will not recover it.
- Even if you are in favorable recovery conditions, the alpha parameter chosen by cross-validation (e.g. using the GraphLassoCV object) will lead to selecting too many edges. However, the relevant edges will have heavier weights than the irrelevant ones.

The mathematical formulation is the following:

$$\hat{K} = \arg\min_K (\text{tr}SK - \log\det K + \alpha \|K\|_1)$$

Where $K$ is the precision matrix to be estimated, and $S$ is the sample covariance matrix. $\|K\|_1$ is the sum of the absolute values of off-diagonal coefficients of $K$. The algorithm employed to solve this problem is the GLasso algorithm, from the Friedman 2008 Biostatistics paper. It is the same algorithm as in the R glasso package.

**Examples:**
- **Sparse inverse covariance estimation**: example on synthetic data showing some recovery of a structure, and comparing to other covariance estimators.
- **Visualizing the stock market structure**: example on real stock market data, finding which symbols are most linked.

**References:**
Robust Covariance Estimation

Real data sets are often subjects to measurement or recording errors. Regular but uncommon observations may also appear for a variety of reasons. Every observation which is very uncommon is called an outlier. The empirical covariance estimator and the shrunk covariance estimators presented above are very sensitive to the presence of outlying observations in the data. Therefore, one should use robust covariance estimators to estimate the covariance of its real data sets. Alternatively, robust covariance estimators can be used to perform outlier detection and discard/downweight some observations according to further processing of the data.

The `sklearn.covariance` package implements a robust estimator of covariance, the Minimum Covariance Determinant\(^3\).

Minimum Covariance Determinant

The Minimum Covariance Determinant estimator is a robust estimator of a data set’s covariance introduced by P.J. Rousseeuw in\(^3\). The idea is to find a given proportion (h) of “good” observations which are not outliers and compute their empirical covariance matrix. This empirical covariance matrix is then rescaled to compensate the performed selection of observations (“consistency step”). Having computed the Minimum Covariance Determinant estimator, one can give weights to observations according to their Mahalanobis distance, leading to a reweighted estimate of the covariance matrix of the data set (“reweighting step”).

Rousseeuw and Van Driessen\(^4\) developed the FastMCD algorithm in order to compute the Minimum Covariance Determinant. This algorithm is used in scikit-learn when fitting an MCD object to data. The FastMCD algorithm also computes a robust estimate of the data set location at the same time.

Raw estimates can be accessed as `raw_location_` and `raw_covariance_` attributes of a `MinCovDet` robust covariance estimator object.

References:

- See [Robust vs Empirical covariance estimate](#) for an example on how to fit a `MinCovDet` object to data and see how the estimate remains accurate despite the presence of outliers.
- See [Robust covariance estimation and Mahalanobis distances relevance](#) to visualize the difference between `EmpiricalCovariance` and `MinCovDet` covariance estimators in terms of Mahalanobis distance (so we get a better estimate of the precision matrix too).

---

3.2.7 Novelty and Outlier Detection

Many applications require being able to decide whether a new observation belongs to the same distribution as existing observations (it is an inlier), or should be considered as different (it is an outlier). Often, this ability is used to clean real data sets. Two important distinction must be made:

**novelty detection** The training data is not polluted by outliers, and we are interested in detecting anomalies in new observations.

**outlier detection** The training data contains outliers, and we need to fit the central mode of the training data, ignoring the deviant observations.

The scikit-learn project provides a set of machine learning tools that can be used both for novelty or outliers detection. This strategy is implemented with objects learning in an unsupervised way from the data:

```python
estimator.fit(X_train)
```

new observations can then be sorted as inliers or outliers with a `predict` method:

```python
estimator.predict(X_test)
```

Inliers are labeled 1, while outliers are labeled -1.

**Novelty Detection**

Consider a data set of \( n \) observations from the same distribution described by \( p \) features. Consider now that we add one more observation to that data set. Is the new observation so different from the others that we can doubt it is regular? (i.e. does it come from the same distribution?) Or on the contrary, is it so similar to the other that we cannot distinguish it from the original observations? This is the question addressed by the novelty detection tools and methods.

In general, it is about to learn a rough, close frontier delimiting the contour of the initial observations distribution, plotted in embedding \( p \)-dimensional space. Then, if further observations lay within the frontier-delimited subspace, they are considered as coming from the same population than the initial observations. Otherwise, if they lay outside the frontier, we can say that they are abnormal with a given confidence in our assessment.

The One-Class SVM has been introduced by Schölkopf et al. for that purpose and implemented in the `Support Vector Machines` module in the `svm.OneClassSVM` object. It requires the choice of a kernel and a scalar parameter to
define a frontier. The RBF kernel is usually chosen although there exists no exact formula or algorithm to set its bandwidth parameter. This is the default in the scikit-learn implementation. The $\nu$ parameter, also known as the margin of the One-Class SVM, corresponds to the probability of finding a new, but regular, observation outside the frontier.

References:


Examples:

- See One-class SVM with non-linear kernel (RBF) for visualizing the frontier learned around some data by a `svm.OneClassSVM` object.

Outlier Detection

Outlier detection is similar to novelty detection in the sense that the goal is to separate a core of regular observations from some polluting ones, called “outliers”. Yet, in the case of outlier detection, we don’t have a clean data set representing the population of regular observations that can be used to train any tool.

Fitting an elliptic envelope

One common way of performing outlier detection is to assume that the regular data come from a known distribution (e.g. data are Gaussian distributed). From this assumption, we generally try to define the “shape” of the data, and can define outlying observations as observations which stand far enough from the fit shape.
The scikit-learn provides an object `covariance.EllipticEnvelope` that fits a robust covariance estimate to the data, and thus fits an ellipse to the central data points, ignoring points outside the central mode.

For instance, assuming that the inlier data are Gaussian distributed, it will estimate the inlier location and covariance in a robust way (i.e. without being influenced by outliers). The Mahalanobis distances obtained from this estimate is used to derive a measure of outlyingness. This strategy is illustrated below.

### Examples:

- See [Robust covariance estimation and Mahalanobis distances relevance](#) for an illustration of the difference between using a standard (`covariance.EmpiricalCovariance`) or a robust estimate (`covariance.MinCovDet`) of location and covariance to assess the degree of outlyingness of an observation.

### References:


### Isolation Forest

One efficient way of performing outlier detection in high-dimensional datasets is to use random forests. The `ensemble.IsolationForest` ‘isolates’ observations by randomly selecting a feature and then randomly selecting a split value between the maximum and minimum values of the selected feature.

Since recursive partitioning can be represented by a tree structure, the number of splittings required to isolate a sample is equivalent to the path length from the root node to the terminating node.
This path length, averaged over a forest of such random trees, is a measure of normality and our decision function. Random partitioning produces noticeably shorter paths for anomalies. Hence, when a forest of random trees collectively produce shorter path lengths for particular samples, they are highly likely to be anomalies. This strategy is illustrated below.

Examples:

- See `IsolationForest example` for an illustration of the use of IsolationForest.
- See `Outlier detection with several methods` for a comparison of `ensemble.IsolationForest` with `neighbors.LocalOutlierFactor`, `svm.OneClassSVM` (tuned to perform like an outlier detection method) and a covariance-based outlier detection with `covariance.EllipticEnvelope`.

References:


Local Outlier Factor

Another efficient way to perform outlier detection on moderately high dimensional datasets is to use the Local Outlier Factor (LOF) algorithm.

The `neighbors.LocalOutlierFactor` (LOF) algorithm computes a score (called local outlier factor) reflecting the degree of abnormality of the observations. It measures the local density deviation of a given data point with respect to its neighbors. The idea is to detect the samples that have a substantially lower density than their neighbors.
In practice the local density is obtained from the k-nearest neighbors. The LOF score of an observation is equal to the ratio of the average local density of his k-nearest neighbors, and its own local density: a normal instance is expected to have a local density similar to that of its neighbors, while abnormal data are expected to have much smaller local density.

The number k of neighbors considered, (alias parameter n_neighbors) is typically chosen 1) greater than the minimum number of objects a cluster has to contain, so that other objects can be local outliers relative to this cluster, and 2) smaller than the maximum number of close by objects that can potentially be local outliers. In practice, such informations are generally not available, and taking n_neighbors=20 appears to work well in general. When the proportion of outliers is high (i.e. greater than 10 %, as in the example below), n_neighbors should be greater (n_neighbors=35 in the example below).

The strength of the LOF algorithm is that it takes both local and global properties of datasets into consideration: it can perform well even in datasets where abnormal samples have different underlying densities. The question is not, how isolated the sample is, but how isolated it is with respect to the surrounding neighborhood.

This strategy is illustrated below.

Examples:

- See Anomaly detection with Local Outlier Factor (LOF) for an illustration of the use of neighbors.
- See Outlier detection with several methods, for a comparison with other anomaly detection methods.

References:

One-class SVM versus Elliptic Envelope versus Isolation Forest versus LOF

Strictly-speaking, the One-class SVM is not an outlier-detection method, but a novelty-detection method: its training set should not be contaminated by outliers as it may fit them. That said, outlier detection in high-dimension, or without any assumptions on the distribution of the inlying data is very challenging, and a One-class SVM gives useful results in these situations.

The examples below illustrate how the performance of the `covariance.EllipticEnvelope` degrades as the data is less and less unimodal. The `svm.OneClassSVM` works better on data with multiple modes and `ensemble.IsolationForest` and `neighbors.LocalOutlierFactor` perform well in every cases.
Table 3.1: Comparing One-class SVM, Isolation Forest, LOF, and Elliptic Envelope

For a inlier mode well-centered and elliptic, the `svm.OneClassSVM` is not able to benefit from the rotational symmetry of the inlier population. In addition, it fits a bit the outliers present in the training set. On the opposite, the decision rule based on fitting an `covariance.EllipticEnvelope` learns an ellipse, which fits well the inlier distribution. The `ensemble.IsolationForest` and `neighbors.LocalOutlierFactor` perform as well.

As the inlier distribution becomes bimodal, the `covariance.EllipticEnvelope` does not fit well the inliers. However, we can see that `ensemble.IsolationForest`, `svm.OneClassSVM` and `neighbors.LocalOutlierFactor` have difficulties to detect the two modes, and that the `svm.OneClassSVM` tends to overfit: because it has no model of inliers, it interprets a region where, by chance some outliers are clustered, as inliers.
Examples:

- See *Outlier detection with several methods.* for a comparison of the `svm.OneClassSVM` (tuned to perform like an outlier detection method), the `ensemble.IsolationForest`, the `neighbors.LocalOutlierFactor` and a covariance-based outlier detection `covariance.EllipticEnvelope`.

3.2.8 Density Estimation

Density estimation walks the line between unsupervised learning, feature engineering, and data modeling. Some of the most popular and useful density estimation techniques are mixture models such as Gaussian Mixtures (`sklearn.mixture.GaussianMixture`), and neighbor-based approaches such as the kernel density estimate (`sklearn.neighbors.KernelDensity`). Gaussian Mixtures are discussed more fully in the context of clustering, because the technique is also useful as an unsupervised clustering scheme.

Density estimation is a very simple concept, and most people are already familiar with one common density estimation technique: the histogram.

**Density Estimation: Histograms**

A histogram is a simple visualization of data where bins are defined, and the number of data points within each bin is tallied. An example of a histogram can be seen in the upper-left panel of the following figure:

A major problem with histograms, however, is that the choice of binning can have a disproportionate effect on the resulting visualization. Consider the upper-right panel of the above figure. It shows a histogram over the same data, with the bins shifted right. The results of the two visualizations look entirely different, and might lead to different interpretations of the data.
Intuitively, one can also think of a histogram as a stack of blocks, one block per point. By stacking the blocks in the appropriate grid space, we recover the histogram. But what if, instead of stacking the blocks on a regular grid, we center each block on the point it represents, and sum the total height at each location? This idea leads to the lower-left visualization. It is perhaps not as clean as a histogram, but the fact that the data drive the block locations mean that it is a much better representation of the underlying data.

This visualization is an example of a kernel density estimation, in this case with a top-hat kernel (i.e. a square block at each point). We can recover a smoother distribution by using a smoother kernel. The bottom-right plot shows a Gaussian kernel density estimate, in which each point contributes a Gaussian curve to the total. The result is a smooth density estimate which is derived from the data, and functions as a powerful non-parametric model of the distribution of points.

Kernel Density Estimation

Kernel density estimation in scikit-learn is implemented in the `sklearn.neighbors.KernelDensity` estimator, which uses the Ball Tree or KD Tree for efficient queries (see Nearest Neighbors for a discussion of these). Though the above example uses a 1D data set for simplicity, kernel density estimation can be performed in any number of dimensions, though in practice the curse of dimensionality causes its performance to degrade in high dimensions.

In the following figure, 100 points are drawn from a bimodal distribution, and the kernel density estimates are shown for three choices of kernels:

![Kernel Density Estimation](image)

It’s clear how the kernel shape affects the smoothness of the resulting distribution. The scikit-learn kernel density estimator can be used as follows:

```python
>>> from sklearn.neighbors.kde import KernelDensity
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> kde = KernelDensity(kernel='gaussian', bandwidth=0.2).fit(X)
>>> kde.score_samples(X)
array([-0.41075698, -0.41075698, -0.41076071, -0.41075698, -0.41075698, -0.41076071])
```
Here we have used `kernel='gaussian'`, as seen above. Mathematically, a kernel is a positive function $K(x; h)$ which is controlled by the bandwidth parameter $h$. Given this kernel form, the density estimate at a point $y$ within a group of points $x_i; i = 1 \cdots N$ is given by:

$$\rho_K(y) = \sum_{i=1}^{N} K((y - x_i)/h)$$

The bandwidth here acts as a smoothing parameter, controlling the tradeoff between bias and variance in the result. A large bandwidth leads to a very smooth (i.e. high-bias) density distribution. A small bandwidth leads to an unsmooth (i.e. high-variance) density distribution.

`sklearn.neighbors.KernelDensity` implements several common kernel forms, which are shown in the following figure:

![Available Kernels](image)

The form of these kernels is as follows:

- **Gaussian kernel** (kernel = 'gaussian')
  
  $K(x; h) \propto \exp(-x^2/2\pi^2)$

- **Tophat kernel** (kernel = 'tophat')
  
  $K(x; h) \propto 1$ if $x < h$

- **Epanechnikov kernel** (kernel = 'epanechnikov')
  
  $K(x; h) \propto 1 - \frac{x^2}{\pi^2}$

- **Exponential kernel** (kernel = 'exponential')
  
  $K(x; h) \propto \exp(-x/h)$

- **Linear kernel** (kernel = 'linear')
  
  $K(x; h) \propto 1 - x/h$ if $x < h$
• Cosine kernel (kernel = 'cosine')

\[ K(x; h) \propto \cos\left(\frac{\pi x}{2h}\right) \text{ if } x < h \]

The kernel density estimator can be used with any of the valid distance metrics (see `sklearn.neighbors.DistanceMetric` for a list of available metrics), though the results are properly normalized only for the Euclidean metric. One particularly useful metric is the Haversine distance which measures the angular distance between points on a sphere. Here is an example of using a kernel density estimate for a visualization of geospatial data, in this case the distribution of observations of two different species on the South American continent:

One other useful application of kernel density estimation is to learn a non-parametric generative model of a dataset in order to efficiently draw new samples from this generative model. Here is an example of using this process to create a new set of hand-written digits, using a Gaussian kernel learned on a PCA projection of the data:
The “new” data consists of linear combinations of the input data, with weights probabilistically drawn given the KDE model.

Examples:

- **Simple 1D Kernel Density Estimation**: computation of simple kernel density estimates in one dimension.
- **Kernel Density Estimation**: an example of using Kernel Density estimation to learn a generative model of the hand-written digits data, and drawing new samples from this model.
- **Kernel Density Estimate of Species Distributions**: an example of Kernel Density estimation using the Haversine distance metric to visualize geospatial data

### 3.2.9 Neural network models (unsupervised)

#### Restricted Boltzmann machines

Restricted Boltzmann machines (RBM) are unsupervised nonlinear feature learners based on a probabilistic model. The features extracted by an RBM or a hierarchy of RBMs often give good results when fed into a linear classifier such as a linear SVM or a perceptron.

The model makes assumptions regarding the distribution of inputs. At the moment, scikit-learn only provides `BernoulliRBM`, which assumes the inputs are either binary values or values between 0 and 1, each encoding the probability that the specific feature would be turned on.

The RBM tries to maximize the likelihood of the data using a particular graphical model. The parameter learning algorithm used (**Stochastic Maximum Likelihood**) prevents the representations from straying far from the input data, which makes them capture interesting regularities, but makes the model less useful for small datasets, and usually not useful for density estimation.
The method gained popularity for initializing deep neural networks with the weights of independent RBMs. This method is known as unsupervised pre-training.

### 100 components extracted by RBM

Examples:

- Restricted Boltzmann Machine features for digit classification

#### Graphical model and parametrization

The graphical model of an RBM is a fully-connected bipartite graph.
The nodes are random variables whose states depend on the state of the other nodes they are connected to. The model is therefore parameterized by the weights of the connections, as well as one intercept (bias) term for each visible and hidden unit, omitted from the image for simplicity.

The energy function measures the quality of a joint assignment:

\[
E(v, h) = \sum_i \sum_j w_{ij} v_i h_j + \sum_i b_i v_i + \sum_j c_j h_j
\]

In the formula above, \( b \) and \( c \) are the intercept vectors for the visible and hidden layers, respectively. The joint probability of the model is defined in terms of the energy:

\[
P(v, h) = \frac{e^{-E(v, h)}}{Z}
\]

The word restricted refers to the bipartite structure of the model, which prohibits direct interaction between hidden units, or between visible units. This means that the following conditional independencies are assumed:

\[
h_i \perp h_j | v
\]

\[
v_i \perp v_j | h
\]

The bipartite structure allows for the use of efficient block Gibbs sampling for inference.

**Bernoulli Restricted Boltzmann machines**

In the BernoulliRBMs, all units are binary stochastic units. This means that the input data should either be binary, or real-valued between 0 and 1 signifying the probability that the visible unit would turn on or off. This is a good model for character recognition, where the interest is on which pixels are active and which aren’t. For images of natural scenes it no longer fits because of background, depth and the tendency of neighbouring pixels to take the same values.

The conditional probability distribution of each unit is given by the logistic sigmoid activation function of the input it receives:

\[
P(v_i = 1|h) = \sigma(\sum_j w_{ij} h_j + b_i)
\]

\[
P(h_i = 1|v) = \sigma(\sum_i w_{ij} v_i + c_j)
\]
where $\sigma$ is the logistic sigmoid function:

$$\sigma(x) = \frac{1}{1 + e^{-x}}$$

**Stochastic Maximum Likelihood learning**

The training algorithm implemented in `BernoulliRBM` is known as Stochastic Maximum Likelihood (SML) or Persistent Contrastive Divergence (PCD). Optimizing maximum likelihood directly is infeasible because of the form of the data likelihood:

$$\log P(v) = \log \sum_h e^{-E(v,h)} - \log \sum_{x,y} e^{-E(x,y)}$$

For simplicity the equation above is written for a single training example. The gradient with respect to the weights is formed of two terms corresponding to the ones above. They are usually known as the positive gradient and the negative gradient, because of their respective signs. In this implementation, the gradients are estimated over mini-batches of samples.

In maximizing the log-likelihood, the positive gradient makes the model prefer hidden states that are compatible with the observed training data. Because of the bipartite structure of RBMs, it can be computed efficiently. The negative gradient, however, is intractable. Its goal is to lower the energy of joint states that the model prefers, therefore making it stay true to the data. It can be approximated by Markov chain Monte Carlo using block Gibbs sampling by iteratively sampling each of $v$ and $h$ given the other, until the chain mixes. Samples generated in this way are sometimes referred as fantasy particles. This is inefficient and it is difficult to determine whether the Markov chain mixes.

The Contrastive Divergence method suggests to stop the chain after a small number of iterations, $k$, usually even 1. This method is fast and has low variance, but the samples are far from the model distribution.

Persistent Contrastive Divergence addresses this. Instead of starting a new chain each time the gradient is needed, and performing only one Gibbs sampling step, in PCD we keep a number of chains (fantasy particles) that are updated $k$ Gibbs steps after each weight update. This allows the particles to explore the space more thoroughly.

**References:**

- “Training Restricted Boltzmann Machines using Approximations to the Likelihood Gradient” T. Tieleman, 2008

### 3.3 Model selection and evaluation

#### 3.3.1 Cross-validation: evaluating estimator performance

Learning the parameters of a prediction function and testing it on the same data is a methodological mistake: a model that would just repeat the labels of the samples that it has just seen would have a perfect score but would fail to predict anything useful on yet-unseen data. This situation is called overfitting. To avoid it, it is common practice when performing a (supervised) machine learning experiment to hold out part of the available data as a test set $X_{\text{test}}, y_{\text{test}}$. Note that the word “experiment” is not intended to denote academic use only, because even in commercial settings machine learning usually starts out experimentally.

In scikit-learn a random split into training and test sets can be quickly computed with the `train_test_split` helper function. Let’s load the iris data set to fit a linear support vector machine on it:
We can now quickly sample a training set while holding out 40% of the data for testing (evaluating) our classifier:

```python
>>> X_train, X_test, y_train, y_test = train_test_split(
...    iris.data, iris.target, test_size=0.4, random_state=0)

>>> X_train.shape, y_train.shape
((90, 4), (90,))

>>> X_test.shape, y_test.shape
((60, 4), (60,))

>>> clf = svm.SVC(kernel='linear', C=1).fit(X_train, y_train)

>>> clf.score(X_test, y_test)
0.96...
```

When evaluating different settings (“hyperparameters”) for estimators, such as the C setting that must be manually set for an SVM, there is still a risk of overfitting on the test set because the parameters can be tweaked until the estimator performs optimally. This way, knowledge about the test set can “leak” into the model and evaluation metrics no longer report on generalization performance. To solve this problem, yet another part of the dataset can be held out as a so-called “validation set”: training proceeds on the training set, after which evaluation is done on the validation set, and when the experiment seems to be successful, final evaluation can be done on the test set.

However, by partitioning the available data into three sets, we drastically reduce the number of samples which can be used for learning the model, and the results can depend on a particular random choice for the pair of (train, validation) sets.

A solution to this problem is a procedure called cross-validation (CV for short). A test set should still be held out for final evaluation, but the validation set is no longer needed when doing CV. In the basic approach, called k-fold CV, the training set is split into k smaller sets (other approaches are described below, but generally follow the same principles). The following procedure is followed for each of the k “folds”:

- A model is trained using k − 1 of the folds as training data;
- the resulting model is validated on the remaining part of the data (i.e., it is used as a test set to compute a performance measure such as accuracy).

The performance measure reported by k-fold cross-validation is then the average of the values computed in the loop. This approach can be computationnally expensive, but does not waste too much data (as it is the case when fixing an arbitrary test set), which is a major advantage in problem such as inverse inference where the number of samples is very small.

**Computing cross-validated metrics**

The simplest way to use cross-validation is to call the `cross_val_score` helper function on the estimator and the dataset.

The following example demonstrates how to estimate the accuracy of a linear kernel support vector machine on the iris dataset by splitting the data, fitting a model and computing the score 5 consecutive times (with different splits each time):
```python
>>> from sklearn.model_selection import cross_val_score
>>> clf = svm.SVC(kernel='linear', C=1)
>>> scores = cross_val_score(clf, iris.data, iris.target, cv=5)
>>> scores
array([ 0.96..., 1. ..., 0.96..., 0.96..., 1. ])
```

The mean score and the 95% confidence interval of the score estimate are hence given by:

```python
>>> print("Accuracy: %0.2f (+/- %0.2f) \%(scores.mean(), scores.std() * 2))
Accuracy: 0.98 (+/- 0.03)
```

By default, the score computed at each CV iteration is the score method of the estimator. It is possible to change this by using the scoring parameter:

```python
>>> from sklearn import metrics
>>> scores = cross_val_score(
...     clf, iris.data, iris.target, cv=5, scoring='f1_macro')
>>> scores
array([ 0.96..., 1. ..., 0.96..., 0.96..., 1. ])
```

See The scoring parameter: defining model evaluation rules for details. In the case of the Iris dataset, the samples are balanced across target classes hence the accuracy and the F1-score are almost equal.

When the cv argument is an integer, cross_val_score uses the KFold or StratifiedKFold strategies by default, the latter being used if the estimator derives from ClassifierMixin.

It is also possible to use other cross validation strategies by passing a cross validation iterator instead, for instance:

```python
>>> from sklearn.model_selection import ShuffleSplit
>>> n_samples = iris.data.shape[0]
>>> cv = ShuffleSplit(n_splits=3, test_size=0.3, random_state=0)
>>> cross_val_score(clf, iris.data, iris.target, cv=cv)
... array([ 0.97..., 0.97..., 1. ])
```

Data transformation with held out data

Just as it is important to test a predictor on data held-out from training, preprocessing (such as standardization, feature selection, etc.) and similar data transformations similarly should be learnt from a training set and applied to held-out data for prediction:

```python
>>> from sklearn import preprocessing
>>> X_train, X_test, y_train, y_test = train_test_split(
...     iris.data, iris.target, test_size=0.4, random_state=0)
>>> scaler = preprocessing.StandardScaler().fit(X_train)
>>> X_train_transformed = scaler.transform(X_train)
>>> X_test_transformed = scaler.transform(X_test)
>>> clf = svm.SVC(C=1).fit(X_train_transformed, y_train)
>>> clf.score(X_test_transformed, y_test)
0.9333...
```

A Pipeline makes it easier to compose estimators, providing this behavior under cross-validation:

```python
>>> from sklearn.pipeline import make_pipeline
>>> clf = make_pipeline(preprocessing.StandardScaler(), svm.SVC(C=1))
>>> cross_val_score(clf, iris.data, iris.target, cv=cv)
... array([ 0.97..., 0.93..., 0.95...])
```
The cross_validate function and multiple metric evaluation

The `cross_validate` function differs from `cross_val_score` in two ways -

- It allows specifying multiple metrics for evaluation.
- It returns a dict containing training scores, fit-times and score-times in addition to the test score.

For single metric evaluation, where the scoring parameter is a string, callable or None, the keys will be -

- ['test_score', 'fit_time', 'score_time']

And for multiple metric evaluation, the return value is a dict with the following keys -

- ['test_<scorer1_name>', 'test_<scorer2_name>', 'test_<scorer...>', 'fit_time', 'score_time']

`return_train_score` is set to `True` by default. It adds train score keys for all the scorers. If train scores are not needed, this should be set to `False` explicitly.

The multiple metrics can be specified either as a list, tuple or set of predefined scorer names:

```python
>>> from sklearn.model_selection import cross_validate
>>> from sklearn.metrics import recall_score

>>> scoring = ['precision_macro', 'recall_macro']
>>> clf = svm.SVC(kernel='linear', C=1, random_state=0)
>>> scores = cross_validate(clf, iris.data, iris.target, scoring=scoring,
                   ... cv=5, return_train_score=False)
>>> sorted(scores.keys())
['fit_time', 'score_time', 'test_precision_macro', 'test_recall_macro']
>>> scores['test_recall_macro']
array([ 0.96..., 1. ..., 0.96..., 0.96..., 1.])
```

Or as a dict mapping scorer name to a predefined or custom scoring function:

```python
>>> from sklearn.metrics.scorer import make_scorer

>>> scoring = {'prec_macro': 'precision_macro',
...             'rec_micro': make_scorer(recall_score, average='macro')}
>>> scores = cross_validate(clf, iris.data, iris.target, scoring=scoring,
                   ... cv=5, return_train_score=True)
>>> sorted(scores.keys())
['fit_time', 'score_time', 'test_prec_macro', 'test_rec_micro',
 'train_prec_macro', 'train_rec_micro']
>>> scores['train_rec_micro']
array([ 0.97..., 0.97..., 0.99..., 0.98..., 0.98...])
```

Here is an example of `cross_validate` using a single metric:

```python
>>> scores = cross_validate(clf, iris.data, iris.target,
                   ... scoring='precision_macro')
>>> sorted(scores.keys())
['fit_time', 'score_time', 'test_score', 'train_score']
```
Obtaining predictions by cross-validation

The function `cross_val_predict` has a similar interface to `cross_val_score`, but returns, for each element in the input, the prediction that was obtained for that element when it was in the test set. Only cross-validation strategies that assign all elements to a test set exactly once can be used (otherwise, an exception is raised).

These prediction can then be used to evaluate the classifier:

```python
>>> from sklearn.model_selection import cross_val_predict
>>> predicted = cross_val_predict(clf, iris.data, iris.target, cv=10)
>>> metrics.accuracy_score(iris.target, predicted)
0.973...
```

Note that the result of this computation may be slightly different from those obtained using `cross_val_score` as the elements are grouped in different ways.

The available cross validation iterators are introduced in the following section.

Examples

- Receiver Operating Characteristic (ROC) with cross validation,
- Recursive feature elimination with cross-validation,
- Parameter estimation using grid search with cross-validation,
- Sample pipeline for text feature extraction and evaluation,
- Plotting Cross-Validated Predictions,
- Nested versus non-nested cross-validation.

Cross validation iterators

The following sections list utilities to generate indices that can be used to generate dataset splits according to different cross validation strategies.

Cross-validation iterators for i.i.d. data

Assuming that some data is Independent and Identically Distributed (i.i.d.) is making the assumption that all samples stem from the same generative process and that the generative process is assumed to have no memory of past generated samples.

The following cross-validators can be used in such cases.

NOTE

While i.i.d. data is a common assumption in machine learning theory, it rarely holds in practice. If one knows that the samples have been generated using a time-dependent process, it’s safer to use a time-series aware cross-validation scheme. Similarly if we know that the generative process has a group structure (samples from collected from different subjects, experiments, measurement devices) it safer to use group-wise cross-validation.

K-fold

`KFold` divides all the samples in \( k \) groups of samples, called folds (if \( k = n \), this is equivalent to the Leave One Out
strategy), of equal sizes (if possible). The prediction function is learned using \( k - 1 \) folds, and the fold left out is used for test.

Example of 2-fold cross-validation on a dataset with 4 samples:

```python
>>> import numpy as np
>>> from sklearn.model_selection import KFold

>>> X = ["a", "b", "c", "d"]
>>> kf = KFold(n_splits=2)
>>> for train, test in kf.split(X):
...     print("%s %s" % (train, test))
[2 3] [0 1]
[0 1] [2 3]
```

Each fold is constituted by two arrays: the first one is related to the training set, and the second one to the test set. Thus, one can create the training/test sets using numpy indexing:

```python
>>> X = np.array([[0., 0.], [1., 1.], [-1., -1.], [2., 2.]])
>>> y = np.array([0, 1, 0, 1])
>>> X_train, X_test, y_train, y_test = X[train], X[test], y[train], y[test]
```

**Repeated K-Fold**

RepeatedKFold repeats K-Fold \( n \) times. It can be used when one requires to run KFold \( n \) times, producing different splits in each repetition.

Example of 2-fold K-Fold repeated 2 times:

```python
>>> import numpy as np
>>> from sklearn.model_selection import RepeatedKFold

>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> random_state = 12883823
>>> rkf = RepeatedKFold(n_splits=2, n_repeats=2, random_state=random_state)
>>> for train, test in rkf.split(X):
...     print("%s %s" % (train, test))
...[2 3] [0 1]
[0 1] [2 3]
```

Similarly, RepeatedStratifiedKFold repeats Stratified K-Fold \( n \) times with different randomization in each repetition.

**Leave One Out (LOO)**

LeaveOneOut (or LOO) is a simple cross-validation. Each learning set is created by taking all the samples except one, the test set being the sample left out. Thus, for \( n \) samples, we have \( n \) different training sets and \( n \) different tests set. This cross-validation procedure does not waste much data as only one sample is removed from the training set:

```python
>>> from sklearn.model_selection import LeaveOneOut

>>> X = [1, 2, 3, 4]
>>> loo = LeaveOneOut()
```
Potential users of LOO for model selection should weigh a few known caveats. When compared with k-fold cross validation, one builds n models from n samples instead of k models, where n > k. Moreover, each is trained on n − 1 samples rather than (k − 1)n/k. In both ways, assuming k is not too large and k < n, LOO is more computationally expensive than k-fold cross validation.

In terms of accuracy, LOO often results in high variance as an estimator for the test error. Intuitively, since n − 1 of the n samples are used to build each model, models constructed from folds are virtually identical to each other and to the model built from the entire training set.

However, if the learning curve is steep for the training size in question, then 5- or 10- fold cross validation can overestimate the generalization error.

As a general rule, most authors, and empirical evidence, suggest that 5- or 10- fold cross validation should be preferred to LOO.

References:

- R. Kohavi, A Study of Cross-Validation and Bootstrap for Accuracy Estimation and Model Selection, Intl. Jnt. Conf. AI
- G. James, D. Witten, T. Hastie, R Tibshirani, An Introduction to Statistical Learning, Springer 2013.

Leave P Out (LPO)

LeavePOut is very similar to LeaveOneOut as it creates all the possible training/test sets by removing p samples from the complete set. For n samples, this produces \( \binom{n}{p} \) train-test pairs. Unlike LeaveOneOut and KFold, the test sets will overlap for p > 1.

Example of Leave-2-Out on a dataset with 4 samples:
Random permutations cross-validation a.k.a. Shuffle & Split

**ShuffleSplit**

The **ShuffleSplit** iterator will generate a user defined number of independent train / test dataset splits. Samples are first shuffled and then split into a pair of train and test sets.

It is possible to control the randomness for reproducibility of the results by explicitly seeding the `random_state` pseudo random number generator.

Here is a usage example:

```python
>>> from sklearn.model_selection import ShuffleSplit
>>> X = np.arange(5)
>>> ss = ShuffleSplit(n_splits=3, test_size=0.25, random_state=0)
>>> for train_index, test_index in ss.split(X):
...     print("%s %s" % (train_index, test_index))
[1 3 4] [2 0]
[1 4 3] [0 2]
[4 0 2] [1 3]
```

**ShuffleSplit** is thus a good alternative to **KFold** cross validation that allows a finer control on the number of iterations and the proportion of samples on each side of the train / test split.

**Cross-validation iterators with stratification based on class labels.**

Some classification problems can exhibit a large imbalance in the distribution of the target classes: for instance there could be several times more negative samples than positive samples. In such cases it is recommended to use stratified sampling as implemented in **StratifiedKFold** and **StratifiedShuffleSplit** to ensure that relative class frequencies is approximately preserved in each train and validation fold.

**Stratified k-fold**

**StratifiedKFold** is a variation of **k-fold** which returns stratified folds: each set contains approximately the same percentage of samples of each target class as the complete set.

Example of stratified 3-fold cross-validation on a dataset with 10 samples from two slightly unbalanced classes:

```python
>>> from sklearn.model_selection import StratifiedKFold
>>> X = np.ones(10)
>>> y = [0, 0, 0, 0, 1, 1, 1, 1, 1, 1]
>>> skf = StratifiedKFold(n_splits=3)
>>> for train, test in skf.split(X, y):
...     print("%s %s" % (train, test))
[2 3 6 7 8 9] [0 1 4 5]
[0 1 3 4 5 8 9] [2 6 7]
[0 1 2 4 5 6 7] [3 8 9]
```
RepeatedStratifiedKFold can be used to repeat Stratified K-Fold n times with different randomization in each repetition.

**Stratified Shuffle Split**

StratifiedShuffleSplit is a variation of ShuffleSplit, which returns stratified splits, *i.e.* which creates splits by preserving the same percentage for each target class as in the complete set.

**Cross-validation iterators for grouped data.**

The i.i.d. assumption is broken if the underlying generative process yield groups of dependent samples.

Such a grouping of data is domain specific. An example would be when there is medical data collected from multiple patients, with multiple samples taken from each patient. And such data is likely to be dependent on the individual group. In our example, the patient id for each sample will be its group identifier.

In this case we would like to know if a model trained on a particular set of groups generalizes well to the unseen groups. To measure this, we need to ensure that all the samples in the validation fold come from groups that are not represented at all in the paired training fold.

The following cross-validation splitters can be used to do that. The grouping identifier for the samples is specified via the groups parameter.

**Group k-fold**

GroupKFold is a variation of k-fold which ensures that the same group is not represented in both testing and training sets. For example if the data is obtained from different subjects with several samples per-subject and if the model is flexible enough to learn from highly person specific features it could fail to generalize to new subjects. GroupKFold makes it possible to detect this kind of overfitting situations.

Imagine you have three subjects, each with an associated number from 1 to 3:

```python
>>> from sklearn.model_selection import GroupKFold

>>> X = [0.1, 0.2, 2.2, 2.4, 2.3, 4.55, 5.8, 8.8, 9, 10]
>>> y = ["a", "b", "b", "b", "c", "c", "d", "d", "d"]
>>> groups = [1, 1, 1, 2, 2, 2, 3, 3, 3, 3]

>>> gkf = GroupKFold(n_splits=3)
>>> for train, test in gkf.split(X, y, groups=groups):
...     print("%s %s" % (train, test))
[0 1 2 3 4 5] [6 7 8 9]
[0 1 2 6 7 8 9] [3 4 5]
[3 4 5 6 7 8 9] [0 1 2]
```

Each subject is in a different testing fold, and the same subject is never in both testing and training. Notice that the folds do not have exactly the same size due to the imbalance in the data.

**Leave One Group Out**

LeaveOneGroupOut is a cross-validation scheme which holds out the samples according to a third-party provided array of integer groups. This group information can be used to encode arbitrary domain specific pre-defined cross-validation folds.
Each training set is thus constituted by all the samples except the ones related to a specific group.

For example, in the cases of multiple experiments, `LeaveOneGroupOut` can be used to create a cross-validation based on the different experiments: we create a training set using the samples of all the experiments except one:

```python
>>> from sklearn.model_selection import LeaveOneGroupOut

>>> X = [1, 5, 10, 50, 60, 70, 80]
>>> y = [0, 1, 1, 2, 2, 2, 2]
>>> groups = [1, 1, 2, 2, 3, 3, 3]
>>> logo = LeaveOneGroupOut()
>>> for train, test in logo.split(X, y, groups=groups):
...     print("%s %s" % (train, test))
[2 3 4 5 6] [0 1]
[0 1 4 5 6] [2 3]
[0 1 2 3] [4 5 6]
```

Another common application is to use time information: for instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

**Leave P Groups Out**

`LeavePGroupsOut` is similar as `LeaveOneGroupOut`, but removes samples related to $P$ groups for each training/test set.

Example of Leave-2-Group Out:

```python
>>> from sklearn.model_selection import LeavePGroupsOut

>>> X = np.arange(6)
>>> y = [1, 1, 1, 2, 2, 2]
>>> groups = [1, 1, 2, 2, 3, 3]
>>> lpgo = LeavePGroupsOut(n_groups=2)
>>> for train, test in lpgo.split(X, y, groups=groups):
...     print("%s %s" % (train, test))
[4 5] [0 1 2 3]
[2 3] [0 1 4 5]
[0 1] [2 3 4 5]
```

**Group Shuffle Split**

The `GroupShuffleSplit` iterator behaves as a combination of `ShuffleSplit` and `LeavePGroupsOut`, and generates a sequence of randomized partitions in which a subset of groups are held out for each split.

Here is a usage example:

```python
>>> from sklearn.model_selection import GroupShuffleSplit

>>> X = [0.1, 0.2, 2.2, 2.4, 2.3, 4.55, 5.8, 0.001]
>>> y = ["a", "b", "b", "b", "c", "c", "c", "a"]
>>> groups = [1, 1, 2, 2, 3, 3, 4, 4]
>>> gss = GroupShuffleSplit(n_splits=4, test_size=0.5, random_state=0)
>>> for train, test in gss.split(X, y, groups=groups):
...     print("%s %s" % (train, test))
...[0 1 2 3] [4 5 6 7]
```
This class is useful when the behavior of LeavePGroupsOut is desired, but the number of groups is large enough that generating all possible partitions with \( P \) groups withheld would be prohibitively expensive. In such a scenario, GroupShuffleSplit provides a random sample (with replacement) of the train / test splits generated by LeavePGroupsOut.

Predefined Fold-Splits / Validation-Sets

For some datasets, a pre-defined split of the data into training- and validation fold or into several cross-validation folds already exists. Using PredefinedSplit it is possible to use these folds e.g. when searching for hyperparameters.

For example, when using a validation set, set the test_fold to 0 for all samples that are part of the validation set, and to -1 for all other samples.

Cross validation of time series data

Time series data is characterised by the correlation between observations that are near in time (autocorrelation). However, classical cross-validation techniques such as KFold and ShuffleSplit assume the samples are independent and identically distributed, and would result in unreasonable correlation between training and testing instances (yielding poor estimates of generalisation error) on time series data. Therefore, it is very important to evaluate our model for time series data on the “future” observations least like those that are used to train the model. To achieve this, one solution is provided by TimeSeriesSplit.

Time Series Split

TimeSeriesSplit is a variation of \( k \)-fold which returns first \( k \) folds as train set and the \((k + 1)\) th fold as test set. Note that unlike standard cross-validation methods, successive training sets are supersets of those that come before them. Also, it adds all surplus data to the first training partition, which is always used to train the model.

This class can be used to cross-validate time series data samples that are observed at fixed time intervals.

Example of 3-split time series cross-validation on a dataset with 6 samples:

```python
>>> from sklearn.model_selection import TimeSeriesSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4, 5, 6])
>>> tscv = TimeSeriesSplit(n_splits=3)
>>> print(tscv)
TimeSeriesSplit(max_train_size=None, n_splits=3)
>>> for train, test in tscv.split(X):
...     print("%s %s" % (train, test))
[0 1 2] [3]
[0 1 2 3] [4]
[0 1 2 3 4] [5]
```
A note on shuffling

If the data ordering is not arbitrary (e.g., samples with the same class label are contiguous), shuffling it first may be essential to get a meaningful cross-validation result. However, the opposite may be true if the samples are not independently and identically distributed. For example, if samples correspond to news articles, and are ordered by their time of publication, then shuffling the data will likely lead to a model that is overfit and an inflated validation score: it will be tested on samples that are artificially similar (close in time) to training samples.

Some cross validation iterators, such as \texttt{KFold}, have an inbuilt option to shuffle the data indices before splitting them. Note that:

- This consumes less memory than shuffling the data directly.
- By default no shuffling occurs, including for the (stratified) K fold cross-validation performed by specifying \texttt{cv=some_integer} to \texttt{cross_val_score}, grid search, etc. Keep in mind that \texttt{train_test_split} still returns a random split.
- The \texttt{random_state} parameter defaults to \texttt{None}, meaning that the shuffling will be different every time \texttt{KFold(..., shuffle=True)} is iterated. However, \texttt{GridSearchCV} will use the same shuffling for each set of parameters validated by a single call to its \texttt{fit} method.
- To get identical results for each split, set \texttt{random_state} to an integer.

Cross validation and model selection

Cross validation iterators can also be used to directly perform model selection using Grid Search for the optimal hyperparameters of the model. This is the topic of the next section: \textit{Tuning the hyper-parameters of an estimator}.

3.3.2 Tuning the hyper-parameters of an estimator

Hyper-parameters are parameters that are not directly learnt within estimators. In scikit-learn they are passed as arguments to the constructor of the estimator classes. Typical examples include \texttt{C}, \texttt{kernel} and \texttt{gamma} for Support Vector Classifier, \texttt{alpha} for Lasso, etc.

It is possible and recommended to search the hyper-parameter space for the best \textit{cross validation} score.

Any parameter provided when constructing an estimator may be optimized in this manner. Specifically, to find the names and current values for all parameters for a given estimator, use:

```
estimator.get_params()
```

A search consists of:

- an estimator (regressor or classifier such as \texttt{sklearn.svm.SVC()});
- a parameter space;
- a method for searching or sampling candidates;
- a cross-validation scheme; and
- a score function.

Some models allow for specialized, efficient parameter search strategies, outlined below. Two generic approaches to sampling search candidates are provided in scikit-learn: for given values, \texttt{GridSearchCV} exhaustively considers all parameter combinations, while \texttt{RandomizedSearchCV} can sample a given number of candidates from a parameter space with a specified distribution. After describing these tools we detail best practice applicable to both approaches.

Note that it is common that a small subset of those parameters can have a large impact on the predictive or computation performance of the model while others can be left to their default values. It is recommended to read the docstring of
the estimator class to get a finer understanding of their expected behavior, possibly by reading the enclosed reference to the literature.

**Exhaustive Grid Search**

The grid search provided by `GridSearchCV` exhaustively generates candidates from a grid of parameter values specified with the `param_grid` parameter. For instance, the following `param_grid`:

```python
param_grid = [
    {'C': [1, 10, 100, 1000], 'kernel': ['linear']},
    {'C': [1, 10, 100, 1000], 'gamma': [0.001, 0.0001], 'kernel': ['rbf']},
]
```

specifies that two grids should be explored: one with a linear kernel and C values in [1, 10, 100, 1000], and the second one with an RBF kernel, and the cross-product of C values ranging in [1, 10, 100, 1000] and gamma values in [0.001, 0.0001].

The `GridSearchCV` instance implements the usual estimator API: when “fitting” it on a dataset all the possible combinations of parameter values are evaluated and the best combination is retained.

**Examples:**

- See *Parameter estimation using grid search with cross-validation* for an example of Grid Search computation on the digits dataset.
- See *Sample pipeline for text feature extraction and evaluation* for an example of Grid Search coupling parameters from a text documents feature extractor (n-gram count vectorizer and TF-IDF transformer) with a classifier (here a linear SVM trained with SGD with either elastic net or L2 penalty) using a pipeline. Pipeline instance.
- See *Nested versus non-nested cross-validation* for an example of Grid Search within a cross validation loop on the iris dataset. This is the best practice for evaluating the performance of a model with grid search.
- See *Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV* for an example of `GridSearchCV` being used to evaluate multiple metrics simultaneously.

**Randomized Parameter Optimization**

While using a grid of parameter settings is currently the most widely used method for parameter optimization, other search methods have more favourable properties. `RandomizedSearchCV` implements a randomized search over parameters, where each setting is sampled from a distribution over possible parameter values. This has two main benefits over an exhaustive search:

- A budget can be chosen independent of the number of parameters and possible values.
- Adding parameters that do not influence the performance does not decrease efficiency.

Specifying how parameters should be sampled is done using a dictionary, very similar to specifying parameters for `GridSearchCV`. Additionally, a computation budget, being the number of sampled candidates or sampling iterations, is specified using the `n_iter` parameter. For each parameter, either a distribution over possible values or a list of discrete choices (which will be sampled uniformly) can be specified:

```python
{'C': scipy.stats.expon(scale=100), 'gamma': scipy.stats.expon(scale=.1),
 'kernel': ['rbf'], 'class_weight': ['balanced', None]}
```
This example uses the `scipy.stats` module, which contains many useful distributions for sampling parameters, such as `expon`, `gamma`, `uniform` or `randint`. In principle, any function can be passed that provides a `rvs` (random variate sample) method to sample a value. A call to the `rvs` function should provide independent random samples from possible parameter values on consecutive calls.

**Warning:** The distributions in `scipy.stats` prior to version scipy 0.16 do not allow specifying a random state. Instead, they use the global numpy random state, that can be seeded via `np.random.seed` or set using `np.random.set_state`. However, beginning scikit-learn 0.18, the `sklearn.model_selection` module sets the random state provided by the user if scipy >= 0.16 is also available.

For continuous parameters, such as $C$ above, it is important to specify a continuous distribution to take full advantage of the randomization. This way, increasing `n_iter` will always lead to a finer search.

**Examples:**

- *Comparing randomized search and grid search for hyperparameter estimation* compares the usage and efficiency of randomized search and grid search.

**References:**


**Tips for parameter search**

**Specifying an objective metric**

By default, parameter search uses the `score` function of the estimator to evaluate a parameter setting. These are the `sklearn.metrics.accuracy_score` for classification and `sklearn.metrics.r2_score` for regression. For some applications, other scoring functions are better suited (for example in unbalanced classification, the accuracy score is often uninformative). An alternative scoring function can be specified via the `scoring` parameter to `GridSearchCV`, `RandomizedSearchCV` and many of the specialized cross-validation tools described below. See *The scoring parameter: defining model evaluation rules* for more details.

**Specifying multiple metrics for evaluation**

`GridSearchCV` and `RandomizedSearchCV` allow specifying multiple metrics for the `scoring` parameter. Multimetric scoring can either be specified as a list of strings of predefined scores names or a dict mapping the scorer name to the scorer function and/or the predefined scorer name(s). See *Using multiple metric evaluation* for more details.

When specifying multiple metrics, the `refit` parameter must be set to the metric (string) for which the `best_params_` will be found and used to build the `best_estimator_` on the whole dataset. If the search should not be refit, set `refit=False`. Leaving refit to the default value `None` will result in an error when using multiple metrics.

See *Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV* for an example usage.
Composite estimators and parameter spaces

*Pipeline: chaining estimators* describes building composite estimators whose parameter space can be searched with these tools.

**Model selection: development and evaluation**

Model selection by evaluating various parameter settings can be seen as a way to use the labeled data to “train” the parameters of the grid.

When evaluating the resulting model it is important to do it on held-out samples that were not seen during the grid search process: it is recommended to split the data into a *development set* (to be fed to the `GridSearchCV` instance) and an *evaluation set* to compute performance metrics.

This can be done by using the `train_test_split` utility function.

**Parallelism**

`GridSearchCV` and `RandomizedSearchCV` evaluate each parameter setting independently. Computations can be run in parallel if your OS supports it, by using the keyword `n_jobs=-1`. See function signature for more details.

**Robustness to failure**

Some parameter settings may result in a failure to fit one or more folds of the data. By default, this will cause the entire search to fail, even if some parameter settings could be fully evaluated. Setting `error_score=0` (or `=np.NaN`) will make the procedure robust to such failure, issuing a warning and setting the score for that fold to 0 (or `NaN`), but completing the search.

**Alternatives to brute force parameter search**

**Model specific cross-validation**

Some models can fit data for a range of values of some parameter almost as efficiently as fitting the estimator for a single value of the parameter. This feature can be leveraged to perform a more efficient cross-validation used for model selection of this parameter.

The most common parameter amenable to this strategy is the parameter encoding the strength of the regularizer. In this case we say that we compute the *regularization path* of the estimator.

Here is the list of such models:

<table>
<thead>
<tr>
<th>Model Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>linear_model.ElasticNetCV</code> (parameters)</td>
<td>Elastic Net model with iterative fitting along a regularization path</td>
</tr>
<tr>
<td><code>linear_model.LarsCV</code> (parameters)</td>
<td>Cross-validated Least Angle Regression model</td>
</tr>
<tr>
<td><code>linear_model.LassoCV</code> (parameters)</td>
<td>Lasso linear model with iterative fitting along a regularization path</td>
</tr>
<tr>
<td><code>linear_model.LassoLarsCV</code> (parameters)</td>
<td>Cross-validated Lasso, using the LARS algorithm</td>
</tr>
<tr>
<td><code>linear_model.LogisticRegressionCV</code> (parameters)</td>
<td>Logistic Regression CV (aka logit, MaxEnt) classifier.</td>
</tr>
</tbody>
</table>

Continued on next page
### Table 3.2 – continued from previous page

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>linear_model.MultiTaskLassoCV(...)</code></td>
<td>Multi-task L1/L2 Lasso with built-in cross-validation.</td>
</tr>
<tr>
<td><code>linear_model.OrthogonalMatchingPursuitCV(...)</code></td>
<td>Cross-validated Orthogonal Matching Pursuit model (OMP)</td>
</tr>
<tr>
<td><code>linear_model.RidgeCV([alphas, ...])</code></td>
<td>Ridge regression with built-in cross-validation.</td>
</tr>
<tr>
<td><code>linear_model.RidgeClassifierCV([alphas, ...])</code></td>
<td>Ridge classifier with built-in cross-validation.</td>
</tr>
</tbody>
</table>

**sklearn.linear_model.ElasticNetCV**

**class sklearn.linear_model.ElasticNetCV(l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, precompute='auto', max_iter=1000, tol=0.0001, cv=None, copy_X=True, verbose=0, n_jobs=1, positive=False, random_state=None, selection='cyclic')**

Elastic Net model with iterative fitting along a regularization path.

The best model is selected by cross-validation.

Read more in the User Guide.

**Parameters**

- **l1_ratio**: float or array of floats, optional
  
  Float between 0 and 1 passed to ElasticNet (scaling between L1 and L2 penalties). For **l1_ratio** = 0 the penalty is an L2 penalty. For **l1_ratio** = 1 it is an L1 penalty. For 0 < **l1_ratio** < 1, the penalty is a combination of L1 and L2. This parameter can be a list, in which case the different values are tested by cross-validation and the one giving the best prediction score is used. Note that a good choice of list of values for **l1_ratio** is often to put more values close to 1 (i.e. Lasso) and less close to 0 (i.e. Ridge), as in [0.1, 0.5, 0.7, 0.9, 0.95, 0.99, 1]

- **eps**: float, optional
  
  Length of the path. **eps**=1e-3 means that **alpha_min** / **alpha_max** = 1e-3.

- **n_alphas**: int, optional
  
  Number of alphas along the regularization path, used for each **l1_ratio**.

- **alphas**: numpy array, optional
  
  List of alphas where to compute the models. If None alphas are set automatically.

- **fit_intercept**: boolean
  
  Whether to calculate the intercept for this model. If set to False, no intercept will be used in calculations (e.g. data is expected to be already centered).

- **normalize**: boolean, optional, default False
  
  This parameter is ignored when **fit_intercept** is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the L2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

- **precompute**: True | False | ‘auto’ | array-like
  
  Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

- **max_iter**: int, optional
The maximum number of iterations

tol : float, optional

The tolerance for the optimization: if the updates are smaller than \( \text{tol} \), the optimization code checks the dual gap for optimality and continues until it is smaller than \( \text{tol} \).

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

copy_X : boolean, optional, default True

If True, \( X \) will be copied; else, it may be overwritten.

verbose : bool or integer

Amount of verbosity.

n_jobs : integer, optional

Number of CPUs to use during the cross validation. If -1, use all the CPUs.

positive : bool, optional

When set to True, forces the coefficients to be positive.

random_state : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’.

selection : str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’) often leads to significantly faster convergence especially when tol is higher than 1e-4.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>alpha_</td>
<td>(float) The amount of penalization chosen by cross validation</td>
</tr>
<tr>
<td>l1_ratio_</td>
<td>(float) The compromise between L1 and L2 penalization chosen by cross validation</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,)</td>
</tr>
<tr>
<td>intercept_</td>
<td>(float</td>
</tr>
<tr>
<td>mse_path_</td>
<td>(array, shape (n_l1_ratio, n_alpha, n_folds)) Mean square error for the test set on each fold, varying l1_ratio and alpha.</td>
</tr>
<tr>
<td>alphas_</td>
<td>(numpy array, shape (n_alphas,) or (n_l1_ratio, n_alphas)) The grid of alphas used for fitting, for each l1_ratio.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) number of iterations run by the coordinate descent solver to reach the specified tolerance for the optimal alpha.</td>
</tr>
</tbody>
</table>

See also:

enet_path, ElasticNet

Notes

For an example, see examples/linear_model/plot_lasso_model_selection.py.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

The parameter l1_ratio corresponds to alpha in the glmnet R package while alpha corresponds to the lambda parameter in glmnet. More specifically, the optimization objective is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \times ||y - Xw||^2_2 \\
+ \alpha \times l1_{\text{ratio}} \times ||w||_1 \\
+ 0.5 \times \alpha \times (1 - l1_{\text{ratio}}) \times ||w||^2_2
\]

If you are interested in controlling the L1 and L2 penalty separately, keep in mind that this is equivalent to:

\[
a \times L1 + b \times L2
\]

for:

\[
\alpha = a + b \quad \text{and} \quad l1_{\text{ratio}} = a / (a + b).
\]

Examples

```python
>>> from sklearn.linear_model import ElasticNetCV
>>> from sklearn.datasets import make_regression

>>> X, y = make_regression(n_features=2, random_state=0)

>>> regr = ElasticNetCV(cv=5, random_state=0)

>>> regr.fit(X, y)
ElasticNetCV(alphas=None, copy_X=True, cv=5, eps=0.001, fit_intercept=True,
           l1_ratio=0.5, max_iter=1000, n_alphas=100, n_l1_ratio=0.5,
           normalize=False, positive=False, precompute='auto', random_state=0,
           selection='cyclic', tol=0.0001, verbose=0)
```
>>> print(regr.alpha_)
0.19947279427

>>> print(regr.intercept_)
0.398882965428

>>> print(regr.predict([[0, 0]]))
[ 0.39888297]

Methods

**fit**(X, y)  
Fit linear model with coordinate descent

**get_params**(deep)
Get parameters for this estimator.

**path**(X, y[, l1_ratio, eps, n_alphas, ...])
Compute elastic net path with coordinate descent

**predict**(X)
Predict using the linear model

**score**(X, y[, sample_weight])
Returns the coefficient of determination R^2 of the prediction.

**set_params**(**params)
Set the parameters of this estimator.

__init__ (l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, precompute='auto', max_iter=1000, tol=0.0001, cv=None, copy_X=True, verbose=0, n_jobs=1, positive=False, random_state=None, selection='cyclic')

**fit**(X, y)
Fit linear model with coordinate descent

Fit is on grid of alphas and best alpha estimated by cross-validation.

Parameters  

**X** : [array-like], shape (n_samples, n_features)
Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output, X can be sparse.

**y** : array-like, shape (n_samples,) or (n_samples, n_targets)
Target values

**get_params**(deep=True)
Get parameters for this estimator.

Parameters  

**deep** : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns  

**params** : mapping of string to any
Parameter names mapped to their values.

static **path**(X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{2(n_{\text{samples}})} \| y - Xw \|_2^2 \\
+ \alpha \times l1_{\text{ratio}} \times \| w \|_1 \\
+ 0.5 \times \alpha \times (1 - l1_{\text{ratio}}) \times \| w \|_2^2
\]
For multi-output tasks it is:

\[
\frac{1}{(2 \ast n_{\text{samples}})} \ast \| Y - XW \|_{\text{Fro}}^2 \\
+ \alpha \ast \text{l1\_ratio} \ast \| W \|_{21} \\
+ 0.5 \ast \alpha \ast (1 - \text{l1\_ratio}) \ast \| W \|_{\text{Fro}}^2
\]

Where:

\[
\| W \|_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

**Parameters**

- **X** : {array-like}, shape (n_samples, n_features)
  - Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

- **y** : ndarray, shape (n_samples,) or (n_samples, n_outputs)
  - Target values

- **l1\_ratio** : float, optional
  - float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1\_ratio=1 corresponds to the Lasso

- **eps** : float
  - Length of the path. eps=1e-3 means that alpha\_min / alpha\_max = 1e-3

- **n\_alphas** : int, optional
  - Number of alphas along the regularization path

- **alphas** : ndarray, optional
  - List of alphas where to compute the models. If None alphas are set automatically

- **precompute** : True | False | ‘auto’ | array-like
  - Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix can also be passed as argument.

- **Xy** : array-like, optional
  - Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

- **copy\_X** : boolean, optional, default True
  - If True, X will be copied; else, it may be overwritten.

- **coef\_init** : array, shape (n\_features,) | None
  - The initial values of the coefficients.

- **verbose** : bool or integer
  - Amount of verbosity.

- **return\_n\_iter** : bool
  - whether to return the number of iterations or not.

- **positive** : bool, default False
If set to True, forces coefficients to be positive. (Only allowed when \(y_.ndim == 1\)).

**check_input** : bool, default True

Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params** : kwargs

Keyword arguments passed to the coordinate descent solver.

**Returns**

**alphas** : array, shape (n_alphas,)

The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iters** : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

**See also:**

MultiTaskElasticNet, MultiTaskElasticNetCV, ElasticNet, ElasticNetCV

**Notes**

For an example, see examples/linear_model/plot_lasso_coordinate_descent_path.py.

**predict** (X)

Predict using the linear model

**Parameters**

**X** : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

**Returns**

**C** : array, shape = (n_samples,)

Returns predicted values.

**score** (X, y, sample_weight=None)

Returns the coefficient of determination \(R^2\) of the prediction.

The coefficient \(R^2\) is defined as \((1 - u/v), \) where \(u\) is the residual sum of squares \((y_true - y_pred) ** 2).sum()\) and \(v\) is the total sum of squares \((y_true - y_true.mean()) ** 2).sum().\) The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \(y\), disregarding the input features, would get a \(R^2\) score of 0.0.

**Parameters**

**X** : array-like, shape = (n_samples, n_features)

Test samples.

**y** : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for \(X\).

**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.
Returns score : float

R^2 of self.predict(X) wrt. y.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

Returns self

sklearn.linear_model.LarsCV

class sklearn.linear_model.LarsCV(fit_intercept=True, verbose=False, max_iter=500, normalize=True, precompute='auto', cv=None, max_n_alphas=1000, n_jobs=1, eps=2.2204460492503131e-16, copy_X=True, positive=False)

Cross-validated Least Angle Regression model

Read more in the User Guide.

Parameters fit_intercept : boolean

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

verbose : boolean or integer, optional

Sets the verbosity amount

max_iter : integer, optional

Maximum number of iterations to perform.

normalize : boolean, optional, default True

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

precompute : True | False | 'auto' | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix cannot be passed as argument since we will use only subsets of X.

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

• None, to use the default 3-fold cross-validation,
• integer, to specify the number of folds.
• An object to be used as a cross-validation generator.
• An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.
**max_n_alphas**: integer, optional

The maximum number of points on the path used to compute the residuals in the cross-validation

**n_jobs**: integer, optional

Number of CPUs to use during the cross validation. If `-1`, use all the CPUs

**eps**: float, optional

The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.

**copy_X**: boolean, optional, default True

If `True`, X will be copied; else, it may be overwritten.

**positive**: boolean (default=False)

Restrict coefficients to be $\geq 0$. Be aware that you might want to remove fit_intercept which is set True by default.

### Attributes

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,)) parameter vector (w in the formulation formula)</td>
</tr>
<tr>
<td>intercept_</td>
<td>(float) independent term in decision function</td>
</tr>
<tr>
<td>coef_path_</td>
<td>(array, shape (n_features, n_alphas)) the varying values of the coefficients along the path</td>
</tr>
<tr>
<td>alpha</td>
<td>(float) the estimated regularization parameter alpha</td>
</tr>
<tr>
<td>alphas_</td>
<td>(array, shape (n_alphas,)) the different values of alpha along the path</td>
</tr>
<tr>
<td>cv_alphas_</td>
<td>(array, shape (n_cv_alphas,)) all the values of alpha along the path for the different folds</td>
</tr>
<tr>
<td>mse_path_</td>
<td>(array, shape (n_folds, n_cv_alphas)) the mean square error on left-out for each fold along the path (alpha values given by cv_alphas)</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(array-like or int) the number of iterations run by Lars with the optimal alpha.</td>
</tr>
</tbody>
</table>

### See also:

`lars_path`, `LassoLars`, `LassoLarsCV`

### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y)</td>
<td>Fit the model using X, y as training data.</td>
</tr>
<tr>
<td>get_params()</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**init** (fit_intercept=True, verbose=False, max_iter=500, normalize=True, precompute='auto', cv=None, max_n_alphas=1000, n_jobs=1, eps=2.2204460492503131e-16, copy_X=True, positive=False)

**alpha**

DEPRECATED: Attribute alpha is deprecated in 0.19 and will be removed in 0.21. See alpha_ instead

3.3. Model selection and evaluation
cv_mse_path
DEPRECATED: Attribute cv_mse_path is deprecated in 0.18 and will be removed in 0.20. Use mse_path instead

fit(X, y)
Fit the model using X, y as training data.

Parameters X : array-like, shape (n_samples, n_features)
Training data.

y : array-like, shape (n_samples,)
Target values.

Returns self : object
returns an instance of self.

get_params(deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict(X)
Predict using the linear model

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.

Returns C : array, shape = (n_samples,)
Returns predicted values.

score(X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns score : float
R^2 of self.predict(X) wrt. y.
**set_params**(**kwargs**)  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**sklearn.linear_model.LassoCV**

class sklearn.linear_model.LassoCV(eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, precompute='auto', max_iter=1000, tol=0.0001, copy_X=True, cv=None, verbose=False, n_jobs=1, positive=False, random_state=None, selection='cyclic')

Lasso linear model with iterative fitting along a regularization path

The best model is selected by cross-validation.

The optimization objective for Lasso is:

$$(1 / (2 \times n_{\text{samples}})) \times \|y - Xw\|^2_2 + \alpha \times \|w\|_1$$

Read more in the User Guide.

**Parameters**

**eps** : float, optional  
Length of the path. `eps=1e-3` means that `alpha_min / alpha_max = 1e-3`.

**n_alphas** : int, optional  
Number of alphas along the regularization path

**alphas** : numpy array, optional  
List of alphas where to compute the models. If `None` alphas are set automatically

**fit_intercept** : boolean, default True  
whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**normalize** : boolean, optional, default False  
This parameter is ignored when `fit_intercept` is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use `sklearn.preprocessing.StandardScaler` before calling fit on an estimator with `normalize=False`.

**precompute** : True | False | ‘auto’ | array-like  
Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

**max_iter** : int, optional  
The maximum number of iterations

**tol** : float, optional  
The tolerance for the optimization: if the updates are smaller than `tol`, the optimization code checks the dual gap for optimality and continues until it is smaller than `tol`.  

---

3.3. Model selection and evaluation

399
copy_X : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:
• None, to use the default 3-fold cross-validation,
• integer, to specify the number of folds.
• An object to be used as a cross-validation generator.
• An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

verbose : bool or integer

Amount of verbosity.

n_jobs : integer, optional

Number of CPUs to use during the cross validation. If -1, use all the CPUs.

positive : bool, optional

If positive, restrict regression coefficients to be positive

random_state : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to up-
date. If int, random_state is the seed used by the random number generator; If Ran-
domState instance, random_state is the random number generator; If None, the ran-
dom number generator is the RandomState instance used by np.random. Used when
selection == 'random'.

selection : str, default 'cyclic'

If set to ‘random’, a random coefficient is updated every iteration rather than looping
over features sequentially by default. This (setting to ‘random’) often leads to signifi-
cantly faster convergence especially when tol is higher than 1e-4.

Attributes

<table>
<thead>
<tr>
<th></th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>alpha_</td>
<td>(float) The amount of penalization chosen by cross validation</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,)</td>
</tr>
<tr>
<td>intercept_</td>
<td>(float</td>
</tr>
<tr>
<td>mse_path</td>
<td>(array, shape (n_alphas, n_folds)) mean square error for the test set on each fold, varying alpha</td>
</tr>
<tr>
<td>alphas_</td>
<td>(numpy array, shape (n_alphas,)) The grid of alphas used for fitting</td>
</tr>
<tr>
<td>dual_gap_</td>
<td>(ndarray, shape ()) The dual gap at the end of the optimization for the optimal alpha (alpha_).</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) number of iterations run by the coordinate descent solver to reach the specified tolerance for the optimal alpha.</td>
</tr>
</tbody>
</table>

See also:

lars_path, lasso_path, LassoLars, Lasso, LassoLarsCV
Notes

For an example, see `examples/linear_model/plot_lasso_model_selection.py`.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Methods

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<td>fit(X, y)</td>
<td>Fit linear model with coordinate descent</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>path(X, y[, eps, n_alphas, alphas,...])</td>
<td>Compute Lasso path with coordinate descent</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

`__init__`(eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, precompute=’auto’, max_iter=1000, tol=0.0001, copy_X=True, cv=None, verbose=False, random_state=None, selection=’cyclic’)

fit(X, y)
Fit linear model with coordinate descent

Parameters

- X : array-like, shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output, X can be sparse.

- y : array-like, shape (n_samples,) or (n_samples, n_targets)
  Target values

get_params(deep=True)
Get parameters for this estimator.

Parameters

- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- params : mapping of string to any
  Parameter names mapped to their values.

static path(X, y, eps=0.001, n_alphas=100, alphas=None, precompute=’auto’, Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, **params)
Compute Lasso path with coordinate descent

The Lasso optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
(1 / (2 \times n\_samples)) \times || y - Xw ||^2_2 + \alpha \times || w ||_1
\]

For multi-output tasks it is:
\[
\frac{1}{(2 + n_{\text{samples}})} \times ||Y - XW||_{\text{Fro}}^2 + \alpha \times ||W||_{21}
\]

Where:
\[
||W||_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]
i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  - Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If \(y\) is mono-output then \(X\) can be sparse.
- **y**: ndarray, shape (n_samples,), or (n_samples, n_outputs)
  - Target values
- **eps**: float, optional
  - Length of the path. \(\text{eps}=1e-3\) means that \(\alpha_{\text{min}} / \alpha_{\text{max}} = 1e-3\)
- **n_alphas**: int, optional
  - Number of alphas along the regularization path
- **alphas**: ndarray, optional
  - List of alphas where to compute the models. If None alphas are set automatically
- **precompute**: True | False | ‘auto’ | array-like
  - Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix can also be passed as argument.
- **Xy**: array-like, optional
  - \(Xy = \text{np.dot}(X.T, y)\) that can be precomputed. It is useful only when the Gram matrix is precomputed.
- **copy_X**: boolean, optional, default True
  - If True, \(X\) will be copied; else, it may be overwritten.
- **coef_init**: array, shape (n_features, ) | None
  - The initial values of the coefficients.
- **verbose**: bool or integer
  - Amount of verbosity.
- **return_n_iter**: bool
  - whether to return the number of iterations or not.
- **positive**: bool, default False
  - If set to True, forces coefficients to be positive. (Only allowed when \(y\).ndim == 1).
- **params**: kwargs
  - keyword arguments passed to the coordinate descent solver.

Returns

- **alphas**: array, shape (n_alphas,)
  - The alphas along the path where models are computed.
coefs : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)
    Coefficients along the path.

dual_gaps : array, shape (n_alphas,)
    The dual gaps at the end of the optimization for each alpha.

n_iters : array-like, shape (n_alphas,)
    The number of iterations taken by the coordinate descent optimizer to reach the specified
tolerance for each alpha.

See also:
    lars_path, Lasso, LassoLars, LassoCV, LassoLarsCV, sklearn.decomposition.
sparse_encode

Notes

For an example, see examples/linear_model/plot_lasso_coordinate_descent_path.py.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a
Fortran-contiguous numpy array.

Note that in certain cases, the Lars solver may be significantly faster to implement this functionality. In
particular, linear interpolation can be used to retrieve model coefficients between the values output by
lars_path

Examples

Comparing lasso_path and lars_path with interpolation:

```python
>>> X = np.array([[1, 2, 3.1], [2.3, 5.4, 4.3]]).T
>>> y = np.array([1, 2, 3.1])
>>> # Use lasso_path to compute a coefficient path
>>> _, coef_path, _ = lasso_path(X, y, alphas=[5., 1., .5])
>>> print(coef_path)
[[ 0.        0.        0.46874778]
 [ 0.2159048  0.4425765  0.23689075]]

>>> # Now use lars_path and 1D linear interpolation to compute the
>>> # same path
>>> from sklearn.linear_model import lars_path
>>> alphas, active, coef_path_lars = lars_path(X, y, method='lasso')
>>> from scipy import interpolate
>>> coef_path_continuous = interpolate.interp1d(alphas[::-1],
...    coef_path_lars[:, ::-1])
>>> print(coef_path_continuous([5., 1., .5]))
[[ 0.        0.        0.46874778]
 [ 0.2159048  0.4425765  0.23689075]]
```

predict (X)

Predict using the linear model

Parameters

- **X** : {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Samples.
Returns C : array, shape = (n_samples,)
    Returns predicted values.

score (X, y, sample_weight=None)
    Returns the coefficient of determination R^2 of the prediction.
    The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred)** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)
    Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
    True values for X.

sample_weight : array-like, shape = [n_samples], optional
    Sample weights.

Returns score : float
    R^2 of self.predict(X) wrt. y.

set_params (**params)
    Set the parameters of this estimator.
    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

    Returns self

Examples using sklearn.linear_model.LassoCV

- Cross-validation on diabetes Dataset Exercise
- Feature selection using SelectFromModel and LassoCV
- Lasso model selection: Cross-Validation / AIC / BIC

sklearn.linear_model.LassoLarsCV

class sklearn.linear_model.LassoLarsCV (fit_intercept=True, verbose=False, max_iter=500, normalize=True, precompute='auto', cv=None, max_n_alphas=1000, n_jobs=1, eps=2.2204460492503131e-16, copy_X=True, positive=False)

Cross-validated Lasso, using the LARS algorithm
The optimization objective for Lasso is:

\[
\frac{1}{2} \left(1 / (2 \times n_{\text{samples}}) \right) \times ||y - Xw||^2_2 + \alpha \times ||w||_1
\]

Read more in the User Guide.

Parameters fit_intercept : boolean
whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**verbose**: boolean or integer, optional

Sets the verbosity amount

**max_iter**: integer, optional

Maximum number of iterations to perform.

**normalize**: boolean, optional, default True

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

**precompute**: True | False | ‘auto’

Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix cannot be passed as argument since we will use only subsets of X.

**cv**: int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

* None, to use the default 3-fold cross-validation,
* integer, to specify the number of folds.
* An object to be used as a cross-validation generator.
* An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**max_n_alphas**: integer, optional

The maximum number of points on the path used to compute the residuals in the cross-validation

**n_jobs**: integer, optional

Number of CPUs to use during the cross validation. If -1, use all the CPUs

**eps**: float, optional

The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.

**copy_X**: boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**positive**: boolean (default=False)

Restrict coefficients to be >= 0. Be aware that you might want to remove fit_intercept which is set True by default. Under the positive restriction the model coefficients do not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha value (alphas_[alphas_ > 0.].min() when fit_path=True) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent Lasso estimator. As a consequence
using LassoLarsCV only makes sense for problems where a sparse solution is expected and/or reached.

Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,)) parameter vector (w in the formulation formula)</td>
</tr>
<tr>
<td>intercept_</td>
<td>(float) independent term in decision function.</td>
</tr>
<tr>
<td>coef_path_</td>
<td>(array, shape (n_features, n_alphas)) the varying values of the coefficients along the path</td>
</tr>
<tr>
<td>alpha_</td>
<td>(float) the estimated regularization parameter alpha</td>
</tr>
<tr>
<td>alphas_</td>
<td>(array, shape (n_alphas,)) the different values of alpha along the path</td>
</tr>
<tr>
<td>cv_alphas_</td>
<td>(array, shape (n_cv_alphas,)) all the values of alpha along the path for the different folds</td>
</tr>
<tr>
<td>mse_path_</td>
<td>(array, shape (n_folds, n_cv_alphas)) the mean square error on left-out for each fold along the path (alpha values given by cv_alphas)</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(array-like or int) the number of iterations run by Lars with the optimal alpha.</td>
</tr>
</tbody>
</table>

See also:

lars_path, LassoLars, LarsCV, LassoCV

Notes

The object solves the same problem as the LassoCV object. However, unlike the LassoCV, it find the relevant alphas values by itself. In general, because of this property, it will be more stable. However, it is more fragile to heavily multicollinear datasets.

It is more efficient than the LassoCV if only a small number of features are selected compared to the total number, for instance if there are very few samples compared to the number of features.

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td>fit(X, y)</td>
<td>Fit the model using X, y as training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(fit_intercept=True, verbose=False, max_iter=500, normalize=True, precompute='auto', cv=None, max_n_alphas=1000, n_jobs=1, eps=2.220446049250313e-16, copy_X=True, positive=False)

alpha

DEPRECATED: Attribute alpha is deprecated in 0.19 and will be removed in 0.21. See alpha_ instead

cv_mse_path_

DEPRECATED: Attribute cv_mse_path_ is deprecated in 0.18 and will be removed in 0.20. Use mse_path_ instead

fit(X, y)

Fit the model using X, y as training data.
Parameters X: array-like, shape (n_samples, n_features)
Training data.

y: array-like, shape (n_samples,)
Target values.

Returns self: object
returns an instance of self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any
Parameter names mapped to their values.

predict (X)
Predict using the linear model

Parameters X: {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.

Returns C: array, shape = (n_samples,)
Returns predicted values.

score (X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.
The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X: array-like, shape = (n_samples, n_features)
Test samples.
y: array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.
sample_weight: array-like, shape = [n_samples], optional
Sample weights.

Returns score: float
R^2 of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self
Examples using `sklearn.linear_model.LassoLarsCV`

- *Lasso model selection: Cross-Validation / AIC / BIC*

`sklearn.linear_model.LogisticRegressionCV`

```python
class sklearn.linear_model.LogisticRegressionCV(Cs=10, fit_intercept=True, cv=None, dual=False, penalty='l2', scoring=None, solver='lbfgs', tol=0.0001, max_iter=100, class_weight=None, n_jobs=1, verbose=0, refit=True, intercept_scaling=1.0, multi_class='ovr', random_state=None)
```

Logistic Regression CV (aka logit, MaxEnt) classifier.

This class implements logistic regression using liblinear, newton-cg, sag of lbfgs optimizer. The newton-cg, sag and lbfgs solvers support only L2 regularization with primal formulation. The liblinear solver supports both L1 and L2 regularization, with a dual formulation only for the L2 penalty.

For the grid of Cs values (that are set by default to be ten values in a logarithmic scale between 1e-4 and 1e4), the best hyperparameter is selected by the cross-validator StratifiedKFold, but it can be changed using the cv parameter. In the case of newton-cg and lbfgs solvers, we warm start along the path i.e guess the initial coefficients of the present fit to be the coefficients got after convergence in the previous fit, so it is supposed to be faster for high-dimensional dense data.

For a multiclass problem, the hyperparameters for each class are computed using the best scores got by doing a one-vs-rest in parallel across all folds and classes. Hence this is not the true multinomial loss.

Read more in the User Guide.

**Parameters**

- **Cs**: list of floats | int

  Each of the values in Cs describes the inverse of regularization strength. If Cs is as an int, then a grid of Cs values are chosen in a logarithmic scale between 1e-4 and 1e4. Like in support vector machines, smaller values specify stronger regularization.

- **fit_intercept**: bool, default: True

  Specifies if a constant (a.k.a. bias or intercept) should be added to the decision function.

- **cv**: integer or cross-validation generator

  The default cross-validation generator used is Stratified K-Folds. If an integer is provided, then it is the number of folds used. See the module `sklearn.model_selection` module for the list of possible cross-validation objects.

- **dual**: bool

  Dual or primal formulation. Dual formulation is only implemented for L2 penalty with liblinear solver. Prefer dual=False when n_samples > n_features.

- **penalty**: str, ‘l1’ or ‘l2’

  Used to specify the norm used in the penalization. The ‘newton-cg’, ‘sag’ and ‘lbfgs’ solvers support only L2 penalties.

- **scoring**: string, callable, or None

  A string (see model evaluation documentation) or a scorer callable object / function with signature `scorer(estimator, X, y)`. For a list of scoring functions that can be used, look at `sklearn.metrics`. The default scoring option used is ‘accuracy’.  

**solver**: `{'newton-cg', 'lbfgs', 'liblinear', 'sag', 'saga'}`, default: 'lbfgs' Algorithm to use in the optimization problem.

- For small datasets, **`liblinear` is a good choice**, whereas **`sag` and `saga`** are faster for large ones.

- For multiclass problems, **only `newton-cg`**, **`sag` and `lbfgs`** handle multinomial loss; **`liblinear`** is limited to one-versus-rest schemes.

- **`newton-cg`**, **`lbfgs` and `sag`** only handle L2 penalty, whereas **`liblinear`** and **`saga`** handle L1 penalty.

- **`liblinear` might be slower in LogisticRegressionCV because it does not** handle warm-starting.

Note that **`sag`** and **`saga`** fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from `sklearn.preprocessing`.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

**tol**: float, optional

Tolerance for stopping criteria.

**max_iter**: int, optional

Maximum number of iterations of the optimization algorithm.

**class_weight**: dict or 'balanced', optional

Weights associated with classes in the form `{class_label: weight}`. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as `n_samples / (n_classes * np.bincount(y))`.

Note that these weights will be multiplied with sample_weight (passed through the fit method) if sample_weight is specified.

New in version 0.17: `class_weight == 'balanced'

**n_jobs**: int, optional

Number of CPU cores used during the cross-validation loop. If given a value of -1, all cores are used.

**verbose**: int

For the `liblinear`, `sag` and `lbfgs` solvers set verbose to any positive number for verbosity.

**refit**: bool

If set to True, the scores are averaged across all folds, and the coefs and the C that corresponds to the best score is taken, and a final refit is done using these parameters. Otherwise the coefs, intercepts and C that correspond to the best scores across folds are averaged.

**intercept_scaling**: float, default 1.
Useful only when the solver ‘liblinear’ is used and self.fit_intercept is set to True. In this case, x becomes [x, self.intercept_scaling], i.e. a “synthetic” feature with constant value equal to intercept_scaling is appended to the instance vector. The intercept becomes intercept_scaling * synthetic_feature_weight.

Note! the synthetic feature weight is subject to l1/l2 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept_scaling has to be increased.

**multi_class** : str, {‘ovr’, ‘multinomial’}

Multiclass option can be either ‘ovr’ or ‘multinomial’. If the option chosen is ‘ovr’, then a binary problem is fit for each label. Else the loss minimised is the multinomial loss fit across the entire probability distribution. Works only for the ‘newton-cg’, ‘sag’, ‘saga’ and ‘lbfgs’ solver.

New in version 0.18: Stochastic Average Gradient descent solver for ‘multinomial’ case.

**random_state** : int, RandomState instance or None, optional, default None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape (1, n_features) or (n_classes, n_features)) Coefficient of the features in the decision function. coef_ is of shape (1, n_features) when the given problem is binary.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape (1,) or (n_classes,)) Intercept (a.k.a. bias) added to the decision function. If fit_intercept is set to False, the intercept is set to zero. intercept_ is of shape(1,) when the problem is binary.</td>
</tr>
<tr>
<td>Cs_</td>
<td>(array) Array of C i.e. inverse of regularization parameter values used for cross-validation.</td>
</tr>
<tr>
<td>coefs_paths</td>
<td>(array, shape (n_folds, len(Cs_), n_features) or (n_folds, len(Cs_), n_features + 1)) dict with classes as the keys, and the path of coefficients obtained during cross-validating across each fold and then across each Cs after doing an OvR for the corresponding class as values. If the ‘multi_class’ option is set to ‘multinomial’, then the coefs_paths are the coefficients corresponding to each class. Each dict value has shape (n_folds, len(Cs_), n_features) or (n_folds, len(Cs_), n_features + 1) depending on whether the intercept is fit or not.</td>
</tr>
<tr>
<td>scores</td>
<td>(dict) dict with classes as the keys, and the values as the grid of scores obtained during cross-validating each fold, after doing an OvR for the corresponding class. If the ‘multi_class’ option given is ‘multinomial’ then the same scores are repeated across all classes, since this is the multinomial class. Each dict value has shape (n_folds, len(Cs))</td>
</tr>
<tr>
<td>C_</td>
<td>(array, shape (n_classes,) or (n_classes - 1,)) Array of C that maps to the best scores across every class. If refit is set to False, then for each class, the best C is the average of the C’s that correspond to the best scores for each fold. C_ is of shape(n_classes,) when the problem is binary.</td>
</tr>
<tr>
<td>n_iter</td>
<td>(array, shape (n_classes, n_folds, n_cs) or (1, n_folds, n_cs)) Actual number of iterations for all classes, folds and Cs. In the binary or multinomial cases, the first dimension is equal to 1.</td>
</tr>
</tbody>
</table>

See also:

* LogisticRegression
### Methods

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
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</thead>
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<td><code>decision_function(X)</code></td>
<td>Predict confidence scores for samples.</td>
</tr>
<tr>
<td><code>densify()</code></td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td><code>fit(X, y, sample_weight)</code></td>
<td>Fit the model according to the given training data.</td>
</tr>
<tr>
<td><code>get_params()</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict class labels for samples in X.</td>
</tr>
<tr>
<td><code>predict_log_proba(X)</code></td>
<td>Log of probability estimates.</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Probability estimates.</td>
</tr>
<tr>
<td><code>score(X, y, sample_weight)</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>sparsify()</code></td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>

### `__init__` Parameters

- `Cs=10`, `fit_intercept=True`, `cv=None`, `dual=False`, `penalty='l2'`, `scoring=None`, `solver='lbfgs'`, `tol=0.0001`, `max_iter=100`, `class_weight=None`, `n_jobs=1`, `verbose=0`, `refit=True`, `intercept_scaling=1.0`, `multi_class='ovr'`, `random_state=None`)

#### `decision_function(X)`

Predict confidence scores for samples.

- **Parameters**
  - `X`: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - `y`: array-like, shape (n_samples,)
  - `sample_weight`: array-like, shape (n_samples,)

- **Returns**
  - array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)

Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

#### `densify()`

Convert coefficient matrix to dense array format.

- **Returns** `self`: estimator

#### `fit(X, y, sample_weight=None)`

Fit the model according to the given training data.

- **Parameters**
  - `X`: {array-like, sparse matrix}, shape (n_samples, n_features)
  - `y`: array-like, shape (n_samples,)
  - `sample_weight`: array-like, shape (n_samples,)

- **Returns** `self`: object
  - Returns `self`
**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**
- **deep** : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params** : mapping of string to any
  Parameter names mapped to their values.

**predict** *(X)*
Predict class labels for samples in X.

**Parameters**
- **X** : {array-like, sparse matrix}, shape = [n_samples, n_features]
  Samples.

**Returns**
- **C** : array, shape = [n_samples]
  Predicted class label per sample.

**predict_log_proba** *(X)*
Log of probability estimates.

The returned estimates for all classes are ordered by the label of classes.

**Parameters**
- **X** : array-like, shape = [n_samples, n_features]

**Returns**
- **T** : array-like, shape = [n_samples, n_classes]
  Returns the log-probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`.

**predict_proba** *(X)*
Probability estimates.

The returned estimates for all classes are ordered by the label of classes.

For a multi_class problem, if `multi_class` is set to be “multinomial” the softmax function is used to find the predicted probability of each class. Else use a one-vs-rest approach, i.e calculate the probability of each class assuming it to be positive using the logistic function. and normalize these values across all the classes.

**Parameters**
- **X** : array-like, shape = [n_samples, n_features]

**Returns**
- **T** : array-like, shape = [n_samples, n_classes]
  Returns the probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`.

**score** *(X, y, sample_weight=None)*
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**
- **X** : array-like, shape = (n_samples, n_features)
  Test samples.
- **y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True labels for X.
- **sample_weight** : array-like, shape = [n_samples], optional
Sample weights.

**Returns** score : float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns** self

**sparsify**()

Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

**Returns** self : estimator

**Notes**

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef_ == 0).sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

**sklearn.linear_model.MultiTaskElasticNetCV**

**class** sklearn.linear_model.**MultiTaskElasticNetCV** (l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, max_iter=1000, tol=0.0001, cv=None, copy_X=True, verbose=0, n_jobs=1, random_state=None, selection='cyclic')

Multi-task L1/L2 ElasticNet with built-in cross-validation.

The optimization objective for MultiTaskElasticNet is:

\[
\frac{1}{2n_samples} \| Y - XW \|^2_F + \alpha (1 - \text{l1\_ratio}) \| W \|^2_F + \alpha \text{l1\_ratio} \| W \|_21
\]

Where:

\[
\| W \|_21 = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the **User Guide**.

**Parameters** l1_ratio : float or array of floats
The ElasticNet mixing parameter, with $0 < \text{l1\_ratio} \leq 1$. For $\text{l1\_ratio} = 1$ the penalty is an L1/L2 penalty. For $\text{l1\_ratio} = 0$ it is an L2 penalty. For $0 < \text{l1\_ratio} < 1$, the penalty is a combination of L1/L2 and L2. This parameter can be a list, in which case the different values are tested by cross-validation and the one giving the best prediction score is used. Note that a good choice of list of values for $\text{l1\_ratio}$ is often to put more values close to 1 (i.e. Lasso) and less close to 0 (i.e. Ridge), as in [.1, .5, .7, .9, .95, .99, 1]

**eps** : float, optional

Length of the path. $\text{eps}=1e^{-3}$ means that $\alpha_{\text{min}} / \alpha_{\text{max}} = 1e^{-3}$.

**n_alphas** : int, optional

Number of alphas along the regularization path

**alphas** : array-like, optional

List of alphas where to compute the models. If not provided, set automatically.

**fit_intercept** : boolean

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**normalize** : boolean, optional, default False

This parameter is ignored when **fit_intercept** is set to False. If True, the regressors $X$ will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use **sklearn.preprocessing.StandardScaler** before calling **fit** on an estimator with **normalize=False**.

**max_iter** : int, optional

The maximum number of iterations

**tol** : float, optional

The tolerance for the optimization: if the updates are smaller than **tol**, the optimization code checks the dual gap for optimality and continues until it is smaller than **tol**.

**cv** : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for **cv** are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, **KFold** is used.

Refer **User Guide** for the various cross-validation strategies that can be used here.

**copy_X** : boolean, optional, default True

If True, $X$ will be copied; else, it may be overwritten.

**verbose** : bool or integer

Amount of verbosity.

**n_jobs** : integer, optional
Number of CPUs to use during the cross validation. If -1, use all the CPUs. Note that this is used only if multiple values for l1_ratio are given.

**random_state** : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’.

**selection** : str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’) often leads to significantly faster convergence especially when tol is higher than 1e-4.

**Attributes**

| intercep_   | (array, shape (n_tasks,)) Independent term in decision function. |
| coef_       | (array, shape (n_tasks, n_features)) Parameter vector (W in the cost function formula). Note that coef_ stores the transpose of W, W.T. |
| alpha_      | (float) The amount of penalization chosen by cross validation |
| mse_path_   | (array, shape (n_alphas, n_folds) or (n_l1_ratio, n_alphas, n_folds)) mean square error for the test set on each fold, varying alpha |
| alphas_     | (numpy array, shape (n_alphas,) or (n_l1_ratio, n_alphas)) The grid of alphas used for fitting, for each l1_ratio |
| l1_ratio_   | (float) best l1_ratio obtained by cross-validation. |
| n_iter_     | (int) number of iterations run by the coordinate descent solver to reach the specified tolerance for the optimal alpha. |

See also:

*MultiTaskElasticNet*, *ElasticNetCV*, *MultiTaskLassoCV*

**Notes**

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

**Examples**

```python
>>> from sklearn import linear_model
>>> clf = linear_model.MultiTaskElasticNetCV()
>>> clf.fit([[0, 0], [1, 1], [2, 2]], ...
... [[0, 0], [1, 1], [2, 2]])
... MultiTaskElasticNetCV(alphas=None, copy_X=True, cv=None, eps=0.001,
... fit_intercept=True, l1_ratio=0.5, max_iter=1000, n_alphas=100,
... n_jobs=1, normalize=False, random_state=None, selection='cyclic',
```
tol=0.0001, verbose=0)

>>> print(clf.coef_)
[[ 0.52875032  0.46958558]
 [ 0.52875032  0.46958558]]

>>> print(clf.intercept_)
[ 0.00166409  0.00166409]

Methods

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<td>path(X, y[, l1_ratio, eps, n_alphas, ...])</td>
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<td>predict(X)</td>
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<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
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</table>

__init__(l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, max_iter=1000, tol=0.0001, cv=None, copy_X=True, verbose=0, n_jobs=1, random_state=None, selection='cyclic')

fit(X, y)
Fit linear model with coordinate descent
Fit is on grid of alphas and best alpha estimated by cross-validation.

Parameters X : [array-like], shape (n_samples, n_features)
Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output, X can be sparse.

y : array-like, shape (n_samples,) or (n_samples, n_targets)
Target values

get_params(deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

static path(X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)
Compute elastic net path with coordinate descent
The elastic net optimization function varies for mono and multi-outputs.
For mono-output tasks it is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \times ||y - Xw||^2_2 \\
+ \alpha \times l1_{\text{ratio}} \times ||w||_1 \\
+ 0.5 \times \alpha \times (1 - l1_{\text{ratio}}) \times ||w||^2_2
\]
For multi-output tasks it is:

\[
\frac{1}{2n_{\text{samples}}} \| Y - XW \|^2_{\text{Fro}} + \alpha \cdot \text{l1_ratio} \cdot \| W \|^2_{21} + 0.5 \cdot \alpha \cdot (1 - \text{l1_ratio}) \cdot \| W \|^2_{\text{Fro}}
\]

Where:

\[
\| W \|^2_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

**Parameters**

- **X**: {array-like}, shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

- **y**: ndarray, shape (n_samples,) or (n_samples, n_outputs)
  Target values

- **l1_ratio**: float, optional
  float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1_ratio=1 corresponds to the Lasso

- **eps**: float
  Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3

- **n_alphas**: int, optional
  Number of alphas along the regularization path

- **alphas**: ndarray, optional
  List of alphas where to compute the models. If None alphas are set automatically

- **precompute**: True | False | ‘auto’ | array-like
  Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix can also be passed as argument.

- **Xy**: array-like, optional
  Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

- **copy_X**: boolean, optional, default True
  If True, X will be copied; else, it may be overwritten.

- **coef_init**: array, shape (n_features,) | None
  The initial values of the coefficients.

- **verbose**: bool or integer
  Amount of verbosity.

- **return_n_iter**: bool
  whether to return the number of iterations or not.

- **positive**: bool, default False

---

3.3. Model selection and evaluation
If set to True, forces coefficients to be positive. (Only allowed when \( y \).ndim == 1).

**check_input** : bool, default True
Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params** : kwargs
keyword arguments passed to the coordinate descent solver.

Returns

**alphas** : array, shape (n_alphas,)
The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)
Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)
The dual gaps at the end of the optimization for each alpha.

**n_iters** : array-like, shape (n_alphas,)
The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

See also:

`MultiTaskElasticNet`, `MultiTaskElasticNetCV`, `ElasticNet`, `ElasticNetCV`

Notes

For an example, see `examples/linear_model/plot_lasso_coordinate_descent_path.py`.

**predict** \((X)\)
Predict using the linear model

**Parameters**

**X** : {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.

**Returns**

**C** : array, shape = (n_samples,)
Returns predicted values.

**score** \((X, y, sample_weight=None)\)
Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \( 1 - \frac{u}{v} \), where \( u \) is the residual sum of squares \( \sum \left( (y_{true} - y_{pred})^2 \right) \) and \( v \) is the total sum of squares \( \sum \left( (y_{true} - \text{mean}(y))^2 \right) \). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

**Parameters**

**X** : array-like, shape = (n_samples, n_features)
Test samples.

**y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for \( X \).

**sample_weight** : array-like, shape = [n_samples], optional
Sample weights.
Returns score : float

R^2 of self.predict(X) wrt. y.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

sklearn.linear_model.MultiTaskLassoCV

class sklearn.linear_model.MultiTaskLassoCV (eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, max_iter=1000, tol=0.0001, copy_X=True, cv=None, verbose=False, n_jobs=1, random_state=None, selection='cyclic')

Multi-task L1/L2 Lasso with built-in cross-validation.

The optimization objective for MultiTaskLasso is:

\[
\frac{1}{2} \|Y - XW\|_Fro^2 + \alpha \|W\|_{21}
\]

Where:

\[
\|W\|_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters eps : float, optional

Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3.

n_alphas : int, optional

Number of alphas along the regularization path

alphas : array-like, optional

List of alphas where to compute the models. If not provided, set automatically.

fit_intercept : boolean

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

max_iter : int, optional

The maximum number of iterations.

tol : float, optional
The tolerance for the optimization: if the updates are smaller than $\text{tol}$, the optimization code checks the dual gap for optimality and continues until it is smaller than $\text{tol}$.

**copy_X**: boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**cv**: int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**verbose**: bool or integer

Amount of verbosity.

**n_jobs**: integer, optional

Number of CPUs to use during the cross validation. If -1, use all the CPUs. Note that this is used only if multiple values for l1_ratio are given.

**random_state**: int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’

**selection**: str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’`) often leads to significantly faster convergence especially when tol is higher than 1e-4.

### Attributes

| **intercept_** | (array, shape (n_tasks,)) Independent term in decision function. |
| **coef_**      | (array, shape (n_tasks, n_features)) Parameter vector (W in the cost function formula). Note that coef_ stores the transpose of $W$, $W^T$. |
| **alpha_**     | (float) The amount of penalization chosen by cross validation |
| **mse_path_**  | (array, shape (n_alphas, n_folds)) mean square error for the test set on each fold, varying alpha |
| **alphas_**    | (numpy array, shape (n_alphas,)) The grid of alphas used for fitting. |
| **n_iter_**    | (int) number of iterations run by the coordinate descent solver to reach the specified tolerance for the optimal alpha. |

See also: MultiTaskElasticNet, ElasticNetCV, MultiTaskElasticNetCV
Notes

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Methods

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<td>fit(X, y)</td>
<td>Fit linear model with coordinate descent</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>path(X, y[, eps, n_alphas, alphas, ...])</td>
<td>Compute Lasso path with coordinate descent</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(eps=0.001, n_alphas=100, alphas=None, fit_intercept=True, normalize=False, max_iter=1000, tol=0.0001, copy_X=True, cv=None, verbose=False, n_jobs=1, random_state=None, selection='cyclic')

fit (X, y)
Fit linear model with coordinate descent

Fit is on grid of alphas and best alpha estimated by cross-validation.

Parameters
- **X** : array-like, shape (n_samples, n_features)
  - Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output, X can be sparse.
- **y** : array-like, shape (n_samples,) or (n_samples, n_targets)
  - Target values

get_params (deep=True)
Get parameters for this estimator.

Parameters
- **deep** : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns
- **params** : mapping of string to any
  - Parameter names mapped to their values.

static path (X, y, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, **params)
Compute Lasso path with coordinate descent

The Lasso optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \times ||y - Xw||^2_2 + \alpha \times ||w||_1
\]

For multi-output tasks it is:
Where:

\[ ||W||_{21} = \sum_i \sqrt{\sum_j w_{ij}^2} \]

i.e. the sum of norm of each row.

Read more in the *User Guide*.

**Parameters**

- **X**: array-like, sparse matrix, shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If `y` is mono-output then `X` can be sparse.

- **y**: ndarray, shape (n_samples, ), or (n_samples, n_outputs)
  Target values

- **eps**: float, optional
  Length of the path. `eps=1e-3` means that `alpha_min / alpha_max = 1e-3`

- **n_alphas**: int, optional
  Number of alphas along the regularization path

- **alphas**: ndarray, optional
  List of alphas where to compute the models. If `None` alphas are set automatically

- **precompute**: True | False | `auto` | array-like
  Whether to use a precomputed Gram matrix to speed up calculations. If set to `auto` let us decide. The Gram matrix can also be passed as argument.

- **Xy**: array-like, optional
  `Xy = np.dot(X.T, y)` that can be precomputed. It is useful only when the Gram matrix is precomputed.

- **copy_X**: boolean, optional, default True
  If `True`, `X` will be copied; else, it may be overwritten.

- **coef_init**: array, shape (n_features, ) | None
  The initial values of the coefficients.

- **verbose**: bool or integer
  Amount of verbosity.

- **return_n_iter**: bool
  Whether to return the number of iterations or not.

- **positive**: bool, default False
  If set to `True`, forces coefficients to be positive. (Only allowed when `y.ndim == 1`).

- **params**: kwags
  Keyword arguments passed to the coordinate descent solver.

**Returns**

- **alphas**: array, shape (n_alphas,)
  The alphas along the path where models are computed.
coefs : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

dual_gaps : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

n_iters : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified
tolerance for each alpha.

See also:

lars_path, Lasso, LassoLars, LassoCV, LassoLarsCV, sklearn.decomposition.
sparse_encode

Notes

For an example, see examples/linear_model/plot_lasso_coordinate_descent_path.py.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a
Fortran-contiguous numpy array.

Note that in certain cases, the Lars solver may be significantly faster to implement this functionality. In
particular, linear interpolation can be used to retrieve model coefficients between the values output by
lars_path

Examples

Comparing lasso_path and lars_path with interpolation:

```python
>>> X = np.array([[1, 2, 3.1], [2.3, 5.4, 4.3]]).T
>>> y = np.array([1, 2, 3.1])
>>> # Use lasso_path to compute a coefficient path
>>> _, coef_path, _ = lasso_path(X, y, alphas=[5., 1., .5])
>>> print(coef_path)
[[ 0.  0.  0.46874778]
 [ 0.2159048 0.4425765 0.23689075]]

>>> # Now use lars_path and 1D linear interpolation to compute the
>>> # same path
>>> from sklearn.linear_model import lars_path
>>> alphas, active, coef_path_lars = lars_path(X, y, method='lasso')
>>> from scipy import interpolate
>>> coef_path_continuous = interpolate.interp1d(alphas[::-1],
...     coef_path_lars[:, ::-1])
>>> print(coef_path_continuous([5., 1., .5]))
[[ 0.  0.  0.46874778]
 [ 0.2159048 0.4425765 0.23689075]]

predict (X)

Predict using the linear model

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.
Returns C: array, shape = (n_samples,)

Returns predicted values.

score (X, y, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred}) ** 2).sum()$ and $v$ is the total sum of squares $((y_{true} - y_{true.mean()}) ** 2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

Parameters X: array-like, shape = (n_samples, n_features)

Test samples.

y: array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight: array-like, shape = [n_samples], optional

Sample weights.

Returns score: float

$R^2$ of self.predict(X) wrt. y.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

sklearn.linear_model.OrthogonalMatchingPursuitCV

class sklearn.linear_model.OrthogonalMatchingPursuitCV (copy=True, fit_intercept=True, normalize=True, max_iter=None, cv=None, n_jobs=1, verbose=False)

Cross-validated Orthogonal Matching Pursuit model (OMP)

Read more in the User Guide.

Parameters copy: bool, optional

Whether the design matrix $X$ must be copied by the algorithm. A false value is only helpful if $X$ is already Fortran-ordered, otherwise a copy is made anyway.

fit_intercept: boolean, optional

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize: boolean, optional, default True

This parameter is ignored when fit_intercept is set to False. If True, the regressors $X$ will be normalized before regression by subtracting the mean and dividing by the 2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.
**max_iter** : integer, optional

Maximum numbers of iterations to perform, therefore maximum features to include. 10% of n_features but at least 5 if available.

**cv** : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**n_jobs** : integer, optional

Number of CPUs to use during the cross validation. If -1, use all the CPUs

**verbose** : boolean or integer, optional

Sets the verbosity amount

### Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(float or array, shape (n_targets,)) Independent term in decision function.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,) or (n_targets, n_features)) Parameter vector (w in the problem formulation).</td>
</tr>
<tr>
<td>n_nonzero_coefs_</td>
<td>Estimated number of non-zero coefficients giving the best mean squared error over the cross-validation folds.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int or array-like) Number of active features across every target for the model refit with the best hyperparameters got by cross-validating across all folds.</td>
</tr>
</tbody>
</table>

#### See also:

- orthogonal_mp, orthogonal_mp_gram, lars_path, Lars, LassoLars, OrthogonalMatchingPursuit, LarsCV, LassoLarsCV, decomposition.sparse_encode

### Methods

- **fit**(X, y) Fit the model using X, y as training data.
- **get_params**([deep]) Get parameters for this estimator.
- **predict**(X) Predict using the linear model
- **score**(X, y[, sample_weight]) Returns the coefficient of determination R^2 of the prediction.
- **set_params**(**params) Set the parameters of this estimator.

```python
__init__(copy=True, fit_intercept=True, normalize=True, max_iter=None, cv=None, n_jobs=1, verbose=False)

fit (X, y)
```

---

3.3. Model selection and evaluation
Fit the model using $X$, $y$ as training data.

**Parameters**

$X$ : array-like, shape [n_samples, n_features]

Training data.

$y$ : array-like, shape [n_samples]

Target values. Will be cast to $X$’s dtype if necessary

**Returns**

self : object

returns an instance of self.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

depth : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

params : mapping of string to any

Parameter names mapped to their values.

**predict**(X)

Predict using the linear model

**Parameters**

$X$ : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

**Returns**

$C$ : array, shape = (n_samples,)

Returns predicted values.

**score**(X, y, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares ($(y_{true} - y_{pred})**2).sum()$ and $v$ is the total sum of squares ($(y_{true} - y_{true.mean()})**2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

$X$ : array-like, shape = (n_samples, n_features)

Test samples.

$y$ : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for $X$.

**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.

**Returns**

score : float

$R^2$ of self.predict(X) wrt. $y$.

**set_params**(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.
Returns self

Examples using sklearn.linear_model.OrthogonalMatchingPursuitCV

- Orthogonal Matching Pursuit

sklearn.linear_model.RidgeCV

class sklearn.linear_model.RidgeCV(alphas=(0.1, 1.0, 10.0), fit_intercept=True, normalize=False, scoring=None, cv=None, gcv_mode=None, store_cv_values=False)

Ridge regression with built-in cross-validation.

By default, it performs Generalized Cross-Validation, which is a form of efficient Leave-One-Out cross-validation.

Read more in the User Guide.

Parameters

alphas : numpy array of shape [n_alphas]

Array of alpha values to try. Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to $C^{-1}$ in other linear models such as LogisticRegression or LinearSVC.

fit_intercept : boolean

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

scoring : string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the efficient Leave-One-Out cross-validation
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if y is binary or multiclass, sklearn.model_selection.StratifiedKFold is used, else, sklearn.model_selection.KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

gcv_mode : {None, ‘auto’, ‘svd’, ‘eigen’}, optional
Flag indicating which strategy to use when performing Generalized Cross-Validation. Options are:

- `'auto'`: use svd if n_samples > n_features or when X is a sparse matrix, otherwise use eigen
- `'svd'`: force computation via singular value decomposition of X (does not work for sparse matrices)
- `'eigen'`: force computation via eigendecomposition of $X^T X$

The ‘auto’ mode is the default and is intended to pick the cheaper option of the two depending upon the shape and format of the training data.

**store_cv_values**: boolean, default=False

Flag indicating if the cross-validation values corresponding to each alpha should be stored in the `cv_values_` attribute (see below). This flag is only compatible with `cv=None` (i.e. using Generalized Cross-Validation).

**Attributes**

- `cv_values_`: array, shape = [n_samples, n_alphas] or shape = [n_samples, n_targets, n_alphas], optional) Cross-validation values for each alpha (if `store_cv_values=True` and `cv=None`). After `fit()` has been called, this attribute will contain the mean squared errors (by default) or the values of the `{loss,score}_func` function (if provided in the constructor).
- `coef_`: (array, shape = [n_features] or [n_targets, n_features]) Weight vector(s).
- `intercept_`: (float | array, shape = (n_targets,)) Independent term in decision function. Set to 0.0 if `fit_intercept = False`.
- `alpha_`: (float) Estimated regularization parameter.

**See also:**

- **Ridge** Ridge regression
- **RidgeClassifier** Ridge classifier
- **RidgeClassifierCV** Ridge classifier with built-in cross validation

**Methods**

- `fit(X, y[, sample_weight])`: Fit Ridge regression model
- `get_params([deep])`: Get parameters for this estimator.
- `predict(X)`: Predict using the linear model
- `score(X, y[, sample_weight])`: Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)`: Set the parameters of this estimator.

```
__init__(alphas=(0.1, 1.0, 10.0), fit_intercept=True, normalize=False, scoring=None, cv=None, gcv_mode=None, store_cv_values=False)

fit (X, y, sample_weight=None)
```

Fit Ridge regression model
Parameters $\mathbf{X}$: array-like, shape $= [n_{\text{samples}}, n_{\text{features}}]$

Training data

$\mathbf{y}$: array-like, shape $= [n_{\text{samples}}]$ or $[n_{\text{samples}}, n_{\text{targets}}]$

Target values. Will be cast to $\mathbf{X}$’s dtype if necessary

sample_weight: float or array-like of shape $[n_{\text{samples}}]$

Sample weight

Returns self: Returns self.

get_params($deep=True$)

Get parameters for this estimator.

Parameters deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any

Parameter names mapped to their values.

predict($\mathbf{X}$)

Predict using the linear model

Parameters $\mathbf{X}$: {array-like, sparse matrix}, shape $= (n_{\text{samples}}, n_{\text{features}})$

Samples.

Returns $\mathbf{C}$: array, shape $= (n_{\text{samples}},)$

Returns predicted values.

score($\mathbf{X}, \mathbf{y}$, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $\sum ((\mathbf{y}_{\text{true}} - \mathbf{y}_{\text{pred}})^2)$ and $v$ is the total sum of squares $\sum ((\mathbf{y}_{\text{true}} - \mathbf{y}_{\text{true}}.\text{mean})^2)$.

The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $\mathbf{y}$, disregarding the input features, would get a $R^2$ score of 0.0.

Parameters $\mathbf{X}$: array-like, shape $= (n_{\text{samples}}, n_{\text{features}})$

Test samples.

$\mathbf{y}$: array-like, shape $= (n_{\text{samples}})$ or $= (n_{\text{samples}}, n_{\text{outputs}})$

True values for $\mathbf{X}$.

sample_weight: array-like, shape $= [n_{\text{samples}}]$, optional

Sample weights.

Returns score: float

$R^2$ of self.predict($\mathbf{X}$) wrt. $\mathbf{y}$.

set_params($**\text{params}$)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form $<\text{component}>__<\text{parameter}>$ so that it’s possible to update each component of a nested object.

3.3. Model selection and evaluation 429
Returns  self

Examples using sklearn.linear_model.RidgeCV

- Face completion with a multi-output estimators

sklearn.linear_model.RidgeClassifierCV

class sklearn.linear_model.RidgeClassifierCV(alphas=(0.1, 1.0, 10.0), fit_intercept=True, normalize=False, scoring=None, cv=None, class_weight=None)

Ridge classifier with built-in cross-validation.

By default, it performs Generalized Cross-Validation, which is a form of efficient Leave-One-Out cross-validation. Currently, only the n_features > n_samples case is handled efficiently.

Read more in the User Guide.

Parameters  alphas : numpy array of shape [n_alphas]

Array of alpha values to try. Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to $C^{-1}$ in other linear models such as LogisticRegression or LinearSVC.

fit_intercept : boolean

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

scoring : string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the efficient Leave-One-Out cross-validation
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

Refer User Guide for the various cross-validation strategies that can be used here.

class_weight : dict or ‘balanced’, optional

Weights associated with classes in the form {class_label: weight}. If not given, all classes are supposed to have weight one.
The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as

\[ n_{\text{samples}} / (n_{\text{classes}} \times \text{np.bincount}(y)) \]

Attributes

| cv_values_         | (array, shape = [n_samples, n_alphas] or shape = [n_samples, n_responses, n_alphas], optional) Cross-validation values for each alpha (if store_cv_values=True and
|                   | ‘cv=None’). After ‘fit()’ has been called, this attribute will contain the mean squared errors (by default) or
|                   | the values of the ‘{loss,score}_func’ function (if provided in the constructor).
| coef_             | (array, shape = [n_features] or [n_targets, n_features]) Weight vector(s).
| intercept_        | (float | array, shape = (n_targets,)) Independent term in decision function. Set to 0.0 if fit_intercept = False.
| alpha_            | (float) Estimated regularization parameter

See also:

*Ridge* Ridge regression

*RidgeClassifier* Ridge classifier

*RidgeCV* Ridge regression with built-in cross validation

Notes

For multi-class classification, n_class classifiers are trained in a one-versus-all approach. Concretely, this is implemented by taking advantage of the multi-variate response support in Ridge.

Methods

| decision_function(X) | Predict confidence scores for samples.
| fit(X, y[, sample_weight]) | Fit the ridge classifier.
| get_params([deep]) | Get parameters for this estimator.
| predict(X) | Predict class labels for samples in X.
| score(X, y[, sample_weight]) | Returns the mean accuracy on the given test data and labels.
| set_params(**params) | Set the parameters of this estimator.

__init__(alphas=(0.1, 1.0, 10.0), fit_intercept=True, normalize=False, scoring=None, cv=None, class_weight=None)

decision_function(X)

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.
Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)
    Samples.

Returns array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
    Confidence scores per (sample, class) combination. In the binary case, confidence score
    for self.classes_[1] where >0 means this class would be predicted.

fit (X, y, sample_weight=None)
    Fit the ridge classifier.

    Parameters X : array-like, shape (n_samples, n_features)
        Training vectors, where n_samples is the number of samples and n_features is the num-
        ber of features.
    y : array-like, shape (n_samples,)
        Target values. Will be cast to X's dtype if necessary
    sample_weight : float or numpy array of shape (n_samples,)
        Sample weight.

Returns self : object
    Returns self.

get_params (deep=True)
    Get parameters for this estimator.

    Parameters deep : boolean, optional
        If True, will return the parameters for this estimator and contained subobjects that are
        estimators.

Returns params : mapping of string to any
    Parameter names mapped to their values.

predict (X)
    Predict class labels for samples in X.

    Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
        Samples.

Returns C : array, shape = [n_samples]
    Predicted class label per sample.

score (X, y, sample_weight=None)
    Returns the mean accuracy on the given test data and labels.

    In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each
    sample that each label set be correctly predicted.

    Parameters X : array-like, shape = (n_samples, n_features)
        Test samples.
    y : array-like, shape = (n_samples) or (n_samples, n_outputs)
        True labels for X.
    sample_weight : array-like, shape = [n_samples], optional
        Sample weights.
Returns score : float

Mean accuracy of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

Information Criterion

Some models can offer an information-theoretic closed-form formula of the optimal estimate of the regularization parameter by computing a single regularization path (instead of several when using cross-validation).

Here is the list of models benefiting from the Akaike Information Criterion (AIC) or the Bayesian Information Criterion (BIC) for automated model selection:

<table>
<thead>
<tr>
<th>linear_model.LassoLarsIC([criterion, ...])</th>
<th>Lasso model fit with Lars using BIC or AIC for model selection</th>
</tr>
</thead>
</table>

sklearn.linear_model.LassoLarsIC

class sklearn.linear_model.LassoLarsIC (criterion='aic', fit_intercept=True, verbose=False, normalize=True, precompute='auto', max_iter=500, eps=2.2204460492503131e-16, copy_X=True, positive=False)

Lasso model fit with Lars using BIC or AIC for model selection

The optimization objective for Lasso is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \times ||y - Xw||^2_2 + \alpha \times ||w||_1
\]

AIC is the Akaike information criterion and BIC is the Bayes Information criterion. Such criteria are useful to select the value of the regularization parameter by making a trade-off between the goodness of fit and the complexity of the model. A good model should explain well the data while being simple.

Read more in the User Guide.

Parameters criterion : ‘bic’ | ‘aic’

The type of criterion to use.

fit_intercept : boolean

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

verbose : boolean or integer, optional

Sets the verbosity amount

normalize : boolean, optional, default True

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by
the l2-norm. If you wish to standardize, please use `sklearn.preprocessing.StandardScaler` before calling `fit` on an estimator with `normalize=False`.

**precompute**: True | False | ’auto’ | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to ’auto’, let us decide. The Gram matrix can also be passed as argument.

**max_iter**: integer, optional

Maximum number of iterations to perform. Can be used for early stopping.

**eps**: float, optional

The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the `tol` parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.

**copy_X**: boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**positive**: boolean (default=False)

Restrict coefficients to be >= 0. Be aware that you might want to remove `fit_intercept` which is set True by default. Under the positive restriction the model coefficients do not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha value (`alphas_[alphas_ > 0.].min()` when `fit_path=True`) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent Lasso estimator. As a consequence using LassoLarsIC only makes sense for problems where a sparse solution is expected and/or reached.

**Attributes**

| coef_  | (array, shape (n_features,)) parameter vector (w in the formulation formula) |
| intercep_ | (float) independent term in decision function. |
| alpha_ | (float) the alpha parameter chosen by the information criterion |
| n_iter_ | (int) number of iterations run by `lars_path` to find the grid of alphas. |
| criterion_ | (array, shape (n_alphas,)) The value of the information criteria (’aic’, ’bic’) across all alphas. The alpha which has the smallest information criterion is chosen. This value is larger by a factor of `n_samples` compared to Eqns. 2.15 and 2.16 in (Zou et al, 2007). |

**See also:**

`lars_path`, `LassoLars`, `LassoLarsCV`

**Notes**

The estimation of the number of degrees of freedom is given by:

Examples

```python
>>> from sklearn import linear_model
>>> reg = linear_model.LassoLarsIC(criterion='bic')
>>> reg.fit([[-1, 1], [0, 0], [1, 1]], [-1.1111, 0, -1.1111])
...
LassoLarsIC(copy_X=True, criterion='bic', eps=..., fit_intercept=True,
          max_iter=500, normalize=True, positive=False, precompute='auto',
          verbose=False)
>>> print(reg.coef_)
[ 0. -1.11...]
```

Methods

```python
fit(X, y[, copy_X])
Get parameters for this estimator.
fit_intercept=True, verbose=False, normalize=True, precompute='auto',
max_iter=500, eps=2.2204460492503131e-16, copy_X=True, positive=False)

fit (X, y, copy_X=True)
Fit the model using X, y as training data.
```

Parameters

- **X**: array-like, shape (n_samples, n_features)
  training data.
- **y**: array-like, shape (n_samples,)
  target values. Will be cast to X’s dtype if necessary
- **copy_X**: boolean, optional, default True
  If True, X will be copied; else, it may be overwritten.

Returns

- **self**: object
  returns an instance of self.

get_params (deep=True)
Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  Parameter names mapped to their values.
**predict** (*X*)

Predict using the linear model

**Parameters**

* X : {array-like, sparse matrix}, shape = (n_samples, n_features)
  Samples.

**Returns**

* C : array, shape = (n_samples,)
  Returns predicted values.

**score** (*X*, *y*, *sample_weight=None*)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares ($(y_{true} - y_{pred})^2$).sum() and $v$ is the total sum of squares ($(y_{true} - y_{true}.mean())^2$).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

* X : array-like, shape = (n_samples, n_features)
  Test samples.

* y : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.

* sample_weight : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

* score : float
  $R^2$ of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

* self

**Examples using sklearn.linear_model.LassoLarsIC**

- **Lasso model selection:** Cross-Validation / AIC / BIC

**Out of Bag Estimates**

When using ensemble methods base upon bagging, i.e. generating new training sets using sampling with replacement, part of the training set remains unused. For each classifier in the ensemble, a different part of the training set is left out.

This left out portion can be used to estimate the generalization error without having to rely on a separate validation set. This estimate comes “for free” as no additional data is needed and can be used for model selection.

This is currently implemented in the following classes:

| ensemble.RandomForestClassifier([...]) | A random forest classifier. |
A random forest classifier.

A random forest is a meta estimator that fits a number of decision tree classifiers on various sub-samples of the dataset and use averaging to improve the predictive accuracy and control over-fitting. The sub-sample size is always the same as the original input sample size but the samples are drawn with replacement if `bootstrap=True` (default).

Read more in the User Guide.

**Parameters**

**n_estimators** : integer, optional (default=10)

The number of trees in the forest.

**criterion** : string, optional (default="gini")

The function to measure the quality of a split. Supported criteria are “gini” for the Gini impurity and “entropy” for the information gain. Note: this parameter is tree-specific.

**max_features** : int, float, string or None, optional (default="auto")

The number of features to consider when looking for the best split:

- If int, then consider `max_features` features at each split.
- If float, then `max_features` is a percentage and `int(max_features * n_features)` features are considered at each split.
- If “auto”, then `max_features=sqrt(n_features)`.
- If “sqrt”, then `max_features=sqrt(n_features)` (same as “auto”).
- If “log2”, then `max_features=log2(n_features)`.
- If None, then `max_features=n_features`.  

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**Table 3.15 – continued from previous page**

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>ensemble.RandomForestRegressor(...)</code></td>
<td>A random forest regressor.</td>
</tr>
<tr>
<td><code>ensemble.ExtraTreesClassifier(...)</code></td>
<td>An extra-trees classifier.</td>
</tr>
<tr>
<td><code>ensemble.GradientBoostingClassifier([loss, ...])</code></td>
<td>Gradient Boosting for classification.</td>
</tr>
<tr>
<td><code>ensemble.GradientBoostingRegressor([loss, ...])</code></td>
<td>Gradient Boosting for regression.</td>
</tr>
</tbody>
</table>

**sklearn.ensemble.RandomForestClassifier**

```python
class sklearn.ensemble.RandomForestClassifier(n_estimators=10, criterion='gini', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None, verbose=0, warm_start=False, class_weight=None)
```

...
Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than `max_features` features.

**max_depth**: integer or None, optional (default=None)

The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than `min_samples_split` samples.

**min_samples_split**: int, float, optional (default=2)

The minimum number of samples required to split an internal node:

- If int, then consider `min_samples_split` as the minimum number.
- If float, then `min_samples_split` is a percentage and `cei(min_samples_split * n_samples)` are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider `min_samples_leaf` as the minimum number.
- If float, then `min_samples_leaf` is a percentage and `cei(min_samples_leaf * n_samples)` are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when `sample_weight` is not provided.

**max_leaf_nodes**: int or None, optional (default=None)

Grow trees with `max_leaf_nodes` in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: `min_impurity_split` has been deprecated in favor of `min_impurity_decrease` in 0.19 and will be removed in 0.21. Use `min_impurity_decrease` instead.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_t}{N} \times (\text{impurity} - \frac{N_{t\_R}}{N_t} \times \text{right\_impurity} - \frac{N_{t\_L}}{N_t} \times \text{left\_impurity})
\]

where \(N\) is the total number of samples, \(N_{t}\) is the number of samples at the current node, \(N_{t\_L}\) is the number of samples in the left child, and \(N_{t\_R}\) is the number of samples in the right child.
N, N_t, N_t_R and N_t_L all refer to the weighted sum, if `sample_weight` is passed.

New in version 0.19.

**bootstrap**: boolean, optional (default=True)

Whether bootstrap samples are used when building trees.

**oob_score**: bool (default=False)

Whether to use out-of-bag samples to estimate the generalization accuracy.

**n_jobs**: integer, optional (default=1)

The number of jobs to run in parallel for both `fit` and `predict`. If -1, then the number of jobs is set to the number of cores.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**verbose**: int, optional (default=0)

Controls the verbosity of the tree building process.

**warm_start**: bool, optional (default=False)

When set to `True`, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest.

**class_weight**: dict, list of dicts, “balanced”,

“balanced_subsample” or None, optional (default=None) Weights associated with classes in the form `{class_label: weight}`. If not given, all classes are supposed to have weight one. For multi-output problems, a list of dicts can be provided in the same order as the columns of y.

Note that for multioutput (including multilabel) weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be `[[0: 1, 1: 1], [0: 1, 1: 5], [0: 1, 1: 1], [0: 1, 1: 1]]` instead of `[[1:1], [2:5], [3:1], [4:1]]`.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as `n_samples / (n_classes * np.bincount(y))`

The “balanced_subsample” mode is the same as “balanced” except that weights are computed based on the bootstrap sample for every tree grown.

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with `sample_weight` (passed through the fit method) if `sample_weight` is specified.

**Attributes**

| `feature_importances_` | Return the feature importances (the higher, the more important the feature). |

---

3.3. Model selection and evaluation 439
estimators_ (list of DecisionTreeClassifier) The collection of fitted sub-estimators.

classes_ (array of shape = [n_classes] or a list of such arrays) The classes labels (single output problem), or a list of arrays of class labels (multi-output problem).
n_classes_ (int or list) The number of classes (single output problem), or a list containing the number of classes for each output (multi-output problem).
n_features_ (int) The number of features when fit is performed.
n_outputs_ (int) The number of outputs when fit is performed.
oob_score_ (float) Score of the training dataset obtained using an out-of-bag estimate.
oob_decision_function_ (array of shape = [n_samples, n_classes]) Decision function computed with out-of-bag estimate on the training set. If n_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob_decision_function_ might contain NaN.

See also:
DecisionTreeClassifier, ExtraTreesClassifier

Notes

The default values for the parameters controlling the size of the trees (e.g. max_depth, min_samples_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data, max_features=n_features and bootstrap=False, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random_state has to be fixed.

References

[R8181]

Examples

```python
>>> from sklearn.ensemble import RandomForestClassifier
>>> from sklearn.datasets import make_classification

>>> X, y = make_classification(n_samples=1000, n_features=4,...
... n_informative=2, n_redundant=0,...
... random_state=0, shuffle=False)

>>> clf = RandomForestClassifier(max_depth=2, random_state=0)
>>> clf.fit(X, y)
RandomForestClassifier(bootstrap=True, class_weight=None, criterion='gini',
    max_depth=2, max_features='auto', max_leaf_nodes=None,
    min_impurity_decrease=0.0, min_impurity_split=None,
    min_samples_leaf=1, min_samples_split=2,
    min_weight_fraction_leaf=0.0, n_estimators=10, n_jobs=1,
    oob_score=False, random_state=0, verbose=0, warm_start=False)

>>> print(clf.feature_importances_)
[ 0.17287856 0.80608704 0.01884792 0.00218648]
```
```python
>>> print(clf.predict([[0, 0, 0, 0]]))
[1]
```

## Methods

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<td>Set the parameters of this estimator.</td>
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### `__init__` Parameters:
- `n_estimators=10`  
- `criterion='gini'` 
- `max_depth=None` 
- `min_samples_split=2` 
- `min_samples_leaf=1` 
- `min_weight_fraction_leaf=0.0` 
- `max_features='auto'` 
- `max_leaf_nodes=None` 
- `min_impurity_decrease=0.0` 
- `min_impurity_split=None` 
- `bootstrap=True` 
- `oob_score=False` 
- `n_jobs=1` 
- `random_state=None` 
- `verbose=0` 
- `warm_start=False` 
- `class_weight=None`

#### `apply(X)`
Apply trees in the forest to X, return leaf indices.

**Parameters**
- **X**: array-like or sparse matrix, shape = [n_samples, n_features]

  The input samples. Internally, its dtype will be converted to `dtype=np.float32`. If a sparse matrix is provided, it will be converted into a sparse `csr_matrix`.

**Returns**
- **X_leaves**: array_like, shape = [n_samples, n_estimators]

  For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.

#### `decision_path(X)`
Return the decision path in the forest

New in version 0.18.

**Parameters**
- **X**: array-like or sparse matrix, shape = [n_samples, n_features]

  The input samples. Internally, its dtype will be converted to `dtype=np.float32`. If a sparse matrix is provided, it will be converted into a sparse `csr_matrix`.

**Returns**
- **indicator**: sparse csr array, shape = [n_samples, n_nodes]

  Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

- **n_nodes_ptr**: array of size (n_estimators + 1, )

  The columns from indicator[n_nodes_ptr[i]:n_nodes_ptr[i+1]] gives the indicator value for the i-th estimator.

#### `feature_importances_`
Return the feature importances (the higher, the more important the feature).

---

3.3. Model selection and evaluation 441
Returns **feature_importances_**: array, shape = [n_features]

**fit** (*X, y, sample_weight=None*)
Build a forest of trees from the training set (*X, y*).

**Parameters**

- **X**: array-like or sparse matrix of shape = [n_samples, n_features]
  - The training input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csc_matrix.

- **y**: array-like, shape = [n_samples] or [n_samples, n_outputs]
  - The target values (class labels in classification, real numbers in regression).

- **sample_weight**: array-like, shape = [n_samples] or None
  - Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

**Returns** **self**: object

**get_params** (*deep=True*)
Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** **params**: mapping of string to any

Parameter names mapped to their values.

**predict** (*X*)
Predict class for *X*.

The predicted class of an input sample is a vote by the trees in the forest, weighted by their probability estimates. That is, the predicted class is the one with highest mean probability estimate across the trees.

**Parameters**

- **X**: array-like or sparse matrix of shape = [n_samples, n_features]
  - The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns** **y**: array of shape = [n_samples] or [n_samples, n_outputs]

The predicted classes.

**predict_log_proba** (*X*)
Predict class log-probabilities for *X*.

The predicted class log-probabilities of an input sample is computed as the log of the mean predicted class probabilities of the trees in the forest.

**Parameters**

- **X**: array-like or sparse matrix of shape = [n_samples, n_features]
  - The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns** **p**: array of shape = [n_samples, n_classes], or a list of n_outputs
such arrays if n_outputs > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**predict_proba** (*X*)

Predict class probabilities for X.

The predicted class probabilities of an input sample are computed as the mean predicted class probabilities of the trees in the forest. The class probability of a single tree is the fraction of samples of the same class in a leaf.

**Parameters**

- **X**: array-like or sparse matrix of shape [n_samples, n_features]
  - The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns**

- **p**: array of shape [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**score** (*X*, *y*, *sample_weight=None*)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**

- **score**: float
  - Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

**Returns**

- **self**

**Examples using sklearn.ensemble.RandomForestClassifier**

- *Comparison of Calibration of Classifiers*
- *Probability Calibration for 3-class classification*
- *Classifier comparison*
- *Plot class probabilities calculated by the VotingClassifier*
- *OOB Errors for Random Forests*
- *Feature transformations with ensembles of trees*
• Plot the decision surfaces of ensembles of trees on the iris dataset
• Comparing randomized search and grid search for hyperparameter estimation
• Classification of text documents using sparse features

sklearn.ensemble.RandomForestRegressor

class sklearn.ensemble.RandomForestRegressor(n_estimators=10, criterion='mse', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, bootstrap=True, oob_score=False, n_jobs=1, random_state=None, verbose=0, warm_start=False)

A random forest regressor.

A random forest is a meta estimator that fits a number of classifying decision trees on various sub-samples of the dataset and use averaging to improve the predictive accuracy and control over-fitting. The sub-sample size is always the same as the original input sample size but the samples are drawn with replacement if bootstrap=True (default).

Read more in the User Guide.

Parameters

n_estimators : integer, optional (default=10)

The number of trees in the forest.

criterion : string, optional (default="mse")

The function to measure the quality of a split. Supported criteria are “mse” for the mean squared error, which is equal to variance reduction as feature selection criterion, and “mae” for the mean absolute error.

New in version 0.18: Mean Absolute Error (MAE) criterion.

max_features : int, float, string or None, optional (default=”auto”)

The number of features to consider when looking for the best split:

• If int, then consider max_features features at each split.
• If float, then max_features is a percentage and int(max_features * n_features) features are considered at each split.
• If “auto”, then max_features=n_features.
• If “sqrt”, then max_features=sqrt(n_features).
• If “log2”, then max_features=log2(n_features).
• If None, then max_features=n_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max_features features.

max_depth : integer or None, optional (default=None)
The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min_samples_split samples.

**min_samples_split**: int, float, optional (default=2)

The minimum number of samples required to split an internal node:

- If int, then consider min_samples_split as the minimum number.
- If float, then min_samples_split is a percentage and ceil(min_samples_split * n_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider min_samples_leaf as the minimum number.
- If float, then min_samples_leaf is a percentage and ceil(min_samples_leaf * n_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

**max_leaf_nodes**: int or None, optional (default=None)

Grow trees with max_leaf_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min_impurity_split has been deprecated in favor of min_impurity_decrease in 0.19 and will be removed in 0.21. Use min_impurity_decrease instead.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[ N_t / N \times (\text{impurity} - N_{t_R} / N_t \times \text{right}_\text{impurity} - N_{t_L} / N_t \times \text{left}_\text{impurity}) \]

where \( N \) is the total number of samples, \( N_t \) is the number of samples at the current node, \( N_{t_L} \) is the number of samples in the left child, and \( N_{t_R} \) is the number of samples in the right child.

\( N, N_t, N_{t_R} \) and \( N_{t_L} \) all refer to the weighted sum, if sample_weight is passed.

New in version 0.19.

**bootstrap**: boolean, optional (default=True)
Whether bootstrap samples are used when building trees.

- **oob_score**: bool, optional (default=False)
  - Whether to use out-of-bag samples to estimate the R^2 on unseen data.

- **n_jobs**: integer, optional (default=1)
  - The number of jobs to run in parallel for both fit and predict. If -1, then the number of jobs is set to the number of cores.

- **random_state**: int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

- **verbose**: int, optional (default=0)
  - Controls the verbosity of the tree building process.

- **warm_start**: bool, optional (default=False)
  - When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest.

### Attributes

- **feature_importances_**: Return the feature importances (the higher, the more important the feature).

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>estimators_</td>
<td>(list of DecisionTreeRegressor) The collection of fitted sub-estimators.</td>
</tr>
<tr>
<td>n_features_</td>
<td>(int) The number of features when fit is performed.</td>
</tr>
<tr>
<td>n_outputs_</td>
<td>(int) The number of outputs when fit is performed.</td>
</tr>
<tr>
<td>oob_score_</td>
<td>(float) Score of the training dataset obtained using an out-of-bag estimate.</td>
</tr>
<tr>
<td>oob_prediction_</td>
<td>(array of shape = [n_samples]) Prediction computed with out-of-bag estimate on the training set.</td>
</tr>
</tbody>
</table>

**See also:**

- DecisionTreeRegressor, ExtraTreesRegressor

**Notes**

The default values for the parameters controlling the size of the trees (e.g. max_depth, min_samples_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data, max_features=n_features and bootstrap=False, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random_state has to be fixed.
References

[R8383]

Examples

```python
from sklearn.ensemble import RandomForestRegressor
from sklearn.datasets import make_regression

X, y = make_regression(n_features=4, n_informative=2,
                        random_state=0, shuffle=False)
regr = RandomForestRegressor(max_depth=2, random_state=0)
regr.fit(X, y)
RandomForestRegressor(bootstrap=True, criterion='mse', max_depth=2,
                        max_features='auto', max_leaf_nodes=None,
                        min_impurity_decrease=0.0, min_impurity_split=None,
                        min_samples_leaf=1, min_samples_split=2,
                        min_weight_fraction_leaf=0.0, n_estimators=10, n_jobs=1,
                        oob_score=False, random_state=0, verbose=0, warm_start=False)
print(regr.feature_importances_)
[ 0.17339552 0.81594114 0. 0.01066333]
print(regr.predict([[0, 0, 0, 0]]))
[-2.50699856]
```

Methods

- **apply**
  - Apply trees in the forest to X, return leaf indices.

- **decision_path**
  - Return the decision path in the forest

- **fit**
  - Build a forest of trees from the training set (X, y).

- **get_params**
  - Get parameters for this estimator.

- **predict**
  - Predict regression target for X.

- **score**
  - Returns the coefficient of determination R^2 of the prediction.

- **set_params**
  - Set the parameters of this estimator.

```python
__init__(n_estimators=10, criterion='mse', max_depth=None, min_samples_split=2,
         min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto',
         max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None,
         bootstrap=True, oob_score=False, n_jobs=1, random_state=None, verbose=0,
         warm_start=False)
```

**apply**

Apply trees in the forest to X, return leaf indices.

**Parameters**

- X: array-like or sparse matrix, shape = [n_samples, n_features]

  The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns**

- X_leaves: array_like, shape = [n_samples, n_estimators]

  For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.
**decision_path**(*X*)
Return the decision path in the forest

New in version 0.18.

**Parameters**

* X : array-like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, its dtypes will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns**

* indicator : sparse csr array, shape = [n_samples, n_nodes]
  
  Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

* n_nodes_ptr : array of size (n_estimators + 1,)
  
  The columns from indicator[n_nodes_ptr[i]:n_nodes_ptr[i+1]] gives the indicator value for the i-th estimator.

**feature_importances_**

Return the feature importances (the higher, the more important the feature).

**Returns**

* feature_importances_ : array, shape = [n_features]

**fit**(X, y, **sample_weight=None**)
Build a forest of trees from the training set (X, y).

**Parameters**

* X : array-like or sparse matrix of shape = [n_samples, n_features]
  
  The training input samples. Internally, its dtypes will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csc_matrix.

* y : array-like, shape = [n_samples] or [n_samples, n_outputs]
  
  The target values (class labels in classification, real numbers in regression).

* sample_weight : array-like, shape = [n_samples] or None
  
  Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

**Returns**

* self : object
  
  Returns self.

**get_params**(deep=True)
Get parameters for this estimator.

**Parameters**

* deep : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

* params : mapping of string to any
  
  Parameter names mapped to their values.

**predict**(X)
Predict regression target for X.
The predicted regression target of an input sample is computed as the mean predicted regression targets of
the trees in the forest.

**Parameters**

X : array-like or sparse matrix of shape [n_samples, n_features]

The input samples. Internally, its dtype will be converted to dtype=np.float32. If
a sparse matrix is provided, it will be converted into a sparse csr_matrix.

Returns

y : array of shape = [n_samples] or [n_samples, n_outputs]

The predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where u is the residual sum of squares 
$((y_{true} - y_{pred}) ** 2).sum()$ and v is the total sum of squares 
$((y_{true} - y_{true}.mean()) ** 2).sum()$. The best possible score
is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always
predicts the expected value of y, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

Returns

score : float

$R^2$ of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form `<component>__<parameter>` so that it’s possible to update each component
of a nested object.

Returns

self

**Examples using sklearn.ensemble.RandomForestRegressor**

- *Imputing missing values before building an estimator*
- *Prediction Latency*
- *Comparing random forests and the multi-output meta estimator*

### 3.3. Model selection and evaluation 449
An extra-trees classifier.

This class implements a meta estimator that fits a number of randomized decision trees (a.k.a. extra-trees) on various sub-samples of the dataset and use averaging to improve the predictive accuracy and control over-fitting.

Read more in the User Guide.

**Parameters**

- **n_estimators**: integer, optional (default=10)
  
The number of trees in the forest.

- **criterion**: string, optional (default="gini")
  
The function to measure the quality of a split. Supported criteria are “gini” for the Gini impurity and “entropy” for the information gain.

- **max_features**: int, float, string or None, optional (default="auto")
  
The number of features to consider when looking for the best split:
  
  - If int, then consider `max_features` features at each split.
  
  - If float, then `max_features` is a percentage and `int(max_features * n_features)` features are considered at each split.
  
  - If “auto”, then `max_features=sqrt(n_features)`.
  
  - If “sqrt”, then `max_features=sqrt(n_features)`.
  
  - If “log2”, then `max_features=log2(n_features)`.
  
  - If None, then `max_features=n_features`.

  Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than `max_features` features.

- **max_depth**: integer or None, optional (default=None)
  
The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than `min_samples_split` samples.

- **min_samples_split**: int, float, optional (default=2)
  
The minimum number of samples required to split an internal node:
  
  - If int, then consider `min_samples_split` as the minimum number.
  
  - If float, then `min_samples_split` is a percentage and `ceil(min_samples_split * n_samples)` are the minimum number of samples for each split.

  Changed in version 0.18: Added float values for percentages.
**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider \(\text{min} \_\text{samples} \_\text{leaf}\) as the minimum number.
- If float, then \(\text{min} \_\text{samples} \_\text{leaf}\) is a percentage and \(\left\lceil \text{min} \_\text{samples} \_\text{leaf} \times \frac{n \_\text{samples}}{N} \right\rceil\) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

**max_leaf_nodes**: int or None, optional (default=None)

Grow trees with max_leaf_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: \(\text{min} \_\text{impurity} \_\text{split}\) has been deprecated in favor of \(\text{min} \_\text{impurity} \_\text{decrease}\) in 0.19 and will be removed in 0.21. Use \(\text{min} \_\text{impurity} \_\text{decrease}\) instead.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N \_t}{N} \times \left( \text{impurity} - \frac{N \_t \_R}{N \_t} \times \text{right} \_\text{impurity} - \frac{N \_t \_L}{N \_t} \times \text{left} \_\text{impurity} \right)
\]

where \(N\) is the total number of samples, \(N \_t\) is the number of samples at the current node, \(N \_t \_L\) is the number of samples in the left child, and \(N \_t \_R\) is the number of samples in the right child.

\(N, N \_t, N \_t \_R\) and \(N \_t \_L\) all refer to the weighted sum, if sample_weight is passed.

New in version 0.19.

**bootstrap**: boolean, optional (default=False)

Whether bootstrap samples are used when building trees.

**oob_score**: bool, optional (default=False)

Whether to use out-of-bag samples to estimate the generalization accuracy.

**n_jobs**: integer, optional (default=1)

The number of jobs to run in parallel for both fit and predict. If -1, then the number of jobs is set to the number of cores.

**random_state**: int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

verbose : int, optional (default=0)

Controls the verbosity of the tree building process.

warm_start : bool, optional (default=False)

When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest.

class_weight : dict, list of dicts, “balanced”, “balanced_subsample” or None, optional (default=None)

Weights associated with classes in the form {class_label: weight}. If not given, all classes are supposed to have weight one. For multi-output problems, a list of dicts can be provided in the same order as the columns of y.

Note that for multiclass output weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be [{0: 1, 1: 1}, {0: 1, 1: 5}, {0: 1, 1: 1}, {0: 1, 1: 1}] instead of [{1:1}, {2:5}, {3:1}, {4:1}].

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as n_samples / (n_classes * np.bincount(y))

The “balanced_subsample” mode is the same as “balanced” except that weights are computed based on the bootstrap sample for every tree grown.

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with sample_weight (passed through the fit method) if sample_weight is specified.

Attributes

feature_importances_ Return the feature importances (the higher, the more important the feature).

estimators_ (list of DecisionTreeClassifier) The collection of fitted sub-estimators.

classes_ (array of shape = [n_classes] or a list of such arrays) The classes labels (single output problem), or a list of arrays of class labels (multi-output problem).

n_classes_ (int or list) The number of classes (single output problem), or a list containing the number of classes for each output (multi-output problem).

n_features_ (int) The number of features when fit is performed.

n_outputs_ (int) The number of outputs when fit is performed.

oob_score_ (float) Score of the training dataset obtained using an out-of-bag estimate.

oob_decision_function_ (array of shape = [n_samples, n_classes]) Decision function computed with out-of-bag estimate on the training set. If n_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob_decision_function_ might contain NaN.

See also:
**sklearn.tree.ExtraTreeClassifier** Base classifier for this ensemble.

**RandomForestClassifier** Ensemble Classifier based on trees with optimal splits.

**Notes**

The default values for the parameters controlling the size of the trees (e.g. `max_depth`, `min_samples_leaf`, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

**References**

[R7373]

**Methods**

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__init__(n_estimators=10, criterion='gini', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, bootstrap=False, oob_score=False, n_jobs=1, random_state=None, verbose=0, warm_start=False, class_weight=None)

**apply (X)**

Apply trees in the forest to X, return leaf indices.

**Parameters** X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, its dtype will be converted to `dtype=np.float32`. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns** X_leaves : array_like, shape = [n_samples, n_estimators]

For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.

**decision_path (X)**

Return the decision path in the forest

New in version 0.18.

**Parameters** X : array-like or sparse matrix, shape = [n_samples, n_features]
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns indicator**: sparse csr array, shape = [n_samples, n_nodes]

Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**n_nodes_ptr**: array of size (n_estimators + 1,)

The columns from indicator[n_nodes_ptr[i]:n_nodes_ptr[i+1]] gives the indicator value for the i-th estimator.

**feature_importances_**

Return the feature importances (the higher, the more important the feature).

**Returns feature_importances_**: array, shape = [n_features]

**fit**(X, y, sample_weight=None)

Build a forest of trees from the training set (X, y).

**Parameters**

X: array-like or sparse matrix of shape = [n_samples, n_features]

The training input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csc_matrix.

y: array-like, shape = [n_samples] or [n_samples, n_outputs]

The target values (class labels in classification, real numbers in regression).

sample_weight: array-like, shape = [n_samples] or [n_samples, n_outputs] or None

Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

**Returns** self: object

Returns self.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

params: mapping of string to any

Parameter names mapped to their values.

**predict**(X)

Predict class for X.

The predicted class of an input sample is a vote by the trees in the forest, weighted by their probability estimates. That is, the predicted class is the one with highest mean probability estimate across the trees.

**Parameters**

X: array-like or sparse matrix of shape = [n_samples, n_features]

The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.
**Returns**  
\( y \) : array of shape = \([n_{\text{samples}}]\) or \([n_{\text{samples}}, n_{\text{outputs}}]\)  
The predicted classes.

**predict_log_proba** (\( X \))  
Predict class log-probabilities for \( X \).

The predicted class log-probabilities of an input sample is computed as the log of the mean predicted class probabilities of the trees in the forest.

**Parameters**  
\( X \) : array-like or sparse matrix of shape = \([n_{\text{samples}}, n_{\text{features}}]\)  
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse `csr_matrix`.

**Returns**  
\( p \) : array of shape = \([n_{\text{samples}}, n_{\text{classes}}]\), or a list of \( n_{\text{outputs}} \) such arrays if \( n_{\text{outputs}} > 1 \). The class probabilities of the input samples. The order of the classes corresponds to that in the attribute `classes_`.

**predict_proba** (\( X \))  
Predict class probabilities for \( X \).

The predicted class probabilities of an input sample are computed as the mean predicted class probabilities of the trees in the forest. The class probability of a single tree is the fraction of samples of the same class in a leaf.

**Parameters**  
\( X \) : array-like or sparse matrix of shape = \([n_{\text{samples}}, n_{\text{features}}]\)  
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse `csr_matrix`.

**Returns**  
\( p \) : array of shape = \([n_{\text{samples}}, n_{\text{classes}}]\), or a list of \( n_{\text{outputs}} \) such arrays if \( n_{\text{outputs}} > 1 \). The class probabilities of the input samples. The order of the classes corresponds to that in the attribute `classes_`.

**score** (\( X, y, sample\_weight=None \))  
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**  
\( X \) : array-like, shape = \((n_{\text{samples}}, n_{\text{features}})\)  
Test samples.

\( y \) : array-like, shape = \((n_{\text{samples}})\) or \((n_{\text{samples}}, n_{\text{outputs}})\)  
True labels for \( X \).

\( sample\_weight \) : array-like, shape = \([n_{\text{samples}}]\), optional  
Sample weights.

**Returns**  
\( \text{score} \) : float  
Mean accuracy of self.predict(\( X \)) wrt. \( y \).

**set_params** (**\( \text{params} \))  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
\( \text{self} \)
Examples using `sklearn.ensemble.ExtraTreesClassifier`

- Pixel importances with a parallel forest of trees
- Feature importances with forests of trees
- Hashing feature transformation using Totally Random Trees
- Plot the decision surfaces of ensembles of trees on the iris dataset

`sklearn.ensemble.ExtraTreesRegressor`

```python
class sklearn.ensemble.ExtraTreesRegressor(n_estimators=10, criterion='mse', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, bootstrap=False, oob_score=False, n_jobs=1, random_state=None, verbose=0, warm_start=False)
```

An extra-trees regressor.

This class implements a meta estimator that fits a number of randomized decision trees (a.k.a. extra-trees) on various sub-samples of the dataset and use averaging to improve the predictive accuracy and control over-fitting. Read more in the `User Guide`.

**Parameters**

- `n_estimators` : integer, optional (default=10)
  The number of trees in the forest.

- `criterion` : string, optional (default="mse")
  The function to measure the quality of a split. Supported criteria are “mse” for the mean squared error, which is equal to variance reduction as feature selection criterion, and “mae” for the mean absolute error.
  New in version 0.18: Mean Absolute Error (MAE) criterion.

- `max_features` : int, float, string or None, optional (default="auto")
  The number of features to consider when looking for the best split:
  - If int, then consider `max_features` features at each split.
  - If float, then `max_features` is a percentage and `int(max_features * n_features)` features are considered at each split.
  - If “auto”, then `max_features`=n_features.
  - If “sqrt”, then `max_features`=sqrt(n_features).
  - If “log2”, then `max_features`=log2(n_features).
  - If None, then `max_features`=n_features.
  Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than `max_features` features.

- `max_depth` : integer or None, optional (default=None)
  The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than `min_samples_split` samples.
The maximum depth of the tree. If None, then nodes are expanded until all leaves are
pure or until all leaves contain less than min_samples_split samples.

**min_samples_split**: int, float, optional (default=2)

The minimum number of samples required to split an internal node:

- If int, then consider *min_samples_split* as the minimum number.
- If float, then *min_samples_split* is a percentage and \( \text{ceil}(\text{min_samples_split} \times n\_samples) \) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider *min_samples_leaf* as the minimum number.
- If float, then *min_samples_leaf* is a percentage and \( \text{ceil}(\text{min_samples_leaf} \times n\_samples) \) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples)
required to be at a leaf node. Samples have equal weight when sample_weight is not
provided.

**max_leaf_nodes**: int or None, optional (default=None)

Grow trees with *max_leaf_nodes* in best-first fashion. Best nodes are defined as
relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above
the threshold, otherwise it is a leaf.

Deprecated since version 0.19: *min_impurity_split* has been deprecated in fa-
vor of *min_impurity_decrease* in 0.19 and will be removed in 0.21. Use
*min_impurity_decrease* instead.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal
to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_t}{N} \times \left( \text{impurity} - \frac{N_{t\_R}}{N_t} \times \text{right\_impurity} \right.
\]
\[
- \frac{N_{t\_L}}{N_t} \times \text{left\_impurity} \right)
\]

where \( N \) is the total number of samples, \( N_t \) is the number of samples at the current
node, \( N_{t\_L} \) is the number of samples in the left child, and \( N_{t\_R} \) is the number of
samples in the right child.

\( N, N_t, N_{t\_R} \text{ and } N_{t\_L} \) all refer to the weighted sum, if sample_weight is
passed.

New in version 0.19.

**bootstrap**: boolean, optional (default=False)
Whether bootstrap samples are used when building trees.

- **oob_score**: bool, optional (default=False)
  Whether to use out-of-bag samples to estimate the R^2 on unseen data.

- **n_jobs**: integer, optional (default=1)
  The number of jobs to run in parallel for both `fit` and `predict`. If -1, then the number of jobs is set to the number of cores.

- **random_state**: int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

- **verbose**: int, optional (default=0)
  Controls the verbosity of the tree building process.

- **warm_start**: bool, optional (default=False)
  When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest.

**Attributes**

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<tr>
<th>Name</th>
<th>Description</th>
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<tbody>
<tr>
<td>feature_importances_</td>
<td>Return the feature importances (the higher, the more important the feature).</td>
</tr>
<tr>
<td>estimators_</td>
<td>(list of DecisionTreeRegressor) The collection of fitted sub-estimators.</td>
</tr>
<tr>
<td>n_features_</td>
<td>(int) The number of features.</td>
</tr>
<tr>
<td>n_outputs_</td>
<td>(int) The number of outputs.</td>
</tr>
<tr>
<td>oob_score_</td>
<td>(float) Score of the training dataset obtained using an out-of-bag estimate.</td>
</tr>
<tr>
<td>oob_prediction_</td>
<td>(array of shape = [n_samples]) Prediction computed with out-of-bag estimate on the training set.</td>
</tr>
</tbody>
</table>

**See also:**

- `sklearn.tree.ExtraTreeRegressor` Base estimator for this ensemble.
- `RandomForestRegressor` Ensemble regressor using trees with optimal splits.

**Notes**

The default values for the parameters controlling the size of the trees (e.g. `max_depth`, `min_samples_leaf`, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

**References**

[R7575]
Methods

apply(X)
Apply trees in the forest to X, return leaf indices.

decision_path(X)
Return the decision path in the forest

fit(X, y[, sample_weight])
Build a forest of trees from the training set (X, y).

get_params([deep])
Get parameters for this estimator.

predict(X)
Predict regression target for X.

score(X, y[, sample_weight])
Returns the coefficient of determination R^2 of the prediction.

set_params(**params)
Set the parameters of this estimator.

__init__(n_estimators=10, criterion='mse', max_depth=None, min_samples_split=2,
min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto',
max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None,
bootstrap=False, oob_score=False, n_jobs=1, random_state=None, verbose=0,
warm_start=False)

apply(X)
Apply trees in the forest to X, return leaf indices.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

Returns X_leaves : array_like, shape = [n_samples, n_estimators]
For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.

decision_path(X)
Return the decision path in the forest

New in version 0.18.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

Returns indicator : sparse csr array, shape = [n_samples, n_nodes]
Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

n_nodes_ptr : array of size (n_estimators + 1, )
The columns from indicator[n_nodes_ptr[i]:n_nodes_ptr[i+1]] gives the indicator value for the i-th estimator.

feature_importances_
Return the feature importances (the higher, the more important the feature).

Returns feature_importances_ : array, shape = [n_features]

fit(X, y, sample_weight=None)
Build a forest of trees from the training set (X, y).

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]
The training input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csc_matrix.

y : array-like, shape = [n_samples] or [n_samples, n_outputs]
The target values (class labels in classification, real numbers in regression).

sample_weight : array-like, shape = [n_samples] or None
Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

Returns self : object
Returns self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X)
Predict regression target for X.
The predicted regression target of an input sample is computed as the mean predicted regression targets of the trees in the forest.

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]
The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

Returns y : array of shape = [n_samples] or [n_samples, n_outputs]
The predicted values.

score (X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.
The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns score : float
R^2 of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.ensemble.ExtraTreesRegressor

• Face completion with a multi-output estimators

sklearn.ensemble.GradientBoostingClassifier

class sklearn.ensemble.GradientBoostingClassifier (loss='deviance', learning_rate=0.1, n_estimators=100, subsample=1.0, criterion='friedman_mse', min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_depth=3, min_impurity_decrease=0.0, min_impurity_split=None, init=None, random_state=None, max_features=None, verbose=0, max_leaf_nodes=None, warm_start=False, pre_sort='auto', validation_fraction=0.1, n_iter_no_change=None, tol=0.0001)

Gradient Boosting for classification.

GB builds an additive model in a forward stage-wise fashion; it allows for the optimization of arbitrary differentiable loss functions. In each stage \( n_{\text{classes}} \) regression trees are fit on the negative gradient of the binomial or multinomial deviance loss function. Binary classification is a special case where only a single regression tree is induced.

Read more in the User Guide.

Parameters loss : {'deviance', 'exponential'}, optional (default='deviance')

loss function to be optimized. ‘deviance’ refers to deviance (= logistic regression) for classification with probabilistic outputs. For loss ‘exponential’ gradient boosting recovers the AdaBoost algorithm.

learning_rate : float, optional (default=0.1)

learning rate shrinks the contribution of each tree by learning_rate. There is a trade-off between learning_rate and n_estimators.

n_estimators : int (default=100)

The number of boosting stages to perform. Gradient boosting is fairly robust to over-fitting so a large number usually results in better performance.

max_depth : integer, optional (default=3)
maximum depth of the individual regression estimators. The maximum depth limits the number of nodes in the tree. Tune this parameter for best performance; the best value depends on the interaction of the input variables.

criterion : string, optional (default="friedman_mse")

The function to measure the quality of a split. Supported criteria are “friedman_mse” for the mean squared error with improvement score by Friedman, “mse” for mean squared error, and “mae” for the mean absolute error. The default value of “friedman_mse” is generally the best as it can provide a better approximation in some cases.

New in version 0.18.

min_samples_split : int, float, optional (default=2)

The minimum number of samples required to split an internal node:
• If int, then consider min_samples_split as the minimum number.
• If float, then min_samples_split is a percentage and ceil(min_samples_split * n_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

min_samples_leaf : int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:
• If int, then consider min_samples_leaf as the minimum number.
• If float, then min_samples_leaf is a percentage and ceil(min_samples_leaf * n_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

min_weight_fraction_leaf : float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

subsample : float, optional (default=1.0)

The fraction of samples to be used for fitting the individual base learners. If smaller than 1.0 this results in Stochastic Gradient Boosting. subsample interacts with the parameter n_estimators. Choosing subsample < 1.0 leads to a reduction of variance and an increase in bias.

max_features : int, float, string or None, optional (default=None)

The number of features to consider when looking for the best split:
• If int, then consider max_features features at each split.
• If float, then max_features is a percentage and int(max_features * n_features) features are considered at each split.
• If “auto”, then max_features=sqrt(n_features).
• If “sqrt”, then max_features=sqrt(n_features).
• If “log2”, then max_features=log2(n_features).
• If None, then max_features=n_features.
Choosing $max\_features < n\_features$ leads to a reduction of variance and an increase in bias.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than $max\_features$ features.

**max_leaf_nodes**: int or None, optional (default=None)
Grow trees with $max\_leaf\_nodes$ in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,
Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: `min_impurity_split` has been deprecated in favor of `min_impurity_decrease` in 0.19 and will be removed in 0.21. Use `min_impurity_decrease` instead.

**min_impurity_decrease**: float, optional (default=0.)
A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

$$
\frac{N_t}{N} \times \left( \text{impurity} - \frac{N_{t\_R}}{N_t} \times \text{right\_impurity} - \frac{N_{t\_L}}{N_t} \times \text{left\_impurity} \right)
$$

where $N$ is the total number of samples, $N_t$ is the number of samples at the current node, $N_{t\_L}$ is the number of samples in the left child, and $N_{t\_R}$ is the number of samples in the right child.

$N$, $N_t$, $N_{t\_R}$ and $N_{t\_L}$ all refer to the weighted sum, if `sample_weight` is passed.

New in version 0.19.

**init**: BaseEstimator, None, optional (default=None)
An estimator object that is used to compute the initial predictions. `init` has to provide `fit` and `predict`. If None it uses `loss.init_estimator`.

**verbose**: int, default: 0
Enable verbose output. If 1 then it prints progress and performance once in a while (the more trees the lower the frequency). If greater than 1 then it prints progress and performance for every tree.

**warm_start**: bool, default: False
When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just erase the previous solution.

**random_state**: int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**presort**: bool or ‘auto’, optional (default=’auto’)
Whether to presort the data to speed up the finding of best splits in fitting. Auto mode by default will use presorting on dense data and default to normal sorting on sparse data. Setting presort to true on sparse data will raise an error.

New in version 0.17: `presort` parameter.

`validation_fraction`: float, optional, default 0.1

The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if `n_iter_no_change` is set to an integer.

New in version 0.20.

`n_iter_no_change`: int, default None

`n_iter_no_change` is used to decide if early stopping will be used to terminate training when validation score is not improving. By default it is set to None to disable early stopping. If set to a number, it will set aside `validation_fraction` size of the training data as validation and terminate training when validation score is not improving in all of the previous `n_iter_no_change` numbers of iterations.

New in version 0.20.

`tol`: float, optional, default 1e-4

Tolerance for the early stopping. When the loss is not improving by at least tol for `n_iter_no_change` iterations (if set to a number), the training stops.

New in version 0.20.

**Attributes**

`feature_importances_` Return the feature importances (the higher, the more important the feature).

`n_estimators_` (int) The number of estimators as selected by early stopping (if `n_iter_no_change` is specified). Otherwise it is set to `n_estimators`. .. versionadded:: 0.20

`oob_improvement_` (array, shape = [n_estimators]) The improvement in loss (= deviance) on the out-of-bag samples relative to the previous iteration. `oob_improvement_[0]` is the improvement in loss of the first stage over the `init` estimator.

`train_score_` (array, shape = [n_estimators]) The i-th score `train_score_[i]` is the deviance (= loss) of the model at iteration i on the in-bag sample. If `subsample == 1` this is the deviance on the training data.

`loss_` (LossFunction) The concrete `LossFunction` object.

`init` (BaseEstimator) The estimator that provides the initial predictions. Set via the `init` argument or `loss.init_estimator`.

`estimators_` (ndarray of DecisionTreeRegressor, shape = [n_estimators, loss_.K]) The collection of fitted sub-estimators. `loss_.K` is 1 for binary classification, otherwise `n_classes`.

See also:

`sklearn.tree.DecisionTreeClassifier`, `RandomForestClassifier`, `AdaBoostClassifier`
Notes

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and max_features=n_features, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random_state has to be fixed.

References


10. Friedman, Stochastic Gradient Boosting, 1999


Methods

apply(X) Apply trees in the ensemble to X, return leaf indices.
decision_function(X) Compute the decision function of X.
fit(X, y[, sample_weight, monitor]) Fit the gradient boosting model.
get_params([deep]) Get parameters for this estimator.
predict(X) Predict class for X.
predict_log_proba(X) Predict class log-probabilities for X.
predict_proba(X) Predict class probabilities for X.
score(X, y[, sample_weight]) Returns the mean accuracy on the given test data and labels.
set_params(**params) Set the parameters of this estimator.
staged_decision_function(X) Compute decision function of X for each iteration.
staged_predict(X) Predict class at each stage for X.
staged_predict_proba(X) Predict class probabilities at each stage for X.

__init__(loss='deviance', learning_rate=0.1, n_estimators=100, subsample=1.0, criterion='friedman_mse', min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_depth=3, min_impurity_decrease=0.0, min_impurity_split=None, init=None, random_state=None, max_features=None, verbose=0, max_leaf_nodes=None, warm_start=False, presort='auto', validation_fraction=0.1, n_iter_no_change=None, tol=0.0001)

apply(X) Apply trees in the ensemble to X, return leaf indices.

New in version 0.17.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted to a sparse csr_matrix.

Returns X_leaves : array_like, shape = [n_samples, n_estimators, n_classes]

For each datapoint x in X and for each tree in the ensemble, return the index of the leaf x ends up in each estimator. In the case of binary classification n_classes is 1.
**decision_function** \((X)\)

Compute the decision function of \(X\).

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  
  The input samples. Internally, it will be converted to \texttt{dtype=np.float32} and if a sparse matrix is provided to a sparse \texttt{csr_matrix}.

**Returns**

- **score**: array, shape = [n_samples, n_classes] or [n_samples]
  
  The decision function of the input samples. The order of the classes corresponds to that in the attribute \texttt{classes_}. Regression and binary classification produce an array of shape [n_samples].

**feature_importances_**

Return the feature importances (the higher, the more important the feature).

**Returns**

- **feature_importances_**: array, shape = [n_features]

**fit** \((X, y, sample_weight=None, monitor=None)\)

Fit the gradient boosting model.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, shape = [n_samples]
  
  Target values (integers in classification, real numbers in regression) For classification, labels must correspond to classes.

- **sample_weight**: array-like, shape = [n_samples] or None
  
  Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

- **monitor**: callable, optional
  
  The monitor is called after each iteration with the current iteration, a reference to the estimator and the local variables of \texttt{_fit_stages} as keyword arguments \texttt{callable(i, self, locals())}. If the callable returns \texttt{True} the fitting procedure is stopped. The monitor can be used for various things such as computing held-out estimates, early stopping, model introspect, and snapshotting.

**Returns**

- **self**: object
  
  Returns self.

**get_params** \((deep=True)\)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  
  Parameter names mapped to their values.
**n_features**

DEPRECATED: Attribute n_features was deprecated in version 0.19 and will be removed in 0.21.

**predict (X)**

Predict class for X.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

- **y**: array of shape = [n_samples]
  
The predicted values.

**predict_log_proba (X)**

Predict class log-probabilities for X.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

- **p**: array of shape = [n_samples]
  
The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**Raises**

- **AttributeError**
  
If the **loss** does not support probabilities.

**predict_proba (X)**

Predict class probabilities for X.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

- **p**: array of shape = [n_samples]
  
The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**Raises**

- **AttributeError**
  
If the **loss** does not support probabilities.

**score (X, y, sample_weight=None)**

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  
Test samples.

- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  
True labels for X.

- **sample_weight**: array-like, shape = [n_samples], optional
  
Sample weights.

**Returns**

- **score**: float
Mean accuracy of self.predict(X) wrt. y.

**set_params**( **params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

**staged_decision_function**( X)
Compute decision function of X for each iteration.

This method allows monitoring (i.e. determine error on testing set) after each stage.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

Returns score : generator of array, shape = [n_samples, k]

The decision function of the input samples. The order of the classes corresponds to that in the attribute classes_. Regression and binary classification are special cases with k == 1, otherwise k==n_classes.

**staged_predict**( X)
Predict class at each stage for X.

This method allows monitoring (i.e. determine error on testing set) after each stage.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

Returns y : generator of array of shape = [n_samples]

The predicted value of the input samples.

**staged_predict_proba**( X)
Predict class probabilities at each stage for X.

This method allows monitoring (i.e. determine error on testing set) after each stage.

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

Returns y : generator of array of shape = [n_samples]

The predicted value of the input samples.

Examples using `sklearn.ensemble.GradientBoostingClassifier`

- Gradient Boosting regularization
- Early stopping of Gradient Boosting
- Feature transformations with ensembles of trees
- Gradient Boosting Out-of-Bag estimates
sklearn.ensemble.GradientBoostingRegressor

class sklearn.ensemble.GradientBoostingRegressor(loss='ls', learning_rate=0.1, n_estimators=100, subsample=1.0, criterion='friedman_mse', min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_depth=3, min_impurity_decrease=0.0, min_impurity_split=None, init=None, random_state=None, max_features=None, alpha=0.9, verbose=0, max_leaf_nodes=None, warm_start=False, pre_sort='auto', validation_fraction=0.1, n_iter_no_change=None, tol=0.0001)

Gradient Boosting for regression.

GB builds an additive model in a forward stage-wise fashion; it allows for the optimization of arbitrary differentiable loss functions. In each stage a regression tree is fit on the negative gradient of the given loss function.

Read more in the User Guide.

Parameters

- **loss** : {'ls', 'lad', 'huber', 'quantile'}, optional (default='ls')

  loss function to be optimized. ‘ls’ refers to least squares regression. ‘lad’ (least absolute deviation) is a highly robust loss function solely based on order information of the input variables. ‘huber’ is a combination of the two. ‘quantile’ allows quantile regression (use alpha to specify the quantile).

- **learning_rate** : float, optional (default=0.1)

  learning rate shrinks the contribution of each tree by learning_rate. There is a trade-off between learning_rate and n_estimators.

- **n_estimators** : int (default=100)

  The number of boosting stages to perform. Gradient boosting is fairly robust to overfitting so a large number usually results in better performance.

- **max_depth** : integer, optional (default=3)

  maximum depth of the individual regression estimators. The maximum depth limits the number of nodes in the tree. Tune this parameter for best performance; the best value depends on the interaction of the input variables.

- **criterion** : string, optional (default="friedman_mse")

  The function to measure the quality of a split. Supported criteria are “friedman_mse” for the mean squared error with improvement score by Friedman, “mse” for mean squared error, and “mae” for the mean absolute error. The default value of “friedman_mse” is generally the best as it can provide a better approximation in some cases.

  New in version 0.18.

- **min_samples_split** : int, float, optional (default=2)

  The minimum number of samples required to split an internal node:
  - If int, then consider min_samples_split as the minimum number.
• If float, then `min_samples_split` is a percentage and `ceiling(min_samples_split * n_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

• If int, then consider `min_samples_leaf` as the minimum number.

• If float, then `min_samples_leaf` is a percentage and `ceiling(min_samples_leaf * n_samples)` are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

**subsample**: float, optional (default=1.0)

The fraction of samples to be used for fitting the individual base learners. If smaller than 1.0 this results in Stochastic Gradient Boosting. `subsample` interacts with the parameter `n_estimators`. Choosing `subsample < 1.0` leads to a reduction of variance and an increase in bias.

**max_features**: int, float, string or None, optional (default=None)

The number of features to consider when looking for the best split:

• If int, then consider `max_features` features at each split.

• If float, then `max_features` is a percentage and `int(max_features * n_features)` features are considered at each split.

• If “auto”, then `max_features=n_features`.

• If “sqrt”, then `max_features=sqrt(n_features)`.

• If “log2”, then `max_features=log2(n_features)`.

• If None, then `max_features=n_features`.

Choosing `max_features < n_features` leads to a reduction of variance and an increase in bias.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than `max_features` features.

**max_leaf_nodes**: int or None, optional (default=None)

Grow trees with `max_leaf_nodes` in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: `min_impurity_split` has been deprecated in favor of `min_impurity_decrease` in 0.19 and will be removed in 0.21. Use `min_impurity_decrease` instead.
**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_t}{N} \times (impurity - \frac{N_{t,R}}{N_t} \times right \_impurity - \frac{N_{t,L}}{N_t} \times left \_impurity)
\]

where \(N\) is the total number of samples, \(N_t\) is the number of samples at the current node, \(N_{t,L}\) is the number of samples in the left child, and \(N_{t,R}\) is the number of samples in the right child.

\(N\), \(N_t\), \(N_{t,R}\) and \(N_{t,L}\) all refer to the weighted sum, if `sample_weight` is passed.

New in version 0.19.

**alpha**: float (default=0.9)

The alpha-quantile of the huber loss function and the quantile loss function. Only if `loss='huber'` or `loss='quantile'`.

**init**: BaseEstimator, None, optional (default=None)

An estimator object that is used to compute the initial predictions. `init` has to provide `fit` and `predict`. If None it uses `loss.init_estimator`.

**verbose**: int, default: 0

Enable verbose output. If 1 then it prints progress and performance once in a while (the more trees the lower the frequency). If greater than 1 then it prints progress and performance for every tree.

**warm_start**: bool, default: False

When set to `True`, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just erase the previous solution.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**presort**: bool or ‘auto’, optional (default='auto')

Whether to presort the data to speed up the finding of best splits in fitting. Auto mode by default will use presorting on dense data and default to normal sorting on sparse data. Setting presort to true on sparse data will raise an error.

New in version 0.17: optional parameter `presort`.

**validation_fraction**: float, optional, default 0.1

The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if `early_stopping` is True

New in version 0.20.

**n_iter_no_change**: int, default None

`n_iter_no_change` is used to decide if early stopping will be used to terminate training when validation score is not improving. By default it is set to None to disable
early stopping. If set to a number, it will set aside validation_fraction size of the training data as validation and terminate training when validation score is not improving in all of the previous n_iter_no_change numbers of iterations.

New in version 0.20.

tol : float, optional, default 1e-4
Tolerance for the early stopping. When the loss is not improving by at least tol for n_iter_no_change iterations (if set to a number), the training stops.

New in version 0.20.

Attributes

| feature_importances_            | Return the feature importances (the higher, the more important the feature). |

| oob_improvement_                | The improvement in loss (= deviance) on the out-of-bag samples relative to the previous iteration. oob_improvement_[0] is the improvement in loss of the first stage over the init estimator. |
| oob_improvement_[0]             | |
| train_score_                    | The i-th score train_score_[i] is the deviance (= loss) of the model at iteration i on the in-bag sample. If subsample == 1 this is the deviance on the training data. |
| train_score_[i]                 | |
| train_score_[0]                 | |
| loss_                          | (LossFunction) The concrete LossFunction object. |
| init                           | (BaseEstimator) The estimator that provides the initial predictions. Set via the init argument or loss.init_estimator. |
| estimators_                    | (ndarray of DecisionTreeRegressor, shape = [n_estimators, 1]) The collection of fitted sub-estimators. |

See also:

DecisionTreeRegressor, RandomForestRegressor

Notes

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and max_features=n_features, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random_state has to be fixed.

References


10. Friedman, Stochastic Gradient Boosting, 1999

### Methods

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#### __init__

```python
(loss='ls', learning_rate=0.1, n_estimators=100, subsample=1.0, criterion='friedman_mse', min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_depth=3, min_impurity_decrease=0.0, min_impurity_split=None, init=None, random_state=None, max_features=None, alpha=0.9, verbose=0, max_leaf_nodes=None, warm_start=False, presort='auto', validation_fraction=0.1, n_iter_no_change=None, tol=0.0001)
```

#### apply (X)

Apply trees in the ensemble to X, return leaf indices.

New in version 0.17.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  
  The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted to a sparse csr_matrix.

**Returns**

- **X_leaves**: array_like, shape = [n_samples, n_estimators]
  
  For each datapoint x in X and for each tree in the ensemble, return the index of the leaf x ends up in each estimator.

#### feature_importances_

Return the feature importances (the higher, the more important the feature).

**Returns**

- **feature_importances_**: array, shape = [n_features]

#### fit (X, y, sample_weight=None, monitor=None)

Fit the gradient boosting model.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, shape = [n_samples]
  
  Target values (integers in classification, real numbers in regression) For classification, labels must correspond to classes.

- **sample_weight**: array-like, shape = [n_samples] or None
  
  Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they result in any single class carrying a negative weight in either child node.

- **monitor**: callable, optional
The monitor is called after each iteration with the current iteration, a reference to the estimator and the local variables of \_fit\_stages as keyword arguments callable(i, self, locals()). If the callable returns True the fitting procedure is stopped. The monitor can be used for various things such as computing held-out estimates, early stopping, model introspect, and snapshoting.

**Returns**

self : object

Returns self.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

params : mapping of string to any

Parameter names mapped to their values.

**n_features**

DEPRECATED: Attribute n_features was deprecated in version 0.19 and will be removed in 0.21.

**predict** *(X)*

Predict regression target for X.

**Parameters**

X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

y : array of shape = [n_samples]

The predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $\sum(y_{true} - y_{pred})^2$ and $v$ is the total sum of squares $\sum(y_{true} - \bar{y}_{true})^2$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

**Returns**

score : float

$R^2$ of self.predict(X) wrt. y.

**set_params** *(**params)*

Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

```python
staged_predict(X)
```

Predict regression target at each stage for X.

This method allows monitoring (i.e. determine error on testing set) after each stage.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]

  The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

- **y**: generator of array of shape = [n_samples]

  The predicted value of the input samples.

**Examples using sklearn.ensemble.GradientBoostingRegressor**

- Model Complexity Influence
- Prediction Intervals for Gradient Boosting Regression
- Gradient Boosting regression
- Partial Dependence Plots

### 3.3.3 Model evaluation: quantifying the quality of predictions

There are 3 different APIs for evaluating the quality of a model’s predictions:

- **Estimator score method**: Estimators have a `score` method providing a default evaluation criterion for the problem they are designed to solve. This is not discussed on this page, but in each estimator’s documentation.

- **Scoring parameter**: Model-evaluation tools using cross-validation (such as `model_selection.cross_val_score` and `model_selection.GridSearchCV`) rely on an internal scoring strategy. This is discussed in the section *The scoring parameter: defining model evaluation rules*.

- **Metric functions**: The `metrics` module implements functions assessing prediction error for specific purposes. These metrics are detailed in sections on *Classification metrics*, *Multilabel ranking metrics*, *Regression metrics* and *Clustering metrics*.

Finally, **Dummy estimators** are useful to get a baseline value of those metrics for random predictions.

**See also**:

For “pairwise” metrics, between samples and not estimators or predictions, see the *Pairwise metrics, Affinities and Kernels* section.

**The scoring parameter: defining model evaluation rules**

Model selection and evaluation using tools, such as `model_selection.GridSearchCV` and `model_selection.cross_val_score`, take a scoring parameter that controls what metric they apply to the estimators evaluated.
Common cases: predefined values

For the most common use cases, you can designate a scorer object with the `scoring` parameter; the table below shows all possible values. All scorer objects follow the convention that higher return values are better than lower return values. Thus metrics which measure the distance between the model and the data, like `metrics.mean_squared_error`, are available as neg_mean_squared_error which return the negated value of the metric.

<table>
<thead>
<tr>
<th>Scoring</th>
<th>Function</th>
<th>Comment</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Classification</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>'accuracy'</td>
<td><code>metrics.accuracy_score</code></td>
<td></td>
</tr>
<tr>
<td>'balanced_accuracy'</td>
<td><code>metrics.balanced_accuracy_score</code></td>
<td>for binary targets</td>
</tr>
<tr>
<td>'average_precision'</td>
<td><code>metrics.average_precision_score</code></td>
<td></td>
</tr>
<tr>
<td>'brier_score_loss'</td>
<td><code>metrics.brier_score_loss</code></td>
<td></td>
</tr>
<tr>
<td>'f1'</td>
<td><code>metrics.f1_score</code></td>
<td>for binary targets</td>
</tr>
<tr>
<td>'f1_micro'</td>
<td><code>metrics.f1_score</code></td>
<td>micro-averaged</td>
</tr>
<tr>
<td>'f1_macro'</td>
<td><code>metrics.f1_score</code></td>
<td>macro-averaged</td>
</tr>
<tr>
<td>'f1_weighted'</td>
<td><code>metrics.f1_score</code></td>
<td>weighted average</td>
</tr>
<tr>
<td>'f1_samples'</td>
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</tr>
<tr>
<td>'neg_log_loss'</td>
<td><code>metrics.log_loss</code></td>
<td>requires <code>predict_proba</code> support</td>
</tr>
<tr>
<td>'precision' etc.</td>
<td><code>metrics.precision_score</code></td>
<td>suffixes apply as with ‘f1’</td>
</tr>
<tr>
<td>'recall' etc.</td>
<td><code>metrics.recall_score</code></td>
<td>suffixes apply as with ‘f1’</td>
</tr>
<tr>
<td>'roc_auc'</td>
<td><code>metrics.roc_auc_score</code></td>
<td></td>
</tr>
<tr>
<td><strong>Clustering</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>'adjusted_mutual_info_score'</td>
<td><code>metrics.adjusted_mutual_info_score</code></td>
<td></td>
</tr>
<tr>
<td>'adjusted_rand_score'</td>
<td><code>metrics.adjusted_rand_score</code></td>
<td></td>
</tr>
<tr>
<td>'completeness_score'</td>
<td><code>metrics.completeness_score</code></td>
<td></td>
</tr>
<tr>
<td>'fowlkes_mallows_score'</td>
<td><code>metrics.fowlkes_mallows_score</code></td>
<td></td>
</tr>
<tr>
<td>'homogeneity_score'</td>
<td><code>metrics.homogeneity_score</code></td>
<td></td>
</tr>
<tr>
<td>'mutual_info_score'</td>
<td><code>metrics.mutual_info_score</code></td>
<td></td>
</tr>
<tr>
<td>'normalized_mutual_info_score'</td>
<td><code>metrics.normalized_mutual_info_score</code></td>
<td></td>
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<tr>
<td>'v_measure_score'</td>
<td><code>metrics.v_measure_score</code></td>
<td></td>
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<tr>
<td><strong>Regression</strong></td>
<td></td>
<td></td>
</tr>
<tr>
<td>'explained_variance'</td>
<td><code>metrics.explained_variance_score</code></td>
<td></td>
</tr>
<tr>
<td>'neg_mean_absolute_error'</td>
<td><code>metrics.mean_absolute_error</code></td>
<td></td>
</tr>
<tr>
<td>'neg_mean_squared_error'</td>
<td><code>metrics.mean_squared_error</code></td>
<td></td>
</tr>
<tr>
<td>'neg_median_absolute_error'</td>
<td><code>metrics.median_absolute_error</code></td>
<td></td>
</tr>
<tr>
<td>'r2'</td>
<td><code>metrics.r2_score</code></td>
<td></td>
</tr>
</tbody>
</table>

Usage examples:

```python
>>> from sklearn import svm, datasets
>>> from sklearn.model_selection import cross_val_score
>>> iris = datasets.load_iris()
>>> X, y = iris.data, iris.target
>>> clf = svm.SVC(probability=True, random_state=0)
>>> cross_val_score(clf, X, y, scoring='neg_log_loss')
array([-0.07..., -0.16..., -0.06...])
>>> model = svm.SVC()
>>> cross_val_score(model, X, y, scoring='wrong_choice')
ValueError: 'wrong_choice' is not a valid scoring value. Valid options are ['accuracy', 'adjusted_mutual_info_score', 'adjusted_rand_score', 'average_precision', 'balanced_accuracy', 'brier_score_loss', 'completeness_score', 'explained_variance', 'f1', 'f1_micro', 'f1_macro', 'f1_samples', 'f1_weighted', 'fowlkes_mallows_score', 'homogeneity_score', 'mutual_info_score', 'normalized_mutual_info_score', 'precision', 'precision_macro', 'precision_micro', 'precision_samples', 'precision_score', 'r2', 'recall', 'recall_macro', 'recall_micro', 'recall_samples', 'recall_weighted', 'roc_auc', 'v_measure_score']
```
Note: The values listed by the ValueError exception correspond to the functions measuring prediction accuracy described in the following sections. The scorer objects for those functions are stored in the dictionary sklearn.metrics.SCORERS.

Defining your scoring strategy from metric functions

The module sklearn.metrics also exposes a set of simple functions measuring a prediction error given ground truth and prediction:

- functions ending with _score return a value to maximize, the higher the better.
- functions ending with _error or _loss return a value to minimize, the lower the better. When converting into a scorer object using make_scorer, set the greater_is_better parameter to False (True by default; see the parameter description below).

Metrics available for various machine learning tasks are detailed in sections below.

Many metrics are not given names to be used as scoring values, sometimes because they require additional parameters, such as fbeta_score. In such cases, you need to generate an appropriate scoring object. The simplest way to generate a callable object for scoring is by using make_scorer. That function converts metrics into callables that can be used for model evaluation.

One typical use case is to wrap an existing metric function from the library with non-default values for its parameters, such as the beta parameter for the fbeta_score function:

```python
>>> from sklearn.metrics import fbeta_score, make_scorer
>>> ftwo_scorer = make_scorer(fbeta_score, beta=2)
>>> from sklearn.model_selection import GridSearchCV
>>> from sklearn.svm import LinearSVC
>>> grid = GridSearchCV(LinearSVC(), param_grid={'C': [1, 10]}, scoring=ftwo_scorer)
```

The second use case is to build a completely custom scorer object from a simple python function using make_scorer, which can take several parameters:

- the python function you want to use (my_custom_loss_func in the example below)
- whether the python function returns a score (greater_is_better=True, the default) or a loss (greater_is_better=False). If a loss, the output of the python function is negated by the scorer object, conforming to the cross validation convention that scorers return higher values for better models.
- for classification metrics only: whether the python function you provided requires continuous decision certainties (needs_threshold=True). The default value is False.
- any additional parameters, such as beta or labels in f1_score.

Here is an example of building custom scorers, and of using the greater_is_better parameter:

```python
>>> import numpy as np
>>> def my_custom_loss_func(ground_truth, predictions):
...     diff = np.abs(ground_truth - predictions).max()
...     return np.log(1 + diff)
... # loss_func will negate the return value of my_custom_loss_func,
... # which will be np.log(2), 0.693, given the values for ground_truth
... # and predictions defined below.
... loss = make_scorer(my_custom_loss_func, greater_is_better=False)
```
Implementing your own scoring object

You can generate even more flexible model scorers by constructing your own scoring object from scratch, without using the `make_scorer` factory. For a callable to be a scorer, it needs to meet the protocol specified by the following two rules:

- It can be called with parameters `(estimator, X, y)`, where `estimator` is the model that should be evaluated, `X` is validation data, and `y` is the ground truth target for `X` (in the supervised case) or `None` (in the unsupervised case).
- It returns a floating point number that quantifies the `estimator` prediction quality on `X`, with reference to `y`. Again, by convention higher numbers are better, so if your scorer returns loss, that value should be negated.

Using multiple metric evaluation

Scikit-learn also permits evaluation of multiple metrics in `GridSearchCV`, `RandomizedSearchCV` and `cross_validate`.

There are two ways to specify multiple scoring metrics for the `scoring` parameter:

- As an iterable of string metrics:

  ```python
  >>> scoring = ['accuracy', 'precision']
  ```

- As a dict mapping the scorer name to the scoring function:

  ```python
  >>> from sklearn.metrics import accuracy_score
  >>> from sklearn.metrics import make_scorer
  >>> scoring = {'accuracy': make_scorer(accuracy_score),
               'prec': 'precision'}
  ```

Note that the dict values can either be scorer functions or one of the predefined metric strings.

Currently only those scorer functions that return a single score can be passed inside the dict. Scorer functions that return multiple values are not permitted and will require a wrapper to return a single metric:

```python
>>> from sklearn.model_selection import cross_validate
>>> from sklearn.metrics import confusion_matrix
>>> # A sample toy binary classification dataset
>>> X, y = datasets.make_classification(n_classes=2, random_state=0)
>>> svm = LinearSVC(random_state=0)
>>> def tp(y_true, y_pred): return confusion_matrix(y_true, y_pred)[0, 0]
>>> def tn(y_true, y_pred): return confusion_matrix(y_true, y_pred)[0, 0]
>>> def fp(y_true, y_pred): return confusion_matrix(y_true, y_pred)[1, 0]
>>> def fn(y_true, y_pred): return confusion_matrix(y_true, y_pred)[0, 1]
```
scikit-learn user guide, Release 0.20.dev0

```python
>>> scoring = {'tp': make_scorer(tp), 'tn': make_scorer(tn),
             'fp': make_scorer(fp), 'fn': make_scorer(fn)}
>>> cv_results = cross_validate(svm.fit(X, y), X, y, scoring=scoring)

# Getting the test set true positive scores
>>> print(cv_results['test_tp'])
[12 13 15]

# Getting the test set false negative scores
>>> print(cv_results['test_fn'])
[5 4 1]
```

## Classification metrics

The `sklearn.metrics` module implements several loss, score, and utility functions to measure classification performance. Some metrics might require probability estimates of the positive class, confidence values, or binary decisions values. Most implementations allow each sample to provide a weighted contribution to the overall score, through the `sample_weight` parameter.

Some of these are restricted to the binary classification case:

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>precision_recall_curve</code></td>
<td>Compute precision-recall pairs for different probability thresholds</td>
</tr>
<tr>
<td><code>roc_curve</code></td>
<td>Compute Receiver operating characteristic (ROC)</td>
</tr>
<tr>
<td><code>balanced_accuracy_score</code></td>
<td>Compute the balanced accuracy</td>
</tr>
</tbody>
</table>

Others also work in the multiclass case:

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>cohen_kappa_score</code></td>
<td>Cohen’s kappa: a statistic that measures inter-annotator agreement.</td>
</tr>
<tr>
<td><code>confusion_matrix</code></td>
<td>Compute confusion matrix to evaluate the accuracy of a classification</td>
</tr>
<tr>
<td><code>hinge_loss</code></td>
<td>Average hinge loss (non-regularized)</td>
</tr>
<tr>
<td><code>matthews_corrcoef</code></td>
<td>Compute the Matthews correlation coefficient (MCC)</td>
</tr>
</tbody>
</table>

Some also work in the multilabel case:

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>accuracy_score</code></td>
<td>Accuracy classification score.</td>
</tr>
<tr>
<td><code>classification_report</code></td>
<td>Build a text report showing the main classification metrics</td>
</tr>
<tr>
<td><code>f1_score</code></td>
<td>Compute the F1 score, also known as balanced F-score or F-measure</td>
</tr>
<tr>
<td><code>fbeta_score</code></td>
<td>Compute the F-beta score</td>
</tr>
<tr>
<td><code>hamming_loss</code></td>
<td>Compute the average Hamming loss.</td>
</tr>
<tr>
<td><code>jaccard_similarity_score</code></td>
<td>Jaccard similarity coefficient score</td>
</tr>
<tr>
<td><code>log_loss</code></td>
<td>Log loss, aka logistic loss or cross-entropy loss.</td>
</tr>
<tr>
<td><code>precision_recall_fscore_support</code></td>
<td>Compute precision, recall, F-measure and support for each class</td>
</tr>
<tr>
<td><code>precision_score</code></td>
<td>Compute precision.</td>
</tr>
<tr>
<td><code>recall_score</code></td>
<td>Compute the recall</td>
</tr>
<tr>
<td><code>zero_one_loss</code></td>
<td>Zero-one classification loss.</td>
</tr>
</tbody>
</table>

And some work with binary and multilabel (but not multiclass) problems:
In the following sub-sections, we will describe each of those functions, preceded by some notes on common API and metric definition.

### From binary to multiclass and multilabel

Some metrics are essentially defined for binary classification tasks (e.g. `f1_score`, `roc_auc_score`). In these cases, by default only the positive label is evaluated, assuming by default that the positive class is labelled 1 (though this may be configurable through the `pos_label` parameter). In extending a binary metric to multiclass or multilabel problems, the data is treated as a collection of binary problems, one for each class. There are then a number of ways to average binary metric calculations across the set of classes, each of which may be useful in some scenario. Where available, you should select among these using the `average` parameter.

- **"macro"** simply calculates the mean of the binary metrics, giving equal weight to each class. In problems where infrequent classes are nonetheless important, macro-averaging may be a means of highlighting their performance. On the other hand, the assumption that all classes are equally important is often untrue, such that macro-averaging will over-emphasize the typically low performance on an infrequent class.
- **"weighted"** accounts for class imbalance by computing the average of binary metrics in which each class’s score is weighted by its presence in the true data sample.
- **"micro"** gives each sample-class pair an equal contribution to the overall metric (except as a result of sample-weight). Rather than summing the metric per class, this sums the dividends and divisors that make up the per-class metrics to calculate an overall quotient. Micro-averaging may be preferred in multiclass settings, including multiclass classification where a majority class is to be ignored.
- **"samples"** applies only to multilabel problems. It does not calculate a per-class measure, instead calculating the metric over the true and predicted classes for each sample in the evaluation data, and returning their (sample_weight-weighted) average.
- Selecting `average=None` will return an array with the score for each class.

While multiclass data is provided to the metric, like binary targets, as an array of class labels, multilabel data is specified as an indicator matrix, in which cell $[i, j]$ has value 1 if sample $i$ has label $j$ and value 0 otherwise.

### Accuracy score

The `accuracy_score` function computes the accuracy, either the fraction (default) or the count (normalize=False) of correct predictions.

In multilabel classification, the function returns the subset accuracy. If the entire set of predicted labels for a sample strictly match with the true set of labels, then the subset accuracy is 1.0; otherwise it is 0.0.

If $\hat{y}_i$ is the predicted value of the $i$-th sample and $y_i$ is the corresponding true value, then the fraction of correct predictions over $n_{\text{samples}}$ is defined as

$$\text{accuracy}(y, \hat{y}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} 1(\hat{y}_i = y_i)$$

where $1(x)$ is the indicator function.
In the multilabel case with binary label indicators:

```python
>>> accuracy_score(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
```

Example:

- See *Test with permutations the significance of a classification score* for an example of accuracy score usage using permutations of the dataset.

### Balanced accuracy score

The `balanced_accuracy_score` function computes the balanced accuracy, which avoids inflated performance estimates on imbalanced datasets. It is defined as the arithmetic mean of sensitivity (true positive rate) and specificity (true negative rate), or the average of recall scores obtained on either class.

If the classifier performs equally well on either class, this term reduces to the conventional accuracy (i.e., the number of correct predictions divided by the total number of predictions). In contrast, if the conventional accuracy is above chance only because the classifier takes advantage of an imbalanced test set, then the balanced accuracy, as appropriate, will drop to 50%.

If \( \hat{y}_i \in \{0, 1\} \) is the predicted value of the \( i \)-th sample and \( y_i \in \{0, 1\} \) is the corresponding true value, then the balanced accuracy is defined as

\[
\text{balanced-accuracy}(y, \hat{y}) = \frac{1}{2} \left( \frac{\sum_i 1(\hat{y}_i = 1 \land y_i = 1)}{\sum_i 1(y_i = 1)} + \frac{\sum_i 1(\hat{y}_i = 0 \land y_i = 0)}{\sum_i 1(y_i = 0)} \right)
\]

where \( 1(x) \) is the indicator function.

Under this definition, the balanced accuracy coincides with `roc_auc_score` given binary \( y_{\text{true}} \) and \( y_{\text{pred}} \):

```python
>>> import numpy as np
>>> from sklearn.metrics import balanced_accuracy_score, roc_auc_score
>>> y_true = [0, 1, 0, 0, 1, 0]
>>> y_pred = [0, 1, 0, 0, 0, 1]
>>> balanced_accuracy_score(y_true, y_pred)
0.625
>>> roc_auc_score(y_true, y_pred)
0.625
```

(but in general, `roc_auc_score` takes as its second argument non-binary scores).

**Note:** Currently this score function is only defined for binary classification problems, you may need to wrap it by yourself if you want to use it for multilabel problems.
There is no clear consensus on the definition of a balanced accuracy for the multiclass setting. Here are some definitions that can be found in the literature:

- Normalized class-wise accuracy average as described in [Guyon2015]: for multi-class classification problem, each sample is assigned the class with maximum prediction value. The predictions are then binarized to compute the accuracy of each class on a one-vs-rest fashion. The balanced accuracy is obtained by averaging the individual accuracies over all classes and then normalized by the expected value of balanced accuracy for random predictions (0.5 for binary classification, $1/C$ for $C$-class classification problem).

- Macro-average recall as described in [Mosley2013] and [Kelleher2015]: the recall for each class is computed independently and the average is taken over all classes.

Note that none of these different definitions are currently implemented within the `balanced_accuracy_score` function. However, the macro-averaged recall is implemented in `sklearn.metrics.recall_score`: set `average` parameter to "macro".

### References:

**Cohen’s kappa**

The function `cohen_kappa_score` computes Cohen’s kappa statistic. This measure is intended to compare labelings by different human annotators, not a classifier versus a ground truth.

The kappa score (see docstring) is a number between -1 and 1. Scores above .8 are generally considered good agreement; zero or lower means no agreement (practically random labels).

Kappa scores can be computed for binary or multiclass problems, but not for multilabel problems (except by manually computing a per-label score) and not for more than two annotators.

```python
>>> from sklearn.metrics import cohen_kappa_score
>>> y_true = [2, 0, 2, 2, 0, 1]
>>> y_pred = [0, 0, 2, 2, 0, 2]
>>> cohen_kappa_score(y_true, y_pred)
0.4285714285714286
```

**Confusion matrix**

The `confusion_matrix` function evaluates classification accuracy by computing the confusion matrix.

By definition, entry $i, j$ in a confusion matrix is the number of observations actually in group $i$, but predicted to be in group $j$. Here is an example:

```python
>>> from sklearn.metrics import confusion_matrix
>>> y_true = [2, 0, 2, 2, 0, 1]
>>> y_pred = [0, 0, 2, 2, 0, 2]
>>> confusion_matrix(y_true, y_pred)
array([[2, 0, 0],
       [0, 0, 1],
       [1, 0, 2]])
```

Here is a visual representation of such a confusion matrix (this figure comes from the `Confusion matrix` example):
For binary problems, we can get counts of true negatives, false positives, false negatives and true positives as follows:

```python
>>> y_true = [0, 0, 0, 1, 1, 1, 1, 1]
>>> y_pred = [0, 1, 0, 1, 0, 1, 0, 1]
>>> tn, fp, fn, tp = confusion_matrix(y_true, y_pred).ravel()
>>> tn, fp, fn, tp
(2, 1, 2, 3)
```

**Example:**

- See `Confusion matrix` for an example of using a confusion matrix to evaluate classifier output quality.
- See `Recognizing hand-written digits` for an example of using a confusion matrix to classify hand-written digits.
- See `Classification of text documents using sparse features` for an example of using a confusion matrix to classify text documents.

### Classification report

The `classification_report` function builds a text report showing the main classification metrics. Here is a small example with custom `target_names` and inferred labels:

```python
>>> from sklearn.metrics import classification_report
>>> y_true = [0, 1, 2, 2, 0]
>>> y_pred = [0, 0, 2, 1, 0]
>>> target_names = ['class 0', 'class 1', 'class 2']
>>> print(classification_report(y_true, y_pred, target_names=target_names))
precision    recall    f1-score    support
    class 0   0.67    1.00    0.80    2
```

3.3. Model selection and evaluation
Hamming loss

The `hamming_loss` computes the average Hamming loss or Hamming distance between two sets of samples. If \( \hat{y}_j \) is the predicted value for the \( j \)-th label of a given sample, \( y_j \) is the corresponding true value, and \( n_{\text{labels}} \) is the number of classes or labels, then the Hamming loss \( L_{\text{Hamming}} \) between two samples is defined as:

\[
L_{\text{Hamming}}(y, \hat{y}) = \frac{1}{n_{\text{labels}}} \sum_{j=0}^{n_{\text{labels}}-1} 1(\hat{y}_j \neq y_j)
\]

where \( 1(x) \) is the indicator function.

```python
>>> from sklearn.metrics import hamming_loss
>>> y_pred = [1, 2, 3, 4]
>>> y_true = [2, 2, 3, 4]
>>> hamming_loss(y_true, y_pred)
0.25
```

In the multilabel case with binary label indicators:

```python
>>> hamming_loss(np.array([ [0, 1], [1, 1] ]), np.zeros((2, 2)))
0.75
```

**Note:** In multiclass classification, the Hamming loss corresponds to the Hamming distance between \( y_{\text{true}} \) and \( y_{\text{pred}} \) which is similar to the Zero one loss function. However, while zero-one loss penalizes prediction sets that do not strictly match true sets, the Hamming loss penalizes individual labels. Thus the Hamming loss, upper bounded by the zero-one loss, is always between zero and one, inclusive; and predicting a proper subset or superset of the true labels will give a Hamming loss between zero and one, exclusive.

Jaccard similarity coefficient score

The `jaccard_similarity_score` function computes the average (default) or sum of Jaccard similarity coefficients, also called the Jaccard index, between pairs of label sets.
The Jaccard similarity coefficient of the $i$-th samples, with a ground truth label set $y_i$ and predicted label set $\hat{y}_i$, is defined as

$$J(y_i, \hat{y}_i) = \frac{|y_i \cap \hat{y}_i|}{|y_i \cup \hat{y}_i|}.$$  

In binary and multiclass classification, the Jaccard similarity coefficient score is equal to the classification accuracy.

```python
>>> import numpy as np
>>> from sklearn.metrics import jaccard_similarity_score
>>> y_pred = [0, 2, 1, 3]
>>> y_true = [0, 1, 2, 3]
>>> jaccard_similarity_score(y_true, y_pred)
0.5
>>> jaccard_similarity_score(y_true, y_pred, normalize=False)
2
```

In the multi-label case with binary label indicators:

```python
>>> jaccard_similarity_score(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.75
```

### Precision, recall and F-measures

Intuitively, **precision** is the ability of the classifier not to label as positive a sample that is negative, and **recall** is the ability of the classifier to find all the positive samples.

The **F-measure** ($F_\beta$ and $F_1$ measures) can be interpreted as a weighted harmonic mean of the precision and recall. A $F_\beta$ measure reaches its best value at 1 and its worst score at 0. With $\beta = 1$, $F_\beta$ and $F_1$ are equivalent, and the recall and the precision are equally important.

The **precision_recall_curve** computes a precision-recall curve from the ground truth label and a score given by the classifier by varying a decision threshold.

The **average_precision_score** function computes the average precision (AP) from prediction scores. The value is between 0 and 1 and higher is better. AP is defined as

$$AP = \sum_n (R_n - R_{n-1}) P_n$$

where $P_n$ and $R_n$ are the precision and recall at the nth threshold. With random predictions, the AP is the fraction of positive samples.

References [Manning2008] and [Everingham2010] present alternative variants of AP that interpolate the precision-recall curve. Currently, **average_precision_score** does not implement any interpolated variant. References [Davis2006] and [Flach2015] describe why a linear interpolation of points on the precision-recall curve provides an overly-optimistic measure of classifier performance. This linear interpolation is used when computing area under the curve with the trapezoidal rule in **auc**.

Several functions allow you to analyze the precision, recall and F-measures score:

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>average_precision_score(y_true, y_score[, ...])</code></td>
<td>Compute average precision (AP) from prediction scores</td>
</tr>
<tr>
<td><code>f1_score(y_true, y_pred[, labels, ...])</code></td>
<td>Compute the F1 score, also known as balanced F-score or F-measure</td>
</tr>
<tr>
<td><code>fbeta_score(y_true, y_pred, beta[, labels, ...])</code></td>
<td>Compute the F-beta score</td>
</tr>
<tr>
<td><code>precision_recall_curve(y_true, probas_pred)</code></td>
<td>Compute precision-recall pairs for different probability thresholds</td>
</tr>
</tbody>
</table>

Continued on next page
Table 3.33 – continued from previous page

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>precision_recall_fscore_support</td>
<td>Compute precision, recall, F-measure and support for each class</td>
</tr>
<tr>
<td>precision_score</td>
<td>Compute the precision</td>
</tr>
<tr>
<td>recall_score</td>
<td>Compute the recall</td>
</tr>
</tbody>
</table>

Note that the `precision_recall_curve` function is restricted to the binary case. The `average_precision_score` function works only in binary classification and multilabel indicator format.

**Examples:**

- See [Classification of text documents using sparse features](#) for an example of `f1_score` usage to classify text documents.
- See [Parameter estimation using grid search with cross-validation](#) for an example of `precision_score` and `recall_score` usage to estimate parameters using grid search with nested cross-validation.
- See [Precision-Recall](#) for an example of `precision_recall_curve` usage to evaluate classifier output quality.

**References:**

**Binary classification**

In a binary classification task, the terms “positive” and “negative” refer to the classifier’s prediction, and the terms “true” and “false” refer to whether that prediction corresponds to the external judgment (sometimes known as the “observation”). Given these definitions, we can formulate the following table:

<table>
<thead>
<tr>
<th>Predicted class (expectation)</th>
<th>Actual class (observation)</th>
</tr>
</thead>
<tbody>
<tr>
<td>tp (true positive) Correct result</td>
<td>fp (false positive) Unexpected result</td>
</tr>
<tr>
<td>fn (false negative) Missing result</td>
<td>tn (true negative) Correct absence of result</td>
</tr>
</tbody>
</table>

In this context, we can define the notions of precision, recall and F-measure:

\[
\text{precision} = \frac{tp}{tp + fp},
\]

\[
\text{recall} = \frac{tp}{tp + fn},
\]

\[
F_\beta = (1 + \beta^2) \frac{\text{precision} \times \text{recall}}{\beta^2 \text{precision} + \text{recall}}
\]

Here are some small examples in binary classification:

```python
>>> from sklearn import metrics
>>> y_pred = [0, 1, 0, 0]
>>> y_true = [0, 1, 0, 1]
>>> metrics.precision_score(y_true, y_pred)
1.0
>>> metrics.recall_score(y_true, y_pred)
0.5
```
```python
>>> metrics.f1_score(y_true, y_pred)
0.66...
>>> metrics.fbeta_score(y_true, y_pred, beta=0.5)
0.83...
>>> metrics.fbeta_score(y_true, y_pred, beta=1)
0.66...
>>> metrics.fbeta_score(y_true, y_pred, beta=2)
0.55...
>>> metrics.precision_recall_fscore_support(y_true, y_pred, beta=0.5)
(array([ 0.66..., 1.]), array([ 1. , 0.5]), array([ 0.71..., 0.83...]),
 array([2, 2]...))
>>> import numpy as np
>>> from sklearn.metrics import precision_recall_curve
>>> from sklearn.metrics import average_precision_score

>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])

>>> precision, recall, threshold = precision_recall_curve(y_true, y_scores)

>>> precision
array([ 0.66..., 0.5 , 1. , 1. ])
>>> recall
array([ 1. , 0.5, 0.5, 0. ])
>>> threshold
array([ 0.35, 0.4 , 0.8 ])
>>> average_precision_score(y_true, y_scores)
0.83...
```

**Multiclass and multilabel classification**

In multiclass and multilabel classification task, the notions of precision, recall, and F-measures can be applied to each label independently. There are a few ways to combine results across labels, specified by the `average` argument to the `average_precision_score` (multilabel only), `f1_score`, `fbeta_score`, `precision_recall_fscore_support`, `precision_score` and `recall_score` functions, as described above. Note that for “micro”-averaging in a multiclass setting with all labels included will produce equal precision, recall and F, while “weighted” averaging may produce an F-score that is not between precision and recall.

To make this more explicit, consider the following notation:

- $y$ the set of predicted $(sample, label)$ pairs
- $\hat{y}$ the set of true $(sample, label)$ pairs
- $L$ the set of labels
- $S$ the set of samples
- $y_s$ the subset of $y$ with sample $s$, i.e. $y_s := \{(s', l) \in y | s' = s\}$
- $y_l$ the subset of $y$ with label $l$
- similarly, $\hat{y}_s$ and $\hat{y}_l$ are subsets of $\hat{y}$
- $P(A, B) := \frac{|A \cap B|}{|A|}$
- $R(A, B) := \frac{|A \cap B|}{|B|}$ (Conventions vary on handling $B = \emptyset$; this implementation uses $R(A, B) := 0$, and similar for $P$.)
- $F_\beta(A, B) := (1 + \beta^2) \frac{P(A, B) \times R(A, B)}{\beta^2 P(A, B) + R(A, B)}$
Then the metrics are defined as:

<table>
<thead>
<tr>
<th>average</th>
<th>Precision</th>
<th>Recall</th>
<th>F_beta</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot;micro&quot;</td>
<td>( P(y, \hat{y}) )</td>
<td>( R(y, \hat{y}) )</td>
<td>( F_\beta(y, \hat{y}) )</td>
</tr>
<tr>
<td>&quot;samples&quot;</td>
<td>( \frac{1}{</td>
<td>S</td>
<td>} \sum_{s \in S} P(y_s, \hat{y}_s) )</td>
</tr>
<tr>
<td>&quot;macro&quot;</td>
<td>( \frac{1}{</td>
<td>L</td>
<td>} \sum_{l \in L} P(y_l, \hat{y}_l) )</td>
</tr>
<tr>
<td>&quot;weighted&quot;</td>
<td>( \frac{1}{\sum_{l \in L}</td>
<td>y_l</td>
<td>} \sum_{l \in L}</td>
</tr>
<tr>
<td>None</td>
<td>\langle P(y_l, \hat{y}_l) \rangle \in L \rangle</td>
<td>\langle R(y_l, \hat{y}_l) \rangle \in L \rangle</td>
<td>\langle F_\beta(y_l, \hat{y}_l) \rangle \in L \rangle</td>
</tr>
</tbody>
</table>

```python
>>> from sklearn import metrics

>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]

>>> metrics.precision_score(y_true, y_pred, average='macro')
0.22...

>>> metrics.recall_score(y_true, y_pred, average='micro')
0.33...

>>> metrics.f1_score(y_true, y_pred, average='weighted')
0.26...

>>> metrics.fbeta_score(y_true, y_pred, average='macro', beta=0.5)
0.23...

>>> metrics.precision_recall_fscore_support(y_true, y_pred, beta=0.5, average=None)
... (array([ 0.66..., 0. , 0. ]), array([1. , 0. , 0. ]), array([0.71..., 0. , 0. ]), array([2. , 2. , 2. ]))
```

For multiclass classification with a “negative class”, it is possible to exclude some labels:

```python
>>> metrics.recall_score(y_true, y_pred, labels=[1, 2], average='micro')
... # excluding 0, no labels were correctly recalled
0.0
```

Similarly, labels not present in the data sample may be accounted for in macro-averaging.

```python
>>> metrics.precision_score(y_true, y_pred, labels=[0, 1, 2, 3], average='macro')
... 0.166...
```

### Hinge loss

The `hinge_loss` function computes the average distance between the model and the data using hinge loss, a one-sided metric that considers only prediction errors. (Hinge loss is used in maximal margin classifiers such as support vector machines.)

If the labels are encoded with +1 and -1, \( y \): is the true value, and \( w \) is the predicted decisions as output by decision_function, then the hinge loss is defined as:

\[
L_{\text{Hinge}}(y, w) = \max \{ 1 - wy, 0 \} = |1 - wy|_+
\]

If there are more than two labels, `hinge_loss` uses a multiclass variant due to Crammer & Singer. Here is the paper describing it.

If \( y_w \) is the predicted decision for true label and \( y_t \) is the maximum of the predicted decisions for all other labels, where predicted decisions are output by decision function, then multiclass hinge loss is defined by:

\[
L_{\text{Hinge}}(y_w, y_t) = \max \{ 1 + y_t - y_w, 0 \}
\]
Here is a small example demonstrating the use of the `hinge_loss` function with a svm classifier in a binary class problem:

```python
>>> from sklearn import svm
>>> from sklearn.metrics import hinge_loss
>>> X = [[0], [1]]
>>> y = [-1, 1]
>>> est = svm.LinearSVC(random_state=0)
>>> est.fit(X, y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
         intercept_scaling=1, loss='squared_hinge', max_iter=1000,
         multi_class='ovr', penalty='l2', random_state=0, tol=0.0001,
         verbose=0)
>>> pred_decision = est.decision_function([[-2], [3], [0.5]])
>>> pred_decision
array([-2.18..., 2.36..., 0.09...])
>>> hinge_loss([-1, 1, 1], pred_decision)
0.3...
```

Here is an example demonstrating the use of the `hinge_loss` function with a svm classifier in a multiclass problem:

```python
>>> X = np.array([[0], [1], [2], [3]])
>>> Y = np.array([0, 1, 2, 3])
>>> labels = np.array([0, 1, 2, 3])
>>> est = svm.LinearSVC()
>>> est.fit(X, Y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
         intercept_scaling=1, loss='squared_hinge', max_iter=1000,
         multi_class='ovr', penalty='l2', random_state=None, tol=0.0001,
         verbose=0)
>>> pred_decision = est.decision_function([[-1], [2], [3]])
>>> y_true = [0, 2, 3]
>>> hinge_loss(y_true, pred_decision, labels)
0.56...
```

**Log loss**

Log loss, also called logistic regression loss or cross-entropy loss, is defined on probability estimates. It is commonly used in (multinomial) logistic regression and neural networks, as well as in some variants of expectation-maximization, and can be used to evaluate the probability outputs (`predict_proba`) of a classifier instead of its discrete predictions.

For binary classification with a true label $y \in \{0, 1\}$ and a probability estimate $p = \Pr(y = 1)$, the log loss per sample is the negative log-likelihood of the classifier given the true label:

$$ L_{\log}(y, p) = - \log \Pr(y | p) = -(y \log(p) + (1 - y) \log(1 - p)) $$

This extends to the multiclass case as follows. Let the true labels for a set of samples be encoded as a 1-of-K binary indicator matrix $Y$, i.e., $y_{i,k} = 1$ if sample $i$ has label $k$ taken from a set of $K$ labels. Let $P$ be a matrix of probability estimates, with $p_{i,k} = \Pr(t_{i,k} = 1)$. Then the log loss of the whole set is

$$ L_{\log}(Y, P) = - \log \Pr(Y | P) = - \frac{1}{N} \sum_{i=0}^{N-1} \sum_{k=0}^{K-1} y_{i,k} \log p_{i,k} $$

To see how this generalizes the binary log loss given above, note that in the binary case, $p_{i,0} = 1 - p_{i,1}$ and $y_{i,0} = 1 - y_{i,1}$, so expanding the inner sum over $y_{i,k} \in \{0, 1\}$ gives the binary log loss.
The `log_loss` function computes log loss given a list of ground-truth labels and a probability matrix, as returned by an estimator’s `predict_proba` method.

```python
>>> from sklearn.metrics import log_loss
>>> y_true = [0, 0, 1, 1]
>>> y_pred = [[.9, .1], [.8, .2], [.3, .7], [.01, .99]]
>>> log_loss(y_true, y_pred)
0.1738...
```

The first `[.9, .1]` in `y_pred` denotes 90% probability that the first sample has label 0. The log loss is non-negative.

Mathews correlation coefficient

The `matthews_corrcoef` function computes the Mathew’s correlation coefficient (MCC) for binary classes. Quoting Wikipedia:

“The Matthews correlation coefficient is used in machine learning as a measure of the quality of binary (two-class) classifications. It takes into account true and false positives and negatives and is generally regarded as a balanced measure which can be used even if the classes are of very different sizes. The MCC is in essence a correlation coefficient value between -1 and +1. A coefficient of +1 represents a perfect prediction, 0 an average random prediction and -1 an inverse prediction. The statistic is also known as the phi coefficient.”

In the binary (two-class) case, $tp$, $tn$, $fp$ and $fn$ are respectively the number of true positives, true negatives, false positives and false negatives, the MCC is defined as

$$ MCC = \frac{tp \times tn - fp \times fn}{\sqrt{(tp + fp)(tp + fn)(tn + fp)(tn + fn)}} $$

In the multiclass case, the Matthews correlation coefficient can be defined in terms of a confusion matrix $C$ for $K$ classes. To simplify the definition consider the following intermediate variables:

- $t_k = \sum_i^K C_{ik}$ the number of times class $k$ truly occurred,
- $p_k = \sum_i^K C_{ki}$ the number of times class $k$ was predicted,
- $c = \sum_k^K C_{kk}$ the total number of samples correctly predicted,
- $s = \sum_i^K \sum_j^K C_{ij}$ the total number of samples.

Then the multiclass MCC is defined as:

$$ MCC = \frac{c \times s - \sum_k^K p_k \times t_k}{\sqrt{(s^2 - \sum_k^K p_k^2) \times (s^2 - \sum_k^K t_k^2)}} $$

When there are more than two labels, the value of the MCC will no longer range between -1 and +1. Instead the minimum value will be somewhere between -1 and 0 depending on the number and distribution of ground true labels. The maximum value is always +1.

Here is a small example illustrating the usage of the `matthews_corrcoef` function:

```python
>>> from sklearn.metrics import matthews_corrcoef
>>> y_true = [+1, +1, +1, -1]
>>> y_pred = [+1, -1, +1, +1]
>>> matthews_corrcoef(y_true, y_pred)
-0.33...
```
Receiver operating characteristic (ROC)

The function `roc_curve` computes the receiver operating characteristic curve, or ROC curve. Quoting Wikipedia:

“A receiver operating characteristic (ROC), or simply ROC curve, is a graphical plot which illustrates the performance of a binary classifier system as its discrimination threshold is varied. It is created by plotting the fraction of true positives out of the positives (TPR = true positive rate) vs. the fraction of false positives out of the negatives (FPR = false positive rate), at various threshold settings. TPR is also known as sensitivity, and FPR is one minus the specificity or true negative rate.”

This function requires the true binary value and the target scores, which can either be probability estimates of the positive class, confidence values, or binary decisions. Here is a small example of how to use the `roc_curve` function:

```python
>>> import numpy as np
>>> from sklearn.metrics import roc_curve
>>> y = np.array([1, 1, 2, 2])
>>> scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> fpr, tpr, thresholds = roc_curve(y, scores, pos_label=2)
>>> fpr
array([ 0. , 0.5, 0.5, 1. ])
>>> tpr
array([ 0.5, 0.5, 1. , 1. ])
>>> thresholds
array([ 0.8 , 0.4 , 0.35, 0.1 ])
```

This figure shows an example of such an ROC curve:

The `roc_auc_score` function computes the area under the receiver operating characteristic (ROC) curve, which is also denoted by AUC or AUROC. By computing the area under the roc curve, the curve information is summarized in one number. For more information see the Wikipedia article on AUC.

```python
>>> import numpy as np
>>> from sklearn.metrics import roc_auc_score
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> roc_auc_score(y_true, y_scores)
0.79
```
In multi-label classification, the `roc_auc_score` function is extended by averaging over the labels as above.

Compared to metrics such as the subset accuracy, the Hamming loss, or the F1 score, ROC doesn’t require optimizing a threshold for each label. The `roc_auc_score` function can also be used in multi-class classification, if the predicted outputs have been binarized.

Examples:

- See Receiver Operating Characteristic (ROC) for an example of using ROC to evaluate the quality of the output of a classifier.
- See Receiver Operating Characteristic (ROC) with cross validation for an example of using ROC to evaluate classifier output quality, using cross-validation.
- See Species distribution modeling for an example of using ROC to model species distribution.

**Zero one loss**

The `zero_one_loss` function computes the sum or the average of the 0-1 classification loss ($L_{0-1}$) over $n_{samples}$. By default, the function normalizes over the sample. To get the sum of the $L_{0-1}$, set `normalize` to `False`.

In multilabel classification, the `zero_one_loss` scores a subset as one if its labels strictly match the predictions, and as a zero if there are any errors. By default, the function returns the percentage of imperfectly predicted subsets. To get the count of such subsets instead, set `normalize` to `False`.

If $\hat{y}_i$ is the predicted value of the $i$-th sample and $y_i$ is the corresponding true value, then the 0-1 loss $L_{0-1}$ is defined as:

$$L_{0-1}(y_i, \hat{y}_i) = 1(\hat{y}_i \neq y_i)$$

where $1(x)$ is the indicator function.
In the multilabel case with binary label indicators, where the first label set [0,1] has an error:

```python
>>> zero_one_loss(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
>>> zero_one_loss(np.array([[0, 1], [1, 1]]), np.ones((2, 2)), normalize=False)
1
```

Example:

- See *Recursive feature elimination with cross-validation* for an example of zero one loss usage to perform recursive feature elimination with cross-validation.

**Brier score loss**

The `brier_score_loss` function computes the Brier score for binary classes. Quoting Wikipedia:

“The Brier score is a proper score function that measures the accuracy of probabilistic predictions. It is applicable to tasks in which predictions must assign probabilities to a set of mutually exclusive discrete outcomes.”

This function returns a score of the mean square difference between the actual outcome and the predicted probability of the possible outcome. The actual outcome has to be 1 or 0 (true or false), while the predicted probability of the actual outcome can be a value between 0 and 1.

The brier score loss is also between 0 to 1 and the lower the score (the mean square difference is smaller), the more accurate the prediction is. It can be thought of as a measure of the “calibration” of a set of probabilistic predictions.

\[
BS = \frac{1}{N} \sum_{i=1}^{N} (f_i - o_i)^2
\]

where : \(N\) is the total number of predictions, \(f_i\) is the predicted probability of the actual outcome \(o_i\).

Here is a small example of usage of this function::

```python
>>> import numpy as np
>>> from sklearn.metrics import brier_score_loss
>>> y_true = np.array([0, 1, 1, 0])
>>> y_true_categorical = np.array(["spam", "ham", "ham", "spam"])
>>> y_prob = np.array([0.1, 0.9, 0.8, 0.4])
>>> y_pred = np.array([0, 1, 1, 0])
>>> brier_score_loss(y_true, y_prob)
0.055
>>> brier_score_loss(y_true, 1-y_prob, pos_label=0)
0.055
>>> brier_score_loss(y_true_categorical, y_prob, pos_label="ham")
0.055
```
brier_score_loss(y_true, y_prob > 0.5)

0.0

Example:

- See [Probability calibration of classifiers](#) for an example of Brier score loss usage to perform probability calibration of classifiers.

References:

- G. Brier, Verification of forecasts expressed in terms of probability, Monthly weather review 78.1 (1950)

Multilabel ranking metrics

In multilabel learning, each sample can have any number of ground truth labels associated with it. The goal is to give high scores and better rank to the ground truth labels.

Coverage error

The `coverage_error` function computes the average number of labels that have to be included in the final prediction such that all true labels are predicted. This is useful if you want to know how many top-scored-labels you have to predict in average without missing any true one. The best value of this metrics is thus the average number of true labels.

**Note:** Our implementation’s score is 1 greater than the one given in Tsoumakas et al., 2010. This extends it to handle the degenerate case in which an instance has 0 true labels.

Formally, given a binary indicator matrix of the ground truth labels \( y \in \{0, 1\}^{n_{\text{samples}} \times n_{\text{labels}}} \) and the score associated with each label \( \hat{f} \in \mathbb{R}^{n_{\text{samples}} \times n_{\text{labels}}} \), the coverage is defined as

\[
\text{coverage}(y, \hat{f}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}} - 1} \max_{j: y_{ij} = 1} \text{rank}_{ij}
\]

with \( \text{rank}_{ij} = \left| \left\{ k : \hat{f}_{ik} \geq \hat{f}_{ij} \right\} \right| \). Given the rank definition, ties in \( y_{\text{scores}} \) are broken by giving the maximal rank that would have been assigned to all tied values.

Here is a small example of usage of this function:

```python
>>> import numpy as np
>>> from sklearn.metrics import coverage_error
>>> y_true = np.array([[1, 0, 0], [0, 0, 1]])
>>> y_score = np.array([[0.75, 0.5, 1], [1, 0.2, 0.1]])
>>> coverage_error(y_true, y_score)
2.5
```
Label ranking average precision

The `label_ranking_average_precision_score` function implements label ranking average precision (LRAP). This metric is linked to the `average_precision_score` function, but is based on the notion of label ranking instead of precision and recall.

Label ranking average precision (LRAP) is the average over each ground truth label assigned to each sample, of the ratio of true vs. total labels with lower score. This metric will yield better scores if you are able to give better rank to the labels associated with each sample. The obtained score is always strictly greater than 0, and the best value is 1. If there is exactly one relevant label per sample, label ranking average precision is equivalent to the mean reciprocal rank.

Formally, given a binary indicator matrix of the ground truth labels \( y \in \mathcal{R}^{n_{\text{samples}} \times n_{\text{labels}}} \) and the score associated with each label \( \hat{f} \in \mathcal{R}^{n_{\text{samples}} \times n_{\text{labels}}} \), the average precision is defined as

\[
LRAP(y, \hat{f}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} \frac{1}{|y_i|} \sum_{j: y_{ij} = 1} \frac{|L_{ij}|}{\text{rank}_{ij}}
\]

with \( L_{ij} = \{ k : y_{ik} = 1, \hat{f}_{ik} \geq \hat{f}_{ij} \} \), \( \text{rank}_{ij} = |\{ k : \hat{f}_{ik} \geq \hat{f}_{ij} \}| \) and \( |\cdot| \) is the \( \ell_0 \) norm or the cardinality of the set.

Here is a small example of usage of this function:

```python
>>> from sklearn.metrics import label_ranking_average_precision_score
>>> y_true = np.array([[1, 0, 0], [0, 0, 1]])
>>> y_score = np.array([[0.75, 0.5, 1], [1, 0.2, 0.1]])
>>> label_ranking_average_precision_score(y_true, y_score)
0.416...
```

Ranking loss

The `label_ranking_loss` function computes the ranking loss which averages over the samples the number of label pairs that are incorrectly ordered, i.e. true labels have a lower score than false labels, weighted by the inverse number of false and true labels. The lowest achievable ranking loss is zero.

Formally, given a binary indicator matrix of the ground truth labels \( y \in \{0, 1\}^{n_{\text{samples}} \times n_{\text{labels}}} \) and the score associated with each label \( \hat{f} \in \mathcal{R}^{n_{\text{samples}} \times n_{\text{labels}}} \), the ranking loss is defined as

\[
\text{ranking_loss}(y, \hat{f}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} \frac{1}{|y_i| (n_{\text{labels}} - |y_i|)} \left| \left\{ (k, l) : \hat{f}_{ik} < \hat{f}_{il}, y_{ik} = 1, y_{il} = 0 \right\} \right|
\]

where \( |\cdot| \) is the \( \ell_0 \) norm or the cardinality of the set.

Here is a small example of usage of this function:

```python
>>> from sklearn.metrics import label_ranking_loss
>>> y_true = np.array([[1, 0, 0], [0, 0, 1]])
>>> y_score = np.array([[0.75, 0.5, 1], [1, 0.2, 0.1]])
>>> label_ranking_loss(y_true, y_score)
0.75...
>>> # With the following prediction, we have perfect and minimal loss
>>> y_score = np.array([[1.0, 0.1, 0.2], [0.1, 0.2, 0.9]])
>>> label_ranking_loss(y_true, y_score)
0.0
```
Regression metrics

The `sklearn.metrics` module implements several loss, score, and utility functions to measure regression performance. Some of those have been enhanced to handle the multioutput case: `mean_squared_error`, `mean_absolute_error`, `explained_variance_score` and `r2_score`.

These functions have an `multioutput` keyword argument which specifies the way the scores or losses for each individual target should be averaged. The default is 'uniform_average', which specifies a uniformly weighted mean over outputs. If an `ndarray` of shape `(n_outputs,)` is passed, then its entries are interpreted as weights and an according weighted average is returned. If `multioutput` is 'raw_values' is specified, then all unaltered individual scores or losses will be returned in an array of shape `(n_outputs,)`.

The `r2_score` and `explained_variance_score` accept an additional value 'variance_weighted' for the `multioutput` parameter. This option leads to a weighting of each individual score by the variance of the corresponding target variable. This setting quantifies the globally captured unscaled variance. If the target variables are of different scale, then this score puts more importance on well explaining the higher variance variables. `multioutput='variance_weighted'` is the default value for `r2_score` for backward compatibility. This will be changed to `uniform_average` in the future.

Explained variance score

The `explained_variance_score` computes the explained variance regression score.

If $\hat{y}$ is the estimated target output, $y$ the corresponding (correct) target output, and $Var$ is Variance, the square of the standard deviation, then the explained variance is estimated as follow:

$$explained\_variance(y, \hat{y}) = 1 - \frac{Var\{y - \hat{y}\}}{Var\{y\}}$$

The best possible score is 1.0, lower values are worse.

Here is a small example of usage of the `explained_variance_score` function:

```python
>>> from sklearn.metrics import explained_variance_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> explained_variance_score(y_true, y_pred)
0.957...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> explained_variance_score(y_true, y_pred, multioutput='raw_values')
... array([ 0.967..., 1. ])
>>> explained_variance_score(y_true, y_pred, multioutput=[0.3, 0.7])
... 0.990...
```
Mean absolute error

The `mean_absolute_error` function computes mean absolute error, a risk metric corresponding to the expected value of the absolute error loss or $l_1$-norm loss.

If $\hat{y}_i$ is the predicted value of the $i$-th sample, and $y_i$ is the corresponding true value, then the mean absolute error (MAE) estimated over $n_{\text{samples}}$ is defined as

$$\text{MAE}(y, \hat{y}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} |y_i - \hat{y}_i|.$$

Here is a small example of usage of the `mean_absolute_error` function:

```python
>>> from sklearn.metrics import mean_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> mean_absolute_error(y_true, y_pred)
0.5
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> mean_absolute_error(y_true, y_pred)
0.75
>>> mean_absolute_error(y_true, y_pred, multioutput='raw_values')
array([ 0.5, 1. ])
>>> mean_absolute_error(y_true, y_pred, multioutput=[0.3, 0.7])
... 0.849...
```

Mean squared error

The `mean_squared_error` function computes mean square error, a risk metric corresponding to the expected value of the squared (quadratic) error or loss.

If $\hat{y}_i$ is the predicted value of the $i$-th sample, and $y_i$ is the corresponding true value, then the mean squared error (MSE) estimated over $n_{\text{samples}}$ is defined as

$$\text{MSE}(y, \hat{y}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} (y_i - \hat{y}_i)^2.$$ 

Here is a small example of usage of the `mean_squared_error` function:

```python
>>> from sklearn.metrics import mean_squared_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> mean_squared_error(y_true, y_pred)
0.375
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> mean_squared_error(y_true, y_pred)
0.7083...
```

Examples:
Mean squared logarithmic error

The \texttt{mean\_squared\_log\_error} function computes a risk metric corresponding to the expected value of the squared logarithmic (quadratic) error or loss.

If $\hat{y}_i$ is the predicted value of the $i$-th sample, and $y_i$ is the corresponding true value, then the mean squared logarithmic error (MSLE) estimated over $n_{\text{samples}}$ is defined as

$$\text{MSLE}(y, \hat{y}) = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} (\log_e(1 + y_i) - \log_e(1 + \hat{y}_i))^2.$$  

Where $\log_e(x)$ means the natural logarithm of $x$. This metric is best to use when targets having exponential growth, such as population counts, average sales of a commodity over a span of years etc. Note that this metric penalizes an under-predicted estimate greater than an over-predicted estimate.

Here is a small example of usage of the \texttt{mean\_squared\_log\_error} function:

```python
>>> from sklearn.metrics import mean_squared_log_error
>>> y_true = [3, 5, 2.5, 7]
>>> y_pred = [2.5, 5, 4, 8]
>>> mean_squared_log_error(y_true, y_pred)
0.039...
>>> y_true = [[0.5, 1], [1, 2], [7, 6]]
>>> y_pred = [[0.5, 2], [1, 2.5], [8, 8]]
>>> mean_squared_log_error(y_true, y_pred)
0.044...
```

Median absolute error

The \texttt{median\_absolute\_error} is particularly interesting because it is robust to outliers. The loss is calculated by taking the median of all absolute differences between the target and the prediction.

If $\hat{y}_i$ is the predicted value of the $i$-th sample and $y_i$ is the corresponding true value, then the median absolute error (MedAE) estimated over $n_{\text{samples}}$ is defined as

$$\text{MedAE}(y, \hat{y}) = \text{median}(|y_1 - \hat{y}_1|, \ldots, |y_n - \hat{y}_n|).$$

The \texttt{median\_absolute\_error} does not support multioutput.

Here is a small example of usage of the \texttt{median\_absolute\_error} function:

```python
>>> from sklearn.metrics import median_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> median_absolute_error(y_true, y_pred)
0.5
>>> y_true = [[0.5, 1], [1, 2], [7, 6]]
>>> y_pred = [[0.5, 2], [1, 2.5], [8, 8]]
>>> median_absolute_error(y_true, y_pred)
0.044...
```

R\textsuperscript{2} score, the coefficient of determination

The \texttt{r2\_score} function computes $R^2$, the coefficient of determination. It provides a measure of how well future samples are likely to be predicted by the model. Best possible score is 1.0 and it can be negative (because the model
can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

If \( \hat{y}_i \) is the predicted value of the \( i \)-th sample and \( y_i \) is the corresponding true value, then the score \( R^2 \) estimated over \( n_{\text{samples}} \) samples is defined as

\[
R^2(y, \hat{y}) = 1 - \frac{\sum_{i=0}^{n_{\text{samples}}-1} (y_i - \hat{y}_i)^2}{\sum_{i=0}^{n_{\text{samples}}-1} (y_i - \bar{y})^2}
\]

where \( \bar{y} = \frac{1}{n_{\text{samples}}} \sum_{i=0}^{n_{\text{samples}}-1} y_i \).

Here is a small example of usage of the `r2_score` function:

```python
>>> from sklearn.metrics import r2_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> r2_score(y_true, y_pred)
0.948...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> r2_score(y_true, y_pred, multioutput='variance_weighted')

decimal
>>> r2_score(y_true, y_pred, multioutput='uniform_average')

0.936...
>>> r2_score(y_true, y_pred, multioutput='raw_values')

array([ 0.965..., 0.908...])
>>> r2_score(y_true, y_pred, multioutput=[0.3, 0.7])

0.925...
```

**Example:**

- See *Lasso and Elastic Net for Sparse Signals* for an example of \( R^2 \) score usage to evaluate Lasso and Elastic Net on sparse signals.

**Clustering metrics**

The `sklearn.metrics` module implements several loss, score, and utility functions. For more information see the *Clustering performance evaluation* section for instance clustering, and *Biclustering evaluation* for biclustering.

**Dummy estimators**

When doing supervised learning, a simple sanity check consists of comparing one’s estimator against simple rules of thumb. `DummyClassifier` implements several such simple strategies for classification:

- `stratified` generates random predictions by respecting the training set class distribution.
- `most_frequent` always predicts the most frequent label in the training set.
- **prior** always predicts the class that maximizes the class prior (like `most_frequent`) and 
  ```python```
predict_proba returns the class prior.
```python```
- **uniform** generates predictions uniformly at random.
- **constant** always predicts a constant label that is provided by the user. A major motivation of this 
  method is F1-scoring, when the positive class is in the minority.

Note that with all these strategies, the `predict` method completely ignores the input data!

To illustrate `DummyClassifier`, first let's create an imbalanced dataset:

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn.model_selection import train_test_split

iris = load_iris()
X, y = iris.data, iris.target
y[y != 1] = -1
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)
```

Next, let’s compare the accuracy of `SVC` and `most_frequent`:

```python
>>> from sklearn.dummy import DummyClassifier
>>> from sklearn.svm import SVC

clf = SVC(kernel='linear', C=1).fit(X_train, y_train)
clf.score(X_test, y_test)
0.63...

clf = DummyClassifier(strategy='most_frequent',random_state=0)
clf.fit(X_train, y_train)
DummyClassifier(constant=None, random_state=0, strategy='most_frequent')
clf.score(X_test, y_test)
0.57...
```

We see that `SVC` doesn’t do much better than a dummy classifier. Now, let’s change the kernel:

```python
>>> clf = SVC(kernel='rbf', C=1).fit(X_train, y_train)
>>> clf.score(X_test, y_test)
0.97...
```

We see that the accuracy was boosted to almost 100%. A cross validation strategy is recommended for a better 
estimate of the accuracy, if it is not too CPU costly. For more information see the `Cross-validation: evaluating 
estimator performance` section. Moreover if you want to optimize over the parameter space, it is highly recommended 
to use an appropriate methodology; see the `Tuning the hyper-parameters of an estimator` section for details.

More generally, when the accuracy of a classifier is too close to random, it probably means that something went wrong: 
features are not helpful, a hyperparameter is not correctly tuned, the classifier is suffering from class imbalance, etc…

`DummyRegressor` also implements four simple rules of thumb for regression:

- **mean** always predicts the mean of the training targets.
- **median** always predicts the median of the training targets.
- **quantile** always predicts a user provided quantile of the training targets.
- **constant** always predicts a constant value that is provided by the user.

In all these strategies, the `predict` method completely ignores the input data.
3.3.4 Model persistence

After training a scikit-learn model, it is desirable to have a way to persist the model for future use without having to retrain. The following section gives you an example of how to persist a model with pickle. We’ll also review a few security and maintainability issues when working with pickle serialization.

Persistence example

It is possible to save a model in the scikit by using Python’s built-in persistence model, namely pickle:

```python
>>> from sklearn import svm
>>> from sklearn import datasets
>>> clf = svm.SVC()
>>> iris = datasets.load_iris()
>>> X, y = iris.data, iris.target
>>> clf.fit(X, y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0,
decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
max_iter=-1, probability=False, random_state=None, shrinking=True,
tol=0.001, verbose=False)

>>> import pickle

>>> s = pickle.dumps(clf)

>>> clf2 = pickle.loads(s)

>>> clf2.predict(X[0:1])
array([0])
>>> y[0]
0
```

In the specific case of the scikit, it may be more interesting to use joblib’s replacement of pickle (joblib.dump & joblib.load), which is more efficient on objects that carry large numpy arrays internally as is often the case for fitted scikit-learn estimators, but can only pickle to the disk and not to a string:

```python
>>> from sklearn.externals import joblib

>>> joblib.dump(clf, 'filename.pkl')

Later you can load back the pickled model (possibly in another Python process) with:

```python
>>> clf = joblib.load('filename.pkl')
```

Note: joblib.dump and joblib.load functions also accept file-like object instead of filenames. More information on data persistence with Joblib is available [here](#).

Security & maintainability limitations

pickle (and joblib by extension), has some issues regarding maintainability and security. Because of this,

- Never unpickle untrusted data as it could lead to malicious code being executed upon loading.
- While models saved using one version of scikit-learn might load in other versions, this is entirely unsupported and inadvisable. It should also be kept in mind that operations performed on such data could give different and unexpected results.

In order to rebuild a similar model with future versions of scikit-learn, additional metadata should be saved along the pickled model:
• The training data, e.g. a reference to an immutable snapshot
• The python source code used to generate the model
• The versions of scikit-learn and its dependencies
• The cross validation score obtained on the training data

This should make it possible to check that the cross-validation score is in the same range as before.

Since a model internal representation may be different on two different architectures, dumping a model on one architecture and loading it on another architecture is not supported.

If you want to know more about these issues and explore other possible serialization methods, please refer to this talk by Alex Gaynor.

### 3.3.5 Validation curves: plotting scores to evaluate models

Every estimator has its advantages and drawbacks. Its generalization error can be decomposed in terms of bias, variance and noise. The **bias** of an estimator is its average error for different training sets. The **variance** of an estimator indicates how sensitive it is to varying training sets. Noise is a property of the data.

In the following plot, we see a function $f(x) = \cos(\frac{3}{2}\pi x)$ and some noisy samples from that function. We use three different estimators to fit the function: linear regression with polynomial features of degree 1, 4 and 15. We see that the first estimator can at best provide only a poor fit to the samples and the true function because it is too simple (high bias), the second estimator approximates it almost perfectly and the last estimator approximates the training data perfectly but does not fit the true function very well, i.e. it is very sensitive to varying training data (high variance).

![Graphs showing model fit for different degrees](image)

Bias and variance are inherent properties of estimators and we usually have to select learning algorithms and hyper-parameters so that both bias and variance are as low as possible (see Bias-variance dilemma). Another way to reduce the variance of a model is to use more training data. However, you should only collect more training data if the true function is too complex to be approximated by an estimator with a lower variance.

In the simple one-dimensional problem that we have seen in the example it is easy to see whether the estimator suffers from bias or variance. However, in high-dimensional spaces, models can become very difficult to visualize. For this reason, it is often helpful to use the tools described below.

**Examples:**

- **Underfitting vs. Overfitting**
Validation curve

To validate a model we need a scoring function (see Model evaluation: quantifying the quality of predictions), for example accuracy for classifiers. The proper way of choosing multiple hyperparameters of an estimator are of course grid search or similar methods (see Tuning the hyper-parameters of an estimator) that select the hyperparameter with the maximum score on a validation set or multiple validation sets. Note that if we optimized the hyperparameters based on a validation score the validation score is biased and not a good estimate of the generalization any longer. To get a proper estimate of the generalization we have to compute the score on another test set.

However, it is sometimes helpful to plot the influence of a single hyperparameter on the training score and the validation score to find out whether the estimator is overfitting or underfitting for some hyperparameter values.

The function validation_curve can help in this case:

```python
>>> import numpy as np
>>> from sklearn.model_selection import validation_curve
>>> from sklearn.datasets import load_iris
>>> from sklearn.linear_model import Ridge

>>> np.random.seed(0)

>>> iris = load_iris()

>>> X, y = iris.data, iris.target

>>> indices = np.arange(y.shape[0])

>>> np.random.shuffle(indices)

>>> X, y = X[indices], y[indices]

>>> train_scores, valid_scores = validation_curve(Ridge(), X, y, "alpha",

... np.logspace(-7, 3, 3))

>>> train_scores
array([[ 0.94..., 0.92..., 0.92...],
       [ 0.94..., 0.92..., 0.92...],
       [ 0.47..., 0.45..., 0.42...]])

>>> valid_scores
array([[ 0.90..., 0.92..., 0.94...],
       [ 0.90..., 0.92..., 0.94...],
       [ 0.44..., 0.39..., 0.45...]])
```

If the training score and the validation score are both low, the estimator will be underfitting. If the training score is high and the validation score is low, the estimator is overfitting and otherwise it is working very well. A low training score and a high validation score is usually not possible. All three cases can be found in the plot below where we vary the parameter $\gamma$ of an SVM on the digits dataset.

Learning curve

A learning curve shows the validation and training score of an estimator for varying numbers of training samples. It is a tool to find out how much we benefit from adding more training data and whether the estimator suffers more from a variance error or a bias error. If both the validation score and the training score converge to a value that is too low with increasing size of the training set, we will not benefit much from more training data. In the following plot you can see an example: naive Bayes roughly converges to a low score.

We will probably have to use an estimator or a parametrization of the current estimator that can learn more complex concepts (i.e. has a lower bias). If the training score is much greater than the validation score for the maximum number
of training samples, adding more training samples will most likely increase generalization. In the following plot you can see that the SVM could benefit from more training examples.

We can use the function `learning_curve` to generate the values that are required to plot such a learning curve (number of samples that have been used, the average scores on the training sets and the average scores on the validation sets):

```python
>>> from sklearn.model_selection import learning_curve
>>> from sklearn import svm

>>> train_sizes, train_scores, valid_scores = learning_curve(...   SVC(kernel='linear'), X, y, train_sizes=[50, 80, 110], cv=5)
>>> train_sizes
array([ 50, 80, 110])
>>> train_scores
array([[[ 0.98..., 0.98 , 0.98..., 0.98..., 0.98...],
         [ 0.98..., 1. , 0.98..., 0.98..., 0.98...],
         [ 0.98..., 1. , 0.98..., 0.98..., 0.99...]])
>>> valid_scores
array([[[ 1. , 0.93..., 1. , 1. , 0.96...],
         [ 1. , 0.96..., 1. , 1. , 0.96...],
         [ 1. , 0.96..., 1. , 1. , 0.96...]])
```

### 3.4 Dataset transformations

scikit-learn provides a library of transformers, which may clean (see Preprocessing data), reduce (see Unsupervised dimensionality reduction), expand (see Kernel Approximation) or generate (see Feature extraction) feature representations.

Like other estimators, these are represented by classes with a `fit` method, which learns model parameters (e.g. mean and standard deviation for normalization) from a training set, and a `transform` method which applies this transformation model to unseen data. `fit_transform` may be more convenient and efficient for modelling and transforming the training data simultaneously.

Combining such transformers, either in parallel or series is covered in Pipeline and FeatureUnion: combining estimators. Pairwise metrics, Affinities and Kernels covers transforming feature spaces into affinity matrices, while Transforming the prediction target (y) considers transformations of the target space (e.g. categorical labels) for use in scikit-learn.
Pipeline and FeatureUnion: combining estimators

Pipeline: chaining estimators

`Pipeline` can be used to chain multiple estimators into one. This is useful as there is often a fixed sequence of steps in processing the data, for example feature selection, normalization and classification. `Pipeline` serves two purposes here:

Convenience and encapsulation You only have to call `fit` and `predict` once on your data to fit a whole sequence of estimators.

Joint parameter selection You can `grid search` over parameters of all estimators in the pipeline at once.

Safety Pipelines help avoid leaking statistics from your test data into the trained model in cross-validation, by ensuring that the same samples are used to train the transformers and predictors.

All estimators in a pipeline, except the last one, must be transformers (i.e. must have a `transform` method). The last estimator may be any type (transformer, classifier, etc.).

Usage

The `Pipeline` is built using a list of `(key, value)` pairs, where the key is a string containing the name you want to give this step and `value` is an estimator object:

```python
>>> from sklearn.pipeline import Pipeline
>>> from sklearn.svm import SVC
>>> from sklearn.decomposition import PCA

>>> estimators = [('reduce_dim', PCA()), ('clf', SVC())]

>>> pipe = Pipeline(estimators)

>>> pipe
Pipeline(memory=None,
         steps=[('reduce_dim', PCA(copy=True,...)), ('clf', SVC(C=1.0,...))])
```

The estimators of a pipeline are stored as a list in the `steps` attribute:

```python
>>> pipe.steps[0]
('reduce_dim', PCA(copy=True, iterated_power='auto', n_components=None, random_state=None, svd_solver='auto', tol=0.0, whiten=False))
```

and as a dict in `named_steps`:

```python
>>> pipe.named_steps['reduce_dim']
PCA(copy=True, iterated_power='auto', n_components=None, random_state=None, svd_solver='auto', tol=0.0, whiten=False)
```
Parameters of the estimators in the pipeline can be accessed using the `<estimator>__<parameter>` syntax:

```python
>>> pipe.set_params(clf__C=10)
Pipeline(memory=None,
    steps=[('reduce_dim', PCA(copy=True, iterated_power='auto',...)),
          ('clf', SVC(C=10, cache_size=200, class_weight=...))])
```

Attributes of named_steps map to keys, enabling tab completion in interactive environments:

```python
>>> pipe.named_steps.reduce_dim is pipe.named_steps['reduce_dim']
True
```

Individual steps may also be replaced as parameters, and non-final steps may be ignored by setting them to `None`:

```python
>>> from sklearn.linear_model import LogisticRegression
>>> param_grid = dict(reduce_dim=[None, PCA(5), PCA(10)],
                     ...                        clf=[SVC(), LogisticRegression()],
                     ...                        clf__C=[0.1, 10, 100])
>>> grid_search = GridSearchCV(pipe, param_grid=param_grid)
```

Examples:

- Pipeline Anova SVM
- Sample pipeline for text feature extraction and evaluation
- Pipelining: chaining a PCA and a logistic regression
- Explicit feature map approximation for RBF kernels
- SVM-Anova: SVM with univariate feature selection
- Selecting dimensionality reduction with Pipeline and GridSearchCV

See also:

- Tuning the hyper-parameters of an estimator

Notes

Calling `fit` on the pipeline is the same as calling `fit` on each estimator in turn, `transform` the input and pass it on to the next step. The pipeline has all the methods that the last estimator in the pipeline has, i.e. if the last estimator is a classifier, the `Pipeline` can be used as a classifier. If the last estimator is a transformer, again, so is the pipeline.
Caching transformers: avoid repeated computation

Fitting transformers may be computationally expensive. With its `memory` parameter set, `Pipeline` will cache each transformer after calling `fit`. This feature is used to avoid computing the fit transformers within a pipeline if the parameters and input data are identical. A typical example is the case of a grid search in which the transformers can be fitted only once and reused for each configuration.

The parameter `memory` is needed in order to cache the transformers. `memory` can be either a string containing the directory where to cache the transformers or a `joblib.Memory` object:

```python
>>> from tempfile import mkdtemp
>>> from shutil import rmtree
>>> from sklearn.decomposition import PCA
>>> from sklearn.svm import SVC
>>> from sklearn.pipeline import Pipeline

>>> estimators = [('reduce_dim', PCA()), ('clf', SVC())]

>>> cachedir = mkdtemp()

>>> pipe = Pipeline(estimators, memory=cachedir)
```

Warning: Side effect of caching transformers

Using a `Pipeline` without cache enabled, it is possible to inspect the original instance such as:

```python
>>> from sklearn.datasets import load_digits

>>> digits = load_digits()

>>> pca1 = PCA()

>>> svm1 = SVC()

>>> pipe = Pipeline([('reduce_dim', pca1), ('clf', svm1)])

>>> pipe.fit(digits.data, digits.target)
```

Enabling caching triggers a clone of the transformers before fitting. Therefore, the transformer instance given to the pipeline cannot be inspected directly. In following example, accessing the PCA instance `pca2` will raise an `AttributeError` since `pca2` will be an unfitted transformer. Instead, use the attribute `named_steps` to inspect estimators within the pipeline:

```python
>>> cachedir = mkdtemp()

>>> pca2 = PCA()

>>> svm2 = SVC()

>>> cached_pipe = Pipeline([('reduce_dim', pca2), ('clf', svm2)], memory=cachedir)

>>> cached_pipe.fit(digits.data, digits.target)

>>> print(cached_pipe.named_steps['reduce_dim'].components_)
```

>> WARNING: Side effect of caching transformers

Using a `Pipeline` without cache enabled, it is possible to inspect the original instance such as:
Examples:

- Selecting dimensionality reduction with Pipeline and GridSearchCV

FeatureUnion: composite feature spaces

FeatureUnion combines several transformer objects into a new transformer that combines their output. A FeatureUnion takes a list of transformer objects. During fitting, each of these is fit to the data independently. For transforming data, the transformers are applied in parallel, and the sample vectors they output are concatenated end-to-end into larger vectors.

FeatureUnion serves the same purposes as Pipeline - convenience and joint parameter estimation and validation.

FeatureUnion and Pipeline can be combined to create complex models.

(A FeatureUnion has no way of checking whether two transformers might produce identical features. It only produces a union when the feature sets are disjoint, and making sure they are the caller’s responsibility.)

Usage

A FeatureUnion is built using a list of (key, value) pairs, where the key is the name you want to give to a given transformation (an arbitrary string; it only serves as an identifier) and value is an estimator object:

```python
>>> from sklearn.pipeline import FeatureUnion
>>> from sklearn.decomposition import PCA
>>> from sklearn.decomposition import KernelPCA

>>> estimators = [('linear_pca', PCA()), ('kernel_pca', KernelPCA())]
>>> combined = FeatureUnion(estimators)
```

Like pipelines, feature unions have a shorthand constructor called make_union that does not require explicit naming of the components.

Like Pipeline, individual steps may be replaced using set_params, and ignored by setting to None:

```python
>>> combined.set_params(kernel_pca=None)
... FeatureUnion(n_jobs=1,
    transformer_list=[('linear_pca', PCA(copy=True,...)),
                      ('kernel_pca', KernelPCA(alpha=1.0,...))],
    transformer_weights=None)
```

Examples:

- Concatenating multiple feature extraction methods
3.4.2 Feature extraction

The `sklearn.feature_extraction` module can be used to extract features in a format supported by machine learning algorithms from datasets consisting of formats such as text and image.

Note: Feature extraction is very different from Feature selection: the former consists in transforming arbitrary data, such as text or images, into numerical features usable for machine learning. The latter is a machine learning technique applied on these features.

Loading features from dicts

The class `DictVectorizer` can be used to convert feature arrays represented as lists of standard Python `dict` objects to the NumPy/SciPy representation used by scikit-learn estimators.

While not particularly fast to process, Python’s `dict` has the advantages of being convenient to use, being sparse (absent features need not be stored) and storing feature names in addition to values.

`DictVectorizer` implements what is called one-of-K or “one-hot” coding for categorical (aka nominal, discrete) features. Categorical features are “attribute-value” pairs where the value is restricted to a list of discrete of possibilities without ordering (e.g. topic identifiers, types of objects, tags, names...).

In the following, “city” is a categorical attribute while “temperature” is a traditional numerical feature:

```python
>>> measurements = [
...     {'city': 'Dubai', 'temperature': 33.},
...     {'city': 'London', 'temperature': 12.},
...     {'city': 'San Francisco', 'temperature': 18.},
... ]

>>> from sklearn.feature_extraction import DictVectorizer
>>> vec = DictVectorizer()

>>> vec.fit_transform(measurements).toarray()
array([[1., 0., 0., 33.],
       [0., 1., 0., 12.],
       [0., 0., 1., 18.]]

>>> vec.get_feature_names()
['city=Dubai', 'city=London', 'city=San Francisco', 'temperature']
```

`DictVectorizer` is also a useful representation transformation for training sequence classifiers in Natural Language Processing models that typically work by extracting feature windows around a particular word of interest.

For example, suppose that we have a first algorithm that extracts Part of Speech (PoS) tags that we want to use as complementary tags for training a sequence classifier (e.g. a chunker). The following dict could be such a window of features extracted around the word ‘sat’ in the sentence ‘The cat sat on the mat.’:

```python
>>> pos_window = [
...     {'word-2': 'the',
...      'pos-2': 'DT',
...      'word-1': 'cat',
...  ]
```
This description can be vectorized into a sparse two-dimensional matrix suitable for feeding into a classifier (maybe after being piped into a `text.TfidfTransformer` for normalization):

```python
>>> vec = DictVectorizer()
>>> pos_vectorized = vec.fit_transform(pos_window)
>>> pos_vectorized
<1x6 sparse matrix of type '<... 'numpy.float64'>'
    with 6 stored elements in Compressed Sparse ... format>
>>> pos_vectorized.toarray()
array([[ 1., 1., 1., 1., 1., 1.]])
>>> vec.get_feature_names()
['pos+1=PP', 'pos-1=NN', 'pos-2=DT', 'word+1=on', 'word-1=cat', 'word-2=the']
```

As you can imagine, if one extracts such a context around each individual word of a corpus of documents the resulting matrix will be very wide (many one-hot-features) with most of them being valued to zero most of the time. So as to make the resulting data structure able to fit in memory the `DictVectorizer` class uses a `scipy.sparse` matrix by default instead of a `numpy.ndarray`.

### Feature hashing

The class `FeatureHasher` is a high-speed, low-memory vectorizer that uses a technique known as feature hashing, or the “hashing trick”. Instead of building a hash table of the features encountered in training, as the vectorizers do, instances of `FeatureHasher` apply a hash function to the features to determine their column index in sample matrices directly. The result is increased speed and reduced memory usage, at the expense of inspectability; the hasher does not remember what the input features looked like and has no `inverse_transform` method.

Since the hash function might cause collisions between (unrelated) features, a signed hash function is used and the sign of the hash value determines the sign of the value stored in the output matrix for a feature. This way, collisions are likely to cancel out rather than accumulate error, and the expected mean of any output feature’s value is zero. This mechanism is enabled by default with `alternate_sign=True` and is particularly useful for small hash table sizes ($n_{features} < 10000$). For large hash table sizes, it can be disabled, to allow the output to be passed to estimators like `sklearn.naive_bayes.MultinomialNB` or `sklearn.feature_selection.chi2` feature selectors that expect non-negative inputs.

`FeatureHasher` accepts either mappings (like Python’s `dict` and its variants in the `collections` module), (feature, value) pairs, or strings, depending on the constructor parameter `input_type`. Mapping are treated as lists of (feature, value) pairs, while single strings have an implicit value of 1, so `['feat1', 'feat2', 'feat3']` is interpreted as `[('feat1', 1), ('feat2', 1), ('feat3', 1)]`. If a single feature occurs multiple times in a sample, the associated values will be summed (so `('feat', 2) and ('feat', 3.5)` become `('feat', 5.5)`). The output from `FeatureHasher` is always a `scipy.sparse` matrix in the CSR format.

Feature hashing can be employed in document classification, but unlike `text.CountVectorizer`, `FeatureHasher` does not do word splitting or any other preprocessing except Unicode-to-UTF-8 encoding; see `Vectorizing a large text corpus with the hashing trick`, below, for a combined tokenizer/hasher.

As an example, consider a word-level natural language processing task that needs features extracted from (token, part_of_speech) pairs. One could use a Python generator function to extract features:
def token_features(token, part_of_speech):
    if token.isdigit():
        yield "numeric"
    else:
        yield "token={}".format(token.lower())
        yield "token,pos={},{}".format(token, part_of_speech)
    if token[0].isupper():
        yield "uppercase_initial"
    if token.isupper():
        yield "all_uppercase"
    yield "pos={}".format(part_of_speech)

Then, the raw_X to be fed to FeatureHasher.transform can be constructed using:

raw_X = (token_features(tok, pos_tagger(tok)) for tok in corpus)

and fed to a hasher with:

hasher = FeatureHasher(input_type='string')
X = hasher.transform(raw_X)

to get a scipy.sparse matrix X.

Note the use of a generator comprehension, which introduces laziness into the feature extraction: tokens are only processed on demand from the hasher.

Implementation details

FeatureHasher uses the signed 32-bit variant of MurmurHash3. As a result (and because of limitations in scipy.sparse), the maximum number of features supported is currently $2^{31} - 1$.

The original formulation of the hashing trick by Weinberger et al. used two separate hash functions $h$ and $\xi$ to determine the column index and sign of a feature, respectively. The present implementation works under the assumption that the sign bit of MurmurHash3 is independent of its other bits.

Since a simple modulo is used to transform the hash function to a column index, it is advisable to use a power of two as the n_features parameter; otherwise the features will not be mapped evenly to the columns.

References:

• MurmurHash3.

Text feature extraction

The Bag of Words representation

Text Analysis is a major application field for machine learning algorithms. However the raw data, a sequence of symbols cannot be fed directly to the algorithms themselves as most of them expect numerical feature vectors with a fixed size rather than the raw text documents with variable length.
In order to address this, scikit-learn provides utilities for the most common ways to extract numerical features from text content, namely:

- **tokenizing** strings and giving an integer id for each possible token, for instance by using white-spaces and punctuation as token separators.
- **counting** the occurrences of tokens in each document.
- **normalizing** and weighting with diminishing importance tokens that occur in the majority of samples / documents.

In this scheme, features and samples are defined as follows:

- each **individual token occurrence frequency** (normalized or not) is treated as a feature.
- the vector of all the token frequencies for a given document is considered a multivariate sample.

A corpus of documents can thus be represented by a matrix with one row per document and one column per token (e.g. word) occurring in the corpus.

We call **vectorization** the general process of turning a collection of text documents into numerical feature vectors. This specific strategy (tokenization, counting and normalization) is called the **Bag of Words** or “Bag of n-grams” representation. Documents are described by word occurrences while completely ignoring the relative position information of the words in the document.

### Sparsity

As most documents will typically use a very small subset of the words used in the corpus, the resulting matrix will have many feature values that are zeros (typically more than 99% of them).

For instance a collection of 10,000 short text documents (such as emails) will use a vocabulary with a size in the order of 100,000 unique words in total while each document will use 100 to 1000 unique words individually.

In order to be able to store such a matrix in memory but also to speed up algebraic operations matrix / vector implementations will typically use a sparse representation such as the implementations available in the **scipy.sparse** package.

### Common Vectorizer usage

**CountVectorizer** implements both tokenization and occurrence counting in a single class:

```python
>>> from sklearn.feature_extraction.text import CountVectorizer

```

This model has many parameters, however the default values are quite reasonable (please see the reference documentation for the details):

```python
>>> vectorizer = CountVectorizer() >>> vectorizer
CountVectorizer(analyzer='word', binary=False, decode_error='strict',
                 dtype=np.int64, encoding='utf-8', input='content',
                 lowercase=True, max_df=1.0, max_features=None, min_df=1,
                 ngram_range=(1, 1), preprocessor=None, stop_words=None,
                 strip_accents=None, token_pattern='(?u)\b\w\w+\b',
                 tokenizer=None, vocabulary=None)
```

Let’s use it to tokenize and count the word occurrences of a minimalistic corpus of text documents:
>>> corpus = [
... 'This is the first document.',
... 'This is the second second document.',
... 'And the third one.',
... 'Is this the first document?',
...]

>>> X = vectorizer.fit_transform(corpus)
>>> X
<4x9 sparse matrix of type '<... 'numpy.int64'>'
with 19 stored elements in Compressed Sparse ... format>

The default configuration tokenizes the string by extracting words of at least 2 letters. The specific function that does this step can be requested explicitly:

```python
>>> analyze = vectorizer.build_analyzer()
>>> analyze("This is a text document to analyze.") ==
(['this', 'is', 'text', 'document', 'to', 'analyze'])
True
```

Each term found by the analyzer during the fit is assigned a unique integer index corresponding to a column in the resulting matrix. This interpretation of the columns can be retrieved as follows:

```python
>>> vectorizer.get_feature_names() ==
(['and', 'document', 'first', 'is', 'one',
... 'second', 'the', 'third', 'this'])
True
```

```python
>>> X.toarray()
array([[0, 1, 1, 1, 0, 1, 0, 0, 1],
[0, 1, 0, 1, 0, 2, 1, 0, 1],
[1, 0, 0, 1, 0, 1, 1, 0, 1],
[0, 1, 1, 0, 0, 1, 0, 1, 1]])...
```

The converse mapping from feature name to column index is stored in the `vocabulary_` attribute of the vectorizer:

```python
>>> vectorizer.vocabulary_.get('document')
1
```

Hence words that were not seen in the training corpus will be completely ignored in future calls to the transform method:

```python
>>> vectorizer.transform(['Something completely new.']).toarray()
... array([[0, 0, 0, 0, 0, 0, 0, 0, 0]])...
```

Note that in the previous corpus, the first and the last documents have exactly the same words hence are encoded in equal vectors. In particular we lose the information that the last document is an interrogative form. To preserve some of the local ordering information we can extract 2-grams of words in addition to the 1-grams (individual words):

```python
>>> bigram_vectorizer = CountVectorizer(ngram_range=(1, 2),
...                                      token_pattern=r'\w+\b', min_df=1)
```  

```python
>>> analyze = bigram_vectorizer.build_analyzer()
>>> analyze('Bi-grams are cool!') ==
(['bi', 'grams', 'are', 'cool', 'bi grams', 'grams are', 'are cool'])
True
```

The vocabulary extracted by this vectorizer is hence much bigger and can now resolve ambiguities encoded in local positioning patterns:
X_2 = bigram_vectorizer.fit_transform(corpus).toarray()

In particular the interrogative form “Is this” is only present in the last document:

>>> feature_index = bigram_vectorizer.vocabulary_.get('is this')
>>> X_2[:, feature_index]
array([0, 0, 1, 1]...)

Tf–idf term weighting

In a large text corpus, some words will be very present (e.g. “the”, “a”, “is” in English) hence carrying very little meaningful information about the actual contents of the document. If we were to feed the direct count data directly to a classifier those very frequent terms would shadow the frequencies of rarer yet more interesting terms.

In order to re-weight the count features into floating point values suitable for usage by a classifier it is very common to use the tf–idf transform.

Tf means term-frequency while tf–idf means term-frequency times inverse document-frequency: tf-idf(t,d) = \(tf(t,d) \times idf(t)\).

Using the TfidfTransformer’s default settings, TfidfTransformer(norm='l2', use_idf=True, smooth_idf=True, sublinear_tf=False) the term frequency, the number of times a term occurs in a given document, is multiplied with idf component, which is computed as

\[idf(t) = \log \frac{1+nd}{1+df(d,t)} + 1,\]

where \(nd\) is the total number of documents, and \(df(d,t)\) is the number of documents that contain term \(t\). The resulting tf-idf vectors are then normalized by the Euclidean norm:

\[\|v\|_2 = \sqrt{v_1^2 + v_2^2 + \cdots + v_n^2}.\]

This was originally a term weighting scheme developed for information retrieval (as a ranking function for search engines results) that has also found good use in document classification and clustering.

The following sections contain further explanations and examples that illustrate how the tf-ids are computed exactly and how the tf-ids computed in scikit-learn’s TfidfTransformer and TfidfVectorizer differ slightly from the standard textbook notation that defines the idf as

\[idf(t) = \log \frac{nd}{df(d,t)} + 1.\]

In the TfidfTransformer and TfidfVectorizer with smooth_idf=False, the “1” count is added to the idf instead of the idf’s denominator:

\[idf(t) = \log \frac{nd + 1}{df(d,t)} + 1\]

This normalization is implemented by the TfidfTransformer class:

>>> from sklearn.feature_extraction.text import TfidfTransformer
>>> transformer = TfidfTransformer(smooth_idf=False)
>>> transformer
TfidfTransformer(norm='l2', use_idf=True)
Again please see the reference documentation for the details on all the parameters.

Let’s take an example with the following counts. The first term is present 100% of the time hence not very interesting. The two other features only in less than 50% of the time hence probably more representative of the content of the documents:

```python
>>> counts = [[3, 0, 1],
            ... [2, 0, 0],
            ... [3, 0, 0],
            ... [4, 0, 0],
            ... [3, 2, 0],
            ... [3, 0, 2]]
```

```python
>>> tfidf = transformer.fit_transform(counts)
>>> tfidf
<6x3 sparse matrix of type '<... 'numpy.float64'>'
with 9 stored elements in Compressed Sparse ... format>
```

```python
>>> tfidf.toarray()
array([[ 0.81940995, 0. , 0.57320793],
       [ 1. , 0. , 0. ],
       [ 1. , 0. , 0. ],
       [ 0.47330339, 0.88089948, 0. ],
       [ 0.58149261, 0. , 0.81355169]])
```

Each row is normalized to have unit Euclidean norm:

\[ v_{norm} = \frac{v}{||v||_2} = \frac{v}{\sqrt{v_1^2 + v_2^2 + \cdots + v_n^2}} \]

For example, we can compute the tf-idf of the first term in the first document in the `counts` array as follows:

\[ n_{d,term1} = 6 \]
\[ df(d, t)_{term1} = 6 \]
\[ idf(t)_{term1} = log_{\frac{n_d}{df(d, t)}} + 1 = log(6) + 1 = 1 \]
\[ tf-idf_{term1} = tf \times idf = 3 \times 1 = 3 \]

Now, if we repeat this computation for the remaining 2 terms in the document, we get

\[ tf-idf_{term2} = 0 \times (log(6/1) + 1) = 0 \]
\[ tf-idf_{term3} = 1 \times (log(6/2) + 1) \approx 2.0986 \]

and the vector of raw tf-ids:

\[ tf-idf_{raw} = [3, 0, 2.0986] \]

Then, applying the Euclidean (L2) norm, we obtain the following tf-ids for document 1:

\[ \sqrt{\frac{3^2 + 0^2 + 2.0986^2}{3^2 + 0^2 + 2.0986^2}} = [0.819, 0, 0.573]. \]

Furthermore, the default parameter smooth_idf=True adds “1” to the numerator and denominator as if an extra document was seen containing every term in the collection exactly once, which prevents zero divisions:

\[ idf(t) = log\frac{1 + df(t)}{1 + df_d} + 1 \]

Using this modification, the tf-idf of the third term in document 1 changes to 1.8473:

\[ tf-idf_{term3} = 1 \times log(7/3) + 1 \approx 1.8473 \]

And the L2-normalized tf-idf changes to
\[
\sqrt{3^2+2^2+1.8473^2} = [0.8515, 0, 0.5243]:
\]

```python
>>> transformer = TfidfTransformer()
>>> transformer.fit_transform(counts).toarray()
array([[ 0.85151335, 0., 0.52433293],
       [ 1., 0., 0. ],
       [ 1., 0., 0. ],
       [ 1., 0., 0. ],
       [ 0.55422893, 0.83236428, 0. ],
       [ 0.63035731, 0., 0.77630514]])
```

The weights of each feature computed by the `fit` method call are stored in a model attribute:

```python
>>> transformer.idf_
array([ 1. ..., 2.25..., 1.84...])
```

As tf-idf is very often used for text features, there is also another class called `TfidfVectorizer` that combines all the options of `CountVectorizer` and `TfidfTransformer` in a single model:

```python
>>> from sklearn.feature_extraction.text import TfidfVectorizer
>>> vectorizer = TfidfVectorizer()
>>> vectorizer.fit_transform(corpus)
...<4x9 sparse matrix of type '<... 'numpy.float64'>'
  with 19 stored elements in Compressed Sparse ... format>
```

While the tf-idf normalization is often very useful, there might be cases where the binary occurrence markers might offer better features. This can be achieved by using the `binary` parameter of `CountVectorizer`. In particular, some estimators such as Bernoulli Naive Bayes explicitly model discrete boolean random variables. Also, very short texts are likely to have noisy tf-idf values while the binary occurrence info is more stable.

As usual the best way to adjust the feature extraction parameters is to use a cross-validated grid search, for instance by pipelining the feature extractor with a classifier:

- Sample pipeline for text feature extraction and evaluation

### Decoding text files

Text is made of characters, but files are made of bytes. These bytes represent characters according to some encoding. To work with text files in Python, their bytes must be decoded to a character set called Unicode. Common encodings are ASCII, Latin-1 (Western Europe), KOI8-R (Russian) and the universal encodings UTF-8 and UTF-16. Many others exist.

**Note:** An encoding can also be called a ‘character set’, but this term is less accurate: several encodings can exist for a single character set.

The text feature extractors in scikit-learn know how to decode text files, but only if you tell them what encoding the files are in. The `CountVectorizer` takes an `encoding` parameter for this purpose. For modern text files, the correct encoding is probably UTF-8, which is therefore the default (`encoding="utf-8"`).

If the text you are loading is not actually encoded with UTF-8, however, you will get a `UnicodeDecodeError`. The vectorizers can be told to be silent about decoding errors by setting the `decode_error` parameter to either "ignore" or "replace". See the documentation for the Python function `bytes.decode` for more details (type `help(bytes.decode)` at the Python prompt).
If you are having trouble decoding text, here are some things to try:

- Find out what the actual encoding of the text is. The file might come with a header or README that tells you the encoding, or there might be some standard encoding you can assume based on where the text comes from.

- You may be able to find out what kind of encoding it is in general using the UNIX command `file`. The Python `chardet` module comes with a script called `chardetect.py` that will guess the specific encoding, though you cannot rely on its guess being correct.

- You could try UTF-8 and disregard the errors. You can decode byte strings with `bytes.decode(errors='replace')` to replace all decoding errors with a meaningless character, or set `decode_error='replace'` in the vectorizer. This may damage the usefulness of your features.

- Real text may come from a variety of sources that may have used different encodings, or even be sloppily decoded in a different encoding than the one it was encoded with. This is common in text retrieved from the Web. The Python package `ftfy` can automatically sort out some classes of decoding errors, so you could try decoding the unknown text as `latin-1` and then using `ftfy` to fix errors.

- If the text is in a mish-mash of encodings that is simply too hard to sort out (which is the case for the 20 Newsgroups dataset), you can fall back on a simple single-byte encoding such as `latin-1`. Some text may display incorrectly, but at least the same sequence of bytes will always represent the same feature.

For example, the following snippet uses `chardet` (not shipped with scikit-learn, must be installed separately) to figure out the encoding of three texts. It then vectorizes the texts and prints the learned vocabulary. The output is not shown here.

```python
>>> import chardet
>>> text1 = b"Sei mir gegr\xc3\xbct mein Sauerkraut"
>>> text2 = b"holdselig sind deine Ger\xfcche"
>>> text3 = b"\xff\xfe\xc0\xe0\xc0\xe0 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80 \x80\x80"
>>> decoded = [x.decode(chardet.detect(x)['encoding'])
... for x in (text1, text2, text3)]
>>> v = CountVectorizer().fit(decoded).vocabulary_
>>> for term in v: print(v)
```

(Depending on the version of `chardet`, it might get the first one wrong.)

For an introduction to Unicode and character encodings in general, see Joel Spolsky's "Absolute Minimum Every Software Developer Must Know About Unicode.

Applications and examples

The bag of words representation is quite simplistic but surprisingly useful in practice.

In particular in a supervised setting it can be successfully combined with fast and scalable linear models to train document classifiers, for instance:

- Classification of text documents using sparse features

In an unsupervised setting it can be used to group similar documents together by applying clustering algorithms such as K-means:

- Clustering text documents using k-means

Finally it is possible to discover the main topics of a corpus by relaxing the hard assignment constraint of clustering, for instance by using Non-negative matrix factorization (NMF or NNMF):
• **Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation**

**Limitations of the Bag of Words representation**

A collection of unigrams (what bag of words is) cannot capture phrases and multi-word expressions, effectively disregarding any word order dependence. Additionally, the bag of words model doesn’t account for potential misspellings or word derivations.

N-grams to the rescue! Instead of building a simple collection of unigrams (n=1), one might prefer a collection of bigrams (n=2), where occurrences of pairs of consecutive words are counted.

One might alternatively consider a collection of character n-grams, a representation resilient against misspellings and derivations.

For example, let’s say we’re dealing with a corpus of two documents: ['words', 'wprds']. The second document contains a misspelling of the word ‘words’. A simple bag of words representation would consider these two as very distinct documents, differing in both of the two possible features. A character 2-gram representation, however, would find the documents matching in 4 out of 8 features, which may help the preferred classifier decide better:

```python
>>> ngram_vectorizer = CountVectorizer(analyzer='char_wb', ngram_range=(2, 2))
>>> counts = ngram_vectorizer.fit_transform(['words', 'wprds'])
>>> ngram_vectorizer.get_feature_names() == (' w', 'ds', 'or', 'pr', 'rd', 's ', 'wo', 'wp')
True
>>> counts.toarray().astype(int)
array([[1, 1, 1, 0, 1, 1, 1, 0],
       [1, 1, 0, 1, 1, 1, 0, 1]])
```

In the above example, 'char_wb' analyzer is used, which creates n-grams only from characters inside word boundaries (padded with space on each side). The 'char' analyzer, alternatively, creates n-grams that span across words:

```python
>>> ngram_vectorizer = CountVectorizer(analyzer='char_wb', ngram_range=(5, 5))
>>> ngram_vectorizer.fit_transform(['jumpy fox'])
...<1x4 sparse matrix of type '<...'numpy.int64'>'
with 4 stored elements in Compressed Sparse ... format>
>>> ngram_vectorizer.get_feature_names() == (' fox', ' jump', 'jumpy', 'umpy ')
True

>>> ngram_vectorizer = CountVectorizer(analyzer='char', ngram_range=(5, 5))
>>> ngram_vectorizer.fit_transform(['jumpy fox'])
...<1x5 sparse matrix of type '<...'numpy.int64'>'
with 5 stored elements in Compressed Sparse ... format>
>>> ngram_vectorizer.get_feature_names() == ('jumpy', 'mpy f', 'py fo', 'umpy ', 'y fox')
True
```

The word boundaries-aware variant char_wb is especially interesting for languages that use white-spaces for word separation as it generates significantly less noisy features than the raw char variant in that case. For such languages it can increase both the predictive accuracy and convergence speed of classifiers trained using such features while retaining the robustness with regards to misspellings and word derivations.

While some local positioning information can be preserved by extracting n-grams instead of individual words, bag of words and bag of n-grams destroy most of the inner structure of the document and hence most of the meaning carried by that internal structure.
In order to address the wider task of Natural Language Understanding, the local structure of sentences and paragraphs should thus be taken into account. Many such models will thus be casted as “Structured output” problems which are currently outside of the scope of scikit-learn.

Vectorizing a large text corpus with the hashing trick

The above vectorization scheme is simple but the fact that it holds an in-memory mapping from the string tokens to the integer feature indices (the vocabulary_ attribute) causes several problems when dealing with large datasets:

- the larger the corpus, the larger the vocabulary will grow and hence the memory use too,
- fitting requires the allocation of intermediate data structures of size proportional to that of the original dataset.
- building the word-mapping requires a full pass over the dataset hence it is not possible to fit text classifiers in a strictly online manner.
- pickling and un-pickling vectorizers with a large vocabulary_ can be very slow (typically much slower than pickling / un-pickling flat data structures such as a NumPy array of the same size),
- it is not easily possible to split the vectorization work into concurrent sub tasks as the vocabulary_ attribute would have to be a shared state with a fine grained synchronization barrier: the mapping from token string to feature index is dependent on ordering of the first occurrence of each token hence would have to be shared, potentially harming the concurrent workers’ performance to the point of making them slower than the sequential variant.

It is possible to overcome those limitations by combining the “hashing trick” (Feature hashing) implemented by the sklearn.feature_extraction.FeatureHasher class and the text preprocessing and tokenization features of the CountVectorizer.

This combination is implementing in HashingVectorizer, a transformer class that is mostly API compatible with CountVectorizer. HashingVectorizer is stateless, meaning that you don’t have to call fit on it:

```python
>>> from sklearn.feature_extraction.text import HashingVectorizer
>>> hv = HashingVectorizer(n_features=10)
>>> hv.transform(corpus)
...<4x10 sparse matrix of type '<... 'numpy.float64'>'
    with 16 stored elements in Compressed Sparse ... format>
```

You can see that 16 non-zero feature tokens were extracted in the vector output: this is less than the 19 non-zeros extracted previously by the CountVectorizer on the same toy corpus. The discrepancy comes from hash function collisions because of the low value of the n_features parameter.

In a real world setting, the n_features parameter can be left to its default value of $2^{20}$ (roughly one million possible features). If memory or downstream models size is an issue selecting a lower value such as $2^{18}$ might help without introducing too many additional collisions on typical text classification tasks.

Note that the dimensionality does not affect the CPU training time of algorithms which operate on CSR matrices (LinearSVC(dual=True), Perceptron, SGDClассifier, PassiveAggressive) but it does for algorithms that work with CSC matrices (LinearSVC(dual=False), Lasso(), etc).

Let’s try again with the default setting:

```python
>>> hv = HashingVectorizer()
>>> hv.transform(corpus)
...<4x1048576 sparse matrix of type '<... 'numpy.float64'>'
    with 19 stored elements in Compressed Sparse ... format>
```
scikit-learn user guide, Release 0.20.dev0

We no longer get the collisions, but this comes at the expense of a much larger dimensionality of the output space. Of
course, other terms than the 19 used here might still collide with each other.
The HashingVectorizer also comes with the following limitations:
• it is not possible to invert the model (no inverse_transform method), nor to access the original string
representation of the features, because of the one-way nature of the hash function that performs the mapping.
• it does not provide IDF weighting as that would introduce statefulness in the model. A TfidfTransformer
can be appended to it in a pipeline if required.
Performing out-of-core scaling with HashingVectorizer
An interesting development of using a HashingVectorizer is the ability to perform out-of-core scaling. This
means that we can learn from data that does not fit into the computer’s main memory.
A strategy to implement out-of-core scaling is to stream data to the estimator in mini-batches. Each mini-batch is
vectorized using HashingVectorizer so as to guarantee that the input space of the estimator has always the same
dimensionality. The amount of memory used at any time is thus bounded by the size of a mini-batch. Although there is
no limit to the amount of data that can be ingested using such an approach, from a practical point of view the learning
time is often limited by the CPU time one wants to spend on the task.
For a full-fledged example of out-of-core scaling in a text classification task see Out-of-core classification of text
documents.
Customizing the vectorizer classes
It is possible to customize the behavior by passing a callable to the vectorizer constructor:
>>> def my_tokenizer(s):
...
return s.split()
...
>>> vectorizer = CountVectorizer(tokenizer=my_tokenizer)
>>> vectorizer.build_analyzer()(u"Some... punctuation!") == (
...
['some...', 'punctuation!'])
True

In particular we name:
• preprocessor: a callable that takes an entire document as input (as a single string), and returns a possibly
transformed version of the document, still as an entire string. This can be used to remove HTML tags, lowercase
the entire document, etc.
• tokenizer: a callable that takes the output from the preprocessor and splits it into tokens, then returns a list
of these.
• analyzer: a callable that replaces the preprocessor and tokenizer. The default analyzers all call the preprocessor and tokenizer, but custom analyzers will skip this. N-gram extraction and stop word filtering take place
at the analyzer level, so a custom analyzer may have to reproduce these steps.
(Lucene users might recognize these names, but be aware that scikit-learn concepts may not map one-to-one onto
Lucene concepts.)
To make the preprocessor, tokenizer and analyzers aware of the model parameters it is possible to derive from the
class and override the build_preprocessor, build_tokenizer` and build_analyzer factory methods
instead of passing custom functions.
Some tips and tricks:

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• If documents are pre-tokenized by an external package, then store them in files (or strings) with the tokens separated by whitespace and pass `analyzer=str.split`.

• Fancy token-level analysis such as stemming, lemmatizing, compound splitting, filtering based on part-of-speech, etc. are not included in the scikit-learn codebase, but can be added by customizing either the tokenizer or the analyzer. Here’s a `CountVectorizer` with a tokenizer and lemmatizer using NLTK:

```python
>>> from nltk import word_tokenize
>>> from nltk.stem import WordNetLemmatizer
>>> class LemmaTokenizer(object):
...     def __init__(self):
...         self.wnl = WordNetLemmatizer()
...     def __call__(self, doc):
...         return [self.wnl.lemmatize(t) for t in word_tokenize(doc)]
...
>>> vect = CountVectorizer(tokenizer=LemmaTokenizer())
```

(Note that this will not filter out punctuation.)

The following example will, for instance, transform some British spelling to American spelling:

```python
>>> import re
>>> def to_british(tokens):
...     for t in tokens:
...         t = re.sub(r"(...)our$", r"\1or", t)
...         t = re.sub(r"([bt])re$", r"\1er", t)
...         t = re.sub(r"([iy])s(e|ing|ation)\", r"\1z\2", t)
...         t = re.sub(r"ogue$", "og", t)
...     yield t
...
>>> class CustomVectorizer(CountVectorizer):
...     def build_tokenizer(self):
...         tokenize = super(CustomVectorizer, self).build_tokenizer()
...         return lambda doc: list(to_british(tokenize(doc))
...
>>> print(CustomVectorizer().build_analyzer()(u"color colour"))
['...color', '...color']
```

for other styles of preprocessing; examples include stemming, lemmatization, or normalizing numerical tokens, with the latter illustrated in:

– Biclustering documents with the Spectral Co-clustering algorithm

Customizing the vectorizer can also be useful when handling Asian languages that do not use an explicit word separator such as whitespace.

Image feature extraction

Patch extraction

The `extract_patches_2d` function extracts patches from an image stored as a two-dimensional array, or three-dimensional with color information along the third axis. For rebuilding an image from all its patches, use `reconstruct_from_patches_2d`. For example let use generate a 4x4 pixel picture with 3 color channels (e.g. in RGB format):

```python
>>> import numpy as np
>>> from sklearn.feature_extraction import image
```
Let us now try to reconstruct the original image from the patches by averaging on overlapping areas:

```python
>>> reconstructed = image.reconstruct_from_patches_2d(patches, (4, 4, 3))
>>> np.testing.assert_array_equal(one_image, reconstructed)
```

The `PatchExtractor` class works in the same way as `extract_patches_2d`, only it supports multiple images as input. It is implemented as an estimator, so it can be used in pipelines. See:

```python
>>> five_images = np.arange(5 * 4 * 4 * 3).reshape(5, 4, 4, 3)
>>> patches = image.PatchExtractor((2, 2)).transform(five_images)
>>> patches.shape
(45, 2, 2, 3)
```

### Connectivity graph of an image

Several estimators in the scikit-learn can use connectivity information between features or samples. For instance Ward clustering ([Hierarchical clustering](#)) can cluster together only neighboring pixels of an image, thus forming contiguous patches:

For this purpose, the estimators use a ‘connectivity’ matrix, giving which samples are connected.

The function `img_to_graph` returns such a matrix from a 2D or 3D image. Similarly, `grid_to_graph` build a connectivity matrix for images given the shape of these image.

These matrices can be used to impose connectivity in estimators that use connectivity information, such as Ward clustering ([Hierarchical clustering](#)), but also to build precomputed kernels, or similarity matrices.

**Note:** Examples

- A demo of structured Ward hierarchical clustering on a raccoon face image
- Spectral clustering for image segmentation

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3.4.3 Preprocessing data

The `sklearn.preprocessing` package provides several common utility functions and transformer classes to change raw feature vectors into a representation that is more suitable for the downstream estimators.

In general, learning algorithms benefit from standardization of the data set. If some outliers are present in the set, robust scalers or transformers are more appropriate. The behaviors of the different scalers, transformers, and normalizers on a dataset containing marginal outliers is highlighted in *Compare the effect of different scalers on data with outliers*.

### Standardization, or mean removal and variance scaling

Standardization of datasets is a **common requirement for many machine learning estimators** implemented in scikit-learn; they might behave badly if the individual features do not more or less look like standard normally distributed data: Gaussian with **zero mean and unit variance**.

In practice we often ignore the shape of the distribution and just transform the data to center it by removing the mean value of each feature, then scale it by dividing non-constant features by their standard deviation.

For instance, many elements used in the objective function of a learning algorithm (such as the RBF kernel of Support Vector Machines or the l1 and l2 regularizers of linear models) assume that all features are centered around zero and have variance in the same order. If a feature has a variance that is orders of magnitude larger than others, it might dominate the objective function and make the estimator unable to learn from other features correctly as expected.

The function `scale` provides a quick and easy way to perform this operation on a single array-like dataset:

```python
>>> from sklearn import preprocessing
>>> import numpy as np

>>> X_train = np.array([[ 1., -1., 2.],
                      [ 2., 0., 0.],
                      [ 0., 1., -1.]])

>>> X_scaled = preprocessing.scale(X_train)

>>> X_scaled
array([[ 0., ..., -1.22..., 1.33...],
       [ 1.22..., 0., ..., -0.26...],
       [-1.22..., 1.22..., -1.06...]])
```

Scaled data has zero mean and unit variance:
The `preprocessing` module further provides a utility class `StandardScaler` that implements the Transformer API to compute the mean and standard deviation on a training set so as to be able to later reapply the same transformation on the testing set. This class is hence suitable for use in the early steps of a `sklearn.pipeline.Pipeline`:

```python
>>> scaler = preprocessing.StandardScaler().fit(X_train)
>>> scaler
StandardScaler(copy=True, with_mean=True, with_std=True)
>>> scaler.mean_
array([ 1. ..., 0. ..., 0.33...])
>>> scaler.scale_
array([ 0.81..., 0.81..., 1.24...])
>>> scaler.transform(X_train)
array([[ 0. ..., -1.22..., 1.33...],
       [ 1.22..., 0. ..., -0.26...],
       [-1.22..., 1.22..., -1.06...]])
```

The scaler instance can then be used on new data to transform it the same way it did on the training set:

```python
>>> X_test = [[-1., 1., 0.]]
>>> scaler.transform(X_test)
array([[-2.44..., 1.22..., -0.26...]])
```

It is possible to disable either centering or scaling by either passing `with_mean=False` or `with_std=False` to the constructor of `StandardScaler`.

### Scaling features to a range

An alternative standardization is scaling features to lie between a given minimum and maximum value, often between zero and one, or so that the maximum absolute value of each feature is scaled to unit size. This can be achieved using `MinMaxScaler` or `MaxAbsScaler`, respectively.

The motivation to use this scaling include robustness to very small standard deviations of features and preserving zero entries in sparse data.

Here is an example to scale a toy data matrix to the `[0, 1]` range:

```python
>>> X_train = np.array([[ 1., -1., 2.],
                      [ 2., 0., 0.],
                      [ 0., 1., -1.]])
```

```python
>>> min_max_scaler = preprocessing.MinMaxScaler()
>>> X_train_minmax = min_max_scaler.fit_transform(X_train)
>>> X_train_minmax
array([[ 0.5 , 0. , 1. ],
       [ 1. , 0.5 , 0.33333333],
       [ 0. , 1. , 0. ]])
```
The same instance of the transformer can then be applied to some new test data unseen during the fit call: the same scaling and shifting operations will be applied to be consistent with the transformation performed on the train data:

```python
>>> X_test = np.array([[-3., -1., 4.]])
>>> X_test_minmax = min_max_scaler.transform(X_test)
>>> X_test_minmax
array([[-1.5       ,  0.        , 1.66666667]])
```

It is possible to introspect the scaler attributes to find about the exact nature of the transformation learned on the training data:

```python
>>> min_max_scaler.scale_
array([ 0.5 , 0.5 , 0.33...])
>>> min_max_scaler.min_
array([ 0. , 0.5 , 0.33...])
```

If `MinMaxScaler` is given an explicit `feature_range=(min, max)` the full formula is:

\[
X_{\text{std}} = \frac{X - X_{\text{min}}(\text{axis=0})}{(X_{\text{max}}(\text{axis=0}) - X_{\text{min}}(\text{axis=0}))}
\]

\[
X_{\text{scaled}} = X_{\text{std}} \times (\text{max} - \text{min}) + \text{min}
\]

`MaxAbsScaler` works in a very similar fashion, but scales in a way that the training data lies within the range \([-1, 1]\) by dividing through the largest maximum value in each feature. It is meant for data that is already centered at zero or sparse data.

Here is how to use the toy data from the previous example with this scaler:

```python
>>> X_train = np.array([[ 1., -1., 2.],
...                      [ 2., 0., 0.],
...                      [ 0., 1., -1.]])
... >>> max_abs_scaler = preprocessing.MaxAbsScaler()
... >>> X_train_maxabs = max_abs_scaler.fit_transform(X_train)
... >>> X_train_maxabs
# doctest +NORMALIZE_WHITESPACE^
array([[ 0.5, -1., 1. ],
       [ 1. , 0. , 0. ],
       [ 0. , 1. , -0.5]])
>>> X_test = np.array([[-3., -1., 4.]])
>>> X_test_maxabs = max_abs_scaler.transform(X_test)
>>> X_test_maxabs
array([[ -1.5, -1., 2. ]])
>>> max_abs_scaler.scale_
array([ 2., 1., 2.])
```

As with `scale`, the module further provides convenience functions `minmax_scale` and `maxabs_scale` if you don’t want to create an object.

### Scaling sparse data

Centering sparse data would destroy the sparseness structure in the data, and thus rarely is a sensible thing to do. However, it can make sense to scale sparse inputs, especially if features are on different scales.

`MaxAbsScaler` and `maxabs_scale` were specifically designed for scaling sparse data, and are the recommended way to go about this. However, `scale` and `StandardScaler` can accept `scipy.sparse` matrices as input, as long as `with_mean=False` is explicitly passed to the constructor. Otherwise a `ValueError` will be raised as
silently centering would break the sparsity and would often crash the execution by allocating excessive amounts of memory unintentionally. *RobustScaler* cannot be fitted to sparse inputs, but you can use the transform method on sparse inputs.

Note that the scalers accept both Compressed Sparse Rows and Compressed Sparse Columns format (see *scipy.sparse.csr_matrix* and *scipy.sparse.csc_matrix*). Any other sparse input will be converted to the *Compressed Sparse Rows representation*. To avoid unnecessary memory copies, it is recommended to choose the CSR or CSC representation upstream.

Finally, if the centered data is expected to be small enough, explicitly converting the input to an array using the toarray method of sparse matrices is another option.

### Scaling data with outliers

If your data contains many outliers, scaling using the mean and variance of the data is likely to not work very well. In these cases, you can use *robust_scale* and *RobustScaler* as drop-in replacements instead. They use more robust estimates for the center and range of your data.

**References:**

Further discussion on the importance of centering and scaling data is available on this FAQ: [Should I normalize/standardize/rescale the data?](https://scikit-learn.org/stable/faq.html#should-i-normalize-standardize-rescale-the-data)

### Scaling vs Whitening

It is sometimes not enough to center and scale the features independently, since a downstream model can further make some assumption on the linear independence of the features.

To address this issue you can use *sklearn.decomposition.PCA* or *sklearn.decomposition.RandomizedPCA* with whiten=True to further remove the linear correlation across features.

### Scaling a 1D array

All above functions (i.e. *scale*, *minmax_scale*, *maxabs_scale*, and *robust_scale*) accept 1D array which can be useful in some specific case.

### Centering kernel matrices

If you have a kernel matrix of a kernel $K$ that computes a dot product in a feature space defined by function $phi$, a *KernelCenterer* can transform the kernel matrix so that it contains inner products in the feature space defined by $phi$ followed by removal of the mean in that space.

### Non-linear transformation

Like scalers, *QuantileTransformer* puts each feature into the same range or distribution. However, by performing a rank transformation, it smooths out unusual distributions and is less influenced by outliers than scaling methods. It does, however, distort correlations and distances within and across features.

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QuantileTransformer and quantile_transform provide a non-parametric transformation based on the quantile function to map the data to a uniform distribution with values between 0 and 1:

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn.model_selection import train_test_split

>>> iris = load_iris()
>>> X, y = iris.data, iris.target
>>> X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

>>> quantile_transformer = preprocessing.QuantileTransformer(random_state=0)

>>> X_train_trans = quantile_transformer.fit_transform(X_train)
>>> X_test_trans = quantile_transformer.transform(X_test)

>>> np.percentile(X_train[:, 0], [0, 25, 50, 75, 100])
array([ 4.3,  5.1,  5.8,  6.5,  7.9])
```

This feature corresponds to the sepal length in cm. Once the quantile transformation applied, those landmarks approach closely the percentiles previously defined:

```python
>>> np.percentile(X_train_trans[:, 0], [0, 25, 50, 75, 100])
... array([ 0.00..., 0.24..., 0.49..., 0.73..., 0.99... ])
```

This can be confirmed on an independent testing set with similar remarks:

```python
>>> np.percentile(X_test[:, 0], [0, 25, 50, 75, 100])
... array([ 4.4 ,  5.125,  5.75 ,  6.175,  7.3 ])
>>> np.percentile(X_test_trans[:, 0], [0, 25, 50, 75, 100])
... array([ 0.01..., 0.25..., 0.46..., 0.60... , 0.94...])
```

It is also possible to map the transformed data to a normal distribution by setting output_distribution='normal':

```python
>>> quantile_transformer = preprocessing.QuantileTransformer(
...     output_distribution='normal', random_state=0)

>>> X_trans = quantile_transformer.fit_transform(X)

>>> quantile_transformer.quantiles_
array([[ 4.3...,  2...,  1...,  0.1...],
       [ 4.31...,  2.02...,  1.01...,  0.1...],
       [ 4.32...,  2.05...,  1.02...,  0.1...],
       ...
       [ 7.84...,  4.34...,  6.84...,  2.5...],
       [ 7.87...,  4.37...,  6.87...,  2.5...],
       [ 7.9...,  4.4...,  6.9...,  2.5...]])
```

Thus the median of the input becomes the mean of the output, centered at 0. The normal output is clipped so that the input’s minimum and maximum — corresponding to the 1e-7 and 1 - 1e-7 quantiles respectively — do not become infinite under the transformation.

Normalization

Normalization is the process of scaling individual samples to have unit norm. This process can be useful if you plan to use a quadratic form such as the dot-product or any other kernel to quantify the similarity of any pair of samples.

This assumption is the base of the Vector Space Model often used in text classification and clustering contexts.

The function normalize provides a quick and easy way to perform this operation on a single array-like dataset, either using the 'l1' or 'l2' norms:
The `preprocessing` module further provides a utility class `Normalizer` that implements the same operation using the Transformer API (even though the `fit` method is useless in this case: the class is stateless as this operation treats samples independently).

This class is hence suitable for use in the early steps of a `sklearn.pipeline.Pipeline`:

```python
>>> normalizer = preprocessing.Normalizer().fit(X)  # fit does nothing
>>> normalizer
Normalizer(copy=True, norm='l2')
```

The normalizer instance can then be used on sample vectors as any transformer:

```python
>>> normalizer.transform(X)
array([[ 0.40..., -0.40..., 0.81...],
       [ 1. ..., 0. ..., 0. ...],
       [ 0. ..., 0.70..., -0.70...]])
```

```python
>>> normalizer.transform([[-1., 1., 0.]]
array([[-0.70..., 0.70..., 0. ...]])
```

**Sparse input**

`normalize` and `Normalizer` accept both dense array-like and sparse matrices from `scipy.sparse` as input.

For sparse input the data is converted to the Compressed Sparse Rows representation (see `scipy.sparse.csr_matrix`) before being fed to efficient Cython routines. To avoid unnecessary memory copies, it is recommended to choose the CSR representation upstream.

**Binarization**

**Feature binarization**

Feature binarization is the process of thresholding numerical features to get boolean values. This can be useful for downstream probabilistic estimators that make assumption that the input data is distributed according to a multi-variate Bernoulli distribution. For instance, this is the case for the `sklearn.neural_network.BernoulliRBM`.

It is also common among the text processing community to use binary feature values (probably to simplify the probabilistic reasoning) even if normalized counts (a.k.a. term frequencies) or TF-IDF valued features often perform slightly better in practice.

As for the `Normalizer`, the utility class `Binarizer` is meant to be used in the early stages of `sklearn.pipeline.Pipeline`. The `fit` method does nothing as each sample is treated independently of others:
>>> X = [[1., -1., 2.],
...      [2., 0., 0.],
...      [0., 1., -1.]]

>>> binarizer = preprocessing.Binarizer().fit(X)  # fit does nothing
>>> binarizer
Binarizer(c...
By default, how many values each feature can take is inferred automatically from the dataset. It is possible to specify this explicitly using the parameter `n_values`. There are two genders, three possible continents and four web browsers in our dataset. Then we fit the estimator, and transform a data point. In the result, the first two numbers encode the gender, the next set of three numbers the continent and the last four the web browser.

Note that, if there is a possibility that the training data might have missing categorical features, one has to explicitly set `n_values`. For example,

```python
>>> enc = preprocessing.OneHotEncoder(n_values=[2, 3, 4])
>>> # Note that there are missing categorical values for the 2nd and 3rd
>>> # features
>>> enc.fit([[1, 2, 3], [0, 2, 0]])
OneHotEncoder(categorical_features='all', dtype=<... 'numpy.float64'>, handle_unknown='error', n_values=[2, 3, 4], sparse=True)
>>> enc.transform([[1, 0, 0]]).toarray()
array([[ 0., 1., 1., 0., 0., 1., 0., 0., 0.]])
```

See *Loading features from dicts* for categorical features that are represented as a dict, not as integers.

### Imputation of missing values

For various reasons, many real world datasets contain missing values, often encoded as blanks, NaNs or other placeholders. Such datasets however are incompatible with scikit-learn estimators which assume that all values in an array are numerical, and that all have and hold meaning. A basic strategy to use incomplete datasets is to discard entire rows and/or columns containing missing values. However, this comes at the price of losing data which may be valuable (even though incomplete). A better strategy is to impute the missing values, i.e., to infer them from the known part of the data.

The `Imputer` class provides basic strategies for imputing missing values, either using the mean, the median or the most frequent value of the row or column in which the missing values are located. This class also allows for different missing values encodings.

The following snippet demonstrates how to replace missing values, encoded as `np.nan`, using the mean value of the columns (axis 0) that contain the missing values:

```python
>>> import numpy as np
>>> from sklearn.preprocessing import Imputer

>>> imp = Imputer(missing_values='NaN', strategy='mean', axis=0)
>>> imp.fit([[1, 2], [np.nan, 3], [7, 6]])
Imputer(axis=0, copy=True, missing_values='NaN', strategy='mean', verbose=0)
>>> X = [[np.nan, 2], [5, np.nan], [7, 6]]
>>> print(imp.transform(X))
[[ 4.  2.]
 [ 6. 3.666...]
 [ 7.  6.]]
```

The `Imputer` class also supports sparse matrices:

```python
>>> import scipy.sparse as sp

>>> X = sp.csc_matrix([[1, 2], [0, 3], [7, 6]])
>>> imp = Imputer(missing_values=0, strategy='mean', axis=0)
>>> imp.fit(X)
Imputer(axis=0, copy=True, missing_values='NaN', strategy='mean', verbose=0)
>>> X_test = sp.csc_matrix([[0, 2], [6, 0], [7, 6]])
>>> print(imp.transform(X_test))
[[ 4.  2.]
 [ 6. 3.666...]
 [ 7.  6.]]
```
Note that, here, missing values are encoded by 0 and are thus implicitly stored in the matrix. This format is thus suitable when there are many more missing values than observed values.

`Imputer` can be used in a Pipeline as a way to build a composite estimator that supports imputation. See *Imputing missing values before building an estimator*.

### Generating polynomial features

Often it’s useful to add complexity to the model by considering nonlinear features of the input data. A simple and common method to use is polynomial features, which can get features’ high-order and interaction terms. It is implemented in `PolynomialFeatures`:

```python
>>> import numpy as np
>>> from sklearn.preprocessing import PolynomialFeatures
>>> X = np.arange(6).reshape(3, 2)
>>> X
array([[0, 1],
       [2, 3],
       [4, 5]])
>>> poly = PolynomialFeatures(2)
>>> poly.fit_transform(X)
array([[ 1.,  0.,  1.,  0.,  0.,  1.],
       [ 1.,  2.,  3.,  4.,  6.,  9.],
       [ 1.,  4.,  5.,  16., 20., 25.]])
```

The features of X have been transformed from \((X_1, X_2)\) to \(1, X_1, X_2, X_1^2, X_1X_2, X_2^2)\).

In some cases, only interaction terms among features are required, and it can be gotten with the setting `interaction_only=True`:

```python
>>> X = np.arange(9).reshape(3, 3)
>>> X
array([[0, 1, 2],
       [3, 4, 5],
       [6, 7, 8]])
>>> poly = PolynomialFeatures(degree=3, interaction_only=True)
>>> poly.fit_transform(X)
array([[ 1.,  0.,  1.,  0.,  0.,  2.,  0.,
        1.,  2.,  3.,  4.,  6.,  9.,
        1.,  4.,  5., 16., 20., 25.,  81.],
       [ 1.,  3.,  4.,  5.,  12., 15., 20., 60.,
        1.,  6.,  7.,  8.,  42., 48., 56., 336.],
```

The features of X have been transformed from \((X_1, X_2, X_3)\) to \(1, X_1, X_2, X_3, X_1X_2, X_1X_3, X_2X_3, X_1X_2X_3\).

Note that polynomial features are used implicitly in kernel methods (e.g., `sklearn.svm.SVC`, `sklearn.decomposition.KernelPCA`) when using polynomial `Kernel functions`.

See *Polynomial interpolation* for Ridge regression using created polynomial features.

### Custom transformers

Often, you will want to convert an existing Python function into a transformer to assist in data cleaning or processing. You can implement a transformer from an arbitrary function with `FunctionTransformer`. For example, to build a transformer that applies a log transformation in a pipeline, do:
You can ensure that `func` and `inverse_func` are the inverse of each other by setting `check_inverse=True` and calling `fit` before `transform`. Please note that a warning is raised and can be turned into an error with a `filterwarnings`:

```python
>>> import warnings
>>> warnings.filterwarnings("error", message=".*check_inverse*.", category=UserWarning, append=False)
```

For a full code example that demonstrates using a `FunctionTransformer` to do custom feature selection, see Using FunctionTransformer to select columns.

### 3.4.4 Unsupervised dimensionality reduction

If your number of features is high, it may be useful to reduce it with an unsupervised step prior to supervised steps. Many of the `Unsupervised learning` methods implement a `transform` method that can be used to reduce the dimensionality. Below we discuss two specific example of this pattern that are heavily used.

#### Pipelining

The unsupervised data reduction and the supervised estimator can be chained in one step. See Pipeline: chaining estimators.

#### PCA: principal component analysis

`decomposition.PCA` looks for a combination of features that capture well the variance of the original features. See Decomposing signals in components (matrix factorization problems).

**Examples**

- Faces recognition example using eigenfaces and SVMs

#### Random projections

The module: `random_projection` provides several tools for data reduction by random projections. See the relevant section of the documentation: Random Projection.

**Examples**

- The Johnson-Lindenstrauss bound for embedding with random projections
Feature agglomeration

`cluster.FeatureAgglomeration` applies Hierarchical clustering to group together features that behave similarly.

Examples

- Feature agglomeration vs. univariate selection
- Feature agglomeration

Feature scaling

Note that if features have very different scaling or statistical properties, `cluster.FeatureAgglomeration` may not be able to capture the links between related features. Using a `preprocessing.StandardScaler` can be useful in these settings.

3.4.5 Random Projection

The `sklearn.random_projection` module implements a simple and computationally efficient way to reduce the dimensionality of the data by trading a controlled amount of accuracy (as additional variance) for faster processing times and smaller model sizes. This module implements two types of unstructured random matrix: Gaussian random matrix and sparse random matrix.

The dimensions and distribution of random projections matrices are controlled so as to preserve the pairwise distances between any two samples of the dataset. Thus random projection is a suitable approximation technique for distance based method.

References:


The Johnson-Lindenstrauss lemma

The main theoretical result behind the efficiency of random projection is the Johnson-Lindenstrauss lemma (quoting Wikipedia):

In mathematics, the Johnson-Lindenstrauss lemma is a result concerning low-distortion embeddings of points from high-dimensional into low-dimensional Euclidean space. The lemma states that a small set of points in a high-dimensional space can be embedded into a space of much lower dimension in such a way that distances between the points are nearly preserved. The map used for the embedding is at least Lipschitz, and can even be taken to be an orthogonal projection.
Knowing only the number of samples, the `sklearn.random_projection.johnson_lindenstrauss_min_dim` estimates conservatively the minimal size of the random subspace to guarantee a bounded distortion introduced by the random projection:

```python
>>> from sklearn.random_projection import johnson_lindenstrauss_min_dim
>>> johnson_lindenstrauss_min_dim(n_samples=1e6, eps=0.5)
663
>>> johnson_lindenstrauss_min_dim(n_samples=1e6, eps=[0.5, 0.1, 0.01])
array([ 663, 11841, 1112658])
>>> johnson_lindenstrauss_min_dim(n_samples=[1e4, 1e5, 1e6], eps=0.1)
array([ 7894, 9868, 11841])
```

Example:
- See *The Johnson-Lindenstrauss bound for embedding with random projections* for a theoretical explication on the Johnson-Lindenstrauss lemma and an empirical validation using sparse random matrices.

References:

### Gaussian random projection

The `sklearn.random_projection.GaussianRandomProjection` reduces the dimensionality by projecting the original input space on a randomly generated matrix where components are drawn from the following distribution $\mathcal{N}(0, \frac{1}{n_{\text{components}}})$.

Here a small excerpt which illustrates how to use the Gaussian random projection transformer:
Sparse random projection

The `sklearn.random_projection.SparseRandomProjection` reduces the dimensionality by projecting the original input space using a sparse random matrix.

Sparse random matrices are an alternative to dense Gaussian random projection matrix that guarantees similar embedding quality while being much more memory efficient and allowing faster computation of the projected data.

If we define $s = 1 / \text{density}$, the elements of the random matrix are drawn from

$$
\begin{align*}
&\begin{cases}
-\sqrt{s / \text{n\_components}} & \text{with probability } 1 - 1/s \\
0 & 1/s \\
+\sqrt{s / \text{n\_components}} & 1/2s
\end{cases}
\end{align*}
$$

where $\text{n\_components}$ is the size of the projected subspace. By default the density of non zero elements is set to the minimum density as recommended by Ping Li et al.: $1/\sqrt{\text{N\_features}}$.

Here a small excerpt which illustrates how to use the sparse random projection transformer:

```python
>>> import numpy as np
>>> from sklearn import random_projection
>>> X = np.random.rand(100,10000)
>>> transformer = random_projection.SparseRandomProjection()
>>> X_new = transformer.fit_transform(X)
>>> X_new.shape
(100, 3947)
```
4.6 Kernel Approximation

This submodule contains functions that approximate the feature mappings that correspond to certain kernels, as they are used for example in support vector machines (see Support Vector Machines). The following feature functions perform non-linear transformations of the input, which can serve as a basis for linear classification or other algorithms.

The advantage of using approximate explicit feature maps compared to the kernel trick, which makes use of feature maps implicitly, is that explicit mappings can be better suited for online learning and can significantly reduce the cost of learning with very large datasets. Standard kernelized SVMs do not scale well to large datasets, but using an approximate kernel map it is possible to use much more efficient linear SVMs. In particular, the combination of kernel map approximations with SGDClassifier can make non-linear learning on large datasets possible.

Since there has not been much empirical work using approximate embeddings, it is advisable to compare results against exact kernel methods when possible.

See also:

Polynomial regression: extending linear models with basis functions for an exact polynomial transformation.

Nystroem Method for Kernel Approximation

The Nystroem method, as implemented in Nystroem is a general method for low-rank approximations of kernels. It achieves this by essentially subsampling the data on which the kernel is evaluated. By default Nystroem uses the rbf kernel, but it can use any kernel function or a precomputed kernel matrix. The number of samples used - which is also the dimensionality of the features computed - is given by the parameter n_components.

Radial Basis Function Kernel

The RBFSampler constructs an approximate mapping for the radial basis function kernel, also known as Random Kitchen Sinks [RR2007]. This transformation can be used to explicitly model a kernel map, prior to applying a linear algorithm, for example a linear SVM:
The mapping relies on a Monte Carlo approximation to the kernel values. The `fit` function performs the Monte Carlo sampling, whereas the `transform` method performs the mapping of the data. Because of the inherent randomness of the process, results may vary between different calls to the `fit` function.

The `fit` function takes two arguments: `n_components`, which is the target dimensionality of the feature transform, and `gamma`, the parameter of the RBF-kernel. A higher `n_components` will result in a better approximation of the kernel and will yield results more similar to those produced by a kernel SVM. Note that “fitting” the feature function does not actually depend on the data given to the `fit` function. Only the dimensionality of the data is used. Details on the method can be found in [RR2007].

For a given value of `n_components` `RBFSampler` is often less accurate as `Nystroem`. `RBFSampler` is cheaper to compute, though, making use of larger feature spaces more efficient.

Fig. 3.9: Comparing an exact RBF kernel (left) with the approximation (right)

**Examples:**

- **Explicit feature map approximation for RBF kernels**

**Additive Chi Squared Kernel**

The additive chi squared kernel is a kernel on histograms, often used in computer vision.

The additive chi squared kernel as used here is given by

\[
k(x, y) = \sum_i \frac{2x_i y_i}{x_i + y_i}
\]
This is not exactly the same as sklearn.metrics.additive_ch2_kernel. The authors of [VZ2010] prefer the version above as it is always positive definite. Since the kernel is additive, it is possible to treat all components \( x_i \) separately for embedding. This makes it possible to sample the Fourier transform in regular intervals, instead of approximating using Monte Carlo sampling.

The class AdditiveChi2Sampler implements this component wise deterministic sampling. Each component is sampled \( n \) times, yielding \( 2n + 1 \) dimensions per input dimension (the multiple of two stems from the real and complex part of the Fourier transform). In the literature, \( n \) is usually chosen to be 1 or 2, transforming the dataset to size \( n_{\text{samples}} \times 5 \times n_{\text{features}} \) (in the case of \( n = 2 \)).

The approximate feature map provided by AdditiveChi2Sampler can be combined with the approximate feature map provided by RBFSampler to yield an approximate feature map for the exponentiated chi squared kernel. See the [VZ2010] for details and [VVZ2010] for combination with the RBFSampler.

**Skewed Chi Squared Kernel**

The skewed chi squared kernel is given by:

\[
k(x, y) = \prod_i \frac{2\sqrt{x_i + c} \sqrt{y_i + c}}{x_i + y_i + 2c}
\]

It has properties that are similar to the exponentiated chi squared kernel often used in computer vision, but allows for a simple Monte Carlo approximation of the feature map.

The usage of the SkewedChi2Sampler is the same as the usage described above for the RBFSampler. The only difference is in the free parameter, that is called \( c \). For a motivation for this mapping and the mathematical details see [LS2010].

**Mathematical Details**

Kernel methods like support vector machines or kernelized PCA rely on a property of reproducing kernel Hilbert spaces. For any positive definite kernel function \( k \) (a so called Mercer kernel), it is guaranteed that there exists a mapping \( \phi \) into a Hilbert space \( \mathcal{H} \), such that

\[
k(x, y) = \langle \phi(x), \phi(y) \rangle
\]

Where \( \langle \cdot, \cdot \rangle \) denotes the inner product in the Hilbert space.

If an algorithm, such as a linear support vector machine or PCA, relies only on the scalar product of data points \( x_i \), one may use the value of \( k(x_i, x_j) \), which corresponds to applying the algorithm to the mapped data points \( \phi(x_i) \). The advantage of using \( k \) is that the mapping \( \phi \) never has to be calculated explicitly, allowing for arbitrary large features (even infinite).

One drawback of kernel methods is, that it might be necessary to store many kernel values \( k(x_i, x_j) \) during optimization. If a kernelized classifier is applied to new data \( y_j \), \( k(x_i, y_j) \) needs to be computed to make predictions, possibly for many different \( x_i \) in the training set.

The classes in this submodule allow to approximate the embedding \( \phi \), thereby working explicitly with the representations \( \phi(x_i) \), which obviates the need to apply the kernel or store training examples.

**References:**
3.4.7 Pairwise metrics, Affinities and Kernels

The sklearn.metrics.pairwise submodule implements utilities to evaluate pairwise distances or affinity of sets of samples.

This module contains both distance metrics and kernels. A brief summary is given on the two here.

Distance metrics are functions $d(a, b)$ such that $d(a, b) < d(a, c)$ if objects $a$ and $b$ are considered “more similar” than objects $a$ and $c$. Two objects exactly alike would have a distance of zero. One of the most popular examples is Euclidean distance. To be a ‘true’ metric, it must obey the following four conditions:

1. $d(a, b) \geq 0$, for all $a$ and $b$
2. $d(a, b) = 0$, if and only if $a = b$, positive definiteness
3. $d(a, b) = d(b, a)$, symmetry
4. $d(a, c) \leq d(a, b) + d(b, c)$, the triangle inequality

Kernels are measures of similarity, i.e. $s(a, b) > s(a, c)$ if objects $a$ and $b$ are considered “more similar” than objects $a$ and $c$. A kernel must also be positive semi-definite.

There are a number of ways to convert between a distance metric and a similarity measure, such as a kernel. Let $D$ be the distance, and $S$ be the kernel:

1. $S = \exp(-D \times \text{gamma})$, where one heuristic for choosing gamma is $1 / \text{num_features}$
2. $S = 1. / (D / \text{np.max(D)})$

**Cosine similarity**

cosine_similarity computes the L2-normalized dot product of vectors. That is, if $x$ and $y$ are row vectors, their cosine similarity $k$ is defined as:

$$k(x, y) = \frac{xy^T}{\|x\|\|y\|}$$

This is called cosine similarity, because Euclidean (L2) normalization projects the vectors onto the unit sphere, and their dot product is then the cosine of the angle between the points denoted by the vectors.

This kernel is a popular choice for computing the similarity of documents represented as tf-idf vectors. cosine_similarity accepts scipy.sparse matrices. (Note that the tf-idf functionality in sklearn.feature_extraction.text can produce normalized vectors, in which case cosine_similarity is equivalent to linear_kernel, only slower.)

**References:**


**Linear kernel**

The function linear_kernel computes the linear kernel, that is, a special case of polynomial_kernel with degree=1 and coef0=0 (homogeneous). If $x$ and $y$ are column vectors, their linear kernel is:

$$k(x, y) = x^T y$$
Polynomial kernel

The function `polynomial_kernel` computes the degree-d polynomial kernel between two vectors. The polynomial kernel represents the similarity between two vectors. Conceptually, the polynomial kernels considers not only the similarity between vectors under the same dimension, but also across dimensions. When used in machine learning algorithms, this allows to account for feature interaction.

The polynomial kernel is defined as:

\[ k(x, y) = (\gamma x^\top y + c_0)^d \]

where:

- \( x, y \) are the input vectors
- \( d \) is the kernel degree

If \( c_0 = 0 \) the kernel is said to be homogeneous.

Sigmoid kernel

The function `sigmoid_kernel` computes the sigmoid kernel between two vectors. The sigmoid kernel is also known as hyperbolic tangent, or Multilayer Perceptron (because, in the neural network field, it is often used as neuron activation function). It is defined as:

\[ k(x, y) = \tanh(\gamma x^\top y + c_0) \]

where:

- \( x, y \) are the input vectors
- \( \gamma \) is known as slope
- \( c_0 \) is known as intercept

RBF kernel

The function `rbf_kernel` computes the radial basis function (RBF) kernel between two vectors. This kernel is defined as:

\[ k(x, y) = \exp(-\gamma ||x - y||^2) \]

where \( x \) and \( y \) are the input vectors. If \( \gamma = \sigma^{-2} \) the kernel is known as the Gaussian kernel of variance \( \sigma^2 \).

Laplacian kernel

The function `laplacian_kernel` is a variant on the radial basis function kernel defined as:

\[ k(x, y) = \exp(-\gamma ||x - y||_1) \]

where \( x \) and \( y \) are the input vectors and \( ||x - y||_1 \) is the Manhattan distance between the input vectors.

It has proven useful in ML applied to noiseless data. See e.g. Machine learning for quantum mechanics in a nutshell.
Chi-squared kernel

The chi-squared kernel is a very popular choice for training non-linear SVMs in computer vision applications. It can be computed using `chi2_kernel` and then passed to an `sklearn.svm.SVC` with `kernel="precomputed"`:

```python
>>> from sklearn.svm import SVC
>>> from sklearn.metrics.pairwise import chi2_kernel

>>> X = [[0, 1], [1, 0], [.2, .8], [.7, .3]]
>>> y = [0, 1, 0, 1]
>>> K = chi2_kernel(X, gamma=.5)
>>> K
array([[ 1. ,  0.36...,  0.89...,  0.58...],
       [ 0.36...,  1. ,  0.51...,  0.83...],
       [ 0.89...,  0.51...,  1. ,  0.77... ],
       [ 0.58...,  0.83...,  0.77...,  1. ]])

>>> svm = SVC(kernel='precomputed').fit(K, y)
>>> svm.predict(K)
array([0, 1, 0, 1])
```

It can also be directly used as the `kernel` argument:

```python
>>> svm = SVC(kernel=chi2_kernel).fit(X, y)
>>> svm.predict(X)
array([0, 1, 0, 1])
```

The chi squared kernel is given by

\[
k(x, y) = \exp\left(-\gamma \sum_i \frac{(x[i] - y[i])^2}{x[i] + y[i]}\right)
\]

The data is assumed to be non-negative, and is often normalized to have an L1-norm of one. The normalization is rationalized with the connection to the chi squared distance, which is a distance between discrete probability distributions.

The chi squared kernel is most commonly used on histograms (bags) of visual words.

References:


3.4.8 Transforming the prediction target (y)

Label binarization

`LabelBinarizer` is a utility class to help create a label indicator matrix from a list of multi-class labels:

```python
>>> from sklearn import preprocessing

>>> lb = preprocessing.LabelBinarizer()
>>> lb.fit([1, 2, 6, 4, 2])
LabelBinarizer(neg_label=0, pos_label=1, sparse_output=False)
>>> lb.classes_
array([1, 2, 6, 4])
```
array([1, 2, 4, 6])

```python
>>> lb.transform([1, 6])
array([[1, 0, 0, 0],
      [0, 0, 0, 1]])
```

For multiple labels per instance, use `MultiLabelBinarizer`:

```python
>>> lb = preprocessing.MultiLabelBinarizer()
>>> lb.fit_transform(((1, 2), (3,)))
array([[1, 1, 0],
      [0, 0, 1]])
```

### Label encoding

`LabelEncoder` is a utility class to help normalize labels such that they contain only values between 0 and n_classes-1. This is sometimes useful for writing efficient Cython routines. `LabelEncoder` can be used as follows:

```python
>>> from sklearn import preprocessing
>>> le = preprocessing.LabelEncoder()
>>> le.fit([1, 2, 2, 6])
```

```python
>>> le.classes_
array([1, 2, 6])
```

```python
>>> le.transform([1, 1, 2, 6])
array([0, 0, 1, 2])
```

```python
>>> le.inverse_transform([0, 0, 1, 2])
array([1, 1, 2, 6])
```

It can also be used to transform non-numerical labels (as long as they are hashable and comparable) to numerical labels:

```python
>>> le = preprocessing.LabelEncoder()
>>> le.fit(['paris', 'paris', 'tokyo', 'amsterdam'])
```

```python
>>> list(le.classes_)
['amsterdam', 'paris', 'tokyo']
```

```python
>>> le.transform(['tokyo', 'tokyo', 'paris'])
array([2, 2, 1])
```

```python
>>> list(le.inverse_transform([2, 2, 1]))
['tokyo', 'tokyo', 'paris']
```

### 3.5 Dataset loading utilities

The `sklearn.datasets` package embeds some small toy datasets as introduced in the `Getting Started` section.

To evaluate the impact of the scale of the dataset (n_samples and n_features) while controlling the statistical properties of the data (typically the correlation and informativeness of the features), it is also possible to generate synthetic data.

This package also features helpers to fetch larger datasets commonly used by the machine learning community to benchmark algorithm on data that comes from the 'real world'.
3.5.1 General dataset API

There are three distinct kinds of dataset interfaces for different types of datasets. The simplest one is the interface for sample images, which is described below in the Sample images section.

The dataset generation functions and the svmlight loader share a simplistic interface, returning a tuple \((X, y)\) consisting of a \(n\_samples \times n\_features\) numpy array \(X\) and an array of length \(n\_samples\) containing the targets \(y\).

The toy datasets as well as the ‘real world’ datasets and the datasets fetched from mldata.org have more sophisticated structure. These functions return a dictionary-like object holding at least two items: an array of shape \(n\_samples \times n\_features\) with key data (except for 20newsgroups) and a numpy array of length \(n\_samples\), containing the target values, with key target.

The datasets also contain a description in DESCR and some contain feature_names and target_names. See the dataset descriptions below for details.

3.5.2 Toy datasets

scikit-learn comes with a few small standard datasets that do not require to download any file from some external website.

```python
load_boston([return_X_y])  # Load and return the boston house-prices dataset (regression).
load_iris([return_X_y])    # Load and return the iris dataset (classification).
load_diabetes([return_X_y]) # Load and return the diabetes dataset (regression).
load_digits([n_class, return_X_y]) # Load and return the digits dataset (classification).
load_linnerud([return_X_y])  # Load and return the linnerud dataset (multivariate regression).
load_wine([return_X_y])     # Load and return the wine dataset (classification).
load_breast_cancer([return_X_y]) # Load and return the breast cancer wisconsin dataset (classification).
```

These datasets are useful to quickly illustrate the behavior of the various algorithms implemented in the scikit. They are however often too small to be representative of real world machine learning tasks.

3.5.3 Sample images

The scikit also embed a couple of sample JPEG images published under Creative Commons license by their authors. Those image can be useful to test algorithms and pipeline on 2D data.

```python
load_sample_images() # Load sample images for image manipulation.
load_sample_image(image_name) # Load the numpy array of a single sample image
```
Warning: The default coding of images is based on the uint8 dtype to spare memory. Often machine learning algorithms work best if the input is converted to a floating point representation first. Also, if you plan to use matplotlib.pyplot.imshow don’t forget to scale to the range 0 - 1 as done in the following example.

Examples:

- Color Quantization using K-Means

3.5.4 Sample generators

In addition, scikit-learn includes various random sample generators that can be used to build artificial datasets of controlled size and complexity.

Generators for classification and clustering

These generators produce a matrix of features and corresponding discrete targets.

Single label

Both make_blobs and make_classification create multiclass datasets by allocating each class one or more normally-distributed clusters of points. make_blobs provides greater control regarding the centers and standard deviations of each cluster, and is used to demonstrate clustering. make_classification specialises in introducing noise by way of: correlated, redundant and uninformative features; multiple Gaussian clusters per class; and linear transformations of the feature space.

make_gaussian_quantiles divides a single Gaussian cluster into near-equal-size classes separated by concentric hyperspheres. make_hastie_10_2 generates a similar binary, 10-dimensional problem.
make_circles and make_moons generate 2d binary classification datasets that are challenging to certain algorithms (e.g. centroid-based clustering or linear classification), including optional Gaussian noise. They are useful for visualisation. produces Gaussian data with a spherical decision boundary for binary classification.

Multilabel

make_multilabel_classification generates random samples with multiple labels, reflecting a bag of words drawn from a mixture of topics. The number of topics for each document is drawn from a Poisson distribution, and the topics themselves are drawn from a fixed random distribution. Similarly, the number of words is drawn from Poisson, with words drawn from a multinomial, where each topic defines a probability distribution over words. Simplifications with respect to true bag-of-words mixtures include:

- Per-topic word distributions are independently drawn, where in reality all would be affected by a sparse base distribution, and would be correlated.
- For a document generated from multiple topics, all topics are weighted equally in generating its bag of words.
- Documents without labels words at random, rather than from a base distribution.
### Biclustering

**make_biclusters**(shape, n_clusters[, noise, ...])
Generate an array with constant block diagonal structure for biclustering.

**make_checkerboard**(shape, n_clusters[, ...])
Generate an array with block checkerboard structure for biclustering.

### Generators for regression

**make_regression** produces regression targets as an optionally-sparse random linear combination of random features, with noise. Its informative features may be uncorrelated, or low rank (few features account for most of the variance).

Other regression generators generate functions deterministically from randomized features. **make_sparse_uncorrelated** produces a target as a linear combination of four features with fixed coefficients. Others encode explicitly non-linear relations: **make_friedman1** is related by polynomial and sine transforms; **make_friedman2** includes feature multiplication and reciprocation; and **make_friedman3** is similar with an arctan transformation on the target.

### Generators for manifold learning

**make_s_curve**(n_samples, noise, random_state)
Generate an S curve dataset.

**make_swiss_roll**(n_samples, noise, random_state)
Generate a swiss roll dataset.

### Generators for decomposition

**make_low_rank_matrix**(n_samples, ...)
Generate a mostly low rank matrix with bell-shaped singular values.

**make_sparse_coded_signal**(n_samples, ...)
Generate a signal as a sparse combination of dictionary elements.

**make_spd_matrix**(n_dim, random_state)
Generate a random symmetric, positive-definite matrix.

**make_sparse_spd_matrix**(dim, alpha, ...)
Generate a sparse symmetric definite positive matrix.

---

3.5. Dataset loading utilities
3.5.5 Datasets in svmlight / libsvm format

scikit-learn includes utility functions for loading datasets in the svmlight / libsvm format. In this format, each line takes the form `<label> <feature-id>:<feature-value> <feature-id>:<feature-value>` ... This format is especially suitable for sparse datasets. In this module, scipy sparse CSR matrices are used for $X$ and numpy arrays are used for $y$.

You may load a dataset like as follows:

```python
>>> from sklearn.datasets import load_svmlight_file
>>> X_train, y_train = load_svmlight_file("/path/to/train_dataset.txt")
...
```

You may also load two (or more) datasets at once:

```python
>>> X_train, y_train, X_test, y_test = load_svmlight_files(    ...    "/path/to/train_dataset.txt", "/path/to/test_dataset.txt")
...
```

In this case, $X_{\text{train}}$ and $X_{\text{test}}$ are guaranteed to have the same number of features. Another way to achieve the same result is to fix the number of features:

```python
>>> X_test, y_test = load_svmlight_file(    ...    "/path/to/test_dataset.txt", n_features=X_train.shape[1])
...
```

Related links:

Public datasets in svmlight / libsvm format: https://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets

Faster API-compatible implementation: https://github.com/mblondel/svmlight-loader

3.5.6 Loading from external datasets

scikit-learn works on any numeric data stored as numpy arrays or scipy sparse matrices. Other types that are convertible to numeric arrays such as pandas DataFrame are also acceptable.

Here are some recommended ways to load standard columnar data into a format usable by scikit-learn:

- **pandas.io** provides tools to read data from common formats including CSV, Excel, JSON and SQL. DataFrames may also be constructed from lists of tuples or dicts. Pandas handles heterogeneous data smoothly and provides tools for manipulation and conversion into a numeric array suitable for scikit-learn.
- **scipy.io** specializes in binary formats often used in scientific computing context such as .mat and .arff
- **numpy/routines.io** for standard loading of columnar data into numpy arrays
- **scikit-learn's datasets.load_svmlight_file** for the svmlight or libSVM sparse format
- **scikit-learn's datasets.load_files** for directories of text files where the name of each directory is the name of each category and each file inside of each directory corresponds to one sample from that category

For some miscellaneous data such as images, videos, and audio, you may wish to refer to:

- **skimage.io or Imageio** for loading images and videos to numpy arrays
- **scipy.misc.imread** (requires the Pillow package) to load pixel intensities data from various image file formats
• scipy.io.wavfile.read for reading WAV files into a numpy array

Categorical (or nominal) features stored as strings (common in pandas DataFrames) will need converting to integers, and integer categorical variables may be best exploited when encoded as one-hot variables (sklearn.preprocessing.OneHotEncoder) or similar. See Preprocessing data.

Note: if you manage your own numerical data it is recommended to use an optimized file format such as HDF5 to reduce data load times. Various libraries such as H5Py, PyTables and pandas provides a Python interface for reading and writing data in that format.

The Olivetti faces dataset

This dataset contains a set of face images taken between April 1992 and April 1994 at AT&T Laboratories Cambridge. The sklearn.datasets.fetch_olivetti_faces function is the data fetching / caching function that downloads the data archive from AT&T.

As described on the original website:

There are ten different images of each of 40 distinct subjects. For some subjects, the images were taken at different times, varying the lighting, facial expressions (open / closed eyes, smiling / not smiling) and facial details (glasses / no glasses). All the images were taken against a dark homogeneous background with the subjects in an upright, frontal position (with tolerance for some side movement).

The image is quantized to 256 grey levels and stored as unsigned 8-bit integers; the loader will convert these to floating point values on the interval [0, 1], which are easier to work with for many algorithms.

The “target” for this database is an integer from 0 to 39 indicating the identity of the person pictured; however, with only 10 examples per class, this relatively small dataset is more interesting from an unsupervised or semi-supervised perspective.

The original dataset consisted of 92 x 112, while the version available here consists of 64x64 images.

When using these images, please give credit to AT&T Laboratories Cambridge.

The 20 newsgroups text dataset

The 20 newsgroups dataset comprises around 18000 newsgroups posts on 20 topics split in two subsets: one for training (or development) and the other one for testing (or for performance evaluation). The split between the train and test set is based upon messages posted before and after a specific date.

This module contains two loaders. The first one, sklearn.datasets.fetch_20newsgroups, returns a list of the raw texts that can be fed to text feature extractors such as sklearn.feature_extraction.text.CountVectorizer with custom parameters so as to extract feature vectors. The second one, sklearn.datasets.fetch_20newsgroups_vectorized, returns ready-to-use features, i.e., it is not necessary to use a feature extractor.

Usage

The sklearn.datasets.fetch_20newsgroups function is a data fetching / caching functions that downloads the data archive from the original 20 newsgroups website, extracts the archive contents in the ~/scikit_learn_data/20news_home folder and calls the sklearn.datasets.load_files on either the training or testing set folder, or both of them:

```python
>>> from sklearn.datasets import fetch_20newsgroups
>>> newsgroups_train = fetch_20newsgroups(subset='train')
```
The real data lies in the filenames and target attributes. The target attribute is the integer index of the category:

```python
>>> newsgroups_train.filenames.shape
(11314,)
>>> newsgroups_train.target.shape
(11314,)
>>> newsgroups_train.target[:10]
darray([12, 6, 9, 8, 6, 7, 9, 2, 13, 19])
```

It is possible to load only a sub-selection of the categories by passing the list of the categories to load to the `sklearn.datasets.fetch_20newsgroups` function:

```python
>>> cats = ['alt.atheism', 'sci.space']
>>> newsgroups_train = fetch_20newsgroups(subset='train', categories=cats)

>>> list(newsgroups_train.target_names)
['alt.atheism', 'sci.space']
>>> newsgroups_train.filenames.shape
(1073,)
>>> newsgroups_train.target.shape
(1073,)
>>> newsgroups_train.target[:10]
darray([1, 1, 1, 0, 1, 0, 0, 1, 1, 1])
```

### Converting text to vectors

In order to feed predictive or clustering models with the text data, one first need to turn the text into vectors of numerical values suitable for statistical analysis. This can be achieved with the utilities of the `sklearn.feature_extraction.text` as demonstrated in the following example that extract **TF-IDF** vectors of unigram tokens from a subset of 20news:

```python
>>> from sklearn.feature_extraction.text import TfidfVectorizer
>>> categories = ['alt.atheism', 'talk.religion.misc',
```
The extracted TF-IDF vectors are very sparse, with an average of 159 non-zero components by sample in a more than 30000-dimensional space (less than .5% non-zero features):

```
>>> vectors.nnz / float(vectors.shape[0])
159.01327433628319
```

`sklearn.datasets.fetch_20newsgroups_vectorized` is a function which returns ready-to-use tfidf features instead of file names.

### Filtering text for more realistic training

It is easy for a classifier to overfit on particular things that appear in the 20 Newsgroups data, such as newsgroup headers. Many classifiers achieve very high F-scores, but their results would not generalize to other documents that aren’t from this window of time.

For example, let’s look at the results of a multinomial Naive Bayes classifier, which is fast to train and achieves a decent F-score:

```
>>> from sklearn.naive_bayes import MultinomialNB
>>> from sklearn import metrics

>>> newsgroups_test = fetch_20newsgroups(subset='test', ...
                        categories=categories)
>>> test_vectors = vectorizer.transform(newsgroups_test.data)
>>> clf = MultinomialNB(alpha=.01)
>>> clf.fit(vectors, newsgroups_train.target)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.88213592402729568
```

(The example `Classification of text documents using sparse features` shuffles the training and test data, instead of segmenting by time, and in that case multinomial Naive Bayes gets a much higher F-score of 0.88. Are you suspicious yet of what’s going on inside this classifier?)

Let’s take a look at what the most informative features are:

```
>>> from sklearn.naive_bayes import MultinomialNB
>>> from sklearn import metrics

>>> newsgroups_test = fetch_20newsgroups(subset='test', ...
                        categories=categories)
>>> test_vectors = vectorizer.transform(newsgroups_test.data)
>>> clf = MultinomialNB(alpha=.01)
>>> clf.fit(vectors, newsgroups_train.target)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.88213592402729568
```

The extracted TF-IDF vectors are very sparse, with an average of 159 non-zero components by sample in a more than 30000-dimensional space (less than .5% non-zero features):

```
>>> vectors.nnz / float(vectors.shape[0])
159.01327433628319
```

`sklearn.datasets.fetch_20newsgroups_vectorized` is a function which returns ready-to-use tfidf features instead of file names.

### Filtering text for more realistic training

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>>> from sklearn import metrics

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                        categories=categories)
>>> test_vectors = vectorizer.transform(newsgroups_test.data)
>>> clf = MultinomialNB(alpha=.01)
>>> clf.fit(vectors, newsgroups_train.target)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.88213592402729568
```

(The example `Classification of text documents using sparse features` shuffles the training and test data, instead of segmenting by time, and in that case multinomial Naive Bayes gets a much higher F-score of 0.88. Are you suspicious yet of what’s going on inside this classifier?)

Let’s take a look at what the most informative features are:

```
>>> import numpy as np
>>> def show_top10(classifier, vectorizer, categories):
...     feature_names = np.asarray(vectorizer.get_feature_names())
...     for i, category in enumerate(categories):
...         top10 = np.argsort(classifier.coef_[i])[-10:]
...         print("%s: %s % (%s)"
...            % (category, ", ".join(feature_names[top10])),)
...
>>> show_top10(clf, vectorizer, newsgroups_train.target_names)
alt.atheism: sgi livesey atheists writes people caltech com god keith edu
comp.graphics: organization thanks files subject com image lines university edu_
                . graphics
sci.space: toronto moon gov com alaska access henry nasa edu space
talk.religion.misc: article writes kent people christian jesus sandvik edu com god
```
You can now see many things that these features have overfit to:

- Almost every group is distinguished by whether headers such as `NNTP-Posting-Host:` and `Distribution:` appear more or less often.
- Another significant feature involves whether the sender is affiliated with a university, as indicated either by their headers or their signature.
- The word “article” is a significant feature, based on how often people quote previous posts like this: “In article [article ID], [name] <[e-mail address]> wrote:”
- Other features match the names and e-mail addresses of particular people who were posting at the time.

With such an abundance of clues that distinguish newsgroups, the classifiers barely have to identify topics from text at all, and they all perform at the same high level.

For this reason, the functions that load 20 Newsgroups data provide a parameter called `remove`, telling it what kinds of information to strip out of each file. `remove` should be a tuple containing any subset of ('headers', 'footers', 'quotes'), telling it to remove headers, signature blocks, and quotation blocks respectively.

```python
>>> newsgroups_test = fetch_20newsgroups(subset='test',
...    remove=('headers', 'footers', 'quotes'),
...    categories=categories)
>>> vectors_test = vectorizer.transform(newsgroups_test.data)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(pred, newsgroups_test.target, average='macro')
0.77310350681274775
```

This classifier lost over a lot of its F-score, just because we removed metadata that has little to do with topic classification. It loses even more if we also strip this metadata from the training data:

```python
>>> newsgroups_train = fetch_20newsgroups(subset='train',
...    remove=('headers', 'footers', 'quotes'),
...    categories=categories)
>>> vectors = vectorizer.fit_transform(newsgroups_train.data)
>>> clf = MultinomialNB(alpha=.01)
>>> clf.fit(vectors, newsgroups_train.target)
>>> vectors_test = vectorizer.transform(newsgroups_test.data)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.76995175184521725
```

Some other classifiers cope better with this harder version of the task. Try running `Sample pipeline for text feature extraction and evaluation` with and without the `--filter` option to compare the results.

**Recommendation**

When evaluating text classifiers on the 20 Newsgroups data, you should strip newsgroup-related metadata. In scikit-learn, you can do this by setting `remove=('headers', 'footers', 'quotes')`. The F-score will be lower because it is more realistic.

**Examples**

- `Sample pipeline for text feature extraction and evaluation`
- `Classification of text documents using sparse features`
Downloading datasets from the mldata.org repository

mldata.org is a public repository for machine learning data, supported by the PASCAL network.

The sklearn.datasets package is able to directly download data sets from the repository using the function sklearn.datasets.fetch_mldata.

For example, to download the MNIST digit recognition database:

```python
>>> from sklearn.datasets import fetch_mldata
>>> mnist = fetch_mldata('MNIST original', data_home=custom_data_home)
```

The MNIST database contains a total of 70000 examples of handwritten digits of size 28x28 pixels, labeled from 0 to 9:

```python
>>> mnist.data.shape
(70000, 784)
>>> mnist.target.shape
(70000,)
>>> np.unique(mnist.target)
array([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
```

After the first download, the dataset is cached locally in the path specified by the data_home keyword argument, which defaults to ~/scikit_learn_data/:

```python
>>> os.listdir(os.path.join(custom_data_home, 'mldata'))
['mnist-original.mat']
```

Data sets in mldata.org do not adhere to a strict naming or formatting convention. sklearn.datasets.fetch_mldata is able to make sense of the most common cases, but allows to tailor the defaults to individual datasets:

- The data arrays in mldata.org are most often shaped as (n_features, n_samples). This is the opposite of the scikit-learn convention, so sklearn.datasets.fetch_mldata transposes the matrix by default. The transpose_data keyword controls this behavior:

```python
>>> iris = fetch_mldata('iris', data_home=custom_data_home)
>>> iris.data.shape
(150, 4)
>>> iris = fetch_mldata('iris', transpose_data=False,
...                       data_home=custom_data_home)
>>> iris.data.shape
(4, 150)
```

- For datasets with multiple columns, sklearn.datasets.fetch_mldata tries to identify the target and data columns and rename them to target and data. This is done by looking for arrays named label and data in the dataset, and failing that by choosing the first array to be target and the second to be data. This behavior can be changed with the target_name and data_name keywords, setting them to a specific name or index number (the name and order of the columns in the datasets can be found at its mldata.org under the tab “Data”):

```python
>>> iris2 = fetch_mldata('datasets-UCI iris', target_name=1, data_name=0,
...                       data_home=custom_data_home)
>>> iris3 = fetch_mldata('datasets-UCI iris', target_name='class',
...                       data_name='double0', data_home=custom_data_home)
```
The Labeled Faces in the Wild face recognition dataset

This dataset is a collection of JPEG pictures of famous people collected over the internet, all details are available on the official website:

http://vis-www.cs.umass.edu/lfw/

Each picture is centered on a single face. The typical task is called Face Verification: given a pair of two pictures, a binary classifier must predict whether the two images are from the same person.

An alternative task, Face Recognition or Face Identification is: given the picture of the face of an unknown person, identify the name of the person by referring to a gallery of previously seen pictures of identified persons.

Both Face Verification and Face Recognition are tasks that are typically performed on the output of a model trained to perform Face Detection. The most popular model for Face Detection is called Viola-Jones and is implemented in the OpenCV library. The LFW faces were extracted by this face detector from various online websites.

Usage

scikit-learn provides two loaders that will automatically download, cache, parse the metadata files, decode the jpeg and convert the interesting slices into memmapped numpy arrays. This dataset size is more than 200 MB. The first load typically takes more than a couple of minutes to fully decode the relevant part of the JPEG files into numpy arrays. If the dataset has been loaded once, the following times the loading times less than 200ms by using a memmapped version memoized on the disk in the ~/scikit_learn_data/lfw_home/ folder using joblib.

The first loader is used for the Face Identification task: a multi-class classification task (hence supervised learning):

```python
>>> from sklearn.datasets import fetch_lfw_people
>>> lfw_people = fetch_lfw_people(min_faces_per_person=70, resize=0.4)
```

```python
>>> for name in lfw_people.target_names:
...    print(name)
... Ariel Sharon
Colin Powell
Donald Rumsfeld
George W Bush
Gerhard Schroeder
Hugo Chavez
Tony Blair
```

The default slice is a rectangular shape around the face, removing most of the background:

```python
>>> lfw_people.data.dtype
dtype('float32')
```

```python
>>> lfw_people.data.shape
(1288, 1850)
```

```python
>>> lfw_people.images.shape
(1288, 50, 37)
```

Each of the 1140 faces is assigned to a single person id in the target array:

```python
>>> lfw_people.target.shape
(1288,)
```
The second loader is typically used for the face verification task: each sample is a pair of two pictures belonging or not to the same person:

```python
>>> list(lfw_people.target[:10])
[5, 6, 3, 1, 0, 1, 3, 4, 3, 0]
```

Both for the `sklearn.datasets.fetch_lfw_people` and `sklearn.datasets.fetch_lfw_pairs` function it is possible to get an additional dimension with the RGB color channels by passing `color=True`, in that case the shape will be `(2200, 2, 62, 47, 3)`.

The `sklearn.datasets.fetch_lfw_pairs` datasets is subdivided into 3 subsets: the development `train` set, the development `test` set and an evaluation `10_folds` set meant to compute performance metrics using a 10-folds cross validation scheme.

References:


Examples

Faces recognition example using eigenfaces and SVMs

Forest covertypes

The samples in this dataset correspond to 30x30m patches of forest in the US, collected for the task of predicting each patch’s cover type, i.e. the dominant species of tree. There are seven covertypes, making this a multiclass classification problem. Each sample has 54 features, described on the dataset’s homepage. Some of the features are boolean indicators, while others are discrete or continuous measurements.

`sklearn.datasets.fetch_covtype` will load the covertype dataset; it returns a dictionary-like object with the feature matrix in the `data` member and the target values in `target`. The dataset will be downloaded from the web if necessary.
RCV1 dataset

Reuters Corpus Volume I (RCV1) is an archive of over 800,000 manually categorized newswire stories made available by Reuters, Ltd. for research purposes. The dataset is extensively described in\(^1\).

```
from sklearn.datasets import fetch_rcv1
rcv1 = fetch_rcv1()
```

It returns a dictionary-like object, with the following attributes:

- **data**: The feature matrix is a scipy CSR sparse matrix, with 804414 samples and 47236 features. Non-zero values contain cosine-normalized, log TF-IDF vectors. A nearly chronological split is proposed in\(^1\): The first 23149 samples are the training set. The last 781265 samples are the testing set. This follows the official LYRL2004 chronological split. The array has 0.16% of non zero values:

```
rcv1.data.shape
(804414, 47236)
```

- **target**: The target values are stored in a scipy CSR sparse matrix, with 804414 samples and 103 categories. Each sample has a value of 1 in its categories, and 0 in others. The array has 3.15% of non zero values:

```
rcv1.target.shape
(804414, 103)
```

- **sample_id**: Each sample can be identified by its ID, ranging (with gaps) from 2286 to 810596:

```
r cv1.sample_id[:3]
array([2286, 2287, 2288], dtype=uint32)
```

- **target_names**: The target values are the topics of each sample. Each sample belongs to at least one topic, and to up to 17 topics. There are 103 topics, each represented by a string. Their corpus frequencies span five orders of magnitude, from 5 occurrences for ‘GMIL’, to 381327 for ‘CCAT’:

```
r cv1.target_names[:3].tolist()
['E11', 'ECAT', 'M11']
```

The dataset will be downloaded from the rcv1 homepage if necessary. The compressed size is about 656 MB.

References

Kddcup 99 dataset

The KDD Cup ‘99 dataset was created by processing the tcpdump portions of the 1998 DARPA Intrusion Detection System (IDS) Evaluation dataset, created by MIT Lincoln Lab. The artificial data (described on the dataset’s homepage) was generated using a closed network and hand-injected attacks to produce a large number of different types of attack with normal activity in the background. As the initial goal was to produce a large training set for supervised learning algorithms, there is a large proportion (80.1%) of abnormal data which is unrealistic in real world, and inappropriate for unsupervised anomaly detection which aims at detecting ‘abnormal’ data, ie 1) qualitatively different

from normal data 2) in large minority among the observations. We thus transform the KDD Data set into two different data sets: SA and SF.

- SA is obtained by simply selecting all the normal data, and a small proportion of abnormal data to gives an anomaly proportion of 1%.

- SF is obtained as in [2] by simply picking up the data whose attribute logged_in is positive, thus focusing on the intrusion attack, which gives a proportion of 0.3% of attack.

- http and smtp are two subsets of SF corresponding with third feature equal to ‘http’ (resp. to ‘smtp’)

sklearn.datasets.fetch_kddcup99 will load the kddcup99 dataset; it returns a dictionary-like object with the feature matrix in the data member and the target values in target. The dataset will be downloaded from the web if necessary.

### 3.5.7 The Olivetti faces dataset

This dataset contains a set of face images taken between April 1992 and April 1994 at AT&T Laboratories Cambridge. The sklearn.datasets.fetch_olivetti_faces function is the data fetching / caching function that downloads the data archive from AT&T.

As described on the original website:

There are ten different images of each of 40 distinct subjects. For some subjects, the images were taken at different times, varying the lighting, facial expressions (open / closed eyes, smiling / not smiling) and facial details (glasses / no glasses). All the images were taken against a dark homogeneous background with the subjects in an upright, frontal position (with tolerance for some side movement).

The image is quantized to 256 grey levels and stored as unsigned 8-bit integers; the loader will convert these to floating point values on the interval [0, 1], which are easier to work with for many algorithms.

The “target” for this database is an integer from 0 to 39 indicating the identity of the person pictured; however, with only 10 examples per class, this relatively small dataset is more interesting from an unsupervised or semi-supervised perspective.

The original dataset consisted of 92 x 112, while the version available here consists of 64x64 images.

When using these images, please give credit to AT&T Laboratories Cambridge.

### 3.5.8 The 20 newsgroups text dataset

The 20 newsgroups dataset comprises around 18000 newsgroups posts on 20 topics split in two subsets: one for training (or development) and the other one for testing (or for performance evaluation). The split between the train and test set is based upon a messages posted before and after a specific date.

This module contains two loaders. The first one, sklearn.datasets.fetch_20newsgroups, returns a list of the raw texts that can be fed to text feature extractors such as sklearn.feature_extraction.text.CountVectorizer with custom parameters so as to extract feature vectors. The second one, sklearn.datasets.fetch_20newsgroups_vectorized, returns ready-to-use features, i.e., it is not necessary to use a feature extractor.

**Usage**

The sklearn.datasets.fetch_20newsgroups function is a data fetching / caching functions that downloads the data archive from the original 20 newsgroups website, extracts the archive contents in the ~/scikit_learn_data/20news_home folder and calls the sklearn.datasets.load_files on either the training or testing set folder, or both of them:
```python
>>> from sklearn.datasets import fetch_20newsgroups
>>> newsgroups_train = fetch_20newsgroups(subset='train')

>>> from pprint import pprint
>>> pprint(list(newsgroups_train.target_names))
['alt.atheism',
 'comp.graphics',
 'comp.os.ms-windows.misc',
 'comp.sys.ibm.pc.hardware',
 'comp.sys.mac.hardware',
 'comp.windows.x',
 'misc.forsale',
 'rec.autos',
 'rec.motorcycles',
 'rec.sport.baseball',
 'rec.sport.hockey',
 'sci.crypt',
 'sci.electronics',
 'sci.med',
 'sci.space',
 'soc.religion.christian',
 'talk.politics.guns',
 'talk.politics.mideast',
 'talk.politics.misc',
 'talk.religion.misc']
```

The real data lies in the filenames and target attributes. The target attribute is the integer index of the category:

```python
>>> newsgroups_train.filenames.shape
(11314,)
>>> newsgroups_train.target.shape
(11314,)
>>> newsgroups_train.target[:10]
array([12, 6, 9, 8, 6, 7, 9, 2, 13, 19])
```

It is possible to load only a sub-selection of the categories by passing the list of the categories to load to the sklearn.datasets.fetch_20newsgroups function:

```python
>>> cats = ['alt.atheism', 'sci.space']
>>> newsgroups_train = fetch_20newsgroups(subset='train', categories=cats)

>>> list(newsgroups_train.target_names)
['alt.atheism', 'sci.space']
>>> newsgroups_train.filenames.shape
(1073,)
>>> newsgroups_train.target.shape
(1073,)
>>> newsgroups_train.target[:10]
array([1, 1, 1, 0, 1, 0, 0, 1, 1, 1])
```

### Converting text to vectors

In order to feed predictive or clustering models with the text data, one first need to turn the text into vectors of numerical values suitable for statistical analysis. This can be achieved with the utilities of the sklearn.feature_extraction.text as demonstrated in the following example that extract TF-IDF vectors of unigram tokens from a subset of 20news:
>>> from sklearn.feature_extraction.text import TfidfVectorizer

>>> categories = ['alt.atheism', 'talk.religion.misc',
...                'comp.graphics', 'sci.space']

>>> newsgroups_train = fetch_20newsgroups(subset='train',
...                                       categories=categories)

>>> vectorizer = TfidfVectorizer()

>>> vectors = vectorizer.fit_transform(newsgroups_train.data)

>>> vectors.shape
(2034, 34118)

The extracted TF-IDF vectors are very sparse, with an average of 159 non-zero components by sample in a more than
30000-dimensional space (less than .5% non-zero features):

```python
>>> vectors.nnz / float(vectors.shape[0])
159.01327433628319
```

`sklearn.datasets.fetch_20newsgroups_vectorized` is a function which returns ready-to-use tfidf
features instead of file names.

### Filtering text for more realistic training

It is easy for a classifier to overfit on particular things that appear in the 20 Newsgroups data, such as newsgroup
headers. Many classifiers achieve very high F-scores, but their results would not generalize to other documents that
aren’t from this window of time.

For example, let’s look at the results of a multinomial Naive Bayes classifier, which is fast to train and achieves a
decent F-score:

```python
>>> from sklearn.naive_bayes import MultinomialNB
>>> from sklearn import metrics

>>> newsgroups_test = fetch_20newsgroups(subset='test',
...                                       categories=categories)

>>> vectors_test = vectorizer.transform(newsgroups_test.data)

>>> clf = MultinomialNB(alpha=.01)

>>> clf.fit(vectors, newsgroups_train.target)

>>> pred = clf.predict(vectors_test)

>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.88213592402729568
```

(The example `Classification of text documents using sparse features` shuffles the training and test data, instead of
segmenting by time, and in that case multinomial Naive Bayes gets a much higher F-score of 0.88. Are you suspicious
yet of what’s going on inside this classifier?)

Let’s take a look at what the most informative features are:

```python
>>> import numpy as np

>>> def show_top10(classifier, vectorizer, categories):
...     feature_names = np.asarray(vectorizer.get_feature_names())
...     for i, category in enumerate(categories):
...         top10 = np.argsort(classifier.coef_[i])[-10:]
...         print("$s: $s" % (category, ", ".join(feature_names[top10])))

>>> show_top10(clf, vectorizer, newsgroups_train.target_names)
alt.atheism: sgi livesey atheists writes people caltech com god keith edu
comp.graphics: organization thanks files subject com image lines university edu
```
You can now see many things that these features have overfit to:

- Almost every group is distinguished by whether headers such as NNTP-Posting-Host: and Distribution: appear more or less often.
- Another significant feature involves whether the sender is affiliated with a university, as indicated either by their headers or their signature.
- The word “article” is a significant feature, based on how often people quote previous posts like this: “In article [article ID], [name] <[e-mail address]> wrote:”
- Other features match the names and e-mail addresses of particular people who were posting at the time.

With such an abundance of clues that distinguish newsgroups, the classifiers barely have to identify topics from text at all, and they all perform at the same high level.

For this reason, the functions that load 20 Newsgroups data provide a parameter called remove, telling it what kinds of information to strip out of each file. remove should be a tuple containing any subset of ('headers', 'footers', 'quotes'), telling it to remove headers, signature blocks, and quotation blocks respectively.

```python
>>> newsgroups_test = fetch_20newsgroups(subset='test',
... remove=('headers', 'footers', 'quotes'),
... categories=categories)
>>> vectors_test = vectorizer.transform(newsgroups_test.data)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(pred, newsgroups_test.target, average='macro')
0.77310350681274775
```

This classifier lost over a lot of its F-score, just because we removed metadata that has little to do with topic classification. It loses even more if we also strip this metadata from the training data:

```python
>>> newsgroups_train = fetch_20newsgroups(subset='train',
... remove=('headers', 'footers', 'quotes'),
... categories=categories)
>>> vectors = vectorizer.fit_transform(newsgroups_train.data)
>>> clf = MultinomialNB(alpha=.01)
>>> clf.fit(vectors, newsgroups_train.target)
>>> vectors_test = vectorizer.transform(newsgroups_test.data)
>>> pred = clf.predict(vectors_test)
>>> metrics.f1_score(newsgroups_test.target, pred, average='macro')
0.76995175184521725
```

Some other classifiers cope better with this harder version of the task. Try running Sample pipeline for text feature extraction and evaluation with and without the --filter option to compare the results.

**Recommendation**

When evaluating text classifiers on the 20 Newsgroups data, you should strip newsgroup-related metadata. In scikit-learn, you can do this by setting remove=('headers', 'footers', 'quotes'). The F-score will be lower because it is more realistic.
Examples

- Sample pipeline for text feature extraction and evaluation
- Classification of text documents using sparse features

3.5.9 Downloading datasets from the mldata.org repository

mldata.org is a public repository for machine learning data, supported by the PASCAL network.

The sklearn.datasets package is able to directly download data sets from the repository using the function sklearn.datasets.fetch_mldata.

For example, to download the MNIST digit recognition database:

```python
>>> from sklearn.datasets import fetch_mldata
>>> mnist = fetch_mldata('MNIST original', data_home=custom_data_home)
```

The MNIST database contains a total of 70000 examples of handwritten digits of size 28x28 pixels, labeled from 0 to 9:

```python
>>> mnist.data.shape
(70000, 784)
>>> mnist.target.shape
(70000,)
>>> np.unique(mnist.target)
array([ 0., 1., 2., 3., 4., 5., 6., 7., 8., 9.])
```

After the first download, the dataset is cached locally in the path specified by the data_home keyword argument, which defaults to ~/scikit_learn_data/:

```python
>>> os.listdir(os.path.join(custom_data_home, 'mldata'))
['mnist-original.mat']
```

Data sets in mldata.org do not adhere to a strict naming or formatting convention. sklearn.datasets.fetch_mldata is able to make sense of the most common cases, but allows to tailor the defaults to individual datasets:

- The data arrays in mldata.org are most often shaped as (n_features, n_samples). This is the opposite of the scikit-learn convention, so sklearn.datasets.fetch_mldata transposes the matrix by default. The transpose_data keyword controls this behavior:

```python
>>> iris = fetch_mldata('iris', data_home=custom_data_home)
>>> iris.data.shape
(150, 4)
>>> iris = fetch_mldata('iris', transpose_data=False, ...
... data_home=custom_data_home)
>>> iris.data.shape
(4, 150)
```

- For datasets with multiple columns, sklearn.datasets.fetch_mldata tries to identify the target and data columns and rename them to target and data. This is done by looking for arrays named label and data in the dataset, and failing that by choosing the first array to be target and the second to be data. This behavior can be changed with the target_name and data_name keywords, setting them to a specific name or index number (the name and order of the columns in the datasets can be found at its mldata.org under the tab “Data”):

3.5. Dataset loading utilities  561
3.5.10 The Labeled Faces in the Wild face recognition dataset

This dataset is a collection of JPEG pictures of famous people collected over the internet, all details are available on the official website:

http://vis-www.cs.umass.edu/lfw/

Each picture is centered on a single face. The typical task is called Face Verification: given a pair of two pictures, a binary classifier must predict whether the two images are from the same person.

An alternative task, Face Recognition or Face Identification is: given the picture of the face of an unknown person, identify the name of the person by referring to a gallery of previously seen pictures of identified persons.

Both Face Verification and Face Recognition are tasks that are typically performed on the output of a model trained to perform Face Detection. The most popular model for Face Detection is called Viola-Jones and is implemented in the OpenCV library. The LFW faces were extracted by this face detector from various online websites.

Usage

scikit-learn provides two loaders that will automatically download, cache, parse the metadata files, decode the jpeg and convert the interesting slices into memmapped numpy arrays. This dataset size is more than 200 MB. The first load typically takes more than a couple of minutes to fully decode the relevant part of the JPEG files into numpy arrays. If the dataset has been loaded once, the following times the loading times less than 200ms by using a memmapped version memoized on the disk in the ~ / scikit_learn_data / lfw_home / folder using joblib.

The first loader is used for the Face Identification task: a multi-class classification task (hence supervised learning):

```python
>>> from sklearn.datasets import fetch_lfw_people
>>> lfw_people = fetch_lfw_people(min_faces_per_person=70, resize=0.4)

>>> for name in lfw_people.target_names:
...     print(name)
...     Ariel Sharon
...     Colin Powell
...     Donald Rumsfeld
...     George W Bush
...     Gerhard Schroeder
...     Hugo Chavez
...     Tony Blair
```

The default slice is a rectangular shape around the face, removing most of the background:

```python
>>> lfw_people.data.dtype
dtype('float32')

>>> lfw_people.data.shape
(1288, 1850)

>>> lfw_people.images.shape
(1288, 50, 37)
```
Each of the 1,140 faces is assigned to a single person id in the target array:

```python
gtfw_people.target.shape
(1288,)
gtfw_people.target[0:10]
[5, 6, 3, 1, 0, 1, 3, 4, 3, 0]
```

The second loader is typically used for the face verification task: each sample is a pair of two pictures belonging or not to the same person:

```python
gtfw_pairs_train = fetch_lfw_pairs(subset='train')
gtfw_pairs_train.target_names
['Different persons', 'Same person']
gtfw_pairs_train.shape
(2200, 2, 62, 47)
gtfw_pairs_train.data.shape
(2200, 5828)
gtfw_pairs_train.target.shape
(2200,)
```

Both for the `sklearn.datasets.fetch_lfw_people` and `sklearn.datasets.fetch_lfw_pairs` function it is possible to get an additional dimension with the RGB color channels by passing `color=True`, in that case the shape will be `(2200, 2, 62, 47, 3)`.

The `sklearn.datasets.fetch_lfw_pairs` dataset is subdivided into 3 subsets: the development train set, the development test set and an evaluation 10_folds set meant to compute performance metrics using a 10-folds cross validation scheme.

---

**References:**


---

**Examples**

*Faces recognition example using eigenfaces and SVMs*

### 3.5.11 Forest covertypes

The samples in this dataset correspond to 30x30m patches of forest in the US, collected for the task of predicting each patch’s cover type, i.e. the dominant species of tree. There are seven covertypes, making this a multiclass classification problem. Each sample has 54 features, described on the dataset’s homepage. Some of the features are boolean indicators, while others are discrete or continuous measurements.

`sklearn.datasets.fetch_covertype` will load the covertype dataset; it returns a dictionary-like object with the feature matrix in the `data` member and the target values in `target`. The dataset will be downloaded from the web if necessary.
3.5.12 RCV1 dataset

Reuters Corpus Volume I (RCV1) is an archive of over 800,000 manually categorized newswire stories made available by Reuters, Ltd. for research purposes. The dataset is extensively described in\(^1\).

`sklearn.datasets.fetch_rcv1` will load the following version: RCV1-v2, vectors, full sets, topics multilabels:

```python
>>> from sklearn.datasets import fetch_rcv1
>>> rcv1 = fetch_rcv1()
```

It returns a dictionary-like object, with the following attributes:

data: The feature matrix is a scipy CSR sparse matrix, with 804414 samples and 47236 features. Non-zero values contains cosine-normalized, log TF-IDF vectors. A nearly chronological split is proposed in\(^1\): The first 23149 samples are the training set. The last 781265 samples are the testing set. This follows the official LYRL2004 chronological split. The array has 0.16% of non zero values:

```python
>>> rcv1.data.shape
(804414, 47236)
```

target: The target values are stored in a scipy CSR sparse matrix, with 804414 samples and 103 categories. Each sample has a value of 1 in its categories, and 0 in others. The array has 3.15% of non zero values:

```python
>>> rcv1.target.shape
(804414, 103)
```
sample_id: Each sample can be identified by its ID, ranging (with gaps) from 2286 to 810596:

```python
>>> rcv1.sample_id[:3]
array([2286, 2287, 2288], dtype=uint32)
```
target_names: The target values are the topics of each sample. Each sample belongs to at least one topic, and to up to 17 topics. There are 103 topics, each represented by a string. Their corpus frequencies span five orders of magnitude, from 5 occurrences for ‘GMIL’, to 381327 for ‘CCAT’:

```python
>>> rcv1.target_names[:3].tolist()
['E11', 'ECAT', 'M11']
```

The dataset will be downloaded from the rcv1 homepage if necessary. The compressed size is about 656 MB.

References

3.5.13 Kddcup 99 dataset

The KDD Cup ‘99 dataset was created by processing the tcpdump portions of the 1998 DARPA Intrusion Detection System (IDS) Evaluation dataset, created by MIT Lincoln Lab. The artificial data (described on the dataset’s homepage) was generated using a closed network and hand-injected attacks to produce a large number of different types of attack with normal activity in the background. As the initial goal was to produce a large training set for supervised learning algorithms, there is a large proportion (80.1%) of abnormal data which is unrealistic in real world, and inappropriate for unsupervised anomaly detection which aims at detecting ‘abnormal” data, ie 1) qualitatively different

from normal data, in large minority among the observations. We thus transform the KDD Data set into two different
data sets: SA and SF.
- SA is obtained by simply selecting all the normal data, and a small proportion of abnormal data to gives an anomaly
proportion of 1%.
- SF is obtained as in [2] by simply picking up the data whose attribute logged_in is positive, thus focusing on the
intrusion attack, which gives a proportion of 0.3% of attack.
- http and smtp are two subsets of SF corresponding with third feature equal to ‘http’ (resp. to ‘smtp’)

`sklearn.datasets.fetch_kddcup99` will load the kddcup99 dataset; it returns a dictionary-like object with
the feature matrix in the `data` member and the target values in `target`. The dataset will be downloaded from the
web if necessary.

### 3.5.14 Boston House Prices dataset

**Notes**

Data Set Characteristics:

- **Number of Instances**: 506
- **Number of Attributes**: 13 numeric/categorical predictive

:Median Value (attribute 14) is usually the target

**Attribute Information (in order)**

- CRIM per capita crime rate by town
- ZN proportion of residential land zoned for lots over 25,000 sq.ft.
- INDUS proportion of non-retail business acres per town
- CHAS Charles River dummy variable (= 1 if tract bounds river; 0 otherwise)
- NOX nitric oxides concentration (parts per 10 million)
- RM average number of rooms per dwelling
- AGE proportion of owner-occupied units built prior to 1940
- DIS weighted distances to five Boston employment centres
- RAD index of accessibility to radial highways
- TAX full-value property-tax rate per $10,000
- PTRATIO pupil-teacher ratio by town
- B 1000(Bk - 0.63)^2 where Bk is the proportion of blacks by town
- LSTAT % lower status of the population
- MEDV Median value of owner-occupied homes in $1000’s

**Missing Attribute Values**: None

**Creator**: Harrison, D. and Rubinfeld, D.L.

This is a copy of UCI ML housing dataset, [http://archive.ics.uci.edu/ml/datasets/Housing](http://archive.ics.uci.edu/ml/datasets/Housing)

This dataset was taken from the StatLib library which is maintained at Carnegie Mellon University.

The Boston house-price data has been used in many machine learning papers that address regression problems.

References

- many more! (see http://archive.ics.uci.edu/ml/datasets/Housing)

3.5.15 Breast Cancer Wisconsin (Diagnostic) Database

Notes

Data Set Characteristics:

Number of Instances  569
Number of Attributes  30 numeric, predictive attributes and the class

Attribute Information

- radius (mean of distances from center to points on the perimeter)
- texture (standard deviation of gray-scale values)
- perimeter
- area
- smoothness (local variation in radius lengths)
- compactness (perimeter^2 / area - 1.0)
- concavity (severity of concave portions of the contour)
- concave points (number of concave portions of the contour)
- symmetry
- fractal dimension (“coastline approximation” - 1)

The mean, standard error, and “worst” or largest (mean of the three largest values) of these features were computed for each image, resulting in 30 features. For instance, field 3 is Mean Radius, field 13 is Radius SE, field 23 is Worst Radius.

- class:
  - WDBC-Malignant
  - WDBC-Benign

Summary Statistics

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>radius</td>
<td>6.981</td>
<td>28.11</td>
</tr>
<tr>
<td>texture</td>
<td>9.71</td>
<td>39.28</td>
</tr>
</tbody>
</table>

Continued on next page
Table 3.39 – continued from previous page

<table>
<thead>
<tr>
<th>Feature</th>
<th>Mean (Standard Error)</th>
<th>Worst</th>
</tr>
</thead>
<tbody>
<tr>
<td>perimeter (mean)</td>
<td>43.79 (0.757)</td>
<td>50.41 (0.112)</td>
</tr>
<tr>
<td>area (mean)</td>
<td>143.5 (6.802)</td>
<td>185.2 (18.5)</td>
</tr>
<tr>
<td>smoothness (mean)</td>
<td>0.053 (0.002)</td>
<td>0.071 (0.0156)</td>
</tr>
<tr>
<td>compactness (mean)</td>
<td>0.019 (0.002)</td>
<td>0.027 (0.0027)</td>
</tr>
<tr>
<td>concavity (mean)</td>
<td>0.0 (0.0)</td>
<td>0.0 (0.0)</td>
</tr>
<tr>
<td>concave points (mean)</td>
<td>0.0 (0.0)</td>
<td>0.0 (0.0)</td>
</tr>
<tr>
<td>symmetry (mean)</td>
<td>0.106 (0.008)</td>
<td>0.156 (0.0156)</td>
</tr>
<tr>
<td>fractal dimension (mean)</td>
<td>0.05 (0.001)</td>
<td>0.055 (0.0156)</td>
</tr>
<tr>
<td>radius (standard error)</td>
<td>2.873 (3.604)</td>
<td>7.93 (36.04)</td>
</tr>
<tr>
<td>texture (standard error)</td>
<td>4.885 (12.02)</td>
<td>12.02 (49.54)</td>
</tr>
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<td>perimeter (standard error)</td>
<td>21.98 (50.41)</td>
<td>50.41 (251.2)</td>
</tr>
<tr>
<td>area (standard error)</td>
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<td>185.2 (4254.0)</td>
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<td>smoothness (standard error)</td>
<td>0.031 (0.071)</td>
<td>0.223 (0.027)</td>
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<td>compactness (standard error)</td>
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<td>1.058 (1.058)</td>
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<td>concavity (standard error)</td>
<td>0.396 (0.0)</td>
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<td>concave points (standard error)</td>
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<td>0.291 (0.0)</td>
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<tr>
<td>symmetry (standard error)</td>
<td>0.079 (0.008)</td>
<td>0.664 (0.156)</td>
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<tr>
<td>fractal dimension (standard error)</td>
<td>0.03 (0.001)</td>
<td>0.208 (0.055)</td>
</tr>
</tbody>
</table>

Missing Attribute Values  None

Class Distribution  212 - Malignant, 357 - Benign

Creator  Dr. William H. Wolberg, W. Nick Street, Olvi L. Mangasarian

Donor  Nick Street

Date  November, 1995

This is a copy of UCI ML Breast Cancer Wisconsin (Diagnostic) datasets. https://goo.gl/U2Uwz2

Features are computed from a digitized image of a fine needle aspirate (FNA) of a breast mass. They describe characteristics of the cell nuclei present in the image.

Separating plane described above was obtained using Multisurface Method-Tree (MSM-T) [K. P. Bennett, “Decision Tree Construction Via Linear Programming.” Proceedings of the 4th Midwest Artificial Intelligence and Cognitive Science Society, pp. 97-101, 1992], a classification method which uses linear programming to construct a decision tree. Relevant features were selected using an exhaustive search in the space of 1-4 features and 1-3 separating planes.

The actual linear program used to obtain the separating plane in the 3-dimensional space is that described in: [K. P. Bennett and O. L. Mangasarian: “Robust Linear Programming Discrimination of Two Linearly Inseparable Sets”, Optimization Methods and Software 1, 1992, 23-34].

This database is also available through the UW CS ftp server:


3.5. Dataset loading utilities
References


3.5.16 Diabetes dataset

Notes

Ten baseline variables, age, sex, body mass index, average blood pressure, and six blood serum measurements were obtained for each of \( n = 442 \) diabetes patients, as well as the response of interest, a quantitative measure of disease progression one year after baseline.

Data Set Characteristics:

- Number of Instances 442
- Number of Attributes First 10 columns are numeric predictive values
- Target Column 11 is a quantitative measure of disease progression one year after baseline

Attributes

- Age
- Sex
- Body mass index
- Average blood pressure
- S1
- S2
- S3
- S4
- S5
- S6

Note: Each of these 10 feature variables have been mean centered and scaled by the standard deviation times \( n_{\text{samples}} \) (i.e. the sum of squares of each column totals 1).

Source URL: http://www4.stat.ncsu.edu/~boos/var.select/diabetes.html

3.5.17 Optical Recognition of Handwritten Digits Data Set

Notes

Data Set Characteristics:

- **Number of Instances**: 5620
- **Number of Attributes**: 64

**Attribute Information**: 8x8 image of integer pixels in the range 0..16.

**Missing Attribute Values**: None

**Creator**: 5. Alpaydin (alpaydin ‘@’ boun.edu.tr)

**Date**: July; 1998

This is a copy of the test set of the UCI ML hand-written digits datasets http://archive.ics.uci.edu/ml/datasets/Optical+Recognition+of+Handwritten+Digits

The data set contains images of hand-written digits: 10 classes where each class refers to a digit.

Preprocessing programs made available by NIST were used to extract normalized bitmaps of handwritten digits from a preprinted form. From a total of 43 people, 30 contributed to the training set and different 13 to the test set. 32x32 bitmaps are divided into nonoverlapping blocks of 4x4 and the number of on pixels are counted in each block. This generates an input matrix of 8x8 where each element is an integer in the range 0..16. This reduces dimensionality and gives invariance to small distortions.


**References**


3.5.18 Iris Plants Database

Notes

Data Set Characteristics:

- **Number of Instances**: 150 (50 in each of three classes)
- **Number of Attributes**: 4 numeric, predictive attributes and the class

**Attribute Information**

- sepal length in cm
• sepal width in cm
• petal length in cm
• petal width in cm

• class:
  – Iris-Setosa
  – Iris-Versicolour
  – Iris-Virginica

Summary Statistics

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<thead>
<tr>
<th>attribute</th>
<th>minimum</th>
<th>first quartile</th>
<th>median</th>
<th>third quartile</th>
<th>maximum</th>
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<tr>
<td>sepal length</td>
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<td>5.84</td>
<td>6.83</td>
<td>7.93</td>
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<td>sepal width</td>
<td>2.0</td>
<td>2.8</td>
<td>3.05</td>
<td>3.55</td>
<td>4.4</td>
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<td>petal length</td>
<td>1.0</td>
<td>1.96</td>
<td>2.03</td>
<td>2.1</td>
<td>6.9</td>
</tr>
<tr>
<td>petal width</td>
<td>0.1</td>
<td>0.22</td>
<td>0.4</td>
<td>1.0</td>
<td>2.5</td>
</tr>
</tbody>
</table>

Missing Attribute Values  None

Class Distribution  33.3% for each of 3 classes.

Creator  R.A. Fisher
Donor  Michael Marshall (MARSHALL%PLU@io.arc.nasa.gov)
Date  July, 1988

This is a copy of UCI ML iris datasets. http://archive.ics.uci.edu/ml/datasets/Iris

The famous Iris database, first used by Sir R.A Fisher

This is perhaps the best known database to be found in the pattern recognition literature. Fisher’s paper is a classic in the field and is referenced frequently to this day. (See Duda & Hart, for example.) The data set contains 3 classes of 50 instances each, where each class refers to a type of iris plant. One class is linearly separable from the other 2; the latter are NOT linearly separable from each other.

References


• See also: 1988 MLC Proceedings, 54-64. Cheeseman et al”s AUTOCLASS II conceptual clustering system finds 3 classes in the data.

• Many, many more …
3.5.19 Linnerud dataset

Notes

Data Set Characteristics:

Number of Instances  20
Number of Attributes  3
Missing Attribute Values  None

The Linnerud dataset contains two small dataset:

- exercise: A list containing the following components: exercise data with 20 observations on 3 exercise variables: Weight, Waist and Pulse.
- physiological: Data frame with 20 observations on 3 physiological variables: Chins, Situps and Jumps.

References


3.6 Strategies to scale computationally: bigger data

For some applications the amount of examples, features (or both) and/or the speed at which they need to be processed are challenging for traditional approaches. In these cases scikit-learn has a number of options you can consider to make your system scale.

3.6.1 Scaling with instances using out-of-core learning

Out-of-core (or “external memory”) learning is a technique used to learn from data that cannot fit in a computer’s main memory (RAM).

Here is sketch of a system designed to achieve this goal:

1. a way to stream instances
2. a way to extract features from instances
3. an incremental algorithm

Streaming instances

Basically, 1. may be a reader that yields instances from files on a hard drive, a database, from a network stream etc. However, details on how to achieve this are beyond the scope of this documentation.

Extracting features

2. could be any relevant way to extract features among the different feature extraction methods supported by scikit-learn. However, when working with data that needs vectorization and where the set of features or values is not known in advance one should take explicit care. A good example is text classification where unknown terms are likely to be found during training. It is possible to use a stateful vectorizer if making multiple passes over the data is reasonable from an application point of view. Otherwise, one can turn up the difficulty by using a stateless feature
extractor. Currently the preferred way to do this is to use the so-called hashing trick as implemented by \texttt{sklearn.feature_extraction.FeatureHasher} for datasets with categorical variables represented as list of Python dicts or \texttt{sklearn.feature_extraction.text.HashingVectorizer} for text documents.

**Incremental learning**

Finally, for 3. we have a number of options inside scikit-learn. Although all algorithms cannot learn incrementally (i.e. without seeing all the instances at once), all estimators implementing the \texttt{partial\_fit} API are candidates. Actually, the ability to learn incrementally from a mini-batch of instances (sometimes called “online learning”) is key to out-of-core learning as it guarantees that at any given time there will be only a small amount of instances in the main memory. Choosing a good size for the mini-batch that balances relevancy and memory footprint could involve some tuning\(^1\).

Here is a list of incremental estimators for different tasks:

- **Classification**
  - \texttt{sklearn.naive\_bayes.MultinomialNB}
  - \texttt{sklearn.naive\_bayes.BernoulliNB}
  - \texttt{sklearn.linear\_model.Perceptron}
  - \texttt{sklearn.linear\_model.SGDClassifier}
  - \texttt{sklearn.linear\_model.PassiveAggressiveClassifier}
  - \texttt{sklearn.neural\_network.MLPClassifier}

- **Regression**
  - \texttt{sklearn.linear\_model.SGDRegressor}
  - \texttt{sklearn.linear\_model.PassiveAggressiveRegressor}
  - \texttt{sklearn.neural\_network.MLPRegressor}

- **Clustering**
  - \texttt{sklearn.cluster.MiniBatchKMeans}
  - \texttt{sklearn.cluster.Birch}

- **Decomposition / feature Extraction**
  - \texttt{sklearn.decomposition.MiniBatchDictionaryLearning}
  - \texttt{sklearn.decomposition.IncrementalPCA}
  - \texttt{sklearn.decomposition.LatentDirichletAllocation}

- **Preprocessing**
  - \texttt{sklearn.preprocessing.StandardScaler}
  - \texttt{sklearn.preprocessing.MinMaxScaler}
  - \texttt{sklearn.preprocessing.MaxAbsScaler}

\(^1\) Depending on the algorithm the mini-batch size can influence results or not. SGD*, PassiveAggressive*, and discrete NaiveBayes are truly online and are not affected by batch size. Conversely, MiniBatchKMeans convergence rate is affected by the batch size. Also, its memory footprint can vary dramatically with batch size.
For classification, a somewhat important thing to note is that although a stateless feature extraction routine may be able to cope with new/unseen attributes, the incremental learner itself may be unable to cope with new/unseen targets classes. In this case you have to pass all the possible classes to the first `partial_fit` call using the `classes=` parameter.

Another aspect to consider when choosing a proper algorithm is that all of them don’t put the same importance on each example over time. Namely, the Perceptron is still sensitive to badly labeled examples even after many examples whereas the SGD* and PassiveAggressive* families are more robust to this kind of artifacts. Conversely, the later also tend to give less importance to remarkably different, yet properly labeled examples when they come late in the stream as their learning rate decreases over time.

**Examples**

Finally, we have a full-fledged example of *Out-of-core classification of text documents*. It is aimed at providing a starting point for people wanting to build out-of-core learning systems and demonstrates most of the notions discussed above.

Furthermore, it also shows the evolution of the performance of different algorithms with the number of processed examples.

Now looking at the computation time of the different parts, we see that the vectorization is much more expensive than learning itself. From the different algorithms, MultinomialNB is the most expensive, but its overhead can be mitigated by increasing the size of the mini-batches (exercise: change `minibatch_size` to 100 and 10000 in the program and compare).
3.7 Computational Performance

For some applications the performance (mainly latency and throughput at prediction time) of estimators is crucial. It may also be of interest to consider the training throughput but this is often less important in a production setup (where it often takes place offline).

We will review here the orders of magnitude you can expect from a number of scikit-learn estimators in different contexts and provide some tips and tricks for overcoming performance bottlenecks.

Prediction latency is measured as the elapsed time necessary to make a prediction (e.g. in micro-seconds). Latency is often viewed as a distribution and operations engineers often focus on the latency at a given percentile of this distribution (e.g. the 90 percentile).

Prediction throughput is defined as the number of predictions the software can deliver in a given amount of time (e.g. in predictions per second).

An important aspect of performance optimization is also that it can hurt prediction accuracy. Indeed, simpler models (e.g. linear instead of non-linear, or with fewer parameters) often run faster but are not always able to take into account the same exact properties of the data as more complex ones.

3.7.1 Prediction Latency

One of the most straight-forward concerns one may have when using/choosing a machine learning toolkit is the latency at which predictions can be made in a production environment.

The main factors that influence the prediction latency are

1. Number of features
2. Input data representation and sparsity
3. Model complexity
4. Feature extraction

A last major parameter is also the possibility to do predictions in bulk or one-at-a-time mode.

**Bulk versus Atomic mode**

In general doing predictions in bulk (many instances at the same time) is more efficient for a number of reasons (branching predictability, CPU cache, linear algebra libraries optimizations etc.). Here we see on a setting with few features that independently of estimator choice the bulk mode is always faster, and for some of them by 1 to 2 orders of magnitude:
To benchmark different estimators for your case you can simply change the `n_features` parameter in this example: 

*Prediction Latency*. This should give you an estimate of the order of magnitude of the prediction latency.

---

### Configuring Scikit-learn for reduced validation overhead

Scikit-learn does some validation on data that increases the overhead per call to `predict` and similar functions. In particular, checking that features are finite (not NaN or infinite) involves a full pass over the data. If you ensure that your data is acceptable, you may suppress checking for finiteness by setting the environment variable `SKLEARN_ASSUME_FINITE` to a non-empty string before importing scikit-learn, or configure it in Python with `sklearn.set_config`. For more control than these global settings, a `config_context` allows you to set this configuration within a specified context:

```python
>>> import sklearn
>>> with sklearn.config_context(assume_finite=True):
...    pass  # do learning/prediction here with reduced validation
```

Note that this will affect all uses of `sklearn.utils.assert_all_finite` within the context.

---

### Influence of the Number of Features

Obviously when the number of features increases so does the memory consumption of each example. Indeed, for a matrix of $M$ instances with $N$ features, the space complexity is in $O(NM)$. From a computing perspective it also means that the number of basic operations (e.g., multiplications for vector-matrix products in linear models) increases too. Here is a graph of the evolution of the prediction latency with the number of features:
Overall you can expect the prediction time to increase at least linearly with the number of features (non-linear cases can happen depending on the global memory footprint and estimator).

### Influence of the Input Data Representation

Scipy provides sparse matrix data structures which are optimized for storing sparse data. The main feature of sparse formats is that you don’t store zeros so if your data is sparse then you use much less memory. A non-zero value in a sparse (CSR or CSC) representation will only take on average one 32bit integer position + the 64 bit floating point value + an additional 32bit per row or column in the matrix. Using sparse input on a dense (or sparse) linear model can speedup prediction by quite a bit as only the non zero valued features impact the dot product and thus the model predictions. Hence if you have 100 non zeros in 1e6 dimensional space, you only need 100 multiply and add operation instead of 1e6.

Calculation over a dense representation, however, may leverage highly optimised vector operations and multithreading in BLAS, and tends to result in fewer CPU cache misses. So the sparsity should typically be quite high (10% non-zeros max, to be checked depending on the hardware) for the sparse input representation to be faster than the dense input representation on a machine with many CPUs and an optimized BLAS implementation.

Here is sample code to test the sparsity of your input:

```python
def sparsity_ratio(X):
    return 1.0 - np.count_nonzero(X) / float(X.shape[0] * X.shape[1])
print("input sparsity ratio: ", sparsity_ratio(X))
```

As a rule of thumb you can consider that if the sparsity ratio is greater than 90% you can probably benefit from sparse formats. Check Scipy’s sparse matrix formats documentation for more information on how to build (or convert your data to) sparse matrix formats. Most of the time the CSR and CSC formats work best.
Influence of the Model Complexity

Generally speaking, when model complexity increases, predictive power and latency are supposed to increase. Increasing predictive power is usually interesting, but for many applications we would better not increase prediction latency too much. We will now review this idea for different families of supervised models.

For `sklearn.linear_model` (e.g. Lasso, ElasticNet, SGDClassifier/Regressor, Ridge & RidgeClassifier, PassiveAggressiveClassifier/Regressor, LinearSVC, LogisticRegression...) the decision function that is applied at prediction time is the same (a dot product), so latency should be equivalent.

Here is an example using `sklearn.linear_model.stochastic_gradient.SGDClassifier` with the `elasticnet` penalty. The regularization strength is globally controlled by the `alpha` parameter. With a sufficiently high `alpha`, one can then increase the `l1_ratio` parameter of `elasticnet` to enforce various levels of sparsity in the model coefficients. Higher sparsity here is interpreted as less model complexity as we need fewer coefficients to describe it fully. Of course sparsity influences in turn the prediction time as the sparse dot-product takes time roughly proportional to the number of non-zero coefficients.

![Influence of Model Complexity - SGDClassifier](image)

For the `sklearn.svm` family of algorithms with a non-linear kernel, the latency is tied to the number of support vectors (the fewer the faster). Latency and throughput should (asymptotically) grow linearly with the number of support vectors in a SVC or SVR model. The kernel will also influence the latency as it is used to compute the projection of the input vector once per support vector. In the following graph the `nu` parameter of `sklearn.svm.classes.NuSVR` was used to influence the number of support vectors.
For *sklearn.ensemble* of trees (e.g. RandomForest, GBT, ExtraTrees etc) the number of trees and their depth play the most important role. Latency and throughput should scale linearly with the number of trees. In this case we used directly the *n_estimators* parameter of *sklearn.ensemble.gradient_boosting*. GradientBoostingRegressor.

In any case be warned that decreasing model complexity can hurt accuracy as mentioned above. For instance a non-linearly separable problem can be handled with a speedy linear model but prediction power will very likely suffer in the process.
Feature Extraction Latency

Most scikit-learn models are usually pretty fast as they are implemented either with compiled Cython extensions or optimized computing libraries. On the other hand, in many real world applications the feature extraction process (i.e. turning raw data like database rows or network packets into numpy arrays) governs the overall prediction time. For example on the Reuters text classification task the whole preparation (reading and parsing SGML files, tokenizing the text and hashing it into a common vector space) is taking 100 to 500 times more time than the actual prediction code, depending on the chosen model.

In many cases it is thus recommended to carefully time and profile your feature extraction code as it may be a good place to start optimizing when your overall latency is too slow for your application.

3.7.2 Prediction Throughput

Another important metric to care about when sizing production systems is the throughput i.e. the number of predictions you can make in a given amount of time. Here is a benchmark from the Prediction Latency example that measures this quantity for a number of estimators on synthetic data:
These throughputs are achieved on a single process. An obvious way to increase the throughput of your application is to spawn additional instances (usually processes in Python because of the GIL) that share the same model. One might also add machines to spread the load. A detailed explanation on how to achieve this is beyond the scope of this documentation though.

### 3.7.3 Tips and Tricks

#### Linear algebra libraries

As scikit-learn relies heavily on Numpy/Scipy and linear algebra in general it makes sense to take explicit care of the versions of these libraries. Basically, you ought to make sure that Numpy is built using an optimized BLAS / LAPACK library.

Not all models benefit from optimized BLAS and Lapack implementations. For instance models based on (randomized) decision trees typically do not rely on BLAS calls in their inner loops, nor do kernel SVMs (SVC, SVR, NuSVC, NuSVR). On the other hand a linear model implemented with a BLAS DGEMM call (via `numpy.dot`) will typically benefit hugely from a tuned BLAS implementation and lead to orders of magnitude speedup over a non-optimized BLAS.

You can display the BLAS / LAPACK implementation used by your NumPy / SciPy / scikit-learn install with the following commands:

```python
from numpy.distutils.system_info import get_info
print(get_info('blas_opt'))
print(get_info('lapack_opt'))
```

Optimized BLAS / LAPACK implementations include:

- Atlas (need hardware specific tuning by rebuilding on the target machine)
• OpenBLAS
• MKL
• Apple Accelerate and vecLib frameworks (OSX only)

More information can be found on the Scipy install page and in this blog post from Daniel Nouri which has some nice step by step install instructions for Debian / Ubuntu.

**Warning:** Multithreaded BLAS libraries sometimes conflict with Python’s `multiprocessing` module, which is used by e.g. GridSearchCV and most other estimators that take an `n_jobs` argument (with the exception of SGDClassifier, SGDRegressor, Perceptron, PassiveAggressiveClassifier and tree-based methods such as random forests). This is true of Apple’s Accelerate and OpenBLAS when built with OpenMP support.

Besides scikit-learn, NumPy and SciPy also use BLAS internally, as explained earlier.

If you experience hanging subprocesses with `n_jobs>1` or `n_jobs=-1`, make sure you have a single-threaded BLAS library, or set `n_jobs=1`, or upgrade to Python 3.4 which has a new version of `multiprocessing` that should be immune to this problem.

---

**Model Compression**

Model compression in scikit-learn only concerns linear models for the moment. In this context it means that we want to control the model sparsity (i.e. the number of non-zero coordinates in the model vectors). It is generally a good idea to combine model sparsity with sparse input data representation.

Here is sample code that illustrates the use of the `sparsify()` method:

```python
clf = SGDRegressor(penalty='elasticnet', l1_ratio=0.25)
clf.fit(X_train, y_train).sparsify()
clf.predict(X_test)
```

In this example we prefer the `elasticnet` penalty as it is often a good compromise between model compactness and prediction power. One can also further tune the `l1_ratio` parameter (in combination with the regularization strength `alpha`) to control this tradeoff.

A typical benchmark on synthetic data yields a >30% decrease in latency when both the model and input are sparse (with 0.000024 and 0.027400 non-zero coefficients ratio respectively). Your mileage may vary depending on the sparsity and size of your data and model. Furthermore, sparsifying can be very useful to reduce the memory usage of predictive models deployed on production servers.

---

**Model Reshaping**

Model reshaping consists in selecting only a portion of the available features to fit a model. In other words, if a model discards features during the learning phase we can then strip those from the input. This has several benefits. Firstly it reduces memory (and therefore time) overhead of the model itself. It also allows to discard explicit feature selection components in a pipeline once we know which features to keep from a previous run. Finally, it can help reduce processing time and I/O usage upstream in the data access and feature extraction layers by not collecting and building features that are discarded by the model. For instance if the raw data come from a database, it can make it possible to write simpler and faster queries or reduce I/O usage by making the queries return lighter records. At the moment, reshaping needs to be performed manually in scikit-learn. In the case of sparse input (particularly in CSR format), it is generally sufficient to not generate the relevant features, leaving their columns empty.
Links

- scikit-learn developer performance documentation
- Scipy sparse matrix formats documentation
General-purpose and introductory examples for the scikit.

### 4.1 Plotting Cross-Validated Predictions

This example shows how to use `cross_val_predict` to visualize prediction errors.

```python
from sklearn import datasets
from sklearn.model_selection import cross_val_predict
from sklearn import linear_model
import matplotlib.pyplot as plt
```

```python
from sklearn import datasets
from sklearn.model_selection import cross_val_predict
from sklearn import linear_model
import matplotlib.pyplot as plt
```
```python
lr = linear_model.LinearRegression()
boston = datasets.load_boston()
y = boston.target

# cross_val_predict returns an array of the same size as 'y' where each entry
# is a prediction obtained by cross validation:
predicted = cross_val_predict(lr, boston.data, y, cv=10)

fig, ax = plt.subplots()
ax.scatter(y, predicted, edgecolors=(0, 0, 0))
ax.plot([y.min(), y.max()], [y.min(), y.max()], 'k--', lw=4)
ax.set_xlabel('Measured')
ax.set_ylabel('Predicted')
plt.show()
```

**Total running time of the script:** ( 0 minutes 0.097 seconds)

### 4.2 Concatenating multiple feature extraction methods

In many real-world examples, there are many ways to extract features from a dataset. Often it is beneficial to combine several methods to obtain good performance. This example shows how to use FeatureUnion to combine features obtained by PCA and univariate selection.

Combining features using this transformer has the benefit that it allows cross validation and grid searches over the whole process.

The combination used in this example is not particularly helpful on this dataset and is only used to illustrate the usage of FeatureUnion.

Out:

<table>
<thead>
<tr>
<th>Fitting 3 folds for each of 18 candidates, totalling 54 fits</th>
</tr>
</thead>
<tbody>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=0.1, score=0.9607843137254902, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=0.1, score=0.9019607843137255, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=0.1, score=0.9791666666666666, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=1, score=0.9411764705882353, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=1, score=0.9215686274509803, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=10, score=0.9607843137254902, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=10, score=0.9215686274509803, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=10, score=0.9607843137254902, total= 0.0s</td>
</tr>
<tr>
<td>[CV] features_pca__n_components=1, features_univ_select__k=1, svm__C=10, score=0.9215686274509803, total= 0.0s</td>
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<td>CV</td>
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</tbody>
</table>

### 4.2. Concatenating multiple feature extraction methods

This section discusses the process of combining multiple feature extraction methods in a machine learning pipeline. It explains how to configure and evaluate different combinations of feature selection and transformation techniques, such as PCA and univariate selection, along with various SVM hyperparameters.

The table above illustrates several examples where different feature sets are compared. Each row represents a different combination of parameters tested, such as the number of components in PCA (`features__pca__n_components`) and the number of features selected using univariate selection (`features__univ_select__k`). The `svm__C` parameter varies across the rows to illustrate the impact of different regularization strengths on classification performance.

The `score` column indicates the accuracy metric (e.g., 0.979) obtained for each combination, and the `total` column shows the time taken for each cross-validation (CV) run, which is consistently 0.0 seconds for all examples, suggesting that the computations are very efficient.

This approach allows for a systematic exploration of different feature extraction strategies to optimize model performance, especially in scenarios where data dimensionality reduction and feature selection are critical for improving model interpretability and efficiency.
Chapter 4. General examples

```python
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=0.1, score=0.9803921568627451, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=0.1
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=0.1, score=0.9411764705882353, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=0.1, score=0.9791666666666666, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=1
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=1, score=1.0, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=1
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=1, score=0.9215686274509803, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=10
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=10, score=1.0, total= 0.0s
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=10
[CV] features__pca__n_components=2, features__univ_select__k=2, svm__C=10, score=0.9215686274509803, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=0.1
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=0.1, score=0.9803921568627451, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=0.1, score=0.9411764705882353, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=0.1, score=0.9791666666666666, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=1
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=1, score=0.9411764705882353, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=1, score=0.9791666666666666, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=10
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=10, score=1.0, total= 0.0s
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=10
[CV] features__pca__n_components=3, features__univ_select__k=1, svm__C=10, score=0.9215686274509803, total= 0.0s
```
Pipeline(memory=None, 
steps=[('features', FeatureUnion(n_jobs=1, 
    transformer_list=[('pca', PCA(copy=True, iterated_power='auto', n_components=2, 
    random_state=None, 
    svd_solver='auto', tol=0.0, whiten=False)), ('univ_select', SelectKBest(k=2, score_func=<function f_classif at 0x2ab9d90e1ae8>))]), 
    transformer..., 
    max_iter=-1, probability=False, random_state=None, shrinking=True, 
    tol=0.001, verbose=False))])

# Author: Andreas Mueller <amueller@ais.uni-bonn.de>
#
# License: BSD 3 clause

deficit from sklearn.pipeline import Pipeline, FeatureUnion
from sklearn.model_selection import GridSearchCV
from sklearn.svm import SVC
from sklearn.datasets import load_iris
from sklearn.decomposition import PCA
from sklearn.feature_selection import SelectKBest

iris = load_iris()
X, y = iris.data, iris.target

# This dataset is way too high-dimensional. Better do PCA.
# pca = PCA(n_components=2)

# Maybe some original features where good, too?
selection = SelectKBest(k=1)

# Build estimator from PCA and Univariate selection:

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combined_features = FeatureUnion(["pca", pca], ["univ_select", selection])

# Use combined features to transform dataset:
X_features = combined_features.fit(X, y).transform(X)

svm = SVC(kernel="linear")

# Do grid search over k, n_components and C:

pipeline = Pipeline(["features", combined_features], ["svm", svm])

param_grid = dict(features__pca__n_components=[1, 2, 3],
                  features__univ_select__k=[1, 2],
                  svm__C=[0.1, 1, 10])

grid_search = GridSearchCV(pipeline, param_grid=param_grid, verbose=10)
grid_search.fit(X, y)
print(grid_search.best_estimator_)

Total running time of the script: ( 0 minutes 0.416 seconds)

4.3 Pipelining: chaining a PCA and a logistic regression

The PCA does an unsupervised dimensionality reduction, while the logistic regression does the prediction.

We use a GridSearchCV to set the dimensionality of the PCA

print(__doc__)
import numpy as np
import matplotlib.pyplot as plt

from sklearn import linear_model, decomposition, datasets
from sklearn.pipeline import Pipeline
from sklearn.model_selection import GridSearchCV

logistic = linear_model.LogisticRegression()
pca = decomposition.PCA()
pipe = Pipeline(steps=[('pca', pca), ('logistic', logistic)])
digits = datasets.load_digits()
X_digits = digits.data
y_digits = digits.target

# Plot the PCA spectrum
pca.fit(X_digits)
plt.figure(1, figsize=(4, 3))
plt.clf()
plt.axes([.2, .2, .7, .7])
plt.plot(pca.explained_variance_, linewidth=2)
plt.axis('tight')
plt.xlabel('n_components')
plt.ylabel('explained_variance_')

# Prediction
n_components = [20, 40, 64]
Cs = np.logspace(-4, 4, 3)

# Parameters of pipelines can be set using '__' separated parameter names:
estimator = GridSearchCV(pipe,
        dict(pca__n_components=n_components,
             logistic__C=Cs))
estimator.fit(X_digits, y_digits)

plt.axvline(estimator.best_estimator_.named_steps['pca'].n_components,
            linestyle=':', label='n_components chosen')
plt.legend(prop=dict(size=12))
plt.show()

Total running time of the script: ( 0 minutes 9.273 seconds)

4.4 Isotonic Regression

An illustration of the isotonic regression on generated data. The isotonic regression finds a non-decreasing approximation of a function while minimizing the mean squared error on the training data. The benefit of such a model is that it does not assume any form for the target function such as linearity. For comparison a linear regression is also presented.
# Author: Nelle Varoquaux <nelle.varoquaux@gmail.com>
# Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD

import numpy as np
import matplotlib.pyplot as plt
from matplotlib.collections import LineCollection
from sklearn.linear_model import LinearRegression
from sklearn.isotonic import IsotonicRegression
from sklearn.utils import check_random_state

n = 100
x = np.arange(n)
rs = check_random_state(0)
y = rs.randint(-50, 50, size=(n,)) + 50. * np.log(1 + np.arange(n))

# Fit IsotonicRegression and LinearRegression models

ir = IsotonicRegression()
y_ = ir.fit_transform(x, y)

```python
lr = LinearRegression()
lr.fit(x[:, np.newaxis], y)  # x needs to be 2d for LinearRegression

# Plot result
segments = [[i, y[i]], [i, y[i]_]] for i in range(n)]
lc = LineCollection(segments, zorder=0)
lc.set_array(np.ones(len(y)))
lc.set_linewidths(0.5 * np.ones(n))
fig = plt.figure()
plt.plot(x, y, 'r.', markersize=12)
plt.plot(x, y_, 'g.-', markersize=12)
plt.plot(x, lr.predict(x[:, np.newaxis]), 'b-')
plt.gca().add_collection(lc)
plt.legend(('Data', 'Isotonic Fit', 'Linear Fit'), loc='lower right')
plt.title('Isotonic regression')
plt.show()
```

Total running time of the script: 0 minutes 0.071 seconds

### 4.5 Imputing missing values before building an estimator

This example shows that imputing the missing values can give better results than discarding the samples containing any missing value. Imputing does not always improve the predictions, so please check via cross-validation. Sometimes dropping rows or using marker values is more effective.

Missing values can be replaced by the mean, the median or the most frequent value using the `strategy` hyper-parameter. The median is a more robust estimator for data with high magnitude variables which could dominate results (otherwise known as a ‘long tail’).

Script output:

```
Score with the entire dataset = 0.56
Score without the samples containing missing values = 0.48
Score after imputation of the missing values = 0.55
```

In this case, imputing helps the classifier get close to the original score.

Out:

```
Score with the entire dataset = 0.56
Score without the samples containing missing values = 0.48
Score after imputation of the missing values = 0.57
```
from sklearn.preprocessing import Imputer
from sklearn.model_selection import cross_val_score

rng = np.random.RandomState(0)

dataset = load_boston()
X_full, y_full = dataset.data, dataset.target
n_samples = X_full.shape[0]
n_features = X_full.shape[1]

# Estimate the score on the entire dataset, with no missing values
estimator = RandomForestRegressor(random_state=0, n_estimators=100)
score = cross_val_score(estimator, X_full, y_full).mean()
print("Score with the entire dataset = %.2f" % score)

# Add missing values in 75% of the lines
missing_rate = 0.75
n_missing_samples = int(np.floor(n_samples * missing_rate))
missing_samples = np.hstack((np.zeros(n_samples - n_missing_samples,
dtype=np.bool),
np.ones(n_missing_samples,
dtype=np.bool))

rng.shuffle(missing_samples)
missing_features = rng.randint(0, n_features, n_missing_samples)

# Estimate the score without the lines containing missing values
X_filtered = X_full[~np.isnan(missing_samples), :]
y_filtered = y_full[~np.isnan(missing_samples)]

estimator = RandomForestRegressor(random_state=0, n_estimators=100)
score = cross_val_score(estimator, X_filtered, y_filtered).mean()
print("Score without the samples containing missing values = %.2f" % score)

# Estimate the score after imputation of the missing values
X_missing = X_full.copy()
X_missing[missing_samples, missing_features] = 0
y_missing = y_full.copy()

estimator = Pipeline([("imputer", Imputer(missing_values=0,
                          strategy="mean",
                          axis=0)),
                      ("forest", RandomForestRegressor(random_state=0,
                          n_estimators=100))])

score = cross_val_score(estimator, X_missing, y_missing).mean()
print("Score after imputation of the missing values = %.2f" % score)

Total running time of the script: ( 0 minutes 1.574 seconds)

4.6 Face completion with a multi-output estimators

This example shows the use of multi-output estimator to complete images. The goal is to predict the lower half of a face given its upper half.

The first column of images shows true faces. The next columns illustrate how extremely randomized trees, k nearest neighbors, linear regression and ridge regression complete the lower half of those faces.
Face completion with multi-output estimators

```
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets import fetch_olivetti_faces
from sklearn.utils.validation import check_random_state
from sklearn.ensemble import ExtraTreesRegressor
```
from sklearn.neighbors import KNeighborsRegressor
from sklearn.linear_model import LinearRegression
from sklearn.linear_model import RidgeCV

# Load the faces datasets
data = fetch_olivetti_faces()
targets = data.target

data = data.images.reshape((len(data.images), -1))
train = data[targets < 30]
test = data[targets >= 30]  # Test on independent people

# Test on a subset of people
n_faces = 5
rng = check_random_state(4)
face_ids = rng.randint(test.shape[0], size=(n_faces, ))
test = test[face_ids, :]

n_pixels = data.shape[1]
# Upper half of the faces
X_train = train[:, :(n_pixels + 1) // 2]
# Lower half of the faces
y_train = train[:, n_pixels // 2:]
X_test = test[:, :(n_pixels + 1) // 2]
y_test = test[:, n_pixels // 2:]

# Fit estimators
ESTIMATORS = {
    "Extra trees": ExtraTreesRegressor(n_estimators=10, max_features=32,
                                        random_state=0),
    "K-nn": KNeighborsRegressor(),
    "Linear regression": LinearRegression(),
    "Ridge": RidgeCV(),
}

y_test_predict = dict()
for name, estimator in ESTIMATORS.items():
    estimator.fit(X_train, y_train)
    y_test_predict[name] = estimator.predict(X_test)

# Plot the completed faces
image_shape = (64, 64)

n_cols = 1 + len(ESTIMATORS)
plt.figure(figsize=(2. * n_cols, 2.26 * n_faces))
plt.suptitle("Face completion with multi-output estimators", size=16)

for i in range(n_faces):
    true_face = np.hstack((X_test[i], y_test[i]))

    if i:
        sub = plt.subplot(n_faces, n_cols, i * n_cols + 1)
    else:
        sub = plt.subplot(n_faces, n_cols, i * n_cols + 1,
                          title="true faces")

    sub.axis("off")
    sub.imshow(true_face.reshape(image_shape),

Chapter 4. General examples
for j, est in enumerate(sorted(ESTIMATORS)):
    completed_face = np.hstack((X_test[i], y_test_predict[est][i]))
    if i:
        sub = plt.subplot(n_faces, n_cols, i * n_cols + 2 + j)
    else:
        sub = plt.subplot(n_faces, n_cols, i * n_cols + 2 + j,
                          title=est)
    sub.axis("off")
    sub.imshow(completed_face.reshape(image_shape),
               cmap=plt.cm.gray,
               interpolation="nearest")
plt.show()

Total running time of the script: ( 0 minutes 3.860 seconds)

4.7 Selecting dimensionality reduction with Pipeline and GridSearchCV

This example constructs a pipeline that does dimensionality reduction followed by prediction with a support vector classifier. It demonstrates the use of GridSearchCV and Pipeline to optimize over different classes of estimators in a single CV run – unsupervised PCA and NMF dimensionality reductions are compared to univariate feature selection during the grid search.

Additionally, Pipeline can be instantiated with the memory argument to memoize the transformers within the pipeline, avoiding to fit again the same transformers over and over.

Note that the use of memory to enable caching becomes interesting when the fitting of a transformer is costly.

4.7.1 Illustration of Pipeline and GridSearchCV

This section illustrates the use of a Pipeline with GridSearchCV

# Authors: Robert McGibbon, Joel Nothman, Guillaume Lemaitre

from __future__ import print_function, division

import numpy as np
import matplotlib.pyplot as plt
from sklearn.datasets import load_digits
from sklearn.model_selection import GridSearchCV
from sklearn.pipeline import Pipeline
from sklearn.svm import LinearSVC
from sklearn.decomposition import PCA, NMF
from sklearn.feature_selection import SelectKBest, chi2

print(__doc__)
```python
pipe = Pipeline([('reduce_dim', PCA()), ('classify', LinearSVC())])

N_FEATURES_OPTIONS = [2, 4, 8]
C_OPTIONS = [1, 10, 100, 1000]
param_grid = [
    {'reduce_dim': [PCA(iterated_power=7), NMF()],
     'reduce_dim__n_components': N_FEATURES_OPTIONS,
     'classify__C': C_OPTIONS},
    {'reduce_dim': [SelectKBest(chi2)],
     'reduce_dim__k': N_FEATURES_OPTIONS,
     'classify__C': C_OPTIONS},
]
reducer_labels = ['PCA', 'NMF', 'KBest(chi2)']

grid = GridSearchCV(pipe, cv=3, n_jobs=1, param_grid=param_grid)
digits = load_digits()
grid.fit(digits.data, digits.target)
mean_scores = np.array(grid.cv_results_['mean_test_score'])
# scores are in the order of param_grid iteration, which is alphabetical
mean_scores = mean_scores.reshape(len(C_OPTIONS), -1, len(N_FEATURES_OPTIONS))
# select score for best C
bar_offsets = (np.arange(len(N_FEATURES_OPTIONS)) * (len(reducer_labels) + 1) + .5)

plt.figure()
COLORS = 'bgrcmyk'
for i, (label, reducer_scores) in enumerate(zip(reducer_labels, mean_scores)):
    plt.bar(bar_offsets + i, reducer_scores, label=label, color=COLORS[i])

plt.title("Comparing feature reduction techniques")
plt.xlabel('Reduced number of features')
plt.xticks(bar_offsets + len(reducer_labels) / 2, N_FEATURES_OPTIONS)
plt.ylabel('Digit classification accuracy')
plt.ylim((0, 1))
plt.legend(loc='upper left')
```
4.7.2 Caching transformers within a Pipeline

It is sometimes worthwhile storing the state of a specific transformer since it could be used again. Using a pipeline in GridSearchCV triggers such situations. Therefore, we use the argument memory to enable caching.

**Warning:** Note that this example is, however, only an illustration since for this specific case fitting PCA is not necessarily slower than loading the cache. Hence, use the memory constructor parameter when the fitting of a transformer is costly.

```python
from tempfile import mkdtemp
from shutil import rmtree
from sklearn.externals.joblib import Memory

# Create a temporary folder to store the transformers of the pipeline
cachedir = mkdtemp()
memory = Memory(cachedir=cachedir, verbose=10)
cached_pipe = Pipeline([('reduce_dim', PCA()),
                        ('classify', LinearSVC())],
                        memory=memory)

# This time, a cached pipeline will be used within the grid search
```

4.7. Selecting dimensionality reduction with Pipeline and GridSearchCV
grid = GridSearchCV(cached_pipe, cv=3, n_jobs=1, param_grid=param_grid)
digits = load_digits()
grid.fit(digits.data, digits.target)

# Delete the temporary cache before exiting
rmtree(cachedir)

Out:

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=2, random_state=None, svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
   ...,
   [ 0., ..., 0.]]), array([0, ..., 8]))      _fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=2, random_state=None, svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
   ...,
   [ 0., ..., 0.]]), array([0, ..., 4]))      _fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=4, random_state=None, svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
   ...,
   [ 0., ..., 0.]]), array([0, ..., 8]))      _fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=4, random_state=None, svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
   ...,
   [ 0., ..., 0.]]), array([0, ..., 4]))      _fit_transform_one - 0.0s, 0.0min
4.7. Selecting dimensionality reduction with Pipeline and GridSearchCV

```python
[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=8, random_state=None,
svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=8, random_state=None,
svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(PCA(copy=True, iterated_power=7, n_components=8, random_state=None,
svd_solver='auto', tol=0.0, whiten=False),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 4]))
________________________________________________fit_transform_one - 0.0s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=None, l1_ratio=0.0, max_iter=200,
n_components=2, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=None, l1_ratio=0.0, max_iter=200,
n_components=2, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=None, l1_ratio=0.0, max_iter=200,
n_components=2, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=None, l1_ratio=0.0, max_iter=200,
n_components=4, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,[ 0., ..., 0.]), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min
```
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=\nNone, l1_ratio=0.0, max_iter=200,
  n_components=4, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=\nNone, l1_ratio=0.0, max_iter=200,
  n_components=8, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=\nNone, l1_ratio=0.0, max_iter=200,
  n_components=8, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=\nNone, l1_ratio=0.0, max_iter=200,
  n_components=8, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 8]))
________________________________________________fit_transform_one - 0.1s, 0.0min

[Memory] Calling sklearn.pipeline._fit_transform_one...
_fit_transform_one(NMF(alpha=0.0, beta_loss='frobenius', init=\nNone, l1_ratio=0.0, max_iter=200,
  n_components=8, random_state=None, shuffle=False, solver='cd',
tol=0.0001, verbose=0),
None, array([[ 0., ..., 0.],
...,
[ 0., ..., 0.])), array([0, ..., 4]))

 0.0s, 0.0min: Loading _fit_transform_one from /tmp/tmpejyu36o7/joblib/sklearn/pipeline/_fit_transform_one/d8a616f804252c078fc32f6bd670f55

 0.0s, 0.0min: _fit_transform_one cache loaded - 0.0s, 0.0min
4.7. Selecting dimensionality reduction with Pipeline and GridSearchCV
4.7. Selecting dimensionality reduction with Pipeline and GridSearchCV 605
fit_transform_one(SelectKBest(k=2, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 4]))

fit_transform_one(SelectKBest(k=4, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 8]))

fit_transform_one(SelectKBest(k=4, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 4]))

fit_transform_one(SelectKBest(k=8, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 8]))

fit_transform_one(SelectKBest(k=8, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 4]))

fit_transform_one(SelectKBest(k=8, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 8]))

fit_transform_one(SelectKBest(k=8, score_func=<function chi2 at 0x2ab9d90e1bf8>), None, array([0., ..., 0.]), array([0, ..., 4]))

0.0s, 0.0min: Loading _fit_transform_one from /tmp/tmpejyu36o7/joblib/
sklearn/pipeline/_fit_transform_one/a1f421076765dbdfe3b91a792d7622b7

0.0s, 0.0min: Loading _fit_transform_one from /tmp/tmpejyu36o7/joblib/
sklearn/pipeline/_fit_transform_one/a9f9602be0de32a37575531214e3dc62

0.0s, 0.0min: Loading _fit_transform_one from /tmp/tmpejyu36o7/joblib/
sklearn/pipeline/_fit_transform_one/56a54583eee027f0706ed9c9ed62b3f5

0.0s, 0.0min: Loading _fit_transform_one from /tmp/tmpejyu36o7/joblib/
sklearn/pipeline/_fit_transform_one/dc5d8487baf2f525a443dc33fa7f830
4.7. Selecting dimensionality reduction with Pipeline and GridSearchCV
The PCA fitting is only computed at the evaluation of the first configuration of the C parameter of the LinearSVC classifier. The other configurations of C will trigger the loading of the cached PCA estimator data, leading to save processing time. Therefore, the use of caching the pipeline using memory is highly beneficial when fitting a transformer is costly.

plt.show()

Total running time of the script: ( 1 minutes 22.419 seconds)

4.8 Multilabel classification

This example simulates a multi-label document classification problem. The dataset is generated randomly based on the following process:

- pick the number of labels: \( n \sim \text{Poisson}(n_{\text{labels}}) \)
- \( n \) times, choose a class \( c \sim \text{Multinomial}(\theta) \)
- pick the document length: \( k \sim \text{Poisson}(\text{length}) \)
- \( k \) times, choose a word: \( w \sim \text{Multinomial}(\theta_c) \)

In the above process, rejection sampling is used to make sure that \( n \) is more than 2, and that the document length is never zero. Likewise, we reject classes which have already been chosen. The documents that are assigned to both classes are plotted surrounded by two colored circles.

The classification is performed by projecting to the first two principal components found by PCA and CCA for visualisation purposes, followed by using the sklearn.multiclass.OneVsRestClassifier metaclassifier using two SVCs with linear kernels to learn a discriminative model for each class. Note that PCA is used to perform an unsupervised dimensionality reduction, while CCA is used to perform a supervised one.

Note: in the plot, “unlabeled samples” does not mean that we don’t know the labels (as in semi-supervised learning) but that the samples simply do not have a label.
import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets import make_multilabel_classification
from sklearn.multiclass import OneVsRestClassifier
from sklearn.svm import SVC
from sklearn.preprocessing import LabelBinarizer
from sklearn.decomposition import PCA
from sklearn.cross_decomposition import CCA

# get the separating hyperplane
w = clf.coef_[0]
a = -w[0] / w[1]
xx = np.linspace(min_x - 5, max_x + 5)  # make sure the line is long enough
yy = a * xx - (clf.intercept_[0]) / w[1]
plt.plot(xx, yy, linestyle, label=label)

def plot_subfigure(X, Y, subplot, title, transform):
    if transform == "pca":  
        X = PCA(n_components=2).fit_transform(X)
    elif transform == "cca":  
        # process CCA

4.8. Multilabel classification 609
```
X = CCA(n_components=2).fit(X, Y).transform(X)
else:
    raise ValueError

min_x = np.min(X[:, 0])
max_x = np.max(X[:, 0])

min_y = np.min(X[:, 1])
max_y = np.max(X[:, 1])

classif = OneVsRestClassifier(SVC(kernel='linear'))
classif.fit(X, Y)

plt.subplot(2, 2, subplot)
plt.title(title)

zero_class = np.where(Y[:, 0])
one_class = np.where(Y[:, 1])
plt.scatter(X[:, 0], X[:, 1], s=40, c='gray', edgecolors=(0, 0, 0))
plt.scatter(X[zero_class, 0], X[zero_class, 1], s=160, edgecolors='b',
            facecolors='none', linewidths=2, label='Class 1')
plt.scatter(X[one_class, 0], X[one_class, 1], s=80, edgecolors='orange',
            facecolors='none', linewidths=2, label='Class 2')

plot_hyperplane(classif.estimators_[0], min_x, max_x, 'k--',
                 'Boundary

               for class 1')
plot_hyperplane(classif.estimators_[1], min_x, max_x, 'k-.',
                 'Boundary

               for class 2')
plt.xticks(())
plt.yticks(())
plt.xlim(min_x - .5 * max_x, max_x + .5 * max_x)
plt.ylim(min_y - .5 * max_y, max_y + .5 * max_y)
if subplot == 2:
    plt.xlabel('First principal component')
    plt.ylabel('Second principal component')
    plt.legend(loc="upper left")

plt.figure(figsize=(8, 6))

X, Y = make_multilabel_classification(n_classes=2, n_labels=1,
                                      allow_unlabeled=True,
                                      random_state=1)

plot_subfigure(X, Y, 1, "With unlabeled samples + CCA", "cca")
plot_subfigure(X, Y, 2, "With unlabeled samples + PCA", "pca")

X, Y = make_multilabel_classification(n_classes=2, n_labels=1,
                                      allow_unlabeled=False,
                                      random_state=1)

plot_subfigure(X, Y, 3, "Without unlabeled samples + CCA", "cca")
plot_subfigure(X, Y, 4, "Without unlabeled samples + PCA", "pca")

plt.subplots_adjust(.04, .02, .97, .94, .09, .2)
plt.show()
```
The Johnson-Lindenstrauss bound for embedding with random projections

The Johnson-Lindenstrauss lemma states that any high dimensional dataset can be randomly projected into a lower dimensional Euclidean space while controlling the distortion in the pairwise distances.

4.9.1 Theoretical bounds

The distortion introduced by a random projection $p$ is asserted by the fact that $p$ is defining an eps-embedding with good probability as defined by:

$$ (1 - \epsilon)\|u - v\|^2 < \|p(u) - p(v)\|^2 < (1 + \epsilon)\|u - v\|^2 $$

Where $u$ and $v$ are any rows taken from a dataset of shape [n_samples, n_features] and $p$ is a projection by a random Gaussian N(0, 1) matrix with shape [n_components, n_features] (or a sparse Achlioptas matrix).

The minimum number of components to guarantees the eps-embedding is given by:

$$ n_{components} \geq 4\log(n_{samples})/(\epsilon^2/2 - \epsilon^3/3) $$

The first plot shows that with an increasing number of samples $n_{samples}$, the minimal number of dimensions $n_{components}$ increased logarithmically in order to guarantee an eps-embedding.

The second plot shows that an increase of the admissible distortion $\epsilon$ allows to reduce drastically the minimal number of dimensions $n_{components}$ for a given number of samples $n_{samples}$

4.9.2 Empirical validation

We validate the above bounds on the digits dataset or on the 20 newsgroups text document (TF-IDF word frequencies) dataset:

- for the digits dataset, some 8x8 gray level pixels data for 500 handwritten digits pictures are randomly projected to spaces for various larger number of dimensions $n_{components}$.

- for the 20 newsgroups dataset some 500 documents with 100k features in total are projected using a sparse random matrix to smaller euclidean spaces with various values for the target number of dimensions $n_{components}$.

The default dataset is the digits dataset. To run the example on the twenty newsgroups dataset, pass the --twenty-newsgroups command line argument to this script.

For each value of $n_{components}$, we plot:

- 2D distribution of sample pairs with pairwise distances in original and projected spaces as x and y axis respectively.

- 1D histogram of the ratio of those distances (projected / original).

We can see that for low values of $n_{components}$ the distribution is wide with many distorted pairs and a skewed distribution (due to the hard limit of zero ratio on the left as distances are always positives) while for larger values of $n_{components}$ the distortion is controlled and the distances are well preserved by the random projection.
4.9.3 Remarks

According to the JL lemma, projecting 500 samples without too much distortion will require at least several thousands dimensions, irrespective of the number of features of the original dataset.

Hence using random projections on the digits dataset which only has 64 features in the input space does not make sense: it does not allow for dimensionality reduction in this case.

On the twenty newsgroups on the other hand the dimensionality can be decreased from 56436 down to 10000 while reasonably preserving pairwise distances.
4.9. The Johnson-Lindenstrauss bound for embedding with random projections
Embedding 500 samples with dim 64 using various random projections
Projected 500 samples from 64 to 300 in 0.019s
Random matrix with size: 0.029MB
Mean distances rate: 1.03 (0.08)
Projected 500 samples from 64 to 1000 in 0.036s
Random matrix with size: 0.095MB
Mean distances rate: 1.00 (0.04)
Projected 500 samples from 64 to 10000 in 0.351s
Random matrix with size: 0.959MB
Mean distances rate: 1.00 (0.01)

print(__doc__)

import sys
from time import time
import numpy as np
import matplotlib.pyplot as plt
from sklearn.random_projection import johnson_lindenstrauss_min_dim
from sklearn.random_projection import SparseRandomProjection
from sklearn.datasets import fetch_20newsgroups_vectorized
from sklearn.datasets import load_digits
from sklearn.metrics.pairwise import euclidean_distances

# Part 1: plot the theoretical dependency between n_components_min and
# n_samples

# range of admissible distortions
eps_range = np.linspace(0.1, 0.99, 5)
colors = plt.cm.Blues(np.linspace(0.3, 1.0, len(eps_range)))

# range of number of samples (observation) to embed
n_samples_range = np.logspace(1, 9, 9)

plt.figure()
for eps, color in zip(eps_range, colors):
    min_n_components = johnson_lindenstrauss_min_dim(n_samples_range, eps=eps)
    plt.loglog(n_samples_range, min_n_components, color=color)
plt.legend(["eps = %0.1f" % eps for eps in eps_range], loc="lower right")
plt.xlabel("Number of observations to eps-embed")
plt.ylabel("Minimum number of dimensions")
plt.title("Johnson-Lindenstrauss bounds: \nn_samples vs n_components")

# range of admissible distortions
eps_range = np.linspace(0.01, 0.99, 100)
# range of number of samples (observation) to embed
n_samples_range = np.logspace(2, 6, 5)
colors = plt.cm.Blues(np.linspace(0.3, 1.0, len(n_samples_range)))

plt.figure()
for n_samples, color in zip(n_samples_range, colors):
    min_n_components = johnson_lindenstrauss_min_dim(n_samples, eps=eps_range)
    plt.semilogy(eps_range, min_n_components, color=color)
plt.legend(["n_samples = %d" % n for n in n_samples_range], loc="upper right")
plt.xlabel("Distortion eps")
plt.ylabel("Minimum number of dimensions")
plt.title("Johnson-Lindenstrauss bounds: \nn_components vs eps")

# Part 2: perform sparse random projection of some digits images which are
# quite low dimensional and dense or documents of the 20 newsgroups dataset
# which is both high dimensional and sparse

if '--twenty-newsgroups' in sys.argv:
    # Need an internet connection hence not enabled by default
    data = fetch_20newsgroups_vectorized().data[:500]
else:
    data = load_digits().data[:500]

n_samples, n_features = data.shape
print("Embedding \%d samples with dim \%d using various random projections" % (n_samples, n_features))

n_components_range = np.array([300, 1000, 10000])
dists = euclidean_distances(data, squared=True).ravel()

# select only non-identical samples pairs
nonzero = dists != 0
dists = dists[nonzero]

for n_components in n_components_range:
    t0 = time()
    rp = SparseRandomProjection(n_components=n_components)
    projected_data = rp.fit_transform(data)
    print("Projected %d samples from %d to %d in %0.3fs" % (n_samples, n_features, n_components, time() - t0))
    if hasattr(rp, 'components_ '):
        n_bytes = rp.components_.data.nbytes
        n_bytes += rp.components_.indices.nbytes
        print("Random matrix with size: %.3fMB % (n_bytes / 1e6))

projected_dists = euclidean_distances(
    projected_data, squared=True).ravel()[nonzero]

plt.figure()
plt.hexbin(dists, projected_dists, gridsize=100, cmap=plt.cm.PuBu)
plt.xlabel("Pairwise squared distances in original space")
plt.ylabel("Pairwise squared distances in projected space")
plt.title("Pairwise distances distribution for n_components=\$d\" % n_components)
cb = plt.colorbar()
cb.set_label('Sample pairs counts')

rates = projected_dists / dists
print("Mean distances rate: %.2f (\$%.2f\")
      % (np.mean(rates), np.std(rates)))

plt.figure()
plt.hist(rates, bins=50, normed=True, range=(0., 2.), edgecolor='k')
plt.xlabel("Squared distances rate: projected / original")
plt.ylabel("Distribution of samples pairs")
plt.title("Histogram of pairwise distance rates for n_components=\$d\" % n_components)

# TODO: compute the expected value of eps and add them to the previous plot
# as vertical lines / region

plt.show()

Total running time of the script: ( 0 minutes 2.204 seconds)

4.10 Comparison of kernel ridge regression and SVR

Both kernel ridge regression (KRR) and SVR learn a non-linear function by employing the kernel trick, i.e., they
learn a linear function in the space induced by the respective kernel which corresponds to a non-linear function in
the original space. They differ in the loss functions (ridge versus epsilon-insensitive loss). In contrast to SVR, fitting a
KRR can be done in closed-form and is typically faster for medium-sized datasets. On the other hand, the learned
model is non-sparse and thus slower than SVR at prediction-time.

This example illustrates both methods on an artificial dataset, which consists of a sinusoidal target function and strong
noise added to every fifth datapoint. The first figure compares the learned model of KRR and SVR when both com-
plexity/regularization and bandwidth of the RBF kernel are optimized using grid-search. The learned functions are
very similar; however, fitting KRR is approx. seven times faster than fitting SVR (both with grid-search). However,
prediction of 100000 target values is more than three times faster with SVR since it has learned a sparse model using only approx. 1/3 of the 100 training datapoints as support vectors.

The next figure compares the time for fitting and prediction of KRR and SVR for different sizes of the training set. Fitting KRR is faster than SVR for medium-sized training sets (less than 1000 samples); however, for larger training sets SVR scales better. With regard to prediction time, SVR is faster than KRR for all sizes of the training set because of the learned sparse solution. Note that the degree of sparsity and thus the prediction time depends on the parameters epsilon and C of the SVR.
scikit-learn user guide, Release 0.20.dev0

SVR complexity
KRR complexity
Support vector
SVR prediction
KRR prediction

and bandwidth selected and
and bandwidth selected and
ratio: 0.320
for 100000 inputs in 0.151
for 100000 inputs in 0.384

model fitted in 0.871 s
model fitted in 0.402 s
s
s

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD 3 clause

from __future__ import division
import time
import numpy as np
from sklearn.svm import SVR
from sklearn.model_selection import GridSearchCV
from sklearn.model_selection import learning_curve
from sklearn.kernel_ridge import KernelRidge
import matplotlib.pyplot as plt
rng = np.random.RandomState(0)
#
#
X
y

#############################################################################
Generate sample data
= 5 * rng.rand(10000, 1)
= np.sin(X).ravel()

# Add noise to targets
y[::5] += 3 * (0.5 - rng.rand(X.shape[0] // 5))
X_plot = np.linspace(0, 5, 100000)[:, None]
# #############################################################################
# Fit regression model
train_size = 100
svr = GridSearchCV(SVR(kernel='rbf', gamma=0.1), cv=5,
param_grid={"C": [1e0, 1e1, 1e2, 1e3],
"gamma": np.logspace(-2, 2, 5)})
kr = GridSearchCV(KernelRidge(kernel='rbf', gamma=0.1), cv=5,
param_grid={"alpha": [1e0, 0.1, 1e-2, 1e-3],
"gamma": np.logspace(-2, 2, 5)})
t0 = time.time()
svr.fit(X[:train_size], y[:train_size])
svr_fit = time.time() - t0
print("SVR complexity and bandwidth selected and model fitted in %.3f s"
% svr_fit)
t0 = time.time()
kr.fit(X[:train_size], y[:train_size])
kr_fit = time.time() - t0

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Chapter 4. General examples


print("KRR complexity and bandwidth selected and model fitted in %.3f s" % kr_fit)

sv_ratio = svr.best_estimator_.support_.shape[0] / train_size
print("Support vector ratio: %.3f" % sv_ratio)

t0 = time.time()
y_svr = svr.predict(X_plot)
svr_predict = time.time() - t0
print("SVR prediction for %d inputs in %.3f s" % (X_plot.shape[0], svr_predict))

t0 = time.time()
y_kr = kr.predict(X_plot)
kr_predict = time.time() - t0
print("KRR prediction for %d inputs in %.3f s" % (X_plot.shape[0], kr_predict))

# Look at the results
sv_ind = svr.best_estimator_.support_
plt.scatter(X[sv_ind], y[sv_ind], c='r', s=50, label='SVR support vectors', zorder=2, edgecolors=(0, 0, 0))
plt.scatter(X[:100], y[:100], c='k', label='data', zorder=1, edgecolors=(0, 0, 0))
plt.plot(X_plot, y_svr, c='r', label='SVR (fit: %.3f s, predict: %.3f s)' % (svr_fit, svr_predict))
plt.plot(X_plot, y_kr, c='g', label='KRR (fit: %.3f s, predict: %.3f s)' % (kr_fit, kr_predict))
plt.xlabel('data')
plt.ylabel('target')
plt.title('SVR versus Kernel Ridge')
plt.legend()

# Visualize training and prediction time
plt.figure()
# Generate sample data
X = 5 * rng.rand(10000, 1)
y = np.sin(X).ravel()
y[::5] += 3 * (0.5 - rng.rand(X.shape[0] // 5))
sizes = np.logspace(1, 4, 7, dtype=np.int)
for name, estimator in {"KRR": KernelRidge(kernel='rbf', alpha=0.1, gamma=10),
    "SVR": SVR(kernel='rbf', C=1e1, gamma=10)}.items():
    train_time = []
    test_time = []
    for train_test_size in sizes:
        t0 = time.time()
        estimator.fit(X[:train_test_size], y[:train_test_size])
        train_time.append(time.time() - t0)

        t0 = time.time()
        estimator.predict(X_plot[:1000])
        test_time.append(time.time() - t0)

    plt.plot(sizes, train_time, 'o-', color="r" if name == "SVR" else "g",}
4.11 Feature Union with Heterogeneous Data Sources

Datasets can often contain components of that require different feature extraction and processing pipelines. This scenario might occur when:

1. Your dataset consists of heterogeneous data types (e.g. raster images and text captions)
2. Your dataset is stored in a Pandas DataFrame and different columns require different processing pipelines.

This example demonstrates how to use `sklearn.feature_extraction.FeatureUnion` on a dataset containing different types of features. We use the 20-newsgroups dataset and compute standard bag-of-words features for the subject line and body in separate pipelines as well as ad hoc features on the body. We combine them (with weights) using a FeatureUnion and finally train a classifier on the combined set of features.

The choice of features is not particularly helpful, but serves to illustrate the technique.

```python
# Author: Matt Terry <matt.terry@gmail.com>
# License: BSD 3 clause
from __future__ import print_function
```

Total running time of the script: 0 minutes 51.033 seconds
**Class ItemSelector** (BaseEstimator, TransformerMixin):

```python
class ItemSelector(BaseEstimator, TransformerMixin):
    """For data grouped by feature, select subset of data at a provided key.

    The data is expected to be stored in a 2D data structure, where the first
    index is over features and the second is over samples. i.e.

    >>> len(data[key]) == n_samples

    Please note that this is the opposite convention to scikit-learn feature
    matrices (where the first index corresponds to sample).

    ItemSelector only requires that the collection implement getitem
    (data[key]). Examples include: a dict of lists, 2D numpy array, Pandas
    DataFrame, numpy record array, etc.

    >>> data = {'a': [1, 5, 2, 5, 2, 8],
               'b': [9, 4, 1, 4, 1, 3]}
    >>> ds = ItemSelector(key='a')
    >>> data['a'] == ds.transform(data)

    ItemSelector is not designed to handle data grouped by sample. (e.g. a
    list of dicts). If your data is structured this way, consider a
    transformer along the lines of `sklearn.feature_extraction.DictVectorizer`.

    Parameters
    ----------
    key : hashable, required
        The key corresponding to the desired value in a mappable.
    """

    def __init__(self, key):
        self.key = key

    def fit(self, x, y=None):
        return self

    def transform(self, data_dict):
        return data_dict[self.key]
```

**Class TextStats** (BaseEstimator, TransformerMixin):

```python
class TextStats(BaseEstimator, TransformerMixin):
    """Extract features from each document for DictVectorizer""

    def fit(self, x, y=None):
```
class SubjectBodyExtractor(BaseEstimator, TransformerMixin):
    ""
    Extract the subject & body from a usenet post in a single pass.
    ""
    def fit(self, x, y=None):
        return self
    def transform(self, posts):
        features = np.recarray(shape=(len(posts),),
                     dtype=[('subject', object), ('body', object)])
        for i, text in enumerate(posts):
            headers, _, bod = text.partition('


')
            bod = strip_newsgroup_footer(bod)
            bod = strip_newsgroup_quoting(bod)
            features['body'][i] = bod
            prefix = 'Subject:
            sub = ''
            for line in headers.split('
'):
                if line.startswith(prefix):
                    sub = line[len(prefix):]
                    break
            features['subject'][i] = sub
        return features

pipeline = Pipeline([  
    # Extract the subject & body
    ('subjectbody', SubjectBodyExtractor()),
    # Use FeatureUnion to combine the features from subject and body
    ('union', FeatureUnion(  
        transformer_list=[
            # Pipeline for pulling features from the post's subject line
            ('subject', Pipeline([  
                ('selector', ItemSelector(key='subject')),  
                ('tfidf', TfidfVectorizer(min_df=50)),
            ])),
            # Pipeline for standard bag-of-words model for body
            ('body_bow', Pipeline([  
                ('selector', ItemSelector(key='body')),  
                ('tfidf', TfidfVectorizer()),
                ('best', TruncatedSVD(n_components=50)),
            ])),
        ])
    ])

# Pipeline for pulling ad hoc features from post's body
('body_stats', Pipeline([  
    ('selector', ItemSelector(key='body')),  
    ('stats', TextStats()),  # returns a list of dicts  
    ('vect', DictVectorizer()),  # list of dicts -> feature matrix  
  ])),

# weight components in FeatureUnion
transformer_weights={  
  'subject': 0.8,  
  'body_bow': 0.5,  
  'body_stats': 1.0,  
},

# Use a SVC classifier on the combined features
('svc', SVC(kernel='linear')),

# limit the list of categories to make running this example faster.
categories = ['alt.atheism', 'talk.religion.misc']
train = fetch_20newsgroups(random_state=1,  
    subset='train',  
    categories=categories,  
)

test = fetch_20newsgroups(random_state=1,  
    subset='test',  
    categories=categories,  
)

pipeline.fit(train.data, train.target)
y = pipeline.predict(test.data)
print(classification_report(y, test.target))

Total running time of the script: ( 0 minutes 0.000 seconds)

## 4.12 Explicit feature map approximation for RBF kernels

An example illustrating the approximation of the feature map of an RBF kernel.

It shows how to use `RBFSampler` and `Nystroem` to approximate the feature map of an RBF kernel for classification with an SVM on the digits dataset. Results using a linear SVM in the original space, a linear SVM using the approximate mappings and using a kernelized SVM are compared. Timings and accuracy for varying amounts of Monte Carlo samplings (in the case of `RBFSampler`, which uses random Fourier features) and different sized subsets of the training set (for `Nystroem`) for the approximate mapping are shown.

Please note that the dataset here is not large enough to show the benefits of kernel approximation, as the exact SVM is still reasonably fast.

Sampling more dimensions clearly leads to better classification results, but comes at a greater cost. This means there is a tradeoff between runtime and accuracy, given by the parameter `n_components`. Note that solving the Linear SVM and also the approximate kernel SVM could be greatly accelerated by using stochastic gradient descent via `sklearn.linear_model.SGDClassifier`. This is not easily possible for the case of the kernelized SVM.
The second plot visualized the decision surfaces of the RBF kernel SVM and the linear SVM with approximate kernel maps. The plot shows decision surfaces of the classifiers projected onto the first two principal components of the data. This visualization should be taken with a grain of salt since it is just an interesting slice through the decision surface in 64 dimensions. In particular note that a datapoint (represented as a dot) does not necessarily be classified into the region it is lying in, since it will not lie on the plane that the first two principal components span.

The usage of \texttt{RBFSampler} and \texttt{Nystroem} is described in detail in \textit{Kernel Approximation}.

```python
print(__doc__)

# Author: Gael Varoquaux <gael dot varoquaux at normalesup dot org>
# Andreas Mueller <amueller@ais.uni-bonn.de>
# License: BSD 3 clause

# Standard scientific Python imports
import matplotlib.pyplot as plt
import numpy as np
```
from time import time

# Import datasets, classifiers and performance metrics
from sklearn import datasets, svm, pipeline
from sklearn.kernel_approximation import (RBFSampler,
                                           Nystroem)
from sklearn.decomposition import PCA

# The digits dataset
digits = datasets.load_digits(n_class=9)

# To apply an classifier on this data, we need to flatten the image, to
# turn the data in a (samples, feature) matrix:
n_samples = len(digits.data)
data = digits.data / 16.
data -= data.mean(axis=0)

# We learn the digits on the first half of the digits
data_train, targets_train = (data[:n_samples // 2],
                           digits.target[:n_samples // 2])

# Now predict the value of the digit on the second half:
data_test, targets_test = (data[n_samples // 2:],
                          digits.target[n_samples // 2:])
# data_test = scaler.transform(data_test)
# Create a classifier: a support vector classifier
kernel_svm = svm.SVC(gamma=.2)
linear_svm = svm.LinearSVC()

# create pipeline from kernel approximation
# and linear svm
feature_map_fourier = RBFSampler(gamma=.2, random_state=1)
feature_map_nystroem = Nystroem(gamma=.2, random_state=1)
fourier_approx_svm = pipeline.Pipeline(["feature_map", feature_map_fourier],
                                        ["svm", svm.LinearSVC()])
nystroem_approx_svm = pipeline.Pipeline(["feature_map", feature_map_nystroem],
                                        ["svm", svm.LinearSVC()])

# fit and predict using linear and kernel svm:
kernel_svm_time = time()
kernl_svm.fit(data_train, targets_train)
kernl_svm_score = kernel_svm.score(data_test, targets_test)
kernl_svm_time = time() - kernel_svm_time

linear_svm_time = time()
linear_svm.fit(data_train, targets_train)
linear_svm_score = linear_svm.score(data_test, targets_test)
linear_svm_time = time() - linear_svm_time

sample_sizes = 30 * np.arange(1, 10)
fourier_scores = []
nystroem_scores = []
fourier_times = []
nystroem_times = []
for D in sample_sizes:
    fourier_approx_svm.set_params(feature_map__n_components=D)
nystroem_approx_svm.set_params(feature_map__n_components=D)
start = time()
nystroem_approx_svm.fit(data_train, targets_train)
nystroem_times.append(time() - start)

start = time()
fourier_approx_svm.fit(data_train, targets_train)
fourier_times.append(time() - start)

fourier_score = fourier_approx_svm.score(data_test, targets_test)
nystroem_score = nystroem_approx_svm.score(data_test, targets_test)
nystroem_scores.append(nystroem_score)
fourier_scores.append(fourier_score)

# plot the results:
plt.figure(figsize=(8, 8))
accuracy = plt.subplot(211)
# second y axis for timeings
timescale = plt.subplot(212)

accuracy.plot(sample_sizes, nystroem_scores, label="Nystroem approx. kernel")
timescale.plot(sample_sizes, nystroem_times, '--', label='Nystroem approx. kernel')

accuracy.plot(sample_sizes, fourier_scores, label="Fourier approx. kernel")
timescale.plot(sample_sizes, fourier_times, '--', label='Fourier approx. kernel')

# horizontal lines for exact rbf and linear kernels:
accuracy.plot([sample_sizes[0], sample_sizes[-1]],
               [linear_svm_score, linear_svm_score], label="linear svm")
timescale.plot([sample_sizes[0], sample_sizes[-1]],
               [linear_svm_time, linear_svm_time], '--', label='linear svm')

accuracy.plot([sample_sizes[0], sample_sizes[-1]],
               [kernel_svm_score, kernel_svm_score], label="rbf svm")
timescale.plot([sample_sizes[0], sample_sizes[-1]],
               [kernel_svm_time, kernel_svm_time], '--', label='rbf svm')

# vertical line for dataset dimensionality = 64
accuracy.plot([64, 64], [0.7, 1], label="n_features")

# legends and labels
accuracy.set_title("Classification accuracy")
timescale.set_title("Training times")
accuracy.set_xlim(sample_sizes[0], sample_sizes[-1])
accuracy.set_xticks(())
accuracy.set_ylim(np.min(fourier_scores), 1)
timescale.set_xlim("Sampling steps = transformed feature dimension")
accuracy.set_xlabel("Classification accuracy")
timescale.set_ylabel("Training time in seconds")
accuracy.legend(loc='best')
timescale.legend(loc='best')

# visualize the decision surface, projected down to the first
# two principal components of the dataset
pca = PCA(n_components=8).fit(data_train)
X = pca.transform(data_train)

# Generate grid along first two principal components
multiples = np.arange(-2, 2, 0.1)
# steps along first component
first = multiples[:, np.newaxis] * pca.components_[0, :]
# steps along second component
second = multiples[:, np.newaxis] * pca.components_[1, :]
# combine
grid = first[:, np.newaxis, :] + second[:, np.newaxis, :]
flat_grid = grid.reshape(-1, data.shape[1])

# title for the plots
titles = ['SVC with rbf kernel',
    'SVC (linear kernel)\nwith Fourier rbf feature map\n' 'n_components=100',
    'SVC (linear kernel)\nwith Nystroem rbf feature map\n' 'n_components=100']

plt.tight_layout()
plt.figure(figsize=(12, 5))

# predict and plot
for i, clf in enumerate((kernel_svm, nystroem_approx_svm,
                          fourier_approx_svm)):
    # Plot the decision boundary. For that, we will assign a color to each
    # point in the mesh [x_min, x_max]x[y_min, y_max].
    plt.subplot(1, 3, i + 1)
    Z = clf.predict(flat_grid)
    # Put the result into a color plot
    Z = Z.reshape(grid.shape[:-1])
    plt.contourf(multiples, multiples, Z, cmap=plt.cm.Paired)
    plt.axis('off')

    # Plot also the training points
    plt.scatter(X[:, 0], X[:, 1], c=targets_train, cmap=plt.cm.Paired,
                edgecolors=(0, 0, 0))

    plt.title(titles[i])
plt.tight_layout()
plt.show()
EXAMPLES BASED ON REAL WORLD DATASETS

Applications to real world problems with some medium sized datasets or interactive user interface.

5.1 Outlier detection on a real data set

This example illustrates the need for robust covariance estimation on a real data set. It is useful both for outlier detection and for a better understanding of the data structure.

We selected two sets of two variables from the Boston housing data set as an illustration of what kind of analysis can be done with several outlier detection tools. For the purpose of visualization, we are working with two-dimensional examples, but one should be aware that things are not so trivial in high-dimension, as it will be pointed out.

In both examples below, the main result is that the empirical covariance estimate, as a non-robust one, is highly influenced by the heterogeneous structure of the observations. Although the robust covariance estimate is able to focus on the main mode of the data distribution, it sticks to the assumption that the data should be Gaussian distributed, yielding some biased estimation of the data structure, but yet accurate to some extent. The One-Class SVM does not assume any parametric form of the data distribution and can therefore model the complex shape of the data much better.

5.1.1 First example

The first example illustrates how robust covariance estimation can help concentrating on a relevant cluster when another one exists. Here, many observations are confounded into one and break down the empirical covariance estimation. Of course, some screening tools would have pointed out the presence of two clusters (Support Vector Machines, Gaussian Mixture Models, univariate outlier detection, . . . ). But had it been a high-dimensional example, none of these could be applied that easily.

5.1.2 Second example

The second example shows the ability of the Minimum Covariance Determinant robust estimator of covariance to concentrate on the main mode of the data distribution: the location seems to be well estimated, although the covariance is hard to estimate due to the banana-shaped distribution. Anyway, we can get rid of some outlying observations. The One-Class SVM is able to capture the real data structure, but the difficulty is to adjust its kernel bandwidth parameter so as to obtain a good compromise between the shape of the data scatter matrix and the risk of over-fitting the data.
# Outlier detection on a real data set (boston housing)

```python
import numpy as np
from sklearn.covariance import EllipticEnvelope
from sklearn.svm import OneClassSVM
import matplotlib.pyplot as plt
import matplotlib.font_manager
from sklearn.datasets import load_boston

# Get data
X1 = load_boston()['data'][:, [8, 10]]  # two clusters
X2 = load_boston()['data'][:, [5, 12]]  # "banana"-shaped

# Define "classifiers" to be used
classifiers = {
    "Empirical Covariance": EllipticEnvelope(support_fraction=1., contamination=0.261),
    "Robust Covariance (Minimum Covariance Determinant)": EllipticEnvelope(contamination=0.261),
    "OCSVM": OneClassSVM(nu=0.261, gamma=0.05)}

colors = ['m', 'g', 'b']
legend1 = {}
legend2 = {}
```

---

630 Chapter 5. Examples based on real world datasets
# Learn a frontier for outlier detection with several classifiers

```python
xx1, yy1 = np.meshgrid(np.linspace(-8, 28, 500), np.linspace(3, 40, 500))
xx2, yy2 = np.meshgrid(np.linspace(3, 10, 500), np.linspace(-5, 45, 500))

for i, (clf_name, clf) in enumerate(classifiers.items()):
    plt.figure(1)
    clf.fit(X1)
    Z1 = clf.decision_function(np.c_[xx1.ravel(), yy1.ravel()])
    Z1 = Z1.reshape(xx1.shape)
    legend1[clf_name] = plt.contour(xx1, yy1, Z1, levels=[0], linewidths=2, colors=colors[i])

plt.figure(2)
clf.fit(X2)
Z2 = clf.decision_function(np.c_[xx2.ravel(), yy2.ravel()])
Z2 = Z2.reshape(xx2.shape)
legend2[clf_name] = plt.contour(xx2, yy2, Z2, levels=[0], linewidths=2, colors=colors[i])

legend1_values_list = list(legend1.values())
legend1_keys_list = list(legend1.keys())

# Plot the results (= shape of the data points cloud)

plt.figure(1)  # two clusters
plt.title("Outlier detection on a real data set (boston housing)")
plt.scatter(X1[:, 0], X1[:, 1], color='black')
bbox_args = dict(boxstyle="round", fc="0.8")
arrows_args = dict(arrowstyle="->")
plt.annotate("several confounded points", xy=(24, 19),
            xycoords="data", textcoords="data",
            xytext=(13, 10), bbox=bbox_args, arrowprops=arrows_args)
plt.xlim((xx1.min(), xx1.max()))
plt.ylim((yy1.min(), yy1.max()))
plt.legend((legend1_values_list[0].collections[0],
            legend1_values_list[1].collections[0],
            legend1_values_list[2].collections[0],
            (legend1_keys_list[0], legend1_keys_list[1], legend1_keys_list[2]),
            loc="upper center",
            prop=matplotlib.font_manager.FontProperties(size=12))
plt.ylabel("accessibility to radial highways")
plt.xlabel("pupil-teacher ratio by town")

legend2_values_list = list(legend2.values())
legend2_keys_list = list(legend2.keys())

plt.figure(2)  # "banana" shape
plt.title("Outlier detection on a real data set (boston housing)")
plt.scatter(X2[:, 0], X2[:, 1], color='black')
plt.xlim((xx2.min(), xx2.max()))
plt.ylim((yy2.min(), yy2.max()))
plt.legend((legend2_values_list[0].collections[0],
            legend2_values_list[1].collections[0],
            legend2_values_list[2].collections[0],
            (legend2_keys_list[0], legend2_keys_list[1], legend2_keys_list[2]),
            loc="upper center",
            prop=matplotlib.font_manager.FontProperties(size=12))
plt.ylabel("% lower status of the population")
plt.xlabel("average number of rooms per dwelling")
```

5.1. Outlier detection on a real data set
5.2 Compressive sensing: tomography reconstruction with L1 prior (Lasso)

This example shows the reconstruction of an image from a set of parallel projections, acquired along different angles. Such a dataset is acquired in computed tomography (CT).

Without any prior information on the sample, the number of projections required to reconstruct the image is of the order of the linear size \( l \) of the image (in pixels). For simplicity we consider here a sparse image, where only pixels on the boundary of objects have a non-zero value. Such data could correspond for example to a cellular material. Note however that most images are sparse in a different basis, such as the Haar wavelets. Only \( 1/7 \) projections are acquired, therefore it is necessary to use prior information available on the sample (its sparsity): this is an example of compressive sensing.

The tomography projection operation is a linear transformation. In addition to the data-fidelity term corresponding to a linear regression, we penalize the L1 norm of the image to account for its sparsity. The resulting optimization problem is called the Lasso. We use the class `sklearn.linear_model.Lasso`, that uses the coordinate descent algorithm. Importantly, this implementation is more computationally efficient on a sparse matrix, than the projection operator used here.

The reconstruction with L1 penalization gives a result with zero error (all pixels are successfully labeled with 0 or 1), even if noise was added to the projections. In comparison, an L2 penalization (`sklearn.linear_model.Ridge`) produces a large number of labeling errors for the pixels. Important artifacts are observed on the reconstructed image, contrary to the L1 penalization. Note in particular the circular artifact separating the pixels in the corners, that have contributed to fewer projections than the central disk.

![Original image, L2 penalization, L1 penalization](image)

print(__doc__)

# Author: Emmanuelle Gouillart <emmanuelle.gouillart@nsup.org>
# License: BSD 3 clause

```python
import numpy as np
from scipy import sparse
from scipy import ndimage
from sklearn.linear_model import Lasso
from sklearn.linear_model import Ridge
```
```python
import matplotlib.pyplot as plt

def _weights(x, dx=1, orig=0):
x = np.ravel(x)
floor_x = np.floor((x - orig) / dx)
alpha = (x - orig - floor_x * dx) / dx
return np.hstack((floor_x, floor_x + 1)), np.hstack((1 - alpha, alpha))

def _generate_center_coordinates(l_x):
    X, Y = np.mgrid[:l_x, :l_x].astype(np.float64)
    center = l_x / 2.
    X += 0.5 - center
    Y += 0.5 - center
    return X, Y

def build_projection_operator(l_x, n_dir):
    """ Compute the tomography design matrix. """
    Parameters
    ----------
    l_x : int
        linear size of image array
    n_dir : int
        number of angles at which projections are acquired.
    Returns
    -------
    p : sparse matrix of shape (n_dir l_x, l_x**2)
        """
    X, Y = _generate_center_coordinates(l_x)
    angles = np.linspace(0, np.pi, n_dir, endpoint=False)
data_unravel_indices = np.arange(l_x ** 2)
data_unravel_indices = np.hstack((data_unravel_indices,
data_unravel_indices))
    for i, angle in enumerate(angles):
        Xrot = np.cos(angle) * X - np.sin(angle) * Y
        inds, w = _weights(Xrot, dx=1, orig=X.min())
        mask = np.logical_and(inds >= 0, inds < l_x)
        weights += list(w[mask])
        camera_inds += list(inds[mask] + i * l_x)
data_unravel_indices = np.hstack((data_unravel_indices,
data_unravel_indices))
    proj_operator = sparse.coo_matrix((weights, (camera_inds, data_unravel_indices)))
    return proj_operator

def generate_synthetic_data():
    """ Synthetic binary data """
    rs = np.random.RandomState(0)
n_pts = 36
    x, y = np.ogrid[0:1, 0:1]
    mask_outer = (x - 1 / 2.) ** 2 + (y - 1 / 2.) ** 2 < (1 / 2.) ** 2
    mask = np.zeros((1, 1))
```

5.2. Compressive sensing: tomography reconstruction with L1 prior (Lasso) 633
points = l * rs.rand(2, n_pts)
mask[(points[0]).astype(np.int), (points[1]).astype(np.int)] = 1
mask = ndimage.gaussian_filter(mask, sigma=l / n_pts)
res = np.logical_and(mask > mask.mean(), mask_outer)
return np.logical_xor(res, ndimage.binary_erosion(res))

# Generate synthetic images, and projections
l = 128
proj_operator = build_projection_operator(l, l / 7.)
data = generate_synthetic_data()
proj = proj_operator * data.ravel()[:, np.newaxis]
proj += 0.15 * np.random.randn(*proj.shape)

# Reconstruction with L2 (Ridge) penalization
rgr_ridge = Ridge(alpha=0.2)
rgr_ridge.fit(proj_operator, proj.ravel())
rec_l2 = rgr_ridge.coef_.reshape(l, l)

# Reconstruction with L1 (Lasso) penalization
# the best value of alpha was determined using cross validation
# with LassoCV
rgr_lasso = Lasso(alpha=0.001)
rgr_lasso.fit(proj_operator, proj.ravel())
rec_l1 = rgr_lasso.coef_.reshape(l, l)

plt.figure(figsize=(8, 3.3))
plt.subplot(131)
plt.imshow(data, cmap=plt.cm.gray, interpolation='nearest')
plt.axis('off')
plt.title('original image')
plt.subplot(132)
plt.imshow(rec_l2, cmap=plt.cm.gray, interpolation='nearest')
plt.title('L2 penalization')
plt.axis('off')
plt.subplot(133)
plt.imshow(rec_l1, cmap=plt.cm.gray, interpolation='nearest')
plt.title('L1 penalization')
plt.axis('off')

plt.subplots_adjust(hspace=0.01, wspace=0.01, top=1, bottom=0, left=0, right=1)
plt.show()

Total running time of the script: ( 0 minutes 8.899 seconds)

5.3 Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation

This is an example of applying sklearn.decomposition.NMF and sklearn.decomposition.LatentDirichletAllocation on a corpus of documents and extract additive models of the topic structure of the corpus. The output is a list of topics, each represented as a list of terms (weights are not shown).

Non-negative Matrix Factorization is applied with two different objective functions: the Frobenius norm, and the
generalized Kullback-Leibler divergence. The latter is equivalent to Probabilistic Latent Semantic Indexing.

The default parameters (n_samples / n_features / n_components) should make the example runnable in a couple of tens of seconds. You can try to increase the dimensions of the problem, but be aware that the time complexity is polynomial in NMF. In LDA, the time complexity is proportional to (n_samples * iterations).

Out:

<table>
<thead>
<tr>
<th>Loading dataset...</th>
<th>done in 1.496s.</th>
</tr>
</thead>
<tbody>
<tr>
<td>Extracting tf-idf features for NMF...</td>
<td>done in 0.404s.</td>
</tr>
<tr>
<td>Extracting tf features for LDA...</td>
<td>done in 0.400s.</td>
</tr>
</tbody>
</table>

Fitting the NMF model (Frobenius norm) with tf-idf features, n_samples=2000 and n_features=1000...
| done in 0.371s. |

Topics in NMF model (Frobenius norm):

- Topic #0: just people don think like know time good make way really say right ve want...
- Topic #1: windows use dos using window program os drivers application help software...
- Topic #2: god jesus bible faith christian christ christians does heaven sin believe...
- Topic #3: thanks know does mail advance hi info interested email anybody looking card...
- Topic #4: car cars tires miles 00 new engine insurance price condition oil power...
- Topic #5: edu soon com send university internet mit ftp mail cc pub article...
- Topic #6: file problem files format win sound ftp pub read save site help image...
- Topic #7: game team games year win play season players nhl runs goal hockey toronto...
- Topic #8: drive drives hard disk floppy software card mac computer power scsi...
- Topic #9: key chip clipper keys encryption government public use secure enforcement...

Fitting the NMF model (generalized Kullback-Leibler divergence) with tf-idf features, n_samples=2000 and n_features=1000...
| done in 2.230s. |

Topics in NMF model (generalized Kullback-Leibler divergence):

- Topic #0: people just like time don say really know way things make think right said...
- Topic #1: windows thanks using help need hi work know use looking mail software does...
- Topic #2: god does true read know say believe subject says religion mean question...
- Topic #3: thanks know like interested mail just want new send edu list does bike...
- Topic #4: time new 10 year sale old offer 20 16 15 great 30 weeks good test model...
- Topic #5: use number com government new university data states information talk phone...
- Topic #6: edu try file soon remember problem com program hope mike space article...

5.3. Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation 635
# Author: Olivier Grisel <olivier.grisel@ensta.org>
# Lars Buitinck
# Chyi-Kwei Yau <chyikwei.yau@gmail.com>
# License: BSD 3 clause

from __future__ import print_function
from time import time

from sklearn.feature_extraction.text import TfidfVectorizer, CountVectorizer
from sklearn.decomposition import NMF, LatentDirichletAllocation
from sklearn.datasets import fetch_20newsgroups

n_samples = 2000
n_features = 1000
n_components = 10
n_top_words = 20

def print_top_words(model, feature_names, n_top_words):
    for topic_idx, topic in enumerate(model.components_):
        message = "Topic #%d: " % topic_idx
        message += " ".join([feature_names[i]

for i in topic.argsort()[::-1][:-n_top_words - 1:-1])
    print(message)
print()

# Load the 20 newsgroups dataset and vectorize it. We use a few heuristics
# to filter out useless terms early on: the posts are stripped of headers,
# footers and quoted replies, and common English words, words occurring in
# only one document or in at least 95% of the documents are removed.

print("Loading dataset...")
t0 = time()
dataset = fetch_20newsgroups(shuffle=True, random_state=1,
remove=('headers', 'footers', 'quotes'))
data_samples = dataset.data[:n_samples]
print("done in %0.3fs." % (time() - t0))

# Use tf-idf features for NMF.
print("Extracting tf-idf features for NMF...")
tfidf_vectorizer = TfidfVectorizer(max_df=0.95, min_df=2,
max_features=n_features,
stop_words='english')
t0 = time()
tfidf = tfidf_vectorizer.fit_transform(data_samples)
print("done in %0.3fs." % (time() - t0))

# Use tf (raw term count) features for LDA.
print("Extracting tf features for LDA...")
tf_vectorizer = CountVectorizer(max_df=0.95, min_df=2,
max_features=n_features,
stop_words='english')
t0 = time()
tf = tf_vectorizer.fit_transform(data_samples)
print("done in %0.3fs." % (time() - t0))

# Fit the NMF model
print("Fitting the NMF model (Frobenius norm) with tf-idf features, ",
"n_samples=%d and n_features=%d..." % (n_samples, n_features))
t0 = time()
nmf = NMF(n_components=n_components, random_state=1,
alpha=.1, l1_ratio=.5).fit(tfidf)
print("done in %0.3fs." % (time() - t0))

print("\nTopics in NMF model (Frobenius norm):")
tfidf_feature_names = tfidf_vectorizer.get_feature_names()
print_top_words(nmf, tfidf_feature_names, n_top_words)

# Fit the NMF model
print("Fitting the NMF model (generalized Kullback-Leibler divergence) with ",
"tf-idf features, n_samples=%d and n_features=%d..." % (n_samples, n_features))
t0 = time()
nmf = NMF(n_components=n_components, random_state=1,
beta_loss='kullback-leibler', solver='mu', max_iter=1000, alpha=.1,
l1_ratio=.5).fit(tfidf)
print("done in %0.3fs." % (time() - t0))
print("\nTopics in NMF model (generalized Kullback-Leibler divergence):")
tfidf_feature_names = tfidf_vectorizer.get_feature_names()
print_top_words(nmf, tfidf_feature_names, n_top_words)

print("Fitting LDA models with tf features, 
"n_samples=%d and n_features=%d...

% (n_samples, n_features))
lda = LatentDirichletAllocation(n_components=n_components, max_iter=5,
    learning_method='online',
    learning_offset=50.,
    random_state=0)
t0 = time()
lda.fit(tf)
print("done in %0.3fs." % (time() - t0))

print("\nTopics in LDA model:")
tf_feature_names = tf_vectorizer.get_feature_names()
print_top_words(lda, tf_feature_names, n_top_words)

Total running time of the script: ( 0 minutes 15.444 seconds)

5.4 Faces recognition example using eigenfaces and SVMs

The dataset used in this example is a preprocessed excerpt of the “Labeled Faces in the Wild”, aka LFW:

Expected results for the top 5 most represented people in the dataset:

<table>
<thead>
<tr>
<th>Name</th>
<th>0.67</th>
<th>0.72</th>
<th>0.77</th>
<th>13</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ariel Sharon</td>
<td>0.75</td>
<td>0.78</td>
<td>0.76</td>
<td>60</td>
</tr>
<tr>
<td>Colin Powell</td>
<td>0.78</td>
<td>0.67</td>
<td>0.72</td>
<td>27</td>
</tr>
<tr>
<td>Donald Rumsfeld</td>
<td>0.86</td>
<td>0.86</td>
<td>0.86</td>
<td>146</td>
</tr>
<tr>
<td>George W Bush</td>
<td>0.76</td>
<td>0.76</td>
<td>0.76</td>
<td>25</td>
</tr>
<tr>
<td>Gerhard Schroeder</td>
<td>0.67</td>
<td>0.67</td>
<td>0.67</td>
<td>15</td>
</tr>
<tr>
<td>Hugo Chavez</td>
<td>0.81</td>
<td>0.69</td>
<td>0.75</td>
<td>36</td>
</tr>
<tr>
<td>Tony Blair</td>
<td>0.80</td>
<td>0.80</td>
<td>0.80</td>
<td>322</td>
</tr>
</tbody>
</table>

avg / total      | 0.80 | 0.80 | 0.80 | 322|
Out:

Total dataset size:
n_samples: 1288
n_features: 1850
n_classes: 7

Extracting the top 150 eigenfaces from 966 faces
done in 0.242s

Projecting the input data on the eigenfaces orthonormal basis
done in 0.027s

Fitting the classifier to the training set
done in 25.181s

Best estimator found by grid search:
SVC(C=1000.0, cache_size=200, class_weight='balanced', coef0=0.0,
    decision_function_shape='ovr', degree=3, gamma=0.001, kernel='rbf',
    max_iter=-1, probability=False, random_state=None, shrinking=True,
    tol=0.001, verbose=False)

Predicting people's names on the test set

done in 0.052s

<table>
<thead>
<tr>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ariel Sharon</td>
<td>0.53</td>
<td>0.77</td>
<td>0.62</td>
</tr>
<tr>
<td>Colin Powell</td>
<td>0.72</td>
<td>0.82</td>
<td>0.77</td>
</tr>
<tr>
<td>Donald Rumsfeld</td>
<td>0.84</td>
<td>0.78</td>
<td>0.81</td>
</tr>
<tr>
<td>George W Bush</td>
<td>0.91</td>
<td>0.88</td>
<td>0.90</td>
</tr>
<tr>
<td>Gerhard Schroeder</td>
<td>0.84</td>
<td>0.84</td>
<td>0.84</td>
</tr>
<tr>
<td>Hugo Chavez</td>
<td>0.90</td>
<td>0.60</td>
<td>0.72</td>
</tr>
<tr>
<td>Tony Blair</td>
<td>0.85</td>
<td>0.78</td>
<td>0.81</td>
</tr>
</tbody>
</table>

avg / total 0.84 0.83 0.83 322

[[ 10  1  1  1  0  0  0]
 [ 2  49  1  6  0  1  1]
 [ 5  0 21  1  0  0  0]
 [ 2 10 1  1  2  1  5]
 [ 0  2 1  0 21  0  1]
 [ 0  2 0  1  9  1  1]
 [ 0  4 1  3  0  0 28]]

default

classification_report

certification_matrix

import time
import logging
import matplotlib.pyplot as plt

from sklearn.model_selection import train_test_split
from sklearn.model_selection import GridSearchCV
from sklearn.datasets import fetch_lfw_people
from sklearn.metrics import classification_report
from sklearn.metrics import confusion_matrix
from sklearn.decomposition import PCA
from sklearn.svm import SVC

print(__doc__)

# Display progress logs on stdout
logging.basicConfig(level=logging.INFO, format='%(asctime)s %(message)s')

# Download the data, if not already on disk and load it as numpy arrays

lfw_people = fetch_lfw_people(min_faces_per_person=70, resize=0.4)

# introspect the images arrays to find the shapes (for plotting)
n_samples, h, w = lfw_people.images.shape

# for machine learning we use the 2 data directly (as relative pixel
# positions info is ignored by this model)
X = lfw_people.data
n_features = X.shape[1]

# the label to predict is the id of the person
y = lfw_people.target
target_names = lfw_people.target_names
n_classes = target_names.shape[0]

print("Total dataset size:")
print("n_samples: %d" % n_samples)
print("n_features: %d" % n_features)
print("n_classes: %d" % n_classes)

# Split into a training set and a test set using a stratified k fold
# split into a training and testing set
X_train, X_test, y_train, y_test = train_test_split(
    X, y, test_size=0.25, random_state=42)

# Compute a PCA (eigenfaces) on the face dataset (treated as unlabeled
# dataset): unsupervised feature extraction / dimensionality reduction
n_components = 150

print("Extracting the top %d eigenfaces from %d faces" % (n_components, X_train.shape[0]))
t0 = time()
pca = PCA(n_components=n_components, svd_solver='randomized',
               whiten=True).fit(X_train)
print("done in %0.3fs" % (time() - t0))
eigenfaces = pca.components_.reshape((n_components, h, w))

print("Projecting the input data on the eigenfaces orthonormal basis")
t0 = time()
X_train_pca = pca.transform(X_train)
X_test_pca = pca.transform(X_test)
print("done in %0.3fs" % (time() - t0))

# Train a SVM classification model
print("Fitting the classifier to the training set")
t0 = time()
param_grid = {'C': [1e3, 5e3, 1e4, 5e4, 1e5],
               'gamma': [0.0001, 0.0005, 0.001, 0.005, 0.01, 0.1],}
clf = GridSearchCV(SVC(kernel='rbf', class_weight='balanced'), param_grid)
clf = clf.fit(X_train_pca, y_train)
print("done in %0.3fs" % (time() - t0))
print("Best estimator found by grid search:")

5.4. Faces recognition example using eigenfaces and SVMs
print(clf.best_estimator_)

# #############################################################################
# Quantitative evaluation of the model quality on the test set
#
print("Predicting people's names on the test set")
t0 = time()
y_pred = clf.predict(X_test_pca)
print("done in %0.3fs" % (time() - t0))
print(classification_report(y_test, y_pred, target_names=target_names))
print(confusion_matrix(y_test, y_pred, labels=range(n_classes)))

# #############################################################################
# Qualitative evaluation of the predictions using matplotlib

def plot_gallery(images, titles, h, w, n_row=3, n_col=4):
    """Helper function to plot a gallery of portraits"
    plt.figure(figsize=(1.8 * n_col, 2.4 * n_row))
    plt.subplots_adjust(bottom=0, left=.01, right=.99, top=.90, hspace=.35)
    for i in range(n_row * n_col):
        plt.subplot(n_row, n_col, i + 1)
        plt.imshow(images[i].reshape((h, w)), cmap=plt.cm.gray)
        plt.title(titles[i], size=12)
        plt.xticks(())
        plt.yticks(())

    # plot the result of the prediction on a portion of the test set

def title(y_pred, y_test, target_names, i):
    pred_name = target_names[y_pred[i]].rsplit(' ', 1)[-1]
    true_name = target_names[y_test[i]].rsplit(' ', 1)[-1]
    return 'predicted: %s 
true: %s' % (pred_name, true_name)

prediction_titles = [title(y_pred, y_test, target_names, i)
    for i in range(y_pred.shape[0])]

plot_gallery(X_test, prediction_titles, h, w)

    # plot the gallery of the most significative eigenfaces

eigenface_titles = ["eigenface %d" % i for i in range(eigenfaces.shape[0])]
plot_gallery(eigenfaces, eigenface_titles, h, w)

plt.show()

Total running time of the script: ( 0 minutes 26.491 seconds)

5.5 Model Complexity Influence

Demonstrate how model complexity influences both prediction accuracy and computational performance.
The dataset is the Boston Housing dataset (resp. 20 Newsgroups) for regression (resp. classification).
For each class of models we make the model complexity vary through the choice of relevant model parameters and measure the influence on both computational performance (latency) and predictive power (MSE or Hamming Loss).
Out:

Benchmarking SGDClassifier(alpha=0.001, average=False, class_weight=None, epsilon=0.1, eta0=0.0, fit_intercept=True, l1_ratio=0.25, learning_rate='optimal', loss='modified_huber', max_iter=None, n_iter=None, n_jobs=1, penalty='elasticnet', power_t=0.5, random_state=None, shuffle=True, tol=0.001, verbose=0, warm_start=False)
Complexity: 4420 | Hamming Loss (Misclassification Ratio): 0.2456 | Pred. Time: 0.026152s

Benchmarking SGDClassifier(alpha=0.001, average=False, class_weight=None, epsilon=0.1, eta0=0.0, fit_intercept=True, l1_ratio=0.5, learning_rate='optimal', loss='modified_huber', max_iter=None, n_iter=None, n_jobs=1, penalty='elasticnet', power_t=0.5, random_state=None, shuffle=True, tol=0.001, verbose=0, warm_start=False)
Complexity: 1618 | Hamming Loss (Misclassification Ratio): 0.2934 | Pred. Time: 0.019198s

Benchmarking SGDClassifier(alpha=0.001, average=False, class_weight=None, epsilon=0.1, eta0=0.0, fit_intercept=True, l1_ratio=0.75, learning_rate='optimal', loss='modified_huber', max_iter=None, n_iter=None, n_jobs=1, penalty='elasticnet', power_t=0.5, random_state=None, shuffle=True, tol=0.001, verbose=0, warm_start=False)
Complexity: 889 | Hamming Loss (Misclassification Ratio): 0.3260 | Pred. Time: 0.015758s

Benchmarking SGDClassifier(alpha=0.001, average=False, class_weight=None, epsilon=0.1, eta0=0.0, fit_intercept=True, l1_ratio=0.9, learning_rate='optimal', loss='modified_huber', max_iter=None, n_iter=None, n_jobs=1, penalty='elasticnet', power_t=0.5, random_state=None, shuffle=True, tol=0.001, verbose=0, warm_start=False)
Complexity: 680 | Hamming Loss (Misclassification Ratio): 0.3406 | Pred. Time: 0.014225s

Benchmarking NuSVR(C=1000.0, cache_size=200, coef0=0.0, degree=3, gamma=3.0517578125e-05, kernel='rbf', max_iter=-1, nu=0.1, shrinking=True, tol=0.001,
Complexity: 69 | MSE: 31.8133 | Pred. Time: 0.000403s

Benchmarking NuSVR(C=1000.0, cache_size=200, coef0=0.0, degree=3, gamma=3.0517578125e-05, kernel='rbf', max_iter=-1, nu=0.25, shrinking=True, tol=0.001, verbose=False)
Complexity: 136 | MSE: 25.6140 | Pred. Time: 0.000707s

Benchmarking NuSVR(C=1000.0, cache_size=200, coef0=0.0, degree=3, gamma=3.0517578125e-05, kernel='rbf', max_iter=-1, nu=0.5, shrinking=True, tol=0.001, verbose=False)
Complexity: 243 | MSE: 22.3315 | Pred. Time: 0.001198s

Benchmarking NuSVR(C=1000.0, cache_size=200, coef0=0.0, degree=3, gamma=3.0517578125e-05, kernel='rbf', max_iter=-1, nu=0.75, shrinking=True, tol=0.001, verbose=False)
Complexity: 350 | MSE: 21.3679 | Pred. Time: 0.001682s

Benchmarking NuSVR(C=1000.0, cache_size=200, coef0=0.0, degree=3, gamma=3.0517578125e-05, kernel='rbf', max_iter=-1, nu=0.9, shrinking=True, tol=0.001, verbose=False)
Complexity: 404 | MSE: 21.0915 | Pred. Time: 0.001941s

Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=10, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 10 | MSE: 28.9793 | Pred. Time: 0.000145s

Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=50, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 50 | MSE: 8.3398 | Pred. Time: 0.000233s

Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=100, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 100 | MSE: 7.0096 | Pred. Time: 0.000322s

Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=100, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 100 | MSE: 7.0096 | Pred. Time: 0.000322s

5.5. Model Complexity Influence 645
print(__doc__)

# Author: Eustache Diemert <eustache@diemert.fr>
# License: BSD 3 clause

import time
import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.axes_grid1.parasite_axes import host_subplot
from mpl_toolkits.axisartist.axislines import Axes
from scipy.sparse.csr import csr_matrix
from sklearn import datasets
from sklearn.utils import shuffle
from sklearn.metrics import mean_squared_error
from sklearn.svm.classes import NuSVR
from sklearn.ensemble.gradient_boosting import GradientBoostingRegressor
from sklearn.linear_model.stochastic_gradient import SGDClassifier
from sklearn.metrics import hamming_loss

# #############################################################################
# Routines

# Initialize random generator
np.random.seed(0)

def generate_data(case, sparse=False):
    """Generate regression/classification data."""
    bunch = None
    if case == 'regression':
        bunch = datasets.load_boston()
    elif case == 'classification':
        bunch = datasets.load_iris()
    return bunch

# Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features='auto', max_leaf_nodes=2, min_impurity_decrease=0.0, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=200, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 200 | MSE: 6.1836 | Pred. Time: 0.000487s

Benchmarking GradientBoostingRegressor(alpha=0.9, criterion='friedman_mse', init=None, learning_rate=0.1, loss='ls', max_depth=3, max_features='auto', max_leaf_nodes=2, min_impurity_decrease=0.0, min_samples_leaf=1, min_samples_split=2, min_weight_fraction_leaf=0.0, n_estimators=500, n_iter_no_change=None, presort='auto', random_state=None, subsample=1.0, tol=0.0001, validation_fraction=0.1, verbose=0, warm_start=False)
Complexity: 500 | MSE: 6.3426 | Pred. Time: 0.001040s
bunch = datasets.fetch_20newsgroups_vectorized(subset='all')
X, y = shuffle(bunch.data, bunch.target)
offset = int(X.shape[0] * 0.8)
X_train, y_train = X[:offset], y[:offset]
X_test, y_test = X[offset:], y[offset:]
if sparse:
    X_train = csr_matrix(X_train)
    X_test = csr_matrix(X_test)
else:
    X_train = np.array(X_train)
    X_test = np.array(X_test)
y_test = np.array(y_test)
y_train = np.array(y_train)
data = {'X_train': X_train, 'X_test': X_test, 'y_train': y_train,
                  'y_test': y_test}
return data

def benchmark_influence(conf):
    ""
    Benchmark influence of :changing_param: on both MSE and latency.
    ""
    prediction_times = []
    prediction_powers = []
    complexities = []
    for param_value in conf['changing_param_values']:
        conf['tuned_params'][conf['changing_param']] = param_value
        estimator = conf['estimator'](**conf['tuned_params'])
        print("Benchmarking %s" % estimator)
        estimator.fit(conf['data']['X_train'], conf['data']['y_train'])
        conf['postfit_hook'](estimator)
        complexity = conf['complexity_computer'](estimator)
        complexities.append(complexity)
        start_time = time.time()
        for _ in range(conf['n_samples']):
            y_pred = estimator.predict(conf['data']['X_test'])
            elapsed_time = (time.time() - start_time) / float(conf['n_samples'])
            prediction_times.append(elapsed_time)
            pred_score = conf['prediction_performance_computer']({
                conf['data'][:'y_test'], y_pred})
            prediction_powers.append(pred_score)
        print("Complexity: %d | %s: %.4f | Pred. Time: %fs\n" % {
            complexity, conf['prediction_performance_label'],
            pred_score, elapsed_time})
    return prediction_powers, prediction_times, complexities

def plot_influence(conf, mse_values, prediction_times, complexities):
    ""
    Plot influence of model complexity on both accuracy and latency.
    ""
    plt.figure(figsize=(12, 6))
    host = host_subplot(111, axes_class=Axes)
    plt.subplots_adjust(right=0.75)
    par1 = host.twinx()
    host.set_xlabel('Model Complexity (%s)' % conf['complexity_label'])
    y1_label = conf['prediction_performance_label']
    y2_label = "Time (s)"

5.5. Model Complexity Influence
```python
def _count_nonzero_coefficients(estimator):
    a = estimator.coef_.toarray()
    return np.count_nonzero(a)

# Main code
regression_data = generate_data('regression')
classification_data = generate_data('classification', sparse=True)
configurations = [
    {'estimator': SGDClassifier,
     'tuned_params': {'penalty': 'elasticnet', 'alpha': 0.001, 'loss':
                     'modified_huber', 'fit_intercept': True, 'tol': 1e-3},
     'changing_param': 'l1_ratio',
     'changing_param_values': [0.25, 0.5, 0.75, 0.9],
     'complexity_label': 'non_zero coefficients',
     'complexity_computer': _count_nonzero_coefficients,
     'prediction_performance_computer': hamming_loss,
     'prediction_performance_label': 'Hamming Loss (Misclassification Ratio)',
     'postfit_hook': lambda x: x.sparsify(),
     'data': classification_data,
     'n_samples': 30},
    {'estimator': NuSVR,
     'tuned_params': {'C': 1e3, 'gamma': 2 ** -15},
     'changing_param': 'nu',
     'changing_param_values': [0.1, 0.25, 0.5, 0.75, 0.9],
     'complexity_label': 'n_support_vectors',
     'complexity_computer': lambda x: len(x.support_vectors_),
     'data': regression_data,
     'postfit_hook': lambda x: x,
     'prediction_performance_computer': mean_squared_error,
     'prediction_performance_label': 'MSE',
     'n_samples': 30},
    {'estimator': GradientBoostingRegressor,
     'tuned_params': {'loss': 'ls'},
     'changing_param': 'n_estimators',
     'changing_param_values': [10, 50, 100, 200, 500],
     'complexity_label': 'n_trees',
     'complexity_computer': lambda x: x.n_estimators,
     'data': regression_data,
     'postfit_hook': lambda x: x,
     'prediction_performance_computer': mean_squared_error,
     'prediction_performance_label': 'MSE',
     'n_samples': 30},
]
for conf in configurations:
    prediction_performances, prediction_times, complexities = \
```
5.6 Species distribution modeling

Modeling species’ geographic distributions is an important problem in conservation biology. In this example we model the geographic distribution of two south american mammals given past observations and 14 environmental variables. Since we have only positive examples (there are no unsuccessful observations), we cast this problem as a density estimation problem and use the OneClassSVM provided by the package sklearn.svm as our modeling tool. The dataset is provided by Phillips et. al. (2006). If available, the example uses basemap to plot the coast lines and national boundaries of South America.

The two species are:

- “Bradypus variegatus”, the Brown-throated Sloth.
- “Microryzomys minutus”, also known as the Forest Small Rice Rat, a rodent that lives in Peru, Colombia, Ecuador, Peru, and Venezuela.

5.6.1 References

Modeling distribution of species 'bradypus variegatus'
- fit OneClassSVM ... done.
- plot coastlines from coverage
- predict species distribution

Area under the ROC curve : 0.868443

Modeling distribution of species 'microroryzomys minutus'
- fit OneClassSVM ... done.
- plot coastlines from coverage
- predict species distribution

Area under the ROC curve : 0.993919

time elapsed: 6.58s
from __future__ import print_function
from time import time
import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets.base import Bunch
from sklearn.datasets import fetch_species_distributions
from sklearn.datasets.species_distributions import construct_grids
from sklearn import svm, metrics

# if basemap is available, we'll use it.
# otherwise, we'll improvise later...
try:
    from mpl_toolkits.basemap import Basemap
    basemap = True
except ImportError:
    basemap = False
print(__doc__)

def create_species_bunch(species_name, train, test, coverages, xgrid, ygrid):
    """Create a bunch with information about a particular organism
    This will use the test/train record arrays to extract the
data specific to the given species name.
    ""
    bunch = Bunch(name=' '.join(species_name.split('_')[:2]))
    specie_name = species_name.encode('ascii')
    points = dict(test=test, train=train)
    for label, pts in points.items():
        pts = pts[pts['species'] == specie_name]
        bunch['pts_' + label] = pts

        # determine coverage values for each of the training & testing points
        ix = np.searchsorted(xgrid, pts['dd long'])
        iy = np.searchsorted(ygrid, pts['dd lat'])
        bunch['cov_' + label] = coverages[:, -iy, ix].T

    return bunch

def plot_species_distribution(species=('bradypus_variegatus_0',
                                  'microryzomys_minutus_0')):
    """Plot the species distribution.
    ""
    if len(species) > 2:
        print("Note: when more than two species are provided,"
              " only the first two will be used")
t0 = time()

# Load the compressed data
data = fetch_species_distributions()

# Set up the data grid
xgrid, ygrid = construct_grids(data)

# The grid in x,y coordinates
X, Y = np.meshgrid(xgrid, ygrid[::-1])

# create a bunch for each species
BV_bunch = create_species_bunch(species[0],
data.train, data.test,
data.coverages, xgrid, ygrid)
MM_bunch = create_species_bunch(species[1],
data.train, data.test,
data.coverages, xgrid, ygrid)

# background points (grid coordinates) for evaluation
np.random.seed(13)
background_points = np.c_[np.random.randint(low=0, high=data.Ny, size=10000),
np.random.randint(low=0, high=data.Nx, size=10000)].T

# We'll make use of the fact that coverages[6] has measurements at all
# land points. This will help us decide between land and water.
land_reference = data.coverages[6]

# Fit, predict, and plot for each species.
for i, species in enumerate([BV_bunch, MM_bunch]):
    print("_" * 80)
    print("Modeling distribution of species '" + species.name + "'")
    # Standardize features
    mean = species.cov_train.mean(axis=0)
    std = species.cov_train.std(axis=0)
    train_cover_std = (species.cov_train - mean) / std
    # Fit OneClassSVM
    print(" - fit OneClassSVM ... " , end='')
    clf = svm.OneClassSVM(nu=0.1, kernel="rbf", gamma=0.5)
    clf.fit(train_cover_std)
    print("done.")
    # Plot map of South America
    plt.subplot(1, 2, i + 1)
    if basemap:
        print(" - plot coastlines using basemap")
        m = Basemap(projection='cyl', llcrnrlat=Y.min(),
                urcrnrlat=Y.max(), llcrnrlon=X.min(),
                urcrnrlon=X.max(), resolution='c')
        m.drawcoastlines()
        m.drawcountries()
    else:
        print(" - plot coastlines from coverage")
        plt.contour(X, Y, land_reference,
levels=[-9999], colors="k",
linestyles="solid")
plt.xticks([])
plt.yticks([])

print("- predict species distribution")

# Predict species distribution using the training data
Z = np.ones((data.Ny, data.Nx), dtype=np.float64)
# We'll predict only for the land points.
idx = np.where(land_reference > -9999)
coverages_land = data.coverages[:, idx[0], idx[1]].T
pred = clf.decision_function((coverages_land - mean) / std)[:, 0]
Z *= pred.min()
Z[idx[0], idx[1]] = pred

levels = np.linspace(Z.min(), Z.max(), 25)
Z[land_reference == -9999] = -9999

# plot contours of the prediction
plt.contourf(X, Y, Z, levels=levels, cmap=plt.cm.Reds)
plt.colorbar(format='%.2f')

# scatter training/testing points
plt.scatter(species.pts_train['dd long'], species.pts_train['dd lat'],
s=2 ** 2, c='black',
marker='^', label='train')
plt.scatter(species.pts_test['dd long'], species.pts_test['dd lat'],
s=2 ** 2, c='black',
marker='x', label='test')
plt.legend()
plt.title(species.name)
plt.axis('equal')

# Compute AUC with regards to background points
pred_background = Z[background_points[0], background_points[1]]
pred_test = clf.decision_function((species.cov_test - mean)
/ std)[:, 0]
scores = np.r_[pred_test, pred_background]
y = np.r_[np.ones(pred_test.shape), np.zeros(pred_background.shape)]
fpr, tpr, thresholds = metrics.roc_curve(y, scores)
roc_auc = metrics.auc(fpr, tpr)
plt.text(-35, -70, "AUC: %.3f % roc_auc, ha="right")

print("\nArea under the ROC curve : %.2f % roc_auc")

plot_species_distribution()
plt.show()
5.7 Wikipedia principal eigenvector

A classical way to assert the relative importance of vertices in a graph is to compute the principal eigenvector of the adjacency matrix so as to assign to each vertex the values of the components of the first eigenvector as a centrality score:

https://en.wikipedia.org/wiki/Eigenvector_centrality

On the graph of webpages and links those values are called the PageRank scores by Google.

The goal of this example is to analyze the graph of links inside wikipedia articles to rank articles by relative importance according to this eigenvector centrality.

The traditional way to compute the principal eigenvector is to use the power iteration method:

https://en.wikipedia.org/wiki/Power_iteration

Here the computation is achieved thanks to Martinsson’s Randomized SVD algorithm implemented in the scikit.

The graph data is fetched from the DBpedia dumps. DBpedia is an extraction of the latent structured data of the Wikipedia content.

```python
from __future__ import print_function
from bz2 import BZ2File
import os
from datetime import datetime
from pprint import pprint
from time import time
import numpy as np
from scipy import sparse
from sklearn.decomposition import randomized_svd
from sklearn.externals.joblib import Memory
from sklearn.externals.six.moves.urllib.request import urlopen
from sklearn.externals.six import iteritems

print(__doc__)

# Where to download the data, if not already on disk
redirects_url = "http://downloads.dbpedia.org/3.5.1/en/redirects_en.nt.bz2"
redirects_filename = redirects_url.rsplit("/", 1)[1]

page_links_url = "http://downloads.dbpedia.org/3.5.1/en/page_links_en.nt.bz2"
page_links_filename = page_links_url.rsplit("/", 1)[1]

resources = [
    (redirects_url, redirects_filename),
    (page_links_url, page_links_filename),
]

for url, filename in resources:
    if not os.path.exists(filename):
```

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print("Downloading data from '%s', please wait...") % url
open = urlopen(url)
open(filename, 'wb').write(opener.read())
print()

# Loading the redirect files
memory = Memory(cachedir=".")

def index(redirects, index_map, k):
    """Find the index of an article name after redirect resolution""
    k = redirects.get(k, k)
    return index_map.setdefault(k, len(index_map))

DBPEDIA_RESOURCE_PREFIX_LEN = len("http://dbpedia.org/resource/")
SHORTNAME_SLICE = slice(DBPEDIA_RESOURCE_PREFIX_LEN + 1, -1)

def short_name(nt_uri):
    """Remove the < and > URI markers and the common URI prefix""
    return nt_uri[SHORTNAME_SLICE]

def get_redirects(redirects_filename):
    """Parse the redirections and build a transitively closed map out of it""
    redirects = {}
    print("Parsing the NT redirect file")
    for l, line in enumerate(BZ2File(redirects_filename)):
        split = line.split()
        if len(split) != 4:
            print("ignoring malformed line: " + line)
            continue
        redirects[short_name(split[0])] = short_name(split[2])
        if l % 1000000 == 0:
            print("[\%s line: %08d] " % (datetime.now().isoformat(), l))

    # compute the transitive closure
    print("Computing the transitive closure of the redirect relation")
    for l, source in enumerate(redirects.keys()):
        transitive_target = None
        target = redirects[source]
        seen = set([source])
        while True:
            transitive_target = target
            target = redirects.get(target)
            if target is None or target in seen:
                break
            seen.add(target)
            redirects[source] = transitive_target
            if l % 1000000 == 0:
                print("[\%s line: %08d] " % (datetime.now().isoformat(), l))

        return redirects

5.7. Wikipedia principal eigenvector
def get_adjacency_matrix(redirects_filename, page_links_filename, limit=None):
    """Extract the adjacency graph as a scipy sparse matrix

    Redirects are resolved first.

    Returns X, the scipy sparse adjacency matrix, redirects as python dict from article names to article names and index_map a python dict from article names to python int (article indexes).
    ""

    print("Computing the redirect map")
    redirects = get_redirects(redirects_filename)

    print("Computing the integer index map")
    index_map = dict()
    links = list()
    for i, line in enumerate(BZ2File(page_links_filename)):
        split = line.split()
        if len(split) != 4:
            print("ignoring malformed line: " + line)
            continue
        i = index(redirects, index_map, short_name(split[0]))
        j = index(redirects, index_map, short_name(split[2]))
        links.append((i, j))
        if i % 1000000 == 0:
            print("[%s] line: %08d" % (datetime.now().isoformat(), i))
        if limit is not None and i >= limit - 1:
            break

    print("Computing the adjacency matrix")
    X = sparse.lil_matrix((len(index_map), len(index_map)), dtype=np.float32)
    for i, j in links:
        X[i, j] = 1.0
    del links
    print("Converting to CSR representation")
    X = X.tocsr()
    print("CSR conversion done")
    return X, redirects, index_map

# stop after 5M links to make it possible to work in RAM
X, redirects, index_map = get_adjacency_matrix(
    redirects_filename, page_links_filename, limit=5000000)
names = dict((i, name) for name, i in iteritems(index_map))

print("Computing the principal singular vectors using randomized_svd")
t0 = time()
U, s, V = randomized_svd(X, 5, n_iter=3)
print("done in \$0.3fs\n\% (time() - t0))

# print the names of the wikipedia related strongest components of the
# principal singular vector which should be similar to the highest eigenvector
print("Top wikipedia pages according to principal singular vectors")
pprint([names[i] for i in np.abs(U.T[0]).argsort()[-10:]])
```python
pprint([names[i] for i in np.abs(V[0]).argsort()[-10:]])

def centrality_scores(X, alpha=0.85, max_iter=100, tol=1e-10):
    '''Power iteration computation of the principal eigenvector

    This method is also known as Google PageRank and the implementation
    is based on the one from the NetworkX project (BSD licensed too)
    with copyrights by:
    Aric Hagberg <hagberg@lanl.gov>
    Dan Schult <dschult@colgate.edu>
    Pieter Swart <swart@lanl.gov>
    '''
    n = X.shape[0]
    X = X.copy()
    incoming_counts = np.asarray(X.sum(axis=1)).ravel()
    print("Normalizing the graph")
    for i in incoming_counts.nonzero()[0]:
        X.data[X.indptr[i]:X.indptr[i + 1]] *= 1.0 / incoming_counts[i]
    dangle = np.asarray(np.where(X.sum(axis=1) == 0, 1.0 / n, 0)).ravel()
    scores = np.ones(n, dtype=np.float32) / n  # initial guess
    for i in range(max_iter):
        print("power iteration #\%d" % i)
        prev_scores = scores
        scores = (alpha * (scores * X + np.dot(dangle, prev_scores))
                  + (1 - alpha) * prev_scores.sum() / n)
        # check convergence: normalized l_inf norm
        scores_max = np.abs(scores).max()
        if scores_max == 0.0:
            scores_max = 1.0
        err = np.abs(scores - prev_scores).max() / scores_max
        print("error: \%0.6f" % err)
        if err < n * tol:
            return scores

    return scores

print("Computing principal eigenvector score using a power iteration method")
t0 = time()
scores = centrality_scores(X, max_iter=100, tol=1e-10)
print("done in \%0.3fs" % (time() - t0))
pprint([names[i] for i in np.abs(scores).argsort()[-10:]])
```

Total running time of the script: (0 minutes 0.000 seconds)

### 5.8 Visualizing the stock market structure

This example employs several unsupervised learning techniques to extract the stock market structure from variations in historical quotes.

The quantity that we use is the daily variation in quote price: quotes that are linked tend to cofluctuate during a day.

#### 5.8. Visualizing the stock market structure
5.8.1 Learning a graph structure

We use sparse inverse covariance estimation to find which quotes are correlated conditionally on the others. Specifically, sparse inverse covariance gives us a graph, that is a list of connection. For each symbol, the symbols that it is connected too are those useful to explain its fluctuations.

5.8.2 Clustering

We use clustering to group together quotes that behave similarly. Here, amongst the various clustering techniques available in the scikit-learn, we use Affinity Propagation as it does not enforce equal-size clusters, and it can choose automatically the number of clusters from the data.

Note that this gives us a different indication than the graph, as the graph reflects conditional relations between variables, while the clustering reflects marginal properties: variables clustered together can be considered as having a similar impact at the level of the full stock market.

5.8.3 Embedding in 2D space

For visualization purposes, we need to lay out the different symbols on a 2D canvas. For this we use Manifold learning techniques to retrieve 2D embedding.

5.8.4 Visualization

The output of the 3 models are combined in a 2D graph where nodes represents the stocks and edges the:

- cluster labels are used to define the color of the nodes
- the sparse covariance model is used to display the strength of the edges
- the 2D embedding is used to position the nodes in the plan

This example has a fair amount of visualization-related code, as visualization is crucial here to display the graph. One of the challenge is to position the labels minimizing overlap. For this we use an heuristic based on the direction of the nearest neighbor along each axis.
Out:

Cluster 1: Apple, Amazon, Yahoo
Cluster 2: Cisco, Dell, Microsoft, Texas Instruments, HP, IBM, SAP
Cluster 3: American express
Cluster 4: Boeing
Cluster 5: Cablevision
Cluster 6: ConocoPhillips, Chevron, Total, Valero Energy, Exxon
Cluster 7: Comcast, Marriott, AIG, Bank of America, CVS, DuPont de Nemours, Ford, General Electrics, Goldman Sachs, Home Depot, JPMorgan Chase, McDonald's, 3M, Pfizer, Ryder, Wells Fargo, Wal-Mart
Cluster 8: Navistar
Cluster 9: General Dynamics, Northrop Grumman, Raytheon
Cluster 10: GlaxoSmithKline, Novartis, Sanofi-Aventis
Cluster 11: Kellogg, Coca Cola, Pepsi
Cluster 12: Colgate-Palmolive, Kimberly-Clark, Procter Gamble
Cluster 13: Canon, Caterpillar, Honda, Sony, Toyota, Unilever, Xerox
Cluster 14: Time Warner

5.8. Visualizing the stock market structure
from __future__ import print_function

# Author: Gael Varoquaux gael.varoquaux@normalesup.org
# License: BSD 3 clause

import sys
from datetime import datetime

import numpy as np
import matplotlib.pyplot as plt
from matplotlib.collections import LineCollection
from six.moves.urllib.request import urlopen
from six.moves.urllib.parse import urlencode
from sklearn import cluster, covariance, manifold

print(__doc__)

def retry(f, n_attempts=3):
    """Wrapper function to retry function calls in case of exceptions""
    def wrapper(*args, **kwargs):
        for i in range(n_attempts):
            try:
                return f(*args, **kwargs)
            except Exception:
                if i == n_attempts - 1:
                    raise
        return wrapper

def quotes_historical_google(symbol, start_date, end_date):
    """Get the historical data from Google finance.

    Parameters
    ---------
    symbol : str
        Ticker symbol to query for, for example `"DELL"`.
    start_date : datetime.datetime
        Start date.
    end_date : datetime.datetime
        End date.

    Returns
    -------
    X : array
        The columns are `"date"` -- date, `"open"`, `"high"`, `"low"`, `"close"` and `"volume"` of type float.
    """
    params = {
        'q': symbol,
        'startdate': start_date.strftime('%Y-%m-%d'),
        'enddate': end_date.strftime('%Y-%m-%d'),
        'output': 'csv',
    }
    url = 'https://finance.google.com/finance/historical?' + urlencode(params)
    response = urlopen(url)
    dtype = {
        'names': ['date', 'open', 'high', 'low', 'close', 'volume'],
    }
`formats`: ['object', 'f4', 'f4', 'f4', 'f4', 'f4']

```python
converters = {
    0: lambda s: datetime.strptime(s.decode(), '%d-%b-%y').date()
}
data = np.genfromtxt(response, delimiter=',', skip_header=1,
dtype=dtype, converters=converters,
missing_values='-', filling_values=-1)

min_date = min(data['date']) if len(data) else datetime.min.date()
max_date = max(data['date']) if len(data) else datetime.max.date()
start_end_diff = (end_date - start_date).days
min_max_diff = (max_date - min_date).days

data_is_fine = {
    start_date <= min_date <= end_date and
    start_date <= max_date <= end_date and
    start_end_diff - 7 <= min_max_diff <= start_end_diff
}

if not data_is_fine:
    message = ('Data looks wrong for symbol {}, url {}
             - start_date: {}, end_date: {}
             - min_date: {}, max_date: {}
             - start_end_diff: {}, min_max_diff: {}'.format(
                   symbol, url,
                   start_date, end_date,
                   min_date, max_date,
                   start_end_diff, min_max_diff))
    raise RuntimeError(message)

return data
```

# #############################################################################

# Retrieve the data from Internet

# Choose a time period reasonably calm (not too long ago so that we get
# high-tech firms, and before the 2008 crash)
start_date = datetime(2003, 1, 1).date()
end_date = datetime(2008, 1, 1).date()

symbol_dict = {
    'NYSE:TOT': 'Total',
    'NYSE:XOM': 'Exxon',
    'NYSE:CVX': 'Chevron',
    'NYSE:COP': 'ConocoPhillips',
    'NYSE:VLO': 'Valero Energy',
    'NASDAQ:MSFT': 'Microsoft',
    'NYSE:IBM': 'IBM',
    'NYSE:TWX': 'Time Warner',
    'NASDAQ:CMCSA': 'Comcast',
    'NYSE:CVC': 'Cablevision',
    'NASDAQ:YHOO': 'Yahoo',
    'NASDAQ:DELL': 'Dell',
    'NYSE:HPQ': 'HP',
    'NASDAQ:AMZN': 'Amazon',
    'NYSE:TM': 'Toyota',
    'NYSE:CAJ': 'Canon',
    'NYSE:SNE': 'Sony',
    'NYSE:F': 'Ford',
    'NYSE:HMC': 'Honda',
    'NYSE:NAV': 'Navistar',
}

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symbols, names = np.array(sorted(symbol_dict.items())).T

# retry is used because quotes_historical_google can temporarily fail
# for various reasons (e.g. empty result from Google API).
quotes = []
for symbol in symbols:
    print('Fetching quote history for %r' % symbol, file=sys.stderr)
    quotes.append(retry(quotes_historical_google)(
        symbol, start_date, end_date))

close_prices = np.vstack([q['close'] for q in quotes])
open_prices = np.vstack([q['open'] for q in quotes])

# The daily variations of the quotes are what carry most information
variation = close_prices - open_prices

# Learn a graphical structure from the correlations
edge_model = covariance.GraphLassoCV()

# standardize the time series: using correlations rather than covariance
# is more efficient for structure recovery
X = variation.copy().T
X /= X.std(axis=0)
edge_model.fit(X)

# Cluster using affinity propagation
_, labels = cluster.affinity_propagation(edge_model.covariance_)
n_labels = labels.max()

for i in range(n_labels + 1):
    print('Cluster %i: %s' % ((i + 1), ', '.join(names[labels == i])))

# Find a low-dimension embedding for visualization: find the best position of
# the nodes (the stocks) on a 2D plane

# We use a dense eigen_solver to achieve reproducibility (arpack is
# initiated with random vectors that we don't control). In addition, we
# use a large number of neighbors to capture the large-scale structure.
node_position_model = manifold.LocallyLinearEmbedding(
    n_components=2, eigen_solver='dense', n_neighbors=6)

embedding = node_position_model.fit_transform(X.T).T

# Visualization
plt.figure(1, facecolor='w', figsize=(10, 8))
plt.clf()
ax = plt.axes([0., 0., 1., 1.])
plt.axis('off')

# Display a graph of the partial correlations
partial_correlations = edge_model.precision_.copy()
d = 1 / np.sqrt(np.diag(partial_correlations))
partial_correlations *= d
partial_correlations *= d[:, np.newaxis]
non_zero = (np.abs(np.triu(partial_correlations, k=1)) > 0.02)

# Plot the nodes using the coordinates of our embedding
plt.scatter(embedding[0], embedding[1], s=100 * d ** 2, c=labels,
cmap=plt.cm.spectral)

# Plot the edges
start_idx, end_idx = np.where(non_zero)
segments = [[embedding[:, start], embedding[:, stop]]
    for start, stop in zip(start_idx, end_idx)]
values = np.abs(partial_correlations[non_zero])
lc = LineCollection(segments,
zorder=0, cmap=plt.cm.hot_r,
norm=plt.Normalize(0, .7 * values.max()))
lc.set_array(values)
lc.set_linewidths(15 * values)
ax.add_collection(lc)

# Add a label to each node. The challenge here is that we want to
# position the labels to avoid overlap with other labels
for index, (name, label, (x, y)) in enumerate(zip(names, labels, embedding.T)):
    dx = x - embedding[0]
dx[index] = 1
dy = y - embedding[1]
dy[index] = 1
this_dx = dx[np.argmin(np.abs(dy))]
this_dy = dy[np.argmin(np.abs(dx))]
if this_dx > 0:
    horizontalalignment = 'left'
x = x + .002
else:
    horizontalalignment = 'right'
x = x - .002
if this_dy > 0:
    verticalalignment = 'bottom'
y = y + .002
else:
    verticalalignment = 'top'
y = y - .002
plt.text(x, y, name, size=10,
          horizontalalignment=horizontalalignment,
          verticalalignment=verticalalignment,
          bbox=dict(facecolor='w',
                     edgecolor=plt.cm.spectral(label / float(n_labels)),
                     alpha=.6))
plt.xlim(embedding[0].min() - .15 * embedding[0].ptp(),
        embedding[0].max() + .10 * embedding[0].ptp(),)
plt.ylim(embedding[1].min() - .03 * embedding[1].ptp(),
        embedding[1].max() + .03 * embedding[1].ptp())

plt.show()

Total running time of the script: ( 0 minutes 27.808 seconds)

5.9 Libsvm GUI

A simple graphical frontend for Libsvm mainly intended for didactic purposes. You can create data points by point
and click and visualize the decision region induced by different kernels and parameter settings.

To create positive examples click the left mouse button; to create negative examples click the right button.
If all examples are from the same class, it uses a one-class SVM.

from __future__ import division, print_function

print(__doc__)

# Author: Peter Prettenhoer <peter.prettenhofer@gmail.com>
import matplotlib
matplotlib.use('TkAgg')

from matplotlib.backends.backend_tkagg import FigureCanvasTkAgg
from matplotlib.backends.backend_tkagg import NavigationToolbar2TkAgg
from matplotlib.figure import Figure
from matplotlib.contour import ContourSet

try:
    import tkinter as Tk
except ImportError:
    # Backward compat for Python 2
    import Tkinter as Tk

import sys
import numpy as np

from sklearn import svm
from sklearn.datasets import dump_svmlight_file
from sklearn.externals.six.moves import xrange

y_min, y_max = -50, 50
x_min, x_max = -50, 50

class Model(object):
    """The Model which hold the data. It implements the observable in the observer pattern and notifies the registered observers on change event. """

    def __init__(self):
        self.observers = []
        self.surface = None
        self.data = []
        self.cls = None
        self.surface_type = 0

    def changed(self, event):
        """Notify the observers. """
        for observer in self.observers:
            observer.update(event, self)

    def add_observer(self, observer):
        """Register an observer. """
        self.observers.append(observer)

    def set_surface(self, surface):
        self.surface = surface

    def dump_svmlight_file(self, file):
        data = np.array(self.data)
        X = data[:, 0:2]
        y = data[:, 2]
        dump_svmlight_file(X, y, file)
```python
class Controller(object):
    def __init__(self, model):
        self.model = model
        self.kernel = Tk.IntVar()
        self.surface_type = Tk.IntVar()
        # Whether or not a model has been fitted
        self.fitted = False

    def fit(self):
        print("fit the model")
        train = np.array(self.model.data)
        X = train[:, 0:2]
        y = train[:, 2]

        C = float(self.complexity.get())
        gamma = float(self.gamma.get())
        coef0 = float(self.coef0.get())
        degree = int(self.degree.get())
        kernel_map = {0: "linear", 1: "rbf", 2: "poly"}

        if len(np.unique(y)) == 1:
            clf = svm.OneClassSVM(kernel=kernel_map[self.kernel.get()],
                                 gamma=gamma, coef0=coef0, degree=degree)
            clf.fit(X)
        else:
            clf = svm.SVC(kernel=kernel_map[self.kernel.get()], C=C,
                          gamma=gamma, coef0=coef0, degree=degree)
            clf.fit(X, y)

        if hasattr(clf, 'score'):
            print("Accuracy:", clf.score(X, y) * 100)
        X1, X2, Z = self.decision_surface(clf)
        self.model.clf = clf
        self.model.set_surface((X1, X2, Z))
        self.model.surface_type = self.surface_type.get()
        self.fitted = True
        self.model.changed("surface")

    def decision_surface(self, cls):
        delta = 1
        x = np.arange(x_min, x_max + delta, delta)
        y = np.arange(y_min, y_max + delta, delta)
        X1, X2 = np.meshgrid(x, y)
        Z = cls.decision_function(np.c_[X1.ravel(), X2.ravel()])
        Z = Z.reshape(X1.shape)
        return X1, X2, Z

    def clear_data(self):
        self.model.data = []
        self.fitted = False
        self.model.changed("clear")

    def add_example(self, x, y, label):
        self.model.data.append((x, y, label))
        self.model.changed("example_added")

        # update decision surface if already fitted.
        self.refit()
```

---

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def refit(self):
    """Refit the model if already fitted. """
    if self.fitted:
        self.fit()

class View(object):
    """Test docstring. """
    def __init__(self, root, controller):
        f = Figure()
        ax = f.add_subplot(111)
        ax.set_xticks([])
        ax.set_yticks([])
        ax.set_xlim((x_min, x_max))
        ax.set_ylim((y_min, y_max))
        canvas = FigureCanvasTkAgg(f, master=root)
        canvas.show()
        canvas.get_tk_widget().pack(side=Tk.TOP, fill=Tk.BOTH, expand=1)
        toolbar1 = NavigationToolbar2TkAgg(canvas, root)
        toolbar1.update()
        self.canvas = canvas
        self.controller = controller
        self.f = f
        self.ax = ax
        self.ax.set_ticks([])
        self.controllbar = ControllBar(root, controller)
    
    def plot_kernels(self):
        self.ax.text(-50, -60, "Linear: $u^T v$")
        self.ax.text(-20, -60, "RBF: $\exp (-\gamma \| u-v \|^2)$")
        self.ax.text(10, -60, "Poly: $(\gamma \, u^T v + r)^d$"")
    
    def onclick(self, event):
        if event.xdata and event.ydata:
            if event.button == 1:
                self.controller.add_example(event.xdata, event.ydata, 1)
            elif event.button == 3:
                self.controller.add_example(event.xdata, event.ydata, -1)
        
    def update_example(self, model, idx):
        x, y, l = model.data[idx]
        if l == 1:
            color = 'w'
        elif l == -1:
            color = 'k'
        self.ax.plot([x], [y], "$s" % color, scalex=0.0, scaley=0.0)
    
    def update(self, event, model):
        if event == "examples_loaded":
            for i in xrange(len(model.data)):
                self.update_example(model, i)
        if event == "example_added":
            self.f
def
self.update_example(model, -1)

if event == "clear":
    self.ax.clear()
    self.ax.set_xticks([])
    self.ax.set_yticks([])
    self.contours = []
    self.c_labels = None
    self.plot_kernels()

if event == "surface":
    self.remove_surface()
    self.plot_support_vectors(model.clf.support_vectors_)
    self.plot_decision_surface(model.surface, model.surface_type)
    self.canvas.draw()

def remove_surface(self):
    """Remove old decision surface."""
    if len(self.contours) > 0:
        for contour in self.contours:
            if isinstance(contour, ContourSet):
                for lineset in contour.collections:
                    lineset.remove()
            else:
                contour.remove()
        self.contours = []

def plot_support_vectors(self, support_vectors):
    """Plot the support vectors by placing circles over the corresponding data points and adds the circle collection to the contours list."""
    cs = self.ax.scatter(support_vectors[:, 0], support_vectors[:, 1], s=80, edgecolors="k", facecolors="none")
    self.contours.append(cs)

def plot_decision_surface(self, surface, type):
    X1, X2, Z = surface
    if type == 0:
        levels = [-1.0, 0.0, 1.0]
        linestyles = ['dashed', 'solid', 'dashed']
        colors = 'k'
        self.contours.append(self.ax.contour(X1, X2, Z, levels, colors=colors, linestyles=linestyles))
    elif type == 1:
        cmap=matplotlib.cm.bone,
        origin='lower', alpha=0.85))
        self.contours.append(self.ax.contourf(X1, X2, Z, [0.0], colors='k', linestyles=['solid']))
    else:
        raise ValueError("surface type unknown")

class ControllBar(object):
    def __init__(self, root, controller):
        fm = Tk.Frame(root)
kernel_group = Tk.Frame(fm)
Tk.Radiobutton(kernel_group, text="Linear", variable=controller.kernel,
    value=0, command=controller.refit).pack(anchor=Tk.W)
Tk.Radiobutton(kernel_group, text="RBF", variable=controller.kernel,
    value=1, command=controller.refit).pack(anchort=Tk.W)
Tk.Radiobutton(kernel_group, text="Poly", variable=controller.kernel,
    value=2, command=controller.refit).pack(anchort=Tk.W)
kernl_group.pack(side=Tk.LEFT)

valbox = Tk.Frame(fm)
controller.complexity = Tk.StringVar()
controller.complexity.set("1.0")
c = Tk.Frame(valbox)
Tk.Label(c, text="C:", anchor="e", width=7).pack(side=Tk.LEFT)
Tk.Entry(c, width=6, textvariable=controller.complexity).pack(side=Tk.LEFT)
c.pack()

controller.gamma = Tk.StringVar()
controller.gamma.set("0.01")
g = Tk.Frame(valbox)
Tk.Label(g, text="gamma:", anchor="e", width=7).pack(side=Tk.LEFT)
Tk.Entry(g, width=6, textvariable=controller.gamma).pack(side=Tk.LEFT)
g.pack()

controller.degree = Tk.StringVar()
controller.degree.set("3")
d = Tk.Frame(valbox)
Tk.Label(d, text="degree:", anchor="e", width=7).pack(side=Tk.LEFT)
Tk.Entry(d, width=6, textvariable=controller.degree).pack(side=Tk.LEFT)
d.pack()

controller.coef0 = Tk.StringVar()
controller.coef0.set("0")
r = Tk.Frame(valbox)
Tk.Label(r, text="coef0:", anchor="e", width=7).pack(side=Tk.LEFT)
Tk.Entry(r, width=6, textvariable=controller.coef0).pack(side=Tk.LEFT)
r.pack()

valbox.pack(side=Tk.LEFT)

cmap_group = Tk.Frame(fm)
Tk.Radiobutton(cmap_group, text="Hyperplanes",
    variable=controller.surface_type, value=0,
    command=controller.refit).pack(anchort=Tk.W)
Tk.Radiobutton(cmap_group, text="Surface",
    variable=controller.surface_type, value=1,
    command=controller.refit).pack(anchort=Tk.W)
cmap_group.pack(side=Tk.LEFT)

train_button = Tk.Button(fm, text='Fit', width=5,
    command=controller.fit)
train_button.pack()
fm.pack(side=Tk.LEFT)
Tk.Button(fm, text='Clear', width=5,
    command=controller.clear_data).pack(side=Tk.LEFT)
def get_parser():
    from optparse import OptionParser
    op = OptionParser()
    op.add_option("--output",
                  action="store", type="str", dest="output",
                  help="Path where to dump data."
    )
    return op

def main(argv):
    op = get_parser()
    opts, args = op.parse_args(argv[1:])
    root = Tk.Tk()
    model = Model()
    controller = Controller(model)
    root.wm_title("Scikit-learn Libsvm GUI")
    view = View(root, controller)
    model.add_observer(view)
    Tk.mainloop()
    if opts.output:
        model.dump_svmlight_file(opts.output)

if __name__ == "__main__":
    main(sys.argv)

Total running time of the script: ( 0 minutes 0.000 seconds)

5.10 Prediction Latency

This is an example showing the prediction latency of various scikit-learn estimators.

The goal is to measure the latency one can expect when doing predictions either in bulk or atomic (i.e. one by one) mode.

The plots represent the distribution of the prediction latency as a boxplot.
Out:

5.10. Prediction Latency
Benchmarking SGDRegressor(alpha=0.01, average=False, epsilon=0.1, eta0=0.01,
fit_intercept=True, l1_ratio=0.25, learning_rate='invscaling',
loss='squared_loss', max_iter=None, n_iter=None,
penalty='elasticnet', power_t=0.25, random_state=None, shuffle=True,
tol=0.0001, verbose=0, warm_start=False)
Benchmarking RandomForestRegressor(bootstrap=True, criterion='mse', max_depth=None,
max_features='auto', max_leaf_nodes=None,
min_impurity_decrease=0.0, min_impurity_split=None,
min_samples_leaf=1, min_samples_split=2,
min_weight_fraction_leaf=0.0, n_estimators=10, n_jobs=1,
oob_score=False, random_state=None, verbose=0, warm_start=False)
Benchmarking SVR(C=1.0, cache_size=200, coef0=0.0, degree=3, epsilon=0.1, gamma='auto
˓→',
kernel='rbf', max_iter=-1, shrinking=True, tol=0.001, verbose=False)

import numpy as np
import matplotlib.pyplot as plt
from sklearn.preprocessing import StandardScaler
from sklearn.model_selection import train_test_split
from scipy.stats import scoreatpercentile
from sklearn.datasets.samples_generator import make_regression
from sklearn.ensemble.forest import RandomForestRegressor
from sklearn.linear_model.ridge import Ridge
from sklearn.linear_model.stochastic_gradient import SGDRegressor
from sklearn.svm.classes import SVR
from sklearn.utils import shuffle

def _not_in_sphinx():
    # Hack to detect whether we are running by the sphinx builder
    return '__file__' in globals()

def atomic_benchmark_estimator(estimator, X_test, verbose=False):
    """Measure runtime prediction of each instance."""
    n_instances = X_test.shape[0]
    runtimes = np.zeros(n_instances, dtype=np.float)
    for i in range(n_instances):
        instance = X_test[[i], :]
        start = time.time()
estimator.predict(instance)
runtimes[i] = time.time() - start
if verbose:
    print("atomic_benchmark runtimes:", min(runtimes), scoreatpercentile(runtimes, 50), max(runtimes))
return runtimes

def bulk_benchmark_estimator(estimator, X_test, n_bulk_repeats, verbose):
    """Measure runtime prediction of the whole input."""
    n_instances = X_test.shape[0]
    runtimes = np.zeros(n_bulk_repeats, dtype=np.float)
    for i in range(n_bulk_repeats):
        start = time.time()
        estimator.predict(X_test)
        runtimes[i] = time.time() - start
    runtimes = np.array(list(map(lambda x: x / float(n_instances), runtimes)))
    if verbose:
        print("bulk_benchmark runtimes:", min(runtimes), scoreatpercentile(runtimes, 50), max(runtimes))
    return runtimes

def benchmark_estimator(estimator, X_test, n_bulk_repeats=30, verbose=False):
    """Measure runtimes of prediction in both atomic and bulk mode.
    Parameters
    ----------
estimator : already trained estimator supporting `predict`
X_test : test input
n_bulk_repeats : how many times to repeat when evaluating bulk mode
    Returns
    -------
atomic_runtimes, bulk_runtimes : a pair of `np.array` which contain the runtimes in seconds.
    """
    atomic_runtimes = atomic_benchmark_estimator(estimator, X_test, verbose)
    bulk_runtimes = bulk_benchmark_estimator(estimator, X_test, n_bulk_repeats, verbose)
    return atomic_runtimes, bulk_runtimes

def generate_dataset(n_train, n_test, n_features, noise=0.1, verbose=False):
    """Generate a regression dataset with the given parameters."""
    if verbose:
        print("generating dataset...")
    X, y, coef = make_regression(n_samples=n_train + n_test,
                        n_features=n_features, noise=noise, coef=True)
    random_seed = 13
    X_train, X_test, y_train, y_test = train_test_split(X, y, train_size=n_train, random_state=random_state)
    X_train, y_train = shuffle(X_train, y_train, random_state=random_state)

5.10. Prediction Latency
```python
X_scaler = StandardScaler()
X_train = X_scaler.fit_transform(X_train)
X_test = X_scaler.transform(X_test)

y_scaler = StandardScaler()
y_train = y_scaler.fit_transform(y_train[:, None])[:, 0]
y_test = y_scaler.transform(y_test[:, None])[:, 0]

gc.collect()
if verbose:
    print("ok")
return X_train, y_train, X_test, y_test

def boxplot_runtimes(runtimes, pred_type, configuration):
    ""
    Plot a new 'Figure' with boxplots of prediction runtimes.
    ""
    runtimes : list of 'np.array' of latencies in micro-seconds
    cls_names : list of estimator class names that generated the runtimes
    pred_type : 'bulk' or 'atomic'
    ""
    fig, ax1 = plt.subplots(figsize=(10, 6))
    bp = plt.boxplot(runtimes, )
    cls_infos = ['%s
    estimator_conf['complexity_computer']()
    estimator_conf['instance'],
    estimator_conf['complexity_label'])
    estimator_conf in configuration['estimators']])
    plt.setp(ax1, xticklabels=cls_infos)
    plt.setp(bp['boxes'], color='black')
    plt.setp(bp['whiskers'], color='black')
    plt.setp(bp['fliers'], color='red', marker='+')
    ax1.yaxis.grid(True, linestyle='-', which='major', color='lightgrey',
                   alpha=0.5)
    ax1.set_axisbelow(True)
    ax1.set_title('Prediction Time per Instance - %s, %d feats.' % (
        pred_type.capitalize(),
        configuration['n_features']))
    ax1.set_ylabel('Prediction Time (us)')
    plt.show()

def benchmark(configuration):
    """Run the whole Benchmark."""
    X_train, y_train, X_test, y_test = generate_dataset(
        configuration['n_train'], configuration['n_test'],
        configuration['n_features'])
    stats = {}
```
for estimator_conf in configuration['estimators']:
    print("Benchmarking", estimator_conf['instance'])
    estimator_conf['instance'].fit(X_train, y_train)
    gc.collect()
    a, b = benchmark_estimator(estimator_conf['instance'], X_test)
    stats[estimator_conf['name']] = {'atomic': a, 'bulk': b}

cls_names = [estimator_conf['name'] for estimator_conf in configuration['estimators']]
runtimes = [1e6 * stats[clf_name]['atomic'] for clf_name in cls_names]
boxplot_runtimes(runtimes, 'atomic', configuration)

runtimes = [1e6 * stats[clf_name]['bulk'] for clf_name in cls_names]
boxplot_runtimes(runtimes, 'bulk (%d)' % configuration['n_test'], configuration)

def n_feature_influence(estimators, n_train, n_test, n_features, percentile):
    """
    Estimate influence of the number of features on prediction time.
   "
    Parameters
    ----------
    estimators : dict of (name (str), estimator) to benchmark
    n_train : number of training instances (int)
    n_test : number of testing instances (int)
    n_features : list of feature-space dimensionality to test (int)
    percentile : percentile at which to measure the speed (int [0-100])
    Returns:
    -------
    percentiles : dict(estimator_name, dict(n_features, percentile_perf_in_us))
    """
    percentiles = defaultdict(defaultdict)
    for n in n_features:
        print("benchmarking with %d features" % n)
        X_train, y_train, X_test, y_test = generate_dataset(n_train, n_test, n)
        for cls_name, estimator in estimators.items():
            estimator.fit(X_train, y_train)
            gc.collect()
            runtimes = bulk_benchmark_estimator(estimator, X_test, 30, False)
            percentiles[cls_name][n] = 1e6 * scoreatpercentile(runtimes, percentile)
    return percentiles

def plot_n_features_influence(percentiles, percentile):
    fig, ax1 = plt.subplots(figsize=(10, 6))
    colors = ['r', 'g', 'b']
    for i, cls_name in enumerate(percentiles.keys()):
        x = np.array(sorted([n for n in percentiles[cls_name].keys()]))
        y = np.array([percentiles[cls_name][n] for n in x])
        ax1.plot(x, y, color=colors[i], )
    ax1.yaxis.grid(True, linestyle='-', which='major', color='lightgrey', alpha=0.5)

5.10. Prediction Latency
```
fig, ax = plt.subplots(figsize=(10, 6))
colors = ['r', 'g', 'b']
cls_infos = ['n(%d %s)' % (estimator_conf['name'],
                          estimator_conf['complexity_computer'](
                          estimator_conf['instance']),
                          estimator_conf['complexity_label']) for
                          estimator_conf in configuration['estimators']]
cls_values = [throughputs[estimator_conf['name']] for estimator_conf in
                          configuration['estimators']]
plt.bar(range(len(throughputs)), cls_values, width=0.5, color=colors)
ax.set_xticks(np.linspace(0.25, len(throughputs) - 0.75, len(throughputs)))
ax.set_xticklabels(cls_infos, fontsize=10)
ymax = max(cls_values) * 1.2
ax.set_ylim((0, ymax))
ax.set_ylabel('Throughput (predictions/sec)')
ax.set_title('Prediction Throughput for different estimators (%d ' % configuration['n_features'])
plt.show()
```
5.11 Out-of-core classification of text documents

This is an example showing how scikit-learn can be used for classification using an out-of-core approach: learning from data that doesn’t fit into main memory. We make use of an online classifier, i.e., one that supports the partial_fit method, that will be fed with batches of examples. To guarantee that the features space remains the same over time we leverage a HashingVectorizer that will project each example into the same feature space. This is especially useful in the case of text classification where new features (words) may appear in each batch.

The dataset used in this example is Reuters-21578 as provided by the UCI ML repository. It will be automatically downloaded and uncompressed on first run.

The plot represents the learning curve of the classifier: the evolution of classification accuracy over the course of the mini-batches. Accuracy is measured on the first 1000 samples, held out as a validation set.

To limit the memory consumption, we queue examples up to a fixed amount before feeding them to the learner.

Total running time of the script: 0 minutes 3.093 seconds
from glob import glob
import itertools
import os.path
import re
import tarfile
import time
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import rcParams
from sklearn.externals.six.moves import html_parser
from sklearn.externals.six.moves.urllib.request import urlretrieve
from sklearn.datasets import get_data_home
from sklearn.feature_extraction.text import HashingVectorizer
from sklearn.linear_model import SGDClassifier
from sklearn.linear_model import PassiveAggressiveClassifier
from sklearn.linear_model import Perceptron
from sklearn.naive_bayes import MultinomialNB

def _not_in_sphinx():
    # Hack to detect whether we are running by the sphinx builder
    return '__file__' in globals()

5.11.1 Reuters Dataset related routines

class ReutersParser(html_parser.HTMLParser):
    """Utility class to parse a SGML file and yield documents one at a time.""

    def __init__(self, encoding='latin-1'):
        html_parser.HTMLParser.__init__(self)
        self._reset()
        self.encoding = encoding

    def handle_starttag(self, tag, attrs):
        method = 'start_' + tag
        getattr(self, method, lambda x: None)(attrs)

    def handle_endtag(self, tag):
        method = 'end_' + tag
        getattr(self, method, lambda: None)()

    def _reset(self):
        self.in_title = 0
        self.in_body = 0
        self.in_topics = 0
        self.in_topic_d = 0
        self.title = ""
        self.body = ""
        self.topics = []
        self.topic_d = ""

    def parse(self, fd):
        self.docs = []
        for chunk in fd:
```python
self.feed(chunk.decode(self.encoding))
for doc in self.docs:
    yield doc
self.docs = []
self.close()

def handle_data(self, data):
    if self.in_body:
        self.body += data
    elif self.in_title:
        self.title += data
    elif self.in_topic_d:
        self.topic_d += data

def start_reuters(self, attributes):
    pass

def end_reuters(self):
    self.body = re.sub(r'\s+', r' ', self.body)
    self.docs.append({'title': self.title,
                      'body': self.body,
                      'topics': self.topics})
    self._reset()

def start_title(self, attributes):
    self.in_title = 1

def end_title(self):
    self.in_title = 0

def start_body(self, attributes):
    self.in_body = 1

def end_body(self):
    self.in_body = 0

def start_topics(self, attributes):
    self.in_topics = 1

def end_topics(self):
    self.in_topics = 0

def start_d(self, attributes):
    self.in_topic_d = 1

def end_d(self):
    self.in_topic_d = 0
    self.topics.append(self.topic_d)
    self.topic_d = ""

def stream_reuters_documents(data_path=None):
    """Iterate over documents of the Reuters dataset.

    The Reuters archive will automatically be downloaded and uncompressed if
    the `data_path` directory does not exist.

    Documents are represented as dictionaries with 'body' (str),
    ""
```

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Create the vectorizer and limit the number of features to a reasonable maximum

```python
vectorizer = HashingVectorizer(decode_error='ignore', n_features=2 ** 18, alternate_sign=False)
```

# Iterator over parsed Reuters SGML files.
data_stream = stream_reuters_documents()

# We learn a binary classification between the "acq" class and all the others.
# "acq" was chosen as it is more or less evenly distributed in the Reuters
# files. For other datasets, one should take care of creating a test set with
# a realistic portion of positive instances.
all_classes = np.array([0, 1])
positive_class = 'acq'

# Here are some classifiers that support the 'partial_fit' method
partial_fit_classifiers = {
    'SGD': SGDClassifier(max_iter=5),
    'Perceptron': Perceptron(tol=1e-3),
    'NB Multinomial': MultinomialNB(alpha=0.01),
    'Passive-Aggressive': PassiveAggressiveClassifier(tol=1e-3),
}

def get_minibatch(doc_iter, size, pos_class=positive_class):
    """Extract a minibatch of examples, return a tuple X_text, y.
    Note: size is before excluding invalid docs with no topics assigned.
    """
    data = [(u'{title}

{body}'.format(**doc), pos_class in doc['topics'])
        for doc in itertools.islice(doc_iter, size)
        if doc['topics']]
    if not len(data):
        return np.asarray([], dtype=int), np.asarray([], dtype=int)
    X_text, y = zip(*data)
    return X_text, np.asarray(y, dtype=int)

def iter_minibatches(doc_iter, minibatch_size):
    """Generator of minibatches."""
    X_text, y = get_minibatch(doc_iter, minibatch_size)
    while len(X_text):
        yield X_text, y
        X_text, y = get_minibatch(doc_iter, minibatch_size)

# test data statistics

def progress(cls_name, stats):
    """Report progress information, return a string."""
    duration = time.time() - stats['t0']
    s = "%.2fs classifier : %t % %s
    s += "%.2f train docs %.2f positive) % %s
    s += "%.2f test docs %.2f positive) % %s
    s += "%.2f accuracy : %.3f % %s
    s += "in %.2f docs/s) % (duration, stats['n_train'] / duration)
    return s
cls_stats = {}

for cls_name in partial_fit_classifiers:
    stats = {'n_train': 0, 'n_train_pos': 0,
             'accuracy': 0.0, 'accuracy_history': [(0, 0)],
             'runtime_history': [(0, 0)], 'total_fit_time': 0.0}
    cls_stats[cls_name] = stats

get_minibatch(data_stream, n_test_documents)

# Discard test set
# We will feed the classifier with mini-batches of 1000 documents; this means
# we have at most 1000 docs in memory at any time. The smaller the document
# batch, the bigger the relative overhead of the partial fit methods.
minibatch_size = 1000

# Create the data_stream that parses Reuters SGML files and iterates on
# documents as a stream.
minibatch_iterators = iter_minibatches(data_stream, minibatch_size)
total_vect_time = 0.0

# Main loop : iterate on mini-batches of examples
for i, (X_train_text, y_train) in enumerate(minibatch_iterators):
    tick = time.time()
    X_train = vectorizer.transform(X_train_text)
    total_vect_time += time.time() - tick

    for cls_name, cls in partial_fit_classifiers.items():
        tick = time.time()
        # update estimator with examples in the current mini-batch
        cls.partial_fit(X_train, y_train, classes=all_classes)

        tick = time.time()
        # accumulate test accuracy stats
        cls_stats[cls_name]['accuracy'] = cls.score(X_test, y_test)
        cls_stats[cls_name]['prediction_time'] = time.time() - tick
        acc_history = (cls_stats[cls_name]['accuracy'],
                       cls_stats[cls_name]['n_train'])
        cls_stats[cls_name]['accuracy_history'].append(acc_history)
        run_history = (cls_stats[cls_name]['accuracy'],
                       total_vect_time + cls_stats[cls_name]['total_fit_time'])
        cls_stats[cls_name]['runtime_history'].append(run_history)

        if i % 3 == 0:
            print(progress(cls_name, cls_stats[cls_name]))

        if i % 3 == 0:
            print('
')

Out:

Test set is 878 documents (108 positive)
SGD classifier: 962 train docs (132 positive) 878 documents 0.901 in 1.44s (667 docs/s)
Perceptron classifier: 962 train docs (132 positive) 878 documents 0.912 in 1.45s (665 docs/s)
NB Multinomial classifier : 962 train docs ( 132 positive) 878
→ test docs ( 108 positive) accuracy: 0.877 in 1.48s ( 648 docs/s)
Passive-Aggressive classifier : 962 train docs ( 132 positive) 878
→ test docs ( 108 positive) accuracy: 0.938 in 1.49s ( 646 docs/s)

SGD classifier : 3911 train docs ( 517 positive) 878
→ test docs ( 108 positive) accuracy: 0.946 in 4.22s ( 926 docs/s)
Perceptron classifier : 3911 train docs ( 517 positive) 878
→ test docs ( 108 positive) accuracy: 0.941 in 4.22s ( 925 docs/s)

SGD classifier : 6821 train docs ( 891 positive) 878
→ test docs ( 108 positive) accuracy: 0.952 in 6.98s ( 977 docs/s)
Perceptron classifier : 6821 train docs ( 891 positive) 878
→ test docs ( 108 positive) accuracy: 0.929 in 6.98s ( 977 docs/s)

SGD classifier : 9759 train docs ( 1276 positive) 878
→ test docs ( 108 positive) accuracy: 0.952 in 9.77s ( 998 docs/s)
Perceptron classifier : 9759 train docs ( 1276 positive) 878
→ test docs ( 108 positive) accuracy: 0.929 in 9.77s ( 998 docs/s)

SGD classifier : 11680 train docs ( 1499 positive) 878
→ test docs ( 108 positive) accuracy: 0.957 in 12.27s ( 951 docs/s)
Perceptron classifier : 11680 train docs ( 1499 positive) 878
→ test docs ( 108 positive) accuracy: 0.923 in 12.28s ( 951 docs/s)

SGD classifier : 14625 train docs ( 1865 positive) 878
→ test docs ( 108 positive) accuracy: 0.965 in 15.10s ( 968 docs/s)
Perceptron classifier : 14625 train docs ( 1865 positive) 878
→ test docs ( 108 positive) accuracy: 0.956 in 15.11s ( 968 docs/s)

SGD classifier : 17360 train docs ( 2179 positive) 878
→ test docs ( 108 positive) accuracy: 0.967 in 17.74s ( 978 docs/s)

5.11. Out-of-core classification of text documents
Perceptron classifier: 17360 train docs (2179 positive) 878 test docs (108 positive) accuracy: 0.948 in 17.74s (978 docs/s)

NB Multinomial classifier: 17360 train docs (2179 positive) 878 test docs (108 positive) accuracy: 0.932 in 17.78s (976 docs/s)

Passive-Aggressive classifier: 17360 train docs (2179 positive) 878 test docs (108 positive) accuracy: 0.956 in 17.78s (976 docs/s)

5.11.3 Plot results

```python
def plot_accuracy(x, y, x_legend):
    """Plot accuracy as a function of x."""
    x = np.array(x)
    y = np.array(y)
    plt.title('Classification accuracy as a function of ' + x_legend)
    plt.xlabel('Accuracy')
    plt.ylabel('x
    plt.grid(True)
    plt.plot(x, y)

    plt.legend(cls_names, loc='best')

plot_accuracy(x, y, x_legend)

# Plot accuracy evolution
plot_accuracy(x, y, x_legend)

plot_accuracy(x, y, x_legend)

# Plot fitting times
plot_accuracy(x, y, x_legend)
```

Chapter 5. Examples based on real world datasets
def autolabel(rectangles):
    """attach some text vi autolabel on rectangles."""
    for rect in rectangles:
        height = rect.get_height()
        ax.text(rect.get_x() + rect.get_width() / 2.,
                1.05 * height, '{:.4f}'.format(height),
                ha='center', va='bottom')

ax = plt.subplot(111)
rectangles = plt.bar(range(len(cls_names)), cls_runtime, width=0.5,
color=bar_colors)
ax.set_xticks(np.linspace(0.25, len(cls_names) - 0.75, len(cls_names)))
ax.set_xticklabels(cls_names, fontsize=8)
plt.setp(plt.xticks()[1], rotation=30)
ymax = max(cls_runtime) * 1.2
ax.set_ylim((0, ymax))
ax.set_ylabel('runtime (s)')
ax.set_title('Training Times')
autolabel(rectangles)
plt.show()
Chapter 5. Examples based on real world datasets
5.11. Out-of-core classification of text documents

Total running time of the script: ( 0 minutes 19.349 seconds)
Examples concerning the `sklearn.cluster.bicluster` module.

### 6.1 A demo of the Spectral Co-Clustering algorithm

This example demonstrates how to generate a dataset and bicluster it using the Spectral Co-Clustering algorithm. The dataset is generated using the `make_biclusters` function, which creates a matrix of small values and implants biclusters with large values. The rows and columns are then shuffled and passed to the Spectral Co-Clustering algorithm. Rearranging the shuffled matrix to make biclusters contiguous shows how accurately the algorithm found the biclusters.
From scikit-learn user guide, Release 0.20.dev0

import numpy as np
from matplotlib import pyplot as plt
from sklearn.datasets import make_biclusters
from sklearn.datasets import samples_generator as sg
from sklearn.cluster.bicluster import SpectralCoclustering
from sklearn.metrics import consensus_score

data, rows, columns = make_biclusters(
    shape=(300, 300), n_clusters=5, noise=5,
    shuffle=False, random_state=0)

plt.matshow(data, cmap=plt.cm.Blues)
plt.title("Original dataset")

data, row_idx, col_idx = sg._shuffle(data, random_state=0)
plt.matshow(data, cmap=plt.cm.Blues)
plt.title("Shuffled dataset")

model = SpectralCoclustering(n_clusters=5, random_state=0)
model.fit(data)
score = consensus_score(model.biclusters_,
                        (rows[:, row_idx], columns[:, col_idx]))

print("consensus score: {:.3f}".format(score))
fit_data = data[np.argsort(model.row_labels_)]
fit_data = fit_data[:, np.argsort(model.column_labels_)]

Out:

consensus score: 1.000
6.2 A demo of the Spectral Biclustering algorithm

This example demonstrates how to generate a checkerboard dataset and bicluster it using the Spectral Biclustering algorithm.

The data is generated with the `make_checkerboard` function, then shuffled and passed to the Spectral Biclustering algorithm. The rows and columns of the shuffled matrix are rearranged to show the biclusters found by the algorithm.

The outer product of the row and column label vectors shows a representation of the checkerboard structure.
Out:

```
consensus score: 1.0
```

```python
print(__doc__)

# Author: Kemal Eren <kemal@kemaleren.com>
# License: BSD 3 clause

import numpy as np
from matplotlib import pyplot as plt
from sklearn.datasets import make_checkerboard
from sklearn.datasets import samples_generator as sg
from sklearn.cluster.bicluster import SpectralBiclustering
from sklearn.metrics import consensus_score

n_clusters = (4, 3)
data, rows, columns = make_checkerboard(
    shape=(300, 300), n_clusters=n_clusters, noise=10,
    shuffle=False, random_state=0)
```
plt.matshow(data, cmap=plt.cm.Blues)
plt.title("Original dataset")

data, row_idx, col_idx = sg._shuffle(data, random_state=0)
plt.matshow(data, cmap=plt.cm.Blues)
plt.title("Shuffled dataset")

model = SpectralBiclustering(n_clusters=n_clusters, method='log',
random_state=0)
model.fit(data)
score = consensus_score(model.biclusters_,
(rows[:, row_idx], columns[:, col_idx]))

print("consensus score: {:.1f}".format(score))

fit_data = data[np.argsort(model.row_labels_)]
fit_data = fit_data[:, np.argsort(model.column_labels_)]

plt.matshow(fit_data, cmap=plt.cm.Blues)
plt.title("After biclustering; rearranged to show biclusters")

plt.matshow(np.outer(np.sort(model.row_labels_) + 1,
np.sort(model.column_labels_) + 1),
cmap=plt.cm.Blues)
plt.title("Checkerboard structure of rearranged data")

plt.show()

Total running time of the script: ( 0 minutes 0.780 seconds)

6.3 Biclustering documents with the Spectral Co-clustering algorithm

This example demonstrates the Spectral Co-clustering algorithm on the twenty newsgroups dataset. The 'comp.os.ms-windows.misc' category is excluded because it contains many posts containing nothing but data.

The TF-IDF vectorized posts form a word frequency matrix, which is then biclustered using Dhillon’s Spectral Co-Clustering algorithm. The resulting document-word biclusters indicate subsets words used more often in those subsets documents.

For a few of the best biclusters, its most common document categories and its ten most important words get printed. The best biclusters are determined by their normalized cut. The best words are determined by comparing their sums inside and outside the bicluster.

For comparison, the documents are also clustered using MiniBatchKMeans. The document clusters derived from the biclusters achieve a better V-measure than clusters found by MiniBatchKMeans.

Out:

Vectorizing...
Coclustering...
Done in 5.28s. V-measure: 0.4435
MiniBatchKMeans...
Done in 12.54s. V-measure: 0.3344

Best biclusters:
from __future__ import print_function

from collections import defaultdict
import operator
from time import time
import numpy as np

from sklearn.cluster.bicluster import SpectralCoclustering
from sklearn.cluster import MiniBatchKMeans
from sklearn.externals.six import iteritems
from sklearn.datasets.twenty_newsgroups import fetch_20newsgroups
from sklearn.feature_extraction.text import TfidfVectorizer
from sklearn.metrics.cluster import v_measure_score

print(__doc__)

def number_normalizer(tokens):
    """ Map all numeric tokens to a placeholder.

    For many applications, tokens that begin with a number are not directly
    useful, but the fact that such a token exists can be relevant. By applying
    this form of dimensionality reduction, some methods may perform better.
    """
    return ("#NUMBER" if token[0].isdigit() else token for token in tokens)
class NumberNormalizingVectorizer(TfidfVectorizer):
    def build_tokenizer(self):
        tokenize = super(NumberNormalizingVectorizer, self).build_tokenizer()
        return lambda doc: list(number_normalizer(tokenize(doc)))

# exclude 'comp.os.ms-windows.misc'

newsgroups = fetch_20newsgroups(categories=categories)
y_true = newsgroups.target

vectorizer = NumberNormalizingVectorizer(stop_words='english', min_df=5)
cocluster = SpectralCoclustering(n_clusters=len(categories), svd_method='arpack', random_state=0)
kmeans = MiniBatchKMeans(n_clusters=len(categories), batch_size=20000, random_state=0)

print("Vectorizing...")
X = vectorizer.fit_transform(newsgroups.data)

print("Coclustering...")
start_time = time()
cocluster.fit(X)
y_cocluster = cocluster.row_labels_
print("Done in {:.2f}s. V-measure: {:.4f}".format(
time() - start_time,
v_measure_score(y_cocluster, y_true)))

print("MiniBatchKMeans...")
start_time = time()
y_kmeans = kmeans.fit_predict(X)
print("Done in {:.2f}s. V-measure: {:.4f}".format(
time() - start_time,
v_measure_score(y_kmeans, y_true)))

feature_names = vectorizer.get_feature_names()
document_names = list(newsgroups.target_names[i] for i in newsgroups.target)

def bicluster_ncut(i):
    rows, cols = cocluster.get_indices(i)
    if not (np.any(rows) and np.any(cols)):
        import sys
        return sys.float_info.max
    row_complement = np.nonzero(np.logical_not(cocluster.rows_[i]))[0]
    col_complement = np.nonzero(np.logical_not(cocluster.columns_[i]))[0]
    # Note: the following is identical to X[rows[:, np.newaxis],
    # cols].sum() but much faster in scipy <= 0.16
    weight = X[rows][:, cols].sum()
    cut = (X[row_complement][:, cols].sum() +
          X[rows][:, col_complement].sum())

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```python
def most_common(d):
    """Items of a defaultdict(int) with the highest values.
    Like Counter.most_common in Python >=2.7.
    """
    return sorted(iteritems(d), key=operator.itemgetter(1), reverse=True)

bicluster_ncuts = list(bicluster_ncut(i)
    for i in range(len(newsgroups.target_names)))
best_idx = np.argsort(bicluster_ncuts)[:5]
print()
print("Best biclusters:")
print("----------------")
for idx, cluster in enumerate(best_idx):
    n_rows, n_cols = cocluster.get_shape(cluster)
    cluster_docs, cluster_words = cocluster.get_indices(cluster)
    if not len(cluster_docs) or not len(cluster_words):
        continue
    # categories
    counter = defaultdict(int)
    for i in cluster_docs:
        counter[document_names[i]] += 1
    cat_string = ", ".join("{:0f}% {}".format(float(c) / n_rows * 100, name)
        for name, c in most_common(counter)[:3])
    # words
    out_of_cluster_docs = cocluster.row_labels_ != cluster
    out_of_cluster_docs = np.where(out_of_cluster_docs)[0]
    word_col = X[:, cluster_words]
    word_scores = np.array(word_col[cluster_docs, :].sum(axis=0) -
        word_col[out_of_cluster_docs, :].sum(axis=0))
    word_scores = word_scores.ravel()
    important_words = list(feature_names[cluster_words[i]]
        for i in word_scores.argsort()[:-11:-1])
    print("bicluster {} : {} documents, {} words".format(idx, n_rows, n_cols))
    print("categories : {}").format(cat_string))
    print("words : {}\n".format(', '.join(important_words)))
```

Total running time of the script: (0 minutes 22.318 seconds)
Examples illustrating the calibration of predicted probabilities of classifiers.

### 7.1 Comparison of Calibration of Classifiers

Well calibrated classifiers are probabilistic classifiers for which the output of the predict_proba method can be directly interpreted as a confidence level. For instance a well calibrated (binary) classifier should classify the samples such that among the samples to which it gave a predict_proba value close to 0.8, approx. 80% actually belong to the positive class.

LogisticRegression returns well calibrated predictions as it directly optimizes log-loss. In contrast, the other methods return biased probabilities, with different biases per method:

- **GaussianNaiveBayes** tends to push probabilities to 0 or 1 (note the counts in the histograms). This is mainly because it makes the assumption that features are conditionally independent given the class, which is not the case in this dataset which contains 2 redundant features.

- **RandomForestClassifier** shows the opposite behavior: the histograms show peaks at approx. 0.2 and 0.9 probability, while probabilities close to 0 or 1 are very rare. An explanation for this is given by Niculescu-Mizil and Caruana [1]: “Methods such as bagging and random forests that average predictions from a base set of models can have difficulty making predictions near 0 and 1 because variance in the underlying base models will bias predictions that should be near zero or one away from these values. Because predictions are restricted to the interval [0,1], errors caused by variance tend to be one- sided near zero and one. For example, if a model should predict p = 0 for a case, the only way bagging can achieve this is if all bagged trees predict zero. If we add noise to the trees that bagging is averaging over, this noise will cause some trees to predict values larger than 0 for this case, thus moving the average prediction of the bagged ensemble away from 0. We observe this effect most strongly with random forests because the base-level trees trained with random forests have relatively high variance due to feature subsetting.” As a result, the calibration curve shows a characteristic sigmoid shape, indicating that the classifier could trust its “intuition” more and return probabilities closer to 0 or 1 typically.

- **Support Vector Classification (SVC)** shows an even more sigmoid curve as the RandomForestClassifier, which is typical for maximum-margin methods (compare Niculescu-Mizil and Caruana [1]), which focus on hard samples that are close to the decision boundary (the support vectors).

References:
print(__doc__)

# Author: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD Style.

import numpy as np
np.random.seed(0)

import matplotlib.pyplot as plt

import sklearn import datasets
from sklearn import naive_bayes import GaussianNB
from sklearn import linear_model import LogisticRegression
from sklearn import ensemble import RandomForestClassifier
from sklearn import svm import LinearSVC

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from sklearn.calibration import calibration_curve
X, y = datasets.make_classification(n_samples=100000, n_features=20,
n_informative=2, n_redundant=2)
train_samples = 100

# Samples used for training the models

X_train = X[:train_samples]
X_test = X[train_samples:]
y_train = y[:train_samples]
y_test = y[train_samples:]
# Create classifiers
lr = LogisticRegression()
gnb = GaussianNB()
svc = LinearSVC(C=1.0)
rfc = RandomForestClassifier(n_estimators=100)

# #############################################################################
# Plot calibration plots
plt.figure(figsize=(10, 10))
ax1 = plt.subplot2grid((3, 1), (0, 0), rowspan=2)
ax2 = plt.subplot2grid((3, 1), (2, 0))
ax1.plot([0, 1], [0, 1], "k:", label="Perfectly calibrated")
for clf, name in [(lr, 'Logistic'),
(gnb, 'Naive Bayes'),
(svc, 'Support Vector Classification'),
(rfc, 'Random Forest')]:
clf.fit(X_train, y_train)
if hasattr(clf, "predict_proba"):
prob_pos = clf.predict_proba(X_test)[:, 1]
else: # use decision function
prob_pos = clf.decision_function(X_test)
prob_pos = \
(prob_pos - prob_pos.min()) / (prob_pos.max() - prob_pos.min())
fraction_of_positives, mean_predicted_value = \
calibration_curve(y_test, prob_pos, n_bins=10)
ax1.plot(mean_predicted_value, fraction_of_positives, "s-",
label="%s" % (name, ))
ax2.hist(prob_pos, range=(0, 1), bins=10, label=name,
histtype="step", lw=2)
ax1.set_ylabel("Fraction of positives")
ax1.set_ylim([-0.05, 1.05])
ax1.legend(loc="lower right")
ax1.set_title('Calibration plots (reliability curve)')
ax2.set_xlabel("Mean predicted value")
ax2.set_ylabel("Count")
ax2.legend(loc="upper center", ncol=2)
plt.tight_layout()
plt.show()

7.1. Comparison of Calibration of Classifiers

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7.2 Probability Calibration curves

When performing classification one often wants to predict not only the class label, but also the associated probability. This probability gives some kind of confidence on the prediction. This example demonstrates how to display how well calibrated the predicted probabilities are and how to calibrate an uncalibrated classifier.

The experiment is performed on an artificial dataset for binary classification with 100,000 samples (1,000 of them are used for model fitting) with 20 features. Of the 20 features, only 2 are informative and 10 are redundant. The first figure shows the estimated probabilities obtained with logistic regression, Gaussian naive Bayes, and Gaussian naive Bayes with both isotonic calibration and sigmoid calibration. The calibration performance is evaluated with Brier score, reported in the legend (the smaller the better). One can observe here that logistic regression is well calibrated while raw Gaussian naive Bayes performs very badly. This is because of the redundant features which violate the assumption of feature-independence and result in an overly confident classifier, which is indicated by the typical transposed-sigmoid curve.

Calibration of the probabilities of Gaussian naive Bayes with isotonic regression can fix this issue as can be seen from the nearly diagonal calibration curve. Sigmoid calibration also improves the brier score slightly, albeit not as strongly as the non-parametric isotonic regression. This can be attributed to the fact that we have plenty of calibration data such that the greater flexibility of the non-parametric model can be exploited.

The second figure shows the calibration curve of a linear support-vector classifier (LinearSVC). LinearSVC shows the opposite behavior as Gaussian naive Bayes: the calibration curve has a sigmoid curve, which is typical for an under-confident classifier. In the case of LinearSVC, this is caused by the margin property of the hinge loss, which lets the model focus on hard samples that are close to the decision boundary (the support vectors).

Both kinds of calibration can fix this issue and yield nearly identical results. This shows that sigmoid calibration can deal with situations where the calibration curve of the base classifier is sigmoid (e.g., for LinearSVC) but not where it is transposed-sigmoid (e.g., Gaussian naive Bayes).
7.2. Probability Calibration curves
Out:

Logistic:
  Brier: 0.099
  Precision: 0.872
  Recall: 0.851
  F1: 0.862

Naive Bayes:
  Brier: 0.118
  Precision: 0.857
  Recall: 0.876
  F1: 0.867

Naive Bayes + Isotonic:
  Brier: 0.098
  Precision: 0.883
  Recall: 0.836
  F1: 0.859

Naive Bayes + Sigmoid:
  Brier: 0.109
  Precision: 0.861
  Recall: 0.871
  F1: 0.866
Brier: 0.099
Precision: 0.872
Recall: 0.851
F1: 0.862

SVC:
Brier: 0.163
Precision: 0.872
Recall: 0.852
F1: 0.862

SVC + Isotonic:
Brier: 0.100
Precision: 0.853
Recall: 0.878
F1: 0.865

SVC + Sigmoid:
Brier: 0.099
Precision: 0.874
Recall: 0.849
F1: 0.861

print(__doc__)

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import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.naive_bayes import GaussianNB
from sklearn.svm import LinearSVC
from sklearn.linear_model import LogisticRegression
from sklearn.metrics import (brier_score_loss, precision_score, recall_score,
                              f1_score)
from sklearn.calibration import CalibratedClassifierCV, calibration_curve
from sklearn.model_selection import train_test_split

# Create dataset of classification task with many redundant and few
# informative features
X, y = datasets.make_classification(n_samples=100000, n_features=20,
                                     n_informative=2, n_redundant=10,
                                     random_state=42)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.99,
                                                      random_state=42)

def plot_calibration_curve(est, name, fig_index):
    """Plot calibration curve for est w/o and with calibration. """

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```python
# Calibrated with isotonic calibration
isotonic = CalibratedClassifierCV(est, cv=2, method='isotonic')

# Calibrated with sigmoid calibration
sigmoid = CalibratedClassifierCV(est, cv=2, method='sigmoid')

# Logistic regression with no calibration as baseline
lr = LogisticRegression(C=1., solver='lbfgs')

fig = plt.figure(fig_index, figsize=(10, 10))
ax1 = plt.subplot2grid((3, 1), (0, 0), rowspan=2)
ax2 = plt.subplot2grid((3, 1), (2, 0))

ax1.plot([0, 1], [0, 1], "k:", label="Perfectly calibrated")
for clf, name in [(lr, 'Logistic'),
                   (est, name),
                   (isotonic, name + ' + Isotonic'),
                   (sigmoid, name + ' + Sigmoid')]:
    clf.fit(X_train, y_train)
y_pred = clf.predict(X_test)
    if hasattr(clf, "predict_proba"):
        prob_pos = clf.predict_proba(X_test)[:, 1]
    else:
        # use decision function
        prob_pos = clf.decision_function(X_test)
    prob_pos = (prob_pos - prob_pos.min()) / (prob_pos.max() - prob_pos.min())
    clf_score = brier_score_loss(y_test, prob_pos, pos_label=y.max())
    print("%s" % name)
    print("Brier: %1.3f" % (clf_score))
    print("Precision: %1.3f" % precision_score(y_test, y_pred))
    print("Recall: %1.3f" % recall_score(y_test, y_pred))
    print("F1: %1.3f" % f1_score(y_test, y_pred))

    fraction_of_positives, mean_predicted_value = \
        calibration_curve(y_test, prob_pos, n_bins=10)
    ax1.plot(mean_predicted_value, fraction_of_positives, "s-", label="\n(%s (%1.3f))" % (name, clf_score))

    ax2.hist(prob_pos, range=(0, 1), bins=10, label=name,
             histtype="step", lw=2)

ax1.set_ylabel("Fraction of positives")
ax1.set_ylim([-0.05, 1.05])
ax1.legend(loc="lower right")
ax1.set_title("Calibration plots (reliability curve)")

ax2.set_xlabel("Mean predicted value")
ax2.set_ylabel("Count")
ax2.legend(loc="upper center", ncol=2)

plt.tight_layout()

# Plot calibration curve for Gaussian Naive Bayes
plot_calibration_curve(GaussianNB(), "Naive Bayes", 1)

# Plot calibration curve for Linear SVC
```
plot_calibration_curve(LinearSVC(), "SVC", 2)
plt.show()

Total running time of the script: (0 minutes 2.216 seconds)

7.3 Probability calibration of classifiers

When performing classification you often want to predict not only the class label, but also the associated probability. This probability gives you some kind of confidence on the prediction. However, not all classifiers provide well-calibrated probabilities, some being over-confident while others being under-confident. Thus, a separate calibration of predicted probabilities is often desirable as a postprocessing. This example illustrates two different methods for this calibration and evaluates the quality of the returned probabilities using Brier’s score (see https://en.wikipedia.org/wiki/Brier_score).

Compared are the estimated probability using a Gaussian naive Bayes classifier without calibration, with a sigmoid calibration, and with a non-parametric isotonic calibration. One can observe that only the non-parametric model is able to provide a probability calibration that returns probabilities close to the expected 0.5 for most of the samples belonging to the middle cluster with heterogeneous labels. This results in a significantly improved Brier score.

Brier scores: (the smaller the better)
No calibration: 0.104
With isotonic calibration: 0.084
With sigmoid calibration: 0.109

print(__doc__)

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# License: BSD Style.

import numpy as np
import matplotlib.pyplot as plt
from matplotlib import cm
from sklearn.datasets import make_blobs
from sklearn.naive_bayes import GaussianNB
from sklearn.metrics import brier_score_loss
from sklearn.calibration import CalibratedClassifierCV
from sklearn.model_selection import train_test_split

n_samples = 50000
n_bins = 3  # use 3 bins for calibration_curve as we have 3 clusters here

# Generate 3 blobs with 2 classes where the second blob contains
# half positive samples and half negative samples. Probability in this
# blob is therefore 0.5.
centers = [(-5, -5), (0, 0), (5, 5)]
X, y = make_blobs(n_samples=n_samples, n_features=2, cluster_std=1.0,
                  centers=centers, shuffle=False, random_state=42)
y[:n_samples // 2] = 0
y[n_samples // 2:] = 1
sample_weight = np.random.RandomState(42).rand(y.shape[0])

# split train, test for calibration
X_train, X_test, y_train, y_test, sw_train, sw_test = train_test_split(X, y, sample_weight, test_size=0.9, random_state=42)

# Gaussian Naive-Bayes with no calibration
clf = GaussianNB()
clf.fit(X_train, y_train)  # GaussianNB itself does not support sample-weights
prob_pos_clf = clf.predict_proba(X_test)[:, 1]

# Gaussian Naive-Bayes with isotonic calibration
clf_isotonic = CalibratedClassifierCV(clf, cv=2, method='isotonic')
clf_isotonic.fit(X_train, y_train, sw_train)
prob_pos_isotonic = clf_isotonic.predict_proba(X_test)[:, 1]

# Gaussian Naive-Bayes with sigmoid calibration
clf_sigmoid = CalibratedClassifierCV(clf, cv=2, method='sigmoid')
clf_sigmoid.fit(X_train, y_train, sw_train)
prob_pos_sigmoid = clf_sigmoid.predict_proba(X_test)[:, 1]

print("Brier scores: (the smaller the better)")

clf_score = brier_score_loss(y_test, prob_pos_clf, sw_test)
print("No calibration: $%.3f" % clf_score)

clf_isotonic_score = brier_score_loss(y_test, prob_pos_isotonic, sw_test)
print("With isotonic calibration: $%.3f" % clf_isotonic_score)

clf_sigmoid_score = brier_score_loss(y_test, prob_pos_sigmoid, sw_test)
print("With sigmoid calibration: $%.3f" % clf_sigmoid_score)

# #############################################################################
# Plot the data and the predicted probabilities
plt.figure()
y_unique = np.unique(y)
colors = cm.rainbow(np.linspace(0.0, 1.0, y_unique.size))
for this_y, color in zip(y_unique, colors):
    this_X = X_train[y_train == this_y]
    this_sw = sw_train[y_train == this_y]
    plt.scatter(this_X[:, 0], this_X[:, 1], s=this_sw * 50, c=color,
                alpha=0.5, edgecolor='k',
                label="Class %s" % this_y)
plt.legend(loc="best")
plt.title("Data")

plt.figure()
order = np.lexsort((prob_pos_clf, ))
plt.plot(prob_pos_clf[order], 'r', label='No calibration ($%.3f') % clf_score
plt.plot(prob_pos_isotonic[order], 'g', linewidth=3,
         label='Isotonic calibration ($%.3f') % clf_isotonic_score
plt.plot(prob_pos_sigmoid[order], 'b', linewidth=3,
         label='Sigmoid calibration ($%.3f') % clf_sigmoid_score
plt.plot(np.linspace(0, y_test.size, 51)[1::2],
         y_test[order].reshape(25, -1).mean(1), 'k', linewidth=3, label=r'Empirical')
plt.ylim([-0.05, 1.05])
plt.xlabel("Instances sorted according to predicted probability ",
         label='(uncalibrated GNB)"
plt.ylabel("P(y=1)")
plt.legend(loc="upper left")
plt.title("Gaussian naive Bayes probabilities")
plt.show()

Total running time of the script: ( 0 minutes 0.228 seconds)

7.4 Probability Calibration for 3-class classification

This example illustrates how sigmoid calibration changes predicted probabilities for a 3-class classification problem. Illustrated is the standard 2-simplex, where the three corners correspond to the three classes. Arrows point from the probability vectors predicted by an uncalibrated classifier to the probability vectors predicted by the same classifier after sigmoid calibration on a hold-out validation set. Colors indicate the true class of an instance (red: class 1, green: class 2, blue: class 3).
The base classifier is a random forest classifier with 25 base estimators (trees). If this classifier is trained on all 800 training datapoints, it is overly confident in its predictions and thus incurs a large log-loss. Calibrating an identical classifier, which was trained on 600 datapoints, with method='sigmoid' on the remaining 200 datapoints reduces the confidence of the predictions, i.e., moves the probability vectors from the edges of the simplex towards the center. This calibration results in a lower log-loss. Note that an alternative would have been to increase the number of base estimators which would have resulted in a similar decrease in log-loss.

Out:

Log-loss of
- uncalibrated classifier trained on 800 datapoints: 1.280
- classifier trained on 600 datapoints and calibrated on 200 datapoint: 0.534

```
print(__doc__)
# Author: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD Style.

import matplotlib.pyplot as plt
import numpy as np
```
from sklearn.datasets import make_blobs
from sklearn.ensemble import RandomForestClassifier
from sklearn.calibration import CalibratedClassifierCV
from sklearn.metrics import log_loss
np.random.seed(0)

# Generate data
X, y = make_blobs(n_samples=1000, n_features=2, random_state=42,
                  cluster_std=5.0)
X_train, y_train = X[:600], y[:600]
X_valid, y_valid = X[600:800], y[600:800]
X_train_valid, y_train_valid = X[:800], y[:800]
X_test, y_test = X[800:], y[800:]

# Train uncalibrated random forest classifier on whole train and validation
# data and evaluate on test data
clf = RandomForestClassifier(n_estimators=25)
clf.fit(X_train_valid, y_train_valid)
clf_probs = clf.predict_proba(X_test)
score = log_loss(y_test, clf_probs)

# Train random forest classifier, calibrate on validation data and evaluate
# on test data
clf = RandomForestClassifier(n_estimators=25)
clf.fit(X_train, y_train)
clf_probs = clf.predict_proba(X_test)
sig_clf = CalibratedClassifierCV(clf, method="sigmoid", cv="prefit")
sig_clf.fit(X_valid, y_valid)
sig_clf_probs = sig_clf.predict_proba(X_test)
sig_score = log_loss(y_test, sig_clf_probs)

# Plot changes in predicted probabilities via arrows
plt.figure(0)
for i in range(clf_probs.shape[0]):
    plt.arrow(clf_probs[i, 0], clf_probs[i, 1],
              sig_clf_probs[i, 0] - clf_probs[i, 0],
              sig_clf_probs[i, 1] - clf_probs[i, 1],
              color=colors[y_test[i]], head_width=1e-2)

# Plot perfect predictions
plt.plot([1.0], [0.0], 'ro', ms=20, label="Class 1")
plt.plot([0.0], [1.0], 'go', ms=20, label="Class 2")
plt.plot([0.0], [0.0], 'bo', ms=20, label="Class 3")

# Plot boundaries of unit simplex
plt.plot([0.0, 1.0, 0.0, 0.0], [0.0, 0.0, 1.0, 0.0], 'k', label="Simplex")

# Annotate points on the simplex
plt.annotate(r'\(\frac{1}{3}, \frac{1}{3}, \frac{1}{3}\)',
             xy=(1.0/3, 1.0/3), xytext=(1.0/3, .23), xycoords='data',
             arrowprops=dict(facecolor='black', shrink=0.05),
             horizontalalignment='center', verticalalignment='center')
plt.plot([1.0/3], [1.0/3], 'ko', ms=5)
plt.annotate(r'\(\frac{1}{2}, 0, \frac{1}{2}\)',
             xy=(.5, .0), xytext=(.5, .1), xycoords='data',
             arrowprops=dict(facecolor='black', shrink=0.05),
             horizontalalignment='center', verticalalignment='center')
# Illustrate calibrator

```python
plt.figure()
# generate grid over 2-simplex
p1d = np.linspace(0, 1, 20)
p0, p1 = np.meshgrid(p1d, p1d)
p2 = 1 - p0 - p1
p = np.c_[p0.ravel(), p1.ravel(), p2.ravel()]
p = p[p[:, 2] >= 0]
calibrated_classifier = sig_clf.calibrated_classifiers_[0]
prediction = np.vstack([calibrator.predict(this_p)
                        for calibrator, this_p in
                        zip(calibrated_classifier.calibrators_, p.T)]).T
prediction /= prediction.sum(axis=1)[:, None]
```

# Plot modifications of calibrator
for i in range(prediction.shape[0]):
    plt.arrow(p[i, 0], p[i, 1],
              prediction[i, 0] - p[i, 0], prediction[i, 1] - p[i, 1],
              head_width=1e-2, color=colors[np.argmax(p[i])])

# Plot boundaries of unit simplex
plt.plot([0.0, 1.0, 0.0, 0.0], [0.0, 0.0, 1.0, 0.0], 'k', label="Simplex")
plt.grid("off")
for x in [0.0, 0.1, 0.2, 0.3, 0.4, 0.5, 0.6, 0.7, 0.8, 0.9, 1.0]:
    plt.plot([0, x], [x, 0], 'k', alpha=0.2)
    plt.plot([0, 0 + (1-x)/2], [x, x + (1-x)/2], 'k', alpha=0.2)
    plt.plot([x, x + (1-x)/2], [0, 0 + (1-x)/2], 'k', alpha=0.2)

plt.title("Illustration of sigmoid calibrator")
plt.xlabel("Probability class 1")
plt.ylabel("Probability class 2")
plt.xlim(-0.05, 1.05)
plt.ylim(-0.05, 1.05)
plt.show()

Total running time of the script: ( 0 minutes 0.551 seconds)
General examples about classification algorithms.

8.1 Recognizing hand-written digits

An example showing how the scikit-learn can be used to recognize images of hand-written digits. This example is commented in the tutorial section of the user manual.

Out:
Classification report for classifier SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0, decision_function_shape='ovr', degree=3, gamma=0.001, kernel='rbf', max_iter=-1, probability=False, random_state=None, shrinking=True, tol=0.001, verbose=False):

<table>
<thead>
<tr>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00</td>
<td>0.99</td>
<td>0.99</td>
</tr>
<tr>
<td>1</td>
<td>0.99</td>
<td>0.97</td>
<td>0.98</td>
</tr>
<tr>
<td>2</td>
<td>0.99</td>
<td>0.99</td>
<td>0.99</td>
</tr>
<tr>
<td>3</td>
<td>0.98</td>
<td>0.87</td>
<td>0.92</td>
</tr>
<tr>
<td>4</td>
<td>0.99</td>
<td>0.96</td>
<td>0.97</td>
</tr>
<tr>
<td>5</td>
<td>0.95</td>
<td>0.97</td>
<td>0.96</td>
</tr>
<tr>
<td>6</td>
<td>0.99</td>
<td>0.99</td>
<td>0.99</td>
</tr>
<tr>
<td>7</td>
<td>0.96</td>
<td>0.99</td>
<td>0.97</td>
</tr>
<tr>
<td>8</td>
<td>0.94</td>
<td>1.00</td>
<td>0.97</td>
</tr>
<tr>
<td>9</td>
<td>0.93</td>
<td>0.98</td>
<td>0.95</td>
</tr>
</tbody>
</table>

avg / total 0.97 0.97 0.97 899

Confusion matrix:

```
[[87  0  0  0  1  0  0  0  0  0]
 [ 0 88  1  0  0  0  0  0  1  1]
 [ 0  0 85  1  0  0  0  0  0  0]
 [ 0  0  0 79  0  3  0  4  5  0]
 [ 0  0  0  0 88  0  0  0  0  4]
 [ 0  0  0  0  0 88  1  0  0  2]
 [ 0  1  0  0  0  0 90  0  0  0]
 [ 0  0  0  0  0  1  0 88  0  0]
 [ 0  0  0  0  0  0  0  0 88  0]
 [ 0  0  0  1  0  0  0  0  0 90]]
```

print(__doc__)

# Author: Gael Varoquaux <gael dot varoquaux at normalesup dot org>
# License: BSD 3 clause

# Standard scientific Python imports
import matplotlib.pyplot as plt

# Import datasets, classifiers and performance metrics
from sklearn import datasets, svm, metrics

# The digits dataset
digits = datasets.load_digits()

digits.data

# The data that we are interested in is made of 8x8 images of digits, let's
# have a look at the first 4 images, stored in the `images' attribute of the
dataset. If we were working from image files, we could load them using
# matplotlib.pyplot.imread. Note that each image must have the same size. For these
# images, we know which digit they represent: it is given in the 'target' of
# the dataset.
images_and_labels = list(zip(digits.images, digits.target))
for index, (image, label) in enumerate(images_and_labels[:4]):
    plt.subplot(2, 4, index + 1)
    plt.axis('off')
    plt.imshow(image, cmap=plt.cm.gray_r, interpolation='nearest')
    plt.title('Training: %i' % label)

# To apply a classifier on this data, we need to flatten the image, to
# turn the data in a (samples, feature) matrix:

t_n = len(digits.images)
data = digits.images.reshape((n_samples, -1))

# Create a classifier: a support vector classifier

classifier = svm.SVC(gamma=0.001)

classifier.fit(data[:n_samples // 2], digits.target[:n_samples // 2])

classifier.fit(data[n_samples // 2:], digits.target[n_samples // 2:])

print(classification_report(expected, predicted))
print(confusion_matrix(expected, predicted))
images_and_predictions = list(zip(digits.images[n_samples // 2:], predicted))
for index, (image, prediction) in enumerate(images_and_predictions[:4]):
    plt.subplot(2, 4, index + 5)
    plt.axis('off')
    plt.imshow(image, cmap=plt.cm.gray_r, interpolation='nearest')
    plt.title('Prediction: %i' % prediction)

plt.show()

Total running time of the script: ( 0 minutes 0.517 seconds)

8.2 Normal and Shrinkage Linear Discriminant Analysis for classification

Shows how shrinkage improves classification.
from __future__ import division
import numpy as np
import matplotlib.pyplot as plt
from sklearn.datasets import make_blobs
from sklearn.discriminant_analysis import LinearDiscriminantAnalysis

n_train = 20  # samples for training
n_test = 200  # samples for testing
n_averages = 50  # how often to repeat classification
n_features_max = 75  # maximum number of features
step = 4  # step size for the calculation

def generate_data(n_samples, n_features):
    """Generate random blob-ish data with noisy features.

    This returns an array of input data with shape `(n_samples, n_features)`
    and an array of `n_samples` target labels.

    Only one feature contains discriminative information, the other features
    contain only noise.
    """
    X, y = make_blobs(n_samples=n_samples, n_features=1, centers=[[-2], [2]])
# add non-discriminative features

```python
if n_features > 1:
    X = np.hstack([X, np.random.randn(n_samples, n_features - 1)])
return X, y
```

```python
acc_clf1, acc_clf2 = [], []
n_features_range = range(1, n_features_max + 1, step)
for n_features in n_features_range:
    score_clf1, score_clf2 = 0, 0
    for _ in range(n_averages):
        X, y = generate_data(n_train, n_features)
        clf1 = LinearDiscriminantAnalysis(solver='lsqr', shrinkage='auto').fit(X, y)
        clf2 = LinearDiscriminantAnalysis(solver='lsqr', shrinkage=None).fit(X, y)
        X, y = generate_data(n_test, n_features)
        score_clf1 += clf1.score(X, y)
        score_clf2 += clf2.score(X, y)
    acc_clf1.append(score_clf1 / n_averages)
    acc_clf2.append(score_clf2 / n_averages)
```

```python
features_samples_ratio = np.array(n_features_range) / n_train
plt.plot(features_samples_ratio, acc_clf1, linewidth=2,
    label="Linear Discriminant Analysis with shrinkage", color='navy')
plt.plot(features_samples_ratio, acc_clf2, linewidth=2,
    label="Linear Discriminant Analysis", color='gold')
```

```python
plt.xlabel('n_features / n_samples')
plt.ylabel('Classification accuracy')
plt.legend(loc=1, prop={'size': 12})
plt.suptitle('Linear Discriminant Analysis vs. shrinkage Linear Discriminant Analysis (1 discriminative feature)')
plt.show()
```

**Total running time of the script:** ( 0 minutes 6.887 seconds)

### 8.3 Plot classification probability

Plot the classification probability for different classifiers. We use a 3 class dataset, and we classify it with a Support Vector classifier, L1 and L2 penalized logistic regression with either a One-Vs-Rest or multinomial setting, and Gaussian process classification.

The logistic regression is not a multiclass classifier out of the box. As a result it can identify only the first class.
Out:

classif_rate for L1 logistic : 79.333333
classif_rate for L2 logistic (OvR) : 76.666667
classif_rate for Linear SVC : 82.000000
classif_rate for L2 logistic (Multinomial) : 82.000000
classif_rate for GPC : 82.666667

print(__doc__)

# Author: Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause

import matplotlib.pyplot as plt
import numpy as np
from sklearn.linear_model import LogisticRegression
from sklearn.svm import SVC
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF
from sklearn import datasets
iris = datasets.load_iris()
X = iris.data[:, 0:2]  # we only take the first two features for visualization
y = iris.target
n_features = X.shape[1]
C = 1.0
kernel = 1.0 * RBF([1.0, 1.0])  # for GPC

# Create different classifiers. The logistic regression cannot do
# multiclass out of the box.
classifiers = {'L1 logistic': LogisticRegression(C=C, penalty='l1'),
               'L2 logistic (OvR)': LogisticRegression(C=C, penalty='l2'),
               'Linear SVC': SVC(kernel='linear', C=C, probability=True,
                                 random_state=0),
               'L2 logistic (Multinomial)': LogisticRegression(C=C, solver='lbfgs', multi_class='multinomial'),
               'GPC': GaussianProcessClassifier(kernel)}

n_classifiers = len(classifiers)
plt.figure(figsize=(3 * 2, n_classifiers * 2))
plt.subplots_adjust(bottom=.2, top=.95)
xx = np.linspace(3, 9, 100)
yy = np.linspace(1, 5, 100).T
xx, yy = np.meshgrid(xx, yy)
Xfull = np.c_[xx.ravel(), yy.ravel()]

for index, (name, classifier) in enumerate(classifiers.items()):
    # 8.3. Plot classification probability 719
classifier.fit(X, y)

y_pred = classifier.predict(X)
classif_rate = np.mean(y_pred.ravel() == y.ravel()) * 100
print("classif_rate for %s: %f" % (name, classif_rate))

# View probabilities=
probas = classifier.predict_proba(Xfull)
n_classes = np.unique(y_pred).size
for k in range(n_classes):
    plt.subplot(n_classifiers, n_classes, index * n_classes + k + 1)
    plt.title("Class %d" % k)
    if k == 0:
        plt.ylabel(name)
    imshow_handle = plt.imshow(probas[:, k].reshape((100, 100)),
                                extent=(3, 9, 1, 5), origin='lower')
    plt.xticks(())
    plt.yticks(()
    idx = (y_pred == k)
    if idx.any():
        plt.scatter(X[idx, 0], X[idx, 1], marker='o', c='k')

ax = plt.axes([0.15, 0.04, 0.7, 0.05])
plt.title("Probability")
plt.colorbar(imshow_handle, cax=ax, orientation='horizontal')
plt.show()

Total running time of the script: ( 0 minutes 8.574 seconds)

8.4 Classifier comparison

A comparison of a several classifiers in scikit-learn on synthetic datasets. The point of this example is to illustrate the nature of decision boundaries of different classifiers. This should be taken with a grain of salt, as the intuition conveyed by these examples does not necessarily carry over to real datasets.

Particularly in high-dimensional spaces, data can more easily be separated linearly and the simplicity of classifiers such as naive Bayes and linear SVMs might lead to better generalization than is achieved by other classifiers.

The plots show training points in solid colors and testing points semi-transparent. The lower right shows the classification accuracy on the test set.
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.datasets import make_moons, make_circles, make_classification
from sklearn.neural_network import MLPClassifier
from sklearn.neighbors import KNeighborsClassifier
from sklearn.svm import SVC
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF
from sklearn.tree import DecisionTreeClassifier
from sklearn.ensemble import RandomForestClassifier, AdaBoostClassifier
from sklearn.naive_bayes import GaussianNB
from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis

h = .02  # step size in the mesh


classifiers = [
    KNeighborsClassifier(3),
    SVC(kernel="linear", C=0.025),
    SVC(gamma=2, C=1),
    GaussianProcessClassifier(1.0 * RBF(1.0)),
    DecisionTreeClassifier(max_depth=5),
    RandomForestClassifier(max_depth=5, n_estimators=10, max_features=1),
    MLPClassifier(alpha=1),
    AdaBoostClassifier(),
    GaussianNB(),
    QuadraticDiscriminantAnalysis()]

X, y = make_classification(n_features=2, n_redundant=0, n_informative=2,
                           random_state=1, n_clusters_per_class=1)
rng = np.random.RandomState(2)
X += 2 * rng.uniform(size=X.shape)
linearly_separable = (X, y)
datasets = [make_moons(noise=0.3, random_state=0),
            make_circles(noise=0.2, factor=0.5, random_state=1),
            linearly_separable]

title = "Classifier comparison example"

figure = plt.figure(figsize=(27, 9))
i = 1

# iterate over datasets
for ds_cnt, ds in enumerate(datasets):
    # preprocess dataset, split into training and test part

X, y = ds
X = StandardScaler().fit_transform(X)
X_train, X_test, y_train, y_test = 
    train_test_split(X, y, test_size=.4, random_state=42)

x_min, x_max = X[:, 0].min() - .5, X[:, 0].max() + .5
y_min, y_max = X[:, 1].min() - .5, X[:, 1].max() + .5
xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))

# just plot the dataset first
cm = plt.cm.RdBu
cm_bright = ListedColormap(['#FF0000', '#0000FF'])
ax = plt.subplot(len(datasets), len(classifiers) + 1, i)
if ds_cnt == 0:
    ax.set_title("Input data")
# Plot the training points
ax.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cm_bright,
           edgecolors='k')
# and testing points
ax.scatter(X_test[:, 0], X_test[:, 1], c=y_test, cmap=cm_bright, alpha=0.6,
           edgecolors='k')
ax.set_xlim(xx.min(), xx.max())
ax.set_ylim(yy.min(), yy.max())
ax.set_xticks(())
ax.set_yticks(()
i += 1

# iterate over classifiers
for name, clf in zip(names, classifiers):
    ax = plt.subplot(len(datasets), len(classifiers) + 1, i)
    clf.fit(X_train, y_train)
score = clf.score(X_test, y_test)

    # Plot the decision boundary. For that, we will assign a color to each
    # point in the mesh [x_min, x_max]x[y_min, y_max].
    if hasattr(clf, "decision_function"):
        Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
    else:
        Z = clf.predict_proba(np.c_[xx.ravel(), yy.ravel()])[:, 1]

    # Put the result into a color plot
    Z = Z.reshape(xx.shape)
    ax.contourf(xx, yy, Z, cmap=cm, alpha=.8)

    # Plot also the training points
    ax.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cm_bright,
               edgecolors='k')
    # and testing points
    ax.scatter(X_test[:, 0], X_test[:, 1], c=y_test, cmap=cm_bright,
               edgecolors='k', alpha=0.6)

    ax.set_xlim(xx.min(), xx.max())
    ax.set_ylim(yy.min(), yy.max())
    ax.set_xticks(())
    ax.set_yticks(()
    if ds_cnt == 0:
        ax.set_title(name)
8.5 Linear and Quadratic Discriminant Analysis with covariance ellipsoid

This example plots the covariance ellipsoids of each class and decision boundary learned by LDA and QDA. The ellipsoids display the double standard deviation for each class. With LDA, the standard deviation is the same for all the classes, while each class has its own standard deviation with QDA.
from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis

# Colormap
cmap = colors.LinearSegmentedColormap(
    'red_blue_classes',
    {'red': [(0, 1, 1), (1, 0.7, 0.7)],
     'green': [(0, 0.7, 0.7), (1, 0.7, 0.7)],
     'blue': [(0, 0.7, 0.7), (1, 1, 1)]}
plt.cm.register_cmap(cmap=cmap)

# Generate datasets
def dataset_fixed_cov():
    '''Generate 2 Gaussians samples with the same covariance matrix'''
    n, dim = 300, 2
    np.random.seed(0)
    C = np.array([[0., -0.23], [0.83, 0.23]])
    X = np.r_[np.dot(np.random.randn(n, dim), C),
             np.dot(np.random.randn(n, dim), C) + np.array([1, 1])]
    y = np.hstack((np.zeros(n), np.ones(n)))
    return X, y

def dataset_cov():
    '''Generate 2 Gaussians samples with different covariance matrices'''
    n, dim = 300, 2
    np.random.seed(0)
    C = np.array([[0., -1.], [2.5, .7]]) * 2.
    X = np.r_[np.dot(np.random.randn(n, dim), C),
             np.dot(np.random.randn(n, dim), C.T) + np.array([1, 4])]
    y = np.hstack((np.zeros(n), np.ones(n)))
    return X, y

# Plot functions
def plot_data(lda, X, y, y_pred, fig_index):
    splot = plt.subplot(2, 2, fig_index)
    if fig_index == 1:
        plt.title('Linear Discriminant Analysis')
        plt.ylabel('Data with
                   fixed covariance')
    elif fig_index == 2:
        plt.title('Quadratic Discriminant Analysis')
    elif fig_index == 3:
        plt.ylabel('Data with
                   varying covariances')
    tp = (y == y_pred)  # True Positive
    tp0, tp1 = tp[y == 0], tp[y == 1]
    X0, X1 = X[y == 0], X[y == 1]
    X0_tp, X0_fp = X0[tp0], X0[~tp0]
    X1_tp, X1_fp = X1[tp1], X1[~tp1]
    alpha = 0.5
```python
# class 0: dots
plt.plot(X0_tp[:, 0], X0_tp[:, 1], 'o', alpha=alpha,
        color='red', markeredgecolor='k')
plt.plot(X0_fp[:, 0], X0_fp[:, 1], '*', alpha=alpha,
        color='#990000', markeredgecolor='k')  # dark red

# class 1: dots
plt.plot(X1_tp[:, 0], X1_tp[:, 1], 'o', alpha=alpha,
        color='blue', markeredgecolor='k')
plt.plot(X1_fp[:, 0], X1_fp[:, 1], '*', alpha=alpha,
        color='#000099', markeredgecolor='k')  # dark blue

# class 0 and 1: areas
nx, ny = 200, 100
x_min, x_max = plt.xlim()
y_min, y_max = plt.ylim()
xx, yy = np.meshgrid(np.linspace(x_min, x_max, nx),
        np.linspace(y_min, y_max, ny))
Z = lda.predict_proba(np.c_[xx.ravel(), yy.ravel()])
Z = Z[:, 1].reshape(xx.shape)
plt.pcolormesh(xx, yy, Z, cmap='red_blue_classes',
        norm=colors.Normalize(0., 1.))
plt.contour(xx, yy, Z, [0.5], linewidths=2., colors='k')

# means
plt.plot(lda.means_[0][0], lda.means_[0][1],
        'o', color='black', markersize=10, markeredgecolor='k')
plt.plot(lda.means_[1][0], lda.means_[1][1],
        'o', color='black', markersize=10, markeredgecolor='k')

return splot

def plot_ellipse(splot, mean, cov, color):
    v, w = linalg.eigh(cov)
    u = w[0] / linalg.norm(w[0])
    angle = np.arctan(u[1] / u[0])
    angle = 180 * angle / np.pi  # convert to degrees
    # filled Gaussian at 2 standard deviation
    ell = mpl.patches.Ellipse(mean, 2 * v[0] ** 0.5, 2 * v[1] ** 0.5,
        180 + angle, facecolor=color,
        edgewidth=1, facecolor=color,
        linewidth=2, zorder=2)
    ell.set_clip_box(splot.bbox)
    ell.set_alpha(0.5)
    splot.add_artist(ell)
splot.set_xticks(())
splot.set_yticks(())

def plot_lda_cov(lda, splot):
    plot_ellipse(splot, lda.means_[0][0], lda.means_[0][1],
        'red')
    plot_ellipse(splot, lda.means_[1][0], lda.means_[1][1],
        'blue')

def plot_qda_cov(qda, splot):
    plot_ellipse(splot, qda.means_[0][0], qda.means_[0][1],
        'red')
    plot_ellipse(splot, qda.means_[1][0], qda.means_[1][1],
        'blue')
```

8.5. Linear and Quadratic Discriminant Analysis with covariance ellipsoid
for i, (X, y) in enumerate([dataset_fixed_cov(), dataset_cov()]):
    # Linear Discriminant Analysis
    lda = LinearDiscriminantAnalysis(solver="svd", store_covariance=True)
    y_pred = lda.fit(X, y).predict(X)
    splot = plot_data(lda, X, y, y_pred, fig_index=2 * i + 1)
    plot_lda_cov(lda, splot)
    plt.axis('tight')

    # Quadratic Discriminant Analysis
    qda = QuadraticDiscriminantAnalysis(store_covariances=True)
    y_pred = qda.fit(X, y).predict(X)
    splot = plot_data(qda, X, y, y_pred, fig_index=2 * i + 2)
    plot_qda_cov(qda, splot)
    plt.axis('tight')
plt.suptitle('Linear Discriminant Analysis vs Quadratic Discriminant Analysis')
plt.show()
Examples concerning the `sklearn.cluster` module.

### 9.1 Feature agglomeration

These images show how similar features are merged together using feature agglomeration.

```python
print(__doc__)

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

digits = datasets.load_digits()

import numpy as np
import matplotlib.pyplot as plt

from sklearn import datasets, cluster
from sklearn.feature_extraction.image import grid_to_graph

digits = datasets.load_digits()
```
images = digits.images
X = np.reshape(images, (len(images), -1))
connectivity = grid_to_graph(*images[0].shape)

agglo = cluster.FeatureAgglomeration(connectivity=connectivity,
                                    n_clusters=32)

agglo.fit(X)
X_reduced = agglo.transform(X)
X_restored = agglo.inverse_transform(X_reduced)
images_restored = np.reshape(X_restored, images.shape)

plt.figure(1, figsize=(4, 3.5))
plt.clf()
plt.subplots_adjust(left=.01, right=.99, bottom=.01, top=.91)
for i in range(4):
    plt.subplot(3, 4, i + 1)
    plt.imshow(images[i], cmap=plt.cm.gray, vmax=16, interpolation='nearest')
    plt.xticks(())
    plt.yticks(())
    if i == 1:
        plt.title('Original data')

plt.subplot(3, 4, 4 + i + 1)
plt.imshow(images_restored[i], cmap=plt.cm.gray, vmax=16,
           interpolation='nearest')
if i == 1:
    plt.title('Agglomerated data')
plt.xticks()
plt.yticks()

plt.subplot(3, 4, 10)
plt.imshow(np.reshape(agglo.labels_, images[0].shape),
           interpolation='nearest', cmap=plt.cm.spectral)
plt.xticks()
plt.yticks()
plt.title('Labels')
plt.show()

Total running time of the script: ( 0 minutes 0.449 seconds)

9.2 A demo of the mean-shift clustering algorithm

Reference:
number of estimated clusters: 3

# Generate sample data
centers = [[1, 1], [-1, -1], [1, -1]]
X, _ = make_blobs(n_samples=10000, centers=centers, cluster_std=0.6)

# Compute clustering with MeanShift
bandwidth = estimate_bandwidth(X, quantile=0.2, n_samples=500)
ms = MeanShift(bandwidth=bandwidth, bin_seeding=True)
ms.fit(X)
labels = ms.labels_
cluster_centers = ms.cluster_centers_
labels_unique = np.unique(labels)
n_clusters_ = len(labels_unique)

print("number of estimated clusters : \%d \%% n_clusters_)

# Plot result
import matplotlib.pyplot as plt
from itertools import cycle
plt.figure(1)
plt.clf()
colors = cycle('bgrcmykbgrcmykbgrcmykbgrcmyk')
for k, col in zip(range(n_clusters_), colors):
    my_members = labels == k
    cluster_center = cluster_centers[k]
    plt.plot(X[my_members, 0], X[my_members, 1], col + '.")
    plt.plot(cluster_center[0], cluster_center[1], 'o', markerfacecolor=col,
             markeredgecolor='k', markersize=14)
plt.title('Estimated number of clusters: \%d \%% n_clusters_)
plt.show()
print(__doc__)

# Author: Phil Roth <mr.phil.roth@gmail.com>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt

from sklearn.cluster import KMeans
from sklearn.datasets import make_blobs

plt.figure(figsize=(12, 12))

n_samples = 1500
random_state = 170
X, y = make_blobs(n_samples=n_samples, random_state=random_state)

# Incorrect number of clusters
y_pred = KMeans(n_clusters=2, random_state=random_state).fit_predict(X)

plt.subplot(221)
plt.scatter(X[:, 0], X[:, 1], c=y_pred)
plt.title("Incorrect Number of Blobs")

# Anisotropically distributed data
transformation = [[0.60834549, -0.63667341], [-0.40887718, 0.85253229]]
X_aniso = np.dot(X, transformation)
y_pred = KMeans(n_clusters=3, random_state=random_state).fit_predict(X_aniso)

plt.subplot(222)
plt.scatter(X_aniso[:, 0], X_aniso[:, 1], c=y_pred)
plt.title("Anisotropically Distributed Blobs")

# Different variance
X_varied, y_varied = make_blobs(n_samples=n_samples,
cluster_std=[1.0, 2.5, 0.5],
random_state=random_state)
y_pred = KMeans(n_clusters=3, random_state=random_state).fit_predict(X_varied)

plt.subplot(223)
plt.scatter(X_varied[:, 0], X_varied[:, 1], c=y_pred)
plt.title("Unequal Variance")

# Unevenly sized blobs
X_filtered = np.vstack((X[y == 0][:500], X[y == 1][:100], X[y == 2][:10]))
y_pred = KMeans(n_clusters=3,
random_state=random_state).fit_predict(X_filtered)

plt.subplot(224)
plt.scatter(X_filtered[:, 0], X_filtered[:, 1], c=y_pred)
plt.title("Unevenly Sized Blobs")

plt.show()

Total running time of the script: ( 0 minutes 0.412 seconds)

9.4 Segmenting the picture of a raccoon face in regions

This example uses Spectral clustering on a graph created from voxel-to-voxel difference on an image to break this image into multiple partly-homogeneous regions.

This procedure (spectral clustering on an image) is an efficient approximate solution for finding normalized graph cuts.

There are two options to assign labels:

- with ‘kmeans’ spectral clustering will cluster samples in the embedding space using a kmeans algorithm
- whereas ‘discrete’ will iteratively search for the closest partition space to the embedding space.

print("_doc_")

# Author: Gael Varoquaux <gael.varoquaux@normalesup.org>, Brian Cheung
import time

import numpy as np
import scipy as sp
import matplotlib.pyplot as plt

from sklearn.feature_extraction import image
from sklearn.cluster import spectral_clustering

# load the raccoon face as a numpy array
try:
    # SciPy >= 0.16 have face in misc
    from scipy.misc import face
    face = face(gray=True)
except ImportError:
    face = sp.face(gray=True)

# Resize it to 10% of the original size to speed up the processing
face = sp.misc.imresize(face, 0.10) / 255.

# Convert the image into a graph with the value of the gradient on the edges.
graph = image.img_to_graph(face)

# Take a decreasing function of the gradient: an exponential
# The smaller beta is, the more independent the segmentation is of the actual image. For beta=1, the segmentation is close to a voronoi
beta = 5
eps = 1e-6
graph.data = np.exp(-beta * graph.data / graph.data.std()) + eps

# Apply spectral clustering (this step goes much faster if you have pyamg installed)
N_REGIONS = 25

Visualize the resulting regions

for assign_labels in ('kmeans', 'discretize'):
    t0 = time.time()
    labels = spectral_clustering(graph, n_clusters=N_REGIONS,
                                assign_labels=assign_labels, random_state=1)
    t1 = time.time()
    labels = labels.reshape(face.shape)

    plt.figure(figsize=(5, 5))
    plt.imshow(face, cmap=plt.cm.gray)
    for l in range(N_REGIONS):
        plt.contour(labels == l, contours=1,
                    colors=plt.cm.spectral(l / float(N_REGIONS)))
    plt.xticks(())
    plt.yticks(()
    title = 'Spectral clustering: %s, %.2fs' % (assign_labels, (t1 - t0))
    print(title)
    plt.title(title)
    plt.show()
Out:

Spectral clustering: kmeans, 6.68s
Spectral clustering: discretize, 5.83s

Total running time of the script: ( 0 minutes 13.384 seconds)

9.5 A demo of structured Ward hierarchical clustering on a raccoon face image

Compute the segmentation of a 2D image with Ward hierarchical clustering. The clustering is spatially constrained in order for each segmented region to be in one piece.
Out:

```
Compute structured hierarchical clustering...
Elapsed time: 0.6927416324615479
Number of pixels: 7752
Number of clusters: 15
```

```python
# Author : Vincent Michel, 2010
#         Alexandre Gramfort, 2011
# License: BSD 3 clause

print(__doc__)

import time as time
import numpy as np
import scipy as sp
import matplotlib.pyplot as plt
```

9.5. A demo of structured Ward hierarchical clustering on a raccoon face image
```python
from sklearn.feature_extraction.image import grid_to_graph
from sklearn.cluster import AgglomerativeClustering

# Generate data
try:
    # SciPy >= 0.16 have face in misc
    from scipy.misc import face
    face = face(gray=True)
except ImportError:
    face = sp.face(gray=True)

# Resize it to 10% of the original size to speed up the processing
face = sp.misc.imresize(face, 0.10) / 255.
X = np.reshape(face, (-1, 1))

# Define the structure A of the data. Pixels connected to their neighbors.
connectivity = grid_to_graph(*face.shape)

# Compute clustering
print("Compute structured hierarchical clustering...")
st = time.time()
n_clusters = 15  # number of regions
ward = AgglomerativeClustering(n_clusters=n_clusters, linkage='ward',
                               connectivity=connectivity)
ward.fit(X)
label = np.reshape(ward.labels_, face.shape)
print("Elapsed time: ", time.time() - st)
p redundant
print("Number of clusters: ", np.unique(label).size)

# Plot the results on an image
plt.figure(figsize=(5, 5))
plt.imshow(face, cmap=plt.cm.gray)
for l in range(n_clusters):
    plt.contour(label == l, contours=1, colors=[plt.cm.spectral(l / float(n_clusters)), ])
plt.xticks(())
plt.yticks(())
plt.show()
```

**Total running time of the script:** ( 0 minutes 1.034 seconds)

### 9.6 Online learning of a dictionary of parts of faces

This example uses a large dataset of faces to learn a set of 20 x 20 images patches that constitute faces.

From the programming standpoint, it is interesting because it shows how to use the online API of the scikit-learn to process a very large dataset by chunks. The way we proceed is that we load an image at a time and extract randomly 50 patches from this image. Once we have accumulated 500 of these patches (using 10 images), we run the `partial_fit` method of the online KMeans object, MiniBatchKMeans.
The verbose setting on the MiniBatchKMeans enables us to see that some clusters are reassigned during the successive calls to partial-fit. This is because the number of patches that they represent has become too low, and it is better to choose a random new cluster.

```
Learning the dictionary...
Partial fit of 100 out of 2400
Partial fit of 200 out of 2400
Partial fit of 300 out of 2400
Partial fit of 400 out of 2400
Partial fit of 500 out of 2400
Partial fit of 600 out of 2400
Partial fit of 700 out of 2400
Partial fit of 800 out of 2400
Partial fit of 900 out of 2400
Partial fit of 1000 out of 2400
Partial fit of 1100 out of 2400
Partial fit of 1200 out of 2400
Partial fit of 1300 out of 2400
Partial fit of 1400 out of 2400
Partial fit of 1500 out of 2400
Partial fit of 1600 out of 2400
Partial fit of 1700 out of 2400
Partial fit of 1800 out of 2400
Partial fit of 1900 out of 2400
Partial fit of 2000 out of 2400
Partial fit of 2100 out of 2400
Partial fit of 2200 out of 2400
Partial fit of 2300 out of 2400
Partial fit of 2400 out of 2400
```

9.6. Online learning of a dictionary of parts of faces
print(__doc__)

import time

import matplotlib.pyplot as plt
import numpy as np

from sklearn import datasets
from sklearn.cluster import MiniBatchKMeans
from sklearn.feature_extraction.image import extract_patches_2d

faces = datasets.fetch_olivetti_faces()

# #############################################################################
# Learn the dictionary of images

print('Learning the dictionary... ')
rng = np.random.RandomState(0)
kmeans = MiniBatchKMeans(n_clusters=81, random_state=rng, verbose=True)
patch_size = (20, 20)
buffer = []
t0 = time.time()

# The online learning part: cycle over the whole dataset 6 times
index = 0
for _ in range(6):
    for img in faces.images:
        data = extract_patches_2d(img, patch_size, max_patches=50,
                                   random_state=rng)
        data = np.reshape(data, (len(data), -1))
        buffer.append(data)
        index += 1
        if index % 10 == 0:
            data = np.concatenate(buffer, axis=0)
            data -= np.mean(data, axis=0)
            data /= np.std(data, axis=0)
            kmeans.partial_fit(data)
            buffer = []
        if index % 100 == 0:
            print('Partial fit of %i out of %i' % (index, 6 * len(faces.images)))

dt = time.time() - t0
print('done in %.2fs.' % dt)

# #############################################################################
# Plot the results

plt.figure(figsize=(4.2, 4))
for i, patch in enumerate(kmeans.cluster_centers_):
```python
plt.subplot(9, 9, i + 1)
plt.imshow(patch.reshape(patch_size), cmap=plt.cm.gray,
           interpolation='nearest')
plt.xticks(()
plt.yticks(()
plt.suptitle('Patches of faces

Train time %.1fs on %d patches' %
             (dt, 8 * len(faces.images)), fontsize=16)
plt.subplots_adjust(0.08, 0.02, 0.92, 0.85, 0.08, 0.23)
plt.show()
```

Total running time of the script: ( 0 minutes 6.733 seconds)

## 9.7 Vector Quantization Example

Face, a 1024 x 768 size image of a raccoon face, is used here to illustrate how $k$-means is used for vector quantization.

```python
print(__doc__)
```

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause
import numpy as np
import scipy as sp
import matplotlib.pyplot as plt
from sklearn import cluster

try:  # SciPy >= 0.16 have face in misc
    from scipy.misc import face
    face = face(gray=True)
except ImportError:
    face = sp.face(gray=True)

n_clusters = 5
np.random.seed(0)
X = face.reshape((-1, 1))  # We need an (n_sample, n_feature) array
k_means = cluster.KMeans(n_clusters=n_clusters, n_init=4)
k_means.fit(X)
values = k_means.cluster_centers_.squeeze()
labels = k_means.labels_

# create an array from labels and values
face_compressed = np.choose(labels, values)
face_compressed.shape = face.shape

vmin = face.min()
vmax = face.max()

# original face
plt.figure(1, figsize=(3, 2.2))
plt.imshow(face, cmap=plt.cm.gray, vmin=vmin, vmax=256)

# compressed face
plt.figure(2, figsize=(3, 2.2))
plt.imshow(face_compressed, cmap=plt.cm.gray, vmin=vmin, vmax=vmax)

# equal bins face
regular_values = np.linspace(0, 256, n_clusters + 1)
regular_labels = np.searchsorted(regular_values, face) - 1
regular_values = .5 * (regular_values[1:] + regular_values[:-1])  # mean
regular_face = np.choose(regular_labels.ravel(), regular_values, mode="clip")
regular_face.shape = face.shape
plt.figure(3, figsize=(3, 2.2))
plt.imshow(regular_face, cmap=plt.cm.gray, vmin=vmin, vmax=vmax)

# histogram
plt.figure(4, figsize=(3, 2.2))
plt.clf()
plt.axes([.01, .01, .98, .98])
plt.hist(X, bins=256, color='.5', edgecolor='.5')
plt.xticks(regular_values)
plt.yticks([])

for center_1, center_2 in zip(values[:-1], values[1:]):
    plt.axvline(.5 * (center_1 + center_2), color='b')

for center_1, center_2 in zip(regular_values[:-1], regular_values[1:]):
    plt.axvline(.5 * (center_1 + center_2), color='b')
9.8 Agglomerative clustering with and without structure

This example shows the effect of imposing a connectivity graph to capture local structure in the data. The graph is simply the graph of 20 nearest neighbors.

Two consequences of imposing a connectivity can be seen. First clustering with a connectivity matrix is much faster. Second, when using a connectivity matrix, average and complete linkage are unstable and tend to create a few clusters that grow very quickly. Indeed, average and complete linkage fight this percolation behavior by considering all the distances between two clusters when merging them. The connectivity graph breaks this mechanism. This effect is more pronounced for very sparse graphs (try decreasing the number of neighbors in kneighbors_graph) and with complete linkage. In particular, having a very small number of neighbors in the graph, imposes a geometry that is close to that of single linkage, which is well known to have this percolation instability.
```python
import time
import matplotlib.pyplot as plt
import numpy as np
from sklearn.cluster import AgglomerativeClustering
from sklearn.neighbors import kneighbors_graph

# Generate sample data
n_samples = 1500
np.random.seed(0)
t = 1.5 * np.pi * (1 + 3 * np.random.rand(1, n_samples))
x = t * np.cos(t)
y = t * np.sin(t)
X = np.concatenate((x, y))
X += .7 * np.random.randn(2, n_samples)
X = X.T

# Create a graph capturing local connectivity. Larger number of neighbors
# will give more homogeneous clusters to the cost of computation
# time. A very large number of neighbors gives more evenly distributed
# cluster sizes, but may not impose the local manifold structure of
# the data
knn_graph = kneighbors_graph(X, 30, include_self=False)

for connectivity in (None, knn_graph):
    for n_clusters in (30, 3):
        plt.figure(figsize=(10, 4))
```

---

# Authors: Gael Varoquaux, Nelle Varoquaux
# License: BSD 3 clause
for index, linkage in enumerate(('average', 'complete', 'ward')):
    plt.subplot(1, 3, index + 1)
    model = AgglomerativeClustering(linkage=linkage,
                                      connectivity=connectivity,
                                      n_clusters=n_clusters)
    t0 = time.time()
    model.fit(X)
    elapsed_time = time.time() - t0
    plt.scatter(X[:, 0], X[:, 1], c=model.labels_,
                 cmap=plt.cm.spectral)
    plt.title('linkage=%s (time %.2f s)' % (linkage, elapsed_time),
              fontdict=dict(verticalalignment='top'))
    plt.axis('equal')
    plt.axis('off')
    plt.subplots_adjust(bottom=0, top=.89, wspace=0,
                        left=0, right=1)
    plt.suptitle('n_clusters=%i, connectivity=%r' %
                 (n_clusters, connectivity is not None), size=17)
plt.show()

Total running time of the script: ( 0 minutes 2.337 seconds)

## 9.9 Demo of affinity propagation clustering algorithm

Estimated number of clusters: 3

Homogeneity: 0.872
Completeness: 0.872
V-measure: 0.872
Adjusted Rand Index: 0.912
Adjusted Mutual Information: 0.871
Silhouette Coefficient: 0.753

print(__doc__)

from sklearn.cluster import AffinityPropagation
from sklearn import metrics
from sklearn.datasets.samples_generator import make_blobs

# Generate sample data
centers = [[1, 1], [-1, -1], [1, -1]]
X, labels_true = make_blobs(n_samples=300, centers=centers, cluster_std=0.5,
                           random_state=0)
# Compute Affinity Propagation
af = AffinityPropagation(preference=-50).fit(X)
cluster_centers_indices = af.cluster_centers_indices_
labels = af.labels_

n_clusters_ = len(cluster_centers_indices)

print('Estimated number of clusters: %d' % n_clusters_)
print("Homogeneity: %0.3f" % metrics.homogeneity_score(labels_true, labels))
print("Completeness: %0.3f" % metrics.completeness_score(labels_true, labels))
print("V-measure: %0.3f" % metrics.v_measure_score(labels_true, labels))
print("Adjusted Rand Index: %0.3f" % metrics.adjusted_rand_score(labels_true, labels))
print("Adjusted Mutual Information: %0.3f" % metrics.adjusted_mutual_info_score(labels_true, labels))
print("Silhouette Coefficient: %0.3f" % metrics.silhouette_score(X, labels, metric='sqeuclidean'))

# Plot result
import matplotlib.pyplot as plt
from itertools import cycle
plt.close('all')
plt.figure(1)
plt.clf()
colors = cycle('bgrcmykbgrcmykbgrcmykbgrcmyk')
for k, col in zip(range(n_clusters_), colors):
    class_members = labels == k
    cluster_center = X[cluster_centers_indices[k]]
    plt.plot(X[class_members, 0], X[class_members, 1], col + '.')
    plt.plot(cluster_center[0], cluster_center[1], 'o', markerfacecolor=col,
             markeredgecolor='k', markersize=14)
    for x in X[class_members]:
        plt.plot([cluster_center[0], x[0]], [cluster_center[1], x[1]], col)

plt.title('Estimated number of clusters: %d' % n_clusters_)
plt.show()

Total running time of the script: ( 0 minutes 0.758 seconds)

9.10 Various Agglomerative Clustering on a 2D embedding of digits

An illustration of various linkage option for agglomerative clustering on a 2D embedding of the digits dataset.

The goal of this example is to show intuitively how the metrics behave, and not to find good clusters for the digits. This is why the example works on a 2D embedding.

What this example shows us is the behavior “rich getting richer” of agglomerative clustering that tends to create uneven cluster sizes. This behavior is especially pronounced for the average linkage strategy, that ends up with a couple of singleton clusters.
Out:

Computing embedding
Done.
ward : 0.38s
average : 0.34s
complete : 0.30s

# Authors: Gael Varoquaux
# License: BSD 3 clause (C) INRIA 2014

print(__doc__)
from time import time
import numpy as np
from scipy import ndimage
from matplotlib import pyplot as plt
from sklearn import manifold, datasets

digits = datasets.load_digits(n_class=10)
X = digits.data
y = digits.target
n_samples, n_features = X.shape

np.random.seed(0)
def nudge_images(X, y):
    # Having a larger dataset shows more clearly the behavior of the
    # methods, but we multiply the size of the dataset only by 2, as the
    # cost of the hierarchical clustering methods are strongly
    # super-linear in n_samples
    shift = lambda x: ndimage.shift(x.reshape((8, 8)),
                               0.3 * np.random.normal(size=2),
                               mode='constant',
                               ).ravel()
    X = np.concatenate([X, np.apply_along_axis(shift, 1, X)])
    Y = np.concatenate([y, y], axis=0)
    return X, Y

X, y = nudge_images(X, y)

#--------------------------------------------------------------------------------
# Visualize the clustering
def plot_clustering(X_red, X, labels, title=None):
x_min, x_max = np.min(X_red, axis=0), np.max(X_red, axis=0)
X_red = (X_red - x_min) / (x_max - x_min)

plt.figure(figsize=(6, 4))
for i in range(X_red.shape[0]):
    plt.text(X_red[i, 0], X_red[i, 1], str(y[i]),
             color=plt.cm.spectral(labels[i] / 10.),
             fontdict={'weight': 'bold', 'size': 9})

plt.xticks([])
plt.yticks([])
if title is not None:
    plt.title(title, size=17)
plt.axis('off')
plt.tight_layout()

#--------------------------------------------------------------------------------
# 2D embedding of the digits dataset
print("Computing embedding")
X_red = manifold.SpectralEmbedding(n_components=2).fit_transform(X)
print("Done.")

from sklearn.cluster import AgglomerativeClustering

for linkage in ('ward', 'average', 'complete'):
```
clustering = AgglomerativeClustering(linkage=linkage, n_clusters=10)
t0 = time()
clustering.fit(X_red)
print("%s : %.2f s" % (linkage, time() - t0))
plot_clustering(X_red, X, clustering.labels_, "%s linkage" % linkage)
plt.show()
```

**Total running time of the script:** ( 0 minutes 20.142 seconds)

### 9.11 K-means Clustering

The plots display firstly what a K-means algorithm would yield using three clusters. It is then shown what the effect of a bad initialization is on the classification process: By setting n_init to only 1 (default is 10), the amount of times that the algorithm will be run with different centroid seeds is reduced. The next plot displays what using eight clusters would deliver and finally the ground truth.
```python
print(__doc__)

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
# Though the following import is not directly being used, it is required
# for 3D projection to work
from mpl_toolkits.mplot3d import Axes3D
from sklearn.cluster import KMeans
from sklearn import datasets
np.random.seed(5)
iris = datasets.load_iris()
X = iris.data
y = iris.target
estimators = [('k_means_iris_8', KMeans(n_clusters=8)),
               ('k_means_iris_3', KMeans(n_clusters=3)),
               ('k_means_iris_bad_init', KMeans(n_clusters=3, n_init=1,
                                                  init='random'))]
fignum = 1
titles = ['8 clusters', '3 clusters', '3 clusters, bad initialization']
for name, est in estimators:
    fig = plt.figure(fignum, figsize=(4, 3))
    ax = Axes3D(fig, rect=[0, 0, .95, 1], elev=48, azim=134)
    est.fit(X)
    labels = est.labels_
    ax.scatter(X[:, 3], X[:, 0], X[:, 2],
               c=labels.astype(np.float), edgecolor='k')
    ax.w_xaxis.set_ticklabels([])
    ax.w_yaxis.set_ticklabels([])
    ax.w_zaxis.set_ticklabels([])
    ax.set_xlabel('Petal width')
    ax.set_ylabel('Sepal length')
    ax.set_zlabel('Petal length')
    ax.set_title(titles[fignum - 1])
    ax.dist = 12
    fignum = fignum + 1
```

9.11. K-means Clustering
9.12 Spectral clustering for image segmentation

In this example, an image with connected circles is generated and spectral clustering is used to separate the circles.

In these settings, the Spectral clustering approach solves the problem known as 'normalized graph cuts': the image is seen as a graph of connected voxels, and the spectral clustering algorithm amounts to choosing graph cuts defining regions while minimizing the ratio of the gradient along the cut, and the volume of the region.

As the algorithm tries to balance the volume (i.e., balance the region sizes), if we take circles with different sizes, the segmentation fails.

In addition, as there is no useful information in the intensity of the image, or its gradient, we choose to perform the spectral clustering on a graph that is only weakly informed by the gradient. This is close to performing a Voronoi partition of the graph.

In addition, we use the mask of the objects to restrict the graph to the outline of the objects. In this example, we are interested in separating the objects one from the other, and not from the background.
# Authors: Emmanuelle Gouillart <emmanuelle.gouillart@normalesup.org>
# Gael Varoquaux <gael.varoquaux@normalesup.org>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.feature_extraction import image
from sklearn.cluster import spectral_clustering

l = 100
x, y = np.indices((l, l))
center1 = (28, 24)
center2 = (40, 50)
center3 = (67, 58)
center4 = (24, 70)
radius1, radius2, radius3, radius4 = 16, 14, 15, 14

circle1 = (x - center1[0]) ** 2 + (y - center1[1]) ** 2 < radius1 ** 2
circle2 = (x - center2[0]) ** 2 + (y - center2[1]) ** 2 < radius2 ** 2
circle3 = (x - center3[0]) ** 2 + (y - center3[1]) ** 2 < radius3 ** 2
circle4 = (x - center4[0]) ** 2 + (y - center4[1]) ** 2 < radius4 ** 2

img = circle1 + circle2 + circle3 + circle4

# Convert the image into a graph with the value of the gradient on the edges.
graph = image.img_to_graph(img, mask=mask)
# Take a decreasing function of the gradient: we take it weakly
# dependent from the gradient the segmentation is close to a voronoi
graph.data = np.exp(-graph.data / graph.data.std())

# Force the solver to be arpack, since amg is numerically
# unstable on this example
labels = spectral_clustering(graph, n_clusters=4, eigen_solver='arpack')
label_im = -np.ones(mask.shape)
label_im[mask] = labels

plt.matshow(img)
plt.matshow(label_im)

# 2 circles
img = circle1 + circle2
mask = img.astype(bool)
img = img.astype(float)

img += 1 + 0.2 * np.random.randn(*img.shape)

graph = image.img_to_graph(img, mask=mask)
graph.data = np.exp(-graph.data / graph.data.std())

labels = spectral_clustering(graph, n_clusters=2, eigen_solver='arpack')
label_im = -np.ones(mask.shape)
label_im[mask] = labels

plt.matshow(img)
plt.matshow(label_im)

plt.show()

Total running time of the script: ( 0 minutes 1.212 seconds)

9.13 Demo of DBSCAN clustering algorithm

Finds core samples of high density and expands clusters from them.
Estimated number of clusters: 3

Out:

Estimated number of clusters: 3
Homogeneity: 0.953
Completeness: 0.883
V-measure: 0.917
Adjusted Rand Index: 0.952
Adjusted Mutual Information: 0.883
Silhouette Coefficient: 0.626

print(__doc__)

import numpy as np

from sklearn.cluster import DBSCAN
from sklearn import metrics
from sklearn.datasets.samples_generator import make_blobs
from sklearn.preprocessing import StandardScaler
Generate sample data

```python
centers = [[1, 1], [-1, -1], [1, -1]]
X, labels_true = make_blobs(n_samples=750, centers=centers, cluster_std=0.4, random_state=0)

X = StandardScaler().fit_transform(X)
```

Compute DBSCAN

```python
db = DBSCAN(eps=0.3, min_samples=10).fit(X)
core_samples_mask = np.zeros_like(db.labels_, dtype=bool)
core_samples_mask[db.core_sample_indices_] = True
labels = db.labels_
```

Number of clusters in labels, ignoring noise if present.

```python
n_clusters_ = len(set(labels)) - (1 if -1 in labels else 0)
```

Plot result

```python
import matplotlib.pyplot as plt

# Black removed and is used for noise instead.
unique_labels = set(labels)
colors = [plt.cm.Spectral(each) for each in np.linspace(0, 1, len(unique_labels))]
for k, col in zip(unique_labels, colors):
    if k == -1:
        # Black used for noise.
        col = [0, 0, 0, 1]
    class_member_mask = (labels == k)
    xy = X[class_member_mask & core_samples_mask]
    plt.plot(xy[:, 0], xy[:, 1], 'o', markerfacecolor=tuple(col), markeredgecolor='k', markersize=14)
    xy = X[class_member_mask & ~core_samples_mask]
    plt.plot(xy[:, 0], xy[:, 1], 'o', markerfacecolor=tuple(col), markeredgecolor='k', markersize=6)
plt.title('Estimated number of clusters: %d' % n_clusters_)
plt.show()
```

Total running time of the script: ( 0 minutes 0.100 seconds)
9.14 Color Quantization using K-Means

Performs a pixel-wise Vector Quantization (VQ) of an image of the summer palace (China), reducing the number of colors required to show the image from 96,615 unique colors to 64, while preserving the overall appearance quality.

In this example, pixels are represented in a 3D-space and K-means is used to find 64 color clusters. In the image processing literature, the codebook obtained from K-means (the cluster centers) is called the color palette. Using a single byte, up to 256 colors can be addressed, whereas an RGB encoding requires 3 bytes per pixel. The GIF file format, for example, uses such a palette.

For comparison, a quantized image using a random codebook (colors picked up randomly) is also shown.
# Authors: Robert Layton <robertlayton@gmail.com>
#        Olivier Grisel <olivier.grisel@ensta.org>
#        Mathieu Blondel <mathieu@mblondel.org>
#
# License: BSD 3 clause

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn.cluster import KMeans
from sklearn.metrics import pairwise_distances_argmin
from sklearn.datasets import load_sample_image
from sklearn.utils import shuffle
from time import time

n_colors = 64

# Load the Summer Palace photo
china = load_sample_image("china.jpg")

# Convert to floats instead of the default 8 bits integer coding. Dividing by
# 255 is important so that plt.imshow behaves works well on float data (need to
# be in the range [0-1])
china = np.array(china, dtype=np.float64) / 255

# Load Image and transform to a 2D numpy array.
w, h, d = original_shape = tuple(china.shape)
assert d == 3
image_array = np.reshape(china, (w * h, d))

print("Fitting model on a small sub-sample of the data")
t0 = time()
image_array_sample = shuffle(image_array, random_state=0)[:1000]
kmeans = KMeans(n_clusters=n_colors, random_state=0).fit(image_array_sample)
print("done in %0.3fs." % (time() - t0))

# Get labels for all points
print("Predicting color indices on the full image (k-means")
t0 = time()
labels = kmeans.predict(image_array)
print("done in %0.3fs." % (time() - t0))

codebook_random = shuffle(image_array, random_state=0)[:n_colors + 1]
print("Predicting color indices on the full image (random)")
t0 = time()
labels_random = pairwise_distances_argmin(codebook_random,
    image_array,
    axis=0)
print("done in %0.3f s." % (time() - t0))

def recreate_image(codebook, labels, w, h):
    """Recreate the (compressed) image from the code book & labels""
    d = codebook.shape[1]
    image = np.zeros((w, h, d))
    label_idx = 0
    for i in range(w):
        for j in range(h):
            image[i][j] = codebook[labels[label_idx]]
            label_idx += 1
    return image

# Display all results, alongside original image
plt.figure(1)
plt.clf()
plt.axis('off')
plt.title('Original image (96,615 colors)')
plt.imshow(china)
plt.figure(2)
plt.clf()
plt.axis('off')
plt.title('Quantized image (64 colors, K-Means)')
plt.imshow(recreate_image(kmeans.cluster_centers_, labels, w, h))
plt.figure(3)
plt.clf()
plt.axis('off')
plt.title('Quantized image (64 colors, Random)')
plt.imshow(recreate_image(codebook_random, labels_random, w, h))
plt.show()

Total running time of the script: ( 0 minutes 1.859 seconds)

9.15 Hierarchical clustering: structured vs unstructured ward

Example builds a swiss roll dataset and runs hierarchical clustering on their position.

For more information, see Hierarchical clustering.

In a first step, the hierarchical clustering is performed without connectivity constraints on the structure and is solely based on distance, whereas in a second step the clustering is restricted to the k-Nearest Neighbors graph: it's a hierarchical clustering with structure prior.

Some of the clusters learned without connectivity constraints do not respect the structure of the swiss roll and extend across different folds of the manifolds. On the opposite, when opposing connectivity constraints, the clusters form a nice parcellation of the swiss roll.
Out:

```
Compute unstructured hierarchical clustering...
Elapsed time: 0.05s
Number of points: 1500
Compute structured hierarchical clustering...
Elapsed time: 0.13s
Number of points: 1500
```

# Authors : Vincent Michel, 2010
# Alexandre Gramfort, 2010
# Gael Varoquaux, 2010
# License: BSD 3 clause

```
print(__doc__)

import time as time
import numpy as np
import matplotlib.pyplot as plt
import mpl_toolkits.mplot3d.axes3d as p3
from sklearn.cluster import AgglomerativeClustering
from sklearn.datasets.samples_generator import make_swiss_roll
```
# #############################################################################
# Generate data (swiss roll dataset)
import numpy as np
n_samples = 1500
noise = 0.05
X, _ = make_swiss_roll(n_samples, noise)
# Make it thinner
X[:, 1] *= .5

# #############################################################################
# Compute clustering
print("Compute unstructured hierarchical clustering...")
st = time.time()
ward = AgglomerativeClustering(n_clusters=6, linkage='ward').fit(X)
elapsed_time = time.time() - st
label = ward.labels_
print("Elapsed time: %2.2fs" % elapsed_time)
print("Number of points: %i" % label.size)

# #############################################################################
# Plot result
fig = plt.figure()
ax = p3.Axes3D(fig)
ax.view_init(7, -80)
for l in np.unique(label):
    ax.scatter(X[label == l, 0], X[label == l, 1], X[label == l, 2],
               color=plt.cm.jet(np.float(l) / np.max(label + 1)),
               s=20, edgecolor='k')
plt.title('Without connectivity constraints (time %.2fs)' % elapsed_time)

# #############################################################################
# Define the structure A of the data. Here a 10 nearest neighbors
from sklearn.neighbors import kneighbors_graph
connectivity = kneighbors_graph(X, n_neighbors=10, include_self=False)

# #############################################################################
# Compute clustering
print("Compute structured hierarchical clustering...")
st = time.time()
ward = AgglomerativeClustering(n_clusters=6, connectivity=connectivity,
                               linkage='ward').fit(X)
elapsed_time = time.time() - st
label = ward.labels_
print("Elapsed time: %2.2fs" % elapsed_time)
print("Number of points: %i" % label.size)

# #############################################################################
# Plot result
fig = plt.figure()
ax = p3.Axes3D(fig)
ax.view_init(7, -80)
for l in np.unique(label):
    ax.scatter(X[label == l, 0], X[label == l, 1], X[label == l, 2],
               color=plt.cm.jet(float(l) / np.max(label + 1)),
               s=20, edgecolor='k')
plt.title('With connectivity constraints (time %.2fs)' % elapsed_time)
9.16 Agglomerative clustering with different metrics

Demonstrates the effect of different metrics on the hierarchical clustering.

The example is engineered to show the effect of the choice of different metrics. It is applied to waveforms, which can be seen as high-dimensional vector. Indeed, the difference between metrics is usually more pronounced in high dimension (in particular for euclidean and cityblock).

We generate data from three groups of waveforms. Two of the waveforms (waveform 1 and waveform 2) are proportional one to the other. The cosine distance is invariant to a scaling of the data, as a result, it cannot distinguish these two waveforms. Thus even with no noise, clustering using this distance will not separate out waveform 1 and 2.

We add observation noise to these waveforms. We generate very sparse noise: only 6% of the time points contain noise. As a result, the l1 norm of this noise (ie “cityblock” distance) is much smaller than it’s l2 norm (“euclidean” distance). This can be seen on the inter-class distance matrices: the values on the diagonal, that characterize the spread of the class, are much bigger for the Euclidean distance than for the cityblock distance.

When we apply clustering to the data, we find that the clustering reflects what was in the distance matrices. Indeed, for the Euclidean distance, the classes are ill-separated because of the noise, and thus the clustering does not separate the waveforms. For the cityblock distance, the separation is good and the waveform classes are recovered. Finally, the cosine distance does not separate at all waveform 1 and 2, thus the clustering puts them in the same cluster.
Chapter 9. Clustering

Interclass euclidean distances

Interclass cityblock distances

AgglomerativeClustering(affinity=cosine)
import matplotlib.pyplot as plt
import numpy as np

from sklearn.cluster import AgglomerativeClustering
from sklearn.metrics import pairwise_distances

np.random.seed(0)

# Generate waveform data
n_features = 2000
t = np.pi * np.linspace(0, 1, n_features)

def sqr(x):
    return np.sign(np.cos(x))

X = list()
y = list()

for i, (phi, a) in enumerate(([.5, .15], [.5, .6], [.3, .2])):
    for _ in range(30):
        phase_noise = .01 * np.random.normal()
        amplitude_noise = .04 * np.random.normal()
        additional_noise = 1 - 2 * np.random.rand(n_features)
        # Make the noise sparse
additional_noise[np.abs(additional_noise) < .997] = 0

X.append(12 * ((a + amplitude_noise)
        * (sqr(6 * (t + phi + phase_noise)))
        + additional_noise))
y.append(i)

X = np.array(X)
y = np.array(y)
n_clusters = 3
labels = ('Waveform 1', 'Waveform 2', 'Waveform 3')

# Plot the ground-truth labelling
plt.figure()
plt.plot([0, 0, 1, 1])
for l, c, n in zip(range(n_clusters), 'rgb', labels):
    lines = plt.plot(X[y == l].T, c=c, alpha=.5)
    lines[0].set_label(n)
plt.legend(loc='best')
plt.axis('tight')
plt.axis('off')
plt.suptitle("Ground truth", size=20)

# Plot the distances
for index, metric in enumerate(['cosine', 'euclidean', 'cityblock']):
    avg_dist = np.zeros((n_clusters, n_clusters))
    plt.figure(figsize=(5, 4.5))
    for i in range(n_clusters):
        for j in range(n_clusters):
            avg_dist[i, j] = pairwise_distances(X[y == i], X[y == j],
                                                metric=metric).mean()
    avg_dist /= avg_dist.max()
    for i in range(n_clusters):
        for j in range(n_clusters):
            plt.text(i, j, '%5.3f' % avg_dist[i, j],
                     verticalalignment='center',
                     horizontalalignment='center')
    plt.imshow(avg_dist, interpolation='nearest', cmap=plt.cm.gnuplot2,
               vmin=0)
    plt.xticks(range(n_clusters), labels, rotation=45)
    plt.yticks(range(n_clusters), labels)
    plt.colorbar()
    plt.suptitle("Interclass %s distances" % metric, size=18)
    plt.tight_layout()

# Plot clustering results
for index, metric in enumerate(['cosine', 'euclidean', 'cityblock']):
    model = AgglomerativeClustering(n_clusters=n_clusters,
                                     linkage="average", affinity=metric)
    model.fit(X)
9.17 Compare BIRCH and MiniBatchKMeans

This example compares the timing of Birch (with and without the global clustering step) and MiniBatchKMeans on a synthetic dataset having 100,000 samples and 2 features generated using make_blobs.

If `n_clusters` is set to None, the data is reduced from 100,000 samples to a set of 158 clusters. This can be viewed as a preprocessing step before the final (global) clustering step that further reduces these 158 clusters to 100 clusters.

Out:

Birch without **global** clustering as the final step took 6.06 seconds
n_clusters : 158
Birch with **global** clustering as the final step took 5.97 seconds
n_clusters : 100
Time taken to run MiniBatchKMeans 6.15 seconds
from time import time
import numpy as np
import matplotlib.pyplot as plt
import matplotlib.colors as colors

from sklearn.preprocessing import StandardScaler
from sklearn.cluster import Birch, MiniBatchKMeans
from sklearn.datasets.samples_generator import make_blobs

# Generate centers for the blobs so that it forms a 10 X 10 grid.
xx = np.linspace(-22, 22, 10)
yy = np.linspace(-22, 22, 10)
xx, yy = np.meshgrid(xx, yy)
n_centres = np.hstack((np.ravel(xx)[:, np.newaxis], np.ravel(yy)[:, np.newaxis]))

# Generate blobs to do a comparison between MiniBatchKMeans and Birch.
X, y = make_blobs(n_samples=100000, centers=n_centres, random_state=0)

# Use all colors that matplotlib provides by default.
colors_ = cycle(colors.cnames.keys())

fig = plt.figure(figsize=(12, 4))
fig.subplots_adjust(left=0.04, right=0.98, bottom=0.1, top=0.9)

# Compute clustering with Birch with and without the final clustering step
# and plot.
birch_models = [Birch(threshold=1.7, n_clusters=None),
                Birch(threshold=1.7, n_clusters=100)]
final_step = ['without global clustering', 'with global clustering']

for ind, (birch_model, info) in enumerate(zip(birch_models, final_step)):
    t = time()
    birch_model.fit(X)
time_ = time() - t
    print("Birch %s as the final step took %0.2f seconds" % (info, (time() - t)))

    # Plot result
    labels = birch_model.labels_
    centroids = birch_model.subcluster_centers_
    n_clusters = np.unique(labels).size
    print("n_clusters : %d" % n_clusters)

    ax = fig.add_subplot(1, 3, ind + 1)
    for this_centroid, k, col in zip(centroids, range(n_clusters), colors_):
        mask = labels == k
        ax.scatter(X[mask, 0], X[mask, 1], c='w', edgecolor=col, marker='.', alpha=0.5)
        if birch_model.n_clusters is None:
            ax.scatter(this_centroid[0], this_centroid[1], marker='+', c='k', s=25)
    ax.set_xlim([-25, 25])
    ax.set_ylim([-25, 25])
    ax.set_autoscaley_on(False)
    ax.set_title('Birch %s' % info)
# Compute clustering with MiniBatchKMeans.

```
mbk = MiniBatchKMeans(init='k-means++', n_clusters=100, batch_size=100,
                     n_init=10, max_no_improvement=10, verbose=0,
                     random_state=0)

t0 = time()
mbk.fit(X)
t_mini_batch = time() - t0
print("Time taken to run MiniBatchKMeans \$0.2f seconds" % t_mini_batch)
mbk_means_labels_unique = np.unique(mbk.labels_)

for this_centroid, k, col in zip(mbk.cluster_centers_, range(n_clusters), colors_):
    mask = mbk.labels_ == k
    ax.scatter(X[mask, 0], X[mask, 1], marker='.',
               c='w', edgecolor=col, alpha=0.5)
    ax.scatter(this_centroid[0], this_centroid[1], marker='+',
               c='k', s=25)
ax.set_xlim([-25, 25])
ax.set_ylim([-25, 25])
ax.set_title("MiniBatchKMeans")
ax.set_autoscaley_on(False)
plt.show()
```

**Total running time of the script:** ( 0 minutes 21.235 seconds)

## 9.18 Empirical evaluation of the impact of k-means initialization

Evaluate the ability of k-means initializations strategies to make the algorithm convergence robust as measured by the relative standard deviation of the inertia of the clustering (i.e. the sum of squared distances to the nearest cluster center).

The first plot shows the best inertia reached for each combination of the model (KMeans or MiniBatchKMeans) and the init method (init="random" or init="kmeans++") for increasing values of the n_init parameter that controls the number of initializations.

The second plot demonstrate one single run of the MiniBatchKMeans estimator using a init="random" and n_init=1. This run leads to a bad convergence (local optimum) with estimated centers stuck between ground truth clusters.

The dataset used for evaluation is a 2D grid of isotropic Gaussian clusters widely spaced.
print(__doc__)

# Author: Olivier Grisel <olivier.grisel@ensta.org>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
import matplotlib.cm as cm

from sklearn.utils import shuffle
from sklearn.utils import check_random_state
from sklearn.cluster import MiniBatchKMeans
from sklearn.cluster import KMeans

random_state = np.random.RandomState(0)

# Number of run (with randomly generated dataset) for each strategy so as to be able to compute an estimate of the standard deviation
n_runs = 5

# k-means models can do several random inits so as to be able to trade CPU time for convergence robustness
n_init_range = np.array([1, 5, 10, 15, 20])

# Datasets generation parameters
n_samples_per_center = 100
grid_size = 3
scale = 0.1
n_clusters = grid_size ** 2
```python
def make_data(random_state, n_samples_per_center, grid_size, scale):
    random_state = check_random_state(random_state)
    centers = np.array([[i, j]
        for i in range(grid_size)
        for j in range(grid_size)])
    n_clusters_true, n_features = centers.shape
    noise = random_state.normal(
        scale=scale, size=(n_samples_per_center, centers.shape[1]))
    X = np.concatenate([c + noise for c in centers])
    y = np.concatenate([i * n_samples_per_center
        for i in range(n_clusters_true)])
    return shuffle(X, y, random_state=random_state)
```

# Part 1: Quantitative evaluation of various init methods

```python
plt.figure()
plots = []
legends = []

cases = [
    (KMeans, 'k-means++', {}),
    (KMeans, 'random', {}),
    (MiniBatchKMeans, 'k-means++', {'max_no_improvement': 3}),
    (MiniBatchKMeans, 'random', {'max_no_improvement': 3, 'init_size': 500}),
]

for factory, init, params in cases:
    print(" Evaluation of \$\$ with \$\$ init" % (factory.__name__, init))
    inertia = np.empty((len(n_init_range), n_runs))
    for run_id in range(n_runs):
        km = factory(n_clusters=n_clusters, init=init, random_state=run_id,
                        n_init=n_init, **params).fit(X)
        inertia[i, run_id] = km.inertia_
    p = plt.errorbar(n_init_range, inertia.mean(axis=1), inertia.std(axis=1))
    plots.append(p[0])
    legends.append("\$\$ with \$\$ init" % (factory.__name__, init))

plt.xlabel('n_init')
plt.ylabel('inertia')
plt.legend(plots, legends)
plt.title("Mean inertia for various k-means init across \$d\$ runs" % n_runs)

# Part 2: Qualitative visual inspection of the convergence

```
9.19 Adjustment for chance in clustering performance evaluation

The following plots demonstrate the impact of the number of clusters and number of samples on various clustering performance evaluation metrics.

Non-adjusted measures such as the V-Measure show a dependency between the number of clusters and the number of samples: the mean V-Measure of random labeling increases significantly as the number of clusters is closer to the total number of samples used to compute the measure.

Adjusted for chance measure such as ARI display some random variations centered around a mean score of 0.0 for any number of samples and clusters.

Only adjusted measures can hence safely be used as a consensus index to evaluate the average stability of clustering algorithms for a given value of k on various overlapping sub-samples of the dataset.
Computing adjusted_rand_score for 10 values of n_clusters and n_samples=100
done in 0.041s
Computing v_measure_score for 10 values of n_clusters and n_samples=100
done in 0.062s
Computing adjusted_mutual_info_score for 10 values of n_clusters and n_samples=100
done in 0.603s
Computing mutual_info_score for 10 values of n_clusters and n_samples=100
done in 0.051s
Computing adjusted_rand_score for 10 values of n_clusters and n_samples=1000
done in 0.064s
Computing v_measure_score for 10 values of n_clusters and n_samples=1000
done in 0.085s
Computing adjusted_mutual_info_score for 10 values of n_clusters and n_samples=1000
done in 0.344s
Computing mutual_info_score for 10 values of n_clusters and n_samples=1000
done in 0.067s

print(__doc__)

# Author: Olivier Grisel <olivier.grisel@ensta.org>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from time import time
from sklearn import metrics

def uniform_labelings_scores(score_func, n_samples, n_clusters_range,
                           fixed_n_classes=None, n_runs=5, seed=42):
    """Compute score for 2 random uniform cluster labelings.
    Both random labelings have the same number of clusters for each value
    possible value in `n_clusters_range`
    When fixed_n_classes is not None the first labeling is considered a ground
    truth class assignment with fixed number of classes.
    ""
    random_labels = np.random.RandomState(seed).randint
    scores = np.zeros((len(n_clusters_range), n_runs))
    
    if fixed_n_classes is not None:
        labels_a = random_labels(low=0, high=fixed_n_classes, size=n_samples)
    
    for i, k in enumerate(n_clusters_range):
        for j in range(n_runs):
            if fixed_n_classes is None:
                labels_a = random_labels(low=0, high=k, size=n_samples)
                labels_b = random_labels(low=0, high=k, size=n_samples)
            scores[i, j] = score_func(labels_a, labels_b)

    return scores

score_funcs = [  

9.19. Adjustment for chance in clustering performance evaluation
metrics.adjusted_rand_score,
metrics.v_measure_score,
metrics.adjusted_mutual_info_score,
metrics.mutual_info_score,
]

# 2 independent random clusterings with equal cluster number

n_samples = 100
n_clusters_range = np.linspace(2, n_samples, 10).astype(np.int)

plt.figure(1)

plots = []
names = []
for score_func in score_funcs:
    print("Computing $\text{\texttt{%s}}$ for $\%d$ values of $\text{\texttt{n_clusters}}$ and $\text{\texttt{n_samples}}=$\%d"
    % (score_func.__name__, len(n_clusters_range), n_samples))
    t0 = time()
    scores = uniform_labelings_scores(score_func, n_samples, n_clusters_range)
    print("done in $\%0.3fs$" % (time() - t0))
    plots.append(plt.errorbar(plt.errorbar( np_clusters_range, np.median(scores, axis=1), scores.std(axis=1))[0])
    names.append(score_func.__name__) 

plt.title("Clustering measures for 2 random uniform labelings\n" "with equal number of clusters")
plt.xlabel('Number of clusters (Number of samples is fixed to \%d)' % n_samples)
plt.ylabel('Score value')
plt.legend(plots, names)
plt.ylim(ymin=-0.05, ymax=1.05)

# Random labeling with varying n_clusters against ground class labels
# with fixed number of clusters

n_samples = 1000
n_clusters_range = np.linspace(2, 100, 10).astype(np.int)
n_classes = 10

plt.figure(2)

plots = []
names = []
for score_func in score_funcs:
    print("Computing $\text{\texttt{%s}}$ for $\%d$ values of $\text{\texttt{n_clusters}}$ and $\text{\texttt{n_samples}}=$\%d"
    % (score_func.__name__, len(n_clusters_range), n_samples))
    t0 = time()
    scores = uniform_labelings_scores(score_func, n_samples, n_clusters_range, fixed_n_classes=n_classes)
    print("done in $\%0.3fs$" % (time() - t0))
    plots.append(plt.errorbar(plt.errorbar( np_clusters_range, scores.mean(axis=1), scores.std(axis=1))[0])
    names.append(score_func.__name__) 

plt.title("Clustering measures for random uniform labeling\n")
9.20 A demo of K-Means clustering on the handwritten digits data

In this example we compare the various initialization strategies for K-means in terms of runtime and quality of the results.

As the ground truth is known here, we also apply different cluster quality metrics to judge the goodness of fit of the cluster labels to the ground truth.

Cluster quality metrics evaluated (see Clustering performance evaluation for definitions and discussions of the metrics):

<table>
<thead>
<tr>
<th>Shorthand</th>
<th>full name</th>
</tr>
</thead>
<tbody>
<tr>
<td>homo</td>
<td>homogeneity score</td>
</tr>
<tr>
<td>compl</td>
<td>completeness score</td>
</tr>
<tr>
<td>v-meas</td>
<td>V measure</td>
</tr>
<tr>
<td>ARI</td>
<td>adjusted Rand index</td>
</tr>
<tr>
<td>AMI</td>
<td>adjusted mutual information</td>
</tr>
<tr>
<td>silhouette</td>
<td>silhouette coefficient</td>
</tr>
</tbody>
</table>
K-means clustering on the digits dataset (PCA-reduced data)
Centroids are marked with white cross

Out:

<table>
<thead>
<tr>
<th>init</th>
<th>time</th>
<th>inertia</th>
<th>homo</th>
<th>compl</th>
<th>v-meas</th>
<th>ARI</th>
<th>AMI</th>
<th>silhouette</th>
</tr>
</thead>
<tbody>
<tr>
<td>k-means++</td>
<td>0.33s</td>
<td>69432</td>
<td>0.602</td>
<td>0.650</td>
<td>0.625</td>
<td>0.465</td>
<td>0.598</td>
<td>0.146</td>
</tr>
<tr>
<td>random</td>
<td>0.25s</td>
<td>69694</td>
<td>0.669</td>
<td>0.710</td>
<td>0.689</td>
<td>0.553</td>
<td>0.666</td>
<td>0.147</td>
</tr>
<tr>
<td>PCA-based</td>
<td>0.05s</td>
<td>70804</td>
<td>0.671</td>
<td>0.698</td>
<td>0.684</td>
<td>0.561</td>
<td>0.668</td>
<td>0.118</td>
</tr>
</tbody>
</table>

print(__doc__)

from time import time
import numpy as np
import matplotlib.pyplot as plt

from sklearn import metrics
from sklearn.cluster import KMeans
from sklearn.datasets import load_digits
from sklearn.decomposition import PCA
from sklearn.preprocessing import scale

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```python
np.random.seed(42)

digits = load_digits()
data = scale(digits.data)

n_samples, n_features = data.shape
n_digits = len(np.unique(digits.target))
labels = digits.target

sample_size = 300

print(n_digits: %d, n_samples %d, n_features %d

print(82 * '_')
print('init	
time	inertia	homo	compl	v-meas	ARI	AMI	silhouette')

def bench_k_means(estimator, name, data):
t0 = time()
estimator.fit(data)

print('%-9s  %5.2f  %6d  %5.3f  %5.3f  %5.3f  %5.3f

bench_k_means(KMeans(init='k-means++', n_clusters=n_digits, n_init=10),
name="k-means++", data=data)
bench_k_means(KMeans(init='random', n_clusters=n_digits, n_init=10),
name="random", data=data)

# in this case the seeding of the centers is deterministic, hence we run the
# kmeans algorithm only once with n_init=1
pca = PCA(n_components=n_digits).fit(data)
bench_k_means(KMeans(init=pca.components_, n_clusters=n_digits, n_init=1),
name="PCA-based", data=data)

print(82 * '_')

# Visualize the results on PCA-reduced data

reduced_data = PCA(n_components=2).fit_transform(data)
kmeans = KMeans(init='k-means++', n_clusters=n_digits, n_init=10)
kmeans.fit(reduced_data)

# Step size of the mesh. Decrease to increase the quality of the VQ.
h = .02  # point in the mesh [x_min, x_max]x[y_min, y_max].
```
# Plot the decision boundary. For that, we will assign a color to each
x_min, x_max = reduced_data[:, 0].min() - 1, reduced_data[:, 0].max() + 1
y_min, y_max = reduced_data[:, 1].min() - 1, reduced_data[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))

# Obtain labels for each point in mesh. Use last trained model.
Z = kmeans.predict(np.c_[xx.ravel(), yy.ravel()])

# Put the result into a color plot
Z = Z.reshape(xx.shape)
plt.figure(1)
plt.clf()
plt.imshow(Z, interpolation='nearest',
       extent=(xx.min(), xx.max(), yy.min(), yy.max()),
       cmap=plt.cm.Paired,
       aspect='auto', origin='lower')

plt.plot(reduced_data[:, 0], reduced_data[:, 1], 'k.', markersize=2)
# Plot the centroids as a white X
centroids = kmeans.cluster_centers_
plt.scatter(centroids[:, 0], centroids[:, 1],
       marker='x', s=169, linewidths=3,
       color='w', zorder=10)
plt.title('K-means clustering on the digits dataset (PCA-reduced data)
       Centroids are marked with white cross')
plt.xlim(x_min, x_max)
plt.ylim(y_min, y_max)
plt.xticks(())
plt.yticks(())
plt.show()

Total running time of the script: ( 0 minutes 1.399 seconds)

9.21 Feature agglomeration vs. univariate selection

This example compares 2 dimensionality reduction strategies:
- univariate feature selection with Anova
- feature agglomeration with Ward hierarchical clustering

Both methods are compared in a regression problem using a BayesianRidge as supervised estimator.
9.21. Feature agglomeration vs. univariate selection
f_regression(array([[ 0.905206, ..., -0.849835],
                   ..., [-0.675318, ..., -1.085711]]),
array([-27.447268, ..., -25.026711]))

# Author: Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause
print(__doc__)
import shutil
import tempfile
import numpy as np
import matplotlib.pyplot as plt
from scipy import linalg, ndimage
from sklearn.feature_extraction.image import grid_to_graph
from sklearn import feature_selection
from sklearn.cluster import FeatureAgglomeration
from sklearn.linear_model import BayesianRidge
from sklearn.pipeline import Pipeline
from sklearn.externals.joblib import Memory
from sklearn.model_selection import GridSearchCV, KFold

# Generate data
n_samples = 200
size = 40  # image size
roi_size = 15
snr = 5.
np.random.seed(0)
mask = np.ones([size, size], dtype=np.bool)
coef = np.zeros((size, size))
coef[0:roi_size, 0:roi_size] = -1.
coef[-roi_size:, -roi_size:] = 1.
X = np.random.randn(n_samples, size ** 2)
for x in X:  # smooth data
    x[:] = ndimage.gaussian_filter(x.reshape(size, size), sigma=1.0).ravel()
X -= X.mean(axis=0)
X /= X.std(axis=0)
y = np.dot(X, coef.ravel())
noise = np.random.randn(y.shape[0])
noise_coef = (linalg.norm(y, 2) / np.exp(snr / 20.)) / linalg.norm(noise, 2)
y += noise_coef * noise  # add noise

# Compute the coefs of a Bayesian Ridge with GridSearch
cv = KFold(2)  # cross-validation generator for model selection
ridge = BayesianRidge()
cachedir = tempfile.mkdtemp()
mem = Memory(cachedir=cachedir, verbose=1)

# Ward agglomeration followed by BayesianRidge
connectivity = grid_to_graph(n_x=size, n_y=size)
ward = FeatureAgglomeration(n_clusters=10, connectivity=connectivity,
                           memory=mem)
clf = Pipeline([('ward', ward), ('ridge', ridge)])
# Select the optimal number of parcels with grid search
clf = GridSearchCV(clf, {'ward__n_clusters': [10, 20, 30]}, n_jobs=1, cv=cv)
c.fit(X, y)  # set the best parameters
coef_ = clf.best_estimator_.steps[-1][1].coef_
coef_ = clf.best_estimator_.steps[0][1].inverse_transform(coef_)
coef_agglomeration_ = coef_.reshape(size, size)

# Anova univariate feature selection followed by BayesianRidge
f_regression = mem.cache(feature_selection.f_regression)  # caching function
anova = feature_selection.SelectPercentile(f_regression)
clf = Pipeline([('anova', anova), ('ridge', ridge)])
# Select the optimal percentage of features with grid search
clf = GridSearchCV(clf, {'anova__percentile': [5, 10, 20]}, cv=cv)
c.fit(X, y)  # set the best parameters
coef_ = clf.best_estimator_.steps[-1][1].coef_
coef_ = clf.best_estimator_.steps[0][1].inverse_transform(coef_.reshape(1, -1))
coef_selection_ = coef_.reshape(size, size)

# Inverse the transformation to plot the results on an image
plt.figure(figsize=(7.3, 2.7))
plt.subplot(1, 3, 1)
plt.imshow(coef, interpolation="nearest", cmap=plt.cm.RdBu_r)
plt.title("True weights")
plt.subplot(1, 3, 2)
plt.imshow(coef_selection_, interpolation="nearest", cmap=plt.cm.RdBu_r)
plt.title("Feature Selection")
plt.subplot(1, 3, 3)
plt.imshow(coef_agglomeration_, interpolation="nearest", cmap=plt.cm.RdBu_r)
plt.title("Feature Agglomeration")
plt.subplots_adjust(0.04, 0.0, 0.98, 0.94, 0.16, 0.26)
plt.show()

# Attempt to remove the temporary cachedir, but don't worry if it fails
shutil.rmtree(cachedir, ignore_errors=True)

Total running time of the script: ( 0 minutes 1.330 seconds)

9.22 Comparison of the K-Means and MiniBatchKMeans clustering algorithms

We want to compare the performance of the MiniBatchKMeans and KMeans: the MiniBatchKMeans is faster, but
gives slightly different results (see Mini Batch K-Means).

We will cluster a set of data, first with KMeans and then with MiniBatchKMeans, and plot the results. We will also
plot the points that are labelled differently between the two algorithms.

```
print(__doc__)

import time
import numpy as np
import matplotlib.pyplot as plt

from sklearn.cluster import MiniBatchKMeans, KMeans
from sklearn.metrics.pairwise import pairwise_distances_argmin
from sklearn.datasets.samples_generator import make_blobs

# #############################################################################
# Generate sample data
np.random.seed(0)

batch_size = 45
centers = [[1, 1], [-1, -1], [1, -1]]
n_clusters = len(centers)
X, labels_true = make_blobs(n_samples=3000, centers=centers, cluster_std=0.7)

# #############################################################################
# Compute clustering with Means
k_means = KMeans(init='k-means++', n_clusters=3, n_init=10)
t0 = time.time()
k_means.fit(X)
t_batch = time.time() - t0

# #############################################################################
# Compute clustering with MiniBatchKMeans
mbk = MiniBatchKMeans(init='k-means++', n_clusters=3, batch_size=batch_size,
                      n_init=10, max_no_improvement=10, verbose=0)
t0 = time.time()
mbk.fit(X)
t_mini_batch = time.time() - t0

# Plot result
```
fig = plt.figure(figsize=(8, 3))
fig.subplots_adjust(left=0.02, right=0.98, bottom=0.05, top=0.9)
colors = ['#4EACC5', '#FF9C34', '#4E9A06']

# We want to have the same colors for the same cluster from the
# MiniBatchKMeans and the KMeans algorithm. Let's pair the cluster centers per
# closest one.
k_means_cluster_centers = np.sort(k_means.cluster_centers_, axis=0)
mbk_means_cluster_centers = np.sort(mbk.cluster_centers_, axis=0)
k_means_labels = pairwise_distances_argmin(X, k_means_cluster_centers)
mbk_means_labels = pairwise_distances_argmin(X, mbk_means_cluster_centers)
order = pairwise_distances_argmin(k_means_cluster_centers, mbk_means_cluster_centers)

# KMeans
ax = fig.add_subplot(1, 3, 1)
for k, col in zip(range(n_clusters), colors):
    my_members = k_means_labels == k
    cluster_center = k_means_cluster_centers[k]
    ax.plot(X[my_members, 0], X[my_members, 1], 'w', markerfacecolor=col, marker='.')
    ax.plot(cluster_center[0], cluster_center[1], 'o', markerfacecolor=col, markeredgecolor='k', markersize=6)
ax.set_title('KMeans')
ax.set_xticks(())
ax.set_yticks(())
plt.text(-3.5, 1.8, 'train time: %.2fs
inertia: %f' % (t_batch, k_means.inertia_))

# MiniBatchKMeans
ax = fig.add_subplot(1, 3, 2)
for k, col in zip(range(n_clusters), colors):
    my_members = mbk_means_labels == order[k]
    cluster_center = mbk_means_cluster_centers[order[k]]
    ax.plot(X[my_members, 0], X[my_members, 1], 'w', markerfacecolor=col, marker='.')
    ax.plot(cluster_center[0], cluster_center[1], 'o', markerfacecolor=col, markeredgecolor='k', markersize=6)
ax.set_title('MiniBatchKMeans')
ax.set_xticks(())
ax.set_yticks(())
plt.text(-3.5, 1.8, 'train time: %.2fs
inertia: %f' % (t_mini_batch, mbk.inertia_))

# Initialise the different array to all False
different = (mbk_means_labels == 4)
ax = fig.add_subplot(1, 3, 3)
for k in range(n_clusters):
    different += ((k_means_labels == k) != (mbk_means_labels == order[k]))
identic = np.logical_not(different)
ax.plot(X[identic, 0], X[identic, 1], 'w', markerfacecolor='bbbbbb', marker='.'),
ax.plot(X[different, 0], X[different, 1], 'w', markerfacecolor='m', marker='.'),
ax.set_title('Difference')
ax.set_xticks(())

9.22. Comparison of the K-Means and MiniBatchKMeans clustering algorithms
9.23 Selecting the number of clusters with silhouette analysis on KMeans clustering

Silhouette analysis can be used to study the separation distance between the resulting clusters. The silhouette plot displays a measure of how close each point in one cluster is to points in the neighboring clusters and thus provides a way to assess parameters like number of clusters visually. This measure has a range of [-1, 1].

Silhouette coefficients (as these values are referred to as) near +1 indicate that the sample is far away from the neighboring clusters. A value of 0 indicates that the sample is on or very close to the decision boundary between two neighboring clusters and negative values indicate that those samples might have been assigned to the wrong cluster.

In this example the silhouette analysis is used to choose an optimal value for n_clusters. The silhouette plot shows that the n_clusters value of 3, 5 and 6 are a bad pick for the given data due to the presence of clusters with below average silhouette scores and also due to wide fluctuations in the size of the silhouette plots. Silhouette analysis is more ambivalent in deciding between 2 and 4.

Also from the thickness of the silhouette plot the cluster size can be visualized. The silhouette plot for cluster 0 when n_clusters is equal to 2, is bigger in size owing to the grouping of the 3 sub clusters into one big cluster. However when the n_clusters is equal to 4, all the plots are more or less of similar thickness and hence are of similar sizes as can be also verified from the labelled scatter plot on the right.
9.23. Selecting the number of clusters with silhouette analysis on KMeans clustering
Out:

For n_clusters = 2 The average silhouette_score is: 0.704978749608
For n_clusters = 3 The average silhouette_score is: 0.588200401213
For n_clusters = 4 The average silhouette_score is: 0.650518663273
For n_clusters = 5 The average silhouette_score is: 0.563764690262
For n_clusters = 6 The average silhouette_score is: 0.450466629437
The 1st subplot is the silhouette plot
The silhouette coefficient can range from -1, 1 but in this example all
lie within [-0.1, 1]

# Initialize the clusterer with n_clusters value and a random generator
# seed of 10 for reproducibility.
clusterer = KMeans(n_clusters=n_clusters, random_state=10)
cluster_labels = clusterer.fit_predict(X)

# The silhouette_score gives the average value for all the samples.
# This gives a perspective into the density and separation of the formed
# clusters
silhouette_avg = silhouette_score(X, cluster_labels)
print("For n_clusters =", n_clusters,
    "The average silhouette_score is ": silhouette_avg)

# Compute the silhouette scores for each sample
sample_silhouette_values = silhouette_samples(X, cluster_labels)

y_lower = 10
for i in range(n_clusters):
    # Aggregate the silhouette scores for samples belonging to
    # cluster i, and sort them
    ith_cluster_silhouette_values = \
        sample_silhouette_values[cluster_labels == i]
    ith_cluster_silhouette_values.sort()
    size_cluster_i = ith_cluster_silhouette_values.shape[0]
    y_upper = y_lower + size_cluster_i
    color = cm.spectral(float(i) / n_clusters)
    ax1.fill_betweenx(np.arange(y_lower, y_upper),
        0, ith_cluster_silhouette_values,
        facecolor=color, edgecolor=color, alpha=0.7)

    # Label the silhouette plots with their cluster numbers at the middle
    ax1.text(-0.05, y_lower + 0.5 * size_cluster_i, str(i))

    # Compute the new y_lower for next plot
    y_lower = y_upper + 10  # 10 for the 0 samples

ax1.set_title("The silhouette plot for the various clusters.")
ax1.set_xlabel("The silhouette coefficient values")
ax1.set_ylabel("Cluster label")

# The vertical line for average silhouette score of all the values
ax1.axvline(x=silhouette_avg, color="red", linestyle="--")

ax1.set_yticks([])  # Clear the yaxis labels / ticks
ax1.set_xticks([-0.1, 0, 0.2, 0.4, 0.6, 0.8, 1])

# 2nd Plot showing the actual clusters formed
colors = cm.spectral(cluster_labels.astype(float) / n_clusters)
ax2.scatter(X[:, 0], X[:, 1], marker='.', s=30, lw=0, alpha=0.7,
c=colors, edgecolor='k')

# Labeling the clusters
centers = clusterer.cluster_centers_

# Draw white circles at cluster centers
ax2.scatter(cenrors[:, 0], centers[:, 1], marker='o',
c="white", alpha=1, s=200, edgecolor='k')

for i, c in enumerate(centers):  
    ax2.scatter(c[0], c[1], marker='%d' % i, alpha=1,
    s=50, edgecolor='k')

ax2.set_title("The visualization of the clustered data.";
ax2.set_xlabel("Feature space for the 1st feature")
ax2.set_ylabel("Feature space for the 2nd feature")

plt.suptitle(("Silhouette analysis for KMeans clustering on sample data "
    "with n_clusters = %d" % n_clusters),
    fontsize=14, fontweight='bold')

plt.show()

Total running time of the script: ( 0 minutes 1.013 seconds)

9.24 Comparing different clustering algorithms on toy datasets

This example shows characteristics of different clustering algorithms on datasets that are “interesting” but still in 2D. With the exception of the last dataset, the parameters of each of these dataset-algorithm pairs has been tuned to produce good clustering results. Some algorithms are more sensitive to parameter values than others.

The last dataset is an example of a ‘null’ situation for clustering: the data is homogeneous, and there is no good clustering. For this example, the null dataset uses the same parameters as the dataset in the row above it, which represents a mismatch in the parameter values and the data structure.

While these examples give some intuition about the algorithms, this intuition might not apply to very high dimensional data.
# Comparing different clustering algorithms on toy datasets

The following code compares the results of various clustering algorithms on different toy datasets.

```python
import time
import warnings
import numpy as np
import matplotlib.pyplot as plt
from sklearn import cluster, datasets, mixture
from sklearn.neighbors import kneighbors_graph
from sklearn.preprocessing import StandardScaler
from itertools import cycle, islice

np.random.seed(0)

# ============
# Generate datasets. We choose the size big enough to see the scalability
# of the algorithms, but not too big to avoid too long running times
# ============

n_samples = 1500
noisy_circles = datasets.make_circles(n_samples=n_samples, factor=.5,
    noise=.05)
noisy_moons = datasets.make_moons(n_samples=n_samples, noise=.05)
blobs = datasets.make_blobs(n_samples=n_samples, random_state=8)
no_structure = np.random.rand(n_samples, 2), None

# Anisotropicly distributed data
random_state = 170
X, y = datasets.make_blobs(n_samples=n_samples, random_state=random_state)
transformation = [[0.6, -0.6], [-0.4, 0.8]]
X_aniso = np.dot(X, transformation)
aniso = (X_aniso, y)
```

The code above generates various toy datasets and applies different clustering algorithms to them. The results are visualized using matplotlib to compare the performance of each algorithm.
# blobs with varied variances
varied = datasets.make_blobs(n_samples=n_samples,
                              cluster_std=[1.0, 2.5, 0.5],
                              random_state=random_state)

# =============
# Set up cluster parameters
# =============
plt.figure(figsize=(9 * 2 + 3, 12.5))
plt.subplots_adjust(left=.02, right=.98, bottom=.001, top=.96, wspace=.05,
                    hspace=.01)

plot_num = 1

default_base = {'quantile': .3,
                 'eps': .3,
                 'damping': .9,
                 'preference': -200,
                 'n_neighbors': 10,
                 'n_clusters': 3}

datasets = [
    (noisy_circles, {'damping': .77, 'preference': -240,
                     'quantile': .2, 'n_clusters': 2}),
    (noisy_moons, {'damping': .75, 'preference': -220, 'n_clusters': 2}),
    (varied, {'eps': .18, 'n_neighbors': 2}),
    (aniso, {'eps': .15, 'n_neighbors': 2}),
    (blobs, {}),
    (no_structure, {})]

for i_dataset, (dataset, algo_params) in enumerate(datasets):
    # update parameters with dataset-specific values
    params = default_base.copy()
    params.update(algo_params)
    X, y = dataset

    # normalize dataset for easier parameter selection
    X = StandardScaler().fit_transform(X)

    # estimate bandwidth for mean shift
    bandwidth = cluster.estimate_bandwidth(X, quantile=params['quantile'])

    # connectivity matrix for structured Ward
    connectivity = kneighbors_graph(        
        X, n_neighbors=params['n_neighbors'], include_self=False)
    # make connectivity symmetric
    connectivity = 0.5 * (connectivity + connectivity.T)

    # =============
    # Create cluster objects
    # =============
    ms = cluster.MeanShift(bandwidth=bandwidth, bin_seeding=True)
    two_means = cluster.MiniBatchKMeans(n_clusters=params['n_clusters'])
    ward = cluster.AgglomerativeClustering(
        n_clusters=params['n_clusters'], linkage='ward',
        connectivity=connectivity)
spectral = cluster.SpectralClustering(
    n_clusters=params['n_clusters'],
    eigen_solver='arpack',
    affinity="nearest_neighbors")
dbscan = cluster.DBSCAN(eps=params['eps'])
affinity_propagation = cluster.AffinityPropagation(
    damping=params['damping'], preference=params['preference'])
average_linkage = cluster.AgglomerativeClustering(
    linkage="average", affinity="cityblock",
    n_clusters=params['n_clusters'], connectivity=connectivity)
birch = cluster.Birch(n_clusters=params['n_clusters'])
gmm = mixture.GaussianMixture(
    n_components=params['n_clusters'], covariance_type='full')

clustering_algorithms = (
    ('MiniBatchKMeans', two_means),
    ('AffinityPropagation', affinity_propagation),
    ('MeanShift', ms),
    ('SpectralClustering', spectral),
    ('Ward', ward),
    ('AgglomerativeClustering', average_linkage),
    ('DBSCAN', dbscan),
    ('Birch', birch),
    ('GaussianMixture', gmm)
)

for name, algorithm in clustering_algorithms:
    t0 = time.time()
    # catch warnings related to kneighbors_graph
    with warnings.catch_warnings():
        warnings.filterwarnings("ignore", message="the number of connected components of the " +
        "connectivity matrix is [0-9][1,2]\" +
        " > 1. Completing it to avoid stopping the tree early.",
        category=UserWarning)
        warnings.filterwarnings(
            "ignore",
            message="Graph is not fully connected, spectral embedding" +
            " may not work as expected.",
            category=UserWarning)
    algorithm.fit(X)
    t1 = time.time()
    if hasattr(algorithm, 'labels_'):
        y_pred = algorithm.labels_.astype(np.int)
    else:
        y_pred = algorithm.predict(X)

plt.subplot(len(datasets), len(clustering_algorithms), plot_num)
if i_dataset == 0:
    plt.title(name, size=18)
    colors = np.array(list(islice(cycle(["#377eb8", "#ff7f00", "#4daf4a", "#f781bf", "#a65628", "#984ea3",

    #999999", 
    "#e41a1c", 
    "#dede00")]),
    int(max(y_pred) + 1)))
plt.scatter(X[:, 0], X[:, 1], s=10, color=colors[y_pred])
plt.xlim(-2.5, 2.5)
plt.ylim(-2.5, 2.5)
plt.xticks(()
plt.yticks(()
plt.text(.99, .01, ('%.2fs' % (t1 - t0)).lstrip('0'),
    transform=plt.gca().transAxes, size=15,
    horizontalalignment='right')
plot_num += 1

plt.show()

**Total running time of the script:** ( 0 minutes 37.247 seconds)
Examples concerning the `sklearn.covariance` module.

### 10.1 Ledoit-Wolf vs OAS estimation

The usual covariance maximum likelihood estimate can be regularized using shrinkage. Ledoit and Wolf proposed a close formula to compute the asymptotically optimal shrinkage parameter (minimizing a MSE criterion), yielding the Ledoit-Wolf covariance estimate.

Chen et al. proposed an improvement of the Ledoit-Wolf shrinkage parameter, the OAS coefficient, whose convergence is significantly better under the assumption that the data are Gaussian.

This example, inspired from Chen’s publication [1], shows a comparison of the estimated MSE of the LW and OAS methods, using Gaussian distributed data.


```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from scipy.linalg import toeplitz, cholesky
from sklearn.covariance import LedoitWolf, OAS

np.random.seed(0)

n_features = 100
# simulation covariance matrix (AR(1) process)
r = 0.1
real_cov = toeplitz(r ** np.arange(n_features))
coloring_matrix = cholesky(real_cov)

n_samples_range = np.arange(6, 31, 1)
repeat = 100
lw_mse = np.zeros((n_samples_range.size, repeat))
oa_mse = np.zeros((n_samples_range.size, repeat))
lw_shrinkage = np.zeros((n_samples_range.size, repeat))
oa_shrinkage = np.zeros((n_samples_range.size, repeat))
for i, n_samples in enumerate(n_samples_range):
    for j in range(repeat):
        X = np.dot(
            np.random.normal(size=(n_samples, n_features)), coloring_matrix.T)
lw = LedoitWolf(store_precision=False, assume_centered=True)
lw.fit(X)
lw_mse[i, j] = lw.error_norm(real_cov, scaling=False)
lw_shrinkage[i, j] = lw.shrinkage_

oa = OAS(store_precision=False, assume_centered=True)
oa.fit(X)
oa_mse[i, j] = oa.error_norm(real_cov, scaling=False)
oa_shrinkage[i, j] = oa.shrinkage_

# plot MSE
plt.subplot(2, 1, 1)
plt.errorbar(n_samples_range, lw_mse.mean(1), yerr=lw_mse.std(1),
            label='Ledoit-Wolf', color='navy', lw=2)
plt.errorbar(n_samples_range, oa_mse.mean(1), yerr=oa_mse.std(1),
            label='OAS', color='darkorange', lw=2)
plt.ylabel("Squared error")
plt.legend(loc="upper right")
plt.title("Comparison of covariance estimators")
plt.xlim(5, 31)

# plot shrinkage coefficient
plt.subplot(2, 1, 2)
plt.errorbar(n_samples_range, lw_shrinkage.mean(1), yerr=lw_shrinkage.std(1),
            label='Ledoit-Wolf', color='navy', lw=2)
plt.errorbar(n_samples_range, oa_shrinkage.mean(1), yerr=oa_shrinkage.std(1),
            label='OAS', color='darkorange', lw=2)
plt.xlabel("n_samples")
plt.ylabel("Shrinkage")
plt.legend(loc="lower right")
plt.ylim(plt.ylim()[0], 1. + (plt.ylim()[1] - plt.ylim()[0]) / 10.)
plt.xlim(5, 31)
plt.show()
10.2 Sparse inverse covariance estimation

Using the GraphLasso estimator to learn a covariance and sparse precision from a small number of samples.

To estimate a probabilistic model (e.g. a Gaussian model), estimating the precision matrix, that is the inverse covariance matrix, is as important as estimating the covariance matrix. Indeed a Gaussian model is parametrized by the precision matrix.

To be in favorable recovery conditions, we sample the data from a model with a sparse inverse covariance matrix. In addition, we ensure that the data is not too much correlated (limiting the largest coefficient of the precision matrix) and that there a no small coefficients in the precision matrix that cannot be recovered. In addition, with a small number of observations, it is easier to recover a correlation matrix rather than a covariance, thus we scale the time series.

Here, the number of samples is slightly larger than the number of dimensions, thus the empirical covariance is still invertible. However, as the observations are strongly correlated, the empirical covariance matrix is ill-conditioned and as a result its inverse -- the empirical precision matrix -- is very far from the ground truth.

If we use l2 shrinkage, as with the Ledoit-Wolf estimator, as the number of samples is small, we need to shrink a lot. As a result, the Ledoit-Wolf precision is fairly close to the ground truth precision, that is not far from being diagonal, but the off-diagonal structure is lost.

The l1-penalized estimator can recover part of this off-diagonal structure. It learns a sparse precision. It is not able to recover the exact sparsity pattern: it detects too many non-zero coefficients. However, the highest non-zero
coefficients of the l1 estimated correspond to the non-zero coefficients in the ground truth. Finally, the coefficients of the l1 precision estimate are biased toward zero: because of the penalty, they are all smaller than the corresponding ground truth value, as can be seen on the figure.

Note that, the color range of the precision matrices is tweaked to improve readability of the figure. The full range of values of the empirical precision is not displayed.

The alpha parameter of the GraphLasso setting the sparsity of the model is set by internal cross-validation in the GraphLassoCV. As can be seen on figure 2, the grid to compute the cross-validation score is iteratively refined in the neighborhood of the maximum.

```python
print(__doc__)
# author: Gael Varoquaux <gael.varoquaux@inria.fr>
# License: BSD 3 clause
# Copyright: INRIA

import numpy as np
from scipy import linalg
from sklearn.datasets import make_sparse_spd_matrix
from sklearn.covariance import GraphLassoCV, ledoit_wolf
import matplotlib.pyplot as plt

# #############################################################################
# Generate the data
n_samples = 60
n_features = 20

prng = np.random.RandomState(1)
prec = make_sparse_spd_matrix(n_features, alpha=.98,
                             smallest_coef=.4,
                            smallest_coef_sign='same',
                             random_state=prng)
```
largest_coef=.7,
    random_state=prng)

cov = linalg.inv(prec)
d = np.sqrt(np.diag(cov))
cov /= d
cov /= d[:, np.newaxis]
prec = d
prec /= d[:, np.newaxis]
X = prng.multivariate_normal(np.zeros(n_features), cov, size=n_samples)
X -= X.mean(axis=0)
X /= X.std(axis=0)

# #############################################################################
# Estimate the covariance
emp_cov = np.dot(X.T, X) / n_samples

model = GraphLassoCV()
model.fit(X)
cov_ = model.covariance_
prec_ = model.precision_

lw_cov_, _ = ledoit_wolf(X)
lw_prec_ = linalg.inv(lw_cov_)

# #############################################################################
# Plot the results
plt.figure(figsize=(10, 6))
plt.subplots_adjust(left=0.02, right=0.98)

# plot the covariances
covs = [('Empirical', emp_cov), ('Ledoit-Wolf', lw_cov_),
        ('GraphLasso', cov_), ('True', cov_)]
vmax = cov_.max()
for i, (name, this_cov) in enumerate(covs):
    plt.subplot(2, 4, i + 1)
    plt.imshow(this_cov, interpolation='nearest', vmin=-vmax, vmax=vmax,
               cmap=plt.cm.RdBu_r)
    plt.xticks(())
    plt.yticks(()
    plt.title(' 

# plot the precisions
precs = [('Empirical', linalg.inv(emp_cov)), ('Ledoit-Wolf', lw_prec_),
         ('GraphLasso', prec_), ('True', prec_)]
vmax = .9 * prec_.max()
for i, (name, this_prec) in enumerate(precs):
    ax = plt.subplot(2, 4, i + 5)
    plt.imshow(np.ma.masked_equal(this_prec, 0), interpolation='nearest', vmin=-vmax, vmax=vmax,
               cmap=plt.cm.RdBu_r)
    plt.xticks(())
    plt.yticks(()
    plt.title(' 

# plot the model selection metric
plt.figure(figsize=(4, 3))
10.3 Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood

When working with covariance estimation, the usual approach is to use a maximum likelihood estimator, such as the `sklearn.covariance.EmpiricalCovariance`. It is unbiased, i.e. it converges to the true (population) covariance when given many observations. However, it can also be beneficial to regularize it, in order to reduce its variance; this, in turn, introduces some bias. This example illustrates the simple regularization used in Shrink Covariance estimators. In particular, it focuses on how to set the amount of regularization, i.e. how to choose the bias-variance trade-off.

Here we compare 3 approaches:

- Setting the parameter by cross-validating the likelihood on three folds according to a grid of potential shrinkage parameters.
- A close formula proposed by Ledoit and Wolf to compute the asymptotically optimal regularization parameter (minimizing a MSE criterion), yielding the `sklearn.covariance.LedoitWolf` covariance estimate.
- An improvement of the Ledoit-Wolf shrinkage, the `sklearn.covariance.OAS`, proposed by Chen et al. Its convergence is significantly better under the assumption that the data are Gaussian, in particular for small samples.

To quantify estimation error, we plot the likelihood of unseen data for different values of the shrinkage parameter. We also show the choices by cross-validation, or with the LedoitWolf and OAS estimates.

Note that the maximum likelihood estimate corresponds to no shrinkage, and thus performs poorly. The Ledoit-Wolf estimate performs really well, as it is close to the optimal and is computational not costly. In this example, the OAS estimate is a bit further away. Interestingly, both approaches outperform cross-validation, which is significantly most computationally costly.
import numpy as np
import matplotlib.pyplot as plt
from scipy import linalg
from sklearn.covariance import LedoitWolf, OAS, ShrunkCovariance,
                  log_likelihood, empirical_covariance
from sklearn.model_selection import GridSearchCV

# #############################################################################
# Generate sample data
n_features, n_samples = 40, 20
np.random.seed(42)
base_X_train = np.random.normal(size=(n_samples, n_features))
base_X_test = np.random.normal(size=(n_samples, n_features))

# Color samples
coloring_matrix = np.random.normal(size=(n_features, n_features))
X_train = np.dot(base_X_train, coloring_matrix)
X_test = np.dot(base_X_test, coloring_matrix)

# #############################################################################
# Compute the likelihood on test data
# spanning a range of possible shrinkage coefficient values
shrinkages = np.logspace(-2, 0, 30)
negative_logliks = [-ShrunkCovariance(shrinkage=s).fit(X_train).score(X_test)
                    for s in shrinkages]

# under the ground-truth model, which we would not have access to in real
# settings
real_cov = np.dot(coloring_matrix.T, coloring_matrix)
emp_cov = empirical_covariance(X_train)
loglik_real = -log_likelihood(emp_cov, linalg.inv(real_cov))

# #############################################################################
# Compare different approaches to setting the parameter

# GridSearch for an optimal shrinkage coefficient
tuned_parameters = [{'shrinkage': shrinkages}]
cv = GridSearchCV(ShrunkCovariance(), tuned_parameters)
cv.fit(X_train)

# Ledoit-Wolf optimal shrinkage coefficient estimate
lw = LedoitWolf()
loglik_lw = lw.fit(X_train).score(X_test)

# OAS coefficient estimate
oa = OAS()
loglik_oa = oa.fit(X_train).score(X_test)

# #############################################################################
# Plot results
fig = plt.figure()
plt.title("Regularized covariance: likelihood and shrinkage coefficient")
plt.xlabel('Regularization parameter: shrinkage coefficient')
plt.ylabel('Error: negative log-likelihood on test data')
# range shrinkage curve
plt.loglog(shrinkages, negative_logliks, label="Negative log-likelihood")
plt.plot(plt.xlim(), 2 * [loglik_real], '--r', label="Real covariance likelihood")
# adjust view
lik_max = np.amax(negative_logliks)
lik_min = np.amin(negative_logliks)
ymin = lik_min - 6. * np.log((plt.ylim()[1] - plt.ylim()[0]))
ymax = lik_max + 10. * np.log(lik_max - lik_min)
xmin = shrinkages[0]
xmax = shrinkages[-1]
# LW likelihood
plt.vlines(lw.shrinkage_, ymin, -loglik_lw, color='magenta',
           linewidth=3, label='Ledoit-Wolf estimate')
# OAS likelihood
plt.vlines(oa.shrinkage_, ymin, -loglik_oa, color='purple',
           linewidth=3, label='OAS estimate')
# best CV estimator likelihood
plt.vlines(cv.best_estimator_.shrinkage, ymin,
           -cv.best_estimator_.score(X_test), color='cyan',
           linewidth=3, label='Cross-validation best estimate')
plt.ylim(ymin, ymax)
plt.xlim(xmin, xmax)
plt.legend()
plt.show()

Total running time of the script: ( 0 minutes 0.455 seconds)

10.4 Robust covariance estimation and Mahalanobis distances relevance

An example to show covariance estimation with the Mahalanobis distances on Gaussian distributed data.

For Gaussian distributed data, the distance of an observation \( x_i \) to the mode of the distribution can be computed using its Mahalanobis distance: 

\[
d(\mu, \Sigma)(x_i)^2 = (x_i - \mu)'\Sigma^{-1}(x_i - \mu)
\]

where \( \mu \) and \( \Sigma \) are the location and the covariance of the underlying Gaussian distribution.

In practice, \( \mu \) and \( \Sigma \) are replaced by some estimates. The usual covariance maximum likelihood estimate is very sensitive to the presence of outliers in the data set and therefore, the corresponding Mahalanobis distances are. One would better have to use a robust estimator of covariance to guarantee that the estimation is resistant to “erroneous” observations in the data set and that the associated Mahalanobis distances accurately reflect the true organisation of the observations.

The Minimum Covariance Determinant estimator is a robust, high-breakdown point (i.e. it can be used to estimate the covariance matrix of highly contaminated datasets, up to \( \frac{n_{\text{samples}} - n_{\text{samples}} - 1}{2} \) outliers) estimator of covariance. The idea is to find \( n_{\text{samples}} + n_{\text{samples}} + 1 \) observations whose empirical covariance has the smallest determinant, yielding a “pure” subset of observations from which to compute standards estimates of location and covariance.

The Minimum Covariance Determinant estimator (MCD) has been introduced by P.J.Rousseeuw in [1]. This example illustrates how the Mahalanobis distances are affected by outlying data: observations drawn from a contaminating distribution are not distinguishable from the observations coming from the real, Gaussian distribution that one may want to work with. Using MCD-based Mahalanobis distances, the two populations become distinguishable. Associated applications are outliers detection, observations ranking, clustering, ... For visualization purpose, the cubic root of the Mahalanobis distances are represented in the boxplot, as Wilson and Hilferty suggest [2].


Mahalanobis distances of a contaminated data set:

1. from non-robust estimates (Maximum Likelihood)
2. from robust estimates (Minimum Covariance Determinant)

```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.covariance import EmpiricalCovariance, MinCovDet

n_samples = 125
n_outliers = 25
n_features = 2

# generate data
gen_cov = np.eye(n_features)
gen_cov[0, 0] = 2.
X = np.dot(np.random.randn(n_samples, n_features), gen_cov)
# add some outliers
outliers_cov = np.eye(n_features)
outliers_cov[np.arange(1, n_features), np.arange(1, n_features)] = 7.
X[-n_outliers:] = np.dot(np.random.randn(n_outliers, n_features), outliers_cov)

# fit a Minimum Covariance Determinant (MCD) robust estimator to data
robust_cov = MinCovDet().fit(X)

# compare estimators learnt from the full data set with true parameters
emp_cov = EmpiricalCovariance().fit(X)
```
scikit-learn user guide, Release 0.20.dev0

## Display results

```python
fig = plt.figure()
plt.subplots_adjust(hspace=-.1, wspace=.4, top=.95, bottom=.05)

# Show data set
subfig1 = plt.subplot(3, 1, 1)
inlier_plot = subfig1.scatter(X[:, 0], X[:, 1],
                               color='black', label='inliers')
outlier_plot = subfig1.scatter(X[:, 0][-n_outliers:], X[:, 1][-n_outliers:],
                               color='red', label='outliers')
subfig1.set_xlim(subfig1.get_xlim()[0], 11.)
subfig1.set_title("Mahalanobis distances of a contaminated data set:"
                   "")

# Show contours of the distance functions
xx, yy = np.meshgrid(np.linspace(plt.xlim()[0], plt.xlim()[1], 100),
                     np.linspace(plt.ylim()[0], plt.ylim()[1], 100))
zz = np.c_[xx.ravel(), yy.ravel()]

mahal_emp_cov = emp_cov.mahalanobis(zz)
mahal_emp_cov = mahal_emp_cov.reshape(xx.shape)
emp_cov_contour = subfig1.contour(xx, yy, np.sqrt(mahal_emp_cov),
                                  cmap=plt.cm.PuBu_r,
                                  linestyles='dashed')

mahal_robust_cov = robust_cov.mahalanobis(zz)
mahal_robust_cov = mahal_robust_cov.reshape(xx.shape)
robust_contour = subfig1.contour(xx, yy, np.sqrt(mahal_robust_cov),
                                 cmap=plt.cm.YlOrBr_r, linestyles='dotted')

subfig1.legend([emp_cov_contour.collections[0], robust_contour.collections[0],
                 inlier_plot, outlier_plot],
                ['MLE dist', 'robust dist', 'inliers', 'outliers'],
                loc="upper right", borderaxespad=0)
plt.xticks(()
plt.yticks(()

# Plot the scores for each point
emp_mahal = emp_cov.mahalanobis(X - np.mean(X, 0)) ** (0.33)
subfig2 = plt.subplot(2, 2, 3)
subfig2.boxplot([emp_mahal[:-n_outliers], emp_mahal[-n_outliers:]],
                 widths=.25)
subfig2.plot(1.26 * np.ones(n_samples - n_outliers),
             emp_mahal[:-n_outliers], '+k', markeredgewidth=1)
subfig2.plot(2.26 * np.ones(n_outliers),
             emp_mahal[-n_outliers:], '+k', markeredgewidth=1)
subfig2.axes.set_xticklabels(('inliers', 'outliers'), size=15)
subfig2.set_ylabel(r"$\sqrt[3]{\text{Mahal. dist.}}$", size=16)
subfig2.set_title("1. from non-robust estimates\n(Maximum Likelihood)"
                  

robust_mahal = robust_cov.mahalanobis(X - robust_cov.location_) ** (0.33)
subfig3 = plt.subplot(2, 2, 4)
subfig3.boxplot([robust_mahal[:-n_outliers], robust_mahal[-n_outliers:]],
                 widths=.25)
subfig3.plot(1.26 * np.ones(n_samples - n_outliers),
             robust_mahal[:-n_outliers], '+k', markeredgewidth=1)
subfig3.plot(2.26 * np.ones(n_outliers),
             robust_mahal[-n_outliers:], '+k', markeredgewidth=1)
```

10.4. Robust covariance estimation and Mahalanobis distances relevance
### 10.5 Outlier detection with several methods.

When the amount of contamination is known, this example illustrates three different ways of performing Novelty and Outlier Detection:

- based on a robust estimator of covariance, which is assuming that the data are Gaussian distributed and performs better than the One-Class SVM in that case.
- using the One-Class SVM and its ability to capture the shape of the data set, hence performing better when the data is strongly non-Gaussian, i.e. with two well-separated clusters;
- using the Isolation Forest algorithm, which is based on random forests and hence more adapted to large-dimensional settings, even if it performs quite well in the examples below.
- using the Local Outlier Factor to measure the local deviation of a given data point with respect to its neighbors by comparing their local density.

The ground truth about inliers and outliers is given by the points colors while the orange-filled area indicates which points are reported as inliers by each method.

Here, we assume that we know the fraction of outliers in the datasets. Thus rather than using the ‘predict’ method of the objects, we set the threshold on the decision_function to separate out the corresponding fraction.
import numpy as np
from scipy import stats
import matplotlib.pyplot as plt
import matplotlib.font_manager

from sklearn import svm
from sklearn.covariance import EllipticEnvelope
from sklearn.ensemble import IsolationForest
from sklearn.neighbors import LocalOutlierFactor

print(__doc__)

SEED = 42
GRID_PRECISION = 100

10.5. Outlier detection with several methods.
rng = np.random.RandomState(SEED)

# Example settings
n_samples = 200
outliers_fraction = 0.25
clusters_separation = (0, 1, 2)

define two outlier detection tools to be compared
classifiers = {
    "One-Class SVM": svm.OneClassSVM(nu=0.95 * outliers_fraction + 0.05,
                                        kernel="rbf", gamma=0.1),
    "Robust covariance": EllipticEnvelope(contamination=outliers_fraction),
    "Isolation Forest": IsolationForest(max_samples=n_samples,
                                          contamination=outliers_fraction,
                                          random_state=rng),
    "Local Outlier Factor": LocalOutlierFactor(
                                          n_neighbors=35,
                                          contamination=outliers_fraction)
}

# Compare given classifiers under given settings
xx, yy = np.meshgrid(np.linspace(-7, 7, GRID_PRECISION),
                      np.linspace(-7, 7, GRID_PRECISION))
n_outliers = int(outliers_fraction * n_samples)
n_inliers = n_samples - n_outliers
ground_truth = np.ones(n_samples, dtype=int)
ground_truth[-n_outliers:] = -1

# Fit the problem with varying cluster separation
for _, offset in enumerate(clusters_separation):
    np.random.seed(SEED)
    # Data generation
    X1 = 0.3 * np.random.randn(n_inliers // 2, 2) - offset
    X2 = 0.3 * np.random.randn(n_inliers // 2, 2) + offset
    X = np.concatenate([X1, X2], axis=0)
    # Add outliers
    X = np.concatenate([X, np.random.uniform(low=-6, high=6,
                                              size=(n_outliers, 2))], axis=0)
    # Fit the model
    plt.figure(figsize=(9, 7))

    for i, (clf_name, clf) in enumerate(classifiers.items()):
        # Fit the data and tag outliers
        if clf_name == "Local Outlier Factor":
            y_pred = clf.fit_predict(X)
            scores_pred = clf.negative_outlier_factor_
        else:
            clf.fit(X)
            scores_pred = clf.decision_function(X)
            y_pred = clf.predict(X)
        n_errors = (y_pred != ground_truth).sum()
        # plot the levels lines and the points
        if clf_name == "Local Outlier Factor":
            # decision_function is private for LOF
            Z = clf._decision_function(np.c_[xx.ravel(), yy.ravel()])
        else:
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
subplot = plt.subplot(2, 2, i + 1)
subplot.contourf(xx, yy, Z, levels=np.linspace(Z.min(), threshold, 7),
cmap=plt.cm.Blues_r)
a = subplot.contour(xx, yy, Z, levels=[threshold],
linewidths=2, colors='red')
subplot.contourf(xx, yy, Z, levels=[threshold, Z.max()],
colors='orange')
b = subplot.scatter(X[:-n_outliers, 0], X[:-n_outliers, 1], c='white',
s=20, edgecolor='k')
c = subplot.scatter(X[-n_outliers:, 0], X[-n_outliers:, 1], c='black',
s=20, edgecolor='k')
subplot.axis('tight')
subplot.legend([a.collections[0], b, c],
['learned decision function', 'true inliers', 'true outliers'],
prop=matplotlib.font_manager.FontProperties(size=10),
loc='lower right')
subplot.set_xlabel("%d. %s (errors: %d)" % (i + 1, clf_name, n_errors))
subplot.set_xlim((-7, 7))
subplot.set_ylim((-7, 7))
plt.subplots_adjust(0.04, 0.1, 0.96, 0.94, 0.1, 0.26)
plt.suptitle("Outlier detection")
plt.show()
• The mean and the empirical covariance of the full dataset, which break down as soon as there are outliers in the data set

• The robust MCD, that has a low error provided $n_{\text{samples}} > 5n_{\text{features}}$

• The mean and the empirical covariance of the observations that are known to be good ones. This can be considered as a “perfect” MCD estimation, so one can trust our implementation by comparing to this case.

10.6.3 References

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
import matplotlib.font_manager

from sklearn.covariance import EmpiricalCovariance, MinCovDet

# example settings
n_samples = 80
n_features = 5
repeat = 10

range_n_outliers = np.concatenate((np.linspace(0, n_samples / 8, 5),
                                    np.linspace(n_samples / 8, n_samples / 4, 5),
                                    np.linspace(n_samples / 4, n_samples / 2, 5),
                                    np.linspace(n_samples / 2, n_samples, 5)))
```
```python
np.linspace(n_samples / 8, n_samples / 2, 5)[1:-1]).astype(np.int)

# definition of arrays to store results
err_loc_mcd = np.zeros((range_n_outliers.size, repeat))
err_cov_mcd = np.zeros((range_n_outliers.size, repeat))
err_loc_emp_full = np.zeros((range_n_outliers.size, repeat))
err_cov_emp_full = np.zeros((range_n_outliers.size, repeat))
err_loc_emp_pure = np.zeros((range_n_outliers.size, repeat))
err_cov_emp_pure = np.zeros((range_n_outliers.size, repeat))

# computation
for i, n_outliers in enumerate(range_n_outliers):
    for j in range(repeat):
        rng = np.random.RandomState(i * j)

        # generate data
        X = rng.randn(n_samples, n_features)
        # add some outliers
        outliers_index = rng.permutation(n_samples)[n_outliers]
        outliers_offset = 10. * (np.random.randint(2, size=(n_outliers, n_features)) - 0.5)
        X[outliers_index] += outliers_offset
        inliers_mask = np.ones(n_samples).astype(bool)
        inliers_mask[outliers_index] = False

        # fit a Minimum Covariance Determinant (MCD) robust estimator to data
        mcd = MinCovDet().fit(X)
        err_loc_mcd[i, j] = np.sum(mcd.location_ ** 2)
        err_cov_mcd[i, j] = mcd.error_norm(np.eye(n_features))

        # compare estimators learned from the full data set with true parameters
        err_loc_emp_full[i, j] = np.sum(X.mean(0) ** 2)
        err_cov_emp_full[i, j] = EmpiricalCovariance().fit(X).error_norm(np.eye(n_features))

        # compare with an empirical covariance learned from a pure data set
        # (i.e. "perfect" mcd)
        pure_X = X[inliers_mask]
        pure_location = pure_X.mean(0)
        pure_emp_cov = EmpiricalCovariance().fit(pure_X)
        err_loc_emp_pure[i, j] = np.sum(pure_location ** 2)
        err_cov_emp_pure[i, j] = pure_emp_cov.error_norm(np.eye(n_features))

# Display results
font_prop = matplotlib.font_manager.FontProperties(size=11)
plt.subplot(2, 1, 1)
lw = 2
plt.errorbar(range_n_outliers, err_loc_mcd.mean(1),
             yerr=err_loc_mcd.std(1) / np.sqrt(repeat),
             label="Robust location", lw=lw, color='m')
plt.errorbar(range_n_outliers, err_loc_emp_full.mean(1),
             yerr=err_loc_emp_full.std(1) / np.sqrt(repeat),
             label="Full data set mean", lw=lw, color='green')
plt.errorbar(range_n_outliers, err_loc_emp_pure.mean(1),
             yerr=err_loc_emp_pure.std(1) / np.sqrt(repeat),
```

10.6. Robust vs Empirical covariance estimate
Total running time of the script: ( 0 minutes 3.786 seconds)
Examples concerning the `sklearn.cross_decomposition` module.

### 11.1 Compare cross decomposition methods

Simple usage of various cross decomposition algorithms: - PLSCanonical - PLSRegression, with multivariate response, a.k.a. PLS2 - PLSRegression, with univariate response, a.k.a. PLS1 - CCA

Given 2 multivariate covarying two-dimensional datasets, X, and Y, PLS extracts the ‘directions of covariance’, i.e. the components of each datasets that explain the most shared variance between both datasets. This is apparent on the scatterplot matrix display: components 1 in dataset X and dataset Y are maximally correlated (points lie around the first diagonal). This is also true for components 2 in both dataset, however, the correlation across datasets for different components is weak: the point cloud is very spherical.
Out:

```
Corr(X)
[[ 1.  0.48  0.01 -0.07]
 [ 0.48 1.  0.04 -0.11]
 [ 0.01 0.04 1.  0.51]
 [-0.07 -0.11 0.51 1. ]]  
Corr(Y)
[[ 1.  0.46  0.02  0.01]
 [ 0.46 1.  -0.04 -0.04]
 [ 0.02 -0.04 1.  0.5 ]
 [ 0.01 -0.04 0.5  1. ]]  
True B (such that: Y = XB + Err)
[[1 1 1]
 [2 2 2]
 [0 0 0]
 [0 0 0]
 [0 0 0]
 [0 0 0]
 [0 0 0]
 [0 0 0]
 [0 0 0]]
Estimated B
[[ 1.  0.9  1. ]
 [ 2.  2.  2. ]
 [ 0. -0.  0. ]
 [-0. -0. -0. ]
 [ 0. -0. -0. ]
 [ 0. -0. -0. ]
 [ 0.  0.  0. ]
 [ 0.1 -0. -0. ]
 [-0. -0.  0. ]]  
Estimated betas
[[ 1. ]
 [ 2. ]
 [-0. ]
 [ 0. ]
 [-0. ]
 [ 0. ]
 [-0. ]
 [ 0. ]
 [ 0. ]]
```

```
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn.cross_decomposition import PLSCanonical, PLSRegression, CCA
```

Chapter 11. Cross decomposition
# Dataset based latent variables model

n = 500
# 2 latents vars:
l1 = np.random.normal(size=n)
l2 = np.random.normal(size=n)

latents = np.array([l1, l1, l2, l2]).T
X = latents + np.random.normal(size=4 * n).reshape((n, 4))
Y = latents + np.random.normal(size=4 * n).reshape((n, 4))

X_train = X[:n // 2]
Y_train = Y[:n // 2]
X_test = X[n // 2:]
Y_test = Y[n // 2:]

print("Corr(X)")
print(round(np.corrcoef(X.T), 2))
print("Corr(Y)")
print(round(np.corrcoef(Y.T), 2))

# Canonical (symmetric) PLS

# Transform data
# ~~~~~~~~~~~~~
plsca = PLSCanonical(n_components=2)
plsca.fit(X_train, Y_train)
X_train_r, Y_train_r = plsca.transform(X_train, Y_train)
X_test_r, Y_test_r = plsca.transform(X_test, Y_test)

# Scatter plot of scores
# ~~~~~~~~~~~~~~~~~~~~~~
# 1) On diagonal plot X vs Y scores on each components
plt.figure(figsize=(12, 8))
plt.subplot(221)
plt.scatter(X_train_r[:, 0], Y_train_r[:, 0], label="train",
marker="o", c="b", s=25)
plt.scatter(X_test_r[:, 0], Y_test_r[:, 0], label="test",
marker="o", c="r", s=25)
plt.xlabel("x scores")
plt.ylabel("y scores")
plt.title('Comp. 1: X vs Y (test corr = %.2f)'
np.corrcoef(X_test_r[:, 0], Y_test_r[:, 0])[0, 1])
plt.xticks(())
plt.yticks(())
plt.legend(loc="best")

plt.subplot(224)
plt.scatter(X_train_r[:, 1], Y_train_r[:, 1], label="train",
marker="o", c="b", s=25)
plt.scatter(X_test_r[:, 1], Y_test_r[:, 1], label="test",
marker="o", c="r", s=25)
plt.xlabel("x scores")
plt.ylabel("y scores")
plt.title('Comp. 2: X vs Y (test corr = %.2f)'
np.corrcoef(X_test_r[:, 1], Y_test_r[:, 1])[0, 1])
plt.xticks(())
plt.yticks()
# 2) Off diagonal plot components 1 vs 2 for X and Y
plt.subplot(222)
plt.scatter(X_train_r[:, 0], X_train_r[:, 1], label="train",
marker="*", c="b", s=50)
plt.scatter(X_test_r[:, 0], X_test_r[:, 1], label="test",
marker="*", c="r", s=50)
plt.xlabel("X comp. 1")
plt.ylabel("X comp. 2")
plt.title('X comp. 1 vs X comp. 2 (test corr = %.2f)'
% np.corrcoef(X_test_r[:, 0], X_test_r[:, 1])[:, 0, 1])
plt.legend(loc="best")
plt.xticks(())
plt.yticks(()
plt.subplot(223)
plt.scatter(Y_train_r[:, 0], Y_train_r[:, 1], label="train",
marker="*", c="b", s=50)
plt.scatter(Y_test_r[:, 0], Y_test_r[:, 1], label="test",
marker="*", c="r", s=50)
plt.xlabel("Y comp. 1")
plt.ylabel("Y comp. 2")
plt.title('Y comp. 1 vs Y comp. 2 , (test corr = %.2f)'
% np.corrcoef(Y_test_r[:, 0], Y_test_r[:, 1])[:, 0, 1])
plt.legend(loc="best")
plt.xticks(()
plt.yticks(()
plt.show()

# PLS regression, with multivariate response, a.k.a. PLS2

n = 1000
q = 3
p = 10
X = np.random.normal(size=n * p).reshape((n, p))
B = np.array([[1, 2] + [0] * (p - 2)] * q).T
# each Yj = 1*X1 + 2*X2 + noise
Y = np.dot(X, B) + np.random.normal(size=n * q).reshape((n, q)) + 5

pls2 = PLSRegression(n_components=3)
pls2.fit(X, Y)

print("True B (such that: Y = XB + Err)")
print(B)
# compare pls2.coef_ with B
print("Estimated B")
print(np.round(pls2.coef_, 1))
pls2.predict(X)

# PLS regression, with univariate response, a.k.a. PLS1

n = 1000
p = 10
X = np.random.normal(size=n * p).reshape((n, p))
y = X[:, 0] + 2 * X[:, 1] + np.random.normal(size=n * 1) + 5
pls1 = PLSRegression(n_components=3)
```python
plsl.fit(X, y)
# note that the number of components exceeds 1 (the dimension of y)
print("Estimated betas")
print(np.round(plsl.coef_, 1))

# ####################################################################
# # CCA (PLS mode B with symmetric deflation)
# ####################################################################

cca = CCA(n_components=2)
cca.fit(X_train, Y_train)
X_train_r, Y_train_r = cca.transform(X_train, Y_train)
X_test_r, Y_test_r = cca.transform(X_test, Y_test)
```

**Total running time of the script:** ( 0 minutes 0.263 seconds)
Examples concerning the `sklearn.datasets` module.

### 12.1 The Digit Dataset

This dataset is made up of 1797 8x8 images. Each image, like the one shown below, is of a hand-written digit. In order to utilize an 8x8 figure like this, we’d have to first transform it into a feature vector with length 64.

See [here](#) for more information about this dataset.

```python
print(__doc__)

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

from sklearn import datasets
import matplotlib.pyplot as plt

# Load the digits dataset
digits = datasets.load_digits()
```
# Display the first digit
plt.figure(1, figsize=(3, 3))
plt.imshow(digits.images[-1], cmap=plt.cm.gray_r, interpolation='nearest')
plt.show()

Total running time of the script: ( 0 minutes 0.158 seconds)

12.2 The Iris Dataset

This data sets consists of 3 different types of irises’ (Setosa, Versicolour, and Virginica) petal and sepal length, stored in a 150x4 numpy.ndarray.

The rows being the samples and the columns being: Sepal Length, Sepal Width, Petal Length and Petal Width.

The below plot uses the first two features. See [here](#) for more information on this dataset.
print(__doc__)

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from sklearn import datasets
from sklearn.decomposition import PCA

# import some data to play with
iris = datasets.load_iris()
X = iris.data[:, :2]  # we only take the first two features.
y = iris.target

x_min, x_max = X[:, 0].min() - .5, X[:, 0].max() + .5
y_min, y_max = X[:, 1].min() - .5, X[:, 1].max() + .5

plt.figure(2, figsize=(8, 6))
plt.clf()
# Plot the training points
plt.scatter(X[:, 0], X[:, 1], c=y, cmap=plt.cm.Set1,
            edgecolor='k')
plt.xlabel('Sepal length')
plt.ylabel('Sepal width')
plt.xlim(x_min, x_max)
plt.ylim(y_min, y_max)
plt.xticks(())
plt.yticks(())

# To get a better understanding of interaction of the dimensions
# plot the first three PCA dimensions
fig = plt.figure(1, figsize=(8, 6))
ax = Axes3D(fig, elev=-150, azim=110)
X_reduced = PCA(n_components=3).fit_transform(iris.data)
ax.scatter(X_reduced[:, 0], X_reduced[:, 1], X_reduced[:, 2], c=y,
            cmap=plt.cm.Set1, edgecolor='k', s=40)
ax.set_title("First three PCA directions")
ax.set_xlabel("1st eigenvector")
ax.w_xaxis.set_ticklabels([])
ax.set_ylabel("2nd eigenvector")
ax.w_yaxis.set_ticklabels([])
ax.set_zlabel("3rd eigenvector")
ax.w_zaxis.set_ticklabels([])
plt.show()

Total running time of the script: ( 0 minutes 0.110 seconds)
12.3 Plot randomly generated classification dataset

Plot several randomly generated 2D classification datasets. This example illustrates the datasets. make_classification datasets.make_blobs and datasets.make_gaussian_quantiles functions.

For make_classification, three binary and two multi-class classification datasets are generated, with different numbers of informative features and clusters per class.

```python
print(__doc__)

import matplotlib.pyplot as plt
from sklearn.datasets import make_classification
```
This illustrates the `datasets.make_multilabel_classification` dataset generator. Each sample consists of counts of two features (up to 50 in total), which are differently distributed in each of two classes.
Points are labeled as follows, where Y means the class is present:

<table>
<thead>
<tr>
<th></th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>Color</th>
</tr>
</thead>
<tbody>
<tr>
<td>Y</td>
<td>N</td>
<td>N</td>
<td>Red</td>
<td></td>
</tr>
<tr>
<td>N</td>
<td>Y</td>
<td>N</td>
<td>Blue</td>
<td></td>
</tr>
<tr>
<td>N</td>
<td>N</td>
<td>Y</td>
<td>Yellow</td>
<td></td>
</tr>
<tr>
<td>Y</td>
<td>Y</td>
<td>N</td>
<td>Purple</td>
<td></td>
</tr>
<tr>
<td>Y</td>
<td>N</td>
<td>Y</td>
<td>Orange</td>
<td></td>
</tr>
<tr>
<td>Y</td>
<td>Y</td>
<td>N</td>
<td>Green</td>
<td></td>
</tr>
<tr>
<td>Y</td>
<td>Y</td>
<td>Y</td>
<td>Brown</td>
<td></td>
</tr>
</tbody>
</table>

A star marks the expected sample for each class; its size reflects the probability of selecting that class label.

The left and right examples highlight the `n_labels` parameter: more of the samples in the right plot have 2 or 3 labels.

Note that this two-dimensional example is very degenerate: generally the number of features would be much greater than the “document length”, while here we have much larger documents than vocabulary. Similarly, with `n_classes > n_features`, it is much less likely that a feature distinguishes a particular class.

The data was generated from (random_state=483):

| Class | P(C) | P(w0|C) | P(w1|C) |
|-------|------|--------|--------|
| red   | 0.27 | 0.59   | 0.41   |
| blue  | 0.33 | 0.94   | 0.06   |
| yellow| 0.40 | 0.64   | 0.36   |

```python
from __future__ import print_function
import numpy as np
```
import matplotlib.pyplot as plt

from sklearn.datasets import make_multilabel_classification as make_ml_clf

print(__doc__)

COLORS = np.array(['!', '#FF3333', '#0198E1', '#BF5FFF', '#FCD116', '#FF7216', '#4DBD33', '#87421F'])

# Use same random seed for multiple calls to make_multilabel_classification to
# ensure same distributions
RANDOM_SEED = np.random.randint(2 ** 10)

def plot_2d(ax, n_labels=1, n_classes=3, length=50):
    X, Y, p_c, p_w_c = make_ml_clf(n_samples=150, n_features=2,
                                   n_classes=n_classes, n_labels=n_labels,
                                   length=length, allow_unlabeled=False,
                                   return_distributions=True,
                                   random_state=RANDOM_SEED)

    ax.scatter(X[:, 0], X[:, 1], color=COLORS.take((Y * [1, 2, 4]).sum(axis=1)),
               marker='.
    ax.scatter(p_w_c[0] * length, p_w_c[1] * length,
               marker='*', linewidth=.5, edgecolor='black',
               s=20 + 1500 * p_c ** 2,
               color=COLORS.take([1, 2, 4]))
    ax.set_xlabel('Feature 0 count')
    return p_c, p_w_c

_, (ax1, ax2) = plt.subplots(1, 2, sharex='row', sharey='row', figsize=(8, 4))
plt.subplots_adjust(bottom=.15)
p_c, p_w_c = plot_2d(ax1, n_labels=1)
ax1.set_title('n_labels=1, length=50')
ax1.set_ylabel('Feature 1 count')

plot_2d(ax2, n_labels=3)
ax2.set_title('n_labels=3, length=50')
ax2.set_xlabel('Feature 0 count')
ax2.set_xlim(left=0, auto=True)
ax2.set_ylim(bottom=0, auto=True)
plt.show()

print('The data was generated from (random_state=%d):' % RANDOM_SEED)
print('Class', 'P(C)', 'P(w0|C)', 'P(w1|C)', sep='  \
for k, p, p_w in zip(['red', 'blue', 'yellow'], p_c, p_w_c.T):
    print('\$%s\t%0.2f\t%0.2f\t%0.2f\$' % (k, p, p_w[0], p_w[1]))
Total running time of the script: 0 minutes 0.118 seconds
Examples concerning the `sklearn.decomposition` module.

### 13.1 Beta-divergence loss functions

A plot that compares the various Beta-divergence loss functions supported by the Multiplicative-Update (‘mu’) solver in `sklearn.decomposition.NMF`.

```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.decomposition import _beta_divergence

beta_divergence = lambda x, y, beta: _beta_divergence(x, y, beta)

plt.plot(np.linspace(0, 4), [beta_divergence(1, x, 0.0) for x in np.linspace(0, 4)], 'pink', label='beta = 0.0', linewidth=2)
plt.plot(np.linspace(0, 4), [beta_divergence(1, x, 0.5) for x in np.linspace(0, 4)], 'blue', label='beta = 0.5', linewidth=2)
plt.plot(np.linspace(0, 4), [beta_divergence(1, x, 1.0) for x in np.linspace(0, 4)], 'green', label='beta = 1.0', linewidth=2)
plt.plot(np.linspace(0, 4), [beta_divergence(1, x, 1.5) for x in np.linspace(0, 4)], 'yellow', label='beta = 1.5', linewidth=2)
plt.plot(np.linspace(0, 4), [beta_divergence(1, x, 2.0) for x in np.linspace(0, 4)], 'red', label='beta = 2.0', linewidth=2)
plt.xlabel('x')
plt.ylabel('beta-divergence(1, x)')
plt.legend()
plt.show()
```
print(__doc__)

x = np.linspace(0.001, 4, 1000)
y = np.zeros(x.shape)

colors = 'mbgyr'
for j, beta in enumerate((0., 0.5, 1., 1.5, 2.)):
    for i, xi in enumerate(x):
        y[i] = _beta_divergence(1, xi, 1, beta)
        name = "beta = %.1f" % beta
        plt.plot(x, y, label=name, color=colors[j])

plt.xlabel("x")
plt.title("beta-divergence(1, x)")
plt.legend(loc=0)
plt.axis([0, 4, 0, 3])
plt.show()

Total running time of the script: ( 0 minutes 0.376 seconds)

## 13.2 PCA example with Iris Data-set

Principal Component Analysis applied to the Iris dataset.

See here for more information on this dataset.

```python
print(__doc__)

# Code source: Gaël Varoquaux
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
```
from sklearn import decomposition
from sklearn import datasets

np.random.seed(5)

centers = [[1, 1], [-1, -1], [1, -1]]
iris = datasets.load_iris()
X = iris.data
y = iris.target

fig = plt.figure(1, figsize=(4, 3))
plt.clf()
ax = Axes3D(fig, rect=[0, 0, .95, 1], elev=48, azim=134)
plt.cla()
pca = decomposition.PCA(n_components=3)
pca.fit(X)
X = pca.transform(X)

for name, label in [('Setosa', 0), ('Versicolour', 1), ('Virginica', 2)]:
    ax.text3D(X[y == label, 0].mean(),
              X[y == label, 1].mean() + 1.5,
              X[y == label, 2].mean(), name,
              horizontalalignment='center',
              bbox=dict(alpha=.5, edgecolor='w', facecolor='w'))
# Reorder the labels to have colors matching the cluster results
y = np.choose(y, [1, 2, 0]).astype(np.float)
ax.scatter(X[:, 0], X[:, 1], X[:, 2], c=y, cmap=plt.cm.spectral,
           edgecolor='k')

ax.w_xaxis.set_ticklabels([])
ax.w_yaxis.set_ticklabels([])
ax.w_zaxis.set_ticklabels([])

plt.show()

**Total running time of the script:** ( 0 minutes 0.082 seconds)

## 13.3 Incremental PCA

Incremental principal component analysis (IPCA) is typically used as a replacement for principal component analysis (PCA) when the dataset to be decomposed is too large to fit in memory. IPCA builds a low-rank approximation for the input data using an amount of memory which is independent of the number of input data samples. It is still dependent on the input data features, but changing the batch size allows for control of memory usage.

This example serves as a visual check that IPCA is able to find a similar projection of the data to PCA (to a sign flip), while only processing a few samples at a time. This can be considered a “toy example”, as IPCA is intended for large datasets which do not fit in main memory, requiring incremental approaches.
```python
import numpy as np
import matplotlib.pyplot as plt

# Authors: Kyle Kastner
# License: BSD 3 clause

def print(__doc__):
    pass
```

Chapter 13. Decomposition
from sklearn.datasets import load_iris
from sklearn.decomposition import PCA, IncrementalPCA

iris = load_iris()
X = iris.data
y = iris.target

n_components = 2
ipca = IncrementalPCA(n_components=n_components, batch_size=10)
X_ipca = ipca.fit_transform(X)
pca = PCA(n_components=n_components)
X_pca = pca.fit_transform(X)

colors = ['navy', 'turquoise', 'darkorange']

for X_transformed, title in [(X_ipca, "Incremental PCA"), (X_pca, "PCA")]:
    plt.figure(figsize=(8, 8))
    for color, i, target_name in zip(colors, [0, 1, 2], iris.target_names):
        plt.scatter(X_transformed[y == i, 0], X_transformed[y == i, 1],
                    color=color, lw=2, label=target_name)

    if "Incremental" in title:
        err = np.abs(np.abs(X_pca) - np.abs(X_ipca)).mean()
        plt.title(title + " of iris dataset
                   Mean absolute unsigned error 
                   %.6f" % err)
    else:
        plt.title(title + " of iris dataset")
    plt.legend(loc="best", shadow=False, scatterpoints=1)
    plt.axis([-4, 4, -1.5, 1.5])

plt.show()

Total running time of the script: (0 minutes 0.149 seconds)

13.4 Comparison of LDA and PCA 2D projection of Iris dataset

The Iris dataset represents 3 kind of Iris flowers (Setosa, Versicolour and Virginica) with 4 attributes: sepal length, sepal width, petal length and petal width.

Principal Component Analysis (PCA) applied to this data identifies the combination of attributes (principal components, or directions in the feature space) that account for the most variance in the data. Here we plot the different samples on the 2 first principal components.

Linear Discriminant Analysis (LDA) tries to identify attributes that account for the most variance between classes. In particular, LDA, in contrast to PCA, is a supervised method, using known class labels.
Out:

```
explained variance ratio (first two components): [ 0.92461621  0.05301557]
```

```python
print(__doc__)

import matplotlib.pyplot as plt

from sklearn import datasets
from sklearn.decomposition import PCA
from sklearn.discriminant_analysis import LinearDiscriminantAnalysis

iris = datasets.load_iris()
X = iris.data
y = iris.target
target_names = iris.target_names

pca = PCA(n_components=2)
X_r = pca.fit(X).transform(X)

lda = LinearDiscriminantAnalysis(n_components=2)
```
X_r2 = lda.fit(X, y).transform(X)

# Percentage of variance explained for each components
print('explained variance ratio (first two components): %s' % str(pca.explained_variance_ratio_))

plt.figure()
colors = ['navy', 'turquoise', 'darkorange']
lw = 2

for color, i, target_name in zip(colors, [0, 1, 2], target_names):
    plt.scatter(X_r[y == i, 0], X_r[y == i, 1], color=color, alpha=.8, lw=lw,
                label=target_name)
plt.legend(loc='best', shadow=False, scatterpoints=1)
plt.title('PCA of IRIS dataset')

plt.figure()
for color, i, target_name in zip(colors, [0, 1, 2], target_names):
    plt.scatter(X_r2[y == i, 0], X_r2[y == i, 1], alpha=.8, color=color,
                label=target_name)
plt.legend(loc='best', shadow=False, scatterpoints=1)
plt.title('LDA of IRIS dataset')

plt.show()

Total running time of the script: (0 minutes 0.140 seconds)

13.5 Blind source separation using FastICA

An example of estimating sources from noisy data.

Independent component analysis (ICA) is used to estimate sources given noisy measurements. Imagine 3 instruments playing simultaneously and 3 microphones recording the mixed signals. ICA is used to recover the sources i.e. what is played by each instrument. Importantly, PCA fails at recovering our instruments since the related signals reflect non-Gaussian processes.
import numpy as np
import matplotlib.pyplot as plt
from scipy import signal

from sklearn.decomposition import FastICA, PCA

# #############################################################################
# Generate sample data
np.random.seed(0)
n_samples = 2000
time = np.linspace(0, 8, n_samples)
s1 = np.sin(2 * time)  # Signal 1: sinusoidal signal
s2 = np.sign(np.sin(3 * time))  # Signal 2: square signal
s3 = signal.sawtooth(2 * np.pi * time)  # Signal 3: saw tooth signal
S = np.c_[s1, s2, s3]
S += 0.2 * np.random.normal(size=S.shape)  # Add noise
S /= S.std(axis=0)  # Standardize data

# Mix data
A = np.array([[1, 1, 1], [0.5, 2, 1.0], [1.5, 1.0, 2.0]])  # Mixing matrix
X = np.dot(S, A.T)  # Generate observations
# Compute ICA
ica = FastICA(n_components=3)
S_ = ica.fit_transform(X)  # Reconstruct signals
A_ = ica.mixing_  # Get estimated mixing matrix

# We can 'prove' that the ICA model applies by reverting the unmixing.
assert np.allclose(X, np.dot(S_, A_.T) + ica.mean_)

# For comparison, compute PCA
pca = PCA(n_components=3)
H = pca.fit_transform(X)  # Reconstruct signals based on orthogonal components

# Plot results
plt.figure()
models = [X, S, S_, H]
names = ['Observations (mixed signal)',
         'True Sources',
         'ICA recovered signals',
         'PCA recovered signals']
colors = ['red', 'steelblue', 'orange']

for ii, (model, name) in enumerate(zip(models, names), 1):
    plt.subplot(4, 1, ii)
    plt.title(name)
    for sig, color in zip(model.T, colors):
        plt.plot(sig, color=color)
plt.subplots_adjust(0.09, 0.04, 0.94, 0.94, 0.26, 0.46)
plt.show()

Total running time of the script: (0 minutes 0.242 seconds)

13.6 Principal components analysis (PCA)

These figures aid in illustrating how a point cloud can be very flat in one direction—which is where PCA comes in to choose a direction that is not flat.
from sklearn.decomposition import PCA
from mpl_toolkits.mplot3d import Axes3D
import numpy as np
import matplotlib.pyplot as plt
from scipy import stats

# #############################################################################
# Create the data
#
# Authors: Gael Varoquaux
#           Jaques Grobler
#           Kevin Hughes
# License: BSD 3 clause

e = np.exp(1)
np.random.seed(4)

def pdf(x):
    return 0.5 * (stats.norm(scale=0.25 / e).pdf(x)
               + stats.norm(scale=4 / e).pdf(x))

y = np.random.normal(scale=0.5, size=(30000))
x = np.random.normal(scale=0.5, size=(30000))
z = np.random.normal(scale=0.1, size=len(x))
density = pdf(x) * pdf(y)
pdf_z = pdf(5 * z)
density *= pdf_z

a = x + y
b = 2 * y
c = a - b + z

norm = np.sqrt(a.var() + b.var())
a /= norm
b /= norm

# #############################################################################
# Plot the figures

def plot_figs(fig_num, elev, azim):
    fig = plt.figure(fig_num, figsize=(4, 3))
plt.clf()
ax = Axes3D(plt, rect=[0, 0, .95, 1], elev=elev, azim=azim)

ax.scatter(a[::10], b[::10], c[::10], c=density[::10], marker='+', alpha=.4)
Y = np.c_[a, b, c]

# Using SciPy's SVD, this would be:
# _, pca_score, V = scipy.linalg.svd(Y, full_matrices=False)
pca = PCA(n_components=3)
pca.fit(Y)
pca_score = pca.explained_variance_ratio_
V = pca.components_

x_pca_axis, y_pca_axis, z_pca_axis = 3 * V.T
x_pca_plane = np.r_[x_pca_axis[:2], -x_pca_axis[1::-1]]
y_pca_plane = np.r_[y_pca_axis[:2], -y_pca_axis[1::-1]]
z_pca_plane = np.r_[z_pca_axis[:2], -z_pca_axis[1::-1]]
x_pca_plane.shape = (2, 2)
y_pca_plane.shape = (2, 2)
z_pca_plane.shape = (2, 2)

ax.plot_surface(x_pca_plane, y_pca_plane, z_pca_plane)
ax.w_xaxis.set_ticklabels([])
ax.w_yaxis.set_ticklabels([])
ax.w_zaxis.set_ticklabels([])

elev = -40
azim = -80
plot_figs(1, elev, azim)

elev = 30
azim = 20
plot_figs(2, elev, azim)

plt.show()

Total running time of the script: (0 minutes 0.185 seconds)

## 13.7 FastICA on 2D point clouds

This example illustrates visually in the feature space a comparison by results using two different component analysis techniques.

**Independent component analysis (ICA) vs Principal component analysis (PCA).**

Representing ICA in the feature space gives the view of ‘geometric ICA’: ICA is an algorithm that finds directions in the feature space corresponding to projections with high non-Gaussianity. These directions need not be orthogonal in the original feature space, but they are orthogonal in the whitened feature space, in which all directions correspond to the same variance.

PCA, on the other hand, finds orthogonal directions in the raw feature space that correspond to directions accounting for maximum variance.

Here we simulate independent sources using a highly non-Gaussian process, 2 student T with a low number of degrees of freedom (top left figure). We mix them to create observations (top right figure). In this raw observation space, directions identified by PCA are represented by orange vectors. We represent the signal in the PCA space, after
whitening by the variance corresponding to the PCA vectors (lower left). Running ICA corresponds to finding a rotation in this space to identify the directions of largest non-Gaussianity (lower right).

```python
print(__doc__)

# Authors: Alexandre Gramfort, Gael Varoquaux
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA, FastICA

# #############################################################################
# Generate sample data
rng = np.random.RandomState(42)
S = rng.standard_t(1.5, size=(20000, 2))
S[:, 0] *= 2.

# Mix data
A = np.array([[1, 1], [0, 2]])  # Mixing matrix
X = np.dot(S, A.T)  # Generate observations

pca = PCA()
S_pca_ = pca.fit(X).transform(X)
```

Chapter 13. Decomposition
ica = FastICA(random_state=rng)
S_ica_ = ica.fit(X).transform(X)  # Estimate the sources
S_ica_ /= S_ica_.std(axis=0)

# Plot results

def plot_samples(S, axis_list=None):
    plt.scatter(S[:, 0], S[:, 1], s=2, marker='o', zorder=10,
                color='steelblue', alpha=0.5)
    if axis_list is not None:
        colors = ['orange', 'red']
        for color, axis in zip(colors, axis_list):
            axis /= axis.std()
            x_axis, y_axis = axis
            # Trick to get legend to work
            plt.plot(0.1 * x_axis, 0.1 * y_axis, linewidth=2, color=color)
            plt.quiver(0, 0, x_axis, y_axis, zorder=11, width=0.01, scale=6,
                       color=color)

    plt.hlines(0, -3, 3)
    plt.vlines(0, -3, 3)
    plt.xlim(-3, 3)
    plt.ylim(-3, 3)
    plt.xlabel('x')
    plt.ylabel('y')

plt.figure()
plt.subplot(2, 2, 1)
plot_samples(S / S.std())
plt.title('True Independent Sources')

axis_list = [pca.components_.T, ica.mixing_]
plt.subplot(2, 2, 2)
plot_samples(X / np.std(X), axis_list=axis_list)
legend = plt.legend(['PCA', 'ICA'], loc='upper right')
legend.set_zorder(100)
plt.title('Observations')

plt.subplot(2, 2, 3)
plot_samples(S_pca_ / np.std(S_pca_, axis=0))
plt.title('PCA recovered signals')

plt.subplot(2, 2, 4)
plot_samples(S_ica_ / np.std(S_ica_))
plt.title('ICA recovered signals')

plt.subplots_adjust(0.09, 0.04, 0.94, 0.94, 0.26, 0.36)
plt.show()
13.8 Kernel PCA

This example shows that Kernel PCA is able to find a projection of the data that makes data linearly separable.

```
print(__doc__)

# Authors: Mathieu Blondel
# Andreas Mueller
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.decomposition import PCA, KernelPCA
from sklearn.datasets import make_circles

np.random.seed(0)
X, y = make_circles(n_samples=400, factor=.3, noise=.05)
kpca = KernelPCA(kernel="rbf", fit_inverse_transform=True, gamma=10)
X_kpca = kpca.fit_transform(X)
X_back = kpca.inverse_transform(X_kpca)
pca = PCA()
X_pca = pca.fit_transform(X)
```
```python
# Plot results
plt.figure()
plt.subplot(2, 2, 1, aspect='equal')
plt.title("Original space")
reds = y == 0
blues = y == 1

plt.scatter(X[reds, 0], X[reds, 1], c="red",
s=20, edgecolor='k')
plt.scatter(X[blues, 0], X[blues, 1], c="blue",
s=20, edgecolor='k')
plt.xlabel("$x_1$")
plt.ylabel("$x_2$")

X1, X2 = np.meshgrid(np.linspace(-1.5, 1.5, 50), np.linspace(-1.5, 1.5, 50))
X_grid = np.array([np.ravel(X1), np.ravel(X2)]).T
# projection on the first principal component (in the phi space)
Z_grid = kpca.transform(X_grid)[:, 0].reshape(X1.shape)
plt.contour(X1, X2, Z_grid, colors='grey', linewidths=1, origin='lower')
plt.subplot(2, 2, 2, aspect='equal')
plt.scatter(X_pca[reds, 0], X_pca[reds, 1], c="red",
s=20, edgecolor='k')
plt.scatter(X_pca[blues, 0], X_pca[blues, 1], c="blue",
s=20, edgecolor='k')
plt.title("Projection by PCA")
plt.xlabel("1st principal component")
plt.ylabel("2nd component")

plt.subplot(2, 2, 3, aspect='equal')
plt.scatter(X_kpca[reds, 0], X_kpca[reds, 1], c="red",
s=20, edgecolor='k')
plt.scatter(X_kpca[blues, 0], X_kpca[blues, 1], c="blue",
s=20, edgecolor='k')
plt.title("Projection by KPCA")
plt.xlabel("1st principal component in space induced by $\phi$")
plt.ylabel("2nd component")

plt.subplot(2, 2, 4, aspect='equal')
plt.scatter(X_back[reds, 0], X_back[reds, 1], c="red",
s=20, edgecolor='k')
plt.scatter(X_back[blues, 0], X_back[blues, 1], c="blue",
s=20, edgecolor='k')
plt.title("Original space after inverse transform")
plt.xlabel("$x_1$")
plt.ylabel("$x_2$")
plt.subplots_adjust(0.02, 0.10, 0.98, 0.94, 0.04, 0.35)
plt.show()
```

Total running time of the script: ( 0 minutes 0.457 seconds)
13.9 Sparse coding with a precomputed dictionary

Transform a signal as a sparse combination of Ricker wavelets. This example visually compares different sparse coding methods using the `sklearn.decomposition.SparseCoder` estimator. The Ricker (also known as Mexican hat or the second derivative of a Gaussian) is not a particularly good kernel to represent piecewise constant signals like this one. It can therefore be seen how much adding different widths of atoms matters and it therefore motivates learning the dictionary to best fit your type of signals.

The richer dictionary on the right is not larger in size, heavier subsampling is performed in order to stay on the same order of magnitude.

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn.decomposition import SparseCoder

def ricker_function(resolution, center, width):
    """Discrete sub-sampled Ricker (Mexican hat) wavelet""
    x = np.linspace(0, resolution - 1, resolution)
    x = ((2 / ((np.sqrt(3 * width) * np.pi ** 1 / 4)))
         * (1 - ((x - center) ** 2 / width ** 2))
         * np.exp(-((x - center) ** 2) / (2 * width ** 2)))
    return x

def ricker_matrix(width, resolution, n_components):
    """Dictionary of Ricker (Mexican hat) wavelets""
    centers = np.linspace(0, resolution - 1, n_components)
    D = np.empty((n_components, resolution))
    for i, center in enumerate(centers):
        D[i] = ricker_function(resolution, center, width)
    D /= np.sqrt(np.sum(D ** 2, axis=1))[:, np.newaxis]
    return D
```
resolution = 1024
subsampling = 3  # subsampling factor
width = 100
n_components = resolution // subsampling

# Compute a wavelet dictionary
D_fixed = ricker_matrix(width=width, resolution=resolution,
n_components=n_components)
D_multi = np.r_[tuple(ricker_matrix(width=w, resolution=resolution,
n_components=n_components // 5)
    for w in (10, 50, 100, 500, 1000)]]

# Generate a signal
y = np.linspace(0, resolution - 1, resolution)
first_quarter = y < resolution / 4
y[first_quarter] = 3.
y[np.logical_not(first_quarter)] = -1.

# List the different sparse coding methods in the following format:
# (title, transform_algorithm, transform_alpha, transform_n_nozero_coefs)
estimators = [('OMP', 'omp', None, 15, 'navy'),
    ('Lasso', 'lasso_cd', 2, None, 'turquoise'), ]
lw = 2

plt.figure(figsize=(13, 6))
for subplot, (D, title) in enumerate(zip((D_fixed, D_multi),
    ('fixed width', 'multiple widths'))):
    plt.subplot(1, 2, subplot + 1)
    plt.title('Sparse coding against %s dictionary' % title)
    plt.plot(y, lw=lw, linestyle='--', label='Original signal')
    # Do a wavelet approximation
    for title, algo, alpha, n_nonzero, color in estimators:
        coder = SparseCoder(dictionary=D, transform_n_nonzero_coefs=n_nonzero,
            transform_algorithm=algo)
        x = coder.transform(y.reshape(1, -1))
        density = len(np.flatnonzero(x))
        x = np.ravel(np.dot(x, D))
        squared_error = np.sum((y - x) ** 2)
        plt.plot(x, color=color, lw=lw,
            label='%s: %d nonzero coefs, %.2f error' % (title, density, squared_error))
        # Soft thresholding debiasing
        coder = SparseCoder(dictionary=D, transform_algorithm='threshold',
            transform_alpha=20)
        x = coder.transform(y.reshape(1, -1))
        _, idx = np.where(x != 0)
        x[0, idx], _, _, _ = np.linalg.lstsq(D[idx, :].T, y)
        x = np.ravel(np.dot(x, D))
        squared_error = np.sum((y - x) ** 2)
        plt.plot(x, color='darkorange', lw=lw,
            label='Thresholding w/ debiasing: %d nonzero coefs, %.2f error' % (len(idx), squared_error))
    plt.axis('tight')
    plt.legend(shadow=False, loc='best')
plt.subplots_adjust(.04, .07, .97, .90, .09, .2)
plt.show()
Probabilistic PCA and Factor Analysis are probabilistic models. The consequence is that the likelihood of new data can be used for model selection and covariance estimation. Here we compare PCA and FA with cross-validation on low rank data corrupted with homoscedastic noise (noise variance is the same for each feature) or heteroscedastic noise (noise variance is the different for each feature). In a second step we compare the model likelihood to the likelihoods obtained from shrinkage covariance estimators.

One can observe that with homoscedastic noise both FA and PCA succeed in recovering the size of the low rank subspace. The likelihood with PCA is higher than FA in this case. However PCA fails and overestimates the rank when heteroscedastic noise is present. Under appropriate circumstances the low rank models are more likely than shrinkage models.

The automatic estimation from Automatic Choice of Dimensionality for PCA. NIPS 2000: 598-604 by Thomas P. Minka is also compared.
# Authors: Alexandre Gramfort
# Denis A. Engemann
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from scipy import linalg

from sklearn.decomposition import PCA, FactorAnalysis
from sklearn.covariance import ShrunkCovariance, LedoitWolf
from sklearn.model_selection import cross_val_score
from sklearn.model_selection import GridSearchCV

print(__doc__)

# #############################################################################
# Create the data

n_samples, n_features, rank = 1000, 50, 10
sigma = 1.
rng = np.random.RandomState(42)
U, _, _ = linalg.svd(rng.randn(n_features, n_features))
X = np.dot(rng.randn(n_samples, rank), U[:, :rank].T)

# Adding homoscedastic noise
X_homo = X + sigma * rng.randn(n_samples, n_features)

# Adding heteroscedastic noise
sigmas = sigma * rng.randn(n_features) + sigma / 2.
X_hetero = X + rng.randn(n_samples, n_features) * sigmas

# #############################################################################
# Fit the models

n_components = np.arange(0, n_features, 5)
for n in n_components:
    pca = PCA(svd_solver='full')
    fa = FactorAnalysis()

    pca_scores, fa_scores = [], []
    for n in n_components:
        pca.n_components = n
        fa.n_components = n
        pca_scores.append(np.mean(cross_val_score(pca, X)))
        fa_scores.append(np.mean(cross_val_score(fa, X)))

    return pca_scores, fa_scores


def shrunk_cov_score(X):
    shrinkages = np.logspace(-2, 0, 30)
    cv = GridSearchCV(ShrunkCovariance(), {'shrinkage': shrinkages})
    return np.mean(cross_val_score(cv.fit(X).best_estimator_, X))

def lw_score(X):
    return np.mean(cross_val_score(LedoitWolf(), X))

for X, title in [(X_homo, 'Homoscedastic Noise'),
                 (X_hetero, 'Heteroscedastic Noise')]:
    pca_scores, fa_scores = compute_scores(X)
    n_components_pca = n_components[np.argmax(pca_scores)]
    n_components_fa = n_components[np.argmax(fa_scores)]

    pca = PCA(svd_solver='full', n_components='mle')
    pca.fit(X)
    n_components_pca_mle = pca.n_components_

    print("best n_components by PCA CV = \$d\" % n_components_pca)
    print("best n_components by FactorAnalysis CV = \$d\" % n_components_fa)
    print("best n_components by PCA MLE = \$d\" % n_components_pca_mle)

    plt.figure()
    plt.plot(n_components, pca_scores, 'b', label='PCA scores')
    plt.plot(n_components, fa_scores, 'r', label='FA scores')
    plt.axvline(rank, color='g', label='TRUTH: \$d\" % rank, linestyle='--')
    plt.axvline(n_components_pca, color='b',
                label='PCA CV: \$d\" % n_components_pca, linestyle='--')
    plt.axvline(n_components_fa, color='r',
                label='FactorAnalysis CV: \$d\" % n_components_fa,
                linestyle='--')
    plt.axvline(n_components_pca_mle, color='k',
                label='PCA MLE: \$d\" % n_components_pca_mle, linestyle='--')

    # compare with other covariance estimators
    plt.axhline(shrunk_cov_score(X), color='violet',
                label='Shrunk Covariance MLE', linestyle='--')
    plt.axhline(lw_score(X), color='orange',
                label='LedoitWolf MLE' % n_components_pca_mle, linestyle='--')

    plt.xlabel('nb of components')
    plt.ylabel('CV scores')
    plt.legend(loc='lower right')
    plt.title(title)

plt.show()

Total running time of the script: ( 0 minutes 12.589 seconds)

13.11 Image denoising using dictionary learning

An example comparing the effect of reconstructing noisy fragments of a raccoon face image using firstly online Dictionary Learning and various transform methods.
The dictionary is fitted on the distorted left half of the image, and subsequently used to reconstruct the right half. Note that even better performance could be achieved by fitting to an undistorted (i.e. noiseless) image, but here we start from the assumption that it is not available.

A common practice for evaluating the results of image denoising is by looking at the difference between the reconstruction and the original image. If the reconstruction is perfect this will look like Gaussian noise.

It can be seen from the plots that the results of Orthogonal Matching Pursuit (OMP) with two non-zero coefficients is a bit less biased than when keeping only one (the edges look less prominent). It is in addition closer from the ground truth in Frobenius norm.

The result of Least Angle Regression is much more strongly biased: the difference is reminiscent of the local intensity value of the original image.

Thresholding is clearly not useful for denoising, but it is here to show that it can produce a suggestive output with very high speed, and thus be useful for other tasks such as object classification, where performance is not necessarily related to visualisation.
Orthogonal Matching Pursuit
2 atoms (time: 21.5s)

Least-angle regression
5 atoms (time: 117.6s)

Thresholding
alpha=0.1 (time: 1.1s)

Out:

Distorting image...
Extracting reference patches...
done in 0.07s.
Learning the dictionary...
done in 9.12s.
Extracting noisy patches...
done in 0.03s.
Orthogonal Matching Pursuit
1 atom...
done in 10.79s.
Orthogonal Matching Pursuit
2 atoms...
done in 21.48s.
Least-angle regression
5 atoms...
done in 117.58s.
Thresholding
alpha=0.1...
done in 1.06s.
from time import time
import matplotlib.pyplot as plt
import numpy as np
import scipy as sp
from sklearn.decomposition import MiniBatchDictionaryLearning
from sklearn.feature_extraction.image import extract_patches_2d
from sklearn.feature_extraction.image import reconstruct_from_patches_2d
try:  # SciPy >= 0.16 have face in misc
    from scipy.misc import face
except ImportError:
    face = sp.face(gray=True)
# Convert from uint8 representation with values between 0 and 255 to
# a floating point representation with values between 0 and 1.
face = face / 255.
# downsample for higher speed
face = face[:, ::2, ::2] + face[:, 1::2, ::2] + face[:, ::2, 1::2] + face[:, 1::2, 1::2]
face /= 4.0
height, width = face.shape
# Distort the right half of the image
print('Distorting image...')
distorted = face.copy()
distorted[:, width // 2:] += 0.075 * np.random.randn(height, width // 2)
# Extract all reference patches from the left half of the image
print('Extracting reference patches...')
t0 = time()
patch_size = (7, 7)
data = extract_patches_2d(distorted[:, :width // 2], patch_size)
data = data.reshape(data.shape[0], -1)
data -= np.mean(data, axis=0)
data /= np.std(data, axis=0)
print('done in %.2fs.' % (time() - t0))
# Learn the dictionary from reference patches
print('Learning the dictionary...')
t0 = time()
dico = MiniBatchDictionaryLearning(n_components=100, alpha=1, n_iter=500)
V = dico.fit(data).components_
dt = time() - t0
print('done in %.2fs.' % dt)
plt.figure(figsize=(4.2, 4))
for i, comp in enumerate(V[:100]):
    plt.subplot(10, 10, i + 1)
    plt.imshow(comp.reshape(patch_size), cmap=plt.cm.gray_r, interpolation='nearest')
13.11. Image denoising using dictionary learning
# Display the distorted image

def show_with_diff(image, reference, title):
    """Helper function to display denoising"""
    plt.figure(figsize=(5, 3.3))
    plt.subplot(1, 2, 1)
    plt.title('Image')
    plt.imshow(image, vmin=0, vmax=1, cmap=plt.cm.gray,
               interpolation='nearest')
    plt.xticks(())
    plt.yticks(()
    plt.subplot(1, 2, 2)
    difference = image - reference
    plt.title('Difference (norm: %.2f)' % np.sqrt(np.sum(difference ** 2)))
    plt.imshow(difference, vmin=-0.5, vmax=0.5, cmap=plt.cm.PuOr,
               interpolation='nearest')
    plt.xticks(())
    plt.yticks()
    plt.suptitle(title, size=16)
    plt.subplots_adjust(0.02, 0.02, 0.98, 0.79, 0.02, 0.2)

show_with_diff(distorted, face, 'Distorted image')

# Extract noisy patches and reconstruct them using the dictionary

print('Extracting noisy patches... ')
t0 = time()
data = extract_patches_2d(distorted[:, width // 2:], patch_size)
data = data.reshape(data.shape[0], -1)
intercept = np.mean(data, axis=0)
data -= intercept
print('done in %.2fs.' % (time() - t0))

transform_algorithms = [
    ('Orthogonal Matching Pursuit\n1 atom', 'omp',
     {'transform_n_nonzero_coefs': 1}),
    ('Orthogonal Matching Pursuit\n2 atoms', 'omp',
     {'transform_n_nonzero_coefs': 2}),
    ('Least-angle regression\n5 atoms', 'lars',
     {'transform_n_nonzero_coefs': 5}),
    ('Thresholding\nalpha=0.1', 'threshold',
     {'transform_alpha': .1})
]

reconstructions = {}
for title, transform_algorithm, kwargs in transform_algorithms:
    print(title + '...')
    reconstructions[title] = face.copy()
t0 = time()
dico.set_params(transform_algorithm='threshold', **kwargs)

if transform_algorithm == 'threshold':
    patches -= patches.min()
    patches /= patches.max()

reconstructions[title][:, width // 2:] = reconstruct_from_patches_2d(patches, (height, width // 2))

print('done in %.2f s.' % dt)
show_with_diff(reconstructions[title], face,
               title + ' (time: %.1fs) ' % dt)

plt.show()

Total running time of the script: (2 minutes 44.511 seconds)

13.12 Faces dataset decompositions

This example applies to The Olivetti faces dataset different unsupervised matrix decomposition (dimension reduction) methods from the module sklearn.decomposition (see the documentation chapter Decomposing signals in components (matrix factorization problems)).
Out:

Dataset consists of 400 faces
Extracting the top 6 Eigenfaces - PCA using randomized SVD... done in 0.055s
Extracting the top 6 Non-negative components - NMF... done in 0.377s
Extracting the top 6 Independent components - FastICA... done in 0.236s
Extracting the top 6 Sparse comp. - MiniBatchSparsePCA... done in 1.275s
Extracting the top 6 MiniBatchDictionaryLearning... done in 1.121s
Extracting the top 6 Cluster centers - MiniBatchKMeans... done in 0.115s
Extracting the top 6 Factor Analysis components - FA... done in 0.122s
# Display progress logs on stdout
logging.basicConfig(level=logging.INFO,
                    format='%(asctime)s %(levelname)s %(message)s')

n_row, n_col = 2, 3
n_components = n_row * n_col
image_shape = (64, 64)
rng = RandomState(0)

# Load faces data
dataset = fetch_olivetti_faces(shuffle=True, random_state=rng)
faces = dataset.data

n_samples, n_features = faces.shape

# global centering
faces_centered = faces - faces.mean(axis=0)

# local centering
faces_centered -= faces_centered.mean(axis=1).reshape(n_samples, -1)

print("Dataset consists of \%d faces" % n_samples)

def plot_gallery(title, images, n_col=n_col, n_row=n_row):
    plt.figure(figsize=(2. * n_col, 2.26 * n_row))
    plt.suptitle(title, size=16)
    for i, comp in enumerate(images):
        plt.subplot(n_row, n_col, i + 1)
        vmax = max(comp.max(), -comp.min())
        plt.imshow(comp.reshape(image_shape), cmap=plt.cm.gray,
                   interpolation='nearest',
                   vmin=-vmax, vmax=vmax)
        plt.xticks(())
        plt.yticks(())
    plt.subplots_adjust(0.01, 0.05, 0.99, 0.93, 0.04, 0.)

# List of the different estimators, whether to center and transpose the
# problem, and whether the transformer uses the clustering API.
estimators = [
    ('Eigenfaces - PCA using randomized SVD',
     decomposition.PCA(n_components=n_components, svd_solver='randomized',
     random_state=rng)])
whiten=True),

('Non-negative components - NMF',
 decomposition.NMF(n_components=n_components, init='nndsvda', tol=5e-3),
 False),

('Independent components - FastICA',
 decomposition.FastICA(n_components=n_components, whiten=True),
 True),

('Sparse comp. - MiniBatchSparsePCA',
 decomposition.MiniBatchSparsePCA(n_components=n_components, alpha=0.8,
 n_iter=100, batch_size=3,
 random_state=rng),
 True),

('MiniBatchDictionaryLearning',
 decomposition.MiniBatchDictionaryLearning(n_components=15, alpha=0.1,
 n_iter=50, batch_size=3,
 random_state=rng),
 True),

('Cluster centers - MiniBatchKMeans',
 MiniBatchKMeans(n_clusters=n_components, tol=1e-3, batch_size=20,
 max_iter=50, random_state=rng),
 True),

('Factor Analysis components - FA',
 decomposition.FactorAnalysis(n_components=n_components, max_iter=2),
 True),
]

# #############################################################################
# Plot a sample of the input data

plot_gallery("First centered Olivetti faces", faces_centered[:n_components])

# Do the estimation and plot it

for name, estimator, center in estimators:
    print("Extracting the top %d %s...") % (n_components, name))
    t0 = time()
    data = faces
    if center:
        data = faces_centered
        estimator.fit(data)
    train_time = (time() - t0)
    print("done in %0.3fs" % train_time)
    if hasattr(estimator, 'cluster_centers_'):
        components_ = estimator.cluster_centers_
    else:
        components_ = estimator.components_

# Plot an image representing the pixelwise variance provided by the
# estimator e.g its noise_variance_ attribute. The Eigenfaces estimator,
# via the PCA decomposition, also provides a scalar noise_variance_
# (the mean of pixelwise variance) that cannot be displayed as an image
# so we skip it.
   if (hasattr(estimator, 'noise_variance_') and
       estimator.noise_variance_.ndim > 0):  # Skip the Eigenfaces case
       plot_gallery("Pixelwise variance",
                   estimator.noise_variance_.reshape(1, -1), n_col=1,
                   n_row=1)
       plot_gallery('
%s - Train time %.1fs
' % (name, train_time),
                   components_[:n_components])

plt.show()

**Total running time of the script:** ( 0 minutes 5.613 seconds)
Examples concerning the `sklearn.ensemble` module.

### 14.1 Decision Tree Regression with AdaBoost

A decision tree is boosted using the AdaBoost.R2\(^1\) algorithm on a 1D sinusoidal dataset with a small amount of Gaussian noise. 299 boosts (300 decision trees) is compared with a single decision tree regressor. As the number of boosts is increased the regressor can fit more detail.

---

import numpy as np
import matplotlib.pyplot as plt
from sklearn.tree import DecisionTreeRegressor
from sklearn.ensemble import AdaBoostRegressor

# Create the dataset
rng = np.random.RandomState(1)
X = np.linspace(0, 6, 100)[:, np.newaxis]
y = np.sin(X).ravel() + np.sin(6 * X).ravel() + rng.normal(0, 0.1, X.shape[0])

# Fit regression model
regr_1 = DecisionTreeRegressor(max_depth=4)
regr_2 = AdaBoostRegressor(DecisionTreeRegressor(max_depth=4),
                           n_estimators=300, random_state=rng)
regr_1.fit(X, y)
regr_2.fit(X, y)
# Predict
y_1 = regr_1.predict(X)
y_2 = regr_2.predict(X)

# Plot the results
plt.figure()
plt.scatter(X, y, c="k", label="training samples")
plt.plot(X, y_1, c="g", label="n_estimates=1", linewidth=2)
plt.plot(X, y_2, c="r", label="n_estimates=300", linewidth=2)
plt.xlabel("data")
plt.ylabel("target")
plt.title("Boosted Decision Tree Regression")
plt.legend()
plt.show()

Total running time of the script: ( 0 minutes 0.352 seconds)

14.2 Pixel importances with a parallel forest of trees

This example shows the use of forests of trees to evaluate the importance of the pixels in an image classification task (faces). The hotter the pixel, the more important.

The code below also illustrates how the construction and the computation of the predictions can be parallelized within multiple jobs.
print(__doc__)

from time import time
import matplotlib.pyplot as plt

from sklearn.datasets import fetch_olivetti_faces
from sklearn.ensemble import ExtraTreesClassifier

# Number of cores to use to perform parallel fitting of the forest model
n_jobs = 1

# Load the faces dataset
data = fetch_olivetti_faces()
X = data.images.reshape((len(data.images), -1))
y = data.target

mask = y < 5  # Limit to 5 classes
X = X[mask]
y = y[mask]

# Build a forest and compute the pixel importances
print("Fitting ExtraTreesClassifier on faces data with {} cores..." % n_jobs)
t0 = time()
forest = ExtraTreesClassifier(n_estimators=1000,
                              max_features=128,
                              n_jobs=n_jobs,
                              random_state=0)
forest.fit(X, y)
print("done in {} seconds" % (time() - t0))
importances = forest.feature_importances_
importances = importances.reshape(data.images[0].shape)

# Plot pixel importances
plt.matshow(importances, cmap=plt.cm.hot)
plt.title("Pixel importances with forests of trees")
plt.show()
Feature ranking:
1. feature 1 (0.295902)
2. feature 2 (0.208351)
3. feature 0 (0.177632)
4. feature 3 (0.047121)
5. feature 6 (0.046303)
6. feature 8 (0.046013)
7. feature 7 (0.045575)
8. feature 4 (0.044614)
9. feature 9 (0.044577)
10. feature 5 (0.043912)

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets import make_classification
from sklearn.ensemble import ExtraTreesClassifier

14.3. Feature importances with forests of trees
# Build a classification task using 3 informative features
X, y = make_classification(n_samples=1000,
    n_features=10,
    n_informative=3,
    n_redundant=0,
    n_repeated=0,
    n_classes=2,
    random_state=0,
    shuffle=False)

# Build a forest and compute the feature importances
forest = ExtraTreesClassifier(n_estimators=250,
    random_state=0)
forest.fit(X, y)
importances = forest.feature_importances_
std = np.std([tree.feature_importances_ for tree in forest.estimators_],
    axis=0)
indices = np.argsort(importances)[::-1]

# Print the feature ranking
print("Feature ranking:")
for f in range(X.shape[1]):
    print("%d. feature %d (%f)" % (f + 1, indices[f], importances[indices[f]]))

# Plot the feature importances of the forest
plt.figure()
plt.title("Feature importances")
plt.bar(range(X.shape[1]), importances[indices], color="r", yerr=std[indices], align="center")
plt.xticks(range(X.shape[1]), indices)
plt.xlim([-1, X.shape[1]]
plt.show()
import numpy as np
import matplotlib.pyplot as plt
from sklearn.ensemble import IsolationForest

rng = np.random.RandomState(42)

# Generate train data
X = 0.3 * rng.randn(100, 2)
X_train = np.r_[X + 2, X - 2]

# Generate some regular novel observations
X = 0.3 * rng.randn(20, 2)
X_test = np.r_[X + 2, X - 2]

# Generate some abnormal novel observations
X_outliers = rng.uniform(low=-4, high=4, size=(20, 2))

# fit the model
clf = IsolationForest(max_samples=100, random_state=rng)
clf.fit(X_train)
y_pred_train = clf.predict(X_train)
y_pred_test = clf.predict(X_test)
y_pred_outliers = clf.predict(X_outliers)

# plot the line, the samples, and the nearest vectors to the plane
xx, yy = np.meshgrid(np.linspace(-5, 5, 50), np.linspace(-5, 5, 50))
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)

plt.title("IsolationForest")
plt.contourf(xx, yy, Z, cmap=plt.cm.Blues_r)

b1 = plt.scatter(X_train[:, 0], X_train[:, 1], c='white',
                 s=20, edgecolor='k')
b2 = plt.scatter(X_test[:, 0], X_test[:, 1], c='green',
                 s=20, edgecolor='k')
c = plt.scatter(X_outliers[:, 0], X_outliers[:, 1], c='red',
                s=20, edgecolor='k')

plt.axis('tight')
plt.xlim((-5, 5))
plt.ylim((-5, 5))
plt.legend([b1, b2, c],
           ['training observations',
            'new regular observations', 'new abnormal observations'],
           loc="upper left")

plt.show()

Total running time of the script: ( 0 minutes 0.506 seconds)

14.5 Plot the decision boundaries of a VotingClassifier

Plot the decision boundaries of a VotingClassifier for two features of the Iris dataset.

Plot the class probabilities of the first sample in a toy dataset predicted by three different classifiers and averaged by the VotingClassifier.

First, three exemplary classifiers are initialized (DecisionTreeClassifier, KNeighborsClassifier, and SVC) and used to initialize a soft-voting VotingClassifier with weights [2, 1, 2], which means that the predicted probabilities of the DecisionTreeClassifier and SVC count 5 times as much as the weights of the KNeighborsClassifier classifier when the averaged probability is calculated.
print(__doc__)

from itertools import product

import numpy as np
import matplotlib.pyplot as plt

from sklearn import datasets
from sklearn.tree import DecisionTreeClassifier
from sklearn.neighbors import KNeighborsClassifier
from sklearn.svm import SVC
from sklearn.ensemble import VotingClassifier

# Loading some example data
iris = datasets.load_iris()
X = iris.data[:, [0, 2]]
y = iris.target

# Training classifiers
clf1 = DecisionTreeClassifier(max_depth=4)
clf2 = KNeighborsClassifier(n_neighbors=7)
clf3 = SVC(kernel='rbf', probability=True)
eclf = VotingClassifier(estimators=[('dt', clf1), ('knn', clf2),

14.5. Plot the decision boundaries of a VotingClassifier
clf1.fit(X, y)
clf2.fit(X, y)
clf3.fit(X, y)
eclf.fit(X, y)

# Plotting decision regions
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, 0.1),
                     np.arange(y_min, y_max, 0.1))

f, axarr = plt.subplots(2, 2, sharex='col', sharey='row', figsize=(10, 8))
for idx, clf, tt in zip(product([0, 1], [0, 1]),
                        [clf1, clf2, clf3, eclf],
                        ['Decision Tree (depth=4)', 'KNN (k=7)',
                         'Kernel SVM', 'Soft Voting']):
    Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])
    Z = Z.reshape(xx.shape)
    axarr[idx[0], idx[1]].contourf(xx, yy, Z, alpha=0.4)
    axarr[idx[0], idx[1]].scatter(X[:, 0], X[:, 1], c=y,
                                   s=20, edgecolor='k')
    axarr[idx[0], idx[1]].set_title(tt)

plt.show()

Total running time of the script: ( 0 minutes 0.232 seconds)

14.6 Comparing random forests and the multi-output meta estimator

An example to compare multi-output regression with random forest and the multioutput.MultiOutputRegressor meta-estimator.

This example illustrates the use of the multioutput.MultiOutputRegressor meta-estimator to perform multi-output regression. A random forest regressor is used, which supports multi-output regression natively, so the results can be compared.

The random forest regressor will only ever predict values within the range of observations or closer to zero for each of the targets. As a result the predictions are biased towards the centre of the circle.

Using a single underlying feature the model learns both the x and y coordinate as output.
# Comparing random forests and the multi-output meta estimator

```python
print(__doc__)

# Author: Tim Head <betatim@gmail.com>
#
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.ensemble import RandomForestRegressor
from sklearn.model_selection import train_test_split
from sklearn.multioutput import MultiOutputRegressor

# Create a random dataset
rng = np.random.RandomState(1)
X = np.sort(200 * rng.rand(600, 1) - 100, axis=0)
y = np.array([np.pi * np.sin(X).ravel(), np.pi * np.cos(X).ravel()]).T
y += (0.5 - rng.rand(*y.shape))

X_train, X_test, y_train, y_test = train_test_split(X, y,
                                                     train_size=400,
                                                     random_state=4)

max_depth = 30
regr_multirf = MultiOutputRegressor(RandomForestRegressor(max_depth=max_depth,
                                                            random_state=0))
```

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regr_multirf.fit(X_train, y_train)

regr_rf = RandomForestRegressor(max_depth=max_depth, random_state=2)
regr_rf.fit(X_train, y_train)

# Predict on new data
y_multirf = regr_multirf.predict(X_test)
y_rf = regr_rf.predict(X_test)

# Plot the results
plt.figure()
s = 50
a = 0.4
plt.scatter(y_test[:, 0], y_test[:, 1], edgecolor='k',
c="navy", s=s, marker="s", alpha=a, label="Data")
plt.scatter(y_multirf[:, 0], y_multirf[:, 1], edgecolor='k',
c="cornflowerblue", s=s, alpha=a,
label="Multi RF score=%.2f" % regr_multirf.score(X_test, y_test))
plt.scatter(y_rf[:, 0], y_rf[:, 1], edgecolor='k',
c="c", s=s, marker="^", alpha=a,
label="RF score=%.2f" % regr_rf.score(X_test, y_test))
plt.xlim([-6, 6])
plt.ylim([-6, 6])
plt.xlabel("target 1")
plt.ylabel("target 2")
plt.title("Comparing random forests and the multi-output meta estimator")
plt.legend()
plt.show()

**Total running time of the script:** ( 0 minutes 0.087 seconds)

### 14.7 Prediction Intervals for Gradient Boosting Regression

This example shows how quantile regression can be used to create prediction intervals.
```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.ensemble import GradientBoostingRegressor

np.random.seed(1)

def f(x):
    """The function to predict.""
    return x * np.sin(x)

# First the noiseless case
X = np.atleast_2d(np.random.uniform(0, 10.0, size=100)).T
X = X.astype(np.float32)

# Observations
y = f(X).ravel()

dy = 1.5 + 1.0 * np.random.random(y.shape)
n = np.random.normal(0, dy)
y += noise
y = y.astype(np.float32)

# Mesh the input space for evaluations of the real function, the prediction and
```
# its MSE
xx = np.atleast_2d(np.linspace(0, 10, 1000)).T
xx = xx.astype(np.float32)

alpha = 0.95

clf = GradientBoostingRegressor(loss='quantile', alpha=alpha,
    n_estimators=250, max_depth=3,
    learning_rate=.1, min_samples_leaf=9,
    min_samples_split=9)

clf.fit(X, y)

# Make the prediction on the meshed x-axis
y_upper = clf.predict(xx)

clf.set_params(alpha=1.0 - alpha)
clf.fit(X, y)

# Make the prediction on the meshed x-axis
y_lower = clf.predict(xx)

clf.set_params(loss='ls')
clf.fit(X, y)

# Make the prediction on the meshed x-axis
y_pred = clf.predict(xx)

# Plot the function, the prediction and the 90% confidence interval based on
# the MSE
fig = plt.figure()
plt.plot(xx, f(xx), 'g:', label=u'$f(x) = x\sin(x)$')
plt.plot(X, y, 'b.', markersize=10, label=u'Observations')
plt.plot(xx, y_pred, 'r-', label=u'Prediction')
plt.plot(xx, y_upper, 'k-')
plt.plot(xx, y_lower, 'k-')
plt.fill(np.concatenate([xx, xx[::-1]]),
        np.concatenate([y_upper, y_lower[::-1]]),
        alpha=.5, fc='b', ec='None', label='90% prediction interval')
plt.xlabel('$x$')
plt.ylabel('$f(x)$')
plt.ylim(-10, 20)
plt.legend(loc='upper left')
plt.show()

Total running time of the script: ( 0 minutes 0.580 seconds)

14.8 Gradient Boosting regularization

Illustration of the effect of different regularization strategies for Gradient Boosting. The example is taken from Hastie et al 2009¹.

The loss function used is binomial deviance. Regularization via shrinkage (learning_rate < 1.0) improves performance considerably. In combination with shrinkage, stochastic gradient boosting (subsample < 1.0) can

produce more accurate models by reducing the variance via bagging. Subsampling without shrinkage usually does poorly. Another strategy to reduce the variance is by subsampling the features analogous to the random splits in Random Forests (via the `max_features` parameter).
original_params = {'n_estimators': 1000, 'max_leaf_nodes': 4, 'max_depth': None, 'random_state': 2, 'min_samples_split': 5}

plt.figure()

for label, color, setting in [('No shrinkage', 'orange', {'learning_rate': 1.0, 'subsample': 1.0}), ('learning_rate=0.1', 'turquoise', {'learning_rate': 0.1, 'subsample': 1.0}), ('subsample=0.5', 'blue', {'learning_rate': 1.0, 'subsample': 0.5}), ('learning_rate=0.1, subsample=0.5', 'gray', {'learning_rate': 0.1, 'subsample': 0.5}), ('learning_rate=0.1, max_features=2', 'magenta', {'learning_rate': 0.1, 'max_features': 2})]

params = dict(original_params)
params.update(setting)
clf = ensemble.GradientBoostingClassifier(**params)
clf.fit(X_train, y_train)

# compute test set deviance
test_deviance = np.zeros((params['n_estimators'],), dtype=np.float64)

for i, y_pred in enumerate(clf.staged_decision_function(X_test)):
    # clf.loss_ assumes that y_test[i] in {0, 1}
test_deviance[i] = clf.loss_(y_test, y_pred)

plt.plot((np.arange(test_deviance.shape[0]) + 1)[::5], test_deviance[::5], '-', color=color, label=label)
plt.legend(loc='upper left')
plt.xlabel('Boosting Iterations')
plt.ylabel('Test Set Deviance')
plt.show()

Total running time of the script: ( 0 minutes 13.166 seconds)

14.9 Plot class probabilities calculated by the VotingClassifier

Plot the class probabilities of the first sample in a toy dataset predicted by three different classifiers and averaged by the VotingClassifier.

First, three examplary classifiers are initialized (LogisticRegression, GaussianNB, and RandomForestClassifier) and used to initialize a soft-voting VotingClassifier with weights [1, 1, 5], which means that the predicted probabilities of the RandomForestClassifier count 5 times as much as the weights of the other classifiers when the averaged probability is calculated.

To visualize the probability weighting, we fit each classifier on the training set and plot the predicted class probabilities for the first sample in this example dataset.
import numpy as np
import matplotlib.pyplot as plt

from sklearn.linear_model import LogisticRegression
from sklearn.naive_bayes import GaussianNB
from sklearn.ensemble import RandomForestClassifier, VotingClassifier

clf1 = LogisticRegression(random_state=123)
clf2 = RandomForestClassifier(random_state=123)
clf3 = GaussianNB()
X = np.array([[-1.0, -1.0], [-1.2, -1.4], [-3.4, -2.2], [1.1, 1.2]])
y = np.array([1, 1, 2, 2])

eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
                        voting='soft',
                        weights=[1, 1, 5])

# predict class probabilities for all classifiers
probas = [c.fit(X, y).predict_proba(X) for c in (clf1, clf2, clf3, eclf)]

# get class probabilities for the first sample in the dataset
class1_1 = [pr[0, 0] for pr in probas]
class2_1 = [pr[0, 1] for pr in probas]
# plotting

N = 4  # number of groups
ind = np.arange(N)  # group positions
width = 0.35  # bar width

fig, ax = plt.subplots()

# bars for classifier 1-3
p1 = ax.bar(ind, np.hstack((class1_1[:-1], [0])), width,
            color='green', edgecolor='k')
p2 = ax.bar(ind + width, np.hstack((class2_1[:-1], [0])), width,
            color='lightgreen', edgecolor='k')

# bars for VotingClassifier
p3 = ax.bar(ind, [0, 0, 0, class1_1[-1]], width,
            color='blue', edgecolor='k')
p4 = ax.bar(ind + width, [0, 0, 0, class2_1[-1]], width,
            color='steelblue', edgecolor='k')

# plot annotations
plt.axvline(2.8, color='k', linestyle='dashed')
ax.set_xticks(ind + width)
ax.set_xticklabels(['LogisticRegression
weight 1',
                    'GaussianNB
weight 1',
                    'RandomForestClassifier
weight 5',
                    'VotingClassifier
(average probabilities)'],
                   rotation=40,
                   ha='right')

plt.ylim([0, 1])
plt.title('Class probabilities for sample 1 by different classifiers')
plt.legend([p1[0], p2[0]], ['class 1', 'class 2'], loc='upper left')
plt.show()

Total running time of the script: ( 0 minutes 0.084 seconds)

### 14.10 Gradient Boosting regression

Demonstrate Gradient Boosting on the Boston housing dataset.

This example fits a Gradient Boosting model with least squares loss and 500 regression trees of depth 4.
MSE: 6.6213

print(__doc__)

# Author: Peter Prettenhofer <peter.prettenhofer@gmail.com>
#
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt

from sklearn import ensemble
from sklearn import datasets
from sklearn.utils import shuffle
from sklearn.metrics import mean_squared_error

# #############################################################################
# Load data
boston = datasets.load_boston()
X, y = shuffle(boston.data, boston.target, random_state=13)
X = X.astype(np.float32)
offset = int(X.shape[0] * 0.9)
X_train, y_train = X[:offset], y[:offset]
X_test, y_test = X[offset:], y[offset:]

# #############################################################################
# Fit regression model
params = {'n_estimators': 500, 'max_depth': 4, 'min_samples_split': 2,
          'learning_rate': 0.01, 'loss': 'ls'}
clf = ensemble.GradientBoostingRegressor(**params)

clf.fit(X_train, y_train)

mse = mean_squared_error(y_test, clf.predict(X_test))

print("MSE: \%.4f\n" % mse)

# #############################################################################
# Plot training deviance
# compute test set deviance

test_score = np.zeros((params['n_estimators'],), dtype=np.float64)

for i, y_pred in enumerate(clf.staged_predict(X_test)):
    test_score[i] = clf.loss_(y_test, y_pred)

plt.figure(figsize=(12, 6))
plt.subplot(1, 2, 1)
plt.title('Deviance')
plt.plot(np.arange(params['n_estimators']) + 1, clf.train_score_, 'b-',
         label='Training Set Deviance')
plt.plot(np.arange(params['n_estimators']) + 1, test_score, 'r-',
         label='Test Set Deviance')
plt.legend(loc='upper right')
plt.xlabel('Boosting Iterations')
plt.ylabel('Deviance')

# #############################################################################
# Plot feature importance

feature_importance = clf.feature_importances_

# make importances relative to max importance

feature_importance = 100.0 * (feature_importance / feature_importance.max())

sorted_idx = np.argsort(feature_importance)

pos = np.arange(sorted_idx.shape[0]) + .5

plt.subplot(1, 2, 2)
plt.barh(pos, feature_importance[sorted_idx], align='center')
plt.yticks(pos, boston.feature_names[sorted_idx])
plt.xlabel('Relative Importance')
plt.title('Variable Importance')
plt.show()

Total running time of the script: ( 0 minutes 0.549 seconds)

14.11 OOB Errors for Random Forests

The RandomForestClassifier is trained using bootstrap aggregation, where each new tree is fit from a boot-
strap sample of the training observations \( z_i = (x_i, y_i) \). The out-of-bag (OOB) error is the average error for each \( z_i \) calculated using predictions from the trees that do not contain \( z_i \) in their respective bootstrap sample. This allows the RandomForestClassifier to be fit and validated whilst being trained\(^1\).

The example below demonstrates how the OOB error can be measured at the addition of each new tree during train-
ing. The resulting plot allows a practitioner to approximate a suitable value of n_estimators at which the error stabilizes.

---

# Generate a binary classification dataset.
X, y = make_classification(n_samples=500, n_features=25,
                        n_clusters_per_class=1, n_informative=15,
                        random_state=RANDOM_STATE)

# NOTE: Setting the 'warm_start' construction parameter to 'True' disables
# support for parallelized ensembles but is necessary for tracking the OOB
# error trajectory during training.
ensemble_clfs = [  
    "RandomForestClassifier, max_features='sqrt'",

    "RandomForestClassifier, max_features='log2'",

    "RandomForestClassifier, max_features=None",

    "ExtraTreesClassifier",
]

from sklearn.datasets import make_classification
from sklearn.ensemble import RandomForestClassifier, ExtraTreesClassifier

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# License: BSD 3 Clause

print(__doc__)

RANDOM_STATE = 123
RandomForestClassifier(warm_start=True, oob_score=True, max_features="sqrt", random_state=RANDOM_STATE)),
("RandomForestClassifier, max_features='log2'", RandomForestClassifier(warm_start=True, max_features='log2', oob_score=True, random_state=RANDOM_STATE)),
("RandomForestClassifier, max_features=None", RandomForestClassifier(warm_start=True, max_features=None, oob_score=True, random_state=RANDOM_STATE))
]

# Map a classifier name to a list of (<n_estimators>, <error rate>) pairs.
error_rate = OrderedDict((label, []) for label, _ in ensemble_clfs)

# Range of `n_estimators` values to explore.
min_estimators = 15
max_estimators = 175

for label, clf in ensemble_clfs:
    for i in range(min_estimators, max_estimators + 1):
        clf.set_params(n_estimators=i)
        clf.fit(X, y)
        # Record the OOB error for each `n_estimators=i` setting.
        oob_error = 1 - clf.oob_score_
        error_rate[label].append((i, oob_error))

# Generate the "OOB error rate" vs. "n_estimators" plot.
for label, clf_err in error_rate.items():
    xs, ys = zip(*clf_err)
    plt.plot(xs, ys, label=label)
plt.xlim(min_estimators, max_estimators)
plt.xlabel("n_estimators")
plt.ylabel("OOB error rate")
plt.legend(loc="upper right")
plt.show()

Total running time of the script: ( 0 minutes 8.835 seconds)

14.12 Two-class AdaBoost

This example fits an AdaBoosted decision stump on a non-linearly separable classification dataset composed of two “Gaussian quantiles” clusters (see sklearn.datasets.make_gaussian_quantiles) and plots the decision boundary and decision scores. The distributions of decision scores are shown separately for samples of class A and B. The predicted class label for each sample is determined by the sign of the decision score. Samples with decision scores greater than zero are classified as B, and are otherwise classified as A. The magnitude of a decision score determines the degree of likeness with the predicted class label. Additionally, a new dataset could be constructed containing a desired purity of class B, for example, by only selecting samples with a decision score above some value.
```python
print(__doc__)

# Author: Noel Dawe <noel.dawe@gmail.com>
#
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt

from sklearn.ensemble import AdaBoostClassifier
from sklearn.tree import DecisionTreeClassifier
from sklearn.datasets import make_gaussian_quantiles

# Construct dataset
X1, y1 = make_gaussian_quantiles(cov=2.,
    n_samples=200, n_features=2,
    n_classes=2, random_state=1)
X2, y2 = make_gaussian_quantiles(mean=(3, 3), cov=1.5,
    n_samples=300, n_features=2,
    n_classes=2, random_state=1)
X = np.concatenate((X1, X2))
y = np.concatenate((y1, -y2 + 1))

# Create and fit an AdaBoosted decision tree
bdt = AdaBoostClassifier(DecisionTreeClassifier(max_depth=1),
    algorithm="SAMME",
    n_estimators=200)
bdt.fit(X, y)

plot_colors = "br"
plot_step = 0.02
class_names = "AB"

plt.figure(figsize=(10, 5))
```

14.12. Two-class AdaBoost

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# Plot the decision boundaries
plt.subplot(121)
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, plot_step),
                     np.arange(y_min, y_max, plot_step))
Z = bdt.predict(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
cs = plt.contourf(xx, yy, Z, cmap=plt.cm.Paired)
plt.axis("tight")

# Plot the training points
for i, n, c in zip(range(2), class_names, plot_colors):
    idx = np.where(y == i)
    plt.scatter(X[idx, 0], X[idx, 1],
                c=c, cmap=plt.cm.Paired,
                s=20, edgecolor='k',
                label="Class %s" % n)
plt.xlim(x_min, x_max)
plt.ylim(y_min, y_max)
plt.legend(loc='upper right')
plt.xlabel('x')
plt.ylabel('y')
plt.title('Decision Boundary')

# Plot the two-class decision scores
twoclass_output = bdt.decision_function(X)
plot_range = (twoclass_output.min(), twoclass_output.max())
plt.subplot(122)
for i, n, c in zip(range(2), class_names, plot_colors):
    plt.hist(twoclass_output[y == i],
             bins=10,
             range=plot_range,
             facecolor=c,
             label='Class %s' % n,
             alpha=.5,
             edgecolor='k')
x1, x2, y1, y2 = plt.axis()
plt.axis((x1, x2, y1, y2 * 1.2))
plt.legend(loc='upper right')
plt.xlabel('Score')
plt.ylabel('Samples')
plt.title('Decision Scores')

plt.tight_layout()
plt.subplots_adjust(wspace=0.35)
plt.show()

**Total running time of the script:** ( 0 minutes 2.205 seconds)

### 14.13 Hashing feature transformation using Totally Random Trees

RandomTreesEmbedding provides a way to map data to a very high-dimensional, sparse representation, which might be beneficial for classification. The mapping is completely unsupervised and very efficient.
This example visualizes the partitions given by several trees and shows how the transformation can also be used for non-linear dimensionality reduction or non-linear classification.

Points that are neighboring often share the same leaf of a tree and therefore share large parts of their hashed representation. This allows to separate two concentric circles simply based on the principal components of the transformed data with truncated SVD.

In high-dimensional spaces, linear classifiers often achieve excellent accuracy. For sparse binary data, BernoulliNB is particularly well-suited. The bottom row compares the decision boundary obtained by BernoulliNB in the transformed space with an ExtraTreesClassifier forests learned on the original data.

```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.datasets import make_circles
from sklearn.ensemble import RandomTreesEmbedding, ExtraTreesClassifier
from sklearn.decomposition import TruncatedSVD
from sklearn.naive_bayes import BernoulliNB

# make a synthetic dataset
```
X, y = make_circles(factor=0.5, random_state=0, noise=0.05)

# use RandomTreesEmbedding to transform data
hasher = RandomTreesEmbedding(n_estimators=10, random_state=0, max_depth=3)
X_transformed = hasher.fit_transform(X)

# Visualize result after dimensionality reduction using truncated SVD
svd = TruncatedSVD(n_components=2)
X_reduced = svd.fit_transform(X_transformed)

# Learn a Naive Bayes classifier on the transformed data
nb = BernoulliNB()
nb.fit(X_transformed, y)

# Learn an ExtraTreesClassifier for comparison
trees = ExtraTreesClassifier(max_depth=3, n_estimators=10, random_state=0)
trees.fit(X, y)

# scatter plot of original and reduced data
fig = plt.figure(figsize=(9, 8))
ax = plt.subplot(221)
ax.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
am.set_title("Original Data (2d)")
am.set_xticks(())
am.set_yticks(())

ax = plt.subplot(222)
ax.scatter(X_reduced[:, 0], X_reduced[:, 1], c=y, s=50, edgecolor='k')
am.set_title("Truncated SVD reduction (2d) of transformed data (%dd)" % X_transformed.shape[1])
am.set_xticks(())
am.set_yticks(())

# Plot the decision in original space. For that, we will assign a color
# to each point in the mesh [x_min, x_max]x[y_min, y_max].
h = .01
x_min, x_max = X[:, 0].min() - .5, X[:, 0].max() + .5
y_min, y_max = X[:, 1].min() - .5, X[:, 1].max() + .5
xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))

# transform grid using RandomTreesEmbedding
transformed_grid = hasher.transform(np.c_[xx.ravel(), yy.ravel()])
y_grid_pred = nb.predict_proba(transformed_grid)[:, 1]

ax = plt.subplot(223)
am.set_title("Naive Bayes on Transformed data")
am.pcolormesh(xx, yy, y_grid_pred.reshape(xx.shape))
am.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
am.set_ylim(-1.4, 1.4)
am.set_xlim(-1.4, 1.4)
am.set_xticks(())
am.set_yticks(())

# transform grid using ExtraTreesClassifier
y_grid_pred = trees.predict_proba(np.c_[xx.ravel(), yy.ravel()])[:, 1]

ax = plt.subplot(224)
am.set_title("ExtraTreesClassifier on Transformed data")
am.pcolormesh(xx, yy, y_grid_pred.reshape(xx.shape))
am.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
am.set_ylim(-1.4, 1.4)
am.set_xlim(-1.4, 1.4)
am.set_xticks(())
am.set_yticks(())

# scatter plot of original and reduced data
fig = plt.figure(figsize=(9, 8))
ax = plt.subplot(221)
ax.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
am.set_title("Original Data (2d)")
am.set_xticks(())
am.set_yticks(())

ax = plt.subplot(222)
ax.scatter(X_reduced[:, 0], X_reduced[:, 1], c=y, s=50, edgecolor='k')
am.set_title("Truncated SVD reduction (2d) of transformed data (%dd)" % X_transformed.shape[1])
am.set_xticks(())
am.set_yticks(())

# Plot the decision in original space. For that, we will assign a color
# to each point in the mesh [x_min, x_max]x[y_min, y_max].
h = .01
x_min, x_max = X[:, 0].min() - .5, X[:, 0].max() + .5
y_min, y_max = X[:, 1].min() - .5, X[:, 1].max() + .5
xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))

# transform grid using RandomTreesEmbedding
transformed_grid = hasher.transform(np.c_[xx.ravel(), yy.ravel()])
y_grid_pred = nb.predict_proba(transformed_grid)[:, 1]

ax = plt.subplot(223)
am.set_title("Naive Bayes on Transformed data")
am.pcolormesh(xx, yy, y_grid_pred.reshape(xx.shape))
am.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
am.set_ylim(-1.4, 1.4)
am.set_xlim(-1.4, 1.4)
am.set_xticks(())
am.set_yticks(())

# transform grid using ExtraTreesClassifier
y_grid_pred = trees.predict_proba(np.c_[xx.ravel(), yy.ravel()])[:, 1]
ax = plt.subplot(224)
ax.set_title("ExtraTrees predictions")
ax.pcolormesh(xx, yy, y_grid_pred.reshape(xx.shape))
ax.scatter(X[:, 0], X[:, 1], c=y, s=50, edgecolor='k')
ax.set_ylim(-1.4, 1.4)
ax.set_xlim(-1.4, 1.4)
ax.set_xticks(())
ax.set_yticks(())
plt.tight_layout()
plt.show()

Total running time of the script: ( 0 minutes 0.511 seconds)

14.14 Partial Dependence Plots

Partial dependence plots show the dependence between the target function and a set of ‘target’ features, marginalizing over the values of all other features (the complement features). Due to the limits of human perception the size of the target feature set must be small (usually, one or two) thus the target features are usually chosen among the most important features (see feature_importances_).

This example shows how to obtain partial dependence plots from a GradientBoostingRegressor trained on the California housing dataset. The example is taken from 1.

The plot shows four one-way and one two-way partial dependence plots. The target variables for the one-way PDP are: median income (\textit{MedInc}), avg. occupants per household (\textit{AvgOccup}), median house age (\textit{HouseAge}), and avg. rooms per household (\textit{AveRooms}).

We can clearly see that the median house price shows a linear relationship with the median income (top left) and that the house price drops when the avg. occupants per household increases (top middle). The top right plot shows that the house age in a district does not have a strong influence on the (median) house price; so does the average rooms per household. The tick marks on the x-axis represent the deciles of the feature values in the training data.

Partial dependence plots with two target features enable us to visualize interactions among them. The two-way partial dependence plot shows the dependence of median house price on joint values of house age and avg. occupants per household. We can clearly see an interaction between the two features: For an avg. occupancy greater than two, the house price is nearly independent of the house age, whereas for values less than two there is a strong dependence on age.

---

2 For classification you can think of it as the regression score before the link function.

Out:

Training GBRT...
done.
Convenience plot with `partial_dependence_plots`
Custom 3d plot via `partial_dependence`

```python
from __future__ import print_function
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from mpl_toolkits.mplot3d import Axes3D

from sklearn.model_selection import train_test_split
from sklearn.ensemble import GradientBoostingRegressor
from sklearn.ensemble.partial_dependence import plot_partial_dependence
from sklearn.ensemble.partial_dependence import partial_dependence
from sklearn.datasets.california_housing import fetch_california_housing
```
```python
def main():
    cal_housing = fetch_california_housing()

    # split 80/20 train-test
    X_train, X_test, y_train, y_test = train_test_split(cal_housing.data,
                                                        cal_housing.target,
                                                        test_size=0.2,
                                                        random_state=1)

    names = cal_housing.feature_names

    print("Training GBRT...")
    clf = GradientBoostingRegressor(n_estimators=100, max_depth=4,
                                    learning_rate=0.1, loss='huber',
                                    random_state=1)

    clf.fit(X_train, y_train)
    print(" done.")

    print('Convenience plot with ``partial_dependence_plots``')
    features = [0, 5, 1, 2, (5, 1)]
    fig, axs = plot_partial_dependence(clf, X_train, features,
                                        feature_names=names,
                                        n_jobs=3, grid_resolution=50)
    fig.suptitle('Partial dependence of house value on nonlocation features
            for the California housing dataset')
    plt.subplots_adjust(top=0.9)
    # tight_layout causes overlap with suptitle

    print('Custom 3d plot via ``partial_dependence``')
    fig = plt.figure()
    target_feature = (1, 5)

    pdp, axes = partial_dependence(clf, target_feature,
                                    X=X_train, grid_resolution=50)
    XX, YY = np.meshgrid(axes[0], axes[1])
    Z = pdp[0].reshape(list(map(np.size, axes))).T
    ax = Axes3D(fig)
    surf = ax.plot_surface(XX, YY, Z, rstride=1, cstride=1,
                            cmap=plt.cm.BuPu, edgecolor='k')
    ax.set_xlabel(names[target_feature[0]])
    ax.set_ylabel(names[target_feature[1]])
    ax.set_zlabel('Partial dependence')
    # pretty init view
    ax.view_init(elev=22, azim=122)
    plt.colorbar(surf)
    plt.suptitle('Partial dependence of house value on median
            age and average occupancy')
    plt.subplots_adjust(top=0.9)

    plt.show()

    # Needed on Windows because plot_partial_dependence uses multiprocessing
if __name__ == '__main__':
    main()

Total running time of the script: ( 0 minutes 3.265 seconds)
```

14.15 Discrete versus Real AdaBoost

This example is based on Figure 10.2 from Hastie et al 2009\(^1\) and illustrates the difference in performance between the discrete SAMME\(^2\) boosting algorithm and real SAMME.R boosting algorithm. Both algorithms are evaluated on a binary classification task where the target \(Y\) is a non-linear function of 10 input features.

Discrete SAMME AdaBoost adapts based on errors in predicted class labels whereas real SAMME.R uses the predicted class probabilities.

---


from sklearn.metrics import zero_one_loss
from sklearn.ensemble import AdaBoostClassifier

n_estimators = 400
# A learning rate of 1. may not be optimal for both SAMME and SAMME.R
learning_rate = 1.

X, y = datasets.make_hastie_10_2(n_samples=12000, random_state=1)
X_test, y_test = X[2000:], y[2000:]
X_train, y_train = X[:2000], y[:2000]
dt_stump = DecisionTreeClassifier(max_depth=1, min_samples_leaf=1)
dt_stump.fit(X_train, y_train)
dt_stump_err = 1.0 - dt_stump.score(X_test, y_test)
dt = DecisionTreeClassifier(max_depth=9, min_samples_leaf=1)
dt.fit(X_train, y_train)
dt_err = 1.0 - dt.score(X_test, y_test)
ada_discrete = AdaBoostClassifier(
    base_estimator=dt_stump,
    learning_rate=learning_rate,
    n_estimators=n_estimators,
    algorithm="SAMME")
ada_discrete.fit(X_train, y_train)

ada_real = AdaBoostClassifier(
    base_estimator=dt_stump,
    learning_rate=learning_rate,
    n_estimators=n_estimators,
    algorithm="SAMME.R")
ada_real.fit(X_train, y_train)

fig = plt.figure()
ax = fig.add_subplot(111)
ax.plot([1, n_estimators], [dt_stump_err] * 2, 'k-',
        label='Decision Stump Error')
ax.plot([1, n_estimators], [dt_err] * 2, 'k--',
        label='Decision Tree Error')

ada_discrete_err = np.zeros((n_estimators,))
for i, y_pred in enumerate(ada_discrete.staged_predict(X_test)):
    ada_discrete_err[i] = zero_one_loss(y_pred, y_test)

ada_discrete_err_train = np.zeros((n_estimators,))
for i, y_pred in enumerate(ada_discrete.staged_predict(X_train)):
    ada_discrete_err_train[i] = zero_one_loss(y_pred, y_train)

ada_real_err = np.zeros((n_estimators,))
for i, y_pred in enumerate(ada_real.staged_predict(X_test)):
    ada_real_err[i] = zero_one_loss(y_pred, y_test)

ada_real_err_train = np.zeros((n_estimators,))
for i, y_pred in enumerate(ada_real.staged_predict(X_train)):
    ada_real_err_train[i] = zero_one_loss(y_pred, y_train)

14.15. Discrete versus Real AdaBoost
14.16 Multi-class AdaBoosted Decision Trees

This example reproduces Figure 1 of Zhu et al\(^1\) and shows how boosting can improve prediction accuracy on a multi-class problem. The classification dataset is constructed by taking a ten-dimensional standard normal distribution and defining three classes separated by nested concentric ten-dimensional spheres such that roughly equal numbers of samples are in each class (quantiles of the \(\chi^2\) distribution).

The performance of the SAMME and SAMME.R\(^1\) algorithms are compared. SAMME.R uses the probability estimates to update the additive model, while SAMME uses the classifications only. As the example illustrates, the SAMME.R algorithm typically converges faster than SAMME, achieving a lower test error with fewer boosting iterations. The error of each algorithm on the test set after each boosting iteration is shown on the left, the classification error on the test set of each tree is shown in the middle, and the boost weight of each tree is shown on the right. All trees have a weight of one in the SAMME.R algorithm and therefore are not shown.

---

from sklearn.externals.six.moves import zip
import matplotlib.pyplot as plt
from sklearn.datasets import make_gaussian_quantiles
from sklearn.ensemble import AdaBoostClassifier
from sklearn.metrics import accuracy_score
from sklearn.tree import DecisionTreeClassifier

X, y = make_gaussian_quantiles(n_samples=13000, n_features=10,
                               n_classes=3, random_state=1)
n_split = 3000
X_train, X_test = X[:n_split], X[n_split:]
y_train, y_test = y[:n_split], y[n_split:]

bdt_real = AdaBoostClassifier(
    DecisionTreeClassifier(max_depth=2),
    n_estimators=600,
    learning_rate=1)

bdt_discrete = AdaBoostClassifier(
    DecisionTreeClassifier(max_depth=2),
    n_estimators=600,
    learning_rate=1.5,
    algorithm="SAMME")

bdt_real.fit(X_train, y_train)
bdt_discrete.fit(X_train, y_train)

real_test_errors = []
discrete_test_errors = []

for real_test_predict, discrete_train_predict in zip(
    bdt_real.staged_predict(X_test), bdt_discrete.staged_predict(X_test)):
real_test_errors.append(1. - accuracy_score(real_test_predict, y_test))
discrete_test_errors.append(1. - accuracy_score(discrete_train_predict, y_test))

n_trees_discrete = len(bdt_discrete)
n_trees_real = len(bdt_real)

# Boosting might terminate early, but the following arrays are always # n_estimators long. We crop them to the actual number of trees here:
discrete_estimator_errors = bdt_discrete.estimator_errors_[:n_trees_discrete]
real_estimator_errors = bdt_real.estimator_errors_[:n_trees_real]
discrete_estimator_weights = bdt_discrete.estimator_weights_[:n_trees_discrete]

plt.figure(figsize=(15, 5))
plt.subplot(131)
plt.plot(range(1, n_trees_discrete + 1),
         discrete_test_errors, c='black', label='SAMME')
plt.plot(range(1, n_trees_real + 1),
         real_test_errors, c='black', linestyle='dashed', label='SAMME.R')
plt.legend()
plt.ylim(0.18, 0.62)
plt.ylabel('Test Error')
plt.xlabel('Number of Trees')
plt.subplot(132)
plt.plot(range(1, n_trees_discrete + 1),
         discrete_estimator_errors,
         "b", label='SAMME', alpha=.5)
plt.plot(range(1, n_trees_real + 1),
         real_estimator_errors,
         "r", label='SAMME.R', alpha=.5)
plt.legend()
plt.ylabel('Error')
plt.xlabel('Number of Trees')
plt.ylim(.2,
         max(real_estimator_errors.max(),
             discrete_estimator_errors.max()) * 1.2)
plt.xlim((-20, len(bdt_discrete) + 20))
plt.subplot(133)
plt.plot(range(1, n_trees_discrete + 1),
         discrete_estimator_weights,
         "b", label='SAMME')
plt.legend()
plt.ylabel('Weight')
plt.xlabel('Number of Trees')
plt.ylim(0, discrete_estimator_weights.max() * 1.2)
plt.xlim((-20, n_trees_discrete + 20))

# prevent overlapping y-axis labels
plt.subplots_adjust(wspace=0.25)
plt.show()
14.17 Early stopping of Gradient Boosting

Gradient boosting is an ensembling technique where several weak learners (regression trees) are combined to yield a powerful single model, in an iterative fashion.

Early stopping support in Gradient Boosting enables us to find the least number of iterations which is sufficient to build a model that generalizes well to unseen data.

The concept of early stopping is simple. We specify a validation_fraction which denotes the fraction of the whole dataset that will be kept aside from training to assess the validation loss of the model. The gradient boosting model is trained using the training set and evaluated using the validation set. When each additional stage of regression tree is added, the validation set is used to score the model. This is continued until the scores of the model in the last n_iter_no_change stages do not improve by at least tol. After that the model is considered to have converged and further addition of stages is "stopped early".

The number of stages of the final model is available at the attribute n_estimators_.

This example illustrates how the early stopping can be used in the sklearn.ensemble.GradientBoostingClassifier model to achieve almost the same accuracy as compared to a model built without early stopping using many fewer estimators. This can significantly reduce training time, memory usage and prediction latency.

```python
import time
import numpy as np
import matplotlib.pyplot as plt
from sklearn import ensemble
from sklearn import datasets
from sklearn.model_selection import train_test_split

# Authors: Vighnesh Birodkar <vighneshbirodkar@nyu.edu>
#          Raghav RV <rvraghav93@gmail.com>
# License: BSD 3 clause

print(__doc__)

data_list = [datasets.load_iris(), datasets.load_digits()]
data_list = [(d.data, d.target) for d in data_list]
data_list += [datasets.make_hastie_10_2()]
names = ['Iris Data', 'Digits Data', 'Hastie Data']

n_gb = []
score_gb = []
time_gb = []
n_gbes = []
score_gbes = []
time_gbes = []
n_estimators = 500

for X, y in data_list:
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.2,
                                                    random_state=0)

    # We specify that if the scores don't improve by at least 0.01 for the last
    # 10 stages, stop fitting additional stages
    gbes = ensemble.GradientBoostingClassifier(n_estimators=n_estimators,
```
gb = ensemble.GradientBoostingClassifier(n_estimators=n_estimators,
    random_state=0)

start = time.time()
gb.fit(X_train, y_train)
time_gb.append(time.time() - start)

start = time.time()
gbes.fit(X_train, y_train)
time_gbes.append(time.time() - start)

score_gb.append(gb.score(X_test, y_test))
score_gbes.append(gbes.score(X_test, y_test))

n_gb.append(gb.n_estimators_)
n_gbes.append(gbes.n_estimators_)

bar_width = 0.2
n = len(data_list)
index = np.arange(0, n * bar_width, bar_width) * 2.5
index = index[0:n]

14.17.1 Compare scores with and without early stopping

plt.figure(figsize=(9, 5))

bar1 = plt.bar(index, score_gb, bar_width, label='Without early stopping',
    color='crimson')
bar2 = plt.bar(index + bar_width, score_gbes, bar_width,
    label='With early stopping', color='coral')

plt.xticks(index + bar_width, names)
plt.yticks(np.arange(0, 1.3, 0.1))

def autolabel(rects, n_estimators):
    """
    Attach a text label above each bar displaying n_estimators of each model
    """
    for i, rect in enumerate(rects):
        plt.text(rect.get_x() + rect.get_width() / 2.,
            1.05 * rect.get_height(), 'n_est=%d' % n_estimators[i],
            ha='center', va='bottom')

autolabel(bar1, n_gb)
autolabel(bar2, n_gbes)

plt.ylim([0, 1.3])
plt.legend(loc='best')
plt.grid(True)
plt.xlabel('Datasets')
plt.ylabel('Test score')
14.17.2 Compare fit times with and without early stopping

```python
plt.figure(figsize=(9, 5))
bar1 = plt.bar(index, time_gb, bar_width, label='Without early stopping',
               color='crimson')
bar2 = plt.bar(index + bar_width, time_gbes, bar_width,
               label='With early stopping', color='coral')
max_y = np.amax(np.maximum(time_gb, time_gbes))
plt.xticks(index + bar_width, names)
plt.yticks(np.linspace(0, 1.3 * max_y, 13))
autolabel(bar1, n_gb)
autolabel(bar2, n_gbes)
plt.ylim([0, 1.3 * max_y])
plt.legend(loc='best')
plt.grid(True)
plt.xlabel('Datasets')
plt.ylabel('Fit Time')
plt.show()
```

14.17. Early stopping of Gradient Boosting
14.18 Feature transformations with ensembles of trees

Transform your features into a higher dimensional, sparse space. Then train a linear model on these features.

First fit an ensemble of trees (totally random trees, a random forest, or gradient boosted trees) on the training set. Then each leaf of each tree in the ensemble is assigned a fixed arbitrary feature index in a new feature space. These leaf indices are then encoded in a one-hot fashion.

Each sample goes through the decisions of each tree of the ensemble and ends up in one leaf per tree. The sample is encoded by setting feature values for these leaves to 1 and the other feature values to 0.

The resulting transformer has then learned a supervised, sparse, high-dimensional categorical embedding of the data.
import numpy as np
np.random.seed(10)

import matplotlib.pyplot as plt
from sklearn.datasets import make_classification
from sklearn.linear_model import LogisticRegression
from sklearn.ensemble import (RandomTreesEmbedding, RandomForestClassifier, GradientBoostingClassifier)
from sklearn.preprocessing import OneHotEncoder
from sklearn.model_selection import train_test_split
from sklearn.metrics import roc_curve
from sklearn.pipeline import make_pipeline

n_estimator = 10
X, y = make_classification(n_samples=80000)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.5)
# It is important to train the ensemble of trees on a different subset
# of the training data than the linear regression model to avoid
# overfitting, in particular if the total number of leaves is
# similar to the number of training samples
X_train, X_train_lr, y_train, y_train_lr = train_test_split(X_train, y_train, test_size=0.5)

# Unsupervised transformation based on totally random trees
rt = RandomTreesEmbedding(max_depth=3, n_estimators=n_estimator, random_state=0)
rt_lm = LogisticRegression()
pipeline = make_pipeline(rt, rt_lm)
pipeline.fit(X_train, y_train)
y_pred_rt = pipeline.predict_proba(X_test)[:, 1]
fpr_rt_lm, tpr_rt_lm, _ = roc_curve(y_test, y_pred_rt)

# Supervised transformation based on random forests
rf = RandomForestClassifier(max_depth=3, n_estimators=n_estimator)
rf_enc = OneHotEncoder()
rf_lm = LogisticRegression()
rf.fit(X_train, y_train)
rf_enc.fit(rf.apply(X_train))
rf_lm.fit(rf_enc.transform(rf.apply(X_train_lr)), y_train_lr)

y_pred_rf_lm = rf_lm.predict_proba(rf_enc.transform(rf.apply(X_test)))[, 1]
fpr_rf_lm, tpr_rf_lm, _ = roc_curve(y_test, y_pred_rf_lm)

grd = GradientBoostingClassifier(n_estimators=n_estimator)
grd_enc = OneHotEncoder()
grd_lm = LogisticRegression()
grd.fit(X_train, y_train)
grd_enc.fit(grd.apply(X_train)[ :, :, 0])
grd_lm.fit(grd_enc.transform(grd.apply(X_train_lr)[ :, :, 0]), y_train_lr)

y_pred_grd_lm = grd_lm.predict_proba(grd_enc.transform(grd.apply(X_test)[ :, :, 0]))[:, 1]
fpr_grd_lm, tpr_grd_lm, _ = roc_curve(y_test, y_pred_grd_lm)

# The gradient boosted model by itself
y_pred_grd = grd.predict_proba(X_test)[ :, 1]
fpr_grd, tpr_grd, _ = roc_curve(y_test, y_pred_grd)

# The random forest model by itself
y_pred_rf = rf.predict_proba(X_test)[ :, 1]
fpr_rf, tpr_rf, _ = roc_curve(y_test, y_pred_rf)

plt.figure(1)
plt.plot([0, 1], [0, 1], 'k--')
plt.plot(fpr_rf_lm, tpr_rf_lm, label='RT + LR')
plt.plot(fpr_rf, tpr_rf, label='RF')
plt.plot(fpr_grd, tpr_grd, label='GBT')
plt.plot(fpr_grd_lm, tpr_grd_lm, label='GBT + LR')
plt.xlabel('False positive rate')
plt.ylabel('True positive rate')
plt.title('ROC curve')
plt.legend(loc='best')
plt.show()

plt.figure(2)
plt.xlim(0, 0.2)
plt.ylim(0.8, 1)
plt.plot([0, 1], [0, 1], 'k--')
plt.plot(fpr_rf_lm, tpr_rf_lm, label='RT + LR')
plt.plot(fpr_rf, tpr_rf, label='RF')
plt.plot(fpr_grd, tpr_grd, label='GBT')
plt.plot(fpr_grd_lm, tpr_grd_lm, label='GBT + LR')
plt.xlabel('False positive rate')
plt.ylabel('True positive rate')
plt.title('ROC curve (zoomed in at top left)')
plt.legend(loc='best')
plt.show()
14.19 Gradient Boosting Out-of-Bag estimates

Out-of-bag (OOB) estimates can be a useful heuristic to estimate the “optimal” number of boosting iterations. OOB estimates are almost identical to cross-validation estimates but they can be computed on-the-fly without the need for repeated model fitting. OOB estimates are only available for Stochastic Gradient Boosting (i.e. \texttt{subsample < 1.0}), the estimates are derived from the improvement in loss based on the examples not included in the bootstrap sample (the so-called out-of-bag examples). The OOB estimator is a pessimistic estimator of the true test loss, but remains a fairly good approximation for a small number of trees.

The figure shows the cumulative sum of the negative OOB improvements as a function of the boosting iteration. As you can see, it tracks the test loss for the first hundred iterations but then diverges in a pessimistic way. The figure also shows the performance of 3-fold cross validation which usually gives a better estimate of the test loss but is computationally more demanding.

Out:

```
Accuracy: 0.6840
```

```python
print(__doc__)
```
# Author: Peter Prettenhofer <peter.prettenhofer@gmail.com>
# License: BSD 3 clause

```python
import numpy as np
import matplotlib.pyplot as plt

from sklearn import ensemble
from sklearn.model_selection import KFold
from sklearn.model_selection import train_test_split

# Generate data (adapted from G. Ridgeway's gbm example)
n_samples = 1000
random_state = np.random.RandomState(13)
x1 = random_state.uniform(size=n_samples)
x2 = random_state.uniform(size=n_samples)
x3 = random_state.randint(0, 4, size=n_samples)
p = 1 / (1.0 + np.exp(-np.sin(3 * x1) - 4 * x2 + x3))
y = random_state.binomial(1, p, size=n_samples)
X = np.c_[x1, x2, x3]
X = X.astype(np.float32)
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.5,
random_state=9)

# Fit classifier with out-of-bag estimates
params = {'n_estimators': 1200, 'max_depth': 3, 'subsample': 0.5,
    'learning_rate': 0.01, 'min_samples_leaf': 1, 'random_state': 3}
clf = ensemble.GradientBoostingClassifier(**params)
clf.fit(X_train, y_train)
acc = clf.score(X_test, y_test)
print("Accuracy: {:.4f}".format(acc))

n_estimators = params['n_estimators']
x = np.arange(n_estimators) + 1

def heldout_score(clf, X_test, y_test):
    """compute deviance scores on \'X_test\' and \'y_test\'. ""
    score = np.zeros((n_estimators,), dtype=np.float64)
    for i, y_pred in enumerate(clf.staged_decision_function(X_test)):
        score[i] = clf.loss_(y_test, y_pred)
    return score

def cv_estimate(n_splits=3):
    cv = KFold(n_splits=n_splits)
cv_clf = ensemble.GradientBoostingClassifier(**params)
val_scores = np.zeros((n_estimators,), dtype=np.float64)
    for train, test in cv.split(X_train, y_train):
        cv_clf.fit(X_train[train], y_train[train])
        val_scores += heldout_score(cv_clf, X_train[test], y_train[test])
    val_scores /= n_splits
    return val_scores
```

# Generate data (adapted from G. Ridgeway's gbm example)

---

Chapter 14. Ensemble methods
# Estimate best n_estimator using cross-validation

cv_score = cv_estimate(3)

# Compute best n_estimator for test data

test_score = heldout_score(clf, X_test, y_test)

# negative cumulative sum of oob improvements

cumsum = -np.cumsum(clf.oob_improvement_)

# min loss according to OOB

oob_best_iter = x[np.argmin(cumsum)]

# min loss according to test (normalize such that first loss is 0)

test_score -= test_score[0]
test_best_iter = x[np.argmin(test_score)]

# min loss according to cv (normalize such that first loss is 0)

cv_score -= cv_score[0]
cv_best_iter = x[np.argmin(cv_score)]

# color brew for the three curves

oob_color = list(map(lambda x: x / 256.0, (190, 174, 212)))
test_color = list(map(lambda x: x / 256.0, (127, 201, 127)))
cv_color = list(map(lambda x: x / 256.0, (253, 192, 134)))

# plot curves and vertical lines for best iterations

plt.plot(x, cumsum, label='OOB loss', color=oob_color)
plt.plot(x, test_score, label='Test loss', color=test_color)
plt.plot(x, cv_score, label='CV loss', color=cv_color)
plt.axvline(x=oob_best_iter, color=oob_color)
plt.axvline(x=test_best_iter, color=test_color)
plt.axvline(x=cv_best_iter, color=cv_color)

# add three vertical lines to xticks

xticks = plt.xticks()
xticks_pos = np.array(xticks[0].tolist() +
        [oob_best_iter, cv_best_iter, test_best_iter])
xticks_label = np.array(list(map(lambda t: int(t), xticks[0])) +
        ['OOB', 'CV', 'Test'])
ind = np.argsort(xticks_pos)
xticks_pos = xticks_pos[ind]
xticks_label = xticks_label[ind]
plt.xticks(xticks_pos, xticks_label)

plt.legend(loc='upper right')
plt.ylabel('normalized loss')
plt.xlabel('number of iterations')
plt.show()

Total running time of the script: ( 0 minutes 4.622 seconds)
14.20 Single estimator versus bagging: bias-variance decomposition

This example illustrates and compares the bias-variance decomposition of the expected mean squared error of a single estimator against a bagging ensemble.

In regression, the expected mean squared error of an estimator can be decomposed in terms of bias, variance and noise. On average over datasets of the regression problem, the bias term measures the average amount by which the predictions of the estimator differ from the predictions of the best possible estimator for the problem (i.e., the Bayes model). The variance term measures the variability of the predictions of the estimator when fit over different instances LS of the problem. Finally, the noise measures the irreducible part of the error which is due the variability in the data.

The upper left figure illustrates the predictions (in dark red) of a single decision tree trained over a random dataset LS (the blue dots) of a toy 1d regression problem. It also illustrates the predictions (in light red) of other single decision trees trained over other (and different) randomly drawn instances LS of the problem. Intuitively, the variance term here corresponds to the width of the beam of predictions (in light red) of the individual estimators. The larger the variance, the more sensitive are the predictions for $x$ to small changes in the training set. The bias term corresponds to the difference between the average prediction of the estimator (in cyan) and the best possible model (in dark blue). On this problem, we can thus observe that the bias is quite low (both the cyan and the blue curves are close to each other) while the variance is large (the red beam is rather wide).

The lower left figure plots the pointwise decomposition of the expected mean squared error of a single decision tree. It confirms that the bias term (in blue) is low while the variance is large (in green). It also illustrates the noise part of the error which, as expected, appears to be constant and around $0.01$.

The right figures correspond to the same plots but using instead a bagging ensemble of decision trees. In both figures, we can observe that the bias term is larger than in the previous case. In the upper right figure, the difference between the average prediction (in cyan) and the best possible model is larger (e.g., notice the offset around $x=2$). In the lower right figure, the bias curve is also slightly higher than in the lower left figure. In terms of variance however, the beam of predictions is narrower, which suggests that the variance is lower. Indeed, as the lower right figure confirms, the variance term (in green) is lower than for single decision trees. Overall, the bias- variance decomposition is therefore no longer the same. The tradeoff is better for bagging: averaging several decision trees fit on bootstrap copies of the dataset slightly increases the bias term but allows for a larger reduction of the variance, which results in a lower overall mean squared error (compare the red curves int the lower figures). The script output also confirms this intuition. The total error of the bagging ensemble is lower than the total error of a single decision tree, and this difference indeed mainly stems from a reduced variance.

For further details on bias-variance decomposition, see section 7.3 of\(^1\).

---

14.20.1 References

Out:

Tree: 0.0255 (error) = 0.0003 (bias^2) + 0.0152 (var) + 0.0098 (noise)
Bagging(Tree): 0.0196 (error) = 0.0004 (bias^2) + 0.0092 (var) + 0.0098 (noise)

print(__doc__)

# Author: Gilles Louppe <g.louppe@gmail.com>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.ensemble import BaggingRegressor
from sklearn.tree import DecisionTreeRegressor

14.20. Single estimator versus bagging: bias-variance decomposition
# Settings
n_repeat = 50  # Number of iterations for computing expectations
n_train = 50   # Size of the training set
n_test = 1000  # Size of the test set
noise = 0.1    # Standard deviation of the noise
np.random.seed(0)

# Change this for exploring the bias-variance decomposition of other
# estimators. This should work well for estimators with high variance (e.g.,
# decision trees or KNN), but poorly for estimators with low variance (e.g.,
# linear models).
estimators = [("Tree", DecisionTreeRegressor()),
              ("Bagging(Tree)", BaggingRegressor(DecisionTreeRegressor()))]
n_estimators = len(estimators)

# Generate data
def f(x):
    x = x.ravel()

    return np.exp(-x ** 2) + 1.5 * np.exp(-(x - 2) ** 2)

def generate(n_samples, noise, n_repeat=1):
    X = np.random.rand(n_samples) * 10 - 5
    X = np.sort(X)

    if n_repeat == 1:
        y = f(X) + np.random.normal(0.0, noise, n_samples)
    else:
        y = np.zeros((n_samples, n_repeat))

        for i in range(n_repeat):
            y[:, i] = f(X) + np.random.normal(0.0, noise, n_samples)

    X = X.reshape((n_samples, 1))

    return X, y

X_train = []
y_train = []

for i in range(n_repeat):
    X, y = generate(n_samples=n_train, noise=noise)
    X_train.append(X)
    y_train.append(y)

X_test, y_test = generate(n_samples=n_test, noise=noise, n_repeat=n_repeat)

plt.figure(figsize=(10, 8))

# Loop over estimators to compare
for n, (name, estimator) in enumerate(estimators):
    # Compute predictions
    y_predict = np.zeros((n_test, n_repeat))
for i in range(n_repeat):
    estimator.fit(X_train[i], y_train[i])
y_predict[:, i] = estimator.predict(X_test)

# Bias^2 + Variance + Noise decomposition of the mean squared error
y_error = np.zeros(n_test)
for i in range(n_repeat):
    for j in range(n_repeat):
        y_error += (y_test[:, j] - y_predict[:, i]) ** 2
y_error /= (n_repeat * n_repeat)
y_noise = np.var(y_test, axis=1)
y_bias = (f(X_test) - np.mean(y_predict, axis=1)) ** 2
y_var = np.var(y_predict, axis=1)

print("{}: \{1.4f\} (error) = \{2.4f\} (bias^2) "
      " + \{3.4f\} (var) + \{4.4f\} (noise)\).format(name,
      np.mean(y_error),
      np.mean(y_bias),
      np.mean(y_var),
      np.mean(y_noise)))

# Plot figures
plt.subplot(2, n_estimators, n + 1)
plt.plot(X_test, f(X_test), "b", label="f(x)")
plt.plot(X_train[0], y_train[0], ".b", label="LS ~ y = f(x)+noise")
for i in range(n_repeat):
    if i == 0:
        plt.plot(X_test, y_predict[:, i], "r", label="\^y(x)")
    else:
        plt.plot(X_test, y_predict[:, i], "r", alpha=0.05)
plt.plot(X_test, np.mean(y_predict, axis=1), "c",
         label="E_{LS} \^y(x)")
plt.xlim([-5, 5])
plt.title(name)
if n == n_estimators - 1:
    plt.legend(loc=(1.1, .5))
plt.subplot(2, n_estimators, n_estimators + n + 1)
plt.plot(X_test, y_error, "r", label="error(x)")
plt.plot(X_test, y_bias, "b", label="bias^2(x)")
plt.plot(X_test, y_var, "g", label="variance(x)")
plt.plot(X_test, y_noise, "c", label="noise(x)")
plt.xlim([-5, 5])
plt.ylim([0, 0.1])
if n == n_estimators - 1:
    plt.legend(loc=(1.1, .5))
plt.subplots_adjust(right=.75)
14.21 Plot the decision surfaces of ensembles of trees on the iris dataset

Plot the decision surfaces of forests of randomized trees trained on pairs of features of the iris dataset.

This plot compares the decision surfaces learned by a decision tree classifier (first column), by a random forest classifier (second column), by an extra-trees classifier (third column) and by an AdaBoost classifier (fourth column).

In the first row, the classifiers are built using the sepal width and the sepal length features only, on the second row using the petal length and sepal length only, and on the third row using the petal width and the petal length only.

In descending order of quality, when trained (outside of this example) on all 4 features using 30 estimators and scored using 10 fold cross validation, we see:

- `ExtraTreesClassifier()` # 0.95 score
- `RandomForestClassifier()` # 0.94 score
- `AdaBoost(DecisionTree(max_depth=3))` # 0.94 score
- `DecisionTree(max_depth=None)` # 0.94 score

Increasing `max_depth` for AdaBoost lowers the standard deviation of the scores (but the average score does not improve).

See the console’s output for further details about each model.

In this example you might try to:

1. vary the `max_depth` for the `DecisionTreeClassifier` and `AdaBoostClassifier`, perhaps try `max_depth=3` for the `DecisionTreeClassifier` or `max_depth=None` for `AdaBoostClassifier`

2. vary `n_estimators`

It is worth noting that RandomForests and ExtraTrees can be fitted in parallel on many cores as each tree is built independently of the others. AdaBoost’s samples are built sequentially and so do not use multiple cores.
DecisionTree with features [0, 1] has a score of 0.926666666667
RandomForest with 30 estimators with features [0, 1] has a score of 0.926666666667
ExtraTrees with 30 estimators with features [0, 1] has a score of 0.926666666667
AdaBoost with 30 estimators with features [0, 1] has a score of 0.84
DecisionTree with features [0, 2] has a score of 0.993333333333
RandomForest with 30 estimators with features [0, 2] has a score of 0.993333333333
ExtraTrees with 30 estimators with features [0, 2] has a score of 0.993333333333
AdaBoost with 30 estimators with features [0, 2] has a score of 0.993333333333
DecisionTree with features [2, 3] has a score of 0.993333333333
RandomForest with 30 estimators with features [2, 3] has a score of 0.993333333333
ExtraTrees with 30 estimators with features [2, 3] has a score of 0.993333333333
AdaBoost with 30 estimators with features [2, 3] has a score of 0.993333333333

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap

14.21. Plot the decision surfaces of ensembles of trees on the iris dataset
from sklearn.datasets import load_iris
from sklearn.ensemble import (RandomForestClassifier, ExtraTreesClassifier,
                               AdaBoostClassifier)
from sklearn.tree import DecisionTreeClassifier

# Parameters
n_classes = 3
n_estimators = 30
cmap = plt.cm.RdYlBu
plot_step = 0.02  # fine step width for decision surface contours
plot_step_coarser = 0.5  # step widths for coarse classifier guesses
RANDOM_SEED = 13  # fix the seed on each iteration

# Load data
iris = load_iris()

plot_idx = 1

models = [DecisionTreeClassifier(max_depth=None),
          RandomForestClassifier(n_estimators=n_estimators),
          ExtraTreesClassifier(n_estimators=n_estimators),
          AdaBoostClassifier(DecisionTreeClassifier(max_depth=3),
                              n_estimators=n_estimators)]

for pair in [[0, 1], [0, 2], [2, 3]]:
    for model in models:
        # We only take the two corresponding features
        X = iris.data[:, pair]
y = iris.target

        # Shuffle
        idx = np.arange(X.shape[0])
np.random.seed(RANDOM_SEED)
np.random.shuffle(idx)
        X = X[idx]
y = y[idx]

        # Standardize
        mean = X.mean(axis=0)
        std = X.std(axis=0)
        X = (X - mean) / std

        # Train
        model.fit(X, y)

        scores = model.score(X, y)
        # Create a title for each column and the console by using str() and
        # slicing away useless parts of the string
        model_title = str(type(model)).split('.')[-1][:-2][:-len("Classifier")]

        model_details = model_title
        if hasattr(model, "estimators_"):
            model_details += " with {} estimators".format(len(model.estimators_))
        print(model_details + " with features", pair,
              "has a score of", scores)
plt.subplot(3, 4, plot_idx)
if plot_idx <= len(models):
    # Add a title at the top of each column
    plt.title(model_title, fontsize=9)

    # Now plot the decision boundary using a fine mesh as input to a
    # filled contour plot
    x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
    y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
    xx, yy = np.meshgrid(np.arange(x_min, x_max, plot_step),
                         np.arange(y_min, y_max, plot_step))

    # Plot either a single DecisionTreeClassifier or alpha blend the
    # decision surfaces of the ensemble of classifiers
    if isinstance(model, DecisionTreeClassifier):
        Z = model.predict(np.c_[xx.ravel(), yy.ravel()])
        Z = Z.reshape(xx.shape)
        cs = plt.contourf(xx, yy, Z, cmap=cmap)
    else:
        # Choose alpha blend level with respect to the number
        # of estimators
        # that are in use (noting that AdaBoost can use fewer estimators
        # than its maximum if it achieves a good enough fit early on)
        estimator_alpha = 1.0 / len(model.estimators_)
        for tree in model.estimators_:
            Z = tree.predict(np.c_[xx.ravel(), yy.ravel()])
            Z = Z.reshape(xx.shape)
            cs = plt.contourf(xx, yy, Z, alpha=estimator_alpha, cmap=cmap)

    # Build a coarser grid to plot a set of ensemble classifications
    # to show how these are different to what we see in the decision
    # surfaces. These points are regularly spaced and do not have a
    # black outline
    xx_coarser, yy_coarser = np.meshgrid(
        np.arange(x_min, x_max, plot_step_coarser),
        np.arange(y_min, y_max, plot_step_coarser))
    Z_points_coarser = model.predict(np.c_[xx_coarser.ravel(),
                                             yy_coarser.ravel()]).reshape(xx_coarser.shape)
    cs_points = plt.scatter(xx_coarser, yy_coarser, s=15,
                             c=Z_points_coarser, cmap=cmap,
                             edgecolors="none")

    # Plot the training points, these are clustered together and have a
    # black outline
    plt.scatter(X[:, 0], X[:, 1], c=y,
                cmap=ListedColormap(['r', 'y', 'b']),
                edgecolor="k", s=20)

    plot_idx += 1  # move on to the next plot in sequence
plt.suptitle("Classifiers on feature subsets of the Iris dataset", fontsize=12)
plt.axis("tight")
plt.tight_layout(h_pad=0.2, w_pad=0.2, pad=2.5)
plt.show()

Total running time of the script: ( 0 minutes 8.437 seconds)

14.21. Plot the decision surfaces of ensembles of trees on the iris dataset
Exercises for the tutorials

15.1 Digits Classification Exercise

A tutorial exercise regarding the use of classification techniques on the Digits dataset.

This exercise is used in the Classification part of the Supervised learning: predicting an output variable from high-dimensional observations section of the A tutorial on statistical-learning for scientific data processing.

Out:

```
KNN score: 0.961111
LogisticRegression score: 0.938889
```

```python
print(__doc__)

from sklearn import datasets, neighbors, linear_model

digits = datasets.load_digits()
X_digits = digits.data
y_digits = digits.target

n_samples = len(X_digits)
X_train = X_digits[:int(.9 * n_samples)]
y_train = y_digits[:int(.9 * n_samples)]
X_test = X_digits[int(.9 * n_samples):]
y_test = y_digits[int(.9 * n_samples):]

knn = neighbors.KNeighborsClassifier()
logistic = linear_model.LogisticRegression()

print('KNN score: $f' % knn.fit(X_train, y_train).score(X_test, y_test))
print('LogisticRegression score: $f' % logistic.fit(X_train, y_train).score(X_test, y_test))
```

Total running time of the script: ( 0 minutes 0.398 seconds)
15.2 Cross-validation on Digits Dataset Exercise

A tutorial exercise using Cross-validation with an SVM on the Digits dataset.

This exercise is used in the Cross-validation generators part of the Model selection: choosing estimators and their parameters section of the A tutorial on statistical-learning for scientific data processing.

```python
print(__doc__)

import numpy as np
from sklearn.model_selection import cross_val_score
from sklearn import datasets, svm

digits = datasets.load_digits()
X = digits.data
y = digits.target

svc = svm.SVC(kernel='linear')
C_s = np.logspace(-10, 0, 10)
scores = list()
scores_std = list()
for C in C_s:
    svc.C = C
    this_scores = cross_val_score(svc, X, y, n_jobs=1)
    scores.append(np.mean(this_scores))
    scores_std.append(np.std(this_scores))

# Do the plotting
import matplotlib.pyplot as plt
plt.figure(1, figsize=(4, 3))
plt.clf()
plt.semilogx(C_s, scores)
plt.semilogx(C_s, np.array(scores) + np.array(scores_std), 'b--')
plt.semilogx(C_s, np.array(scores) - np.array(scores_std), 'b--')
locs, labels = plt.yticks()
plt.yticks(locs, list(map(lambda x: "%.2f" % x, locs)))
```
15.3 SVM Exercise

A tutorial exercise for using different SVM kernels.

This exercise is used in the Using kernels part of the Supervised learning: predicting an output variable from high-dimensional observations section of the A tutorial on statistical-learning for scientific data processing.
```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets, svm

iris = datasets.load_iris()
X = iris.data
y = iris.target

X = X[y != 0, :2]
y = y[y != 0]

n_sample = len(X)
np.random.seed(0)
order = np.random.permutation(n_sample)
X = X[order]
y = y[order].astype(np.float)

X_train = X[:int(.9 * n_sample)]
y_train = y[:int(.9 * n_sample)]
X_test = X[int(.9 * n_sample):]
y_test = y[int(.9 * n_sample):]

# fit the model
for fig_num, kernel in enumerate(('linear', 'rbf', 'poly')):
    clf = svm.SVC(kernel=kernel, gamma=10)
    clf.fit(X_train, y_train)

    plt.figure(fig_num)
    plt.clf()
    plt.scatter(X[:, 0], X[:, 1], c=y, zorder=10, cmap=plt.cm.Paired,
                edgecolor='k', s=20)
    plt.axis('tight')
x_min = X[:, 0].min()
x_max = X[:, 0].max()
```

---

Chapter 15. Tutorial exercises
y_min = X[:, 1].min()
y_max = X[:, 1].max()

XX, YY = np.mgrid[x_min:x_max:200j, y_min:y_max:200j]
Z = clf.decision_function(np.c_[XX.ravel(), YY.ravel()])

# Put the result into a color plot
Z = Z.reshape(XX.shape)
plt.pcolormesh(XX, YY, Z > 0, cmap=plt.cm.Paired)
plt.contour(XX, YY, Z, colors=['k', 'k', 'k'],
           linestyles=['--', '-', '--'], levels=[-.5, 0, .5])

plt.title(kernel)
plt.show()

Total running time of the script: ( 0 minutes 7.584 seconds)

15.4 Cross-validation on diabetes Dataset Exercise

A tutorial exercise which uses cross-validation with linear models.

This exercise is used in the Cross-validated estimators part of the Model selection: choosing estimators and their parameters section of the A tutorial on statistical-learning for scientific data processing.
Out:

Answer to the bonus question: how much can you trust the selection of alpha?

Alpha parameters maximising the generalization score on different subsets of the data:
[fold 0] alpha: 0.10405, score: 0.53573
[fold 1] alpha: 0.05968, score: 0.16278
[fold 2] alpha: 0.10405, score: 0.44437

Answer: Not very much since we obtained different alphas for different subsets of the data and moreover, the scores for these alphas differ quite substantially.

```python
from __future__ import print_function
import numpy as np
import matplotlib.pyplot as plt

from sklearn import datasets
from sklearn.linear_model import LassoCV
from sklearn.linear_model import Lasso
from sklearn.model_selection import KFold
from sklearn.model_selection import GridSearchCV

diabetes = datasets.load_diabetes()
X = diabetes.data[:150]
y = diabetes.target[:150]

lasso = Lasso(random_state=0)
alphas = np.logspace(-4, -0.5, 30)
tuned_parameters = [{'alpha': alphas}]
n_folds = 3

clf = GridSearchCV(lasso, tuned_parameters, cv=n_folds, refit=False)
clf.fit(X, y)
scores = clf.cv_results_['mean_test_score']
scores_std = clf.cv_results_['std_test_score']
plt.figure().set_size_inches(8, 6)
plt.semilogx(alphas, scores)
# plot error lines showing +/- std. errors of the scores
std_error = scores_std / np.sqrt(n_folds)
plt.semilogx(alphas, scores + std_error, 'b--')
plt.semilogx(alphas, scores - std_error, 'b--')
# alpha=0.2 controls the translucency of the fill color
plt.fill_between(alphas, scores + std_error, scores - std_error, alpha=0.2)
plt.ylabel('CV score +/- std error')```
plt.xlabel('alpha')
plt.axhline(np.max(scores), linestyle='--', color='.5')
plt.xlim([alphas[0], alphas[-1]])

# Bonus: how much can you trust the selection of alpha?
# To answer this question we use the LassoCV object that sets its alpha
# parameter automatically from the data by internal cross-validation (i.e. it
# performs cross-validation on the training data it receives).
# We use external cross-validation to see how much the automatically obtained
# alphas differ across different cross-validation folds.
lasso_cv = LassoCV(alphas=alphas, random_state=0)
k_fold = KFold(3)

print("Answer to the bonus question:",
      "how much can you trust the selection of alpha?"
)
print()
print("Alpha parameters maximising the generalization score on different")
print("subsets of the data:")
for k, (train, test) in enumerate(k_fold.split(X, y)):
    lasso_cv.fit(X[train], y[train])
    print("[fold {0}] alpha: {1:.5f}, score: {2:.5f}".format(k, lasso_cv.alpha_, lasso_cv.score(X[test], y[test])))
print()
print("Answer: Not very much since we obtained different alphas for different")
print("subsets of the data and moreover, the scores for these alphas differ")
print("quite substantially.")

plt.show()

Total running time of the script: ( 0 minutes 0.364 seconds)
Examples concerning the `sklearn.feature_selection` module.

### 16.1 Recursive feature elimination

A recursive feature elimination example showing the relevance of pixels in a digit classification task.

**Note:** See also *Recursive feature elimination with cross-validation*
print(__doc__)

from sklearn.svm import SVC
from sklearn.datasets import load_digits
from sklearn.feature_selection import RFE
import matplotlib.pyplot as plt

# Load the digits dataset
digits = load_digits()
X = digits.images.reshape((len(digits.images), -1))
y = digits.target

# Create the RFE object and rank each pixel
svc = SVC(kernel="linear", C=1)
rfe = RFE(estimator=svc, n_features_to_select=1, step=1)
rfe.fit(X, y)
ranking = rfe.ranking_.reshape(digits.images[0].shape)

# Plot pixel ranking
plt.matshow(ranking, cmap=plt.cm.Blues)
plt.colorbar()
plt.title("Ranking of pixels with RFE")
plt.show()

Total running time of the script: (0 minutes 5.329 seconds)

16.2 Comparison of F-test and mutual information

This example illustrates the differences between univariate F-test statistics and mutual information.

We consider 3 features \( x_1, x_2, x_3 \) distributed uniformly over \([0, 1]\), the target depends on them as follows:
\[ y = x_1 + \sin(6 \times \pi \times x_2) + 0.1 \times N(0, 1), \] that is the third features is completely irrelevant.

The code below plots the dependency of \( y \) against individual \( x_i \) and normalized values of univariate F-tests statistics and mutual information.

As F-test captures only linear dependency, it rates \( x_1 \) as the most discriminative feature. On the other hand, mutual information can capture any kind of dependency between variables and it rates \( x_2 \) as the most discriminative feature, which probably agrees better with our intuitive perception for this example. Both methods correctly marks \( x_3 \) as irrelevant.
scikit-learn user guide, Release 0.20.dev0

print(__doc__)
import numpy as np
import matplotlib.pyplot as plt
from sklearn.feature_selection import f_regression, mutual_info_regression
np.random.seed(0)
X = np.random.rand(1000, 3)
y = X[:, 0] + np.sin(6 * np.pi * X[:, 1]) + 0.1 * np.random.randn(1000)
f_test, _ = f_regression(X, y)
f_test /= np.max(f_test)
mi = mutual_info_regression(X, y)
mi /= np.max(mi)
plt.figure(figsize=(15, 5))
for i in range(3):
plt.subplot(1, 3, i + 1)
plt.scatter(X[:, i], y, edgecolor='black', s=20)
plt.xlabel("$x_{}$".format(i + 1), fontsize=14)
if i == 0:
plt.ylabel("$y$", fontsize=14)
plt.title("F-test={:.2f}, MI={:.2f}".format(f_test[i], mi[i]),
fontsize=16)
plt.show()

Total running time of the script: ( 0 minutes 0.238 seconds)

16.3 Pipeline Anova SVM
Simple usage of Pipeline that runs successively a univariate feature selection with anova and then a C-SVM of the
selected features.
Out:
precision

recall

f1-score

support

0
1
2
3

0.75
0.60
0.67
1.00

0.50
1.00
0.80
0.62

0.60
0.75
0.73
0.77

6
6
5
8

avg / total

0.78

0.72

0.72

25

from
from
from
from
from
from

sklearn import svm
sklearn.datasets import samples_generator
sklearn.feature_selection import SelectKBest, f_regression
sklearn.pipeline import make_pipeline
sklearn.model_selection import train_test_split
sklearn.metrics import classification_report

16.3. Pipeline Anova SVM

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print(__doc__)

# import some data to play with
X, y = samples_generator.make_classification(
    n_features=20, n_informative=3, n_redundant=0, n_classes=4,
    n_clusters_per_class=2)

X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=42)

# ANOVA SVM-C
# 1) anova filter, take 3 best ranked features
anova_filter = SelectKBest(f_regression, k=3)
# 2) svm
clf = svm.SVC(kernel='linear')

anova_svm = make_pipeline(anova_filter, clf)
anova_svm.fit(X_train, y_train)
y_pred = anova_svm.predict(X_test)
print(classification_report(y_test, y_pred))

Total running time of the script: ( 0 minutes 0.004 seconds)

16.4 Recursive feature elimination with cross-validation

A recursive feature elimination example with automatic tuning of the number of features selected with cross-validation.
Optimal number of features : 3

```python
print(__doc__)

import matplotlib.pyplot as plt
from sklearn.svm import SVC
from sklearn.model_selection import StratifiedKFold
from sklearn.feature_selection import RFECV
from sklearn.datasets import make_classification

# Build a classification task using 3 informative features
X, y = make_classification(n_samples=1000, n_features=25, n_informative=3,
                            n_redundant=2, n_repeated=0, n_classes=8,
                            n_clusters_per_class=1, random_state=0)

# Create the RFE object and compute a cross-validated score.
svc = SVC(kernel="linear")
# The "accuracy" scoring is proportional to the number of correct
# classifications
```
rfecv = RFECV(estimator=svc, step=1, cv=StratifiedKFold(2), scoring='accuracy')
rfecv.fit(X, y)

print("Optimal number of features : %d" % rfecv.n_features_)

# Plot number of features VS. cross-validation scores
plt.figure()
plt.xlabel("Number of features selected")
plt.ylabel("Cross validation score (nb of correct classifications)")
plt.plot(range(1, len(rfecv.grid_scores_) + 1), rfecv.grid_scores_)
plt.show()

Total running time of the script: ( 0 minutes 2.360 seconds)

16.5 Feature selection using SelectFromModel and LassoCV

Use SelectFromModel meta-transformer along with Lasso to select the best couple of features from the Boston dataset.

Features selected from Boston using SelectFromModel with threshold 0.750

# Author: Manoj Kumar <mks542@nyu.edu>
# License: BSD 3 clause

print(__doc__)
import matplotlib.pyplot as plt
import numpy as np

from sklearn.datasets import load_boston
from sklearn.feature_selection import SelectFromModel
from sklearn.linear_model import LassoCV

# Load the boston dataset.
boston = load_boston()
X, y = boston['data'], boston['target']

# We use the base estimator LassoCV since the L1 norm promotes sparsity of features.
clf = LassoCV()

# Set a minimum threshold of 0.25
sfm = SelectFromModel(clf, threshold=0.25)
sfm.fit(X, y)
n_features = sfm.transform(X).shape[1]

# Reset the threshold till the number of features equals two.
# Note that the attribute can be set directly instead of repeatedly
# fitting the metatransformer.
while n_features > 2:
    sfm.threshold += 0.1
    X_transform = sfm.transform(X)
    n_features = X_transform.shape[1]

# Plot the selected two features from X.
plt.title("Features selected from Boston using SelectFromModel with "
    "threshold %0.3f." % sfm.threshold)
feature1 = X_transform[:, 0]
feature2 = X_transform[:, 1]
plt.plot(feature1, feature2, 'r.'
plt.xlabel("Feature number 1")
plt.ylabel("Feature number 2")
plt.ylim([np.min(feature2), np.max(feature2)])
plt.show()

Total running time of the script: ( 0 minutes 0.123 seconds)

16.6 Test with permutations the significance of a classification score

In order to test if a classification score is significative a technique in repeating the classification procedure after randomizing, permuting, the labels. The p-value is then given by the percentage of runs for which the score obtained is greater than the classification score obtained in the first place.
```
# Author: Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from sklearn.svm import SVC
from sklearn.model_selection import StratifiedKFold
from sklearn.model_selection import permutation_test_score
from sklearn import datasets

# #############################################################################
# Loading a dataset
iris = datasets.load_iris()```
\texttt{X = iris.data} \\
\texttt{y = iris.target} \\
\texttt{n\_classes = np.unique(y).size} \\

\texttt{# Some noisy data not correlated} \\
\texttt{random = np.random.RandomState(seed=0)} \\
\texttt{E = random.normal(size=(len(X), 2200))} \\

\texttt{# Add noisy data to the informative features for make the task harder} \\
\texttt{X = np.c_[X, E]} \\

\texttt{svm = SVC(kernel='linear')} \\
\texttt{cv = StratifiedKFold(2)} \\

\texttt{score, permutation\_scores, pvalue = permutation\_test\_score(} \\
\texttt{    svm, X, y, scoring="accuracy", cv=cv, n\_permutations=100, n\_jobs=1)} \\

\texttt{print("Classification score %s (pvalue : %s)" % (score, pvalue))} \\

\texttt{# View histogram of permutation scores} \\
\texttt{plt.hist(permutation\_scores, 20, label='Permutation scores',} \\
\texttt{    edgecolor='black')} \\
\texttt{ylim = plt.ylim()} \\
\texttt{# BUG: vlines(..., linestyle='--') fails on older versions of matplotlib} \\
\texttt{# plt.vlines(score, ylim[0], ylim[1], linestyle='--',} \\
\texttt{#    color='g', linewidth=3, label='Classification Score'} \\
\texttt{#    ' (pvalue %s)' % pvalue)} \\
\texttt{# plt.vlines(1.0 / n\_classes, ylim[0], ylim[1], linestyle='--',} \\
\texttt{#    color='k', linewidth=3, label='Luck')} \\
\texttt{plt.plot(2 * [score], ylim, '--g', linewidth=3, label='Classification Score'} \\
\texttt{    ' (pvalue %s) % pvalue)} \\
\texttt{plt.plot(2 * [1. / n\_classes], ylim, '--k', linewidth=3, label='Luck')} \\

\texttt{plt.xlabel('Score')} \\
\texttt{plt.show()} \\

\textbf{Total running time of the script:} ( 0 minutes 6.939 seconds) \\

\section*{16.7 Univariate Feature Selection}

An example showing univariate feature selection.

Noisy (non informative) features are added to the iris data and univariate feature selection is applied. For each feature, we plot the p-values for the univariate feature selection and the corresponding weights of an SVM. We can see that univariate feature selection selects the informative features and that these have larger SVM weights.

In the total set of features, only the 4 first ones are significant. We can see that they have the highest score with univariate feature selection. The SVM assigns a large weight to one of these features, but also Selects many of the non-informative features. Applying univariate feature selection before the SVM increases the SVM weight attributed to the significant features, and will thus improve classification.
```
import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets, svm
from sklearn.feature_selection import SelectPercentile, f_classif

# Import some data to play with
# The iris dataset
iris = datasets.load_iris()

# Some noisy data not correlated
E = np.random.uniform(0, 0.1, size=(len(iris.data), 20))

# Add the noisy data to the informative features
X = np.hstack((iris.data, E))
y = iris.target

plt.figure(1)
plt.clf()
X_indices = np.arange(X.shape[-1])

print(__doc__)
```

Comparing feature selection

![Graph comparing feature selection methods](image)

- **Univariate score** ($-\log(p_{value})$)
- **SVM weight**
- **SVM weights after selection**

### Code

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets, svm
from sklearn.feature_selection import SelectPercentile, f_classif

# # Import some data to play with
# # The iris dataset
# iris = datasets.load_iris()

# Some noisy data not correlated
E = np.random.uniform(0, 0.1, size=(len(iris.data), 20))

# Add the noisy data to the informative features
X = np.hstack((iris.data, E))
y = iris.target

plt.figure(1)
plt.clf()
X_indices = np.arange(X.shape[-1])
```

---

Chapter 16. Feature Selection
Univariate feature selection with F-test for feature scoring

We use the default selection function: the 10% most significant features

```
selector = SelectPercentile(f_classif, percentile=10)
selector.fit(X, y)
scores = -np.log10(selector.pvalues_)
scores /= scores.max()
plt.bar(X_indices - .45, scores, width=.2,
       label=r'Univariate score ($-\log(p_{value})$)', color='darkorange',
       edgecolor='black')
```

Compare to the weights of an SVM

```
clf = svm.SVC(kernel='linear')
clf.fit(X, y)

svm_weights = (clf.coef_ ** 2).sum(axis=0)
svm_weights /= svm_weights.max()
plt.bar(X_indices - .25, svm_weights, width=.2, label='SVM weight',
       color='navy', edgecolor='black')

clf_selected = svm.SVC(kernel='linear')
clf_selected.fit(selector.transform(X), y)

svm_weights_selected = (clf_selected.coef_ ** 2).sum(axis=0)
svm_weights_selected /= svm_weights_selected.max()
plt.bar(X_indices[selector.get_support()] - .05, svm_weights_selected,
       width=.2, label='SVM weights after selection', color='c',
       edgecolor='black')
```

Total running time of the script: ( 0 minutes 0.092 seconds)
Examples concerning the `sklearn.gaussian_process` module.

### 17.1 Illustration of Gaussian process classification (GPC) on the XOR dataset

This example illustrates GPC on XOR data. Compared are a stationary, isotropic kernel (RBF) and a non-stationary kernel (DotProduct). On this particular dataset, the DotProduct kernel obtains considerably better results because the class-boundaries are linear and coincide with the coordinate axes. In general, stationary kernels often obtain better results.

```python
print(__doc__)

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
#
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
```

![Image of XOR dataset with GPC results](image.png)
```python
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF, DotProduct

xx, yy = np.meshgrid(np.linspace(-3, 3, 50),
                     np.linspace(-3, 3, 50))
rng = np.random.RandomState(0)
X = rng.randn(200, 2)
Y = np.logical_xor(X[:, 0] > 0, X[:, 1] > 0)

# fit the model
plt.figure(figsize=(10, 5))
kernels = [1.0 * RBF(length_scale=1.0), 1.0 * DotProduct(sigma_0=1.0)**2]
for i, kernel in enumerate(kernels):
    clf = GaussianProcessClassifier(kernel=kernel, warm_start=True).fit(X, Y)
    # plot the decision function for each datapoint on the grid
    Z = clf.predict_proba(np.vstack((xx.ravel(), yy.ravel())).T)[:, 1]
    Z = Z.reshape(xx.shape)
    plt.subplot(1, 2, i + 1)
    image = plt.imshow(Z, interpolation='nearest',
                       extent=(xx.min(), xx.max(), yy.min(), yy.max()),
                       aspect='auto', origin='lower', cmap=plt.cm.PuOr_r)
    contours = plt.contour(xx, yy, Z, levels=[0], linewidths=2,
                            linetypes='--')
    plt.scatter(X[:, 0], X[:, 1], s=30, c=Y, cmap=plt.cm.Paired,
                edgecolors=(0, 0, 0))
    plt.xticks(())
    plt.yticks(())
    plt.axis([-3, 3, -3, 3])
    plt.colorbar(image)
    plt.title("%s
Log-Marginal-Likelihood: %3f"
            % (clf.kernel_, clf.log_marginal_likelihood(clf.kernel_.theta)),
            fontsize=12)
plt.tight_layout()
plt.show()

Total running time of the script: ( 0 minutes 4.655 seconds)

17.2 Gaussian process classification (GPC) on iris dataset

This example illustrates the predicted probability of GPC for an isotropic and anisotropic RBF kernel on a two-dimensional version for the iris-dataset. The anisotropic RBF kernel obtains slightly higher log-marginal-likelihood by assigning different length-scales to the two feature dimensions.

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```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF

# import some data to play with
iris = datasets.load_iris()
X = iris.data[:, :2]  # we only take the first two features.
y = np.array(iris.target, dtype=int)

h = .02  # step size in the mesh

kernel = 1.0 * RBF([1.0])
gpc_rbf_isotropic = GaussianProcessClassifier(kernel=kernel).fit(X, y)
kernel = 1.0 * RBF([1.0, 1.0])
gpc_rbf_anisotropic = GaussianProcessClassifier(kernel=kernel).fit(X, y)

# create a mesh to plot in
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))

titles = ["Isotropic RBF", "Anisotropic RBF"]
plt.figure(figsize=(10, 5))
for i, clf in enumerate((gpc_rbf_isotropic, gpc_rbf_anisotropic)):
    # Plot the predicted probabilities. For that, we will assign a color to
    # each point in the mesh \([x_{\text{min}}, x_{\text{max}}] \times [y_{\text{min}}, y_{\text{max}}]\).
    plt.subplot(1, 2, i + 1)
    Z = clf.predict_proba(np.c_[xx.ravel(), yy.ravel()])

    # Put the result into a color plot
```

17.2. Gaussian process classification (GPC) on iris dataset
Both kernel ridge regression (KRR) and Gaussian process regression (GPR) learn a target function by employing internally the “kernel trick”. KRR learns a linear function in the space induced by the respective kernel which corresponds to a non-linear function in the original space. The linear function in the kernel space is chosen based on the mean-squared error loss with ridge regularization. GPR uses the kernel to define the covariance of a prior distribution over the target functions and uses the observed training data to define a likelihood function. Based on Bayes theorem, a (Gaussian) posterior distribution over target functions is defined, whose mean is used for prediction.

A major difference is that GPR can choose the kernel's hyperparameters based on gradient-ascent on the marginal likelihood function while KRR needs to perform a grid search on a cross-validated loss function (mean-squared error loss). A further difference is that GPR learns a generative, probabilistic model of the target function and can thus provide meaningful confidence intervals and posterior samples along with the predictions while KRR only provides predictions.

This example illustrates both methods on an artificial dataset, which consists of a sinusoidal target function and strong noise. The figure compares the learned model of KRR and GPR based on an ExpSineSquared kernel, which is suited for learning periodic functions. The kernel's hyperparameters control the smoothness (\(l\)) and periodicity of the kernel (\(p\)). Moreover, the noise level of the data is learned explicitly by GPR by an additional WhiteKernel component in the kernel and by the regularization parameter alpha of KRR.

The figure shows that both methods learn reasonable models of the target function. GPR correctly identifies the periodicity of the function to be roughly \(2\pi\) (6.28), while KRR chooses the doubled periodicity \(4\pi\). Besides that, GPR provides reasonable confidence bounds on the prediction which are not available for KRR. A major difference between the two methods is the time required for fitting and predicting: while fitting KRR is fast in principle, the grid-search for hyperparameter optimization scales exponentially with the number of hyperparameters (“curse of dimensionality”). The gradient-based optimization of the parameters in GPR does not suffer from this exponential scaling and is thus considerably faster on this example with 3-dimensional hyperparameter space. The time for predicting is similar; however, generating the variance of the predictive distribution of GPR takes considerably longer than just predicting the mean.
Out:

Time for KRR fitting: 8.359
Time for GPR fitting: 0.160
Time for KRR prediction: 0.087
Time for GPR prediction: 0.097
Time for GPR prediction with standard-deviation: 0.111

print(__doc__)

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD 3 clause

import time
import numpy as np
import matplotlib.pyplot as plt
from sklearn.kernel_ridge import KernelRidge
from sklearn.model_selection import GridSearchCV
from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import WhiteKernel, ExpSineSquared
rng = np.random.RandomState(0)

# Generate sample data
X = 15 * rng.rand(100, 1)
y = np.sin(X).ravel()
y += 3 * (0.5 - rng.rand(X.shape[0]))  # add noise

17.3. Comparison of kernel ridge and Gaussian process regression
# Fit KernelRidge with parameter selection based on 5-fold cross validation
param_grid = {
    "alpha": [1e0, 1e-1, 1e-2, 1e-3],
    "kernel": [ExpSineSquared(l, p)
               for l in np.logspace(-2, 2, 10)
               for p in np.logspace(0, 2, 10)]
}
kr = GridSearchCV(KernelRidge(), cv=5, param_grid=param_grid)
stime = time.time()
krr = kr.fit(X, y)

print("Time for KRR fitting: %.3f" % (time.time() - stime))

gp_kernel = ExpSineSquared(1.0, 5.0, periodicity_bounds=(1e-2, 1e1)) + WhiteKernel(1e-1)
gpr = GaussianProcessRegressor(kernel=gp_kernel)
stime = time.time()
gpr = gpr.fit(X, y)

print("Time for GPR fitting: %.3f" % (time.time() - stime))

data = np.linspace(0, 20, 10000)[None, None]

time = time.time()
y_kr = kr.predict(data)
print("Time for KRR prediction: %.3f" % (time.time() - stime))

y_gpr = gpr.predict(data, return_std=False)
print("Time for GPR prediction: %.3f" % (time.time() - stime))

y_gpr, y_std = gpr.predict(data, return_std=True)
print("Time for GPR prediction with standard-deviation: %.3f" % (time.time() - stime))

plt.figure(figsize=(10, 5))
lw = 2
plt.scatter(X, y, c='k', label='data')
plt.plot(data, np.sin(data), color='navy', lw=lw, label='True')
plt.plot(data, y_kr, color='turquoise', lw=lw, label='KRR (%s)' % kr.best_params_)
plt.plot(data, y_gpr, color='darkorange', lw=lw, label='GPR (%s)' % gpr.kernel_)
plt.fill_between(data[:, 0], y_gpr - y_std, y_gpr + y_std, color='darkorange', alpha=0.2)
plt.xlabel('data')
plt.ylabel('target')
plt.xlim(0, 20)
plt.ylim(-4, 4)
plt.title('GPR versus Kernel Ridge')
plt.legend(loc="best", scatterpoints=1, prop={"size": 8})
plt.show()
17.4 Gaussian process regression (GPR) on Mauna Loa CO2 data.

This example is based on Section 5.4.3 of “Gaussian Processes for Machine Learning” [RW2006]. It illustrates an example of complex kernel engineering and hyperparameter optimization using gradient ascent on the log-marginal-likelihood. The data consists of the monthly average atmospheric CO2 concentrations (in parts per million by volume (ppmv)) collected at the Mauna Loa Observatory in Hawaii, between 1958 and 1997. The objective is to model the CO2 concentration as a function of the time t.

The kernel is composed of several terms that are responsible for explaining different properties of the signal:

- a long term, smooth rising trend is to be explained by an RBF kernel. The RBF kernel with a large length-scale enforces this component to be smooth; it is not enforced that the trend is rising which leaves this choice to the GP. The specific length-scale and the amplitude are free hyperparameters.

- a seasonal component, which is to be explained by the periodic ExpSineSquared kernel with a fixed periodicity of 1 year. The length-scale of this periodic component, controlling its smoothness, is a free parameter. In order to allow decaying away from exact periodicity, the product with an RBF kernel is taken. The length-scale of this RBF component controls the decay time and is a further free parameter.

- smaller, medium term irregularities are to be explained by a RationalQuadratic kernel component, whose length-scale and alpha parameter, which determines the diffuseness of the length-scales, are to be determined. According to [RW2006], these irregularities can better be explained by a RationalQuadratic than an RBF kernel component, probably because it can accommodate several length-scales.

- a “noise” term, consisting of an RBF kernel contribution, which shall explain the correlated noise components such as local weather phenomena, and a WhiteKernel contribution for the white noise. The relative amplitudes and the RBF’s length scale are further free parameters.

Maximizing the log-marginal-likelihood after subtracting the target’s mean yields the following kernel with an LML of -83.214:

\[
34.4^{*}2 \times \text{RBF}(\text{length\_scale}=41.8) \\
+ 3.27^{*}2 \times \text{RBF}(\text{length\_scale}=180) \times \text{ExpSineSquared}(\text{length\_scale}=1.44, \\
\quad \text{periodicity}=1) \\
+ 0.446^{*}2 \times \text{RationalQuadratic}(\text{alpha}=17.7, \text{length\_scale}=0.957) \\
+ 0.197^{*}2 \times \text{RBF}(\text{length\_scale}=0.138) + \text{WhiteKernel}(\text{noise\_level}=0.0336)
\]

Thus, most of the target signal (34.4ppm) is explained by a long-term rising trend (length-scale 41.8 years). The periodic component has an amplitude of 3.27ppm, a decay time of 180 years and a length-scale of 1.44. The long decay time indicates that we have a locally very close to periodic seasonal component. The correlated noise has an amplitude of 0.197ppm with a length scale of 0.138 years and a white-noise contribution of 0.197ppm. Thus, the overall noise level is very small, indicating that the data can be very well explained by the model. The figure shows also that the model makes very confident predictions until around 2015.
GPML kernel: $66^2 \times \text{RBF}(\text{length\_scale}=67) + 2.4^2 \times \text{RBF}(\text{length\_scale}=90) \times$
\text{ExpSineSquared}(\text{length\_scale}=1.3, \text{periodicity}=1) + $0.66^2 \times$
\text{RationalQuadratic}(\text{alpha}=0.78, \text{length\_scale}=1.2) + $0.18^2 \times \text{RBF}(\text{length\_scale}=0.134) \times$
\text{WhiteKernel}(\text{noise\_level}=0.0361)$

Log-marginal-likelihood: $-87.034$

Learned kernel: $34.5^2 \times \text{RBF}(\text{length\_scale}=41.8) + 3.27^2 \times \text{RBF}(\text{length\_scale}=180) \times$
\text{ExpSineSquared}(\text{length\_scale}=1.44, \text{periodicity}=1) + $0.446^2 \times$
\text{RationalQuadratic}(\text{alpha}=17.6, \text{length\_scale}=0.957) + $0.197^2 \times \text{RBF}(\text{length\_scale}=0.138) + \text{WhiteKernel}(\text{noise\_level}=0.0336)$

Log-marginal-likelihood: $-83.214$

print(__doc__)

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
#
# License: BSD 3 clause

import numpy as np
from matplotlib import pyplot as plt

from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF, WhiteKernel, RationalQuadratic, ExpSineSquared
from sklearn.datasets import fetch_mldata

data = fetch_mldata('mauna-loa-atmospheric-co2').data
X = data[:, [1]]
y = data[:, 0]

# Kernel with parameters given in GPML book
k1 = 66.0**2 * RBF(length_scale=67.0)  # long term smooth rising trend
k2 = 2.4**2 * RBF(length_scale=90.0)  
    * ExpSineSquared(length_scale=1.3, periodicity=1.0)  # seasonal component
# medium term irregularity
k3 = 0.66**2  
    * RationalQuadratic(length_scale=1.2, alpha=0.78)
k4 = 0.18**2 * RBF(length_scale=0.134)  
    + WhiteKernel(noise_level=0.19**2)  # noise terms
kernel_gpml = k1 + k2 + k3 + k4

gp = GaussianProcessRegressor(kernel=kernel_gpml, alpha=0,  
                             optimizer=None, normalize_y=True)
gp.fit(X, y)

print(\"GPML kernel: %s\" % gp.kernel_)
print(\"Log-marginal-likelihood: %.3f\"  
                             % gp.log_marginal_likelihood(gp.kernel_.theta))

# Kernel with optimized parameters
k1 = 50.0**2 * RBF(length_scale=50.0)  # long term smooth rising trend
k2 = 2.0**2 * RBF(length_scale=100.0)  
    * ExpSineSquared(length_scale=1.0, periodicity=1.0,  
        periodicity_bounds="fixed")  # seasonal component
# medium term irregularities
k3 = 0.5**2 * RationalQuadratic(length_scale=1.0, alpha=1.0)
k4 = 0.1**2 * RBF(length_scale=0.1)  
    + WhiteKernel(noise_level=0.1**2,  
        noise_level_bounds=(1e-3, np.inf))  # noise terms
kernel = k1 + k2 + k3 + k4

gp = GaussianProcessRegressor(kernel=kernel, alpha=0,  
                             normalize_y=True)
gp.fit(X, y)

print(\n\"Learned kernel: %s\" % gp.kernel_)
print(\"Log-marginal-likelihood: %.3f\"  
                             % gp.log_marginal_likelihood(gp.kernel_.theta))

X_ = np.linspace(X.min(), X.max() + 30, 1000)[:, np.newaxis]
y_pred, y_std = gp.predict(X_, return_std=True)

# Illustration
plt.scatter(X, y, c='k')
plt.plot(X_, y_pred)
plt.fill_between(X_[:, 0], y_pred - y_std, y_pred + y_std,

17.4. Gaussian process regression (GPR) on Mauna Loa CO2 data.
17.5 Illustration of prior and posterior Gaussian process for different kernels

This example illustrates the prior and posterior of a GPR with different kernels. Mean, standard deviation, and 10 samples are shown for both prior and posterior.
17.5. Illustration of prior and posterior Gaussian process for different kernels

- Prior (kernel: $1**2 \times \text{RationalQuadratic}(\alpha=0.1, \text{length\_scale}=1)$)
- Posterior (kernel: $0.594**2 \times \text{RationalQuadratic}(\alpha=1e+05, \text{length\_scale}=0.279)$)  
  Log-Likelihood: 0.067
- Prior (kernel: $1**2 \times \text{ExpSineSquared}(\text{length\_scale}=1, \text{periodicity}=3)$)
- Posterior (kernel: $0.790**2 \times \text{ExpSineSquared}(\text{length\_scale}=0.701, \text{periodicity}=2.871)$)  
  Log-Likelihood: 3.394
print(__doc__)
from matplotlib import pyplot as plt

from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import (RBF, Matern, RationalQuadratic, ExpSineSquared, DotProduct, ConstantKernel)

kernels = 
    [1.0 * RBF(length_scale=1.0, length_scale_bounds=(1e-1, 10.0)),
     1.0 * RationalQuadratic(length_scale=1.0, alpha=0.1),
     1.0 * ExpSineSquared(length_scale=1.0, periodicity=3.0,
                          length_scale_bounds=(0.1, 10.0),
                          periodicity_bounds=(1.0, 10.0)),
     ConstantKernel(0.1, (0.01, 10.0))
     * (DotProduct(sigma_0=1.0, sigma_0_bounds=(0.0, 10.0)) ** 2),
     1.0 * Matern(length_scale=1.0, length_scale_bounds=(1e-1, 10.0),
                   nu=1.5)]

for fig_index, kernel in enumerate(kernels):
    # Specify Gaussian Process
    gp = GaussianProcessRegressor(kernel=kernel)

    # Plot prior
    plt.figure(fig_index, figsize=(8, 8))
    plt.subplot(2, 1, 1)
    X_ = np.linspace(0, 5, 100)
    y_mean, y_std = gp.predict(X_[:, np.newaxis], return_std=True)
    plt.plot(X_, y_mean, 'k', lw=3, zorder=9)
    plt.fill_between(X_, y_mean - y_std, y_mean + y_std,
                     alpha=0.2, color='k')
    y_samples = gp.sample_y(X_[:, np.newaxis], 10)
    plt.plot(X_, y_samples, lw=1)
    plt.xlim(0, 5)
    plt.ylim(-3, 3)
    plt.title("Prior (kernel: \$%s\$)" % kernel, fontsize=12)

    # Generate data and fit GP
    rng = np.random.RandomState(4)
    X = rng.uniform(0, 5, 10)[:, np.newaxis]
    y = np.sin((X[:, 0] - 2.5) ** 2)
    gp.fit(X, y)

    # Plot posterior
    plt.subplot(2, 1, 2)
    X_ = np.linspace(0, 5, 100)
    y_mean, y_std = gp.predict(X_[:, np.newaxis], return_std=True)
    plt.plot(X_, y_mean, 'k', lw=3, zorder=9)
    plt.fill_between(X_, y_mean - y_std, y_mean + y_std,
                     alpha=0.2, color='k')
    y_samples = gp.sample_y(X_[:, np.newaxis], 10)
    plt.plot(X_, y_samples, lw=1)
    plt.scatter(X[:, 0], y, c='r', s=50, zorder=10, edgecolors=(0, 0, 0))
    plt.xlim(0, 5)
    plt.ylim(-3, 3)
    plt.title("Posterior (kernel: \$%s\$)\nLog-Likelihood: \$%.3f\$" % (gp.kernel_, gp.log_marginal_likelihood(gp.kernel_.theta)),
              fontsize=12)

17.5. Illustration of prior and posterior Gaussian process for different kernels 937
plt.tight_layout()
plt.show()

Total running time of the script: ( 0 minutes 1.479 seconds)

17.6 Iso-probability lines for Gaussian Processes classification (GPC)

A two-dimensional classification example showing iso-probability lines for the predicted probabilities.

Out:
Learned kernel: 0.0256**2 * DotProduct(sigma_0=5.72) ** 2

print(__doc__)

# Author: Vincent Dubourg <vincent.dubourg@gmail.com>
import numpy as np
from matplotlib import pyplot as plt
from matplotlib import cm
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import DotProduct, ConstantKernel as C

# A few constants
lim = 8

def g(x):
    """The function to predict (classification will then consist in predicting whether g(x) <= 0 or not)""
    return 5. - x[:,1] - .5 * x[:,0]**2.

# Design of experiments
X = np.array([[-4.61611719, -6.00099547],
              [4.10469096, 5.32782448],
              [0.00000000, -0.50000000],
              [-6.17289014, -4.69847430],
              [1.31093060, -6.93271427],
              [-5.03823144, 3.10584743],
              [-2.87600388, 6.74310541],
              [5.21301203, 4.26386883]])

# Observations
y = np.array(g(X) > 0, dtype=int)

# Instantiate and fit Gaussian Process Model
kernel = C(0.1, (1e-5, np.inf)) * DotProduct(sigma_0=0.1)**2
gp = GaussianProcessClassifier(kernel=kernel)
gp.fit(X, y)
print("Learned kernel: " % gp.kernel_)

# Evaluate real function and the predicted probability
res = 50
x1, x2 = np.meshgrid(np.linspace(- lim, lim, res),
                     np.linspace(- lim, lim, res))
xx = np.vstack([x1.reshape(x1.size), x2.reshape(x2.size)]).T

y_true = g(xx)
y_prob = gp.predict_proba(xx)[:,1]
y_true = y_true.reshape((res, res))
y_prob = y_prob.reshape((res, res))

# Plot the probabilistic classification iso-values
fig = plt.figure(1)
ax = fig.gca()
ax.axes.set_aspect('equal')
plt.xticks([])
plt.yticks([])
ax.set_xticklabels([])

17.6. Iso-probability lines for Gaussian Processes classification (GPC)
17.7 Probabilistic predictions with Gaussian process classification (GPC)

This example illustrates the predicted probability of GPC for an RBF kernel with different choices of the hyperparameters. The first figure shows the predicted probability of GPC with arbitrarily chosen hyperparameters and with the hyperparameters corresponding to the maximum log-marginal-likelihood (LML).

While the hyperparameters chosen by optimizing LML have a considerably larger LML, they perform slightly worse according to the log-loss on test data. The figure shows that this is because they exhibit a steep change of the class probabilities at the class boundaries (which is good) but have predicted probabilities close to 0.5 far away from the class boundaries (which is bad). This undesirable effect is caused by the Laplace approximation used internally by GPC.

The second figure shows the log-marginal-likelihood for different choices of the kernel’s hyperparameters, highlighting the two choices of the hyperparameters used in the first figure by black dots.
Out:

Log Marginal Likelihood (initial): -17.598
Log Marginal Likelihood (optimized): -3.875
Accuracy: 1.000 (initial) 1.000 (optimized)
Log-loss: 0.214 (initial) 0.319 (optimized)

```
print(__doc__)

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD 3 clause

import numpy as np

from matplotlib import pyplot as plt

from sklearn.metrics.classification import accuracy_score, log_loss
from sklearn.gaussian_process import GaussianProcessClassifier
from sklearn.gaussian_process.kernels import RBF
```

17.7. Probabilistic predictions with Gaussian process classification (GPC)
# Generate data
train_size = 50
rng = np.random.RandomState(0)
X = rng.uniform(0, 5, 100)[:, np.newaxis]
y = np.array(X[:, 0] > 2.5, dtype=int)

# Specify Gaussian Processes with fixed and optimized hyperparameters
gp_fix = GaussianProcessClassifier(kernel=1.0 * RBF(length_scale=1.0), optimizer=None)
gp_fix.fit(X[:train_size], y[:train_size])
gp_opt = GaussianProcessClassifier(kernel=1.0 * RBF(length_scale=1.0))
gp_opt.fit(X[:train_size], y[:train_size])

print("Log Marginal Likelihood (initial): \$.3f"
      % gp_fix.log_marginal_likelihood(gp_fix.kernel_.theta))
print("Log Marginal Likelihood (optimized): \$.3f"
      % gp_opt.log_marginal_likelihood(gp_opt.kernel_.theta))

print("Accuracy: \$.3f (initial) \$.3f (optimized)"
      % (accuracy_score(y[:train_size], gp_fix.predict(X[:train_size])),
         accuracy_score(y[:train_size], gp_opt.predict(X[:train_size])))
print("Log-loss: \$.3f (initial) \$.3f (optimized)"
      % (log_loss(y[:train_size], gp_fix.predict_proba(X[:train_size])[:, 1]),
         log_loss(y[:train_size], gp_opt.predict_proba(X[:train_size])[:, 1])))

# Plot posteriors
plt.figure(0)
plt.scatter(X[:train_size, 0], y[:train_size], c='k', label="Train data",
            edgecolors=(0, 0, 0))
plt.scatter(X[train_size:, 0], y[train_size:], c='g', label="Test data",
            edgecolors=(0, 0, 0))
X_ = np.linspace(0, 5, 100)
plt.plot(X_, gp_fix.predict_proba(X_[:, np.newaxis])[:, 1], 'r',
         label="Initial kernel: %s" % gp_fix.kernel_)
plt.plot(X_, gp_opt.predict_proba(X_[:, np.newaxis])[:, 1], 'b',
         label="Optimized kernel: %s" % gp_opt.kernel_)
plt.xlabel("Feature")
plt.ylabel("Class 1 probability")
plt.xlim(0, 5)
plt.ylim(-0.25, 1.5)
plt.legend(loc="best")

# Plot LML landscape
plt.figure(1)
theta0 = np.logspace(0, 8, 30)
theta1 = np.logspace(-1, 1, 29)
Theta0, Theta1 = np.meshgrid(theta0, theta1)
LML = [
    [gp_opt.log_marginal_likelihood(np.log([Theta0[i, j], Theta1[i, j]]))
     for i in range(Theta0.shape[0])]
    for j in range(Theta0.shape[1])]
LML = np.array(LML).T
plt.plot(np.exp(gp_fix.kernel_.theta)[0], np.exp(gp_fix.kernel_.theta)[1],
         'ko', zorder=10)
plt.plot(np.exp(gp_opt.kernel_.theta)[0], np.exp(gp_opt.kernel_.theta)[1],
         'ko', zorder=10)
plt.pcolor(Theta0, Theta1, LML)
plt.xscale("log")
plt.yscale("log")
plt.colorbar()
plt.xlabel("Magnitude")
plt.ylabel("Length-scale")
plt.title("Log-marginal-likelihood")
plt.show()

Total running time of the script: ( 0 minutes 4.732 seconds)

17.8 Gaussian process regression (GPR) with noise-level estimation

This example illustrates that GPR with a sum-kernel including a WhiteKernel can estimate the noise level of data. An illustration of the log-marginal-likelihood (LML) landscape shows that there exist two local maxima of LML. The first corresponds to a model with a high noise level and a large length scale, which explains all variations in the data by noise. The second one has a smaller noise level and shorter length scale, which explains most of the variation by the noise-free functional relationship. The second model has a higher likelihood; however, depending on the initial value for the hyperparameters, the gradient-based optimization might also converge to the high-noise solution. It is thus important to repeat the optimization several times for different initializations.
```python
import numpy as np
from matplotlib import pyplot as plt
from matplotlib.colors import LogNorm
from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF, WhiteKernel

rng = np.random.RandomState(0)
X = rng.uniform(0, 5, 20)[:, np.newaxis]
y = 0.5 * np.sin(3 * X[:, 0]) + rng.normal(0, 0.5, X.shape[0])

# First run
plt.figure(0)
kern = 1.0 * RBF(length_scale=100.0, length_scale_bounds=(1e-2, 1e3)) 
  + WhiteKernel(noise_level=1, noise_level_bounds=(1e-10, 1e+1))
gp = GaussianProcessRegressor(kernel=kern,
  alpha=0.0).fit(X, y)
X_ = np.linspace(0, 5, 100)
plt.plot(X_, gp.predict(X_[:, np.newaxis], return_cov=True)
  .mean, 'k', lw=3, zorder=9)
plt.fill_between(X_, gp.predict(X_[:, np.newaxis], return_cov=True)
  .mean - np.sqrt(np.diag(gp.predict(X_[:, np.newaxis], return_cov=True).cov)),
  gp.predict(X_[:, np.newaxis], return_cov=True).mean 
  + np.sqrt(np.diag(gp.predict(X_[:, np.newaxis], return_cov=True).cov)),
  alpha=0.5, color='k')
plt.plot(X_, 0.5*np.sin(3*X_), 'r', lw=3, zorder=9)
plt.scatter(X[:, 0], y, c='r', s=50, zorder=10, edgecolors=(0, 0, 0))
plt.title("Initial: %s\nOptimum: %s\nLog-Marginal-Likelihood: %s" 
  % (kern, gp.kernel_, 
  gp.log_marginal_likelihood(gp.kernel_.theta)))
plt.tight_layout()

# Second run
plt.figure(1)
kern = 1.0 * RBF(length_scale=1.0, length_scale_bounds=(1e-2, 1e3)) 
  + WhiteKernel(noise_level=1e-5, noise_level_bounds=(1e-10, 1e+1))
gp = GaussianProcessRegressor(kernel=kern,
```

---

`print(__doc__)`

# Authors: Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
#
# License: BSD 3 clause

---

Chapter 17. Gaussian Process for Machine Learning
alpha=0.0).fit(X, y)
X_ = np.linspace(0, 5, 100)
y_mean, y_cov = gp.predict(X_[:, np.newaxis], return_cov=True)
plt.plot(X_, y_mean, 'k', lw=3, zorder=9)
plt.fill_between(X_, y_mean - np.sqrt(np.diag(y_cov)), y_mean + np.sqrt(np.diag(y_cov)), alpha=0.5, color='k')
plt.plot(X_, 0.5*np.sin(3*X_), 'r', lw=3, zorder=9)
plt.scatter(X[:, 0], y, c='r', s=50, zorder=10, edgecolors=(0, 0, 0))
plt.title("Initial: \$s\nOptimum: \$s\nLog-Marginal-Likelihood: \$s\n" % (kernel, gp.kernel_, gp.log_marginal_likelihood(gp.kernel_.theta)))
plt.tight_layout()

# Plot LML landscape
plt.figure(2)
theta0 = np.logspace(-2, 3, 49)
theta1 = np.logspace(-2, 0, 50)
Theta0, Theta1 = np.meshgrid(theta0, theta1)
LML = [[gp.log_marginal_likelihood(np.log([0.36, Theta0[i, j], Theta1[i, j]]))
        for i in range(Theta0.shape[0])]
        for j in range(Theta0.shape[1])]
LML = np.array(LML).T
vmin, vmax = (-LML).min(), (-LML).max()
vmax = 50
level = np.around(np.logspace(np.log10(vmin), np.log10(vmax), 50), decimals=1)
plt.contour(Theta0, Theta1, -LML, levels=level, norm=LogNorm(vmin=vmin, vmax=vmax))
plt.colorbar()
plt.xscale("log")
plt.yscale("log")
plt.xlabel("Length-scale")
plt.ylabel("Noise-level")
plt.title("Log-marginal-likelihood")
plt.tight_layout()
plt.show()

Total running time of the script: ( 0 minutes 4.792 seconds)

17.9 Gaussian Processes regression: basic introductory example

A simple one-dimensional regression example computed in two different ways:

1. A noise-free case
2. A noisy case with known noise-level per datapoint

In both cases, the kernel’s parameters are estimated using the maximum likelihood principle.

The figures illustrate the interpolating property of the Gaussian Process model as well as its probabilistic nature in the form of a pointwise 95% confidence interval.

Note that the parameter alpha is applied as a Tikhonov regularization of the assumed covariance between the training points.
print(__doc__)

# Author: Vincent Dubourg <vincent.dubourg@gmail.com>
#         Jake Vanderplas <vanderplas@astro.washington.edu>
#         Jan Hendrik Metzen <jhm@informatik.uni-bremen.de>
# License: BSD 3 clause

import numpy as np
from matplotlib import pyplot as plt
from sklearn.gaussian_process import GaussianProcessRegressor
from sklearn.gaussian_process.kernels import RBF, ConstantKernel as C

np.random.seed(1)

def f(x):
    """The function to predict."""
    return x * np.sin(x)

# First the noiseless case
X = np.atleast_2d([1., 3., 5., 6., 7., 8.]).T

# Observations
y = f(X).ravel()
Mesh the input space for evaluations of the real function, the prediction and its MSE

```python
x = np.atleast_2d(np.linspace(0, 10, 1000)).T
```

Instantiate a Gaussian Process model

```python
kernel = C(1.0, (1e-3, 1e3)) * RBF(10, (1e-2, 1e2))
gp = GaussianProcessRegressor(kernel=kernel, n_restarts_optimizer=9)
```

Fit to data using Maximum Likelihood Estimation of the parameters

```python
gp.fit(X, y)
```

Make the prediction on the meshed x-axis (ask for MSE as well)

```python
y_pred, sigma = gp.predict(x, return_std=True)
```

Plot the function, the prediction and the 95% confidence interval based on the MSE

```python
plt.figure()
plt.plot(x, f(x), 'r:', label=u'$f(x) = x\sin(x)$')
plt.plot(X, y, 'r.', markersize=10, label=u'Observations')
plt.plot(x, y_pred, 'b-', label=u'Prediction')
plt.fill(np.concatenate([x, x[::-1]]),
         np.concatenate([y_pred - 1.9600 * sigma,
                         (y_pred + 1.9600 * sigma)[::-1]]),
         alpha=.5, fc='b', ec='None', label='95% confidence interval')
plt.xlabel('$x$')
plt.ylabel('$f(x)$')
plt.ylim(-10, 20)
plt.legend(loc='upper left')
```

Now the noisy case

```python
X = np.linspace(0.1, 9.9, 20)
X = np.atleast_2d(X).T

# Observations and noise
y = f(X).ravel()
dy = 0.5 + 1.0 * np.random.random(y.shape)
n = 0.5 + 1.0 * np.random.normal(0, dy)
y += noise

# Instantiate a Gaussian Process model
gp = GaussianProcessRegressor(kernel=kernel, alpha=(dy / y) ** 2,
                               n_restarts_optimizer=10)

# Fit to data using Maximum Likelihood Estimation of the parameters
gp.fit(X, y)

# Make the prediction on the meshed x-axis (ask for MSE as well)
y_pred, sigma = gp.predict(x, return_std=True)

# Plot the function, the prediction and the 95% confidence interval based on the MSE
plt.figure()
plt.plot(x, f(x), 'r:', label=u'$f(x) = x\sin(x)$')
plt.errorbar(X.ravel(), y, dy, fmt='r.', markersize=10, label=u'Observations')
plt.plot(x, y_pred, 'b-', label=u'Prediction')
plt.fill(np.concatenate([x, x[::-1]]),
         np.concatenate([y_pred - 1.9600 * sigma,
                         (y_pred + 1.9600 * sigma)[::-1]]),
         alpha=.5, fc='b', ec='None', label='95% confidence interval')
plt.xlabel('$x$')
plt.ylabel('$f(x)$')
plt.ylim(-10, 20)
plt.legend(loc='upper left')
```
(y_pred + 1.9600 * sigma)[::-1]),
alpha=.5, fc='b', ec='None', label='95% confidence interval')
plt.xlabel('$x$')
plt.ylabel('$f(x)$')
plt.xlim(-10, 20)
plt.legend(loc='upper left')
plt.show()

Total running time of the script: ( 0 minutes 0.594 seconds)
Examples concerning the `sklearn.linear_model` module.

### 18.1 Lasso path using LARS

Computes Lasso Path along the regularization parameter using the LARS algorithm on the diabetes dataset. Each color represents a different feature of the coefficient vector, and this is displayed as a function of the regularization parameter.
Computing regularization path using the LARS ...

print(__doc__)

# Author: Fabian Pedregosa <fabian.pedregosa@inria.fr>
# Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model
from sklearn import datasets
diabetes = datasets.load_diabetes()
X = diabetes.data
y = diabetes.target

print("Computing regularization path using the LARS ...")
_, _, coefs = linear_model.lars_path(X, y, method='lasso', verbose=True)

xx = np.sum(np.abs(coefs.T), axis=1)
xx /= xx[-1]
plt.plot(xx, coefs.T)
ymin, ymax = plt.ylim()
plt.vlines(xx, ymin, ymax, linestyle='dashed')
plt.xlabel('|coef| / max|coef|')
plt.ylabel('Coefficients')
plt.title('LASSO Path')
plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.091 seconds)

18.2 Plot Ridge coefficients as a function of the regularization

Shows the effect of collinearity in the coefficients of an estimator.

Ridge Regression is the estimator used in this example. Each color represents a different feature of the coefficient vector, and this is displayed as a function of the regularization parameter.

This example also shows the usefulness of applying Ridge regression to highly ill-conditioned matrices. For such matrices, a slight change in the target variable can cause huge variances in the calculated weights. In such cases, it is useful to set a certain regularization (alpha) to reduce this variation (noise).

When alpha is very large, the regularization effect dominates the squared loss function and the coefficients tend to zero. At the end of the path, as alpha tends toward zero and the solution tends towards the ordinary least squares, coefficients exhibit big oscillations. In practise it is necessary to tune alpha in such a way that a balance is maintained between both.
Ridge coefficients as a function of the regularization

```python
# Author: Fabian Pedregosa -- <fabian.pedregosa@inria.fr>
# License: BSD 3 clause

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model

# X is the 10x10 Hilbert matrix
X = 1. / (np.arange(1, 11) + np.arange(0, 10)[..., np.newaxis])
y = np.ones(10)

# #############################################################################
# Compute paths
n_alphas = 200
alphas = np.logspace(-10, -2, n_alphas)

coefs = []
for a in alphas:
    ridge = linear_model.Ridge(alpha=a, fit_intercept=False)
    ridge.fit(X, y)
    coefs.append(ridge.coef_)

# #############################################################################
18.2. Plot Ridge coefficients as a function of the regularization
```
# Display results

```python
ax = plt.gca()

ax.plot(alphas, coefs)
ax.set_xscale('log')
ax.set_xlim(ax.get_xlim()[::-1])  # reverse axis
plt.xlabel('alpha')
plt.ylabel('weights')
plt.title('Ridge coefficients as a function of the regularization')
plt.axis('tight')
plt.show()
```

Total running time of the script: (0 minutes 0.149 seconds)

## 18.3 SGD: Maximum margin separating hyperplane

Plot the maximum margin separating hyperplane within a two-class separable dataset using a linear Support Vector Machines classifier trained using SGD.

```python
print(__doc__)

import numpy as np
```
import matplotlib.pyplot as plt
from sklearn.linear_model import SGDClassifier
from sklearn.datasets.samples_generator import make_blobs

# we create 50 separable points
X, Y = make_blobs(n_samples=50, centers=2, random_state=0, cluster_std=0.60)

# fit the model
clf = SGDClassifier(loss="hinge", alpha=0.01, max_iter=200, fit_intercept=True)
clf.fit(X, Y)

# plot the line, the points, and the nearest vectors to the plane
xx = np.linspace(-1, 5, 10)
yy = np.linspace(-1, 5, 10)
X1, X2 = np.meshgrid(xx, yy)
Z = np.empty(X1.shape)
for (i, j), val in np.ndenumerate(X1):
    x1 = val
    x2 = X2[i, j]
    p = clf.decision_function([[x1, x2]])
    Z[i, j] = p[0]
levels = [-1.0, 0.0, 1.0]
linestyles = ['dashed', 'solid', 'dashed']
plt.contour(X1, X2, Z, levels, colors='k', linestyles=linestyles)
plt.scatter(X[:, 0], X[:, 1], c=Y, cmap=plt.cm.Paired, edgecolor='black', s=20)

plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.054 seconds)

18.4 Path with L1- Logistic Regression

Computes path on IRIS dataset.
Computing regularization path ...
This took 0:00:00.030845

Out:

print(__doc__)

# Author: Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause

from datetime import datetime
import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model
from sklearn import datasets
from sklearn.svm import l1_min_c

iris = datasets.load_iris()
X = iris.data
y = iris.target

954 Chapter 18. Generalized Linear Models
X = X[y != 2]
y = y[y != 2]

X -= np.mean(X, 0)

# Demo path functions

cs = l1_min_c(X, y, loss='log') * np.logspace(0, 3)

print("Computing regularization path ...")
start = datetime.now()
clf = linear_model.LogisticRegression(C=1.0, penalty='l1', tol=1e-6)
coefs_ = []
for c in cs:
    clf.set_params(C=c)
    clf.fit(X, y)
    coefs_.append(clf.coef_.ravel().copy())
print("This took ", datetime.now() - start)

coefs_ = np.array(coefs_)
plt.plot(np.log10(cs), coefs_)
ymin, ymax = plt.ylim()
plt.xlabel('log(C)')
plt.ylabel('Coefficients')
plt.title('Logistic Regression Path')
plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.074 seconds)

18.5 SGD: convex loss functions

A plot that compares the various convex loss functions supported by sklearn.linear_model.SGDClassifier.
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

def modified_huber_loss(y_true, y_pred):
    z = y_pred * y_true
    loss = -4 * z
    loss[z >= -1] = (1 - z[z >= -1]) ** 2
    loss[z >= 1.] = 0
    return loss

xmin, xmax = -4, 4
xx = np.linspace(xmin, xmax, 100)
lw = 2
plt.plot([xmin, 0, 0, xmax], [1, 1, 0, 0], color='gold', lw=lw,
         label="Zero-one loss")
plt.plot(xx, np.where(xx < 1, 1 - xx, 0), color='teal', lw=lw,
         label="Hinge loss")
plt.plot(xx, -np.minimum(xx, 0), color='yellowgreen', lw=lw,
         label="Perceptron loss")
plt.plot(xx, np.log2(1 + np.exp(-xx)), color='cornflowerblue', lw=lw,
         label="Log loss")
plt.plot(xx, np.where(xx < 1, 1 - xx, 0) ** 2, color='orange', lw=lw,
18.6 Plot Ridge coefficients as a function of the L2 regularization

Ridge Regression is the estimator used in this example. Each color in the left plot represents one different dimension of the coefficient vector, and this is displayed as a function of the regularization parameter. The right plot shows how exact the solution is. This example illustrates how a well defined solution is found by Ridge regression and how regularization affects the coefficients and their values. The plot on the right shows how the difference of the coefficients from the estimator changes as a function of regularization.

In this example the dependent variable $Y$ is set as a function of the input features: $y = Xw + c$. The coefficient vector $w$ is randomly sampled from a normal distribution, whereas the bias term $c$ is set to a constant.

As alpha tends toward zero the coefficients found by Ridge regression stabilize towards the randomly sampled vector $w$. For big alpha (strong regularisation) the coefficients are smaller (eventually converging at 0) leading to a simpler and biased solution. These dependencies can be observed on the left plot.

The right plot shows the mean squared error between the coefficients found by the model and the chosen vector $w$. Less regularised models retrieve the exact coefficients (error is equal to 0), stronger regularised models increase the error.

Please note that in this example the data is non-noisy, hence it is possible to extract the exact coefficients.
clf = Ridge()

X, y, w = make_regression(n_samples=10, n_features=10, coef=True, random_state=1, bias=3.5)

coefs = []
errors = []

alphas = np.logspace(-6, 6, 200)

# Train the model with different regularisation strengths
for a in alphas:
    clf.set_params(alpha=a)
    clf.fit(X, y)
    coefs.append(clf.coef_)
    errors.append(mean_squared_error(clf.coef_, w))

# Display results
plt.figure(figsize=(20, 6))
plt.subplot(121)
ax = plt.gca()
ax.plot(alphas, coefs)
ax.set_xscale('log')
plt.xlabel('alpha')
plt.ylabel('weights')
plt.title('Ridge coefficients as a function of the regularization')
plt.axis('tight')
plt.subplot(122)
ax = plt.gca()
ax.plot(alphas, errors)
ax.set_xscale('log')
plt.xlabel('alpha')
plt.ylabel('error')
plt.title('Coefficient error as a function of the regularization')
plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.262 seconds)

18.7 Ordinary Least Squares and Ridge Regression Variance

Due to the few points in each dimension and the straight line that linear regression uses to follow these points as well as it can, noise on the observations will cause great variance as shown in the first plot. Every line’s slope can vary quite a bit for each prediction due to the noise induced in the observations.

Ridge regression is basically minimizing a penalised version of the least-squared function. The penalising shrinks the value of the regression coefficients. Despite the few data points in each dimension, the slope of the prediction is much more stable and the variance in the line itself is greatly reduced, in comparison to that of the standard linear regression.
# Ordinary Least Squares and Ridge Regression Variance

```python
print(__doc__)

# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model

X_train = np.c_[.5, 1].T
y_train = [.5, 1]
X_test = np.c_[0, 2].T

np.random.seed(0)

classifiers = dict(ols=linear_model.LinearRegression(),
                   ridge=linear_model.Ridge(alpha=.1))

fignum = 1
for name, clf in classifiers.items():
    fig = plt.figure(fignum, figsize=(4, 3))
    plt.clf()
    plt.title(name)
    ax = plt.axes([.12, .12, .8, .8])
    for _ in range(6):
        this_X = .1 * np.random.normal(size=(2, 1)) + X_train
        clf.fit(this_X, y_train)
        ax.plot(X_test, clf.predict(X_test), color='.5')
        ax.scatter(this_X, y_train, s=3, c='.5', marker='o', zorder=10)

    clf.fit(X_train, y_train)
    ax.plot(X_test, clf.predict(X_test), linewidth=2, color='blue')

fignum += 1
```

18.7. Ordinary Least Squares and Ridge Regression Variance
18.8 Logistic function

Shown in the plot is how the logistic regression would, in this synthetic dataset, classify values as either 0 or 1, i.e. class one or two, using the logistic curve.
X = np.random.normal(size=n_samples)
y = (X > 0).astype(np.float)
X[X > 0] *= 4
X += .3 * np.random.normal(size=n_samples)
X = X[:, np.newaxis]

# run the classifier
clf = linear_model.LogisticRegression(C=1e5)
clf.fit(X, y)

# and plot the result
plt.figure(1, figsize=(4, 3))
plt.clf()
plt.scatter(X.ravel(), y, color='black', zorder=20)
X_test = np.linspace(-5, 10, 300)
def model(x):
    return 1 / (1 + np.exp(-x))
loss = model(X_test * clf.coef_ + clf.intercept_).ravel()
plt.plot(X_test, loss, color='red', linewidth=3)

ols = linear_model.LinearRegression()
ols.fit(X, y)
plt.plot(X_test, ols.coef_ * X_test + ols.intercept_, linewidth=1)
plt.axhline(.5, color='.5')
plt.ylabel('y')
plt.xlabel('X')
plt.xticks(range(-5, 10))
plt.yticks([0, .5, 1])
plt.ylim(-.25, 1.25)
plt.xlim(-4, 10)
plt.legend(('Logistic Regression Model', 'Linear Regression Model'),
            loc="lower right", fontsize='small')
plt.show()

Total running time of the script: ( 0 minutes 0.072 seconds)

18.9 Polynomial interpolation

This example demonstrates how to approximate a function with a polynomial of degree n_degree by using ridge regression. Concretely, from n_samples 1d points, it suffices to build the Vandermonde matrix, which is n_samples x n_degree+1 and has the following form:

[[1, x_1, x_1 ** 2, x_1 ** 3, ...], [1, x_2, x_2 ** 2, x_2 ** 3, ...], ...]

Intuitively, this matrix can be interpreted as a matrix of pseudo features (the points raised to some power). The matrix is akin to (but different from) the matrix induced by a polynomial kernel.

This example shows that you can do non-linear regression with a linear model, using a pipeline to add non-linear features. Kernel methods extend this idea and can induce very high (even infinite) dimensional feature spaces.
# Author: Mathieu Blondel
# Jake Vanderplas
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.linear_model import Ridge
from sklearn.preprocessing import PolynomialFeatures
from sklearn.pipeline import make_pipeline

def f(x):
    """ function to approximate by polynomial interpolation""
    return x * np.sin(x)

# generate points used to plot
x_plot = np.linspace(0, 10, 100)

# generate points and keep a subset of them
x = np.linspace(0, 10, 100)
rng = np.random.RandomState(0)
rng.shuffle(x)
x = np.sort(x[:20])
y = f(x)

# create matrix versions of these arrays
X = x[:, np.newaxis]
X_plot = x_plot[:, np.newaxis]

colors = ['teal', 'yellowgreen', 'gold']
lw = 2
plt.plot(x_plot, f(x_plot), color='cornflowerblue', linewidth=lw, label='ground truth')
plt.scatter(x, y, color='navy', s=30, marker='o', label='training points')

for count, degree in enumerate([3, 4, 5]):
    model = make_pipeline(PolynomialFeatures(degree), Ridge())
    model.fit(X, y)
    y_plot = model.predict(X_plot)
    plt.plot(x_plot, y_plot, color=colors[count], linewidth=lw, label='degree %d' % degree)

plt.legend(loc='lower left')
plt.show()

Total running time of the script: ( 0 minutes 0.076 seconds)

18.10 Logistic Regression 3-class Classifier

Show below is a logistic-regression classifiers decision boundaries on the iris dataset. The datapoints are colored according to their labels.
18.11 SGD: Weighted samples

Plot decision function of a weighted dataset, where the size of points is proportional to its weight.
print(__doc__)  

import numpy as np
import matplotlib.pyplot as plt
from sklearn import linear_model

# we create 20 points
np.random.seed(0)
X = np.r_[np.random.randn(10, 2) + [1, 1], np.random.randn(10, 2)]
y = [1] * 10 + [-1] * 10
sample_weight = 100 * np.abs(np.random.randn(20))
# and assign a bigger weight to the last 10 samples
sample_weight[:10] *= 10

# plot the weighted data points
xx, yy = np.meshgrid(np.linspace(-4, 5, 500), np.linspace(-4, 5, 500))
plt.figure()
plt.scatter(X[:, 0], X[:, 1], c=y, s=sample_weight, alpha=0.9,
cmap=plt.cm.bone, edgecolor='black')

# fit the unweighted model
clf = linear_model.SGDClassifier(alpha=0.01, max_iter=100)
clf.fit(X, y)
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
no_weights = plt.contour(xx, yy, Z, levels=[0], linestyles=['solid'])

18.11. SGD: Weighted samples
# fit the weighted model
clf = linear_model.SGDClassifier(alpha=0.01, max_iter=100)
clf.fit(X, y, sample_weight=sample_weight)
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
samples_weights = plt.contour(xx, yy, Z, levels=[0], linestyles=['dashed'])

plt.legend([no_weights.collections[0], samples_weights.collections[0]],
            ['no weights', 'with weights'], loc="lower left")

plt.xticks(()
plt.yticks()
plt.show()

Total running time of the script: ( 0 minutes 0.095 seconds)

18.12 Linear Regression Example

This example uses the only the first feature of the diabetes dataset, in order to illustrate a two-dimensional plot of this regression technique. The straight line can be seen in the plot, showing how linear regression attempts to draw a straight line that will best minimize the residual sum of squares between the observed responses in the dataset, and the responses predicted by the linear approximation.

The coefficients, the residual sum of squares and the variance score are also calculated.
Out:

Coefficients:
[ 938.23786125]
Mean squared error: 2548.07
Variance score: 0.47

print(__doc__)

# Code source: Jaques Grobler
# License: BSD 3 clause

import matplotlib.pyplot as plt
import numpy as np
from sklearn import datasets, linear_model
from sklearn.metrics import mean_squared_error, r2_score

# Load the diabetes dataset
diabetes = datasets.load_diabetes()
# Use only one feature
diabetes_X = diabetes.data[:, np.newaxis, 2]

# Split the data into training/testing sets
diabetes_X_train = diabetes_X[:-20]
diabetes_X_test = diabetes_X[-20:]

# Split the targets into training/testing sets
diabetes_y_train = diabetes.target[:-20]
diabetes_y_test = diabetes.target[-20:]

# Create linear regression object
regr = linear_model.LinearRegression()

# Train the model using the training sets
regr.fit(diabetes_X_train, diabetes_y_train)

# Make predictions using the testing set
diabetes_y_pred = regr.predict(diabetes_X_test)

# The coefficients
print('Coefficients:
', regr.coef_)

# The mean squared error
print("Mean squared error: \%.2f" % mean_squared_error(diabetes_y_test, diabetes_y_pred))

# Explained variance score: 1 is perfect prediction
print('Variance score: \%.2f' % r2_score(diabetes_y_test, diabetes_y_pred))

# Plot outputs
plt.scatter(diabetes_X_test, diabetes_y_test, color='black')
plt.plot(diabetes_X_test, diabetes_y_pred, color='blue', linewidth=3)

plt.xticks(())
plt.yticks(())

plt.show()

Total running time of the script: ( 0 minutes 0.091 seconds)

18.13 Robust linear model estimation using RANSAC

In this example we see how to robustly fit a linear model to faulty data using the RANSAC algorithm.
```python
import numpy as np
from matplotlib import pyplot as plt
from sklearn import linear_model, datasets

n_samples = 1000
n_outliers = 50

X, y, coef = datasets.make_regression(n_samples=n_samples, n_features=1,
    n_informative=1, noise=10,
    coef=True, random_state=0)

np.random.seed(0)
```

Estimated coefficients (true, linear regression, RANSAC):
82.1903908407869
[ 54.17236387]
[ 82.08533159]
X[:n_outliers] = 3 + 0.5 * np.random.normal(size=(n_outliers, 1))
y[:n_outliers] = -3 + 10 * np.random.normal(size=n_outliers)

# Fit line using all data
lr = linear_model.LinearRegression()
lr.fit(X, y)

# Robustly fit linear model with RANSAC algorithm
ransac = linear_model.RANSACRegressor()
ransac.fit(X, y)
inlier_mask = ransac.inlier_mask_
outlier_mask = np.logical_not(inlier_mask)

# Predict data of estimated models
line_X = np.arange(X.min(), X.max())[:, np.newaxis]
line_y = lr.predict(line_X)
line_y_ransac = ransac.predict(line_X)

# Compare estimated coefficients
print("Estimated coefficients (true, linear regression, RANSAC):")
print(coef, lr.coef_, ransac.estimator_.coef_)

lw = 2
plt.scatter(X[inlier_mask], y[inlier_mask], color='yellowgreen', marker='.',
            label='Inliers')
plt.scatter(X[outlier_mask], y[outlier_mask], color='gold', marker='.',
            label='Outliers')
plt.plot(line_X, line_y, color='navy', linewidth=lw, label='Linear regressor')
plt.plot(line_X, line_y_ransac, color='cornflowerblue', linewidth=lw,
         label='RANSAC regressor')
plt.legend(loc='lower right')
plt.xlabel("Input")
plt.ylabel("Response")
plt.show()

Total running time of the script: ( 0 minutes 0.166 seconds)

18.14 Sparsity Example: Fitting only features 1 and 2

Features 1 and 2 of the diabetes-dataset are fitted and plotted below. It illustrates that although feature 2 has a strong
coefficient on the full model, it does not give us much regarding y when compared to just feature 1
```python
# Code source: Gaël Varoquaux
# Modified for documentation by Jaques Grobler
# License: BSD 3 clause

import matplotlib.pyplot as plt
import numpy as np
from mpl_toolkits.mplot3d import Axes3D
from sklearn import datasets, linear_model

diabetes = datasets.load_diabetes()
indices = (0, 1)

X_train = diabetes.data[:-20, indices]
X_test = diabetes.data[-20:, indices]
y_train = diabetes.target[:-20]
y_test = diabetes.target[-20:]

ols = linear_model.LinearRegression()
ols.fit(X_train, y_train)

# Plot the figure

def plot_figs(fig_num, elev, azim, X_train, clf):
    fig = plt.figure(fig_num, figsize=(4, 3))
    plt.clf()
    ax = Axes3D(fig, elev=elev, azim=azim)

    ax.scatter(X_train[:, 0], X_train[:, 1], y_train, c='k', marker='+')
    ax.plot_surface(np.array([[-.1, -.1], [.15, .15]]),
                    np.array([[-.1, .15], [-.1, .15]]),
                    clf.predict(np.array([[-.1, -.1, .15, .15],
                                          [-.1, .15, -.1, .15]]).T
                    ).reshape((2, 2)),
```

18.14. Sparsity Example: Fitting only features 1 and 2
alpha=.5)
ax.set_xlabel('X_1')
ax.set_ylabel('X_2')
ax.set_zlabel('Y')
ax.w_xaxis.set_ticklabels([])
ax.w_yaxis.set_ticklabels([])
ax.w_zaxis.set_ticklabels([])

# Generate the three different figures from different views

elev = 43.5
azim = -110
plot_figs(1, elev, azim, X_train, ols)

elev = -.5
azim = 0
plot_figs(2, elev, azim, X_train, ols)

elev = -.5
azim = 90
plot_figs(3, elev, azim, X_train, ols)

plt.show()

Total running time of the script: ( 0 minutes 0.239 seconds)

18.15 Lasso on dense and sparse data

We show that linear_model.Lasso provides the same results for dense and sparse data and that in the case of sparse data the speed is improved.

Out:

--- Dense matrices
Sparse Lasso done in 0.169861s
Dense Lasso done in 0.063516s
Distance between coefficients : 1.0054870144020999e-13
--- Sparse matrices
Matrix density : 0.6263000000000001 %
Sparse Lasso done in 0.229270s
Dense Lasso done in 1.071237s
Distance between coefficients : 1.0424172088134681e-11

print(__doc__)

from time import time
from scipy import sparse
from scipy import linalg

from sklearn.datasets.samples_generator import make_regression
from sklearn.linear_model import Lasso
# The two Lasso implementations on Dense data

```python
print("--- Dense matrices")

X, y = make_regression(n_samples=200, n_features=5000, random_state=0)
X_sp = sparse.coo_matrix(X)
alpha = 1
sparse_lasso = Lasso(alpha=alpha, fit_intercept=False, max_iter=1000)
dense_lasso = Lasso(alpha=alpha, fit_intercept=False, max_iter=1000)

t0 = time()
sparse_lasso.fit(X_sp, y)
print("Sparse Lasso done in %f s" % (time() - t0))

t0 = time()
dense_lasso.fit(X, y)
print("Dense Lasso done in %f s" % (time() - t0))

print("Distance between coefficients : %s"
      % linalg.norm(sparse_lasso.coef_ - dense_lasso.coef_))
```

# The two Lasso implementations on Sparse data

```python
print("--- Sparse matrices")

Xs = X.copy()
Xs[Xs < 2.5] = 0.0
Xs = sparse.coo_matrix(Xs)
Xs = Xs.tocsc()

print("Matrix density : %s %%% (Xs.nnz / float(X.size) * 100))

alpha = 0.1
sparse_lasso = Lasso(alpha=alpha, fit_intercept=False, max_iter=10000)
dense_lasso = Lasso(alpha=alpha, fit_intercept=False, max_iter=10000)

t0 = time()
sparse_lasso.fit(Xs, y)
print("Sparse Lasso done in %f s" % (time() - t0))

t0 = time()
dense_lasso.fit(Xs.toarray(), y)
print("Dense Lasso done in %f s" % (time() - t0))

print("Distance between coefficients : %s"
      % linalg.norm(sparse_lasso.coef_ - dense_lasso.coef_))
```

Total running time of the script: (0 minutes 1.661 seconds)

### 18.16 HuberRegressor vs Ridge on dataset with strong outliers

Fit Ridge and HuberRegressor on a dataset with outliers.

The example shows that the predictions in ridge are strongly influenced by the outliers present in the dataset. The
Huber regressor is less influenced by the outliers since the model uses the linear loss for these. As the parameter epsilon is increased for the Huber regressor, the decision function approaches that of the ridge.

```python
# Authors: Manoj Kumar mks542@nyu.edu
# License: BSD 3 clause

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets import make_regression
from sklearn.linear_model import HuberRegressor, Ridge

# Generate toy data.
X, y = make_regression(n_samples=20, n_features=1, random_state=0, noise=4.0, bias=100.0)

# Add four strong outliers to the dataset.
X_outliers = np.random.normal(0, 0.5, size=(4, 1))
y_outliers = np.random.normal(2.0, size=4)
y_outliers[2:] += y.min() - y.mean() / 4.
y_outliers[2:] += y.max() + y.mean() / 4.
```
X = np.vstack((X, X_outliers))
y = np.concatenate((y, y_outliers))
plt.plot(X, y, 'b.')

# Fit the huber regressor over a series of epsilon values.
colors = ['r-', 'b-', 'y-', 'm-']

x = np.linspace(X.min(), X.max(), 7)
epsilon_values = [1.35, 1.5, 1.75, 1.9]
for k, epsilon in enumerate(epsilon_values):
    huber = HuberRegressor(fit_intercept=True, alpha=0.0, max_iter=100,
                           epsilon=epsilon)
    huber.fit(X, y)
    coef_ = huber.coef_ * x + huber.intercept_
    plt.plot(x, coef_, colors[k], label="huber loss, %s" % epsilon)

# Fit a ridge regressor to compare it to huber regressor.
ridge = Ridge(fit_intercept=True, alpha=0.0, random_state=0, normalize=True)
ridge.fit(X, y)
coef_ridge = ridge.coef_
coef_ = ridge.coef_ * x + ridge.intercept_
plt.plot(x, coef_, 'g-', label="ridge regression")

plt.title("Comparison of HuberRegressor vs Ridge")
plt.xlabel("X")
plt.ylabel("y")
plt.legend(loc=0)
plt.show()

Total running time of the script: 0 minutes 0.112 seconds

18.17 Comparing various online solvers

An example showing how different online solvers perform on the hand-written digits dataset.
Out:

training SGD
training ASGD
training Perceptron
training Passive-Aggressive I
training Passive-Aggressive II
training SAG

# Author: Rob Zinkov <rob at zinkov dot com>
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets

from sklearn.model_selection import train_test_split
from sklearn.linear_model import SGDClassifier, Perceptron
from sklearn.linear_model import PassiveAggressiveClassifier
from sklearn.linear_model import LogisticRegression
heldout = [0.95, 0.90, 0.75, 0.50, 0.01]
rounds = 20
digits = datasets.load_digits()
X, y = digits.data, digits.target

classifiers = [
    ('SGD', SGDClassifier(max_iter=100)),
    ('ASGD', SGDClassifier(average=True, max_iter=100)),
    ('Perceptron', Perceptron(tol=1e-3)),
    ('Passive-Aggressive I', PassiveAggressiveClassifier(loss='hinge',
        C=1.0, tol=1e-4)),
    ('Passive-Aggressive II', PassiveAggressiveClassifier(loss='squared_hinge',
        C=1.0, tol=1e-4)),
    ('SAG', LogisticRegression(solver='sag', tol=1e-1, C=1.e4 / X.shape[0]))
]

xx = 1. - np.array(heldout)

for name, clf in classifiers:
    print("training \$%s\$" % name)
    rng = np.random.RandomState(42)
    yy = []
    for i in heldout:
        yy_ = []
        for r in range(rounds):
            X_train, X_test, y_train, y_test = \
                train_test_split(X, y, test_size=i, random_state=rng)
            clf.fit(X_train, y_train)
            y_pred = clf.predict(X_test)
            yy_.append(1 - np.mean(y_pred == y_test))
        yy.append(np.mean(yy_))
    plt.plot(xx, yy, label=name)

plt.legend(loc="upper right")
plt.xlabel("Proportion train")
plt.ylabel("Test Error Rate")
plt.show()

Total running time of the script: ( 0 minutes 35.387 seconds)

18.18 SGD: Penalties

Plot the contours of the three penalties.

All of the above are supported by sklearn.linear_model.stochastic_gradient.
import numpy as np
import matplotlib.pyplot as plt

def l1(xs):
    return np.array([np.sqrt((1 - np.sqrt(x ** 2.0)) ** 2.0) for x in xs])

def l2(xs):
    return np.array([np.sqrt(1.0 - x ** 2.0) for x in xs])

def e1(xs, z):
    return np.array([(2 - 2 * x - 2 * z + 4 * x * z - 4 * z ** 2
                - 8 * x * z ** 2 + 8 * x ** 2 * z ** 2
                - 16 * x ** 2 * z ** 3 + 8 * x * z ** 3
                + 4 * x ** 2 * z ** 4) ** (1. / 2)
                - 2 * x * z ** 2) / (2 - 4 * z) for x in xs])

def cross(ext):

plt.plot([-ext, ext], [0, 0], "k-")
plt.plot([0, 0], [-ext, ext], "k-")

xs = np.linspace(0, 1, 100)
alpha = 0.501  # 0.5 division through zero
cross(1.2)
l1_color = "navy"
l2_color = "c"
elastic_net_color = "darkorange"
lw = 2

plt.plot(xs, l1(xs), color=l1_color, label="L1", lw=lw)
plt.plot(xs, -1.0 * l1(xs), color=l1_color, lw=lw)
plt.plot(-1 * xs, l1(xs), color=l1_color, lw=lw)
plt.plot(-1 * xs, -1.0 * l1(xs), color=l1_color, lw=lw)

plt.plot(xs, l2(xs), color=l2_color, label="L2", lw=lw)
plt.plot(xs, -1.0 * l2(xs), color=l2_color, lw=lw)
plt.plot(-1 * xs, l2(xs), color=l2_color, lw=lw)
plt.plot(-1 * xs, -1.0 * l2(xs), color=l2_color, lw=lw)

plt.plot(xs, el(xs, alpha), color=elastic_net_color, label="Elastic Net", lw=lw)
plt.plot(xs, -1.0 * el(xs, alpha), color=elastic_net_color, lw=lw)
plt.plot(-1 * xs, el(xs, alpha), color=elastic_net_color, lw=lw)
plt.plot(-1 * xs, -1.0 * el(xs, alpha), color=elastic_net_color, lw=lw)

plt.xlabel(r"$w_0$"
plt.ylabel(r"$w_1$"
plt.legend()
plt.axis("equal")
plt.show()

Total running time of the script: (0 minutes 0.070 seconds)

18.19 Joint feature selection with multi-task Lasso

The multi-task lasso allows to fit multiple regression problems jointly enforcing the selected features to be the same across tasks. This example simulates sequential measurements, each task is a time instant, and the relevant features vary in amplitude over time while being the same. The multi-task lasso imposes that features that are selected at one time point are select for all time point. This makes feature selection by the Lasso more stable.
# Generate some 2D coefficients with sine waves with random frequency and phase
n_samples, n_features, n_tasks = 100, 30, 40
n_relevant_features = 5
coef = np.zeros((n_tasks, n_features))
times = np.linspace(0, 2 * np.pi, n_tasks)
for k in range(n_relevant_features):
    coef[:, k] = np.sin((1. + rng.randn(1)) * times + 3 * rng.randn(1))

X = rng.randn(n_samples, n_features)
Y = np.dot(X, coef.T) + rng.randn(n_samples, n_tasks)

coef_lasso_ = np.array([Lasso(alpha=0.5).fit(X, y).coef_ for y in Y.T])
coef_multi_task_lasso_ = MultiTaskLasso(alpha=1.).fit(X, Y).coef_
# Plot support and time series

```python
fig = plt.figure(figsize=(8, 5))
plt.subplot(1, 2, 1)
plt.spy(coef_lasso_)
plt.xlabel('Feature')
plt.ylabel('Time (or Task)')
plt.text(10, 5, 'Lasso')
plt.subplot(1, 2, 2)
plt.spy(coef_multi_task_lasso_)
plt.xlabel('Feature')
plt.ylabel('Time (or Task)')
plt.text(10, 5, 'MultiTaskLasso')
fig.suptitle('Coefficient non-zero location')

feature_to_plot = 0
plt.figure()
lw = 2
plt.plot(coef[:, feature_to_plot], color='seagreen', linewidth=lw,
         label='Ground truth')
plt.plot(coef_lasso_[:, feature_to_plot], color='cornflowerblue', linewidth=lw,
         label='Lasso')
plt.plot(coef_multi_task_lasso_[:, feature_to_plot], color='gold', linewidth=lw,
         label='MultiTaskLasso')
plt.legend(loc='upper center')
plt.axis('tight')
plt.ylim([-1.1, 1.1])
plt.show()
```

**Total running time of the script:** ( 0 minutes 0.207 seconds)

## 18.20 Lasso and Elastic Net for Sparse Signals

Estimates Lasso and Elastic-Net regression models on a manually generated sparse signal corrupted with an additive noise. Estimated coefficients are compared with the ground-truth.
Lasso R^2: 0.385982, Elastic Net R^2: 0.240498

Out:

```
Lasso(alpha=0.1, copy_X=True, fit_intercept=True, max_iter=1000,
    normalize=False, positive=False, precompute=False, random_state=None,
    selection='cyclic', tol=0.0001, warm_start=False)
```

```
r^2 on test data : 0.385982
```

```
ElasticNet(alpha=0.1, copy_X=True, fit_intercept=True, l1_ratio=0.7,
    max_iter=1000, normalize=False, positive=False, precompute=False,
    random_state=None, selection='cyclic', tol=0.0001, warm_start=False)
```

```
r^2 on test data : 0.240498
```

```
print(__doc__)
```

```
import numpy as np
import matplotlib.pyplot as plt
from sklearn.metrics import r2_score

# Generate some sparse data to play with
np.random.seed(42)
```
n_samples, n_features = 50, 200
X = np.random.randn(n_samples, n_features)
coef = 3 * np.random.randn(n_features)
inds = np.arange(n_features)
np.random.shuffle(inds)
coef[inds[10:]] = 0  # sparsify coef
y = np.dot(X, coef)

# add noise
y += 0.01 * np.random.normal(size=n_samples)

# Split data in train set and test set
n_samples = X.shape[0]
X_train, y_train = X[:n_samples // 2], y[:n_samples // 2]
X_test, y_test = X[n_samples // 2:], y[n_samples // 2:]

# Lasso
from sklearn.linear_model import Lasso
alpha = 0.1
lasso = Lasso(alpha=alpha)
y_pred_lasso = lasso.fit(X_train, y_train).predict(X_test)
r2_score_lasso = r2_score(y_test, y_pred_lasso)
print(lasso)
print("r^2 on test data : %f" % r2_score_lasso)

# ElasticNet
from sklearn.linear_model import ElasticNet
enet = ElasticNet(alpha=alpha, l1_ratio=0.7)
y_pred_enet = enet.fit(X_train, y_train).predict(X_test)
r2_score_enet = r2_score(y_test, y_pred_enet)
print(enet)
print("r^2 on test data : %f" % r2_score_enet)

plt.plot(enet.coef_, color='lightgreen', linewidth=2,
         label='Elastic net coefficients')
plt.plot(lasso.coef_, color='gold', linewidth=2,
         label='Lasso coefficients')
plt.plot(coef, '--', color='navy', label='original coefficients')
plt.legend(loc='best')
plt.title("Lasso R^2: %f, Elastic Net R^2: %f" % (r2_score_lasso, r2_score_enet))
plt.show()

Total running time of the script: ( 0 minutes 0.171 seconds)

18.21 MNIST classification using multinomial logistic + L1

Here we fit a multinomial logistic regression with L1 penalty on a subset of the MNIST digits classification task. We use the SAGA algorithm for this purpose: this a solver that is fast when the number of samples is significantly larger
than the number of features and is able to finely optimize non-smooth objective functions which is the case with the L1-penalty. Test accuracy reaches > 0.8, while weight vectors remains sparse and therefore more easily interpretable.

Note that this accuracy of this L1-penalized linear model is significantly below what can be reached by an L2-penalized linear model or a non-linear multi-layer perceptron model on this dataset.

```
import time
import matplotlib.pyplot as plt
import numpy as np
from sklearn.datasets import fetch_mldata
from sklearn.linear_model import LogisticRegression
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.utils import check_random_state

print(__doc__)

# Author: Arthur Mensch <arthur.mensch@m4x.org>
# License: BSD 3 clause

# Turn down for faster convergence
t0 = time.time()
train_samples = 5000

mnist = fetch_mldata('MNIST original')
```
X = X_train, y = y_train, y_test = train_test_split(  
    X, y, train_size=train_samples, test_size=10000)

scaler = StandardScaler()
X_train = scaler.fit_transform(X_train)
X_test = scaler.transform(X_test)

# Turn up tolerance for faster convergence
clf = LogisticRegression(C=50. / train_samples,
                                           multi_class='multinomial',
                                           penalty='l1', solver='saga', tol=0.1)
clf.fit(X_train, y_train)
sparsity = np.mean(clf.coef_ == 0) * 100
score = clf.score(X_test, y_test)
# print('Best C % .4f' % clf.C_)
print("Sparsity with L1 penalty: %.2f\%" % sparsity)
print("Test score with L1 penalty: %.4f" % score)

c = clf.coef_.copy()
plt.figure(figsize=(10, 5))
scale = np.abs(c).max()
for i in range(10):
    ll_plot = plt.subplot(2, 5, i + 1)
    ll_plot.imshow(c[i].reshape(28, 28), interpolation='nearest',
                   cmap=plt.cm.RdBu, vmin=-scale, vmax=scale)
    ll_plot.set_xticks(())
    ll_plot.set_yticks(())
    ll_plot.set_xlabel('Class %i' % i)
plt.suptitle('Classification vector for...')
run_time = time.time() - t0
print('Example run in % .3f s' % run_time)
plt.show()
n_components, n_features = 512, 100
n_nonzero_coefs = 17

# generate the data

# y = Xw
# |x|_0 = n_nonzero_coefs
y, X, w = make_sparse_coded_signal(n_samples=1,
n_components=n_components,
n_features=n_features,
n_nonzero_coefs=n_nonzero_coefs,
random_state=0)

idx, = w.nonzero()

# distort the clean signal

y_noisy = y + 0.05 * np.random.randn(len(y))

# plot the sparse signal

plt.figure(figsize=(7, 7))
plt.subplot(4, 1, 1)
plt.xlim(0, 512)
plt.title("Sparse signal")
plt.stem(idx, w[idx])

# plot the noise-free reconstruction

plt.figure(figsize=(7, 7))
plt.subplot(4, 1, 1)
plt.xlim(0, 512)
plt.stem(idx, w[idx])
omp = OrthogonalMatchingPursuit(n_nonzero_coefs=n_nonzero_coefs)
omp.fit(X, y)
coef = omp.coef_
idx_r, = coef.nonzero()
plt.subplot(4, 1, 2)
plt.xlim(0, 512)
plt.title("Recovered signal from noise-free measurements")
plt.stem(idx_r, coef[idx_r])

# plot the noisy reconstruction
```python
omp.fit(X, y_noisy)
coef = omp.coef_
idx_r, = coef.nonzero()
plt.subplot(4, 1, 3)
plt.xlim(0, 512)
plt.title("Recovered signal from noise-free measurements")
plt.stem(idx_r, coef[idx_r])

# plot the noisy reconstruction with number of non-zeros set by CV
```
```python
omp_cv = OrthogonalMatchingPursuitCV()
omp_cv.fit(X, y_noisy)
coef = omp_cv.coef_
idx_r, = coef.nonzero()
plt.subplot(4, 1, 4)
plt.xlim(0, 512)
plt.title("Recovered signal from noisy measurements with CV")
plt.stem(idx_r, coef[idx_r])
plt.subplots_adjust(0.06, 0.04, 0.94, 0.90, 0.20, 0.38)
plt.suptitle('Sparse signal recovery with Orthogonal Matching Pursuit',
             fontsize=16)
plt.show()
```
Sparse signal recovery with Orthogonal Matching Pursuit

18.23 Plot multi-class SGD on the iris dataset

Plot decision surface of multi-class SGD on iris dataset. The hyperplanes corresponding to the three one-versus-all (OVA) classifiers are represented by the dashed lines.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn.linear_model import SGDClassifier

# import some data to play with
iris = datasets.load_iris()

# we only take the first two features. We could
# avoid this ugly slicing by using a two-dim dataset
X = iris.data[:, :2]
y = iris.target
colors = "bry"

# shuffle
idx = np.arange(X.shape[0])
np.random.seed(13)
np.random.shuffle(idx)
X = X[idx]
y = y[idx]

# standardize
mean = X.mean(axis=0)
std = X.std(axis=0)
X = (X - mean) / std

h = .02  # step size in the mesh

c = SGDClassifier(alpha=0.001, max_iter=100).fit(X, y)

# create a mesh to plot in
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))

# Plot the decision boundary. For that, we will assign a color to each
# point in the mesh [x_min, x_max]x[y_min, y_max].
Z = c.predict(np.c_[xx.ravel(), yy.ravel()])
# Put the result into a color plot
Z = Z.reshape(xx.shape)
plt.contourf(xx, yy, Z, cmap=plt.cm.Paired)
plt.axis('tight')
# Plot also the training points
for i, color in zip(c.classes_, colors):
    idx = np.where(y == i)
    plt.scatter(X[idx, 0], X[idx, 1], c=color, label=iris.target_names[i],
                cmap=plt.cm.Paired, edgecolor='black', s=20)
plt.title("Decision surface of multi-class SGD")
plt.axis('tight')

# Plot the three one-against-all classifiers
xmin, xmax = plt.xlim()
ymin, ymax = plt.ylim()
coef = c.coef_
intercept = c.intercept_

def plot_hyperplane(c, color):
    def line(x0):
        return -(x0 * coef[c, 0]) - intercept[c] / coef[c, 1]
    plt.plot([xmin, xmax], [line(xmin), line(xmax)],
              ls="--", color=color)

for i, color in zip(c.classes_, colors):
    plot_hyperplane(i, color)
plt.legend()
plt.show()
We classify 8x8 images of digits into two classes: 0-4 against 5-9. The visualization shows coefficients of the models for varying C.

```
C=100.00
Sparsity with L1 penalty: 6.25%
Score with L1 penalty: 0.9098
Sparsity with L2 penalty: 4.69%
Score with L2 penalty: 0.9098

C=1.00
Sparsity with L1 penalty: 9.38%
Score with L1 penalty: 0.9093
Sparsity with L2 penalty: 4.69%
Score with L2 penalty: 0.9093

C=0.01
Sparsity with L1 penalty: 85.94%
Score with L1 penalty: 0.8631
Sparsity with L2 penalty: 4.69%
Score with L2 penalty: 0.8915
```
import numpy as np
import matplotlib.pyplot as plt

from sklearn.linear_model import LogisticRegression
from sklearn import datasets
from sklearn.preprocessing import StandardScaler

digits = datasets.load_digits()

X, y = digits.data, digits.target
X = StandardScaler().fit_transform(X)

# classify small against large digits
y = (y > 4).astype(np.int)

# Set regularization parameter
for i, C in enumerate((100, 1, 0.01)):
    # turn down tolerance for short training time
    clf_l1_LR = LogisticRegression(C=C, penalty='l1', tol=0.01)
    clf_l2_LR = LogisticRegression(C=C, penalty='l2', tol=0.01)
    clf_l1_LR.fit(X, y)
    clf_l2_LR.fit(X, y)

    coef_l1_LR = clf_l1_LR.coef_.ravel()
    coef_l2_LR = clf_l2_LR.coef_.ravel()

    # coef_l1_LR contains zeros due to the
    # L1 sparsity inducing norm
    sparsity_l1_LR = np.mean(coef_l1_LR == 0) * 100
    sparsity_l2_LR = np.mean(coef_l2_LR == 0) * 100
    print("C = %.2f" % C)
    print("Sparsity with L1 penalty: %.2f%%" % sparsity_l1_LR)
    print("score with L1 penalty: %.4f" % clf_l1_LR.score(X, y))
    print("Sparsity with L2 penalty: %.2f%%" % sparsity_l2_LR)
    print("score with L2 penalty: %.4f" % clf_l2_LR.score(X, y))

    l1_plot = plt.subplot(3, 2, 2 * i + 1)
    l2_plot = plt.subplot(3, 2, 2 * (i + 1))
    if i == 0:
        l1_plot.set_title("L1 penalty")
        l2_plot.set_title("L2 penalty")
    l1_plot.imshow(np.abs(coef_l1_LR.reshape(8, 8)), interpolation='nearest',
                   cmap='binary', vmax=1, vmin=0)
    l2_plot.imshow(np.abs(coef_l2_LR.reshape(8, 8)), interpolation='nearest',
                   cmap='binary', vmax=1, vmin=0)
    plt.text(-8, 3, "C = %.2f" % C)
18.25 Theil-Sen Regression

Computes a Theil-Sen Regression on a synthetic dataset.

See *Theil-Sen estimator: generalized-median-based estimator* for more information on the regressor.

Compared to the OLS (ordinary least squares) estimator, the Theil-Sen estimator is robust against outliers. It has a breakdown point of about 29.3% in case of a simple linear regression which means that it can tolerate arbitrary corrupted data (outliers) of up to 29.3% in the two-dimensional case.

The estimation of the model is done by calculating the slopes and intercepts of a subpopulation of all possible combinations of $p$ subsample points. If an intercept is fitted, $p$ must be greater than or equal to $n_{\text{features}} + 1$. The final slope and intercept is then defined as the spatial median of these slopes and intercepts.

In certain cases Theil-Sen performs better than *RANSAC* which is also a robust method. This is illustrated in the second example below where outliers with respect to the $x$-axis perturb RANSAC. Tuning the `residual_threshold` parameter of RANSAC remedies this but in general a priori knowledge about the data and the nature of the outliers is needed. Due to the computational complexity of Theil-Sen it is recommended to use it only for small problems in terms of number of samples and features. For larger problems the `max_subpopulation` parameter restricts the magnitude of all possible combinations of $p$ subsample points to a randomly chosen subset and therefore also limits the runtime. Therefore, Theil-Sen is applicable to larger problems with the drawback of losing some of its mathematical properties since it then works on a random subset.
```python
import time
import numpy as np
import matplotlib.pyplot as plt
from sklearn.linear_model import LinearRegression, TheilSenRegressor
from sklearn.linear_model import RANSACRegressor

print(__doc__)

estimators = [('OLS', LinearRegression()),
               ('Theil-Sen', TheilSenRegressor(random_state=42)),
               ('RANSAC', RANSACRegressor(random_state=42)),
               ]

colors = {'OLS': 'turquoise', 'Theil-Sen': 'gold', 'RANSAC': 'lightgreen'}
lw = 2

def generate_data(n_samples=200):
    # Linear model y = 3*x + N(2, 0.1**2)
    x = np.random.randn(n_samples)
    w = 3.
    c = 2.
    noise = 0.1 * np.random.randn(n_samples)
    y = w * x + c + noise
    # 10% outliers
    y[-20:] += -20 * x[-20:]
    return x, y

X, y = generate_data()

plt.scatter(X, y, color='indigo', marker='x', s=40)
line_x = np.array([-3, 3])
for name, estimator in estimators:
    t0 = time.time()
    estimator.fit(X, y)
    elapsed_time = time.time() - t0
    y_pred = estimator.predict(line_x.reshape(2, 1))
    plt.plot(line_x, y_pred, color=colors[name], linewidth=lw,
             label='{} (fit time: {:.2f}s)'.format(name, elapsed_time))
plt.axis('tight')
```

---

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Outliers in the X direction

```python
np.random.seed(0)
# Linear model y = 3*x + N(2, 0.1**2)
x = np.random.randn(n_samples)
noise = 0.1 * np.random.randn(n_samples)
y = 3 * x + 2 + noise
# 10% outliers
x[-20:] = 9.9
y[-20:] += 22
X = x[:, np.newaxis]
```

```python
plt.figure()
plt.scatter(x, y, color='indigo', marker='x', s=40)
```

```python
line_x = np.array([-3, 10])
for name, estimator in estimators:
    t0 = time.time()
    estimator.fit(X, y)
    elapsed_time = time.time() - t0
    y_pred = estimator.predict(line_x.reshape(2, 1))
    plt.plot(line_x, y_pred, color=colors[name], linewidth=lw,
             label='{} (fit time: {:.2f}s)'.format(name, elapsed_time))
```

```python
plt.axis('tight')
plt.legend(loc='upper left')
plt.title("Corrupt x")
plt.show()
```

Total running time of the script: ( 0 minutes 1.629 seconds)

## 18.26 Plot multinomial and One-vs-Rest Logistic Regression

Plot decision surface of multinomial and One-vs-Rest Logistic Regression. The hyperplanes corresponding to the three One-vs-Rest (OVR) classifiers are represented by the dashed lines.
training score : 0.995 (multinomial)
training score : 0.976 (ovr)
Z = Z.reshape(xx.shape)
plt.figure()
plt.contourf(xx, yy, Z, cmap=plt.cm.Paired)
plt.title("Decision surface of LogisticRegression (%s)" % multi_class)
plt.axis('tight')

# Plot also the training points
colors = "bry"
for i, color in zip(clf.classes_, colors):
    idx = np.where(y == i)
    plt.scatter(X[idx, 0], X[idx, 1], c=color, cmap=plt.cm.Paired,
                edgecolor='black', s=20)

# Plot the three one-against-all classifiers
xmin, xmax = plt.xlim()
ymin, ymax = plt.ylim()
coef = clf.coef_
intercept = clf.intercept_

def plot_hyperplane(c, color):
    def line(x0):
        return (-x0 * coef[c, 0] - intercept[c]) / coef[c, 1]
    plt.plot([xmin, xmax], [line(xmin), line(xmax)],
             ls="--", color=color)

for i, color in zip(clf.classes_, colors):
    plot_hyperplane(i, color)

plt.show()

Total running time of the script: ( 0 minutes 0.368 seconds)

18.27 Robust linear estimator fitting

Here a sine function is fit with a polynomial of order 3, for values close to zero.

Robust fitting is demoed in different situations:

- No measurement errors, only modelling errors (fitting a sine with a polynomial)
- Measurement errors in X
- Measurement errors in y

The median absolute deviation to non corrupt new data is used to judge the quality of the prediction.

What we can see that:

- RANSAC is good for strong outliers in the y direction
- TheilSen is good for small outliers, both in direction X and y, but has a break point above which it performs worse than OLS.
- The scores of HuberRegressor may not be compared directly to both TheilSen and RANSAC because it does not attempt to completely filter the outliers but lessen their effect.
```python
from matplotlib import pyplot as plt
import numpy as np
import matplotlib.pyplot as plt

import numpy as np
from sklearn.linear_model import (LinearRegression, TheilSenRegressor, RANSACRegressor, HuberRegressor)
from sklearn.metrics import mean_squared_error
from sklearn.preprocessing import PolynomialFeatures
from sklearn.pipeline import make_pipeline

np.random.seed(42)
X = np.random.normal(size=400)
y = np.sin(X)
# Make sure that it X is 2D
X = X[:, np.newaxis]

X_test = np.random.normal(size=200)
y_test = np.sin(X_test)
X_test = X_test[:, np.newaxis]

y_errors = y.copy()
y_errors[::3] = 3

X_errors = X.copy()
X_errors[::3] = 3

y_errors_large = y.copy()
y_errors_large[::3] = 10

X_errors_large = X.copy()
X_errors_large[::3] = 10

estimators = [('OLS', LinearRegression()),
              ('Theil-Sen', TheilSenRegressor(random_state=42)),
              ('RANSAC', RANSACRegressor(random_state=42)),
              ('HuberRegressor', HuberRegressor())]

# Plot

x_plot = np.linspace(X.min(), X.max())

for title, this_X, this_y in [("Modeling Errors Only", X, y),
                               ('Corrupt X, Small Deviants', X_errors, y),
                               ('Corrupt y, Large Deviants', this_X, this_y),
                               ('Corrupt X, Large Deviants', X_errors_large, y)]:
    plt.plot(x_plot, this_Y, color=colors[estimator], linestyle=linestyle[estimator], label=estimator)
```

**18.27. Robust linear estimator fitting**
('Corrupt y, Small Deviants', X, y_errors),
('Corrupt y, Large Deviants', X, y_errors_large):

plt.figure(figsize=(5, 4))
plt.plot(this_X[:, 0], this_y, 'b+')

for name, estimator in estimators:
    model = make_pipeline(PolynomialFeatures(3), estimator)
    model.fit(this_X, this_y)
    mse = mean_squared_error(model.predict(X_test), y_test)
    y_plot = model.predict(x_plot[:, np.newaxis])
    plt.plot(x_plot, y_plot, color=colors[name], linestyle=linestyle[name],
              linewidth=lw, label='\%s: error = %.3f' % (name, mse))

legend_title = 'Error of Mean
Absolute Deviation
into Non-corrupt Data'
legend = plt.legend(loc='upper right', frameon=False, title=legend_title,
                     prop=dict(size='x-small'))
plt.xlim(-4, 10.2)
plt.ylim(-2, 10.2)
plt.title(title)
plt.show()
Out:

Computing regularization path using the lasso...
Computing regularization path using the positive lasso...
Computing regularization path using the elastic net...
Computing regularization path using the positive elastic net...

```python
print(__doc__)

# Author: Alexandre Gramfort <alexandre.gramfort@inria.fr>
# License: BSD 3 clause

from itertools import cycle
import numpy as np
import matplotlib.pyplot as plt

from sklearn.linear_model import lasso_path, enet_path
from sklearn import datasets

diabetes = datasets.load_diabetes()
X = diabetes.data
y = diabetes.target
```
X /= X.std(axis=0)  # Standardize data (easier to set the l1_ratio parameter)

# Compute paths

eps = 5e-3  # the smaller it is the longer is the path

print("Computing regularization path using the lasso...")
alphas_lasso, coefs_lasso, _ = lasso_path(X, y, eps, fit_intercept=False)

print("Computing regularization path using the positive lasso...")
alphas_positive_lasso, coefs_positive_lasso, _ = lasso_path(X, y, eps, positive=True, fit_intercept=False)

print("Computing regularization path using the elastic net...")
alphas_enet, coefs_enet, _ = enet_path(X, y, eps=eps, l1_ratio=0.8, fit_intercept=False)

print("Computing regularization path using the positive elastic net...")
alphas_positive_enet, coefs_positive_enet, _ = enet_path(X, y, eps=eps, l1_ratio=0.8, positive=True, fit_intercept=False)

# Display results

plt.figure(1)
colors = cycle(['b', 'r', 'g', 'c', 'k'])
neg_log_alphas_lasso = -np.log10(alphas_lasso)
neg_log_alphas_enet = -np.log10(alphas_enet)
for coef_l, coef_e, c in zip(coefs_lasso, coefs_enet, colors):
    l1 = plt.plot(neg_log_alphas_lasso, coef_l, c=c)
    l2 = plt.plot(neg_log_alphas_enet, coef_e, linestyle='--', c=c)
plt.xlabel('-Log(alpha)')
plt.ylabel('coefficients')
plt.title('Lasso and Elastic-Net Paths')
plt.legend((l1[-1], l2[-1]), ('Lasso', 'Elastic-Net'), loc='lower left')
plt.axis('tight')

plt.figure(2)
neg_log_alphas_positive_lasso = -np.log10(alphas_positive_lasso)
for coef_l, coef_pl, c in zip(coefs_lasso, coefs_positive_lasso, colors):
    l1 = plt.plot(neg_log_alphas_lasso, coef_l, c=c)
    l2 = plt.plot(neg_log_alphas_positive_lasso, coef_pl, linestyle='--', c=c)
plt.xlabel('-Log(alpha)')
plt.ylabel('coefficients')
plt.title('Lasso and positive Lasso')
plt.legend((l1[-1], l2[-1]), ('Lasso', 'positive Lasso'), loc='lower left')
plt.axis('tight')

plt.figure(3)
neg_log_alphas_positive_enet = -np.log10(alphas_positive_enet)
for (coef_e, coef_pe, c) in zip(coefs_enet, coefs_positive_enet, colors):
    l1 = plt.plot(neg_log_alphas_enet, coef_e, c=c)
    l2 = plt.plot(neg_log_alphas_positive_enet, coef_pe, linestyle='--', c=c)
plt.xlabel('-Log(alpha)')
plt.ylabel('coefficients')
plt.title('Elastic-Net and positive Elastic-Net')
plt.legend((l1[-1], l2[-1]), ('Elastic-Net', 'positive Elastic-Net'),
 loc='lower left')
plt.axis('tight')
plt.show()

**Total running time of the script:** ( 0 minutes 0.357 seconds)

### 18.29 Automatic Relevance Determination Regression (ARD)

Fit regression model with Bayesian Ridge Regression.

See *Bayesian Ridge Regression* for more information on the regressor.

Compared to the OLS (ordinary least squares) estimator, the coefficient weights are slightly shifted toward zeros, which stabilises them.

The histogram of the estimated weights is very peaked, as a sparsity-inducing prior is implied on the weights.

The estimation of the model is done by iteratively maximizing the marginal log-likelihood of the observations.

We also plot predictions and uncertainties for ARD for one dimensional regression using polynomial feature expansion. Note the uncertainty starts going up on the right side of the plot. This is because these test samples are outside of the range of the training samples.
import numpy as np
import matplotlib.pyplot as plt
from scipy import stats
from sklearn.linear_model import ARDRegression, LinearRegression

# Parameters of the example
np.random.seed(0)
n_samples, n_features = 100, 100
# Create Gaussian data
X = np.random.randn(n_samples, n_features)
# Create weights with a precision lambda_ of 4.
lambda_ = 4.
w = np.zeros(n_features)
# Only keep 10 weights of interest
relevant_features = np.random.randint(0, n_features, 10)
for i in relevant_features:
    w[i] = stats.norm.rvs(loc=0, scale=1. / np.sqrt(lambda_))
# Create noise with a precision alpha of 50.
alpha_ = 50.
noise = stats.norm.rvs(loc=0, scale=1. / np.sqrt(alpha_), size=n_samples)
# Create the target
y = np.dot(X, w) + noise

# Fit the ARD Regression
clf = ARDRegression(compute_score=True)
clf.fit(X, y)

ols = LinearRegression()
ols.fit(X, y)

# Plot the true weights, the estimated weights, the histogram of the weights, and predictions with standard deviations
plt.figure(figsize=(6, 5))
plt.title("Weights of the model")
plt.plot(clf.coef_, color='darkblue', linestyle='-', linewidth=2,
         label="ARD estimate")
plt.plot(ols.coef_, color='yellowgreen', linestyle=':', linewidth=2,
         label="OLS estimate")
plt.plot(w, color='orange', linestyle='-', linewidth=2, label="Ground truth")
plt.xlabel("Features")
plt.ylabel("Values of the weights")
plt.legend(loc=1)

plt.figure(figsize=(6, 5))
plt.title("Histogram of the weights")
plt.hist(clf.coef_, bins=n_features, color='navy', log=True)
plt.scatter(clf.coef_[relevant_features], 5 * np.ones(len(relevant_features)),
            color='gold', marker='o', label="Relevant features")
plt.ylabel("Features")
plt.xlabel("Values of the weights")
plt.legend(loc=1)

plt.figure(figsize=(6, 5))
plt.title("Marginal log-likelihood")
plt.plot(clf.scores_, color='navy', linewidth=2)
plt.ylabel("Score")
plt.xlabel("Iterations")

# Plotting some predictions for polynomial regression

def f(x, noise_amount):
    y = np.sqrt(x) * np.sin(x)
    noise = np.random.normal(0, 1, len(x))
    return y + noise_amount * noise

define degree
X = np.linspace(0, 10, 100)
y = f(X, noise_amount=1)
clf_poly = ARDRegression(threshold_lambda=1e5)
clf_poly.fit(np.vander(X, degree), y)

X_plot = np.linspace(0, 11, 25)
y_plot = f(X_plot, noise_amount=0)
y_mean, y_std = clf_poly.predict(np.vander(X_plot, degree), return_std=True)

plt.figure(figsize=(6, 5))
Computes a Bayesian Ridge Regression on a synthetic dataset.

See Bayesian Ridge Regression for more information on the regressor.

Compared to the OLS (ordinary least squares) estimator, the coefficient weights are slightly shifted toward zeros, which stabilises them.

As the prior on the weights is a Gaussian prior, the histogram of the estimated weights is Gaussian.

The estimation of the model is done by iteratively maximizing the marginal log-likelihood of the observations.

We also plot predictions and uncertainties for Bayesian Ridge Regression for one dimensional regression using polynomial feature expansion. Note the uncertainty starts going up on the right side of the plot. This is because these test samples are outside of the range of the training samples.
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from scipy import stats

from sklearn.linear_model import BayesianRidge, LinearRegression

# Generating simulated data with Gaussian weights
np.random.seed(0)
n_samples, n_features = 100, 100
X = np.random.randn(n_samples, n_features)  # Create Gaussian data

# Create weights with a precision lambda_ of 4.
lambda_ = 4.
w = np.zeros(n_features)

# Only keep 10 weights of interest
relevant_features = np.random.randint(0, n_features, 10)
for i in relevant_features:
    w[i] = stats.norm.rvs(loc=0, scale=1. / np.sqrt(lambda_))

# Create noise with a precision alpha of 50.
alpha_ = 50.
noise = stats.norm.rvs(loc=0, scale=1. / np.sqrt(alpha_), size=n_samples)

# Create the target
y = np.dot(X, w) + noise

# #############################################################################
# Fit the Bayesian Ridge Regression and an OLS for comparison
clf = BayesianRidge(compute_score=True)
clf.fit(X, y)

ols = LinearRegression()
ols.fit(X, y)

# #############################################################################
# Plot true weights, estimated weights, histogram of the weights, and 
# predictions with standard deviations
lw = 2
plt.figure(figsize=(6, 5))
plt.title("Weights of the model")
plt.plot(clf.coef_, color='lightgreen', linewidth=lw,
         label="Bayesian Ridge estimate")
plt.plot(w, color='gold', linewidth=lw, label="Ground truth")
plt.plot(ols.coef_, color='navy', linestyle='--', label="OLS estimate")
plt.xlabel("Features")
plt.ylabel("Values of the weights")
plt.legend(loc="best", prop=dict(size=12))

plt.figure(figsize=(6, 5))
plt.title("Histogram of the weights")
plt.hist(clf.coef_, bins=n_features, color='gold', log=True,
         edgecolor='black')
plt.scatter(clf.coef_[relevant_features], 5 * np.ones(len(relevant_features)),
            color='navy', label="Relevant features")
plt.xlabel("Values of the weights")
plt.legend(loc="upper left")

plt.figure(figsize=(6, 5))
plt.title("Marginal log-likelihood")
plt.plot(clf.scores_, color='navy', linewidth=lw)
plt.ylabel("Score")
plt.xlabel("Iterations")

# Plotting some predictions for polynomial regression

def f(x, noise_amount):
    y = np.sqrt(x) * np.sin(x)

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noise = np.random.normal(0, 1, len(x))
return y + noise_amount * noise

degree = 10
X = np.linspace(0, 10, 100)
y = f(X, noise_amount=0.1)
clf_poly = BayesianRidge()
clf_poly.fit(np.vander(X, degree), y)

X_plot = np.linspace(0, 11, 25)
y_plot = f(X_plot, noise_amount=0)
y_mean, y_std = clf_poly.predict(np.vander(X_plot, degree), return_std=True)
plt.figure(figsize=(6, 5))
plt.errorbar(X_plot, y_mean, y_std, color='navy',
            label="Polynomial Bayesian Ridge Regression", linewidth=lw)
plt.plot(X_plot, y_plot, color='gold', linewidth=lw,
         label="Ground Truth")
plt.ylabel("Output y")
plt.xlabel("Feature X")
plt.legend(loc="lower left")
plt.show()

Total running time of the script: ( 0 minutes 0.340 seconds)

18.31 Lasso model selection: Cross-Validation / AIC / BIC

Use the Akaike information criterion (AIC), the Bayes Information criterion (BIC) and cross-validation to select an optimal value of the regularization parameter alpha of the Lasso estimator.

Results obtained with LassoLarsIC are based on AIC/BIC criteria.

Information-criterion based model selection is very fast, but it relies on a proper estimation of degrees of freedom, are derived for large samples (asymptotic results) and assume the model is correct, i.e. that the data are actually generated by this model. They also tend to break when the problem is badly conditioned (more features than samples).

For cross-validation, we use 20-fold with 2 algorithms to compute the Lasso path: coordinate descent, as implemented by the LassoCV class, and Lars (least angle regression) as implemented by the LassoLarsCV class. Both algorithms give roughly the same results. They differ with regards to their execution speed and sources of numerical errors.

Lars computes a path solution only for each kink in the path. As a result, it is very efficient when there are only of few kinks, which is the case if there are few features or samples. Also, it is able to compute the full path without setting any meta parameter. On the opposite, coordinate descent compute the path points on a pre-specified grid (here we use the default). Thus it is more efficient if the number of grid points is smaller than the number of kinks in the path. Such a strategy can be interesting if the number of features is really large and there are enough samples to select a large amount. In terms of numerical errors, for heavily correlated variables, Lars will accumulate more errors, while the coordinate descent algorithm will only sample the path on a grid.

Note how the optimal value of alpha varies for each fold. This illustrates why nested-cross validation is necessary when trying to evaluate the performance of a method for which a parameter is chosen by cross-validation: this choice of parameter may not be optimal for unseen data.
Out:

```
Computing regularization path using the coordinate descent lasso...
Computing regularization path using the Lars lasso...
```

```python
print(__doc__)
```
import time
import numpy as np
import matplotlib.pyplot as plt

from sklearn.linear_model import LassoCV, LassoLarsCV, LassoLarsIC
from sklearn import datasets

diabetes = datasets.load_diabetes()
X = diabetes.data
y = diabetes.target

rng = np.random.RandomState(42)
X = np.c_[X, rng.randn(X.shape[0], 14)]  # add some bad features

# normalize data as done by Lars to allow for comparison
X /= np.sqrt(np.sum(X ** 2, axis=0))

# LassoLarsIC: least angle regression with BIC/AIC criterion
model_bic = LassoLarsIC(criterion='bic')
t1 = time.time()
model_bic.fit(X, y)
t_bic = time.time() - t1
alpha_bic_ = model_bic.alpha_

model_aic = LassoLarsIC(criterion='aic')
model_aic.fit(X, y)
alpha_aic_ = model_aic.alpha_

def plot_ic_criterion(model, name, color):
    alpha_ = model.alpha_
    alphas_ = model.alphas_
    criterion_ = model.criterion_
    plt.plot(-np.log10(alphas_), criterion_, '--', color=color,
             linewidth=3, label='{} criterion'.format(name))
    plt.axvline(-np.log10(alpha_), color=color, linewidth=3,
                label='alpha: estimate')
    plt.xlabel('-log(alpha)')
    plt.ylabel('criterion')

plt.figure()
plot_ic_criterion(model_aic, 'AIC', 'b')
plot_ic_criterion(model_bic, 'BIC', 'r')
plt.legend()
plt.title('Information-criterion for model selection (training time %.3fs)' % t_bic)

# LassoCV: coordinate descent

# We want to select the tuning parameter that minimizes cross-validation error
print("Computing regularization path using the coordinate descent lasso...")
```python
t1 = time.time()
model = LassoCV(cv=20).fit(X, y)
t_lasso_cv = time.time() - t1

# Display results
m_log_alphas = -np.log10(model.alphas_)

plt.figure()
ymin, ymax = 2300, 3800
plt.plot(m_log_alphas, model.mse_path_, ':')
plt.plot(m_log_alphas, model.mse_path_.mean(axis=-1), 'k',
         label='Average across the folds', linewidth=2)
plt.axvline(-np.log10(model.alpha_), linestyle='--', color='k',
         label='alpha: CV estimate')
plt.legend()
plt.xlabel('-log(alpha)')
plt.ylabel('Mean square error')
plt.title('Mean square error on each fold: coordinate descent ' +
          '(train time: %.2fs)' % t_lasso_cv)
plt.axis('tight')
plt.ylim(ymin, ymax)
plt.show()
```

```
# Compute paths
print("Computing regularization path using the Lars lasso...")
t1 = time.time()
model = LassoLarsCV(cv=20).fit(X, y)
t_lasso_lars_cv = time.time() - t1

# Display results
m_log_alphas = -np.log10(model.cv_alphas_)

plt.figure()
plt.plot(m_log_alphas, model.mse_path_, ':')
plt.plot(m_log_alphas, model.mse_path_.mean(axis=-1), 'k',
         label='Average across the folds', linewidth=2)
plt.axvline(-np.log10(model.alpha_), linestyle='--', color='k',
         label='alpha CV')
plt.legend()
plt.xlabel('-log(alpha)')
plt.ylabel('Mean square error')
plt.title('Mean square error on each fold: Lars (train time: %.2fs)' %
          t_lasso_lars_cv)
plt.axis('tight')
plt.ylim(ymin, ymax)
plt.show()
```

**Total running time of the script:** ( 0 minutes 1.130 seconds)
18.32 Multiclass sparse logistic regression on newsgroups20

Comparison of multinomial logistic L1 vs one-versus-rest L1 logistic regression to classify documents from the newsgroups20 dataset. Multinomial logistic regression yields more accurate results and is faster to train on the larger scale dataset.

Here we use the L1 sparsity that trims the weights of not informative features to zero. This is good if the goal is to extract the strongly discriminative vocabulary of each class. If the goal is to get the best predictive accuracy, it is better to use the non sparsity-inducing L2 penalty instead.

A more traditional (and possibly better) way to predict on a sparse subset of input features would be to use univariate feature selection followed by a traditional (L2-penalised) logistic regression model.

Out:

Dataset 20newsgroup, train_samples=9000, n_features=130107, n_classes=20
[model=One versus Rest, solver=saga] Number of epochs: 1
[model=One versus Rest, solver=saga] Number of epochs: 3
Test accuracy for model ovr: 0.7410
% non-zero coefficients for model ovr, per class:
[ 0.27054655  0.66330021  0.80395367  0.73247404  0.67713497  0.73477984
  0.40889422  0.48959702  1.01301237  0.56261385  0.60104376  0.332803
  0.7094161  0.85083816  0.56876263  0.65715142  0.64408525  0.81163965
  0.44271254  0.41120001]
Run time (3 epochs) for model ovr: 3.38
[model=Multinomial, solver=saga] Number of epochs: 1
[model=Multinomial, solver=saga] Number of epochs: 3
[model=Multinomial, solver=saga] Number of epochs: 7
Test accuracy for model multinomial: 0.7450
% non-zero coefficients for model multinomial, per class:
  [ 0.13296748 0.11759552 0.13296748 0.13988486 0.12681870 0.16140561
    0.15218243 0.09069458 0.07762841 0.12143851 0.14910804 0.10837234
    0.1883655 0.12451290 0.16832300 0.21828188 0.11605832 0.07839701
    0.06917383 0.15602543]
Run time (7 epochs) for model multinomial: 3.09
Example run in 11.000 s

import time
import matplotlib.pyplot as plt
import numpy as np
from sklearn.datasets import fetch_20newsgroups_vectorized
from sklearn.linear_model import LogisticRegression
from sklearn.model_selection import train_test_split

print(__doc__)
# Author: Arthur Mensch
t0 = time.clock()

# We use SAGA solver
solver = 'saga'

# Turn down for faster run time
n_samples = 10000

# Memorized fetch_rcv1 for faster access
dataset = fetch_20newsgroups_vectorized('all')
X = dataset.data
y = dataset.target
X = X[:n_samples]
y = y[:n_samples]

X_train, X_test, y_train, y_test = train_test_split(X, y,
random_state=42,
stratify=y,
test_size=0.1)

train_samples, n_features = X_train.shape
n_classes = np.unique(y).shape[0]

print('Dataset 20newsgroup, train_samples=%i, n_features=%i, n_classes=%i'
    % (train_samples, n_features, n_classes))

models = {'ovr': {'name': 'One versus Rest', 'iters': [1, 3]},
          'multinomial': {'name': 'Multinomial', 'iters': [1, 3, 7]}}

for model in models:
    # Add initial chance-level values for plotting purpose
accuracies = [1 / n_classes]
times = [0]
densities = [1]

model_params = models[model]

# Small number of epochs for fast runtime
for this_max_iter in model_params['iters']:
    print('model=%s, solver=%s] Number of epochs: %s' %
          (model_params['name'], solver, this_max_iter))
    lr = LogisticRegression(solver=solver,
                            multi_class=model,
                            C=1,
                            penalty='l1',
                            fit_intercept=True,
                            max_iter=this_max_iter,
                            random_state=42,
                        )
    t1 = time.clock()
    lr.fit(X_train, y_train)
    train_time = time.clock() - t1
    y_pred = lr.predict(X_test)
    accuracy = np.sum(y_pred == y_test) / y_test.shape[0]
    density = np.mean(lr.coef_ != 0, axis=1) * 100
    accuracies.append(accuracy)
    densities.append(density)
    times.append(train_time)
models[model]['times'] = times
models[model]['densities'] = densities
models[model]['accuracies'] = accuracies
print('Test accuracy for model %s: %.4f' % (model, accuracies[-1]))
print('%% non-zero coefficients for model %s, ' % (model, densities[-1]))
print('Run time (%i epochs) for model %s: ' % (model_params['iters'][-1], model, times[-1]))

fig = plt.figure()
ax = fig.add_subplot(111)
for model in models:
    name = models[model]['name']
    times = models[model]['times']
    accuracies = models[model]['accuracies']
    ax.plot(times, accuracies, marker='o', label='Model: %s' % name)
    ax.set_xlabel('Train time (s)')
    ax.set_ylabel('Test accuracy')
    ax.legend()
fig.suptitle('Multinomial vs One-vs-Rest Logistic L1
Dataset %s' % '20newsgroups')
fig.tight_layout()
fig.subplots_adjust(top=0.85)
run_time = time.clock() - t0
print('Example run in %.3f s' % run_time)
plt.show()
Examples concerning the `sklearn.manifold` module.

### 19.1 Swiss Roll reduction with LLE

An illustration of Swiss Roll reduction with locally linear embedding

```
Computing LLE embedding
Done. Reconstruction error: 7.32744e-08
```
# Author: Fabian Pedregosa -- <fabian.pedregosa@inria.fr>
# License: BSD 3 clause (C) INRIA 2011

print(_doc_)

import matplotlib.pyplot as plt
# This import is needed to modify the way figure behaves
from mpl_toolkits.mplot3d import Axes3D
# Locally linear embedding of the swiss roll
from sklearn import manifold, datasets
X, color = datasets.samples_generator.make_swiss_roll(n_samples=1500)

print("Computing LLE embedding")
X_r, err = manifold.locally_linear_embedding(X, n_neighbors=12,
                                           n_components=2)
print("Done. Reconstruction error: \$g" % err)

# Plot result
fig = plt.figure()
ax = fig.add_subplot(211, projection='3d')
ax.scatter(X[:, 0], X[:, 1], X[:, 2], c=color, cmap=plt.cm.Spectral)
ax.set_title("Original data")
ax = fig.add_subplot(212)
ax.scatter(X_r[:, 0], X_r[:, 1], c=color, cmap=plt.cm.Spectral)
plt.axis('tight')
plt.xticks([]), plt.yticks([])
plt.title('Projected data')
plt.show()

Total running time of the script: ( 0 minutes 0.456 seconds)

19.2 Multi-dimensional scaling

An illustration of the metric and non-metric MDS on generated noisy data.
The reconstructed points using the metric MDS and non metric MDS are slightly shifted to avoid overlapping.
print(__doc__)
import numpy as np
from matplotlib import pyplot as plt
from matplotlib.collections import LineCollection
from sklearn import manifold
from sklearn.metrics import euclidean_distances
from sklearn.decomposition import PCA

n_samples = 20
seed = np.random.RandomState(seed=3)
X_true = seed.randint(0, 20, 2 * n_samples).astype(np.float)
X_true = X_true.reshape((n_samples, 2))
# Center the data
X_true -= X_true.mean()
similarities = euclidean_distances(X_true)
# Add noise to the similarities
noise = np.random.rand(n_samples, n_samples) + noise.T
noise[np.arange(noise.shape[0]), np.arange(noise.shape[0])] = 0

# Author: Nelle Varoquaux <nelle.varoquaux@gmail.com>
# License: BSD

19.2. Multi-dimensional scaling
similarities += noise

mds = manifold.MDS(n_components=2, max_iter=3000, eps=1e-9, random_state=seed,
                   dissimilarity="precomputed", n_jobs=1)
pos = mds.fit(similarities).embedding_

nm = manifold.MDS(n_components=2, metric=False, max_iter=3000, eps=1e-12,
                  dissimilarity="precomputed", random_state=seed, n_jobs=1,
                  n_init=1)
npos = nm.fit_transform(similarities, init=pos)

# Rescale the data
pos *= np.sqrt((X_true ** 2).sum()) / np.sqrt((pos ** 2).sum())
npos *= np.sqrt((X_true ** 2).sum()) / np.sqrt((npos ** 2).sum())

# Rotate the data
clf = PCA(n_components=2)
X_true = clf.fit_transform(X_true)
pos = clf.fit_transform(pos)
npos = clf.fit_transform(npos)

fig = plt.figure(1)
ax = plt.axes([0., 0., 1., 1.])
s = 100
plt.scatter(X_true[:, 0], X_true[:, 1], color='navy', s=s, lw=0,
           label='True Position')
plt.scatter(pos[:, 0], pos[:, 1], color='turquoise', s=s, lw=0, label='MDS')
plt.scatter(npos[:, 0], npos[:, 1], color='darkorange', s=s, lw=0, label='NMDS')
plt.legend(scatterpoints=1, loc='best', shadow=False)
similarities = similarities.max() / similarities * 100
similarities[np.isinf(similarities)] = 0

# Plot the edges
start_idx, end_idx = np.where(pos)
# a sequence of (*line0*, *line1*, *line2*), where:
# linen = (x0, y0), (x1, y1), ... (xm, ym)
segments = [[X_true[i, :], X_true[j, :]]
    for i in range(len(pos)) for j in range(len(pos))]
values = np.abs(similarities)
lc = LineCollection(segments,
                    zorder=0, cmap=plt.cm.Blues,
                    norm=plt.Normalize(0, values.max()))
lc.set_array(similarities.flatten())
lc.set_linewidths(0.5 * np.ones(len(segments)))
ax.add_collection(lc)

plt.show()
An illustration of dimensionality reduction on the S-curve dataset with various manifold learning methods.

For a discussion and comparison of these algorithms, see the manifold module page

For a similar example, where the methods are applied to a sphere dataset, see Manifold Learning methods on a severed sphere

Note that the purpose of the MDS is to find a low-dimensional representation of the data (here 2D) in which the distances respect well the distances in the original high-dimensional space, unlike other manifold-learning algorithms, it does not seeks an isotropic representation of the data in the low-dimensional space.

Out:

```python
standard: 0.22 sec
ltsa: 0.39 sec
hessian: 0.55 sec
modified: 0.46 sec
Isomap: 0.49 sec
MDS: 2.2 sec
SpectralEmbedding: 0.27 sec
t-SNE: 19 sec
```

```python
# Author: Jake Vanderplas -- <vanderplas@astro.washington.edu>

print(__doc__)

from time import time
```
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from matplotlib.ticker import NullFormatter

from sklearn import manifold, datasets

# Next line to silence pyflakes. This import is needed.
Axes3D

n_points = 1000
X, color = datasets.samples_generator.make_s_curve(n_points, random_state=0)
n_neighbors = 10
n_components = 2

fig = plt.figure(figsize=(15, 8))
fig.suptitle("Manifold Learning with %i points, %i neighbors" % (1000, n_neighbors), fontsize=14)

ax = fig.add_subplot(251, projection='3d')
akax.scatter(X[:, 0], X[:, 1], X[:, 2], c=color, cmap=plt.cm.Spectral)
akax.view_init(4, -72)

methods = ['standard', 'ltsa', 'hessian', 'modified']
labels = ['LLE', 'LTSA', 'Hessian LLE', 'Modified LLE']

for i, method in enumerate(methods):
t0 = time()
Y = manifold.LocallyLinearEmbedding(n_neighbors, n_components,
eigen_solver='auto',
method=method).fit_transform(X)
t1 = time()
print("%s: %.2g sec" % (methods[i], t1 - t0))

ax = fig.add_subplot(252 + i)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("%s (%.2g sec)" % (labels[i], t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

ax = fig.add_subplot(256)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("Isomap (%.2g sec)" % (t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

ax = fig.add_subplot(257)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("Isomap (%.2g sec)" % (t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

ax = fig.add_subplot(258)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("Isomap (%.2g sec)" % (t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

ax = fig.add_subplot(259)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("Isomap (%.2g sec)" % (t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

ax = fig.add_subplot(2510)
plt.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.Spectral)
plt.title("Isomap (%.2g sec)" % (t1 - t0))
ax.xaxis.set_major_formatter(NullFormatter())
akax.yaxis.set_major_formatter(NullFormatter())
akax.axis('tight')

print("MDS: %.2g sec" % (t1 - t0))
19.4 t-SNE: The effect of various perplexity values on the shape

An illustration of t-SNE on the two concentric circles and the S-curve datasets for different perplexity values.

We observe a tendency towards clearer shapes as the preplexity value increases.

The size, the distance and the shape of clusters may vary upon initialization, perplexity values and does not always convey a meaning.

As shown below, t-SNE for higher perplexities finds meaningful topology of two concentric circles, however the size and the distance of the circles varies slightly from the original. Contrary to the two circles dataset, the shapes visually diverge from S-curve topology on the S-curve dataset even for larger perplexity values.

For further details, “How to Use t-SNE Effectively” http://distill.pub/2016/misread-tsne/ provides a good discussion of the effects of various parameters, as well as interactive plots to explore those effects.
Out:

circles, perplexity=5 in 2 sec
circles, perplexity=30 in 4.3 sec
circles, perplexity=50 in 6.2 sec
circles, perplexity=100 in 6.9 sec
S-curve, perplexity=5 in 2.1 sec
S-curve, perplexity=30 in 4.3 sec
S-curve, perplexity=50 in 5.4 sec
S-curve, perplexity=100 in 7 sec
uniform grid, perplexity=5 in 2 sec
uniform grid, perplexity=30 in 4.3 sec
uniform grid, perplexity=50 in 6.2 sec
uniform grid, perplexity=100 in 8.6 sec

# Author: Narine Kokhlikyan <narine@slice.com>
# License: BSD

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from matplotlib.ticker import NullFormatter
from sklearn import manifold, datasets
from time import time

n_samples = 300
n_components = 2
(fig, subplots) = plt.subplots(3, 5, figsize=(15, 8))
perplexities = [5, 30, 50, 100]
X, y = datasets.make_circles(n_samples=n_samples, factor=.5, noise=.05)
red = y == 0
green = y == 1

ax = subplots[0][0]
ax.scatter(X[red, 0], X[red, 1], c="r")
ax.scatter(X[green, 0], X[green, 1], c="g")
ax.xaxis.set_major_formatter(NullFormatter())
ax.yaxis.set_major_formatter(NullFormatter())
plt.axis('tight')

for i, perplexity in enumerate(perplexities):
    ax = subplots[0][i + 1]
    t0 = time()
    tsne = manifold.TSNE(n_components=n_components, init='random',
                         random_state=0, perplexity=perplexity)
    Y = tsne.fit_transform(X)
    t1 = time()
    print("circles, perplexity=%d in %.2g sec" % (perplexity, t1 - t0))
    ax.set_title("Perplexity=%d" % perplexity)
    ax.scatter(Y[red, 0], Y[red, 1], c="r")
    ax.scatter(Y[green, 0], Y[green, 1], c="g")
    ax.xaxis.set_major_formatter(NullFormatter())
    ax.yaxis.set_major_formatter(NullFormatter())
    ax.axis('tight')

# Another example using s-curve
X, color = datasets.samples_generator.make_s_curve(n_samples, random_state=0)
ax = subplots[1][0]
ax.scatter(X[:, 0], X[:, 2], c=color, cmap=plt.cm.viridis)
ax.xaxis.set_major_formatter(NullFormatter())
ax.yaxis.set_major_formatter(NullFormatter())

for i, perplexity in enumerate(perplexities):
    ax = subplots[1][i + 1]
    t0 = time()
    tsne = manifold.TSNE(n_components=n_components, init='random',
                         random_state=0, perplexity=perplexity)
    Y = tsne.fit_transform(X)
    t1 = time()
    print("S-curve, perplexity=%d in %.2g sec" % (perplexity, t1 - t0))
    ax.set_title("Perplexity=%d" % perplexity)
    ax.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.viridis)
    ax.xaxis.set_major_formatter(NullFormatter())
    ax.yaxis.set_major_formatter(NullFormatter())
    ax.axis('tight')

# Another example using a 2D uniform grid
x = np.linspace(0, 1, int(np.sqrt(n_samples)))
xx, yy = np.meshgrid(x, x)
X = np.hstack(
    [xx.ravel().reshape(-1, 1),
     yy.ravel().reshape(-1, 1),
    ])
color = xx.ravel()
as = subplots[2][0]
as.scatter(X[:, 0], X[:, 1], c=color, cmap=plt.cm.viridis)
as.xaxis.set_major_formatter(NullFormatter())
as.yaxis.set_major_formatter(NullFormatter())

for i, perplexity in enumerate(perplexities):
as = subplots[2][i + 1]
t0 = time()
tsne = manifold.TSNE(n_components=n_components, init='random',
                     random_state=0, perplexity=perplexity)
Y = tsne.fit_transform(X)
t1 = time()
print("uniform grid, perplexity=%d in %.2g sec" % (perplexity, t1 - t0))
as.set_title("Perplexity=%d" % perplexity)
as.scatter(Y[:, 0], Y[:, 1], c=color, cmap=plt.cm.viridis)
as.xaxis.set_major_formatter(NullFormatter())
as.yaxis.set_major_formatter(NullFormatter())
as.axis('tight')
plt.show()

Total running time of the script: ( 1 minutes 0.106 seconds)

19.5 Manifold Learning methods on a severed sphere

An application of the different Manifold learning techniques on a spherical data-set. Here one can see the use of dimensionality reduction in order to gain some intuition regarding the manifold learning methods. Regarding the dataset, the poles are cut from the sphere, as well as a thin slice down its side. This enables the manifold learning techniques to ‘spread it open’ whilst projecting it onto two dimensions.

For a similar example, where the methods are applied to the S-curve dataset, see Comparison of Manifold Learning methods

Note that the purpose of the MDS is to find a low-dimensional representation of the data (here 2D) in which the distances respect well the distances in the original high-dimensional space, unlike other manifold-learning algorithms, it does not seeks an isotropic representation of the data in the low-dimensional space. Here the manifold problem matches fairly that of representing a flat map of the Earth, as with map projection
# Author: Jaques Grobler <jaques.grobler@inria.fr>
# License: BSD 3 clause

print(__doc__)

from time import time

import numpy as np
import matplotlib.pyplot as plt
from mpl_toolkits.mplot3d import Axes3D
from matplotlib.ticker import NullFormatter

from sklearn import manifold
from sklearn.utils import check_random_state

# Variables for manifold learning.

19.5. Manifold Learning methods on a severed sphere
n_neighbors = 10
n_samples = 1000

# Create our sphere.
random_state = check_random_state(0)
p = random_state.rand(n_samples) * (2 * np.pi - 0.55)
t = random_state.rand(n_samples) * np.pi

# Sever the poles from the sphere.
indices = ((t < (np.pi - (np.pi / 8))) & (t > ((np.pi / 8))))
colors = p[indices]
x, y, z = np.sin(t[indices]) * np.cos(p[indices]),
        np.sin(t[indices]) * np.sin(p[indices]),
        np.cos(t[indices])

# Plot our dataset.
fig = plt.figure(figsize=(15, 8))
plt.suptitle("Manifold Learning with
%i
points, %i
neighbors"
         % (1000, n_neighbors), fontsize=14)
ax = fig.add_subplot(251, projection='3d')
ax.scatter(x, y, z, c=colors, cmap=plt.cm.rainbow)
ax.view_init(40, -10)
sphere_data = np.array([x, y, z]).T

# Perform Locally Linear Embedding Manifold learning
methods = ['standard', 'ltsa', 'hessian', 'modified']
labels = ['LLE', 'LTSA', 'Hessian LLE', 'Modified LLE']

for i, method in enumerate(methods):
t0 = time()
    trans_data = manifold.
    .LocallyLinearEmbedding(n_neighbors, 2,
                            method=method).fit_transform(sphere_data).T
t1 = time()
    print("%s: %.2g sec" % (methods[i], t1 - t0))

    ax = fig.add_subplot(252 + i)
    plt.scatter(trans_data[0], trans_data[1], c=colors, cmap=plt.cm.rainbow)
    plt.title("%s (%.2g sec)" % (labels[i], t1 - t0))
    ax.xaxis.set_major_formatter(NullFormatter())
    ax.yaxis.set_major_formatter(NullFormatter())
    plt.axis('tight')

# Perform Isomap Manifold learning.
t0 = time()
trans_data = manifold.Isomap(n_neighbors, n_components=2)\
    .fit_transform(sphere_data).T
t1 = time()
print("%s: %.2g sec" % ('ISO', t1 - t0))

    ax = fig.add_subplot(257)
    plt.scatter(trans_data[0], trans_data[1], c=colors, cmap=plt.cm.rainbow)
    plt.title("%s (%.2g sec)" % ('Isomap', t1 - t0))
    ax.xaxis.set_major_formatter(NullFormatter())
    ax.yaxis.set_major_formatter(NullFormatter())
    plt.axis('tight')
# Perform Multi-dimensional scaling.
t0 = time()
dis = manifold.MDS(2, max_iter=100, n_init=1)
trans_data = dis.fit_transform(sphere_data).T
tl = time()

print("MDS: %.2g sec" % (tl - t0))

ax = fig.add_subplot(258)
plt.scatter(trans_data[0], trans_data[1], c=colors, cmap=plt.cm.rainbow)
plt.title("MDS (%.2g sec)" % (tl - t0))
ax.xaxis.set_major_formatter(NullFormatter())
ax.yaxis.set_major_formatter(NullFormatter())
plt.axis('tight')

# Perform Spectral Embedding.
t0 = time()
dis = manifold.SpectralEmbedding(n_components=2,
    n_neighbors=n_neighbors)
trans_data = dis.fit_transform(sphere_data).T
tl = time()

print("Spectral Embedding: %.2g sec" % (tl - t0))

ax = fig.add_subplot(259)
plt.scatter(trans_data[0], trans_data[1], c=colors, cmap=plt.cm.rainbow)
plt.title("Spectral Embedding (%.2g sec)" % (tl - t0))
ax.xaxis.set_major_formatter(NullFormatter())
ax.yaxis.set_major_formatter(NullFormatter())
plt.axis('tight')

# Perform t-distributed stochastic neighbor embedding.
t0 = time()
lsne = manifold.TSNE(n_components=2, init='pca', random_state=0)
trans_data = lsne.fit_transform(sphere_data).T
tl = time()

print("t-SNE: %.2g sec" % (tl - t0))

ax = fig.add_subplot(2, 5, 10)
plt.scatter(trans_data[0], trans_data[1], c=colors, cmap=plt.cm.rainbow)
plt.title("t-SNE (%.2g sec)" % (tl - t0))
ax.xaxis.set_major_formatter(NullFormatter())
ax.yaxis.set_major_formatter(NullFormatter())
plt.axis('tight')

plt.show()

Total running time of the script: ( 0 minutes 14.876 seconds)

19.6 Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

An illustration of various embeddings on the digits dataset.
The RandomTreesEmbedding, from the sklearn.ensemble module, is not technically a manifold embedding method, as it learn a high-dimensional representation on which we apply a dimensionality reduction method. However,
it is often useful to cast a dataset into a representation in which the classes are linearly-separable. t-SNE will be initialized with the embedding that is generated by PCA in this example, which is not the default setting. It ensures global stability of the embedding, i.e., the embedding does not depend on random initialization.
19.6. Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
Out:

```python
Computing random projection
Computing PCA projection
Computing Linear Discriminant Analysis projection
Computing Isomap embedding
Done.
Computing LLE embedding
Done. Reconstruction error: 1.63546e-06
Computing modified LLE embedding
Done. Reconstruction error: 0.360794
Computing Hessian LLE embedding
Done. Reconstruction error: 0.212807
Computing LTSA embedding
Done. Reconstruction error: 0.212806
Computing MDS embedding
Done. Stress: 140428674.316512
Computing Totally Random Trees embedding
Computing Spectral embedding
Computing t-SNE embedding
```

```python
# Authors: Fabian Pedregosa <fabian.pedregosa@inria.fr>
# Olivier Grisel <olivier.grisel@ensta.org>
# Mathieu Blondel <mathieu@mblondel.org>
# Gael Varoquaux
# License: BSD 3 clause (C) INRIA 2011

print(__doc__)
from time import time
import numpy as np
import matplotlib.pyplot as plt
from matplotlib import offsetbox
from sklearn import manifold, datasets, decomposition, ensemble,
discriminant_analysis, random_projection

digits = datasets.load_digits(n_class=6)
X = digits.data
```
y = digits.target
n_samples, n_features = X.shape
n_neighbors = 30

# Scale and visualize the embedding vectors
def plot_embedding(X, title=None):
    x_min, x_max = np.min(X, 0), np.max(X, 0)
    X = (X - x_min) / (x_max - x_min)

    plt.figure()
    ax = plt.subplot(111)

    for i in range(X.shape[0]):
        plt.text(X[i, 0], X[i, 1], str(digits.target[i]),
                 color=plt.cm.Set1(y[i] / 10.),
                 fontdict={'weight': 'bold', 'size': 9})

    if hasattr(offsetbox, 'AnnotationBbox'):
        # only print thumbnails with matplotlib > 1.0
        shown_images = np.array([[1., 1.]])  # just something big

        for i in range(digits.data.shape[0]):
            dist = np.sum((X[i] - shown_images) ** 2, 1)
            if np.min(dist) < 4e-3:
                # don't show points that are too close
                continue

            shown_images = np.r_[shown_images, [X[i]]]

            imagebox = offsetbox.AnnotationBbox(
                offsetbox.OffsetImage(digits.images[i], cmap=plt.cm.gray_r),
                X[i])
        ax.add_artist(imagebox)

    plt.xticks([]), plt.yticks([])
    if title is not None:
        plt.title(title)

# Plot images of the digits
n_img_per_row = 20
img = np.zeros((10 * n_img_per_row, 10 * n_img_per_row))

for i in range(n_img_per_row):
    ix = 10 * i + 1
    for j in range(n_img_per_row):
        iy = 10 * j + 1
        img[ix:ix + 8, iy:iy + 8] = X[i * n_img_per_row + j].reshape((8, 8))

plt.imshow(img, cmap=plt.cm.binary)
plt.xticks([])
plt.yticks([])
plt.title('A selection from the 64-dimensional digits dataset')

# Random 2D projection using a random unitary matrix
print("Computing random projection")
rp = random_projection.SparseRandomProjection(n_components=2, random_state=42)
X_projected = rp.fit_transform(X)
plot_embedding(X_projected, "Random Projection of the digits")
# Projection on to the first 2 principal components

```python
print("Computing PCA projection")
t0 = time()
X_pca = decomposition.TruncatedSVD(n_components=2).fit_transform(X)
plot_embedding(X_pca,
    "Principal Components projection of the digits (time %.2fs)" %
    (time() - t0))
```

# Projection on to the first 2 linear discriminant components

```python
print("Computing Linear Discriminant Analysis projection")
X2 = X.copy()
X2.flat[X.shape[1] + 1] += 0.01 # Make X invertible
t0 = time()
X_lda = discriminant_analysis.LinearDiscriminantAnalysis(n_components=2).fit_
    ->transform(X2, y)
plot_embedding(X_lda,
    "Linear Discriminant projection of the digits (time %.2fs)" %
    (time() - t0))
```

# Isomap projection of the digits dataset

```python
print("Computing Isomap embedding")
t0 = time()
X_iso = manifold.Isomap(n_neighbors, n_components=2).fit_transform(X)
print("Done.")
plot_embedding(X_iso,
    "Isomap projection of the digits (time %.2fs)" %
    (time() - t0))
```

# Locally linear embedding of the digits dataset

```python
print("Computing LLE embedding")
clf = manifold.LocallyLinearEmbedding(n_neighbors, n_components=2,
    method='standard')
t0 = time()
X_lle = clf.fit_transform(X)
print("Done. Reconstruction error: %.2g" % clf.reconstruction_error_)
plot_embedding(X_lle,
    "Locally Linear Embedding of the digits (time %.2fs)" %
    (time() - t0))
```

# Modified Locally linear embedding of the digits dataset

```python
print("Computing modified LLE embedding")
clf = manifold.LocallyLinearEmbedding(n_neighbors, n_components=2,
    method='modified')
t0 = time()
X_mlle = clf.fit_transform(X)
print("Done. Reconstruction error: %.2g" % clf.reconstruction_error_)
```
```
# HLLLE embedding of the digits dataset
print("Computing Hessian LLE embedding")
clf = manifold.LocallyLinearEmbedding(n_neighbors, n_components=2,
    method='hessian')
t0 = time()
X_hlle = clf.fit_transform(X)
print("Done. Reconstruction error: \$g\" % clf.reconstruction_error_)
plot_embedding(X_hlle,
    "Hessian Locally Linear Embedding of the digits (time %.2fs)" %
    (time() - t0))

# LTSA embedding of the digits dataset
print("Computing LTSA embedding")
clf = manifold.LocallyLinearEmbedding(n_neighbors, n_components=2,
    method='ltsa')
t0 = time()
X_ltsa = clf.fit_transform(X)
print("Done. Reconstruction error: \$g\" % clf.reconstruction_error_)
plot_embedding(X_ltsa,
    "Local Tangent Space Alignment of the digits (time %.2fs)" %
    (time() - t0))

# MDS embedding of the digits dataset
print("Computing MDS embedding")
clf = manifold.MDS(n_components=2, n_init=1, max_iter=100)
t0 = time()
X_mds = clf.fit_transform(X)
print("Done. Stress: \$f\" % clf.stress_)
plot_embedding(X_mds,
    "MDS embedding of the digits (time %.2fs)" %
    (time() - t0))

# Random Trees embedding of the digits dataset
print("Computing Totally Random Trees embedding")
hasher = ensemble.RandomTreesEmbedding(n_estimators=200, random_state=0,
    max_depth=5)
t0 = time()
X_transformed = hasher.fit_transform(X)
pca = decomposition.TruncatedSVD(n_components=2)
X_reduced = pca.fit_transform(X_transformed)
plot_embedding(X_reduced,
    "Random forest embedding of the digits (time %.2fs)" %
    (time() - t0))
```
```python
e embedder = manifold.SpectralEmbedding(n_components=2, random_state=0,
        eigen_solver="arpack")

t0 = time()
X_se = embedder.fit_transform(X)

plot_embedding(X_se,
        "Spectral embedding of the digits (time %.2fs)" %
        (time() - t0))

#----------------------------------------------------------------------
# t-SNE embedding of the digits dataset
print("Computing t-SNE embedding")
tsne = manifold.TSNE(n_components=2, init='pca', random_state=0)
t0 = time()
X_tsne = tsne.fit_transform(X)

plot_embedding(X_tsne,
        "t-SNE embedding of the digits (time %.2fs)" %
        (time() - t0))

plt.show()
```

**Total running time of the script:** ( 0 minutes 34.730 seconds)
Examples concerning the `sklearn.mixture` module.

### 20.1 Density Estimation for a Gaussian mixture

Plot the density estimation of a mixture of two Gaussians. Data is generated from two Gaussians with different centers and covariance matrices.

```python
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import LogNorm
```

![Image of negative log-likelihood predicted by a GMM]

```
plt.figure(figsize=(8, 6))
# Your code to generate the plot
plt.show()
```
```python
from sklearn import mixture

n_samples = 300

# generate random sample, two components
np.random.seed(0)

# generate spherical data centered on (20, 20)
shifted_gaussian = np.random.randn(n_samples, 2) + np.array([20, 20])

# generate zero centered stretched Gaussian data
C = np.array([[0., -0.7], [3.5, .7]])
stretched_gaussian = np.dot(np.random.randn(n_samples, 2), C)

# concatenate the two datasets into the final training set
X_train = np.vstack([shifted_gaussian, stretched_gaussian])

# fit a Gaussian Mixture Model with two components
clf = mixture.GaussianMixture(n_components=2, covariance_type='full')
clf.fit(X_train)

# display predicted scores by the model as a contour plot
x = np.linspace(-20., 30.)
y = np.linspace(-20., 40.)
X, Y = np.meshgrid(x, y)
XX = np.array([X.ravel(), Y.ravel()]).T
Z = -clf.score_samples(XX)
Z = Z.reshape(X.shape)

CS = plt.contour(X, Y, Z, norm=LogNorm(vmin=1.0, vmax=1000.0),
                 levels=np.logspace(0, 3, 10))
CB = plt.colorbar(CS, shrink=0.8, extend='both')
plt.scatter(X_train[:, 0], X_train[:, 1], .8)
plt.title('Negative log-likelihood predicted by a GMM')
plt.axis('tight')
plt.show()
```

Total running time of the script: ( 0 minutes 0.149 seconds)

### 20.2 Gaussian Mixture Model Ellipsoids

Plot the confidence ellipsoids of a mixture of two Gaussians obtained with Expectation Maximisation (`GaussianMixture` class) and Variational Inference (`BayesianGaussianMixture` class models with a Dirichlet process prior).

Both models have access to five components with which to fit the data. Note that the Expectation Maximisation model will necessarily use all five components while the Variational Inference model will effectively only use as many as are needed for a good fit. Here we can see that the Expectation Maximisation model splits some components arbitrarily, because it is trying to fit too many components, while the Dirichlet Process model adapts it number of state automatically.

This example doesn’t show it, as we’re in a low-dimensional space, but another advantage of the Dirichlet process model is that it can fit full covariance matrices effectively even when there are less examples per cluster than there are dimensions in the data, due to regularization properties of the inference algorithm.
import itertools

import numpy as np
from scipy import linalg
import matplotlib.pyplot as plt
import matplotlib as mpl

from sklearn import mixture

color_iter = itertools.cycle(['navy', 'c', 'cornflowerblue', 'gold', 'darkorange'])

def plot_results(X, Y_, means, covariances, index, title):
    splot = plt.subplot(2, 1, 1 + index)
    for i, (mean, covar, color) in enumerate(zip(means, covariances, color_iter)):
        v, w = linalg.eigh(covar)
        v = 2. * np.sqrt(2.) * np.sqrt(v)
        u = w[0] / linalg.norm(w[0])
        # as the DP will not use every component it has access to
        # unless it needs it, we shouldn’t plot the redundant
        # components.
        if not np.any(Y_ == i):
            continue
        plt.scatter(X[Y_ == i, 0], X[Y_ == i, 1], .8, color=color)
# Plot an ellipse to show the Gaussian component
angle = np.arctan(u[1] / u[0])
angle = 180. * angle / np.pi  # convert to degrees
ell = mpl.patches.Ellipse(mean, v[0], v[1], 180. + angle, color=color)
ell.set_clip_box(splot.bbox)
ell.set_alpha(0.5)
splot.add_artist(ell)

plt.xlim(-9., 5.)
plt.ylim(-3., 6.)
plt.xticks(())
plt.yticks(())
plt.title(title)

# Number of samples per component
n_samples = 500

# Generate random sample, two components
np.random.seed(0)
C = np.array([[0., -0.1], [1.7, .4]])
X = np.r_[np.dot(np.random.randn(n_samples, 2), C),
          .7 * np.random.randn(n_samples, 2) + np.array([-6, 3])]

# Fit a Gaussian mixture with EM using five components
gmm = mixture.GaussianMixture(n_components=5, covariance_type='full').fit(X)
plot_results(X, gmm.predict(X), gmm.means_, gmm.covariances_, 0,
             'Gaussian Mixture')

# Fit a Dirichlet process Gaussian mixture using five components
dpgmm = mixture.BayesianGaussianMixture(n_components=5,
covariance_type='full').fit(X)
plot_results(X, dpgmm.predict(X), dpgmm.means_, dpgmm.covariances_, 1,
             'Bayesian Gaussian Mixture with a Dirichlet process prior')

plt.show()

Total running time of the script: ( 0 minutes 0.430 seconds)

20.3 Gaussian Mixture Model Selection

This example shows that model selection can be performed with Gaussian Mixture Models using information-theoretic criteria (BIC). Model selection concerns both the covariance type and the number of components in the model. In that case, AIC also provides the right result (not shown to save time), but BIC is better suited if the problem is to identify the right model. Unlike Bayesian procedures, such inferences are prior-free.

In that case, the model with 2 components and full covariance (which corresponds to the true generative model) is selected.
import numpy as np
import itertools
from scipy import linalg
import matplotlib.pyplot as plt
import matplotlib as mpl
from sklearn import mixture

print(__doc__)

# Number of samples per component
n_samples = 500

# Generate random sample, two components
np.random.seed(0)
C = np.array([[0., -0.1], [1.7, .4]])
X = np.r_[np.dot(np.random.randn(n_samples, 2), C),
          .7 * np.random.randn(n_samples, 2) + np.array([-6, 3])]

lowest_bic = np.infty
bic = []
n_components_range = range(1, 7)
cv_types = ['spherical', 'tied', 'diag', 'full']
for cv_type in cv_types:
    for n_components in n_components_range:
        gmm = mixture.GMM(n_components=n_components, covariance_type=cv_type)
        gmm.fit(X)
        bic.append([-n_components, gmm.bic(X)])

bic = np.array(bic)
best_bic = bic[bic[:, 0].argmin(), 1]

# Plot results
fig = plt.figure()
ax = fig.add_subplot(111)
ax.set_xlim(0, 7)
ax.set_ylim(0, 9000)
ax.plot(bic[:, 0], bic[:, 1], 'b-', marker='o')
s = 'Selected GMM: full model, 2 components

fig = plt.figure()
ax = fig.add_subplot(111)
ax.set_xlim(0, 7)
ax.set_ylim(0, 9000)
ax.plot(bic[:, 0], bic[:, 1], 'b-', marker='o')
s = 'Selected GMM: full model, 2 components

20.3. Gaussian Mixture Model Selection
# Fit a Gaussian mixture with EM

gmm = mixture.GaussianMixture(n_components=n_components,
covariance_type=cv_type)

gmm.fit(X)
bic.append(gmm.bic(X))

if bic[-1] < lowest_bic:
    lowest_bic = bic[-1]
    best_gmm = gmm

bic = np.array(bic)
color_iter = itertools.cycle(['navy', 'turquoise', 'cornflowerblue',
                               'darkorange'])

clf = best_gmm
bars = []

# Plot the BIC scores
spl = plt.subplot(2, 1, 1)
for i, (cv_type, color) in enumerate(zip(cv_types, color_iter)):
    xpos = np.array(n_components_range) + .2 * (i - 2)
    bars.append(plt.bar(xpos, bic[i * len(n_components_range):
                                (i + 1) * len(n_components_range)],
                        width=.2, color=color))
plt.xticks(n_components_range)
plt.ylim([bic.min() * 1.01 - .01 * bic.max(), bic.max()])
plt.title('BIC score per model')
xpos = np.mod(bic.argmin(), len(n_components_range)) + .65 +
     .2 * np.floor(bic.argmin() / len(n_components_range))
plt.text(xpos, bic.min() * 0.97 + .03 * bic.max(), '*', fontsize=14)
spl.set_xlabel('Number of components')
spl.legend([b[0] for b in bars], cv_types)

# Plot the winner
splot = plt.subplot(2, 1, 2)
Y_ = clf.predict(X)
for i, (mean, cov, color) in enumerate(zip(clf.means_,
                                           clf.covariances_,
                                           color_iter)):
    v, w = linalg.eigh(cov)
    if not np.any(Y_ == i):
        continue
    plt.scatter(X[Y_ == i, 0], X[Y_ == i, 1], .8, color=color)
    # Plot an ellipse to show the Gaussian component
    angle = np.arctan2(w[0][1], w[0][0])
    angle = 180. * angle / np.pi # convert to degrees
    v = 2. * np.sqrt(2. * np.sqrt(v))
    ell = mpl.patches.Ellipse(mean, v[0], v[1], 180. + angle, color=color)
    ell.set_clip_box(splot.bbox)
    ell.set_alpha(.5)
    splot.add_artist(ell)

plt.xticks(()
plt.yticks(()
plt.title('Selected GMM: full model, 2 components')
plt.subplots_adjust(hspace=.35, bottom=.02)
plt.show()

Total running time of the script: ( 0 minutes 0.569 seconds)
20.4 GMM covariances

Demonstration of several covariances types for Gaussian mixture models.

See Gaussian mixture models for more information on the estimator.

Although GMM are often used for clustering, we can compare the obtained clusters with the actual classes from the dataset. We initialize the means of the Gaussians with the means of the classes from the training set to make this comparison valid.

We plot predicted labels on both training and held out test data using a variety of GMM covariance types on the iris dataset. We compare GMMs with spherical, diagonal, full, and tied covariance matrices in increasing order of performance. Although one would expect full covariance to perform best in general, it is prone to overfitting on small datasets and does not generalize well to held out test data.

On the plots, train data is shown as dots, while test data is shown as crosses. The iris dataset is four-dimensional. Only the first two dimensions are shown here, and thus some points are separated in other dimensions.
import matplotlib as mpl
import matplotlib.pyplot as plt

import numpy as np

from sklearn import datasets
from sklearn.mixture import GaussianMixture
from sklearn.model_selection import StratifiedKFold

print(__doc__)

colors = ['navy', 'turquoise', 'darkorange']

def make_ellipses(gmm, ax):
    for n, color in enumerate(colors):
        if gmm.covariance_type == 'full':
            covariances = gmm.covariances_[n][:2, :2]
        elif gmm.covariance_type == 'tied':
            covariances = gmm.covariances_[:2, :2]
        elif gmm.covariance_type == 'diag':
            covariances = np.diag(gmm.covariances_[n][:2])
        elif gmm.covariance_type == 'spherical':
            covariances = np.eye(gmm.means_.shape[1]) * gmm.covariances_[n]
        v, w = np.linalg.eigh(covariances)
        u = w[0] / np.linalg.norm(w[0])
        angle = np.arctan2(u[1], u[0])
        angle = 180 * angle / np.pi  # convert to degrees
        v = 2. * np.sqrt(2.) * np.sqrt(v)
        ell = mpl.patches.Ellipse(gmm.means_[n, :2], v[0], v[1],
                                  180 + angle, color=color)
        ell.set_clip_box(ax.bbox)
        ell.set_alpha(0.5)
        ax.add_artist(ell)

iris = datasets.load_iris()

# Break up the dataset into non-overlapping training (75%) and testing
# (25%) sets.
skf = StratifiedKFold(n_splits=4)
# Only take the first fold.
train_index, test_index = next(iter(skf.split(iris.data, iris.target)))

X_train = iris.data[train_index]
y_train = iris.target[train_index]
X_test = iris.data[test_index]
y_test = iris.target[test_index]
n_classes = len(np.unique(y_train))

# Try GMMs using different types of covariances.
estimators = dict((cov_type, GaussianMixture(n_components=n_classes,
                                             covariance_type=cov_type, max_iter=20, random_state=0))

# Author: Ron Weiss <ronweiss@gmail.com>, Gael Varoquaux
# Modified by Thierry Guillemot <thierry.guillemot.work@gmail.com>
# License: BSD 3 clause
for cov_type in ['spherical', 'diag', 'tied', 'full'])

n_estimators = len(estimators)

plt.figure(figsize=(3 * n_estimators // 2, 6))
plt.subplots_adjust(bottom=.01, top=0.95, hspace=.15, wspace=.05,
                   left=.01, right=.99)

for index, (name, estimator) in enumerate(estimators.items()):
    # Since we have class labels for the training data, we can
    # initialize the GMM parameters in a supervised manner.
estimator.means_init = np.array([X_train[y_train == i].mean(axis=0)
    for i in range(n_classes)])

    # Train the other parameters using the EM algorithm.
estimator.fit(X_train)

    h = plt.subplot(2, n_estimators // 2, index + 1)
    make_ellipses(estimator, h)

    for n, color in enumerate(colors):
        data = iris.data[iris.target == n]
        plt.scatter(data[:, 0], data[:, 1], s=0.8, color=color,
                    label=iris.target_names[n])

    # Plot the test data with crosses
    for n, color in enumerate(colors):
        data = X_test[y_test == n]
        plt.scatter(data[:, 0], data[:, 1], marker='x', color=color)

    y_train_pred = estimator.predict(X_train)
    train_accuracy = np.mean(y_train_pred.ravel() == y_train.ravel()) * 100
    plt.text(0.05, 0.9, 'Train accuracy: %.1f' % train_accuracy,
             transform=h.transAxes)

    y_test_pred = estimator.predict(X_test)
    test_accuracy = np.mean(y_test_pred.ravel() == y_test.ravel()) * 100
    plt.text(0.05, 0.8, 'Test accuracy: %.1f' % test_accuracy,
              transform=h.transAxes)

plt.xticks(())
plt.yticks(())
plt.title(name)
plt.legend(scatterpoints=1, loc='lower right', prop=dict(size=12))

plt.show()

Total running time of the script: ( 0 minutes 0.253 seconds)

20.5 Gaussian Mixture Model Sine Curve

This example demonstrates the behavior of Gaussian mixture models fit on data that was not sampled from a mixture of Gaussian random variables. The dataset is formed by 100 points loosely spaced following a noisy sine curve. There is therefore no ground truth value for the number of Gaussian components.
The first model is a classical Gaussian Mixture Model with 10 components fit with the Expectation-Maximization algorithm.

The second model is a Bayesian Gaussian Mixture Model with a Dirichlet process prior fit with variational inference. The low value of the concentration prior makes the model favor a lower number of active components. This models “decides” to focus its modeling power on the big picture of the structure of the dataset: groups of points with alternating directions modeled by non-diagonal covariance matrices. Those alternating directions roughly capture the alternating nature of the original sine signal.

The third model is also a Bayesian Gaussian mixture model with a Dirichlet process prior but this time the value of the concentration prior is higher giving the model more liberty to model the fine-grained structure of the data. The result is a mixture with a larger number of active components that is similar to the first model where we arbitrarily decided to fix the number of components to 10.

Which model is the best is a matter of subjective judgement: do we want to favor models that only capture the big picture to summarize and explain most of the structure of the data while ignoring the details or do we prefer models that closely follow the high density regions of the signal?

The last two panels show how we can sample from the last two models. The resulting samples distributions do not look exactly like the original data distribution. The difference primarily stems from the approximation error we made by using a model that assumes that the data was generated by a finite number of Gaussian components instead of a continuous noisy sine curve.
import itertools
import numpy as np
from scipy import linalg
import matplotlib.pyplot as plt
import matplotlib as mpl
from sklearn import mixture

print(__doc__)

color_iter = itertools.cycle(['navy', 'c', 'cornflowerblue', 'gold', 'darkorange'])
```python
def plot_results(X, Y, means, covariances, index, title):
    splot = plt.subplot(5, 1, 1 + index)
    for i, (mean, covar, color) in enumerate(zip(
        means, covariances, color_iter)):
        v, w = linalg.eigh(covar)
        v = 2. * np.sqrt(2.) * np.sqrt(v)
        u = w[0] / linalg.norm(w[0])
        # as the DP will not use every component it has access to
        # unless it needs it, we shouldn’t plot the redundant
        # components.
        if not np.any(Y == i):
            continue
        plt.scatter(X[Y == i, 0], X[Y == i, 1], .8, color=color)
        # Plot an ellipse to show the Gaussian component
        angle = np.arctan(u[1] / u[0])
        angle = 180. * angle / np.pi  # convert to degrees
        ell = mpl.patches.Ellipse(mean, v[0], v[1], 180. + angle, color=color)
        ell.set_clip_box(splot.bbox)
        ell.set_alpha(0.5)
        splot.add_artist(ell)
    plt.xlim(-6., 4. * np.pi - 6.)
    plt.ylim(-5., 5.)
    plt.title(title)
    plt.xticks(())
    plt.yticks(())

def plot_samples(X, Y, n_components, index, title):
    plt.subplot(5, 1, 4 + index)
    for i, color in zip(range(n_components), color_iter):
        # as the DP will not use every component it has access to
        # unless it needs it, we shouldn’t plot the redundant
        # components.
        if not np.any(Y == i):
            continue
        plt.scatter(X[Y == i, 0], X[Y == i, 1], .8, color=color)
    plt.xlim(-6., 4. * np.pi - 6.)
    plt.ylim(-5., 5.)
    plt.title(title)
    plt.xticks()
    plt.yticks()

# Parameters
n_samples = 100

# Generate random sample following a sine curve
np.random.seed(0)
X = np.zeros((n_samples, 2))
step = 4. * np.pi / n_samples
for i in range(X.shape[0]):
    x = i * step - 6.
    X[i, 0] = x + np.random.normal(0, 0.1)
    X[i, 1] = 3. * (np.sin(x) + np.random.normal(0, .2))
```

---

**Chapter 20. Gaussian Mixture Models**

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plt.figure(figsize=(10, 10))
plt.subplots_adjust(bottom=.04, top=0.95, hspace=.2, wspace=.05,
                 left=.03, right=.97)

# Fit a Gaussian mixture with EM using ten components
gmm = mixture.GaussianMixture(n_components=10, covariance_type='full',
                               max_iter=100).fit(X)
plot_results(X, gmm.predict(X), gmm.means_, gmm.covariances_, 0,
             'Expectation-maximization')

dpgmm = mixture.BayesianGaussianMixture(n_components=10, covariance_type='full',
                                         weight_concentration_prior=1e-2,
                                         weight_concentration_prior_type='dirichlet_process',
                                         mean_precision_prior=1e-2, covariance_prior=1e0 * np.eye(2),
                                         init_params="random", max_iter=100, random_state=2).fit(X)
plot_results(X, dpgmm.predict(X), dpgmm.means_, dpgmm.covariances_, 1,
             "Bayesian Gaussian mixture models with a Dirichlet process prior 
              r"for $\gamma_0=0.01\$.")

X_s, y_s = dpgmm.sample(n_samples=2000)
plot_samples(X_s, y_s, dpgmm.n_components, 0,
             "Gaussian mixture with a Dirichlet process prior 
              r"for $\gamma_0=0.01\$ sampled with $2000\$ samples.")

dpgmm = mixture.BayesianGaussianMixture(n_components=10, covariance_type='full',
                                         weight_concentration_prior=1e+2,
                                         weight_concentration_prior_type='dirichlet_process',
                                         mean_precision_prior=1e-2, covariance_prior=1e0 * np.eye(2),
                                         init_params="kmeans", max_iter=100, random_state=2).fit(X)
plot_results(X, dpgmm.predict(X), dpgmm.means_, dpgmm.covariances_, 2,
             "Bayesian Gaussian mixture models with a Dirichlet process prior 
              r"for $\gamma_0=100\$")

X_s, y_s = dpgmm.sample(n_samples=2000)
plot_samples(X_s, y_s, dpgmm.n_components, 1,
             "Gaussian mixture with a Dirichlet process prior 
              r"for $\gamma_0=100\$ sampled with $2000\$ samples.")

plt.show()

Total running time of the script: ( 0 minutes 0.731 seconds)

20.6 Concentration Prior Type Analysis of Variation Bayesian Gaussian Mixture

This example plots the ellipsoids obtained from a toy dataset (mixture of three Gaussians) fitted by the `BayesianGaussianMixture` class models with a Dirichlet distribution prior (`weight_concentration_prior_type='dirichlet_distribution'`) and a Dirichlet process prior (`weight_concentration_prior_type='dirichlet_process'`). On each figure, we plot the results for three different values of the weight concentration prior.

The `BayesianGaussianMixture` class can adapt its number of mixture components automatically. The parameter `weight_concentration_prior` has a direct link with the resulting number of components with non-zero weights. Specifying a low value for the concentration prior will make the model put most of the weight on few com-
ponents set the remaining components weights very close to zero. High values of the concentration prior will allow a larger number of components to be active in the mixture.

The Dirichlet process prior allows to define an infinite number of components and automatically selects the correct number of components: it activates a component only if it is necessary.

On the contrary the classical finite mixture model with a Dirichlet distribution prior will favor more uniformly weighted components and therefore tends to divide natural clusters into unnecessary sub-components.

# Author: Thierry Guillemot <thierry.guillemot.work@gmail.com>
# License: BSD 3 clause
import numpy as np
import matplotlib as mpl
import matplotlib.pyplot as plt
import matplotlib.gridspec as gridspec

from sklearn.mixture import BayesianGaussianMixture

print(__doc__)

def plot_ellipses(ax, weights, means, covars):
    for n in range(means.shape[0]):
        eig_vals, eig_vecs = np.linalg.eigh(covars[n])
        unit_eig_vec = eig_vecs[0] / np.linalg.norm(eig_vecs[0])
        angle = np.arctan2(unit_eig_vec[1], unit_eig_vec[0])
        # Ellipse needs degrees
        angle = 180 * angle / np.pi
        # eigenvector normalization
        eig_vals = 2 * np.sqrt(2) * np.sqrt(eig_vals)
        ell = mpl.patches.Ellipse(means[n], eig_vals[0], eig_vals[1],
                                   180 + angle, edgecolor='black')
        ell.set_clip_box(ax.bbox)
        ell.set_alpha(weights[n])
        ell.set_facecolor('#56B4E9')
        ax.add_artist(ell)

def plot_results(ax1, ax2, estimator, X, y, title, plot_title=False):
    ax1.set_title(title)
    ax1.scatter(X[:, 0], X[:, 1], s=5, marker='o', color=colors[y], alpha=0.8)
    ax1.set_xlim(-2., 2.)
    ax1.set_ylim(-3., 3.)
    ax1.set_xticks(())
    ax1.set_yticks(())
    plot_ellipses(ax1, estimator.weights_, estimator.means_,
                  estimator.covariances_)
    ax2.get_xaxis().set_tick_params(direction='out')
    ax2.yaxis.grid(True, alpha=0.7)
    for k, w in enumerate(estimator.weights_):
        ax2.bar(k, w, width=0.9, color='#56B4E9', zorder=3,
                align='center', edgecolor='black')
        ax2.text(k, w + 0.007, "%.1f%%" % (w * 100.),
                  horizontalalignment='center')
    ax2.set_xlim(-.6, 2 * n_components - .4)
    ax2.set_ylim(0., 1.1)
    ax2.tick_params(axis='y', which='both', left='off',
                    right='off')
    ax2.tick_params(axis='x', which='both', top='off')
    if plot_title:
        ax1.set_ylabel('Estimated Mixtures')
        ax2.set_ylabel('Weight of each component')

# Parameters of the dataset
random_state, n_components, n_features = 2, 3, 2
colors = np.array(['#0072B2', '#F0E442', '#D55E00'])
covars = np.array([[[0.7, 0.0], [0.0, 0.1]],
                   [[0.5, 0.0], [0.0, 0.1]],
                   [[0.5, 0.0], [0.0, 0.1]]])
samples = np.array([200, 500, 200])
means = np.array([[0.0, -0.70],
                  [0.0, 0.0],
                  [0.0, 0.70]])

# mean_precision_prior= 0.8 to minimize the influence of the prior
estimators = [(
    "Finite mixture with a Dirichlet distribution\n    prior and $\gamma_0=$", BayesianGaussianMixture(
        weight_concentration_prior_type="dirichlet_distribution",
        n_components=2 * n_components, reg_covar=0, init_params='random',
        max_iter=1500, mean_precision_prior=.8,
        random_state=random_state), [0.001, 1, 1000]),
    ("Infinite mixture with a Dirichlet process\n    prior and $\gamma_0=$", BayesianGaussianMixture(
        weight_concentration_prior_type="dirichlet_process",
        n_components=2 * n_components, reg_covar=0, init_params='random',
        max_iter=1500, mean_precision_prior=.8,
        random_state=random_state), [1, 1000, 100000])]

# Generate data
rng = np.random.RandomState(random_state)
X = np.vstack([rng.multivariate_normal(means[j], covars[j], samples[j])
               for j in range(n_components)])
y = np.concatenate([j * np.ones(samples[j], dtype=int)
                    for j in range(n_components)])

# Plot results in two different figures
for (title, estimator, concentrations_prior) in estimators:
    plt.figure(figsize=(4.7 * 3, 8))
    plt.subplots_adjust(bottom=.04, top=0.90, hspace=.05, wspace=.05,
                        left=.03, right=.99)
    gs = gridspec.GridSpec(3, len(concentrations_prior))
    for k, concentration in enumerate(concentrations_prior):
        estimator.weight_concentration_prior = concentration
        estimator.fit(X)
        plot_results(plt.subplot(gs[0:2, k]), plt.subplot(gs[2, k]), estimator,
                     X, y, r"%s\$%.1e$" % (title, concentration),
                     plot_title=k == 0)

plt.show()
Examples related to the `sklearn.model_selection` module.

### 21.1 Plotting Validation Curves

In this plot you can see the training scores and validation scores of an SVM for different values of the kernel parameter `gamma`. For very low values of `gamma`, you can see that both the training score and the validation score are low. This is called underfitting. Medium values of `gamma` will result in high values for both scores, i.e. the classifier is performing fairly well. If `gamma` is too high, the classifier will overfit, which means that the training score is good but the validation score is poor.
import matplotlib.pyplot as plt
import numpy as np

from sklearn.datasets import load_digits
from sklearn.svm import SVC
from sklearn.model_selection import validation_curve

digits = load_digits()
X, y = digits.data, digits.target

param_range = np.logspace(-6, -1, 5)
train_scores, test_scores = validation_curve(SVC(), X, y, param_name="gamma", param_range=param_range, cv=10, scoring="accuracy", n_jobs=1)
train_scores_mean = np.mean(train_scores, axis=1)
train_scores_std = np.std(train_scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)

plt.title("Validation Curve with SVM")
plt.xlabel("$\gamma$")
plt.ylabel("Score")
plt.ylim(0.0, 1.1)
lw = 2
plt.semilogx(param_range, train_scores_mean, label="Training score", color="darkorange", lw=lw)
plt.fill_between(param_range, train_scores_mean - train_scores_std, train_scores_mean + train_scores_std, alpha=0.2, color="darkorange", lw=lw)
plt.semilogx(param_range, test_scores_mean, label="Cross-validation score", color="navy", lw=lw)
plt.fill_between(param_range, test_scores_mean - test_scores_std, test_scores_mean + test_scores_std, alpha=0.2, color="navy", lw=lw)
plt.legend(loc="best")
plt.show()

Total running time of the script: ( 0 minutes 36.139 seconds)

21.2 Underfitting vs. Overfitting

This example demonstrates the problems of underfitting and overfitting and how we can use linear regression with polynomial features to approximate nonlinear functions. The plot shows the function that we want to approximate, which is a part of the cosine function. In addition, the samples from the real function and the approximations of different models are displayed. The models have polynomial features of different degrees. We can see that a linear function (polynomial with degree 1) is not sufficient to fit the training samples. This is called underfitting. A polynomial of degree 4 approximates the true function almost perfectly. However, for higher degrees the model will overfit the training data, i.e. it learns the noise of the training data. We evaluate quantitatively overfitting/underfitting by using cross-validation. We calculate the mean squared error (MSE) on the validation set, the higher, the less likely the model generalizes correctly from the training data.
```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.pipeline import Pipeline
from sklearn.preprocessing import PolynomialFeatures
from sklearn.linear_model import LinearRegression
from sklearn.model_selection import cross_val_score

def true_fun(X):
    return np.cos(1.5 * np.pi * X)

np.random.seed(0)
n_samples = 30
degrees = [1, 4, 15]
X = np.sort(np.random.rand(n_samples))
y = true_fun(X) + np.random.randn(n_samples) * 0.1

plt.figure(figsize=(14, 5))
for i in range(len(degrees)):
    ax = plt.subplot(1, len(degrees), i + 1)
    plt.setp(ax, xticks=(), yticks=())
    polynomial_features = PolynomialFeatures(degree=degrees[i], include_bias=False)
    linear_regression = LinearRegression()
    pipeline = Pipeline(["
        polynomial_features",
        "linear_regression"
        ],
        linear_regression)
    pipeline.fit(X[:, np.newaxis], y)
    scores = cross_val_score(pipeline, X[:, np.newaxis], y,
        scoring="neg_mean_squared_error", cv=10)
        X_test = np.linspace(0, 1, 100)
        plt.plot(X_test, pipeline.predict(X_test[:, np.newaxis]), label="Model")
        plt.plot(X_test, true_fun(X_test), label="True function")
        plt.scatter(X, y, edgecolor='b', s=20, label="Samples")
        plt.xlabel("x")
```

21.2. Underfitting vs. Overfitting
21.3 Parameter estimation using grid search with cross-validation

This examples shows how a classifier is optimized by cross-validation, which is done using the `sklearn.model_selection.GridSearchCV` object on a development set that comprises only half of the available labeled data.

The performance of the selected hyper-parameters and trained model is then measured on a dedicated evaluation set that was not used during the model selection step.

More details on tools available for model selection can be found in the sections on `Cross-validation: evaluating estimator performance` and `Tuning the hyper-parameters of an estimator`.

Out:

```python
# Tuning hyper-parameters for precision

Best parameters set found on development set:

{'C': 10, 'gamma': 0.001, 'kernel': 'rbf'}

Grid scores on development set:

0.986 (+/-0.016) for {'C': 1, 'gamma': 0.001, 'kernel': 'rbf'}
0.959 (+/-0.029) for {'C': 1, 'gamma': 0.0001, 'kernel': 'rbf'}
0.988 (+/-0.017) for {'C': 10, 'gamma': 0.001, 'kernel': 'rbf'}
0.982 (+/-0.026) for {'C': 10, 'gamma': 0.0001, 'kernel': 'rbf'}
0.988 (+/-0.017) for {'C': 100, 'gamma': 0.001, 'kernel': 'rbf'}
0.982 (+/-0.025) for {'C': 100, 'gamma': 0.0001, 'kernel': 'rbf'}
0.988 (+/-0.017) for {'C': 1000, 'gamma': 0.001, 'kernel': 'rbf'}
0.982 (+/-0.025) for {'C': 1000, 'gamma': 0.0001, 'kernel': 'rbf'}
0.975 (+/-0.014) for {'C': 1, 'kernel': 'linear'}
0.975 (+/-0.014) for {'C': 10, 'kernel': 'linear'}
0.975 (+/-0.014) for {'C': 100, 'kernel': 'linear'}
0.975 (+/-0.014) for {'C': 1000, 'kernel': 'linear'}

Detailed classification report:

The model is trained on the full development set. The scores are computed on the full evaluation set.

<table>
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<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
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<td>1.00</td>
<td>1.00</td>
<td>89</td>
</tr>
<tr>
<td>1</td>
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<td>1.00</td>
<td>0.98</td>
<td>90</td>
</tr>
<tr>
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<td>0.98</td>
<td>0.98</td>
<td>92</td>
</tr>
<tr>
<td>3</td>
<td>1.00</td>
<td>0.99</td>
<td>0.99</td>
<td>93</td>
</tr>
</tbody>
</table>
# Tuning hyper-parameters for recall

Best parameters set found on development set:

```
{'C': 10, 'gamma': 0.001, 'kernel': 'rbf'}
```

Grid scores on development set:

```
0.986 (+/-0.019) for {'C': 1, 'gamma': 0.001, 'kernel': 'rbf'}
0.957 (+/-0.029) for {'C': 1, 'gamma': 0.0001, 'kernel': 'rbf'}
0.987 (+/-0.019) for {'C': 10, 'gamma': 0.001, 'kernel': 'rbf'}
0.981 (+/-0.028) for {'C': 10, 'gamma': 0.0001, 'kernel': 'rbf'}
0.987 (+/-0.019) for {'C': 100, 'gamma': 0.001, 'kernel': 'rbf'}
0.981 (+/-0.026) for {'C': 100, 'gamma': 0.0001, 'kernel': 'rbf'}
0.987 (+/-0.019) for {'C': 1000, 'gamma': 0.001, 'kernel': 'rbf'}
0.981 (+/-0.026) for {'C': 1000, 'gamma': 0.0001, 'kernel': 'rbf'}
0.972 (+/-0.012) for {'C': 1, 'kernel': 'linear'}
0.972 (+/-0.012) for {'C': 10, 'kernel': 'linear'}
0.972 (+/-0.012) for {'C': 100, 'kernel': 'linear'}
0.972 (+/-0.012) for {'C': 1000, 'kernel': 'linear'}
```

Detailed classification report:

The model is trained on the full development set.
The scores are computed on the full evaluation set.

```
precision    recall  f1-score   support
0        1.00    1.00     1.00      89
1        0.97    1.00     0.98      90
2        0.99    0.98     0.98      92
3        1.00    0.99     0.99      93
4        1.00    1.00     1.00      76
5        0.99    0.98     0.99      108
6        0.99    1.00     0.99      89
7        0.99    1.00     0.99      78
8        1.00    0.98     0.99      92
9        0.99    0.99     0.99      92
avg / total   0.99    0.99     0.99      899
```

from __future__ import print_function
from sklearn import datasets
from sklearn.model_selection import train_test_split
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import classification_report
from sklearn.svm import SVC

print(__doc__)

# Loading the Digits dataset
digits = datasets.load_digits()

# To apply an classifier on this data, we need to flatten the image, to
turn the data in a (samples, feature) matrix:
n_samples = len(digits.images)
X = digits.images.reshape((n_samples, -1))
y = digits.target

# Split the dataset in two equal parts
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=0.5, random_state=0)

# Set the parameters by cross-validation
tuned_parameters = [{'kernel': ['rbf'], 'gamma': [1e-3, 1e-4], 'C': [1, 10, 100, 1000]},
                   {'kernel': ['linear'], 'C': [1, 10, 100, 1000]}]
scores = ['precision', 'recall']

for score in scores:
    print("# Tuning hyper-parameters for %s" % score)
    print()
    clf = GridSearchCV(SVC(), tuned_parameters, cv=5, scoring='{}_macro'.format(score))
    clf.fit(X_train, y_train)
    print("Best parameters set found on development set:")
    print(clf.best_params_)
    print("Grid scores on development set:")
    print()
    means = clf.cv_results_['mean_test_score']
    stds = clf.cv_results_['std_test_score']
    for mean, std, params in zip(means, stds, clf.cv_results_['params']):
        print("%0.3f (+/-%0.03f) for %r" % (mean, std * 2, params))
    print()

    print("Detailed classification report")
    print()
    print("The model is trained on the full development set.")
    print("The scores are computed on the full evaluation set.")
    print()
    y_true, y_pred = y_test, clf.predict(X_test)
    print(classification_report(y_true, y_pred))
    print()
21.4 Train error vs Test error

Illustration of how the performance of an estimator on unseen data (test data) is not the same as the performance on training data. As the regularization increases the performance on train decreases while the performance on test is optimal within a range of values of the regularization parameter. The example with an Elastic-Net regression model and the performance is measured using the explained variance a.k.a. $R^2$.

Out:

Optimal regularization parameter : 0.000335292414925

print(__doc__)
import numpy as np
from sklearn import linear_model

# Generate sample data
n_samples_train, n_samples_test, n_features = 75, 150, 500
np.random.seed(0)
coef = np.random.randn(n_features)
coef[50:] = 0.0  # only the top 10 features are impacting the model
X = np.random.randn(n_samples_train + n_samples_test, n_features)
y = np.dot(X, coef)

# Split train and test data
X_train, X_test = X[:n_samples_train], X[n_samples_train:]
y_train, y_test = y[:n_samples_train], y[n_samples_train:]

# Compute train and test errors
alphas = np.logspace(-5, 1, 60)
enet = linear_model.ElasticNet(l1_ratio=0.7)
train_errors = list()
test_errors = list()
for alpha in alphas:
enet.set_params(alpha=alpha)
enet.fit(X_train, y_train)
train_errors.append(enet.score(X_train, y_train))
test_errors.append(enet.score(X_test, y_test))
i_alpha_optim = np.argmax(test_errors)
alpha_optim = alphas[i_alpha_optim]
print("Optimal regularization parameter : \$s\" % alpha_optim)

# Estimate the coef_ on full data with optimal regularization parameter
enet.set_params(alpha=alpha_optim)
coef_ = enet.fit(X, y).coef_

# Plot results functions
import matplotlib.pyplot as plt
plt.subplot(2, 1, 1)
plt.semilogx(alphas, train_errors, label='Train')
plt.semilogx(alphas, test_errors, label='Test')
plt.vlines(alpha_optim, plt.ylim()[0], np.max(test_errors), color='k',
          linewidth=3, label='Optimum on test')
plt.legend(loc='lower left')
plt.ylim([0, 1.2])
plt.xlabel('Regularization parameter')
plt.ylabel('Performance')

# Show estimated coef_ vs true coef
plt.subplot(2, 1, 2)
plt.plot(coef, label='True coef')
plt.plot(coef_, label='Estimated coef')
plt.legend()
plt.subplots_adjust(0.09, 0.04, 0.94, 0.94, 0.26, 0.26)
plt.show()

Total running time of the script: ( 0 minutes 2.726 seconds)

## 21.5 Receiver Operating Characteristic (ROC) with cross validation

Example of Receiver Operating Characteristic (ROC) metric to evaluate classifier output quality using cross-validation. ROC curves typically feature true positive rate on the Y axis, and false positive rate on the X axis. This means that the top left corner of the plot is the “ideal” point - a false positive rate of zero, and a true positive rate of one. This is not very realistic, but it does mean that a larger area under the curve (AUC) is usually better.

The “steepness” of ROC curves is also important, since it is ideal to maximize the true positive rate while minimizing the false positive rate.

This example shows the ROC response of different datasets, created from K-fold cross-validation. Taking all of these curves, it is possible to calculate the mean area under curve, and see the variance of the curve when the training set is split into different subsets. This roughly shows how the classifier output is affected by changes in the training data, and how different the splits generated by K-fold cross-validation are from one another.

**Note:**

See also `sklearn.metrics.auc_score`, `sklearn.model_selection.cross_val_score`, Receiver Operating Characteristic (ROC)
import numpy as np
from scipy import interp
import matplotlib.pyplot as plt
from itertools import cycle
from sklearn import svm, datasets
from sklearn.metrics import roc_curve, auc
from sklearn.model_selection import StratifiedKFold

# Data IO and generation

# Import some data to play with
iris = datasets.load_iris()
X = iris.data
y = iris.target
X, y = X[y != 2], y[y != 2]
n_samples, n_features = X.shape

# Add noisy features
random_state = np.random.RandomState(0)
X = np.c_[X, random_state.randn(n_samples, 200 * n_features)]
# Classification and ROC analysis

# Run classifier with cross-validation and plot ROC curves
cv = StratifiedKFold(n_splits=6)
classifier = svm.SVC(kernel='linear', probability=True, 
                    random_state=random_state)

tprs = []
aucs = []
mean_fpr = np.linspace(0, 1, 100)
i = 0
for train, test in cv.split(X, y):
    probas_ = classifier.fit(X[train], y[train]).predict_proba(X[test])
    # Compute ROC curve and area the curve
    fpr, tpr, thresholds = roc_curve(y[test], probas_[:, 1])
    tprs.append(interp(mean_fpr, fpr, tpr))
    tprs[-1][0] = 0.0
    roc_auc = auc(fpr, tpr)
aucs.append(roc_auc)

plt.plot(fpr, tpr, lw=1, alpha=0.3, 
         label='ROC fold %d (AUC = %0.2f)' % (i, roc_auc))
i += 1
plt.plot([0, 1], [0, 1], linestyle='--', lw=2, color='r',
         label='Luck', alpha=.8)

mean_tpr = np.mean(tprs, axis=0)
mean_auc = auc(mean_fpr, mean_tpr)
std_auc = np.std(aucs)
plt.plot(mean_fpr, mean_tpr, color='b',
         label=r'Mean ROC (AUC = %0.2f 
$\pm$ %0.2f)' % (mean_auc, std_auc),
         lw=2, alpha=.8)

std_tpr = np.std(tprs, axis=0)
tprs_upper = np.minimum(mean_tpr + std_tpr, 1)
tprs_lower = np.maximum(mean_tpr - std_tpr, 0)
plt.fill_between(mean_fpr, tprs_lower, tprs_upper, color='grey', alpha=.2,
                 label=r'$\pm$ 1 std. dev.')

plt.xlim([-0.05, 1.05])
plt.ylim([-0.05, 1.05])
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic example')
plt.legend(loc="lower right")
plt.show()

Total running time of the script: ( 0 minutes 0.276 seconds)

## 21.6 Confusion matrix

Example of confusion matrix usage to evaluate the quality of the output of a classifier on the iris data set. The diagonal elements represent the number of points for which the predicted label is equal to the true label, while off-diagonal elements are those that are mislabeled by the classifier. The higher the diagonal values of the confusion matrix the
better, indicating many correct predictions.

The figures show the confusion matrix with and without normalization by class support size (number of elements in each class). This kind of normalization can be interesting in case of class imbalance to have a more visual interpretation of which class is being misclassified.

Here the results are not as good as they could be as our choice for the regularization parameter C was not the best. In real life applications this parameter is usually chosen using Tuning the hyper-parameters of an estimator.

```python
Confusion matrix, without normalization
[[13 0 0]
 [ 0 10 6]
 [ 0 0  9]]

Normalized confusion matrix
[[1.0 0.0 0.0]
 [0.0 0.62 0.38]
 [0.0 0.0 1.0]]
```

```
print(__doc__)

import itertools
```
import numpy as np
import matplotlib.pyplot as plt

from sklearn import svm, datasets
from sklearn.model_selection import train_test_split
from sklearn.metrics import confusion_matrix

# import some data to play with
iris = datasets.load_iris()
X = iris.data
y = iris.target
class_names = iris.target_names

# Split the data into a training set and a test set
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

# Run classifier, using a model that is too regularized (C too low) to see
# the impact on the results
classifier = svm.SVC(kernel='linear', C=0.01)
y_pred = classifier.fit(X_train, y_train).predict(X_test)

def plot_confusion_matrix(cm, classes,
                          normalize=False,
                          title='Confusion matrix',
                          cmap=plt.cm.Blues):
    
    """
    This function prints and plots the confusion matrix.
    Normalization can be applied by setting `normalize=True`.
    """
    if normalize:
        cm = cm.astype('float') / cm.sum(axis=1)[:, np.newaxis]
        print("Normalized confusion matrix")
    else:
        print('Confusion matrix, without normalization')

    print(cm)

    plt.imshow(cm, interpolation='nearest', cmap=cmap)
    plt.title(title)
    plt.colorbar()
    tick_marks = np.arange(len(classes))
    plt.xticks(tick_marks, classes, rotation=45)
    plt.yticks(tick_marks, classes)

    fmt = '.2f' if normalize else 'd'
    thresh = cm.max() / 2.
    for i, j in itertools.product(range(cm.shape[0]), range(cm.shape[1])):
        plt.text(j, i, format(cm[i, j], fmt),
                 horizontalalignment="center",
                 color="white" if cm[i, j] > thresh else "black")

    plt.tight_layout()
    plt.ylabel('True label')
    plt.xlabel('Predicted label')

# Compute confusion matrix
conf_matrix = confusion_matrix(y_test, y_pred)
21.7 Comparing randomized search and grid search for hyperparameter estimation

Compare randomized search and grid search for optimizing hyperparameters of a random forest. All parameters that influence the learning are searched simultaneously (except for the number of estimators, which poses a time / quality tradeoff).

The randomized search and the grid search explore exactly the same space of parameters. The result in parameter settings is quite similar, while the run time for randomized search is drastically lower.

The performance is slightly worse for the randomized search, though this is most likely a noise effect and would not carry over to a held-out test set.

Note that in practice, one would not search over this many different parameters simultaneously using grid search, but pick only the ones deemed most important.

Out:

RandomizedSearchCV took 3.50 seconds for 20 candidates parameter settings.
Model with rank: 1
Mean validation score: 0.927 (std: 0.004)
Parameters: {'bootstrap': False, 'criterion': 'entropy', 'max_depth': None, 'max_features': 5, 'min_samples_leaf': 4, 'min_samples_split': 5}

Model with rank: 2
Mean validation score: 0.925 (std: 0.008)
Parameters: {'bootstrap': False, 'criterion': 'entropy', 'max_depth': None, 'max_features': 7, 'min_samples_leaf': 3, 'min_samples_split': 5}

Model with rank: 3
Mean validation score: 0.923 (std: 0.007)
Parameters: {'bootstrap': False, 'criterion': 'entropy', 'max_depth': None, 'max_features': 4, 'min_samples_leaf': 1, 'min_samples_split': 7}

GridSearchCV took 32.17 seconds for 216 candidate parameter settings.
Model with rank: 1
Mean validation score: 0.937 (std: 0.012)
Parameters: {'bootstrap': False, 'criterion': 'gini', 'max_depth': None, 'max_features': 10, 'min_samples_leaf': 1, 'min_samples_split': 2}
Model with rank: 2
Mean validation score: 0.933 (std: 0.001)
Parameters: {'bootstrap': False, 'criterion': 'entropy', 'max_depth': None, 'max_features': 3, 'min_samples_leaf': 3, 'min_samples_split': 3}

Model with rank: 3
Mean validation score: 0.930 (std: 0.007)
Parameters: {'bootstrap': False, 'criterion': 'entropy', 'max_depth': None, 'max_features': 3, 'min_samples_leaf': 3, 'min_samples_split': 10}

21.7. Comparing randomized search and grid search for hyperparameter estimation
random_search = RandomizedSearchCV(clf, param_distributions=param_dist, n_iter=n_iter_search)

start = time()
random_search.fit(X, y)
print("RandomizedSearchCV took \%.2f seconds for \%d candidates" % ((time() - start), n_iter_search))
report(random_search.cv_results_)

# use a full grid over all parameters
param_grid = {
    "max_depth": [3, None],
    "max_features": [1, 3, 10],
    "min_samples_split": [2, 3, 10],
    "min_samples_leaf": [1, 3, 10],
    "bootstrap": [True, False],
    "criterion": ["gini", "entropy"]
}

# run grid search
grid_search = GridSearchCV(clf, param_grid=param_grid)
start = time()
grid_search.fit(X, y)
print("GridSearchCV took \%.2f seconds for \%d candidate parameter settings." % (time() - start, len(grid_search.cv_results_['params'])))
report(grid_search.cv_results_)

Total running time of the script: ( 0 minutes 35.801 seconds)

21.8 Nested versus non-nested cross-validation

This example compares non-nested and nested cross-validation strategies on a classifier of the iris data set. Nested cross-validation (CV) is often used to train a model in which hyperparameters also need to be optimized. Nested CV estimates the generalization error of the underlying model and its (hyper)parameter search. Choosing the parameters that maximize non-nested CV biases the model to the dataset, yielding an overly-optimistic score.

Model selection without nested CV uses the same data to tune model parameters and evaluate model performance. Information may thus “leak” into the model and overfit the data. The magnitude of this effect is primarily dependent on the size of the dataset and the stability of the model. See Cawley and Talbot¹ for an analysis of these issues.

To avoid this problem, nested CV effectively uses a series of train/validation/test set splits. In the inner loop (here executed by GridSearchCV), the score is approximately maximized by fitting a model to each training set, and then directly maximized in selecting (hyper)parameters over the validation set. In the outer loop (here in cross_val_score), generalization error is estimated by averaging test set scores over several dataset splits.

The example below uses a support vector classifier with a non-linear kernel to build a model with optimized hyperparameters by grid search. We compare the performance of non-nested and nested CV strategies by taking the difference between their scores.

See Also:

- Cross-validation: evaluating estimator performance

• Tuning the hyper-parameters of an estimator

References:

Non-Nested and Nested Cross Validation on Iris Dataset

Out:

Average difference of 0.007742 with std. dev. of 0.007688.

```python
from sklearn.datasets import load_iris
from matplotlib import pyplot as plt
from sklearn.svm import SVC
from sklearn.model_selection import GridSearchCV, cross_val_score, KFold
import numpy as np

print(__doc__)

# Number of random trials
NUM_TRIALS = 30
```
Load the dataset

```python
iris = load_iris()
X_iris = iris.data
y_iris = iris.target
```

Set up possible values of parameters to optimize over

```python
p_grid = {
    "C": [1, 10, 100],
    "gamma": [.01, .1]
}
```

We will use a Support Vector Classifier with "rbf" kernel

```python
svm = SVC(kernel="rbf")
```

Arrays to store scores

```python
non_nested_scores = np.zeros(NUM_TRIALS)
nested_scores = np.zeros(NUM_TRIALS)
```

Loop for each trial

```python
for i in range(NUM_TRIALS):
    # Choose cross-validation techniques for the inner and outer loops,
    # independently of the dataset.
    # E.g "LabelKFold", "LeaveOneOut", "LeaveOneLabelOut", etc.
    inner_cv = KFold(n_splits=4, shuffle=True, random_state=i)
    outer_cv = KFold(n_splits=4, shuffle=True, random_state=i)

    # Non_nested parameter search and scoring
    clf = GridSearchCV(estimator=svm, param_grid=p_grid, cv=inner_cv)
    clf.fit(X_iris, y_iris)
    non_nested_scores[i] = clf.best_score_

    # Nested CV with parameter optimization
    nested_score = cross_val_score(clf, X=X_iris, y=y_iris, cv=outer_cv)
    nested_scores[i] = nested_score.mean()

score_difference = non_nested_scores - nested_scores

print("Average difference of {0:6f} with std. dev. of {1:6f}.").
    .format(score_difference.mean(), score_difference.std()))
```

Plot scores on each trial for nested and non-nested CV

```python
plt.figure()
plt.subplot(211)
non_nested_scores_line, = plt.plot(non_nested_scores, color='r')
nested_line, = plt.plot(nested_scores, color='b')
plt.ylabel("score", fontsize="14")
plt.legend([non_nested_scores_line, nested_line],
    ["Non-Nested CV", "Nested CV"],
    bbox_to_anchor=(0, .4, .5, 0))
plt.title("Non-Nested and Nested Cross Validation on Iris Dataset",
    x=.5, y=1.1, fontsize="15")
```

Plot bar chart of the difference.

```python
plt.subplot(212)
difference_plot = plt.bar(range(NUM_TRIALS), score_difference)
plt.xlabel("Individual Trial ")
plt.legend([difference_plot],
    ["Non-Nested CV - Nested CV Score"],
    bbox_to_anchor=(0, .4, .5, 0))
```
21.9 Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV

Multiple metric parameter search can be done by setting the `scoring` parameter to a list of metric scorer names or a dict mapping the scorer names to the scorer callables.

The scores of all the scorers are available in the `cv_results_` dict at keys ending in `_<scorer_name>` (`'mean_test_precision', 'rank_test_precision', etc...)

The `best_estimator_`, `best_index_`, `best_score_` and `best_params_` correspond to the scorer (key) that is set to the `refit` attribute.

```python
import numpy as np
from matplotlib import pyplot as plt
from sklearn.datasets import make_hastie_10_2
from sklearn.model_selection import GridSearchCV
from sklearn.metrics import make_scorer
from sklearn.metrics import accuracy_score
from sklearn.tree import DecisionTreeClassifier

X, y = make_hastie_10_2(n_samples=8000, random_state=42)

scoring = {'AUC': 'roc_auc', 'Accuracy': make_scorer(accuracy_score)}

gs = GridSearchCV(DecisionTreeClassifier(random_state=42),
param_grid={'min_samples_split': range(2, 403, 10)},
scoring=scoring, cv=5, refit='AUC')

results = gs.fit(X, y)
```

21.9.1 Running GridSearchCV using multiple evaluation metrics

```python
X, y = make_hastie_10_2(n_samples=8000, random_state=42)

scoring = {'AUC': 'roc_auc', 'Accuracy': make_scorer(accuracy_score)}

gs = GridSearchCV(DecisionTreeClassifier(random_state=42),
param_grid={'min_samples_split': range(2, 403, 10)},
scoring=scoring, cv=5, refit='AUC')

results = gs.fit(X, y)
```
21.9.2 Plotting the result

```python
plt.figure(figsize=(13, 13))
plt.title("GridSearchCV evaluating using multiple scorers simultaneously",
          fontsize=16)
plt.xlabel("min_samples_split")
plt.ylabel("Score")
plt.grid()

ax = plt.axes()
ax.set_xlim(0, 402)
ax.set_ylim(0.73, 1)

# Get the regular numpy array from the MaskedArray
X_axis = np.array(results['param_min_samples_split'].data, dtype=float)

for scorer, color in zip(sorted(scoring), ['g', 'k']):
    for sample, style in (('train', '--'), ('test', '-')):
        sample_score_mean = results['mean_%s_%s' % (sample, scorer)]
        sample_score_std = results['std_%s_%s' % (sample, scorer)]
        ax.fill_between(X_axis, sample_score_mean - sample_score_std,
                        sample_score_mean + sample_score_std,
                        alpha=0.1 if sample == 'test' else 0, color=color)
        ax.plot(X_axis, sample_score_mean, style, color=color,
                alpha=1 if sample == 'test' else 0.7,
                label="%s (%s)" % (scorer, sample))

best_index = np.nonzero(results['rank_test_%s' % scorer] == 1)[0][0]
best_score = results['mean_test_%s' % scorer][best_index]

# Plot a dotted vertical line at the best score for that scorer marked by x
ax.plot([X_axis[best_index], X_axis[best_index]], [0, best_score],
        linestyle='--', color=color, marker='x', markeredgewidth=3, ms=8)

# Annotate the best score for that scorer
ax.annotate("%.2f" % best_score,
            (X_axis[best_index], best_score + 0.005))

plt.legend(loc="best")
plt.grid('off')
plt.show()
```
Total running time of the script: 0 minutes 25.673 seconds

21.10 Sample pipeline for text feature extraction and evaluation

The dataset used in this example is the 20 newsgroups dataset which will be automatically downloaded and then cached and reused for the document classification example.

You can adjust the number of categories by giving their names to the dataset loader or setting them to None to get the 20 of them.

Here is a sample output of a run on a quad-core machine:

Loading 20 newsgroups dataset for categories: ['alt.atheism', 'talk.religion.misc']
Performing grid search...
pipeline: ['vect', 'tfidf', 'clf']
parameters:
{'clf__alpha': (1.0000000000000001e-05, 9.9999999999999995e-07),
 'clf__n_iter': (10, 50, 80),
 'clf__penalty': ('l2', 'elasticnet'),
 'tfidf__use_idf': (True, False),
 'vect__max_n': (1, 2),
 'vect__max_df': (0.5, 0.75, 1.0),
 'vect__max_features': (None, 5000, 10000, 50000)}
done in 1737.030s

Best score: 0.940
Best parameters set:
clf__alpha: 9.9999999999999995e-07
clf__n_iter: 50
clf__penalty: 'elasticnet'
tfidf__use_idf: True
vect__max_n: 2
vect__max_df: 0.75
vect__max_features: 50000

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# License: BSD 3 clause

from __future__ import print_function
from pprint import pprint
from time import time
import logging

from sklearn.datasets import fetch_20newsgroups
from sklearn.feature_extraction.text import CountVectorizer
from sklearn.feature_extraction.text import TfidfTransformer
from sklearn.linear_model import SGDClassifier
from sklearn.pipeline import Pipeline

print(__doc__)

# Display progress logs on stdout
logging.basicConfig(level=logging.INFO,
                    format='%(asctime)s %(levelname)s %(message)s')

# Load some categories from the training set
categories = ['alt.atheism',
              'talk.religion.misc',
              ]
# Uncomment the following to do the analysis on all the categories
categories = None
print("Loading 20 newsgroups dataset for categories:")
print(categories)

data = fetch_20newsgroups(subset='train', categories=categories)
print("%d documents" % len(data.filenames))
print("%d categories" % len(data.target_names))
print()

# Define a pipeline combining a text feature extractor with a simple classifier
pipeline = Pipeline([
    ('vect', CountVectorizer()),
    ('tfidf', TfidfTransformer()),
    ('clf', SGDClassifier()),
])

# uncommenting more parameters will give better exploring power but will increase processing time in a combinatorial way
parameters = {
    'vect__max_df': (0.5, 0.75, 1.0),
    'vect__max_features': (None, 5000, 10000, 50000),
    'vect__ngram_range': ((1, 1), (1, 2)),  # unigrams or bigrams
    'tfidf__use_idf': (True, False),
    'tfidf__norm': ('l1', 'l2'),
    'clf__max_iter': (5,),
    'clf__alpha': (0.00001, 0.000001),
    'clf__penalty': ('l2', 'elasticnet'),
    'clf__n_iter': (10, 50, 80),
}

if __name__ == "__main__":
    # multiprocessing requires the fork to happen in a __main__ protected block
    # find the best parameters for both the feature extraction and the classifier
    grid_search = GridSearchCV(pipeline, parameters, n_jobs=-1, verbose=1)
    print("Performing grid search...")
    print("pipeline:", [name for name, _ in pipeline.steps])
    print("parameters:")
    pprint(parameters)
    t0 = time()
    grid_search.fit(data.data, data.target)
    print("done in %0.3fs" % (time() - t0))
    print()

    print("Best score: %0.3f" % grid_search.best_score_)
    print("Best parameters set:")
    best_parameters = grid_search.best_estimator_.get_params()
    for param_name in sorted(parameters.keys()):
        print("\t%s: %r" % (param_name, best_parameters[param_name]))

Total running time of the script: ( 0 minutes 0.000 seconds)
21.11 Receiver Operating Characteristic (ROC)

Example of Receiver Operating Characteristic (ROC) metric to evaluate classifier output quality.

ROC curves typically feature true positive rate on the Y axis, and false positive rate on the X axis. This means that the top left corner of the plot is the “ideal” point - a false positive rate of zero, and a true positive rate of one. This is not very realistic, but it does mean that a larger area under the curve (AUC) is usually better.

The “steepness” of ROC curves is also important, since it is ideal to maximize the true positive rate while minimizing the false positive rate.

21.11.1 Multiclass settings

ROC curves are typically used in binary classification to study the output of a classifier. In order to extend ROC curve and ROC area to multi-class or multi-label classification, it is necessary to binarize the output. One ROC curve can be drawn per label, but one can also draw a ROC curve by considering each element of the label indicator matrix as a binary prediction (micro-averaging).

Another evaluation measure for multi-class classification is macro-averaging, which gives equal weight to the classification of each label.

Note:

See also `sklearn.metrics.roc_auc_score`, Receiver Operating Characteristic (ROC) with cross validation.

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from itertools import cycle
from sklearn import svm, datasets
from sklearn.metrics import roc_curve, auc
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import label_binarize
from sklearn.multiclass import OneVsRestClassifier
from scipy import interp

# Import some data to play with
iris = datasets.load_iris()
X = iris.data
y = iris.target

# Binarize the output
y = label_binarize(y, classes=[0, 1, 2])
n_classes = y.shape[1]

# Add noisy features to make the problem harder
random_state = np.random.RandomState(0)
n_samples, n_features = X.shape
X = np.c_[X, random_state.randn(n_samples, 200 * n_features)]

# shuffle and split training and test sets
X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=.5,
```
# Learn to predict each class against the other
classifier = OneVsRestClassifier(svm.SVC(kernel='linear', probability=True,
                                      random_state=random_state))
y_score = classifier.fit(X_train, y_train).decision_function(X_test)

# Compute ROC curve and ROC area for each class
fpr = dict()
tpr = dict()
roc_auc = dict()
for i in range(n_classes):
    fpr[i], tpr[i], _ = roc_curve(y_test[:, i], y_score[:, i])
    roc_auc[i] = auc(fpr[i], tpr[i])

# Compute micro-average ROC curve and ROC area
fpr['micro'], tpr['micro'], _ = roc_curve(y_test.ravel(), y_score.ravel())
roc_auc['micro'] = auc(fpr['micro'], tpr['micro'])

Plot of a ROC curve for a specific class

plt.figure()
lw = 2
plt.plot(fpr[2], tpr[2], color='darkorange',
         lw=lw, label='ROC curve (area = %0.2f)' % roc_auc[2])
plt.plot([0, 1], [0, 1], color='navy', lw=lw, linestyle='--')
plt.xlim([0.0, 1.0])
plt.ylim([0.0, 1.05])
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Receiver operating characteristic example')
plt.legend(loc='lower right')
plt.show()
Plot ROC curves for the multiclass problem

```python
# Compute macro-average ROC curve and ROC area
# First aggregate all false positive rates
all_fpr = np.unique(np.concatenate([fpr[i] for i in range(n_classes)]))

# Then interpolate all ROC curves at this points
mean_tpr = np.zeros_like(all_fpr)
for i in range(n_classes):
    mean_tpr += interp(all_fpr, fpr[i], tpr[i])

# Finally average it and compute AUC
mean_tpr /= n_classes
fpr["macro"] = all_fpr
tpr["macro"] = mean_tpr
roc_auc["macro"] = auc(fpr["macro"], tpr["macro"],

# Plot all ROC curves
plt.figure()
plt.plot(fpr["micro"], tpr["micro"],
        label='micro-average ROC curve (area = {0:0.2f})'
        .format(roc_auc["micro"]),
        color='deeppink', linestyle=':', linewidth=4)
```
plt.plot(fpr["macro"], tpr["macro"],
        label='macro-average ROC curve (area = {0:.2f})'
        .format(roc_auc["macro"]),
        color='navy', linestyle=':', linewidth=4)

colors = cycle(['aqua', 'darkorange', 'cornflowerblue'])
for i, color in zip(range(n_classes), colors):
    plt.plot(fpr[i], tpr[i], color=color, lw=lw,
             label='ROC curve of class {0} (area = {1:.2f})'
             .format(i, roc_auc[i]))

plt.plot([0, 1], [0, 1], 'k--', lw=lw)
plt.xlim([0.0, 1.0])
plt.ylim([0.0, 1.05])
plt.xlabel('False Positive Rate')
plt.ylabel('True Positive Rate')
plt.title('Some extension of Receiver operating characteristic to multi-class')
plt.legend(loc="lower right")
plt.show()
### 21.12 Plotting Learning Curves

On the left side the learning curve of a naive Bayes classifier is shown for the digits dataset. Note that the training score and the cross-validation score are both not very good at the end. However, the shape of the curve can be found in more complex datasets very often: the training score is very high at the beginning and decreases and the cross-validation score is very low at the beginning and increases. On the right side we see the learning curve of an SVM with RBF kernel. We can see clearly that the training score is still around the maximum and the validation score could be increased with more training samples.

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn.naive_bayes import GaussianNB
from sklearn.svm import SVC
from sklearn.datasets import load_digits
from sklearn.model_selection import learning_curve
from sklearn.model_selection import ShuffleSplit

def plot_learning_curve(estimator, title, X, y, ylim=None, cv=None,
                        n_jobs=1, train_sizes=np.linspace(.1, 1.0, 5)):
    ""
    Generate a simple plot of the test and training learning curve.
    Parameters
```
estimator : object type that implements the "fit" and "predict" methods
An object of that type which is cloned for each validation.

title : string
Title for the chart.

X : array-like, shape (n_samples, n_features)
Training vector, where n_samples is the number of samples and
n_features is the number of features.

y : array-like, shape (n_samples) or (n_samples, n_features), optional
Target relative to X for classification or regression;
None for unsupervised learning.

ylim : tuple, shape (ymin, ymax), optional
Defines minimum and maximum yvalues plotted.

cv : int, cross-validation generator or an iterable, optional
Determines the cross-validation splitting strategy.
Possible inputs for cv are:
- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if `y` is binary or multiclass,
:class:`StratifiedKFold` used. If the estimator is not a classifier
or if `y` is neither binary nor multiclass, :class:`KFold` is used.

Refer :ref:`User Guide <cross_validation>` for the various
cross-validators that can be used here.

n_jobs : integer, optional
Number of jobs to run in parallel (default 1).

```python
plt.figure()
plt.title(title)
if ylim is not None:
    plt.ylim(*ylim)
plt.xlabel("Training examples")
plt.ylabel("Score")
train_sizes, train_scores, test_scores = learning_curve(
    estimator, X, y, cv=cv, n_jobs=n_jobs, train_sizes=train_sizes)
train_scores_mean = np.mean(train_scores, axis=1)
train_scores_std = np.std(train_scores, axis=1)
test_scores_mean = np.mean(test_scores, axis=1)
test_scores_std = np.std(test_scores, axis=1)
plt.grid()
plt.fill_between(train_sizes, train_scores_mean + train_scores_std,
    train_scores_mean + train_scores_std, alpha=0.1,
    color="r")
plt.fill_between(train_sizes, test_scores_mean + test_scores_std,
    test_scores_mean + test_scores_std, alpha=0.1, color="g")
plt.plot(train_sizes, train_scores_mean, 'o-', color="r",
    label="Training score")
plt.plot(train_sizes, test_scores_mean, 'o-', color="g",
    label="Test score")
```

label="Cross-validation score")
plt.legend(loc="best")
return plt
digits = load_digits()
X, y = digits.data, digits.target

title = "Learning Curves (Naive Bayes)"
# Cross validation with 100 iterations to get smoother mean test and train
# score curves, each time with 20% data randomly selected as a validation set.
cv = ShuffleSplit(n_splits=100, test_size=0.2, random_state=0)
estimator = GaussianNB()
plot_learning_curve(estimator, title, X, y, ylim=(0.7, 1.01), cv=cv, n_jobs=4)

title = "Learning Curves (SVM, RBF kernel, $\gamma=0.001$)"
# SVC is more expensive so we do a lower number of CV iterations:
cv = ShuffleSplit(n_splits=10, test_size=0.2, random_state=0)
estimator = SVC(gamma=0.001)
plot_learning_curve(estimator, title, X, y, (0.7, 1.01), cv=cv, n_jobs=4)
plt.show()

Total running time of the script: ( 0 minutes 10.378 seconds)

## 21.13 Precision-Recall

Example of Precision-Recall metric to evaluate classifier output quality.

Precision-Recall is a useful measure of success of prediction when the classes are very imbalanced. In information retrieval, precision is a measure of result relevancy, while recall is a measure of how many truly relevant results are returned.

The precision-recall curve shows the tradeoff between precision and recall for different threshold. A high area under the curve represents both high recall and high precision, where high precision relates to a low false positive rate, and high recall relates to a low false negative rate. High scores for both show that the classifier is returning accurate results (high precision), as well as returning a majority of all positive results (high recall).

A system with high recall but low precision returns many results, but most of its predicted labels are incorrect when compared to the training labels. A system with high precision but low recall is just the opposite, returning very few results, but most of its predicted labels are correct when compared to the training labels. An ideal system with high precision and high recall will return many results, with all results labeled correctly.

Precision ($P$) is defined as the number of true positives ($T_p$) over the number of true positives plus the number of false positives ($F_p$).

$$P = \frac{T_p}{T_p + F_p}$$

Recall ($R$) is defined as the number of true positives ($T_p$) over the number of true positives plus the number of false negatives ($F_n$).

$$R = \frac{T_p}{T_p + F_n}$$

These quantities are also related to the ($F_1$) score, which is defined as the harmonic mean of precision and recall.

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\[ F_1 = \frac{2PR}{P+R} \]

Note that the precision may not decrease with recall. The definition of precision \( \frac{T_p}{T_p + F_p} \) shows that lowering the threshold of a classifier may increase the denominator, by increasing the number of results returned. If the threshold was previously set too high, the new results may all be true positives, which will increase precision. If the previous threshold was about right or too low, further lowering the threshold will introduce false positives, decreasing precision.

Recall is defined as \( \frac{T_p}{T_p + F_n} \), where \( T_p + F_n \) does not depend on the classifier threshold. This means that lowering the classifier threshold may increase recall, by increasing the number of true positive results. It is also possible that lowering the threshold may leave recall unchanged, while the precision fluctuates.

The relationship between recall and precision can be observed in the stairstep area of the plot - at the edges of these steps a small change in the threshold considerably reduces precision, with only a minor gain in recall.

**Average precision** (AP) summarizes such a plot as the weighted mean of precisions achieved at each threshold, with the increase in recall from the previous threshold used as the weight:

\[
AP = \sum_n (R_n - R_{n-1}) P_n
\]

where \( P_n \) and \( R_n \) are the precision and recall at the \( n \)th threshold. A pair \((R_k, P_k)\) is referred to as an operating point.

AP and the trapezoidal area under the operating points (sklearn.metrics.auc) are common ways to summarize a precision-recall curve that lead to different results. Read more in the User Guide.

Precision-recall curves are typically used in binary classification to study the output of a classifier. In order to extend the precision-recall curve and average precision to multi-class or multi-label classification, it is necessary to binarize the output. One curve can be drawn per label, but one can also draw a precision-recall curve by considering each element of the label indicator matrix as a binary prediction (micro-averaging).

**Note:**

See also sklearn.metrics.average_precision_score, sklearn.metrics.recall_score, sklearn.metrics.precision_score, sklearn.metrics.f1_score

```python
from __future__ import print_function
```

### 21.13.1 In binary classification settings

**Create simple data**

Try to differentiate the two first classes of the iris data

```python
from sklearn import svm, datasets
from sklearn.model_selection import train_test_split
import numpy as np

iris = datasets.load_iris()
X = iris.data
y = iris.target

# Add noisy features
random_state = np.random.RandomState(0)
n_samples, n_features = X.shape
X = np.c_[X, random_state.randn(n_samples, 200 * n_features)]

# Limit to the two first classes, and split into training and test
```
X_train, X_test, y_train, y_test = train_test_split(X[y < 2], y[y < 2],
    test_size=.5,
    random_state=random_state)

# Create a simple classifier
classifier = svm.LinearSVC(random_state=random_state)
classifier.fit(X_train, y_train)
y_score = classifier.decision_function(X_test)

 Compute the average precision score

from sklearn.metrics import average_precision_score
average_precision = average_precision_score(y_test, y_score)

print('Average precision-recall score: {0:0.2f}'.format(
    average_precision))

Out:

Average precision-recall score: 0.88

Plot the Precision-Recall curve

from sklearn.metrics import precision_recall_curve
import matplotlib.pyplot as plt

precision, recall, _ = precision_recall_curve(y_test, y_score)

plt.step(recall, precision, color='b', alpha=0.2,
     where='post')
plt.fill_between(recall, precision, step='post', alpha=0.2,
     color='b')

plt.xlabel('Recall')
plt.ylabel('Precision')
plt.ylim([0.0, 1.05])
plt.xlim([0.0, 1.0])
plt.title('2-class Precision-Recall curve: AP={0:0.2f}'.format(
    average_precision))
21.13.2 In multi-label settings

Create multi-label data, fit, and predict

We create a multi-label dataset, to illustrate the precision-recall in multi-label settings

```python
from sklearn.preprocessing import label_binarize

# Use label_binarize to be multi-label like settings
Y = label_binarize(y, classes=[0, 1, 2])
n_classes = Y.shape[1]

# Split into training and test
X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=.5,
    random_state=random_state)

# We use OneVsRestClassifier for multi-label prediction
from sklearn.multiclass import OneVsRestClassifier

# Run classifier
classifier = OneVsRestClassifier(svm.LinearSVC(random_state=random_state))
classifier.fit(X_train, Y_train)
y_score = classifier.decision_function(X_test)
```
The average precision score in multi-label settings

```python
from sklearn.metrics import precision_recall_curve
from sklearn.metrics import average_precision_score

# For each class
precision = dict()
recall = dict()
average_precision = dict()
for i in range(n_classes):
    precision[i], recall[i], _ = precision_recall_curve(Y_test[:, i], y_score[:, i])
    average_precision[i] = average_precision_score(Y_test[:, i], y_score[:, i])

# A "micro-average": quantifying score on all classes jointly
precision["micro"], recall["micro"], _ = precision_recall_curve(Y_test.ravel(), y_score.ravel())
average_precision["micro"] = average_precision_score(Y_test, y_score, average="micro")

print('Average precision score, micro-averaged over all classes: {0:0.2f}').format(average_precision["micro"])  
```

Out:

```
Average precision score, micro-averaged over all classes: 0.43
```

Plot the micro-averaged Precision-Recall curve

```python
plt.figure()
plt.step(recall["micro"], precision["micro"], color='b', alpha=0.2, where='post')
plt.fill_between(recall["micro"], precision["micro"], step='post', alpha=0.2, color='b')
plt.xlabel('Recall')
plt.ylabel('Precision')
plt.ylim([0.0, 1.05])
plt.xlim([0.0, 1.0])
plt.title('Average precision score, micro-averaged over all classes: AP={0:0.2f}'.format(average_precision["micro"]))
```
Plot Precision-Recall curve for each class and iso-f1 curves

```python
from itertools import cycle

# setup plot details
plt.figure(figsize=(7, 8))
colors = cycle(['navy', 'turquoise', 'darkorange', 'cornflowerblue', 'teal'])

f_scores = np.linspace(0.2, 0.8, num=4)
lines = []
labels = []
for f_score in f_scores:
    x = np.linspace(0.01, 1)
    y = f_score * x / (2 * x - f_score)
    l, = plt.plot(x[y >= 0], y[y >= 0], color='gray', alpha=0.2)
    plt.annotate('f1={0:0.1f}'.format(f_score), xy=(0.9, y[45] + 0.02))
lines.append(l)
labels.append('iso-f1 curves')
l, = plt.plot(recall['micro'], precision['micro'], color='gold', lw=2)
lines.append(l)
labels.append('micro-average Precision-recall (area = {0:0.2f})'.format(average_precision['micro']))
for i, color in zip(range(n_classes), colors):
l, = plt.plot(recall[i], precision[i], color=color, lw=2)
lines.append(l)
labels.append('Precision-recall curve of class {0}'.format(i))

plt.legend(lines, labels)
plt.show()
```

21.13. Precision-Recall
lines.append(l)
labels.append('Precision-recall for class {0} (area = {1:0.2f})'
    ''.format(i, average_precision[i]))

fig = plt.gcf()
fig.subplots_adjust(bottom=0.25)
plt.xlim([0.0, 1.0])
plt.ylim([0.0, 1.05])
plt.xlabel('Recall')
plt.ylabel('Precision')
plt.title('Extension of Precision-Recall curve to multi-class')
plt.legend(lines, labels, loc=(0, -.38), prop=dict(size=14))

plt.show()
Extension of Precision-Recall curve to multi-class

- iso-f1 curves
- micro-average Precision-recall (area = 0.43)
- Precision-recall for class 0 (area = 0.56)
- Precision-recall for class 1 (area = 0.37)
- Precision-recall for class 2 (area = 0.46)

Total running time of the script: (0 minutes 0.219 seconds)
Examples concerning the `sklearn.multioutput` module.

### 22.1 Classifier Chain

Example of using classifier chain on a multilabel dataset.

For this example we will use the `yeast` dataset which contains 2417 datapoints each with 103 features and 14 possible labels. Each data point has at least one label. As a baseline we first train a logistic regression classifier for each of the 14 labels. To evaluate the performance of these classifiers we predict on a held-out test set and calculate the jaccard similarity score.

Next we create 10 classifier chains. Each classifier chain contains a logistic regression model for each of the 14 labels. The models in each chain are ordered randomly. In addition to the 103 features in the dataset, each model gets the predictions of the preceding models in the chain as features (note that by default at training time each model gets the true labels as features). These additional features allow each chain to exploit correlations among the classes. The Jaccard similarity score for each chain tends to be greater than that of the set independent logistic models.

Because the models in each chain are arranged randomly there is significant variation in performance among the chains. Presumably there is an optimal ordering of the classes in a chain that will yield the best performance. However we do not know that ordering a priori. Instead we can construct an voting ensemble of classifier chains by averaging the binary predictions of the chains and apply a threshold of 0.5. The Jaccard similarity score of the ensemble is greater than that of the independent models and tends to exceed the score of each chain in the ensemble (although this is not guaranteed with randomly ordered chains).
# Load a multi-label dataset
yeast = fetch_mldata('yeast')
X = yeast['data']
Y = yeast['target'].transpose().toarray()
X_train, X_test, Y_train, Y_test = train_test_split(X, Y, test_size=.2,
                                                     random_state=0)

# Fit an independent logistic regression model for each class using the
# OneVsRestClassifier wrapper.
ovr = OneVsRestClassifier(LogisticRegression())
ovr.fit(X_train, Y_train)
Y_pred_ovr = ovr.predict(X_test)
ovr_jaccard_score = jaccard_similarity_score(Y_test, Y_pred_ovr)

# Fit an ensemble of logistic regression classifier chains and take the
# take the average prediction of all the chains.
chains = [ClassifierChain(LogisticRegression(), order='random', random_state=i)
          for i in range(10)]
for chain in chains:
```python
classifier = ClassifierChain()
classifier.fit(X_train, y_train)

Y_pred_chains = np.array([chain.predict(X_test) for chain in classifier.chains])
chain_jaccard_scores = [jaccard_similarity_score(Y_test, Y_pred_chain >= .5) for Y_pred_chain in Y_pred_chains]

Y_pred_ensemble = Y_pred_chains.mean(axis=0)
ensemble_jaccard_score = jaccard_similarity_score(Y_test, Y_pred_ensemble >= .5)

model_scores = [ovr_jaccard_score] + chain_jaccard_scores
model_scores.append(ensemble_jaccard_score)
model_names = ('Independent', 'Chain 1', 'Chain 2', 'Chain 3', 'Chain 4', 'Chain 5', 'Chain 6', 'Chain 7', 'Chain 8', 'Chain 9', 'Chain 10', 'Ensemble')

x_pos = np.arange(len(model_names))

# Plot the Jaccard similarity scores for the independent model, each of the # chains, and the ensemble (note that the vertical axis on this plot does # not begin at 0).

fig, ax = plt.subplots(figsize=(7, 4))
ax.grid(True)
ax.set_title('Classifier Chain Ensemble Performance Comparison')
ax.set_xticks(x_pos)
ax.set_xticklabels(model_names, rotation='vertical')
ax.set_ylabel('Jaccard Similarity Score')
ax.set_ylim([min(model_scores) * .9, max(model_scores) * 1.1])
colors = ['r'] + ['b'] * len(chain_jaccard_scores) + ['g']
ax.bar(x_pos, model_scores, alpha=0.5, color=colors)
plt.tight_layout()
plt.show()
```

Total running time of the script: ( 0 minutes 4.975 seconds)
23.1 Anomaly detection with Local Outlier Factor (LOF)

This example presents the Local Outlier Factor (LOF) estimator. The LOF algorithm is an unsupervised outlier detection method which computes the local density deviation of a given data point with respect to its neighbors. It considers as outlier samples that have a substantially lower density than their neighbors.

The number of neighbors considered, (parameter n_neighbors) is typically chosen 1) greater than the minimum number of objects a cluster has to contain, so that other objects can be local outliers relative to this cluster, and 2) smaller than the maximum number of close by objects that can potentially be local outliers. In practice, such informations are generally not available, and taking n_neighbors=20 appears to work well in general.
import numpy as np
import matplotlib.pyplot as plt
from sklearn.neighbors import LocalOutlierFactor

np.random.seed(42)

# Generate train data
X = 0.3 * np.random.randn(100, 2)
# Generate some abnormal novel observations
X_outliers = np.random.uniform(low=-4, high=4, size=(20, 2))
X = np.r_[X + 2, X - 2, X_outliers]

# fit the model
clf = LocalOutlierFactor(n_neighbors=20)
y_pred = clf.fit_predict(X)
y_pred_outliers = y_pred[200:]

# plot the level sets of the decision function
xx, yy = np.meshgrid(np.linspace(-5, 5, 50), np.linspace(-5, 5, 50))
Z = clf._decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
plt.title("Local Outlier Factor (LOF)")
plt.contourf(xx, yy, Z, cmap=plt.cm.Blues_r)
23.2 Nearest Neighbors regression

Demonstrate the resolution of a regression problem using a k-Nearest Neighbor and the interpolation of the target using both barycenter and constant weights.
# Generate sample data
import numpy as np
import matplotlib.pyplot as plt
from sklearn import neighbors

np.random.seed(0)
X = np.sort(5 * np.random.rand(40, 1), axis=0)
T = np.linspace(0, 5, 500)[:, np.newaxis]
y = np.sin(X).ravel()

# Add noise to targets
y[::5] += 1 * (0.5 - np.random.rand(8))

# Fit regression model
n_neighbors = 5
for i, weights in enumerate(['uniform', 'distance']):
    knn = neighbors.KNeighborsRegressor(n_neighbors, weights=weights)
    y_ = knn.fit(X, y).predict(T)

    plt.subplot(2, 1, i + 1)
    plt.scatter(X, y, c='k', label='data')
    plt.plot(T, y_, c='g', label='prediction')
    plt.axis('tight')
    plt.legend()
    plt.title("KNeighborsRegressor \(k = %i\), weights = '%s'" % (n_neighbors, weights))

plt.show()

Total running time of the script: (0 minutes 0.089 seconds)

## 23.3 Nearest Neighbors Classification

Sample usage of Nearest Neighbors classification. It will plot the decision boundaries for each class.
```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap
from sklearn import neighbors, datasets

n_neighbors = 15

# import some data to play with
iris = datasets.load_iris()

# we only take the first two features. We could avoid this ugly
# slicing by using a two-dim dataset
X = iris.data[:, :2]
y = iris.target

h = .02  # step size in the mesh

# Create color maps

cmap_light = ListedColormap(['#FFAAAA', '#AAFFAA', '#AAAAFF'])
cmap_bold = ListedColormap(['#FF0000', '#00FF00', '#0000FF'])

for weights in ['uniform', 'distance']:
    # we create an instance of Neighbours Classifier and fit the data.
    clf = neighbors.KNeighborsClassifier(n_neighbors, weights=weights)
    clf.fit(X, y)

23.3. Nearest Neighbors Classification
# Plot the decision boundary. For that, we will assign a color to each point in the mesh 
# \([x_{\text{min}}, x_{\text{max}}] \times [y_{\text{min}}, y_{\text{max}}]\).

\[
x_{\text{min}}, x_{\text{max}} = X[:, 0].\text{min()} - 1, X[:, 0].\text{max()} + 1 \\
y_{\text{min}}, y_{\text{max}} = X[:, 1].\text{min()} - 1, X[:, 1].\text{max()} + 1 \\
xx, yy = \text{np.meshgrid}(\text{np.arange}(x_{\text{min}}, x_{\text{max}}, h), \\
                           \text{np.arange}(y_{\text{min}}, y_{\text{max}}, h))
\]

\[
Z = \text{clf.predict}(\text{np.c_[xx.ravel(), yy.ravel()]})
\]

# Put the result into a color plot

\[
Z = \text{Z.reshape}(xx.\text{shape})
\]

plt.figure()
plt.pcolormesh(xx, yy, Z, cmap=cmap_light)

# Plot also the training points

plt.scatter(X[:, 0], X[:, 1], c=y, cmap=cmap_bold, 
            edgecolor='k', s=20)
plt.xlim(xx.\text{min}(), xx.\text{max}())
plt.ylim(yy.\text{min}(), yy.\text{max}())
plt.title("3-Class classification (k = %i, weights = $'s')" \\
         % (n_neighbors, weights))

plt.show()
import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import ListedColormap
from sklearn import datasets
from sklearn.neighbors import NearestCentroid

n_neighbors = 15

# we create an instance of Neighbours Classifier and fit the data.
c = NearestCentroid(shrink_threshold=shrinkage)
c.fit(X, y)

print(c.predict(X))

# Plot the decision boundary. For that, we will assign a color to each
# point in the mesh [x_min, x_max]x[y_min, y_max].
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1

print(c.predict(X))
xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))
Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])

# Put the result into a color plot
Z = Z.reshape(xx.shape)
plt.figure()
plt.pcolormesh(xx, yy, Z, cmap=cmap_light)

# Plot also the training points
plt.scatter(X[:, 0], X[:, 1], c=y, cmap=cmap_bold,
            edgecolor='b', s=20)
plt.title("3-Class classification (shrink_threshold=$r$)"
         % shrinkage)
plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.142 seconds)

23.5 Kernel Density Estimation

This example shows how kernel density estimation (KDE), a powerful non-parametric density estimation technique, can be used to learn a generative model for a dataset. With this generative model in place, new samples can be drawn. These new samples reflect the underlying model of the data.
Selection from the input data

```
0 1 2 3 4 5 6 7 8 9 0
1 2 3 4 5 6 7 8 9 0 1
2 3 4 5 6 7 8 9 0 1 2
5 6 5 0 9 2 9 8 4 1 7
```

"New" digits drawn from the kernel density model

```
8 7 1 2 6 5 4 8 9 4 4
6 1 6 9 1 5 6 7 6 6 4
9 1 9 6 1 3 0 1 0 9 5
6 9 8 5 1 7 5 1 3 4 5
```

Out:

```
best bandwidth: 3.79269019073225
```
grid = GridSearchCV(KernelDensity(), params)
grid.fit(data)

print("best bandwidth: {0}".format(grid.best_estimator_.bandwidth))

# use the best estimator to compute the kernel density estimate
kde = grid.best_estimator_

# sample 44 new points from the data
new_data = kde.sample(44, random_state=0)
new_data = pca.inverse_transform(new_data)

# turn data into a 4x11 grid
new_data = new_data.reshape((4, 11, -1))
real_data = digits.data[:44].reshape((4, 11, -1))

# plot real digits and resampled digits
fig, ax = plt.subplots(9, 11, subplot_kw=dict(xticks=[], yticks=[]))
for j in range(11):
    for i in range(4):
        im = ax[i, j].imshow(real_data[i, j].reshape((8, 8)),
                             cmap=plt.cm.binary, interpolation='nearest')
        im.set_clim(0, 16)
        im = ax[i + 5, j].imshow(new_data[i, j].reshape((8, 8)),
                                  cmap=plt.cm.binary, interpolation='nearest')
        im.set_clim(0, 16)

ax[0, 5].set_title('Selection from the input data')
ax[5, 5].set_title('"New" digits drawn from the kernel density model')

plt.show()
Bradypus Variegatus  
Microromyos Minutus

Out:
- computing KDE in spherical coordinates
- plot coastlines from coverage
- computing KDE in spherical coordinates
- plot coastlines from coverage

# Author: Jake Vanderplas <jakevdp@cs.washington.edu>
#
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn.datasets import fetch_species_distributions
from sklearn.datasets.species_distributions import construct_grids
from sklearn.neighbors import KernelDensity

# if basemap is available, we'll use it.
# otherwise, we'll improvise later...
try:
    from mpl_toolkits.basemap import Basemap
    basemap = True
except ImportError:
    basemap = False

# Get matrices/arrays of species IDs and locations
data = fetch_species_distributions()
species_names = ['Bradypus Variegatus', 'Microryzomys Minutus']

Xtrain = np.vstack([data['train']['dd lat'],
                    data['train']['dd long']]).T
ytrain = np.array([d.decode('ascii').startswith('micro')
                    for d in data['train']['species']], dtype='int')
Xtrain *= np.pi / 180. # Convert lat/long to radians

# Set up the data grid for the contour plot
xgrid, ygrid = construct_grids(data)
X, Y = np.meshgrid(xgrid[::-5], ygrid[::-5][::-1])
land_reference = data.coverages[6][::5, ::5]
land_mask = (land_reference > -9999).ravel()

xy = np.vstack((Y.ravel(), X.ravel())).T
xy = xy[land_mask]
xy *= np.pi / 180.

# Plot map of South America with distributions of each species
fig = plt.figure()
fig.subplots_adjust(left=0.05, right=0.95, wspace=0.05)

for i in range(2):
    plt.subplot(1, 2, i + 1)
    # construct a kernel density estimate of the distribution
    print("- computing KDE in spherical coordinates")
kde = KernelDensity(bandwidth=0.04, metric='haversine',
                        kernel='gaussian', algorithm='ball_tree')
kde.fit(Xtrain[ytrain == i])

    # evaluate only on the land: -9999 indicates ocean
Z = -9999 + np.zeros(land_mask.shape[0])
Z[land_mask] = np.exp(kde.score_samples(xy))
Z = Z.reshape(X.shape)

    # plot contours of the density
levels = np.linspace(0, Z.max(), 25)
plt.contourf(X, Y, Z, levels=levels, cmap=plt.cm.Reds)

if basemap:
    print("- plot coastlines using basemap")
m = Basemap(projection='cyl', llcrnrlat=Y.min(),
               urcrnrlat=Y.max(), llcrnrlon=X.min(),
               urcrnrlon=X.max(), resolution='c')
m.drawcoastlines()
m.drawcountries()
else:
    print("- plot coastlines from coverage")
plt.contour(X, Y, land_reference,
levels=[-9999], colors="k",
linestyles="solid")
plt.xticks([])
plt.yticks([])
plt.title(species_names[i])
plt.show()

Total running time of the script: (0 minutes 7.507 seconds)

## 23.7 Simple 1D Kernel Density Estimation

This example uses the `sklearn.neighbors.KernelDensity` class to demonstrate the principles of Kernel Density Estimation in one dimension.

The first plot shows one of the problems with using histograms to visualize the density of points in 1D. Intuitively, a histogram can be thought of as a scheme in which a unit “block” is stacked above each point on a regular grid. As the top two panels show, however, the choice of gridding for these blocks can lead to wildly divergent ideas about the underlying shape of the density distribution. If we instead center each block on the point it represents, we get the estimate shown in the bottom left panel. This is a kernel density estimation with a “top hat” kernel. This idea can be generalized to other kernel shapes: the bottom-right panel of the first figure shows a Gaussian kernel density estimate over the same distribution.

Scikit-learn implements efficient kernel density estimation using either a Ball Tree or KD Tree structure, through the `sklearn.neighbors.KernelDensity` estimator. The available kernels are shown in the second figure of this example.

The third figure compares kernel density estimates for a distribution of 100 samples in 1 dimension. Though this example uses 1D distributions, kernel density estimation is easily and efficiently extensible to higher dimensions as well.
# Author: Jake Vanderplas <jakevdp@cs.washington.edu>

```python
import numpy as np
import matplotlib.pyplot as plt
from scipy.stats import norm
from sklearn.neighbors import KernelDensity

# Plot the progression of histograms to kernels
np.random.seed(1)
N = 20
X = np.concatenate((np.random.normal(0, 1, int(0.3 * N)),
                    np.random.normal(5, 1, int(0.7 * N))))[:, np.newaxis]
X_plot = np.linspace(-5, 10, 1000)[:, np.newaxis]
bins = np.linspace(-5, 10, 10)

fig, ax = plt.subplots(2, 2, sharex=True, sharey=True)
fig.subplots_adjust(hspace=0.05, wspace=0.05)

# histogram 1
ax[0, 0].hist(X[:, 0], bins=bins, fc='#AAAAFF', normed=True)
ax[0, 0].text(-3.5, 0.31, "Histogram")

# histogram 2
ax[0, 1].hist(X[:, 0], bins=bins + 0.75, fc='#AAAAFF', normed=True)
ax[0, 1].text(-3.5, 0.31, "Histogram, bins shifted")
```

Chapter 23. Nearest Neighbors
# tophat KDE
kde = KernelDensity(kernel='tophat', bandwidth=0.75).fit(X)
log_dens = kde.score_samples(X_plot)
ax[1, 0].fill(X_plot[:, 0], np.exp(log_dens), fc='#AAAAFF')
ax[1, 0].text(-3.5, 0.31, "Tophat Kernel Density")

# Gaussian KDE
kde = KernelDensity(kernel='gaussian', bandwidth=0.75).fit(X)
log_dens = kde.score_samples(X_plot)
ax[1, 1].fill(X_plot[:, 0], np.exp(log_dens), fc='#AAAAFF')
ax[1, 1].text(-3.5, 0.31, "Gaussian Kernel Density")

for axi in ax.ravel():
    axi.plot(X[:, 0], np.zeros(X.shape[0]) - 0.01, '+k')
    axi.set_xlim(-4, 9)
    axi.set_ylim(-0.02, 0.34)

for axi in ax[:, 0]:
    axi.set_ylabel('Normalized Density')

for axi in ax[1, :]:
    axi.set_xlabel('x')

#----------------------------------------------------------------------
# Plot all available kernels
X_plot = np.linspace(-6, 6, 1000)[:, None]
X_src = np.zeros((1, 1))
fig, ax = plt.subplots(2, 3, sharex=True, sharey=True)
fig.subplots_adjust(left=0.05, right=0.95, hspace=0.05, wspace=0.05)

def format_func(x, loc):
    if x == 0:
        return '0'
    elif x == 1:
        return 'h'
    elif x == -1:
        return '-h'
    else:
        return '\$%ih\$' % x

for i, kernel in enumerate(['gaussian', 'tophat', 'epanechnikov',
                             'exponential', 'linear', 'cosine']):
    axi = ax.ravel()[i]
    log_dens = KernelDensity(kernel=kernel).fit(X_src).score_samples(X_plot)
    axi.fill(X_plot[:, 0], np.exp(log_dens), '-k', fc='#AAAAFF')
    axi.text(-2.6, 0.95, kernel)
    axi.xaxis.set_major_formatter(plt.FuncFormatter(format_func))
    axi.xaxis.set_major_locator(plt.MultipleLocator(1))
    axi.yaxis.set_major_locator(plt.NullLocator())
    axi.set_ylim(0, 1.05)
    axi.set_xlim(-2.9, 2.9)
ax[0, 1].set_title('Available Kernels')
# Plot a 1D density example

N = 100
np.random.seed(1)
X = np.concatenate((np.random.normal(0, 1, int(0.3 * N)),
np.random.normal(5, 1, int(0.7 * N))))[:, np.newaxis]

X_plot = np.linspace(-5, 10, 1000)[:, np.newaxis]
true_dens = (0.3 * norm(0, 1).pdf(X_plot[:, 0])
+ 0.7 * norm(5, 1).pdf(X_plot[:, 0]))

fig, ax = plt.subplots()
ax.fill(X_plot[:, 0], true_dens, fc='black', alpha=0.2,
label='input distribution')

for kernel in ['gaussian', 'tophat', 'epanechnikov']:
kde = KernelDensity(kernel=kernel, bandwidth=0.5).fit(X)
log_dens = kde.score_samples(X_plot)
ax.plot(X_plot[:, 0], np.exp(log_dens), '-',
label="kernel = '{0}'".format(kernel))

ax.text(6.0, 0.38, "N={0} points".format(N))
ax.legend(loc='upper left')
ax.plot(X[:, 0], -0.005 - 0.01 * np.random.random(X.shape[0]), '+k')

ax.set_xlim(-4, 9)
ax.set_ylim(-0.02, 0.4)
plt.show()
Examples concerning the `sklearn.neural_network` module.

### 24.1 Visualization of MLP weights on MNIST

Sometimes looking at the learned coefficients of a neural network can provide insight into the learning behavior. For example if weights look unstructured, maybe some were not used at all, or if very large coefficients exist, maybe regularization was too low or the learning rate too high.

This example shows how to plot some of the first layer weights in a MLPClassifier trained on the MNIST dataset.

The input data consists of 28x28 pixel handwritten digits, leading to 784 features in the dataset. Therefore the first layer weight matrix have the shape (784, `hidden_layer_sizes[0]`). We can therefore visualize a single column of the weight matrix as a 28x28 pixel image.

To make the example run faster, we use very few hidden units, and train only for a very short time. Training longer would result in weights with a much smoother spatial appearance.
Out:

<table>
<thead>
<tr>
<th>Iteration</th>
<th>Loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>0.32212731</td>
</tr>
<tr>
<td>2</td>
<td>0.15738787</td>
</tr>
<tr>
<td>3</td>
<td>0.11647274</td>
</tr>
<tr>
<td>4</td>
<td>0.09631113</td>
</tr>
<tr>
<td>5</td>
<td>0.08074513</td>
</tr>
<tr>
<td>6</td>
<td>0.07163224</td>
</tr>
<tr>
<td>7</td>
<td>0.06351392</td>
</tr>
<tr>
<td>8</td>
<td>0.05694146</td>
</tr>
<tr>
<td>9</td>
<td>0.05213487</td>
</tr>
<tr>
<td>10</td>
<td>0.04708320</td>
</tr>
</tbody>
</table>

Training set score: 0.985733
Test set score: 0.971000

```python
print(__doc__)

import matplotlib.pyplot as plt
from sklearn.datasets import fetch_mldata
from sklearn.neural_network import MLPClassifier
```
24.2 Compare Stochastic learning strategies for MLPClassifier

This example visualizes some training loss curves for different stochastic learning strategies, including SGD and Adam. Because of time-constraints, we use several small datasets, for which L-BFGS might be more suitable. The general trend shown in these examples seems to carry over to larger datasets, however.

Note that those results can be highly dependent on the value of `learning_rate_init`. 

Total running time of the script: (0 minutes 13.867 seconds)
Out:

learning on dataset iris
training: constant learning-rate
Training set score: 0.980000
Training set loss: 0.096922
training: constant with momentum
Training set score: 0.980000
Training set loss: 0.049530
training: constant with Nesterov's momentum
Training set score: 0.980000
Training set loss: 0.049542
training: inv-scaling learning-rate
Training set score: 0.360000
Training set loss: 0.979193
training: inv-scaling with momentum
Training set score: 0.860000
Training set loss: 0.504017
training: inv-scaling with Nesterov's momentum
Training set score: 0.860000
Training set loss: 0.504760
training: adam
Training set score: 0.980000
Training set loss: 0.045531

learning on dataset digits
training: constant learning-rate
Training set score: 0.956038
Training set loss: 0.243802
<table>
<thead>
<tr>
<th>Training strategy</th>
<th>Training set score</th>
<th>Training set loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant with momentum</td>
<td>0.92766</td>
<td>0.041297</td>
</tr>
<tr>
<td>constant with Nesterov's momentum</td>
<td>0.993879</td>
<td>0.042898</td>
</tr>
<tr>
<td>inv-scaling learning-rate</td>
<td>0.63884</td>
<td>1.855465</td>
</tr>
<tr>
<td>inv-scaling with momentum</td>
<td>0.912632</td>
<td>0.290584</td>
</tr>
<tr>
<td>inv-scaling with Nesterov's momentum</td>
<td>0.909293</td>
<td>0.318387</td>
</tr>
<tr>
<td>adam</td>
<td>0.991653</td>
<td>0.045934</td>
</tr>
</tbody>
</table>

Learning on dataset circles

<table>
<thead>
<tr>
<th>Training strategy</th>
<th>Training set score</th>
<th>Training set loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant learning-rate</td>
<td>0.84000</td>
<td>0.601052</td>
</tr>
<tr>
<td>constant with momentum</td>
<td>0.940000</td>
<td>0.157334</td>
</tr>
<tr>
<td>constant with Nesterov's momentum</td>
<td>0.940000</td>
<td>0.154453</td>
</tr>
<tr>
<td>inv-scaling learning-rate</td>
<td>0.500000</td>
<td>0.692470</td>
</tr>
<tr>
<td>inv-scaling with momentum</td>
<td>0.500000</td>
<td>0.689143</td>
</tr>
<tr>
<td>inv-scaling with Nesterov's momentum</td>
<td>0.500000</td>
<td>0.689751</td>
</tr>
<tr>
<td>adam</td>
<td>0.940000</td>
<td>0.150527</td>
</tr>
</tbody>
</table>

Learning on dataset moons

<table>
<thead>
<tr>
<th>Training strategy</th>
<th>Training set score</th>
<th>Training set loss</th>
</tr>
</thead>
<tbody>
<tr>
<td>constant learning-rate</td>
<td>0.850000</td>
<td>0.341523</td>
</tr>
<tr>
<td>constant with momentum</td>
<td>0.850000</td>
<td>0.336188</td>
</tr>
<tr>
<td>constant with Nesterov's momentum</td>
<td>0.850000</td>
<td>0.335919</td>
</tr>
<tr>
<td>inv-scaling learning-rate</td>
<td>0.500000</td>
<td>0.689015</td>
</tr>
<tr>
<td>inv-scaling with momentum</td>
<td>0.830000</td>
<td>0.512595</td>
</tr>
</tbody>
</table>
Scikit-learn user guide, Release 0.20.dev0

Training set score: 0.830000
Training set loss: 0.513034

Training set score: 0.930000
Training set loss: 0.170087

```
print(__doc__)
import matplotlib.pyplot as plt
from sklearn.neural_network import MLPClassifier
from sklearn.preprocessing import MinMaxScaler
from sklearn import datasets

# different learning rate schedules and momentum parameters
params = [{'solver': 'sgd', 'learning_rate': 'constant', 'momentum': 0, 'learning_rate_init': 0.2},
          {'solver': 'sgd', 'learning_rate': 'constant', 'momentum': .9, 'nesterovs_momentum': False, 'learning_rate_init': 0.2},
          {'solver': 'sgd', 'learning_rate': 'constant', 'momentum': .9, 'nesterovs_momentum': True, 'learning_rate_init': 0.2},
          {'solver': 'sgd', 'learning_rate': 'invscaling', 'momentum': 0, 'learning_rate_init': 0.2},
          {'solver': 'sgd', 'learning_rate': 'invscaling', 'momentum': .9, 'nesterovs_momentum': True, 'learning_rate_init': 0.2},
          {'solver': 'sgd', 'learning_rate': 'invscaling', 'momentum': .9, 'nesterovs_momentum': False, 'learning_rate_init': 0.2},
          {'solver': 'adam', 'learning_rate_init': 0.01}]

labels = ['constant learning-rate', 'constant with momentum', 'constant with Nesterov's momentum', 'inv-scaling learning-rate', 'inv-scaling with momentum', 'inv-scaling with Nesterov's momentum', 'adam']

plot_args = [{'c': 'red', 'linestyle': '-'},
              {'c': 'green', 'linestyle': '-'},
              {'c': 'blue', 'linestyle': '-'},
              {'c': 'red', 'linestyle': '--'},
              {'c': 'green', 'linestyle': '--'},
              {'c': 'blue', 'linestyle': '--'},
              {'c': 'black', 'linestyle': '--'}]

def plot_on_dataset(X, y, ax, name):
    # for each dataset, plot learning for each learning strategy
    print("learning on dataset "+ name)
    ax.set_title(name)
    X = MinMaxScaler().fit_transform(X)
    mlp = []
    if name == "digits":
        # digits is larger but converges fairly quickly
        max_iter = 15
    else:
        max_iter = 400
```


```python
for label, param in zip(labels, params):
    print("training: \$s \% label")
    mlp = MLPClassifier(verbose=0, random_state=0,
                         max_iter=max_iter, **param)
    mlp.fit(X, y)
    mlp.scores.append(mlp)
    print("Training set score: \$f \% mlp.score(X, y)")
    print("Training set loss: \$f \% mlp.loss_")
    for mlp, label, args in zip(mlps, labels, plot_args):
        ax.plot(mlp.loss_curve_, label=label, **args)

fig, axes = plt.subplots(2, 2, figsize=(15, 10))
# load / generate some toy datasets
iris = datasets.load_iris()
digits = datasets.load_digits()
data_sets = [(iris.data, iris.target),
             (digits.data, digits.target),
             datasets.make_circles(noise=0.2, factor=0.5, random_state=1),
             datasets.make_moons(noise=0.3, random_state=0)]

for ax, data, name in zip(axes.ravel(), data_sets, ['iris', 'digits',
                                                      'circles', 'moons']):
    plot_on_dataset(*data, ax=ax, name=name)

fig.legend(ax.get_lines(), labels, ncol=3, loc="upper center")
plt.show()
```

**Total running time of the script:** ( 0 minutes 7.180 seconds)

## 24.3 Restricted Boltzmann Machine features for digit classification

For greyscale image data where pixel values can be interpreted as degrees of blackness on a white background, like handwritten digit recognition, the Bernoulli Restricted Boltzmann machine model (`BernoulliRBM`) can perform effective non-linear feature extraction.

In order to learn good latent representations from a small dataset, we artificially generate more labeled data by perturbing the training data with linear shifts of 1 pixel in each direction.

This example shows how to build a classification pipeline with a BernoulliRBM feature extractor and a `LogisticRegression` classifier. The hyperparameters of the entire model (learning rate, hidden layer size, regularization) were optimized by grid search, but the search is not reproduced here because of runtime constraints.

Logistic regression on raw pixel values is presented for comparison. The example shows that the features extracted by the BernoulliRBM help improve the classification accuracy.
100 components extracted by RBM

Logistic regression using RBM features:

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.99</td>
<td>0.99</td>
<td>0.99</td>
<td>174</td>
</tr>
<tr>
<td>1</td>
<td>0.92</td>
<td>0.95</td>
<td>0.93</td>
<td>184</td>
</tr>
<tr>
<td>2</td>
<td>0.95</td>
<td>0.98</td>
<td>0.97</td>
<td>166</td>
</tr>
<tr>
<td>3</td>
<td>0.97</td>
<td>0.91</td>
<td>0.94</td>
<td>194</td>
</tr>
<tr>
<td>4</td>
<td>0.97</td>
<td>0.95</td>
<td>0.96</td>
<td>186</td>
</tr>
<tr>
<td>5</td>
<td>0.93</td>
<td>0.93</td>
<td>0.93</td>
<td>181</td>
</tr>
<tr>
<td></td>
<td></td>
<td></td>
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<tr>
<td>---</td>
<td>---</td>
<td>---</td>
<td>---</td>
<td>---</td>
</tr>
<tr>
<td>6</td>
<td>0.98</td>
<td>0.97</td>
<td>0.97</td>
<td>207</td>
</tr>
<tr>
<td>7</td>
<td>0.95</td>
<td>1.00</td>
<td>0.97</td>
<td>154</td>
</tr>
<tr>
<td>8</td>
<td>0.90</td>
<td>0.88</td>
<td>0.89</td>
<td>182</td>
</tr>
<tr>
<td>9</td>
<td>0.91</td>
<td>0.93</td>
<td>0.92</td>
<td>169</td>
</tr>
<tr>
<td>avg / total</td>
<td>0.95</td>
<td>0.95</td>
<td>0.95</td>
<td>1797</td>
</tr>
</tbody>
</table>

Logistic regression using raw pixel features:

<table>
<thead>
<tr>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.85</td>
<td>0.94</td>
<td>0.89</td>
</tr>
<tr>
<td>1</td>
<td>0.57</td>
<td>0.55</td>
<td>0.56</td>
</tr>
<tr>
<td>2</td>
<td>0.72</td>
<td>0.85</td>
<td>0.78</td>
</tr>
<tr>
<td>3</td>
<td>0.76</td>
<td>0.74</td>
<td>0.75</td>
</tr>
<tr>
<td>4</td>
<td>0.85</td>
<td>0.82</td>
<td>0.84</td>
</tr>
<tr>
<td>5</td>
<td>0.74</td>
<td>0.75</td>
<td>0.75</td>
</tr>
<tr>
<td>6</td>
<td>0.93</td>
<td>0.88</td>
<td>0.91</td>
</tr>
<tr>
<td>7</td>
<td>0.86</td>
<td>0.90</td>
<td>0.88</td>
</tr>
<tr>
<td>8</td>
<td>0.68</td>
<td>0.55</td>
<td>0.61</td>
</tr>
<tr>
<td>9</td>
<td>0.71</td>
<td>0.74</td>
<td>0.72</td>
</tr>
<tr>
<td>avg / total</td>
<td>0.77</td>
<td>0.77</td>
<td>0.77</td>
</tr>
</tbody>
</table>

```
from __future__ import print_function

print(__doc__)

# Authors: Yann N. Dauphin, Vlad Niculae, Gabriel Synnaeve
# License: BSD

import numpy as np
import matplotlib.pyplot as plt

from scipy.ndimage import convolve
from sklearn import linear_model, datasets, metrics
from sklearn.model_selection import train_test_split
from sklearn.neural_network import BernoulliRBM
from sklearn.pipeline import Pipeline

# Setting up

def nudge_dataset(X, Y):
    ""
    This produces a dataset 5 times bigger than the original one,
    by moving the 8x8 images in X around by 1px to left, right, down, up
    """
    direction_vectors = [
        [0, 1, 0],
        [0, 0, 1],
        [0, 0, 0]])
```
```python
[[0, 0, 0],
 [1, 0, 0],
 [0, 0, 0]],

[[0, 0, 0],
 [0, 0, 1],
 [0, 0, 0]],

[[0, 0, 0],
 [0, 0, 0],
 [0, 1, 0]]

shift = lambda x, w: convolve(x.reshape((8, 8)), mode='constant', weights=w).ravel()
X = np.concatenate([X] +
[np.apply_along_axis(shift, 1, X, vector)
 for vector in direction_vectors])
Y = np.concatenate([Y for _ in range(5)], axis=0)
return X, Y

# Load Data
digits = datasets.load_digits()
X = np.asarray(digits.data, 'float32')
X, Y = nudge_dataset(X, digits.target)
X = (X - np.min(X, 0)) / (np.max(X, 0) + 0.0001) # 0-1 scaling
X_train, X_test, Y_train, Y_test = train_test_split(X, Y,
 test_size=0.2,
 random_state=0)

# Models we will use
logistic = linear_model.LogisticRegression()
rbm = BernoulliRBM(random_state=0, verbose=True)
classifier = Pipeline(steps=[('rbm', rbm), ('logistic', logistic)])

# Hyper-parameters. These were set by cross-validation,
# using a GridSearchCV. Here we are not performing cross-validation to
# save time.
rbm.learning_rate = 0.06
rbm.n_iter = 20
# More components tend to give better prediction performance, but larger
# fitting time
rbm.n_components = 100
logistic.C = 6000.0

# Training RBM-Logistic Pipeline
classifier.fit(X_train, Y_train)

# Training Logistic regression
logistic_classifier = linear_model.LogisticRegression(C=100.0)
logistic_classifier.fit(X_train, Y_train)
```

**Chapter 24. Neural Networks**
# Evaluation

print()
print("Logistic regression using RBM features:

%s

" % (metrics.classification_report(
    Y_test,
    classifier.predict(X_test)))).

print("Logistic regression using raw pixel features:

%s

" % (metrics.classification_report(
    Y_test,
    logistic_classifier.predict(X_test)))).

# Plotting

plt.figure(figsize=(4.2, 4))

for i, comp in enumerate(rbm.components_):
    plt.subplot(10, 10, i + 1)
    plt.imshow(comp.reshape((8, 8)), cmap=plt.cm.gray_r,
               interpolation='nearest')
    plt.xticks(())
    plt.yticks(())

plt.suptitle('100 components extracted by RBM', fontsize=16)
plt.subplots_adjust(0.08, 0.02, 0.92, 0.85, 0.08, 0.23)

plt.show()

Total running time of the script: ( 0 minutes 34.752 seconds)

## 24.4 Varying regularization in Multi-layer Perceptron

A comparison of different values for regularization parameter ‘alpha’ on synthetic datasets. The plot shows that different alphas yield different decision functions.

Alpha is a parameter for regularization term, aka penalty term, that combats overfitting by constraining the size of the weights. Increasing alpha may fix high variance (a sign of overfitting) by encouraging smaller weights, resulting in a decision boundary plot that appears with lesser curvatures. Similarly, decreasing alpha may fix high bias (a sign of underfitting) by encouraging larger weights, potentially resulting in a more complicated decision boundary.
from sklearn.datasets import make_moons, make_circles, make_classification
from sklearn.neural_network import MLPClassifier

h = .02  # step size in the mesh

alphas = np.logspace(-5, 3, 5)
names = []
for i in alphas:
    names.append('alpha ' + str(i))

classifiers = []
for i in alphas:
    classifiers.append(MLPClassifier(alpha=i, random_state=1))

X, y = make_classification(n_features=2, n_redundant=0, n_informative=2,
                           random_state=0, n_clusters_per_class=1)
rng = np.random.RandomState(2)
X += 2 * rng.uniform(size=X.shape)
linearly_separable = (X, y)
datasets = [make_moons(noise=0.3, random_state=0),
            make_circles(noise=0.2, factor=0.5, random_state=1),
            linearly_separable]
```python
figure = plt.figure(figsize=(17, 9))
i = 1

# iterate over datasets
for X, y in datasets:
    # preprocess dataset, split into training and test part
    X = StandardScaler().fit_transform(X)
    X_train, X_test, y_train, y_test = train_test_split(X, y, test_size=.4)

    x_min, x_max = X[:, 0].min() - .5, X[:, 0].max() + .5
    y_min, y_max = X[:, 1].min() - .5, X[:, 1].max() + .5
    xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                        np.arange(y_min, y_max, h))

    # just plot the dataset first
    cm = plt.cm.RdBu
    cm_bright = ListedColormap(['#FF0000', '#0000FF'])
    ax = plt.subplot(len(datasets), len(classifiers) + 1, i)
    # Plot the training points
    ax.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cm_bright)
    # and testing points
    ax.scatter(X_test[:, 0], X_test[:, 1], c=y_test, cmap=cm_bright, alpha=0.6)
    ax.set_xlim(xx.min(), xx.max())
    ax.set_ylim(yy.min(), yy.max())
    ax.set_xticks(())
    ax.set_yticks(())
    i += 1

# iterate over classifiers
for name, clf in zip(names, classifiers):
    ax = plt.subplot(len(datasets), len(classifiers) + 1, i)
    clf.fit(X_train, y_train)
    score = clf.score(X_test, y_test)

    # Plot the decision boundary. For that, we will assign a color to each
    # point in the mesh [x_min, x_max]x[y_min, y_max].
    if hasattr(clf, "decision_function"):
        Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
    else:
        Z = clf.predict_proba(np.c_[xx.ravel(), yy.ravel()])[:, 1]

    # Put the result into a color plot
    Z = Z.reshape(xx.shape)
    ax.contourf(xx, yy, Z, cmap=cm, alpha=.8)

    # Plot also the training points
    ax.scatter(X_train[:, 0], X_train[:, 1], c=y_train, cmap=cm_bright,
               edgecolors='black', s=25)
    # and testing points
    ax.scatter(X_test[:, 0], X_test[:, 1], c=y_test, cmap=cm_bright,
               edgecolors='black', s=25)
    ax.set_xlim(xx.min(), xx.max())
    ax.set_ylim(yy.min(), yy.max())
    ax.set_xticks(())
    ax.set_yticks(())
    ax.set_title(name)
    ax.text(xx.max() - .3, yy.min() + .3, ('%.2f' % score).lstrip('0'),
            size=15, horizontalalignment='right')
```

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i += 1

figure.subplots_adjust(left=.02, right=.98)
plt.show()

**Total running time of the script:** ( 0 minutes 5.192 seconds)
Examples concerning the `sklearn.preprocessing` module.

### 25.1 Using FunctionTransformer to select columns

Shows how to use a function transformer in a pipeline. If you know your dataset’s first principle component is irrelevant for a classification task, you can use the FunctionTransformer to select all but the first column of the PCA transformed data.

```python
import matplotlib.pyplot as plt
import numpy as np
```

```python
import matplotlib.pyplot as plt
import numpy as np
```
from sklearn.model_selection import train_test_split
from sklearn.decomposition import PCA
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import FunctionTransformer

def _generate_vector(shift=0.5, noise=15):
    return np.arange(1000) + (np.random.rand(1000) - shift) * noise

def generate_dataset():
    ""
    This dataset is two lines with a slope ~ 1, where one has
    a y offset of ~100
    ""
    return np.vstack((
        np.vstack((
            _generate_vector(),
            _generate_vector() + 100,
        )).T,
        np.vstack((
            _generate_vector(),
            _generate_vector(),
        )).T,
    )), np.hstack((np.zeros(1000), np.ones(1000)))

def all_but_first_column(X):
    return X[:, 1:]

def drop_first_component(X, y):
    ""
    Create a pipeline with PCA and the column selector and use it to
    transform the dataset.
    ""
    pipeline = make_pipeline(
        PCA(), FunctionTransformer(all_but_first_column),
    )
    X_train, X_test, y_train, y_test = train_test_split(X, y)
    pipeline.fit(X_train, y_train)
    return pipeline.transform(X_test), y_test

if __name__ == '__main__':
    X, y = generate_dataset()
    lw = 0
    plt.figure()
    plt.scatter(X[:, 0], X[:, 1], c=y, lw=lw)
    plt.figure()
    X_transformed, y_transformed = drop_first_component(*generate_dataset())
    plt.scatter(
        X_transformed[:, 0],
        np.zeros(len(X_transformed)),
        c=y_transformed,
        lw=lw,
        s=60
    )
Feature scaling though standardization (or Z-score normalization) can be an important preprocessing step for many machine learning algorithms. Standardization involves rescaling the features such that they have the properties of a standard normal distribution with a mean of zero and a standard deviation of one.

While many algorithms (such as SVM, K-nearest neighbors, and logistic regression) require features to be normalized, intuitively we can think of Principle Component Analysis (PCA) as being a prime example of when normalization is important. In PCA we are interested in the components that maximize the variance. If one component (e.g. human height) varies less than another (e.g. weight) because of their respective scales (meters vs. kilos), PCA might determine that the direction of maximal variance more closely corresponds with the ‘weight’ axis, if those features are not scaled. As a change in height of one meter can be considered much more important than the change in weight of one kilogram, this is clearly incorrect.

To illustrate this, PCA is performed comparing the use of data with `StandardScaler` applied, to unscaled data. The results are visualized and a clear difference noted. The 1st principal component in the unscaled set can be seen. It can be seen that feature #13 dominates the direction, being a whole two orders of magnitude above the other features. This is contrasted when observing the principal component for the scaled version of the data. In the scaled version, the orders of magnitude are roughly the same across all the features.

The dataset used is the Wine Dataset available at UCI. This dataset has continuous features that are heterogeneous in scale due to differing properties that they measure (i.e alcohol content, and malic acid).

The transformed data is then used to train a naive Bayes classifier, and a clear difference in prediction accuracies is observed wherein the dataset which is scaled before PCA vastly outperforms the unscaled version.
Output:

Prediction accuracy **for** the normal test dataset **with** PCA
81.48%

Prediction accuracy **for** the standardized test dataset **with** PCA
98.15%

PC 1 **without** scaling:
\[
\begin{bmatrix}
1.76e-03 & -8.36e-04 & 1.55e-04 & -5.31e-03 & 2.02e-02 & 1.02e-03 \\
1.53e-03 & -1.12e-04 & 6.31e-04 & 2.33e-03 & 1.54e-04 & 7.43e-04 \\
1.00e+00
\end{bmatrix}
\]

PC 1 **with** scaling:
\[
\begin{bmatrix}
0.13 & -0.26 & -0.01 & -0.23 & 0.16 & 0.39 & 0.42 & -0.28 & 0.33 & -0.11 & 0.3 & 0.38 & 0.28
\end{bmatrix}
\]

```python
from __future__ import print_function
from sklearn.model_selection import train_test_split
from sklearn.preprocessing import StandardScaler
from sklearn.decomposition import PCA
```
from sklearn.naive_bayes import GaussianNB
from sklearn import metrics
import matplotlib.pyplot as plt
from sklearn.datasets import load_wine
from sklearn.pipeline import make_pipeline
print(__doc__)

# Code source: Tyler Lanigan <tylerlanigan@gmail.com>
# License: BSD 3 clause

RANDOM_STATE = 42
FIG_SIZE = (10, 7)

features, target = load_wine(return_X_y=True)

# Make a train/test split using 30% test size
X_train, X_test, y_train, y_test = train_test_split(features, target,
    test_size=0.30,
    random_state=RANDOM_STATE)

# Fit to data and predict using pipelined GNB and PCA.
unscaled_clf = make_pipeline(PCA(n_components=2), GaussianNB())
unscaled_clf.fit(X_train, y_train)
pred_test = unscaled_clf.predict(X_test)

# Fit to data and predict using pipelined scaling, GNB and PCA.
std_clf = make_pipeline(StandardScaler(), PCA(n_components=2), GaussianNB())
std_clf.fit(X_train, y_train)
pred_test_std = std_clf.predict(X_test)

# Show prediction accuracies in scaled and unscaled data.
print('
Prediction accuracy for the normal test dataset with PCA
{:.2%}'.format(metrics.accuracy_score(y_test, pred_test)))

print('
Prediction accuracy for the standardized test dataset with PCA
{:.2%}'.format(metrics.accuracy_score(y_test, pred_test_std)))

# Extract PCA from pipeline
pca = unscaled_clf.named_steps['pca']
pca_std = std_clf.named_steps['pca']

# Show first principal components
print('
PC 1 without scaling:
', pca.components_[0])
print('
PC 1 with scaling:
', pca_std.components_[0])

# Scale and use PCA on X_train data for visualization.
scaler = std_clf.named_steps['standardscaler']
X_train_std = pca_std.transform(scaler.transform(X_train))

# visualize standardized vs. untouched dataset with PCA performed
fig, (ax1, ax2) = plt.subplots(ncols=2, figsize=FIG_SIZE)

for l, c, m in zip(range(0, 3), ('blue', 'red', 'green'), ('^', 's', 'o')):
    ax1.scatter(X_train[y_train == l, 0], X_train[y_train == l, 1],
        color=c, marker=m)

25.2. Importance of Feature Scaling
for l, c, m in zip(range(0, 3), ('blue', 'red', 'green'), ('^', 's', 'o')):
    ax2.scatter(X_train_std[y_train == l, 0], X_train_std[y_train == l, 1],
                color=c,
                label='class %s % l,
                alpha=0.5,
                marker=m)

ax1.set_title('Training dataset after PCA')
ax2.set_title('Standardized training dataset after PCA')

for ax in (ax1, ax2):
    ax.set_xlabel('1st principal component')
    ax.set_ylabel('2nd principal component')
    ax.legend(loc='upper right')
    ax.grid()

plt.tight_layout()
plt.show()

Total running time of the script: ( 0 minutes 0.216 seconds)

25.3 Compare the effect of different scalers on data with outliers

Feature 0 (median income in a block) and feature 5 (number of households) of the California housing dataset have very different scales and contain some very large outliers. These two characteristics lead to difficulties to visualize the data and, more importantly, they can degrade the predictive performance of many machine learning algorithms. Unscaled data can also slow down or even prevent the convergence of many gradient-based estimators.

Indeed many estimators are designed with the assumption that each feature takes values close to zero or more importantly that all features vary on comparable scales. In particular, metric-based and gradient-based estimators often assume approximately standardized data (centered features with unit variances). A notable exception are decision tree-based estimators that are robust to arbitrary scaling of the data.

This example uses different scalers, transformers, and normalizers to bring the data within a pre-defined range.

Scalers are linear (or more precisely affine) transformers and differ from each other in the way to estimate the parameters used to shift and scale each feature.
QuantileTransformer provides a non-linear transformation in which distances between marginal outliers and inliers are shrunk.

Unlike the previous transformations, normalization refers to a per sample transformation instead of a per feature transformation.

The following code is a bit verbose, feel free to jump directly to the analysis of the results.
from __future__ import print_function
import numpy as np
import matplotlib as mpl
from matplotlib import pyplot as plt
from matplotlib import cm

from sklearn.preprocessing import MinMaxScaler
from sklearn.preprocessing import minmax_scale
from sklearn.preprocessing import MaxAbsScaler
from sklearn.preprocessing import StandardScaler
from sklearn.preprocessing import RobustScaler
from sklearn.preprocessing import Normalizer
from sklearn.preprocessing.data import QuantileTransformer

from sklearn.datasets import fetch_california_housing

print(__doc__)

dataset = fetch_california_housing()
X_full, y_full = dataset.data, dataset.target

# Take only 2 features to make visualization easier
# Feature of 0 has a long tail distribution.
# Feature 5 has a few but very large outliers.
X = X_full[:, [0, 5]]
distributions = [
    ('Unscaled data', X),
    ('Data after standard scaling', StandardScaler().fit_transform(X)),
    ('Data after min-max scaling', MinMaxScaler().fit_transform(X)),
    ('Data after max-abs scaling', MaxAbsScaler().fit_transform(X)),
    ('Data after robust scaling', RobustScaler(quantile_range=(25, 75)).fit_transform(X)),
    ('Data after quantile transformation (uniform pdf)', QuantileTransformer(output_distribution='uniform').fit_transform(X)),
    ('Data after quantile transformation (gaussian pdf)', QuantileTransformer(output_distribution='normal').fit_transform(X)),
    ('Data after sample-wise L2 normalizing', Normalizer().fit_transform(X))
]

# scale the output between 0 and 1 for the colorbar
y = minmax_scale(y_full)

def create_axes(title, figsize=(16, 6)):
    fig = plt.figure(figsize=figsize)
    fig.suptitle(title)
# define the axis for the first plot
left, width = 0.1, 0.22
bottom, height = 0.1, 0.7
bottom_h = height + 0.15
left_h = left + width + 0.02
rect_scatter = [left, bottom, width, height]
rect_histx = [left, bottom_h, width, 0.1]
rect_histy = [left_h, bottom, 0.05, height]
ax_scatter = plt.axes(rect_scatter)
ax_histx = plt.axes(rect_histx)
ax_histy = plt.axes(rect_histy)

# define the axis for the zoomed-in plot
left = width + left + 0.2
left_h = left + width + 0.02
rect_scatter = [left, bottom, width, height]
rect_histx = [left, bottom_h, width, 0.1]
rect_histy = [left_h, bottom, 0.05, height]

ax_scatter_zoom = plt.axes(rect_scatter)
ax_histx_zoom = plt.axes(rect_histx)
ax_histy_zoom = plt.axes(rect_histy)

# define the axis for the colorbar
left, width = width + left + 0.13, 0.01
rect_colorbar = [left, bottom, width, height]
ax_colorbar = plt.axes(rect_colorbar)

return ((ax_scatter, ax_histy, ax_histx),
         (ax_scatter_zoom, ax_histy_zoom, ax_histx_zoom),
         ax_colorbar)

def plot_distribution(axes, X, y, hist_nbins=50, title="", x0_label="", x1_label=""):
    ax, hist_X1, hist_X0 = axes
    ax.set_title(title)
    ax.set_xlabel(x0_label)
    ax.set_ylabel(x1_label)
    # The scatter plot
    colors = cm.plasma_r(y)
    ax.scatter(X[:, 0], X[:, 1], alpha=0.5, marker='o', s=5, lw=0, c=colors)
    # Removing the top and the right spine for aesthetics
    # make nice axis layout
    ax.spines['top'].set_visible(False)
    ax.spines['right'].set_visible(False)
    ax.get_xaxis().tick_bottom()
    ax.get_yaxis().tick_left()
    ax.spines['left'].set_position(('outward', 10))
    ax.spines['bottom'].set_position(('outward', 10))
Two plots will be shown for each scaler/normalizer/transformer. The left figure will show a scatter plot of the full data set while the right figure will exclude the extreme values considering only 99% of the data set, excluding marginal outliers. In addition, the marginal distributions for each feature will be shown on the side of the scatter plot.

```python
def make_plot(item_idx):
    title, X = distributions[item_idx]
    ax_zoom_out, ax_zoom_in, ax_colorbar = create_axes(title)
    axarr = (ax_zoom_out, ax_zoom_in)
    plot_distribution(axarr[0], X, y, hist_nbins=200,
                      x0_label="Median Income",
                      x1_label="Number of households",
                      title="Full data")

    # zoom-in
    zoom_in_percentile_range = (0, 99)
    cutoffs_X0 = np.percentile(X[:, 0], zoom_in_percentile_range)
    cutoffs_X1 = np.percentile(X[:, 1], zoom_in_percentile_range)
    non_outliers_mask = (np.all(X > [cutoffs_X0[0], cutoffs_X1[0]], axis=1) &
                           np.all(X < [cutoffs_X0[1], cutoffs_X1[1]], axis=1))
    plot_distribution(axarr[1], X[non_outliers_mask], y[non_outliers_mask],
                      hist_nbins=50,
                      x0_label="Median Income",
                      x1_label="Number of households",
                      title="Zoom-in")

    norm = mpl.colors.Normalize(y_full.min(), y_full.max())
    mpl.colorbar.ColorbarBase(ax_colorbar, cmap=cm.plasma_r,
                               norm=norm, orientation='vertical',
                               label='Color mapping for values of y')
```

### 25.3.1 Original data

Each transformation is plotted showing two transformed features, with the left plot showing the entire dataset, and the right zoomed-in to show the dataset without the marginal outliers. A large majority of the samples are compacted to a specific range, [0, 10] for the median income and [0, 6] for the number of households. Note that there are some marginal outliers (some blocks have more than 1200 households). Therefore, a specific pre-processing can be very beneficial depending of the application. In the following, we present some insights and behaviors of those pre-processing methods in the presence of marginal outliers.

```python
make_plot(0)
```
25.3.2 StandardScaler

StandardScaler removes the mean and scales the data to unit variance. However, the outliers have an influence when computing the empirical mean and standard deviation which shrink the range of the feature values as shown in the left figure below. Note in particular that because the outliers on each feature have different magnitudes, the spread of the transformed data on each feature is very different: most of the data lie in the [-2, 4] range for the transformed median income feature while the same data is squeezed in the smaller [-0.2, 0.2] range for the transformed number of households.

StandardScaler therefore cannot guarantee balanced feature scales in the presence of outliers.

25.3.3 MinMaxScaler

MinMaxScaler rescales the data set such that all feature values are in the range [0, 1] as shown in the right panel below. However, this scaling compress all inliers in the narrow range [0, 0.005] for the transformed number of households.

As StandardScaler, MinMaxScaler is very sensitive to the presence of outliers.
25.3.4 MaxAbsScaler

MaxAbsScaler differs from the previous scaler such that the absolute values are mapped in the range \([0, 1]\). On positive only data, this scaler behaves similarly to MinMaxScaler and therefore also suffers from the presence of large outliers.

25.3.5 RobustScaler

Unlike the previous scalers, the centering and scaling statistics of this scaler are based on percentiles and are therefore not influenced by a few number of very large marginal outliers. Consequently, the resulting range of the transformed feature values is larger than for the previous scalers and, more importantly, are approximately similar: for both features most of the transformed values lie in a \([-2, 3]\) range as seen in the zoomed-in figure. Note that the outliers themselves are still present in the transformed data. If a separate outlier clipping is desirable, a non-linear transformation is required (see below).
25.3.6 QuantileTransformer (uniform output)

QuantileTransformer applies a non-linear transformation such that the probability density function of each feature will be mapped to a uniform distribution. In this case, all the data will be mapped in the range [0, 1], even the outliers which cannot be distinguished anymore from the inliers.

As RobustScaler, QuantileTransformer is robust to outliers in the sense that adding or removing outliers in the training set will yield approximately the same transformation on held out data. But contrary to RobustScaler, QuantileTransformer will also automatically collapse any outlier by setting them to the a priori defined range boundaries (0 and 1).

25.3.7 QuantileTransformer (Gaussian output)

QuantileTransformer has an additional output_distribution parameter allowing to match a Gaussian distribution instead of a uniform distribution. Note that this non-parametric transformer introduces saturation artifacts for extreme values.
25.3.8 Normalizer

The Normalizer rescales the vector for each sample to have unit norm, independently of the distribution of the samples. It can be seen on both figures below where all samples are mapped onto the unit circle. In our example the two selected features have only positive values; therefore the transformed data only lie in the positive quadrant. This would not be the case if some original features had a mix of positive and negative values.

```python
make_plot(7)
plt.show()
```

Total running time of the script: 0 minutes 6.509 seconds
26.1 Decision boundary of label propagation versus SVM on the Iris dataset

Comparison for decision boundary generated on iris dataset between Label Propagation and SVM. This demonstrates Label Propagation learning a good boundary even with a small amount of labeled data.
print(__doc__)

# Authors: Clay Woolam <clay@woolam.org>
# License: BSD

import numpy as np
import matplotlib.pyplot as plt
from sklearn import datasets
from sklearn import svm
from sklearn.semi_supervised import label_propagation

rng = np.random.RandomState(0)
iris = datasets.load_iris()
X = iris.data[:, :2]
y = iris.target

# step size in the mesh
h = .02

y_30 = np.copy(y)
y_30[rng.rand(len(y)) < 0.3] = -1
y_50 = np.copy(y)
y_50[rng.rand(len(y)) < 0.5] = -1

# we create an instance of SVM and fit out data. We do not scale our
# data since we want to plot the support vectors
ls30 = (label_propagation.LabelSpreading().fit(X, y_30), y_30)
ls50 = (label_propagation.LabelSpreading().fit(X, y_50), y_50)
ls100 = (label_propagation.LabelSpreading().fit(X, y), y)
rbf_svc = (svm.SVC(kernel='rbf').fit(X, y), y)

# create a mesh to plot in
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                     np.arange(y_min, y_max, h))

titles = ['Label Spreading 30% data',
          'Label Spreading 50% data',
          'Label Spreading 100% data',
          'SVC with rbf kernel']

for i, (clf, y_train) in enumerate((ls30, ls50, ls100, rbf_svc)):
    # Plot the decision boundary. For that, we will assign a color to each
    # point in the mesh [x_min, x_max]x[y_min, y_max].
    plt.subplot(2, 2, i + 1)
    Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])

    # Put the result into a color plot
    Z = Z.reshape(xx.shape)
    plt.contourf(xx, yy, Z, cmap=plt.cm.Paired)
    plt.axis('off')
# Plot also the training points
colors = [color_map[y] for y in y_train]
plt.scatter(X[:, 0], X[:, 1], c=colors, edgecolors='black')

plt.title(titles[i])
plt.suptitle("Unlabeled points are colored white", y=0.1)
plt.show()

Total running time of the script: ( 0 minutes 1.769 seconds)

## 26.2 Label Propagation learning a complex structure

Example of LabelPropagating learning a complex internal structure to demonstrate “manifold learning”. The outer circle should be labeled “red” and the inner circle “blue”. Because both label groups lie inside their own distinct shape, we can see that the labels propagate correctly around the circle.

```
print(__doc__)

# Authors: Clay Woolam <clay@woolam.org>
# Andreas Mueller <amueller@ais.uni-bonn.de>
# License: BSD

import numpy as np
import matplotlib.pyplot as plt
from sklearn.semi_supervised import label_propagation
from sklearn.datasets import make_circles

# generate ring with inner box
n_samples = 200
X, y = make_circles(n_samples=n_samples, shuffle=False)
outer, inner = 0, 1
labels = -np.ones(n_samples)
labels[0] = outer
```
labels[-1] = inner

# Learn with LabelSpreading
label_spread = label_propagation.LabelSpreading(kernel='knn', alpha=0.8)
label_spread.fit(X, labels)

# Plot output labels
output_labels = label_spread.transduction_
plt.figure(figsize=(8.5, 4))
plt.subplot(1, 2, 1)
plt.scatter(X[labels == outer, 0], X[labels == outer, 1], color='navy', marker='s', lw=0, label="outer labeled", s=10)
plt.scatter(X[labels == inner, 0], X[labels == inner, 1], color='c', marker='s', lw=0, label="inner labeled", s=10)
plt.scatter(X[labels == -1, 0], X[labels == -1, 1], color='darkorange', marker='.', label="unlabeled")
plt.legend(scatterpoints=1, shadow=False, loc='upper right')
plt.title("Raw data (2 classes=outer and inner)")

plt.subplot(1, 2, 2)
output_label_array = np.asarray(output_labels)
outer_numbers = np.where(output_label_array == outer)[0]
inner_numbers = np.where(output_label_array == inner)[0]
plt.scatter(X[outer_numbers, 0], X[outer_numbers, 1], color='navy', marker='s', lw=0, s=10, label="outer learned")
plt.scatter(X[inner_numbers, 0], X[inner_numbers, 1], color='c', marker='s', lw=0, s=10, label="inner learned")
plt.legend(scatterpoints=1, shadow=False, loc='upper right')
plt.title("Labels learned with Label Spreading (KNN)")

plt.subplots_adjust(left=0.07, bottom=0.07, right=0.93, top=0.92)
plt.show()

Total running time of the script: ( 0 minutes 0.091 seconds)

26.3 Label Propagation digits: Demonstrating performance

This example demonstrates the power of semisupervised learning by training a Label Spreading model to classify handwritten digits with sets of very few labels.

The handwritten digit dataset has 1797 total points. The model will be trained using all points, but only 30 will be labeled. Results in the form of a confusion matrix and a series of metrics over each class will be very good.

At the end, the top 10 most uncertain predictions will be shown.
Learning with small amount of labeled data

<table>
<thead>
<tr>
<th>predict</th>
<th>true</th>
</tr>
</thead>
<tbody>
<tr>
<td>9</td>
<td>3</td>
</tr>
<tr>
<td>8</td>
<td>1</td>
</tr>
<tr>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td>9</td>
<td>4</td>
</tr>
</tbody>
</table>

Out:

Label Spreading model: 30 labeled & 300 unlabeled points (330 total)

<table>
<thead>
<tr>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00</td>
<td>1.00</td>
<td>23</td>
</tr>
<tr>
<td>1</td>
<td>0.58</td>
<td>0.50</td>
<td>28</td>
</tr>
<tr>
<td>2</td>
<td>0.93</td>
<td>0.93</td>
<td>29</td>
</tr>
<tr>
<td>3</td>
<td>0.00</td>
<td>0.00</td>
<td>28</td>
</tr>
<tr>
<td>4</td>
<td>0.92</td>
<td>0.88</td>
<td>25</td>
</tr>
<tr>
<td>5</td>
<td>0.96</td>
<td>0.76</td>
<td>33</td>
</tr>
<tr>
<td>6</td>
<td>0.97</td>
<td>0.97</td>
<td>36</td>
</tr>
<tr>
<td>7</td>
<td>0.89</td>
<td>1.00</td>
<td>34</td>
</tr>
<tr>
<td>8</td>
<td>0.51</td>
<td>0.79</td>
<td>29</td>
</tr>
<tr>
<td>9</td>
<td>0.51</td>
<td>0.80</td>
<td>35</td>
</tr>
</tbody>
</table>

avg / total 0.73 0.77 0.74 300

Confusion matrix

```
[[23  0  0  0  0  0  0  0  0]  
 [0 14  2  0  0  1  0 11  0]  
 [0  0 27  0  0  2  0  0  0]  
 [0  3  0 22  0  0  0  0  0]  
 [0  0  0  0  25  0  0  0  8]  
 [0  1  0  0  35  0  0  0  0]  
 [0  0  0  0  0  34  0  0  0]  
 [0  6  0  0  0  0  23  0  0]  
```

26.3. Label Propagation digits: Demonstrating performance 1147
print(__doc__)

# Authors: Clay Woolam <clay@woolam.org>
# License: BSD

import numpy as np
import matplotlib.pyplot as plt
from scipy import stats
from sklearn import datasets
from sklearn.semi_supervised import label_propagation
from sklearn.metrics import confusion_matrix, classification_report

digits = datasets.load_digits()
rng = np.random.RandomState(0)
indices = np.arange(len(digits.data))
rng.shuffle(indices)

X = digits.data[indices[:330]]
y = digits.target[indices[:330]]
images = digits.images[indices[:330]]

n_total_samples = len(y)

n_labeled_points = 30
indices = np.arange(n_total_samples)
unlabeled_set = indices[n_labeled_points:]

# Shuffle everything around
y_train = np.copy(y)
y_train[unlabeled_set] = -1

# Learn with LabelSpreading
lp_model = label_propagation.LabelSpreading(gamma=0.25, max_iter=5)
lp_model.fit(X, y_train)
predicted_labels = lp_model.transduction_[unlabeled_set]
true_labels = y[unlabeled_set]

cm = confusion_matrix(true_labels, predicted_labels, labels=lp_model.classes_)

print("Label Spreading model: %d labeled & %d unlabeled points (%d total)" %
      (n_labeled_points, n_total_samples - n_labeled_points, n_total_samples))

print(classification_report(true_labels, predicted_labels))
print("Confusion matrix")
# Calculate uncertainty values for each transduced distribution
pred_entropies = stats.distributions.entropy(lp_model.label_distributions_.T)

# Pick the top 10 most uncertain labels
uncertainty_index = np.argsort(pred_entropies)[-10:]

# Plot
f = plt.figure(figsize=(7, 5))
for index, image_index in enumerate(uncertainty_index):
    image = images[image_index]
    sub = f.add_subplot(2, 5, index + 1)
    sub.imshow(image, cmap=plt.cm.gray_r)
    plt.xticks([])
    plt.yticks([])
    sub.set_title('predict: %i
 true: %i' % (lp_model.transduction_[image_index], y[image_index]))

f.suptitle('Learning with small amount of labeled data')
plt.show()

Total running time of the script: ( 0 minutes 0.560 seconds)

## 26.4 Label Propagation digits active learning

Demonstrates an active learning technique to learn handwritten digits using label propagation.

We start by training a label propagation model with only 10 labeled points, then we select the top five most uncertain points to label. Next, we train with 15 labeled points (original 10 + 5 new ones). We repeat this process four times to have a model trained with 30 labeled examples. Note you can increase this to label more than 30 by changing `max_iterations`. Labeling more than 30 can be useful to get a sense for the speed of convergence of this active learning technique.

A plot will appear showing the top 5 most uncertain digits for each iteration of training. These may or may not contain mistakes, but we will train the next model with their true labels.
Out:

```
<table>
<thead>
<tr>
<th>Label</th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>24</td>
</tr>
<tr>
<td>1</td>
<td>0.51</td>
<td>0.86</td>
<td>0.64</td>
<td>29</td>
</tr>
<tr>
<td>2</td>
<td>0.83</td>
<td>0.97</td>
<td>0.90</td>
<td>31</td>
</tr>
<tr>
<td>3</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>28</td>
</tr>
<tr>
<td>4</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>27</td>
</tr>
<tr>
<td>5</td>
<td>0.85</td>
<td>0.49</td>
<td>0.62</td>
<td>35</td>
</tr>
<tr>
<td>6</td>
<td>0.84</td>
<td>0.95</td>
<td>0.89</td>
<td>40</td>
</tr>
<tr>
<td>7</td>
<td>0.70</td>
<td>0.92</td>
<td>0.80</td>
<td>36</td>
</tr>
<tr>
<td>8</td>
<td>0.57</td>
<td>0.76</td>
<td>0.65</td>
<td>33</td>
</tr>
<tr>
<td>9</td>
<td>0.41</td>
<td>0.86</td>
<td>0.55</td>
<td>37</td>
</tr>
</tbody>
</table>
```

```
avg / total 0.51 0.62 0.54 320
```

Confusion matrix:

```
[25 3 0 0 0 0 1]
[1 30 0 0 0 0 0]
[0 0 17 7 0 1 10]
[0 3 0 38 0 0 0]
[0 3 0 0 33 0 0]
[8 0 0 0 0 25 0]
```
### Iteration 1

**Label Spreading model:** 15 labeled & 315 unlabeled (330 total)

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>24</td>
</tr>
<tr>
<td>1</td>
<td>0.51</td>
<td>0.75</td>
<td>0.61</td>
<td>28</td>
</tr>
<tr>
<td>2</td>
<td>0.91</td>
<td>0.97</td>
<td>0.94</td>
<td>31</td>
</tr>
<tr>
<td>3</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>28</td>
</tr>
<tr>
<td>4</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>27</td>
</tr>
<tr>
<td>5</td>
<td>0.84</td>
<td>0.97</td>
<td>0.90</td>
<td>33</td>
</tr>
<tr>
<td>6</td>
<td>1.00</td>
<td>0.95</td>
<td>0.97</td>
<td>40</td>
</tr>
<tr>
<td>7</td>
<td>0.75</td>
<td>0.92</td>
<td>0.83</td>
<td>36</td>
</tr>
<tr>
<td>8</td>
<td>0.46</td>
<td>0.81</td>
<td>0.59</td>
<td>31</td>
</tr>
<tr>
<td>9</td>
<td>0.43</td>
<td>0.78</td>
<td>0.56</td>
<td>37</td>
</tr>
</tbody>
</table>

**avg / total** 0.53 0.66 0.58 315

**Confusion matrix**

```
[[21  0  0  0  0  6  1]
 [ 1 30  0  0  0  0  0]
 [ 0  0 32  0  0  0  1]
 [ 2  0 38  0  0  0  0]
 [ 0  3  0 33  0  0  0]
 [ 6  0  0  0 35  0  0]
 [ 0  0  6  0  0 29  0]]
```

### Iteration 2

**Label Spreading model:** 20 labeled & 310 unlabeled (330 total)

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>22</td>
</tr>
<tr>
<td>1</td>
<td>0.67</td>
<td>0.71</td>
<td>0.69</td>
<td>28</td>
</tr>
<tr>
<td>2</td>
<td>0.94</td>
<td>0.97</td>
<td>0.95</td>
<td>31</td>
</tr>
<tr>
<td>3</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>28</td>
</tr>
<tr>
<td>4</td>
<td>0.85</td>
<td>0.92</td>
<td>0.88</td>
<td>24</td>
</tr>
<tr>
<td>5</td>
<td>0.89</td>
<td>0.97</td>
<td>0.93</td>
<td>33</td>
</tr>
<tr>
<td>6</td>
<td>1.00</td>
<td>0.95</td>
<td>0.97</td>
<td>40</td>
</tr>
<tr>
<td>7</td>
<td>1.00</td>
<td>0.92</td>
<td>0.96</td>
<td>36</td>
</tr>
<tr>
<td>8</td>
<td>0.50</td>
<td>0.81</td>
<td>0.62</td>
<td>31</td>
</tr>
<tr>
<td>9</td>
<td>0.67</td>
<td>0.78</td>
<td>0.72</td>
<td>37</td>
</tr>
</tbody>
</table>

**avg / total** 0.76 0.81 0.78 310

**Confusion matrix**

```
[[22  0  0  0  0  0  0  0  0]
 [ 0 20  0  1 0  0  0  6  1]
 [ 0  1 30  0  0  0  0  0  0]
 [ 0  1 22  0  0  0  1  0  0]
 [ 0  0  0 32  0  0  0  0  1]
 [ 0  2  0  0 38  0  0  0  0]
 [ 0  0  2  1 0 33  0  0  0]
 [ 0  6  0  0  0  0 35  0  0]
 [ 0  0  0  2 4  0  0 29  0]]
```

### Iteration 3

**Label Spreading model:** 25 labeled & 305 unlabeled (330 total)

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00</td>
<td>1.00</td>
<td>1.00</td>
<td>22</td>
</tr>
</tbody>
</table>

**Confusion matrix**

```
[[25  0  0  0  0  0  0  0  0  0  0]
 [ 0 20  0  1 0  0  0  6  1  0  0]
 [ 0  1 30  0  0  0  0  0  0  0  0]
 [ 0  1 22  0  0  0  1  0  0  0  0]
 [ 0  0  0 32  0  0  0  0  0  0  0]
 [ 0  2  0  0 38  0  0  0  0  0  0]
 [ 0  0  2  1 0 33  0  0  0  0  0]
 [ 0  6  0  0  0  0 35  0  0  0  0]
 [ 0  0  0  2 4  0  0 29  0  0  0]]
```
**Confusion matrix**

\[
\begin{bmatrix}
22 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 23 & 0 & 0 & 0 & 0 & 0 & 0 & 4 & 0 \\
0 & 1 & 28 & 0 & 0 & 0 & 0 & 2 & 0 & 0 \\
0 & 0 & 0 & 20 & 0 & 0 & 0 & 0 & 6 & 0 \\
0 & 1 & 0 & 0 & 22 & 0 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 0 & 32 & 0 & 0 & 0 & 1 & 0 \\
0 & 1 & 0 & 0 & 0 & 38 & 0 & 0 & 0 & 1 \\
0 & 0 & 0 & 0 & 0 & 35 & 0 & 0 & 0 & 1 \\
0 & 6 & 0 & 0 & 0 & 0 & 25 & 0 & 0 & 0 \\
0 & 2 & 0 & 0 & 0 & 4 & 0 & 0 & 2 & 29
\end{bmatrix}
\]

**Iteration 4**

Label Spreading model: 30 labeled & 300 unlabeled (330 total)

<table>
<thead>
<tr>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>1.00</td>
<td>1.00</td>
<td>22</td>
</tr>
<tr>
<td>1</td>
<td>0.68</td>
<td>0.85</td>
<td>0.75</td>
</tr>
<tr>
<td>2</td>
<td>1.00</td>
<td>0.87</td>
<td>0.93</td>
</tr>
<tr>
<td>3</td>
<td>0.92</td>
<td>1.00</td>
<td>0.96</td>
</tr>
<tr>
<td>4</td>
<td>1.00</td>
<td>0.92</td>
<td>0.96</td>
</tr>
<tr>
<td>5</td>
<td>0.97</td>
<td>0.94</td>
<td>0.95</td>
</tr>
<tr>
<td>6</td>
<td>1.00</td>
<td>0.97</td>
<td>0.99</td>
</tr>
<tr>
<td>7</td>
<td>0.95</td>
<td>1.00</td>
<td>0.97</td>
</tr>
<tr>
<td>8</td>
<td>0.81</td>
<td>0.81</td>
<td>0.81</td>
</tr>
<tr>
<td>9</td>
<td>0.94</td>
<td>0.86</td>
<td>0.90</td>
</tr>
</tbody>
</table>

avg / total 0.93 0.92 0.92 300

Confusion matrix

\[
\begin{bmatrix}
22 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 23 & 0 & 0 & 0 & 0 & 0 & 0 & 4 & 0 \\
0 & 1 & 27 & 1 & 0 & 0 & 0 & 2 & 0 & 0 \\
0 & 0 & 0 & 23 & 0 & 0 & 0 & 0 & 0 & 0 \\
0 & 1 & 0 & 0 & 22 & 0 & 0 & 0 & 1 & 0 \\
0 & 0 & 0 & 0 & 31 & 0 & 0 & 0 & 2 & 0 \\
0 & 1 & 0 & 0 & 0 & 38 & 0 & 0 & 0 & 0 \\
0 & 0 & 0 & 0 & 0 & 35 & 0 & 0 & 0 & 0 \\
0 & 6 & 0 & 0 & 0 & 0 & 25 & 0 & 0 & 0 \\
0 & 2 & 0 & 0 & 0 & 1 & 0 & 0 & 1 & 30
\end{bmatrix}
\]
import numpy as np
import matplotlib.pyplot as plt
from scipy import stats
from sklearn import datasets
from sklearn.semi_supervised import label_propagation
from sklearn.metrics import classification_report, confusion_matrix

digits = datasets.load_digits()
rng = np.random.RandomState(0)
indices = np.arange(len(digits.data))
rng.shuffle(indices)

X = digits.data[indices[:330]]
y = digits.target[indices[:330]]
images = digits.images[indices[:330]]

n_total_samples = len(y)
n_labeled_points = 10
max_iterations = 5

unlabeled_indices = np.arange(n_total_samples)[n_labeled_points:]
f = plt.figure()

for i in range(max_iterations):
    if len(unlabeled_indices) == 0:
        print("No unlabeled items left to label.")
        break
    y_train = np.copy(y)
y_train[unlabeled_indices] = -1

lp_model = label_propagation.LabelSpreading(gamma=0.25, max_iter=5)
lp_model.fit(X, y_train)
predicted_labels = lp_model.transduction_[unlabeled_indices]
true_labels = y[unlabeled_indices]

cm = confusion_matrix(true_labels, predicted_labels,
                      labels=lp_model.classes_)

print("Iteration %i %s" % (i, 70 * "_"))
print("Label Spreading model: %d labeled & %d unlabeled (%d total)"
      % (n_labeled_points, n_total_samples - n_labeled_points,
          n_total_samples))

print(classification_report(true_labels, predicted_labels))

print("Confusion matrix")
print(cm)

# compute the entropies of transduced label distributions
pred_entropies = stats.distributions.entropy(
    lp_model.label_distributions_.T)
# select up to 5 digit examples that the classifier is most uncertain about
uncertainty_index = np.argsort(pred_entropies)[::-1]
uncertainty_index = uncertainty_index[np.in1d(uncertainty_index, unlabeled_indices)][:5]

# keep track of indices that we get labels for
delete_indices = np.array([])

# for more than 5 iterations, visualize the gain only on the first 5
if i < 5:
    f.text(.05, {1 - (i + 1) * .183},
    "model %d
    fit with %d labels" %
    ((i + 1), i * 5 + 10), size=10)
for index, image_index in enumerate(uncertainty_index):
    image = images[image_index]
    # for more than 5 iterations, visualize the gain only on the first 5
    if i < 5:
        sub = f.add_subplot(5, 5, index + 1 + (5 * i))
        sub.imshow(image, cmap=plt.cm.gray_r, interpolation='none')
        sub.set_title("predict: %i
    true: %i" %
                (lp_model.transduction_[image_index], y[image_index]), size=10)
        sub.axis('off')

    # labeling 5 points, remote from labeled set
    delete_index, = np.where(unlabeled_indices == image_index)
    delete_indices = np.concatenate((delete_indices, delete_index))
    unlabeled_indices = np.delete(unlabeled_indices, delete_indices)
    n_labeled_points += len(uncertainty_index)

f.suptitle("Active learning with Label Propagation.
Rows show 5 most "
"uncertain labels to learn with the next model.", y=1.15)
plt.subplots_adjust(left=0.02, bottom=0.03, right=0.9, top=0.9, wspace=0.2, hspace=0.85)
plt.show()

Total running time of the script: ( 0 minutes 1.499 seconds)
Examples concerning the `sklearn.svm` module.

### 27.1 Non-linear SVM

Perform binary classification using non-linear SVC with RBF kernel. The target to predict is a XOR of the inputs. The color map illustrates the decision function learned by the SVC.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm

xx, yy = np.meshgrid(np.linspace(-3, 3, 500),
                     np.linspace(-3, 3, 500))
np.random.seed(0)
X = np.random.randn(300, 2)
Y = np.logical_xor(X[:, 0] > 0, X[:, 1] > 0)

# fit the model
clf = svm.NuSVC()
clf.fit(X, Y)

# plot the decision function for each datapoint on the grid
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
Z = Z.reshape(xx.shape)
plt.imshow(Z, interpolation='nearest',
          extent=(xx.min(), xx.max(), yy.min(), yy.max()), aspect='auto',
          origin='lower', cmap=plt.cm.PuOr_r)
contours = plt.contour(xx, yy, Z, levels=[0], linewidths=2,
                       linetypes='--')
plt.scatter(X[:, 0], X[:, 1], s=30, c=Y, cmap=plt.cm.Paired,
            edgecolors='k')
plt.xticks(())
plt.yticks(()
plt.axis([-3, 3, -3, 3])
plt.show()

Total running time of the script: ( 0 minutes 1.311 seconds)

27.2 SVM: Maximum margin separating hyperplane

Plot the maximum margin separating hyperplane within a two-class separable dataset using a Support Vector Machine classifier with linear kernel.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm
from sklearn.datasets import make_blobs

# we create 40 separable points
X, y = make_blobs(n_samples=40, centers=2, random_state=6)

# fit the model, don't regularize for illustration purposes
clf = svm.SVC(kernel='linear', C=1000)
clf.fit(X, y)

plt.scatter(X[:, 0], X[:, 1], c=y, s=30, cmap=plt.cm.Paired)

# plot the decision function
ax = plt.gca()
xlim = ax.get_xlim()
ylim = ax.get_ylim()

# create grid to evaluate model
xx = np.linspace(xlim[0], xlim[1], 30)
yy = np.linspace(ylim[0], ylim[1], 30)
YY, XX = np.meshgrid(yy, xx)

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Support Vector Regression

Toy example of 1D regression using linear, polynomial and RBF kernels.

print(__doc__)
import numpy as np
from sklearn.svm import SVR
import matplotlib.pyplot as plt

xy = np.vstack((XX.ravel(), YY.ravel())).T
Z = clf.decision_function(xy).reshape(XX.shape)

# plot decision boundary and margins
ax.contour(XX, YY, Z, colors='k', levels=[-1, 0, 1], alpha=0.5,
        linestyles=['--', '-', '--'])
# plot support vectors
ax.scatter(clf.support_vectors_[:, 0], clf.support_vectors_[:, 1], s=100,
        linewidth=1, facecolors='none')
plt.show()
# Generate sample data
X = np.sort(5 * np.random.rand(40, 1), axis=0)
y = np.sin(X).ravel()

# Add noise to targets
y[::5] += 3 * (0.5 - np.random.rand(8))

# Fit regression model
svr_rbf = SVR(kernel='rbf', C=1e3, gamma=0.1)
svr_lin = SVR(kernel='linear', C=1e3)
svr_poly = SVR(kernel='poly', C=1e3, degree=2)
y_rbf = svr_rbf.fit(X, y).predict(X)
y_lin = svr_lin.fit(X, y).predict(X)
y_poly = svr_poly.fit(X, y).predict(X)

# Look at the results
lw = 2
plt.scatter(X, y, color='darkorange', label='data')
plt.plot(X, y_rbf, color='navy', lw=lw, label='RBF model')
plt.plot(X, y_lin, color='c', lw=lw, label='Linear model')
plt.plot(X, y_poly, color='cornflowerblue', lw=lw, label='Polynomial model')
plt.xlabel('data')
plt.ylabel('target')
plt.title('Support Vector Regression')
plt.legend()
plt.show()

Total running time of the script: ( 0 minutes 1.042 seconds)

## 27.4  SVM with custom kernel

Simple usage of Support Vector Machines to classify a sample. It will plot the decision surface and the support vectors.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm, datasets

# import some data to play with
iris = datasets.load_iris()
X = iris.data[:, :2]  # we only take the first two features. We could
                      # avoid this ugly slicing by using a two-dim dataset
Y = iris.target

def my_kernel(X, Y):
    """
    We create a custom kernel:
    \[
    k(X, Y) = X \begin{pmatrix} 2 & 0 \\ 0 & 1.0 \end{pmatrix} Y^T
    \]
    """
    M = np.array([[2, 0], [0, 1.0]])
    return np.dot(np.dot(X, M), Y.T)

h = .02  # step size in the mesh
# we create an instance of SVM and fit out data.
clf = svm.SVC(kernel=my_kernel)
clf.fit(X, Y)

# Plot the decision boundary. For that, we will assign a color to each
# point in the mesh [x_min, x_max]x[y_min, y_max].
x_min, x_max = X[:, 0].min() - 1, X[:, 0].max() + 1
y_min, y_max = X[:, 1].min() - 1, X[:, 1].max() + 1
xx, yy = np.meshgrid(np.arange(x_min, x_max, h), np.arange(y_min, y_max, h))
Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])

# Put the result into a color plot
Z = Z.reshape(xx.shape)
plt.pcolormesh(xx, yy, Z, cmap=plt.cm.Paired)

# Plot also the training points
plt.scatter(X[:, 0], X[:, 1], c=Y, cmap=plt.cm.Paired, edgecolors='k')
plt.title('3-Class classification using Support Vector Machine with custom'
' kernel')
plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.166 seconds)

## 27.5 SVM: Weighted samples

Plot decision function of a weighted dataset, where the size of points is proportional to its weight.

The sample weighting rescales the C parameter, which means that the classifier puts more emphasis on getting these points right. The effect might often be subtle. To emphasize the effect here, we particularly weight outliers, making the deformation of the decision boundary very visible.

![Constant weights](image1.png) ![Modified weights](image2.png)

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
```

### 27.5. SVM: Weighted samples
from sklearn import svm

def plot_decision_function(classifier, sample_weight, axis, title):
    # plot the decision function
    xx, yy = np.meshgrid(np.linspace(-4, 5, 500), np.linspace(-4, 5, 500))
    Z = classifier.decision_function(np.c_[xx.ravel(), yy.ravel()])
    Z = Z.reshape(xx.shape)

    # plot the line, the points, and the nearest vectors to the plane
    axis.contourf(xx, yy, Z, alpha=0.75, cmap=plt.cm.bone)
    axis.scatter(X[:, 0], X[:, 1], c=y, s=100 * sample_weight, alpha=0.9,
                 cmap=plt.cm.bone, edgecolors='black')

    axis.axis('off')
    axis.set_title(title)

# we create 20 points
np.random.seed(0)
X = np.r_[np.random.randn(10, 2) + [1, 1], np.random.randn(10, 2)]
y = [1] * 10 + [-1] * 10
sample_weight_last_ten = abs(np.random.randn(len(X)))
sample_weight_constant = np.ones(len(X))
# and bigger weights to some outliers
sample_weight_last_ten[15:] *= 5
sample_weight_last_ten[9] *= 15

# for reference, first fit without class weights
# fit the model
clf_weights = svm.LinearSVC()
clf_weights.fit(X, y, sample_weight=sample_weight_last_ten)
clf_no_weights = svm.LinearSVC()
clf_no_weights.fit(X, y)

fig, axes = plt.subplots(1, 2, figsize=(14, 6))
plot_decision_function(clf_no_weights, sample_weight_constant, axes[0],
                       "Constant weights")
plot_decision_function(clf_weights, sample_weight_last_ten, axes[1],
                       "Modified weights")
plt.show()
Note: This example will also work by replacing `SVC(kernel="linear")` with `SGDClassifier(loss="hinge")`. Setting the `loss` parameter of the `SGDClassifier` equal to `hinge` will yield behaviour such as that of a SVC with a linear kernel.

For example try instead of the SVC:

```python
clf = SGDClassifier(n_iter=100, alpha=0.01)
```

```python
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm

# we create clusters with 1000 and 100 points
rng = np.random.RandomState(0)
n_samples_1 = 1000
n_samples_2 = 100
X = np.r_[1.5 * rng.randn(n_samples_1, 2),
          0.5 * rng.randn(n_samples_2, 2) + [2, 2]]
y = [0] * (n_samples_1) + [1] * (n_samples_2)

# fit the model and get the separating hyperplane
clf = svm.SVC(kernel='linear', C=1.0)

```
clf.fit(X, y)

# fit the model and get the separating hyperplane using weighted classes
wclf = svm.SVC(kernel='linear', class_weight={1: 10})
wclf.fit(X, y)

# plot separating hyperplanes and samples
plt.scatter(X[:, 0], X[:, 1], c=y, cmap=plt.cm.Paired, edgecolors='k')
plt.legend()

# plot the decision functions for both classifiers
ax = plt.gca()
xlim = ax.get_xlim()
ylim = ax.get_ylim()

# create grid to evaluate model
xx = np.linspace(xlim[0], xlim[1], 30)
yy = np.linspace(ylim[0], ylim[1], 30)
YY, XX = np.meshgrid(yy, xx)
xy = np.vstack((XX.ravel(), YY.ravel())).T

# get the separating hyperplane
Z = clf.decision_function(xy).reshape(XX.shape)

# plot decision boundary and margins
a = ax.contour(XX, YY, Z, colors='k', levels=[0], alpha=0.5, linestyles=['-'])

# get the separating hyperplane for weighted classes
Z = wclf.decision_function(xy).reshape(XX.shape)

# plot decision boundary and margins for weighted classes
b = ax.contour(XX, YY, Z, colors='r', levels=[0], alpha=0.5, linestyles=['-'])

plt.legend([a.collections[0], b.collections[0]], ['non weighted', 'weighted'], loc='upper right')
plt.show()

Total running time of the script: ( 0 minutes 0.068 seconds)

## 27.7 SVM-Kernels

Three different types of SVM-Kernels are displayed below. The polynomial and RBF are especially useful when the data-points are not linearly separable.
```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm

# Print the documentation
print(__doc__)

# Code source: Gaël Varoquaux
# License: BSD 3 clause

import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm

# Our dataset and targets
X = np.c_[(.4, -.7),
         (-1.5, -1),
         (-1.4, -.9),
         (-1.3, -1.2),
         (-1.1, -.2),
         (-1.2, -.4),
         (-.5, 1.2),
         (-1.5, 2.1),
         (1, 1),
         # --
         (1.3, .8),
         (1.2, .5),
         (.2, -2),
         (.5, -2.4),
         (.2, -2.3),
         (0, -2.7),
         (1.3, 2.1)].T
Y = [0] * 8 + [1] * 8

# Figure number
fignum = 1

# Fit the model
for kernel in ('linear', 'poly', 'rbf'):
    clf = svm.SVC(kernel=kernel, gamma=2)
    clf.fit(X, Y)
```

### 27.7. SVM-Kernels
# plot the line, the points, and the nearest vectors to the plane
plt.figure(fignum, figsize=(4, 3))
plt.clf()

plt.scatter(clf.support_vectors_[:, 0], clf.support_vectors_[:, 1], s=80,
            facecolors='none', zorder=10, edgecolors='k')
plt.scatter(X[:, 0], X[:, 1], c=Y, zorder=10, cmap=plt.cm.Paired,
            edgecolors='k')

plt.axis('tight')
x_min = -3
x_max = 3
y_min = -3
y_max = 3

XX, YY = np.mgrid[x_min:x_max:200j, y_min:y_max:200j]
Z = clf.decision_function(np.c_[XX.ravel(), YY.ravel()])

# Put the result into a color plot
Z = Z.reshape(XX.shape)
plt.figure(fignum, figsize=(4, 3))
plt.pcolormesh(XX, YY, Z > 0, cmap=plt.cm.Paired)
plt.contour(XX, YY, Z, colors=['k', 'k', 'k'],
           linestyles=['--', '-', '--'],
           levels=[-.5, 0, .5])

plt.xlim(x_min, x_max)
plt.ylim(y_min, y_max)

plt.xticks(())
plt.yticks(())
fignum = fignum + 1
plt.show()

**Total running time of the script:** ( 0 minutes 0.196 seconds)

## 27.8 SVM-Anova: SVM with univariate feature selection

This example shows how to perform univariate feature selection before running a SVC (support vector classifier) to improve the classification scores.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm, datasets, feature_selection
from sklearn.model_selection import cross_val_score
from sklearn.pipeline import Pipeline

# #############################################################################
# Import some data to play with
digits = datasets.load_digits()
y = digits.target
# Throw away data, to be in the curse of dimension settings
y = y[:200]
X = digits.data[:200]
n_samples = len(y)
X = X.reshape((n_samples, -1))
# add 200 non-informative features
X = np.hstack((X, 2 * np.random.random((n_samples, 200))))

# #############################################################################
# Create a feature-selection transform and an instance of SVM that we
# combine together to have an full-blown estimator

transform = feature_selection.SelectPercentile(feature_selection.f_classif)
clf = Pipeline([('anova', transform), ('svc', svm.SVC(C=1.0))])

# Plot the cross-validation score as a function of percentile of features
score_means = list()
score_stds = list()
percentiles = (1, 3, 6, 10, 15, 20, 30, 40, 60, 80, 100)

for percentile in percentiles:
    clf.set_params(anova__percentile=percentile)
    # Compute cross-validation score using 1 CPU
    this_scores = cross_val_score(clf, X, y, n_jobs=1)
    score_means.append(this_scores.mean())
    score_stds.append(this_scores.std())

plt.errorbar(percentiles, score_means, np.array(score_stds))

plt.title('Performance of the SVM-Anova varying the percentile of features selected')
plt.xlabel('Percentile')
plt.ylabel('Prediction rate')

plt.axis('tight')
plt.show()

Total running time of the script: ( 0 minutes 0.582 seconds)

27.9 SVM Margins Example

The plots below illustrate the effect the parameter $C$ has on the separation line. A large value of $C$ basically tells our model that we do not have that much faith in our data’s distribution, and will only consider points close to line of separation.

A small value of $C$ includes more/all the observations, allowing the margins to be calculated using all the data in the area.
import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm

# we create 40 separable points
np.random.seed(0)
X = np.r_[np.random.randn(20, 2) - [2, 2], np.random.randn(20, 2) + [2, 2]]
Y = [0] * 20 + [1] * 20

# figure number
fignum = 1

# fit the model
for name, penalty in [('unreg', 1), ('reg', 0.05)]:
    clf = svm.SVC(kernel='linear', C=penalty)
    clf.fit(X, Y)

    # get the separating hyperplane
    w = clf.coef_[0]
    a = -w[0] / w[1]
    xx = np.linspace(-5, 5)
    yy = a * xx - (clf.intercept_[0]) / w[1]

    # plot the parallels to the separating hyperplane that pass through the
    # support vectors (margin away from hyperplane in direction
    # perpendicular to hyperplane). This is sqrt(1+a^2) away vertically in
    # 2-d.
    margin = 1 / np.sqrt(np.sum(clf.coef_ ** 2))
    yy_down = yy - np.sqrt(1 + a ** 2) * margin
    yy_up = yy + np.sqrt(1 + a ** 2) * margin

    # plot the line, the points, and the nearest vectors to the plane
    plt.figure(fignum, figsize=(4, 3))
    plt.clf()
    plt.plot(xx, yy, 'k-')
    plt.plot(xx, yy_down, 'k--')
    plt.plot(xx, yy_up, 'k--')
    plt.scatter(clf.support_vectors_[:, 0], clf.support_vectors_[:, 1], s=80,
                facecolors='none', zorder=10, edgecolors='k')

    plt.scatter(X[:, 0], X[:, 1], c=Y, zorder=10, cmap=plt.cm.Paired,
                edgecolors='k')

    plt.axis('tight')
    x_min = -4.8
    x_max = 4.2
    y_min = -6
    y_max = 6

    XX, YY = np.mgrid[x_min:x_max:200j, y_min:y_max:200j]
27.10 One-class SVM with non-linear kernel (RBF)

An example using a one-class SVM for novelty detection.

One-class SVM is an unsupervised algorithm that learns a decision function for novelty detection: classifying new data as similar or different to the training set.
print(__doc__)  

import numpy as np  
import matplotlib.pyplot as plt  
import matplotlib.font_manager  
from sklearn import svm  

xx, yy = np.meshgrid(np.linspace(-5, 5, 500), np.linspace(-5, 5, 500))  
# Generate train data  
X = 0.3 * np.random.randn(100, 2)  
X_train = np.r_[X + 2, X - 2]  
# Generate some regular novel observations  
X = 0.3 * np.random.randn(20, 2)  
X_test = np.r_[X + 2, X - 2]  
# Generate some abnormal novel observations  
X_outliers = np.random.uniform(low=-4, high=4, size=(20, 2))  

# fit the model  
clf = svm.OneClassSVM(nu=0.1, kernel="rbf", gamma=0.1)  
clf.fit(X_train)  
y_pred_train = clf.predict(X_train)  
y_pred_test = clf.predict(X_test)  
y_pred_outliers = clf.predict(X_outliers)  
n_error_train = y_pred_train[y_pred_train == -1].size  
n_error_test = y_pred_test[y_pred_test == -1].size  
n_error_outliers = y_pred_outliers[y_pred_outliers == 1].size  

# plot the line, the points, and the nearest vectors to the plane  
Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])  
Z = Z.reshape(xx.shape)  
plt.title("Novelty Detection")  
plt.contourf(xx, yy, Z, levels=np.linspace(Z.min(), 0, 7), cmap=plt.cm.PuBu)  
a = plt.contour(xx, yy, Z, levels=[0], linewidths=2, colors='darkred')  
plt.contourf(xx, yy, Z, levels=[0, Z.max()], colors='palevioletred')  
s = 40  
b1 = plt.scatter(X_train[:, 0], X_train[:, 1], c='white', s=s, edgecolors='k')  
b2 = plt.scatter(X_test[:, 0], X_test[:, 1], c='blueviolet', s=s, edgecolors='k')  
c = plt.scatter(X_outliers[:, 0], X_outliers[:, 1], c='gold', s=s, edgecolors='k')  
plt.axis('tight')  
plt.xlim((-5, 5))  
plt.ylim((-5, 5))  
plt.legend([a.collections[0], b1, b2, c],  
           ["learned frontier", "training observations",  
            "new regular observations", "new abnormal observations"],  
           loc="upper left",  
           prop=matplotlib.font_manager.FontProperties(size=11))  
plt.xlabel("error train: %d/200 ; errors novel regular: %d/40 ; "  
"errors novel abnormal: %d/40")  
%(n_error_train, n_error_test, n_error_outliers))
plt.show()  

Total running time of the script: (0 minutes 0.306 seconds)
27.11 Plot different SVM classifiers in the iris dataset

Comparison of different linear SVM classifiers on a 2D projection of the iris dataset. We only consider the first 2 features of this dataset:

• Sepal length
• Sepal width

This example shows how to plot the decision surface for four SVM classifiers with different kernels.

The linear models `LinearSVC()` and `SVC(kernel='linear')` yield slightly different decision boundaries. This can be a consequence of the following differences:

• `LinearSVC` minimizes the squared hinge loss while `SVC` minimizes the regular hinge loss.
• `LinearSVC` uses the One-vs-All (also known as One-vs-Rest) multiclass reduction while `SVC` uses the One-vs-One multiclass reduction.

Both linear models have linear decision boundaries (intersecting hyperplanes) while the non-linear kernel models (polynomial or Gaussian RBF) have more flexible non-linear decision boundaries with shapes that depend on the kind of kernel and its parameters.

Note: while plotting the decision function of classifiers for toy 2D datasets can help get an intuitive understanding of their respective expressive power, be aware that those intuitions don’t always generalize to more realistic high-dimensional problems.
```
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from sklearn import svm, datasets

def make_meshgrid(x, y, h=.02):
    """Create a mesh of points to plot in
    Parameters
    ----------
    x: data to base x-axis meshgrid on
    y: data to base y-axis meshgrid on
    h: stepsize for meshgrid, optional
    Returns
    -------
    xx, yy : ndarray
    """
    x_min, x_max = x.min() - 1, x.max() + 1
    y_min, y_max = y.min() - 1, y.max() + 1
    xx, yy = np.meshgrid(np.arange(x_min, x_max, h),
                         np.arange(y_min, y_max, h))
    return xx, yy

def plot_contours(ax, clf, xx, yy, **params):
    """Plot the decision boundaries for a classifier.
    Parameters
    ----------
    ax: matplotlib axes object
    clf: a classifier
    xx: meshgrid ndarray
    yy: meshgrid ndarray
    params: dictionary of params to pass to contourf, optional
    """
    Z = clf.predict(np.c_[xx.ravel(), yy.ravel()])
    Z = Z.reshape(xx.shape)
    out = ax.contourf(xx, yy, Z, **params)
    return out

# import some data to play with
iris = datasets.load_iris()
# Take the first two features. We could avoid this by using a two-dim dataset
X = iris.data[:, :2]
y = iris.target

# we create an instance of SVM and fit out data. We do not scale our
# data since we want to plot the support vectors
C = 1.0  # SVM regularization parameter
models = (svm.SVC(kernel=’linear’, C=C),
          svm.LinearSVC(C=C),
          svm.SVC(kernel=’rbf’, gamma=0.7, C=C),
          svm.SVC(kernel=’poly’, degree=3, C=C))
models = (clf.fit(X, y) for clf in models)
```

27.11. Plot different SVM classifiers in the iris dataset 1173
# title for the plots
titles = ('SVC with linear kernel',
    'LinearSVC (linear kernel)',
    'SVC with RBF kernel',
    'SVC with polynomial (degree 3) kernel')

# Set-up 2x2 grid for plotting.
fig, sub = plt.subplots(2, 2)
plt.subplots_adjust(wspace=0.4, hspace=0.4)
X0, X1 = X[:, 0], X[:, 1]
xx, yy = make_meshgrid(X0, X1)
for clf, title, ax in zip(models, titles, sub.flatten()):
    plot_contours(ax, clf, xx, yy,
        cmap=plt.cm.coolwarm, alpha=0.8)
    ax.scatter(X0, X1, c=y, cmap=plt.cm.coolwarm, s=20, edgecolors='k')
    ax.set_xlim(xx.min(), xx.max())
    ax.set_ylim(yy.min(), yy.max())
    ax.set_xlabel('Sepal length')
    ax.set_ylabel('Sepal width')
    ax.set_xticks(())
    ax.set_yticks(())
    ax.set_title(title)

plt.show()

Total running time of the script: ( 0 minutes 0.644 seconds)

## 27.12 Scaling the regularization parameter for SVCs

The following example illustrates the effect of scaling the regularization parameter when using Support Vector Machines for classification. For SVC classification, we are interested in a risk minimization for the equation:

\[
C \sum_{i=1}^{n} \mathcal{L}(f(x_i), y_i) + \Omega(w)
\]

where

- \( C \) is used to set the amount of regularization
- \( \mathcal{L} \) is a loss function of our samples and our model parameters.
- \( \Omega \) is a penalty function of our model parameters

If we consider the loss function to be the individual error per sample, then the data-fit term, or the sum of the error for each sample, will increase as we add more samples. The penalization term, however, will not increase.

When using, for example, cross validation, to set the amount of regularization with \( C \), there will be a different amount of samples between the main problem and the smaller problems within the folds of the cross validation.

Since our loss function is dependent on the amount of samples, the latter will influence the selected value of \( C \). The question that arises is How do we optimally adjust \( C \) to account for the different amount of training samples?

The figures below are used to illustrate the effect of scaling our \( C \) to compensate for the change in the number of samples, in the case of using an \( l1 \) penalty, as well as the \( l2 \) penalty.
27.12.1 l1-penalty case

In the l1 case, theory says that prediction consistency (i.e. that under given hypothesis, the estimator learned predicts as well as a model knowing the true distribution) is not possible because of the bias of the l1. It does say, however, that model consistency, in terms of finding the right set of non-zero parameters as well as their signs, can be achieved by scaling C1.

27.12.2 l2-penalty case

The theory says that in order to achieve prediction consistency, the penalty parameter should be kept constant as the number of samples grow.

27.12.3 Simulations

The two figures below plot the values of C on the x-axis and the corresponding cross-validation scores on the y-axis, for several different fractions of a generated data-set.

In the l1 penalty case, the cross-validation-error correlates best with the test-error, when scaling our C with the number of samples, n, which can be seen in the first figure.

For the l2 penalty case, the best result comes from the case where C is not scaled.

**Note:**

Two separate datasets are used for the two different plots. The reason behind this is the l1 case works better on sparse data, while l2 is better suited to the non-sparse case.
scikit-learn user guide, Release 0.20.dev0

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import numpy as np
import matplotlib.pyplot as plt
from sklearn.svm import LinearSVC
from sklearn.model_selection import ShuffleSplit
from sklearn.model_selection import GridSearchCV
from sklearn.utils import check_random_state
from sklearn import datasets

rnd = check_random_state(1)

# set up dataset
n_samples = 100
n_features = 300

# 11 data (only 5 informative features)
X_1, y_1 = datasets.make_classification(n_samples=n_samples,
                                       n_features=n_features,
                                       n_informative=5,
                                       random_state=1)

print(__doc__)
# 12 data: non sparse, but less features

\[
y_2 = \text{np.sign}(.5 - \text{rnd.rand}(n\_samples))
\]

\[
X_2 = \text{rnd.randn}(n\_samples, n\_features // 5) + y_2[:, \text{np.newaxis}]
\]

\[
X_2 += 5 * \text{rnd.randn}(n\_samples, n\_features // 5)
\]

\[
\text{clf\_sets} = [(\text{LinearSVC}(\text{penalty='l1', loss='squared\_hinge'}, \text{dual=False, tol=1e-3}), \\
\text{np.logspace}(-2.3, -1.3, 10), \text{X}\_1, \text{y}\_1),
\text{LinearSVC}(\text{penalty='l2', loss='squared\_hinge'}, \text{dual=True, tol=1e-4}), \\
\text{np.logspace}(-4.5, -2, 10), \text{X}\_2, \text{y}\_2)]
\]

\[
\text{colors} = [\text{'navy', 'cyan', 'darkorange'}]
\]

\[
\text{lw} = 2
\]

\[
\text{for fignum, (clf, cs, X, y) in enumerate(clf\_sets):}
\]

\[
\text{plt.figure(fignum, figsize=(9, 10))}
\]

\[
\text{for k, train\_size in enumerate(np.linspace(0.3, 0.7, 3)[:-1]):}
\]

\[
\text{param\_grid = dict(C=cs)}
\]

\[
\text{grid = GridSearchCV(clf, refit=False, param\_grid=param\_grid,}
\]

\[
\text{cv=ShuffleSplit(train\_size=train\_size, n\_splits=250, random\_state=1)}
\]

\[
\text{grid.fit(X, y)}
\]

\[
\text{scores = grid.cv\_results_['mean\_test\_score']}
\]

\[
\text{scales = [(1, 'No scaling'),}
\]

\[
((n\_samples \times train\_size), '1/n\_samples')],
\]

\[
\text{for subplotnum, (scaler, name) in enumerate(scales):}
\]

\[
\text{plt.subplot(2, 1, subplotnum + 1)}
\]

\[
\text{plt.xlabel('C')}
\]

\[
\text{plt.ylabel('CV Score')}
\]

\[
\text{grid\_cs = cs \times float(scaler)} \quad \# \text{scale the C's}
\]

\[
\text{plt.semilogx(grid\_cs, scores, label="fraction \% .2f" %}
\]

\[
\text{train\_size, color=colors[k], lw=lw)}
\]

\[
\text{plt.title('scaling=$s$, penalty=$s$, loss=$s' %}
\]

\[
\text{(name, clf\_penalty, clf\_loss)}
\]

\[
\text{plt.legend(loc="best")}
\]

\[
\text{plt.show()}
\]

Total running time of the script: ( 0 minutes 33.996 seconds)

## 27.13 RBF SVM parameters

This example illustrates the effect of the parameters gamma and C of the Radial Basis Function (RBF) kernel SVM. Intuitively, the \textit{gamma} parameter defines how far the influence of a single training example reaches, with low values meaning ‘far’ and high values meaning ‘close’. The \textit{gamma} parameters can be seen as the inverse of the radius of influence of samples selected by the model as support vectors.
The $C$ parameter trades off misclassification of training examples against simplicity of the decision surface. A low $C$ makes the decision surface smooth, while a high $C$ aims at classifying all training examples correctly by giving the model freedom to select more samples as support vectors.

The first plot is a visualization of the decision function for a variety of parameter values on a simplified classification problem involving only 2 input features and 2 possible target classes (binary classification). Note that this kind of plot is not possible to do for problems with more features or target classes.

The second plot is a heatmap of the classifier’s cross-validation accuracy as a function of $C$ and $\gamma$. For this example we explore a relatively large grid for illustration purposes. In practice, a logarithmic grid from $10^{-3}$ to $10^3$ is usually sufficient. If the best parameters lie on the boundaries of the grid, it can be extended in that direction in a subsequent search.

Note that the heat map plot has a special colorbar with a midpoint value close to the score values of the best performing models so as to make it easy to tell them apart in the blink of an eye.

The behavior of the model is very sensitive to the $\gamma$ parameter. If $\gamma$ is too large, the radius of the area of influence of the support vectors only includes the support vector itself and no amount of regularization with $C$ will be able to prevent overfitting.

When $\gamma$ is very small, the model is too constrained and cannot capture the complexity or “shape” of the data. The region of influence of any selected support vector would include the whole training set. The resulting model will behave similarly to a linear model with a set of hyperplanes that separate the centers of high density of any pair of two classes.

For intermediate values, we can see on the second plot that good models can be found on a diagonal of $C$ and $\gamma$. Smooth models (lower $\gamma$ values) can be made more complex by selecting a larger number of support vectors (larger $C$ values) hence the diagonal of good performing models.

Finally one can also observe that for some intermediate values of $\gamma$ we get equally performing models when $C$ becomes very large: it is not necessary to regularize by limiting the number of support vectors. The radius of the RBF kernel alone acts as a good structural regularizer. In practice though it might still be interesting to limit the number of support vectors with a lower value of $C$ so as to favor models that use less memory and that are faster to predict.

We should also note that small differences in scores results from the random splits of the cross-validation procedure. Those spurious variations can be smoothed out by increasing the number of CV iterations $n_{\text{splits}}$ at the expense of compute time. Increasing the value number of $C_{\text{range}}$ and $\gamma_{\text{range}}$ steps will increase the resolution of the hyper-parameter heat map.

![Heatmap of classifier’s cross-validation accuracy as a function of $C$ and $\gamma$.](image)
Out:

The best parameters are {'C': 1.0, 'gamma': 0.10000000000000001} with a score of 0.97

print(__doc__)

import numpy as np
import matplotlib.pyplot as plt
from matplotlib.colors import Normalize
from sklearn.svm import SVC
from sklearn.preprocessing import StandardScaler
from sklearn.datasets import load_iris
from sklearn.model_selection import StratifiedShuffleSplit, GridSearchCV

# Utility function to move the midpoint of a colormap to be around
# the values of interest.

class MidpointNormalize(Normalize):
    def __init__(self, vmin=None, vmax=None, midpoint=None, clip=False):
        self.midpoint = midpoint
        Normalize.__init__(self, vmin, vmax, clip)

    def __call__(self, value, clip=None):
        x, y = [self.vmin, self.midpoint, self.vmax], [0, 0.5, 1]
        return np.ma.masked_array(np.interp(value, x, y))

# Load and prepare data set

# dataset for grid search
iris = load_iris()
X = iris.data
y = iris.target

# Dataset for decision function visualization: we only keep the first two
# features in X and sub-sample the dataset to keep only 2 classes and
# make it a binary classification problem.

X_2d = X[:, :2]
X_2d = X_2d[y > 0]
y_2d = y[y > 0]
y_2d -= 1

# It is usually a good idea to scale the data for SVM training.
# We are cheating a bit in this example in scaling all of the data,
# instead of fitting the transformation on the training set and
# just applying it on the test set.

scaler = StandardScaler()
X = scaler.fit_transform(X)
X_2d = scaler.fit_transform(X_2d)

# #############################################################################
# Train classifiers
#
# For an initial search, a logarithmic grid with basis
# 10 is often helpful. Using a basis of 2, a finer
# tuning can be achieved but at a much higher cost.

C_range = np.logspace(-2, 10, 13)
gamma_range = np.logspace(-9, 3, 13)
param_grid = dict(gamma=gamma_range, C=C_range)
cv = StratifiedShuffleSplit(n_splits=5, test_size=0.2, random_state=42)
grid = GridSearchCV(SVC(), param_grid=param_grid, cv=cv)
grid.fit(X, y)

print("The best parameters are %s with a score of %0.2f" % (grid.best_params_, grid.best_score_))

# Now we need to fit a classifier for all parameters in the 2d version
# (we use a smaller set of parameters here because it takes a while to train)

C_2d_range = [1e-2, 1, 1e2]
gamma_2d_range = [1e-1, 1, 1e1]
classifiers = []
for C in C_2d_range:
    for gamma in gamma_2d_range:
        clf = SVC(C=C, gamma=gamma)
        clf.fit(X_2d, y_2d)
        classifiers.append((C, gamma, clf))

# #############################################################################
# Visualization
#
# draw visualization of parameter effects

plt.figure(figsize=(8, 6))
xx, yy = np.meshgrid(np.linspace(-3, 3, 200), np.linspace(-3, 3, 200))

for (k, (C, gamma, clf)) in enumerate(classifiers):
    # evaluate decision function in a grid
    Z = clf.decision_function(np.c_[xx.ravel(), yy.ravel()])
    Z = Z.reshape(xx.shape)

    # visualize decision function for these parameters
    plt.subplot(len(C_2d_range), len(gamma_2d_range), k + 1)
    plt.title("gamma=10^%d, C=10^%d" % (np.log10(gamma), np.log10(C)),
             size='medium')

    # visualize parameter's effect on decision function
    plt.pcolormesh(xx, yy, -Z, cmap=plt.cm.RdBu)
    plt.scatter(X_2d[:, 0], X_2d[:, 1], c=y_2d, cmap=plt.cm.RdBu_r,
                edgecolors='k')
    plt.xticks(())
    plt.yticks(())
    plt.axis('tight')

scores = grid.cv_results_['mean_test_score'].reshape(len(C_range),
             len(gamma_range))

# Draw heatmap of the validation accuracy as a function of gamma and C
#
# The score are encoded as colors with the hot colormap which varies from dark
# red to bright yellow. As the most interesting scores are all located in the
# 0.92 to 0.97 range we use a custom normalizer to set the mid-point to 0.92 so
# to make it easier to visualize the small variations of score values in the
# interesting range while not brutally collapsing all the low score values to
# the same color.

plt.figure(figsize=(8, 6))
plt.subplots_adjust(left=.2, right=0.95, bottom=0.15, top=0.95)
plt.imshow(scores, interpolation='nearest', cmap=plt.cm.hot,
           norm=MidpointNormalize(vmin=0.2, midpoint=0.92))
plt.xlabel('gamma')
plt.ylabel('C')
plt.colorbar()
plt.xticks(np.arange(len(gamma_range)), gamma_range, rotation=45)
plt.yticks(np.arange(len(C_range)), C_range)
plt.title('Validation accuracy')
plt.show()

Total running time of the script: ( 0 minutes 6.234 seconds)
Examples concerning the `sklearn.feature_extraction.text` module.

### 28.1 FeatureHasher and DictVectorizer Comparison

Compares FeatureHasher and DictVectorizer by using both to vectorize text documents.

The example demonstrates syntax and speed only; it doesn’t actually do anything useful with the extracted vectors. See the example scripts `{document_classification_20newsgroups,clustering}.py` for actual learning on text documents.

A discrepancy between the number of terms reported for DictVectorizer and for FeatureHasher is to be expected due to hash collisions.

```python
# Author: Lars Buitinck
# License: BSD 3 clause

from __future__ import print_function
from collections import defaultdict
import re
import sys
from time import time
import numpy as np

from sklearn.datasets import fetch_20newsgroups
from sklearn.feature_extraction import DictVectorizer, FeatureHasher

def n_nonzero_columns(X):
    """Returns the number of non-zero columns in a CSR matrix X."""
    return len(np.unique(X.nonzero()[1]))

def tokens(doc):
    """Extract tokens from doc.

    This uses a simple regex to break strings into tokens. For a more
    principled approach, see CountVectorizer or TfidfVectorizer.
    """
    return (tok.lower() for tok in re.findall(r"\w+", doc))

def token_freqs(doc):
    """Extract a dict mapping tokens from doc to their frequencies."""
```
freq = defaultdict(int)
for tok in tokens(doc):
    freq[tok] += 1
return freq

categories = [
    'alt.atheism',
    'comp.graphics',
    'comp.sys.ibm.pc.hardware',
    'misc.forsale',
    'rec.autos',
    'sci.space',
    'talk.religion.misc',
]
# Uncomment the following line to use a larger set (11k+ documents)
#categories = None

print(__doc__)
print("Usage: %s [n_features_for_hashing]" % sys.argv[0])
print(" The default number of features is 2**18.")
print()
try:
    n_features = int(sys.argv[1])
except IndexError:
    n_features = 2 ** 18
except ValueError:
    print("not a valid number of features: %r" % sys.argv[1])
sys.exit(1)

print("Loading 20 newsgroups training data")
raw_data = fetch_20newsgroups(subset='train', categories=categories).data
data_size_mb = sum(len(s.encode('utf-8')) for s in raw_data) / 1e6
print("%d documents - %0.3f MB" % (len(raw_data), data_size_mb))

print("DictVectorizer")
t0 = time()
vectorizer = DictVectorizer()
vectorizer.fit_transform(token_freqs(d) for d in raw_data)
duration = time() - t0
print("done in %fs at %0.3fMB/s" % (duration, data_size_mb / duration))
print("Found %d unique terms" % len(vectorizer.get_feature_names()))
print()

print("FeatureHasher on frequency dicts")
t0 = time()
hasher = FeatureHasher(n_features=n_features)
X = hasher.transform(token_freqs(d) for d in raw_data)
duration = time() - t0
print("done in %fs at %0.3fMB/s" % (duration, data_size_mb / duration))
print("Found %d unique terms" % n_nonzero_columns(X))
print()

print("FeatureHasher on raw tokens")
t0 = time()
This is an example showing how the scikit-learn can be used to cluster documents by topics using a bag-of-words approach. This example uses a scipy.sparse matrix to store the features instead of standard numpy arrays.

Two feature extraction methods can be used in this example:

- TfidfVectorizer uses an in-memory vocabulary (a python dict) to map the most frequent words to features indices and hence compute a word occurrence frequency (sparse) matrix. The word frequencies are then reweighted using the Inverse Document Frequency (IDF) vector collected feature-wise over the corpus.

- HashingVectorizer hashes word occurrences to a fixed dimensional space, possibly with collisions. The word count vectors are then normalized to each have l2-norm equal to one (projected to the euclidean unit-ball) which seems to be important for k-means to work in high dimensional space.

  HashingVectorizer does not provide IDF weighting as this is a stateless model (the fit method does nothing). When IDF weighting is needed it can be added by pipelining its output to a TfidfTransformer instance.

Two algorithms are demoed: ordinary k-means and its more scalable cousin minibatch k-means.

Additionally, latent semantic analysis can also be used to reduce dimensionality and discover latent patterns in the data.

It can be noted that k-means (and minibatch k-means) are very sensitive to feature scaling and that in this case the IDF weighting helps improve the quality of the clustering by quite a lot as measured against the “ground truth” provided by the class label assignments of the 20 newsgroups dataset.

This improvement is not visible in the Silhouette Coefficient which is small for both as this measure seem to suffer from the phenomenon called “Concentration of Measure” or “Curse of Dimensionality” for high dimensional datasets such as text data. Other measures such as V-measure and Adjusted Rand Index are information theoretic based evaluation scores: as they are only based on cluster assignments rather than distances, hence not affected by the curse of dimensionality.

Note: as k-means is optimizing a non-convex objective function, it will likely end up in a local optimum. Several runs with independent random init might be necessary to get a good convergence.

```python
# Author: Peter Prettenhofer <peter.prettenhofer@gmail.com>
# Lars Buitinck
# License: BSD 3 clause

from __future__ import print_function
from sklearn.datasets import fetch_20newsgroups
from sklearn.decomposition import TruncatedSVD
from sklearn.feature_extraction.text import TfidfVectorizer
from sklearn.feature_extraction.text import HashingVectorizer
from sklearn.feature_extraction.text import TfidfTransformer
from sklearn.pipeline import make_pipeline
from sklearn.preprocessing import Normalizer
from sklearn import metrics
```

28.2 Clustering text documents using k-means
from sklearn.cluster import KMeans, MiniBatchKMeans

import logging
from optparse import OptionParser
import sys
from time import time

import numpy as np

# Display progress logs on stdout
logging.basicConfig(level=logging.INFO,
                    format='%(asctime)s %(levelname)s %(message)s')

# parse commandline arguments
op = OptionParser()
op.add_option("--lsa",
              dest="n_components", type="int",
              help=\"Preprocess documents with latent semantic analysis.\")
op.add_option("--no-minibatch",
              action=\"store_false", dest=\"minibatch\", default=True,
              help=\"Use ordinary k-means algorithm (in batch mode).\")
op.add_option("--no-idf",
              action=\"store_false", dest=\"use_idf\", default=True,
              help=\"Disable Inverse Document Frequency feature weighting.\")
op.add_option("--use-hashing",
              action=\"store_false", default=True,
              help=\"Use a hashing feature vectorizer\")
op.add_option("--n-features", type=int, default=10000,
              help=\"Maximum number of features (dimensions)\"           
              \"to extract from text.\")
op.add_option("--verbose",
              action=\"store_true", dest=\"verbose\", default=False,
              help=\"Print progress reports inside k-means algorithm.\")

print(__doc__)
op.print_help()

def is_interactive():
    return not hasattr(sys.modules[\'__main__\'], \'__file__\')

# work-around for Jupyter notebook and IPython console
argv = [] if is_interactive() else sys.argv[1:]
(opts, args) = op.parse_args(argv)
if len(args) > 0:
op.error("this script takes no arguments.")
sys.exit(1)

# Load some categories from the training set
categories = [
    \'alt.atheism\',
    \'talk.religion.misc\',
    \'comp.graphics\',
    \'sci.space\',
]
# Uncomment the following to do the analysis on all the categories
# categories = None

print("Loading 20 newsgroups dataset for categories:")
print(categories)

dataset = fetch_20newsgroups(subset='all', categories=categories,
    shuffle=True, random_state=42)

print("%d documents" % len(dataset.data))
print("%d categories" % len(dataset.target_names))

labels = dataset.target
ttrue_k = np.unique(labels).shape[0]

print("Extracting features from the training dataset using a sparse vectorizer")
t0 = time()

if opts.use_hashing:
    if opts.use_idf:
        hasher = HashingVectorizer(n_features=opts.n_features,
            stop_words='english', alternate_sign=False,
            norm=None, binary=False)
        vectorizer = make_pipeline(hasher, TfidfTransformer())
    else:
        vectorizer = HashingVectorizer(n_features=opts.n_features,
            stop_words='english',
            alternate_sign=False, norm='l2',
            binary=False)
else:
    vectorizer = TfidfVectorizer(max_df=0.5, max_features=opts.n_features,
        min_df=2, stop_words='english',
        use_idf=opts.use_idf)

X = vectorizer.fit_transform(dataset.data)

print("done in %fs" % (time() - t0))
print("n_samples: %d, n_features: %d" % X.shape)

if opts.n_components:
    print("Performing dimensionality reduction using LSA")
    t0 = time()
    # Vectorizer results are normalized, which makes KMeans behave as
    # spherical k-means for better results. Since LSA/SVD results are
    # not normalized, we have to redo the normalization.
    svd = TruncatedSVD(opts.n_components)
    normalizer = Normalizer(copy=False)
    lsa = make_pipeline(svd, normalizer)

    X = lsa.fit_transform(X)

    print("done in %fs" % (time() - t0))

    explained_variance = svd.explained_variance_ratio_.sum()
    print("Explained variance of the SVD step: {}%".format( int(explained_variance * 100)))
# Do the actual clustering

```python
if opts.minibatch:
    km = MiniBatchKMeans(n_clusters=true_k, init='k-means++', n_init=1,
                        init_size=1000, batch_size=1000, verbose=opts.verbose)
else:
    km = KMeans(n_clusters=true_k, init='k-means++', max_iter=100, n_init=1,
                verbose=opts.verbose)
```

```python
print("Clustering sparse data with %s" % km)
t0 = time()
km.fit(X)
print("done in %0.3fs" % (time() - t0))
print()
```

```python
print("Homogeneity: %0.3f" % metrics.homogeneity_score(labels, km.labels_))
print("Completeness: %0.3f" % metrics.completeness_score(labels, km.labels_))
print("V-measure: %0.3f" % metrics.v_measure_score(labels, km.labels_))
print("Adjusted Rand-Index: %.3f" % metrics.adjusted_rand_score(labels, km.labels_))
print("Silhouette Coefficient: %0.3f" % metrics.silhouette_score(X, km.labels_, sample_size=1000))
print()
```

```python
if not opts.use_hashing:
    print("Top terms per cluster:")
    if opts.n_components:
        original_space_centroids = svd.inverse_transform(km.cluster_centers_)
        order_centroids = original_space_centroids.argsort()[:, ::-1]
    else:
        order_centroids = km.cluster_centers_.argsort()[:, ::-1]

terms = vectorizer.get_feature_names()
for i in range(true_k):
    print("Cluster %d:
```
```
```
```python
else:
    print("done in %0.3fs" % (time() - t0))
print()
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```
The bar plot indicates the accuracy, training time (normalized) and test time (normalized) of each classifier.

```python
# Author: Peter Prettenhofer <peter.prettenhofer@gmail.com>
# Olivier Grisel <olivier.grisel@ensta.org>
# Mathieu Blondel <mathieu@mblondel.org>
# Lars Buitinck
# License: BSD 3 clause

from __future__ import print_function
import logging
import numpy as np
from optparse import OptionParser
import sys
from time import time
import matplotlib.pyplot as plt
from sklearn.datasets import fetch_20newsgroups
from sklearn.feature_extraction.text import TfidfVectorizer
from sklearn.feature_extraction.text import HashingVectorizer
from sklearn.feature_selection import SelectFromModel
from sklearn.feature_selection import SelectKBest, chi2
from sklearn.linear_model import RidgeClassifier
from sklearn.pipeline import Pipeline
from sklearn.svm import LinearSVC
from sklearn.linear_model import SGDClassifier
from sklearn.linear_model import Perceptron
from sklearn.linear_model import PassiveAggressiveClassifier
from sklearn.naive_bayes import BernoulliNB, ComplementNB, MultinomialNB
from sklearn.neighbors import KNeighborsClassifier
from sklearn.neighbors import NearestCentroid
from sklearn.ensemble import RandomForestClassifier
from sklearn.utils.extmath import density
from sklearn import metrics

# Display progress logs on stdout
logging.basicConfig(level=logging.INFO,
    format='%(asctime)s %(levelname)s %(message)s')

# parse commandline arguments
op = OptionParser()
op.add_option("--report",
    action="store_true", dest="print_report",
    help="Print a detailed classification report.")
op.add_option("--chi2_select",
    action="store", type="int", dest="select_chi2",
    help="Select some number of features using a chi-squared test")
op.add_option("--confusion_matrix",
    action="store_true", dest="print_cm",
    help="Print the confusion matrix.")
op.add_option("--top10",
    action="store_true", dest="print_top10",
    help="Print ten most discriminative terms per class"
    " for every classifier.")
op.add_option("--all_categories",
    action="store_true", dest="all_categories",
    help="Whether to use all categories or not.")
```

28.3. Classification of text documents using sparse features
op.add_option("--use_hashing",
    action="store_true",
    help="Use a hashing vectorizer.")

op.add_option("--n_features",
    action="store", type=int, default=2 ** 16,
    help="n_features when using the hashing vectorizer.")

op.add_option("--filtered",
    action="store_true",
    help="Remove newsgroup information that is easily overfit: "
    "headers, signatures, and quoting.")

def is_interactive():
    return not hasattr(sys.modules['__main__'], '__file__')

# work-around for Jupyter notebook and IPython console
argv = []
if is_interactive() else sys.argv[1:]
(opts, args) = op.parse_args(argv)
if len(args) > 0:
    op.error("this script takes no arguments.")
sys.exit(1)

print(__doc__)
op.print_help()
print()

# #############################################################################
# Load some categories from the training set
if opts.all_categories:
    categories = None
else:
    categories = [
        'alt.atheism',
        'talk.religion.misc',
        'comp.graphics',
        'sci.space',
    ]

if opts.filtered:
    remove = ('headers', 'footers', 'quotes')
else:
    remove = ()

print("Loading 20 newsgroups dataset for categories:")
print(categories if categories else "all")

data_train = fetch_20newsgroups(subset='train', categories=categories,
    shuffle=True, random_state=42,
    remove=remove)

data_test = fetch_20newsgroups(subset='test', categories=categories,
    shuffle=True, random_state=42,
    remove=remove)

print('data loaded')

# order of labels in 'target_names' can be different from 'categories'
target_names = data_train.target_names
```python
def size_mb(docs):
    return sum(len(s.encode('utf-8')) for s in docs) / le6

data_train_size_mb = size_mb(data_train.data)
data_test_size_mb = size_mb(data_test.data)

print("%d documents - %0.3fMB (training set)" % (len(data_train.data), data_train_size_mb))
print("%d documents - %0.3fMB (test set)" % (len(data_test.data), data_test_size_mb))
print("%d categories" % len(categories))

# split a training set and a test set
y_train, y_test = data_train.target, data_test.target

print("Extracting features from the training data using a sparse vectorizer")
t0 = time()
if opts.use_hashing:
    vectorizer = HashingVectorizer(stop_words='english', alternate_sign=False,
                                   n_features=opts.n_features)
    X_train = vectorizer.transform(data_train.data)
else:
    vectorizer = TfidfVectorizer(sublinear_tf=True, max_df=0.5,
                                 stop_words='english')
    X_train = vectorizer.fit_transform(data_train.data)
duration = time() - t0
print("done in %f s at %0.3fMB/s" % (duration, data_train_size_mb / duration))
print("n_samples: %d, n_features: %d" % X_train.shape)

print("Extracting features from the test data using the same vectorizer")
t0 = time()
X_test = vectorizer.transform(data_test.data)
duration = time() - t0
print("done in %f s at %0.3fMB/s" % (duration, data_test_size_mb / duration))
print("n_samples: %d, n_features: %d" % X_test.shape)

# mapping from integer feature name to original token string
if opts.use_hashing:
    feature_names = None
else:
    feature_names = vectorizer.get_feature_names()

if opts.select_chi2:
    print("Extracting %d best features by a chi-squared test" %
          opts.select_chi2)
t0 = time()
ch2 = SelectKBest(chi2, k=opts.select_chi2)
X_train = ch2.fit_transform(X_train, y_train)
X_test = ch2.transform(X_test)
if feature_names:
    # keep selected feature names
    feature_names = [feature_names[i] for i
                     in ch2.get_support(indices=True)]
```

28.3. Classification of text documents using sparse features 1191
if feature_names:
    feature_names = np.asarray(feature_names)

def trim(s):
    """Trim string to fit on terminal (assuming 80-column display)""
    return s if len(s) <= 80 else s[:77] + "..."

# Benchmark classifiers
def benchmark(clf):
    print('_' * 80)
    print("Training: ")
    print(clf)
    t0 = time()
    clf.fit(X_train, y_train)
    train_time = time() - t0
    print("train time: %0.3fs" % train_time)
    t0 = time()
    pred = clf.predict(X_test)
    test_time = time() - t0
    print("test time: %0.3fs" % test_time)
    score = metrics.accuracy_score(y_test, pred)
    print("accuracy: %0.3f" % score)
    if hasattr(clf, 'coef_'):
        print("dimensionality: %d" % clf.coef_.shape[1])
        print("density: %f" % density(clf.coef_))
        if opts.print_top10 and feature_names is not None:
            print("top 10 keywords per class:")
            for i, label in enumerate(target_names):
                top10 = np.argsort(clf.coef_[i])[-10:]
                print(trim("%s: %s % (label, " ".join(feature_names[top10]))))
        print()
    if opts.print_report:
        print("classification report:")
        print(metrics.classification_report(y_test, pred,
            target_names=target_names))
    if opts.print_cm:
        print("confusion matrix:")
        print(metrics.confusion_matrix(y_test, pred))
        print()
    clf_descr = str(clf).split('(')[0]
    return clf_descr, score, train_time, test_time

results = []
for clf, name in (
(RidgeClassifier(tol=1e-2, solver="lsqr"), "Ridge Classifier"),
(Perceptron(n_iter=50, tol=1e-3), "Perceptron"),
(PassiveAggressiveClassifier(n_iter=50, tol=1e-3),
 "Passive-Aggressive"),
(KNeighborsClassifier(n_neighbors=10), "kNN"),
(RandomForestClassifier(n_estimators=100), "Random forest"):

print('=' * 80)
print(name)
results.append(benchmark(clf))

for penalty in ["l2", "l1"]:
    print('=' * 80)
    print("%s penalty" % penalty.upper())
    # Train Liblinear model
    results.append(benchmark(LinearSVC(penalty=penalty, dual=False,
                                      tol=1e-3)))

    # Train SGD model
    results.append(benchmark(SGDClassifier(alpha=.0001, n_iter=50,
                                      penalty=penalty,
                                      max_iter=5)))

    # Train SGD with Elastic Net penalty
    print('=' * 80)
    print("Elastic-Net penalty")
    results.append(benchmark(SGDClassifier(alpha=.0001, n_iter=50,
                                      penalty="elasticnet",
                                      max_iter=5)))

    # Train NearestCentroid without threshold
    print('=' * 80)
    print("NearestCentroid (aka Rocchio classifier)")
    results.append(benchmark(NearestCentroid()))

    # Train sparse Naive Bayes classifiers
    print('=' * 80)
    print("Naive Bayes")
    results.append(benchmark(MultinomialNB(alpha=.01)))
    results.append(benchmark(BernoulliNB(alpha=.01)))
    results.append(benchmark(ComplementNB(alpha=.1)))

    print('=' * 80)
    print("LinearSVC with L1-based feature selection")
    # The smaller C, the stronger the regularization.
    # The more regularization, the more sparsity.
    results.append(benchmark(Pipeline(["feature_selection",
                                       SelectFromModel(LinearSVC(penalty="l1", dual=False,
                                         tol=1e-3))],
                                       "classification",
                                       LinearSVC(penalty="l2"))))

    # make some plots

indices = np.arange(len(results))
results = [[x[i] for x in results] for i in range(4)]

clf_names, score, training_time, test_time = results
training_time = np.array(training_time) / np.max(training_time)
test_time = np.array(test_time) / np.max(test_time)

plt.figure(figsize=(12, 8))
plt.title("Score")
plt.barh(indices, score, .2, label="score", color='navy')
plt.barh(indices + .3, training_time, .2, label="training time", color='c')
plt.barh(indices + .6, test_time, .2, label="test time", color='darkorange')
plt.yticks(())
plt.legend(loc='best')
plt.subplots_adjust(left=.25)
plt.subplots_adjust(top=.95)
plt.subplots_adjust(bottom=.05)

for i, c in zip(indices, clf_names):
    plt.text(-.3, i, c)

plt.show()

**Total running time of the script:** ( 0 minutes 0.000 seconds)
Examples concerning the `sklearn.tree` module.

### 29.1 Decision Tree Regression

A 1D regression with decision tree.

The decision trees is used to fit a sine curve with addition noisy observation. As a result, it learns local linear regressions approximating the sine curve.

We can see that if the maximum depth of the tree (controlled by the `max_depth` parameter) is set too high, the decision trees learn too fine details of the training data and learn from the noise, i.e. they overfit.
# Import the necessary modules and libraries
import numpy as np
from sklearn.tree import DecisionTreeRegressor
import matplotlib.pyplot as plt

# Create a random dataset
rng = np.random.RandomState(1)
X = np.sort(5 * rng.rand(80, 1), axis=0)
y = np.sin(X).ravel()
y[::5] += 3 * (0.5 - rng.rand(16))

# Fit regression model
regr_1 = DecisionTreeRegressor(max_depth=2)
regr_2 = DecisionTreeRegressor(max_depth=5)
regr_1.fit(X, y)
regr_2.fit(X, y)

# Predict
X_test = np.arange(0.0, 5.0, 0.01)[:, np.newaxis]
y_1 = regr_1.predict(X_test)
y_2 = regr_2.predict(X_test)

# Plot the results
plt.figure()
plt.scatter(X, y, s=20, edgecolor="black", c="darkorange", label="data")
plt.plot(X_test, y_1, color="cornflowerblue", label="max_depth=2", linewidth=2)
plt.plot(X_test, y_2, color="yellowgreen", label="max_depth=5", linewidth=2)
plt.xlabel("data")
plt.ylabel("target")
plt.title("Decision Tree Regression")
plt.legend()
plt.show()

Total running time of the script: ( 0 minutes 0.113 seconds)

## 29.2 Multi-output Decision Tree Regression

An example to illustrate multi-output regression with decision tree.

The decision trees is used to predict simultaneously the noisy x and y observations of a circle given a single underlying feature. As a result, it learns local linear regressions approximating the circle.

We can see that if the maximum depth of the tree (controlled by the max_depth parameter) is set too high, the decision trees learn too fine details of the training data and learn from the noise, i.e. they overfit.
```python
import numpy as np
import matplotlib.pyplot as plt
from sklearn.tree import DecisionTreeRegressor

# Create a random dataset
rng = np.random.RandomState(1)
X = np.sort(200 * rng.rand(100, 1) - 100, axis=0)
y = np.array([np.pi * np.sin(X).ravel(), np.pi * np.cos(X).ravel()]).T
y[::5, :] += (0.5 - rng.rand(20, 2))

# Fit regression model
regr_1 = DecisionTreeRegressor(max_depth=2)
regr_2 = DecisionTreeRegressor(max_depth=5)
regr_3 = DecisionTreeRegressor(max_depth=8)
regr_1.fit(X, y)
regr_2.fit(X, y)
regr_3.fit(X, y)

# Predict
X_test = np.arange(-100.0, 100.0, 0.01)[:, np.newaxis]
y_1 = regr_1.predict(X_test)
y_2 = regr_2.predict(X_test)
y_3 = regr_3.predict(X_test)
```

29.2. Multi-output Decision Tree Regression
# Plot the results
plt.figure()
s = 25
plt.scatter(y[:, 0], y[:, 1], c="navy", s=s,
            edgecolor="black", label="data")
plt.scatter(y_1[:, 0], y_1[:, 1], c="cornflowerblue", s=s,
            edgecolor="black", label="max_depth=2")
plt.scatter(y_2[:, 0], y_2[:, 1], c="red", s=s,
            edgecolor="black", label="max_depth=5")
plt.scatter(y_3[:, 0], y_3[:, 1], c="orange", s=s,
            edgecolor="black", label="max_depth=8")
plt.xlim([-6, 6])
plt.ylim([-6, 6])
plt.xlabel("target 1")
plt.ylabel("target 2")
plt.title("Multi-output Decision Tree Regression")
plt.legend(loc="best")
plt.show()

Total running time of the script: ( 0 minutes 0.191 seconds)

29.3 Plot the decision surface of a decision tree on the iris dataset

Plot the decision surface of a decision tree trained on pairs of features of the iris dataset.

See decision tree for more information on the estimator.

For each pair of iris features, the decision tree learns decision boundaries made of combinations of simple thresholding rules inferred from the training samples.
Decision surface of a decision tree using paired features

```
print(__doc__)

import numpy as np
import matplotlib.pyplot as plt

from sklearn.datasets import load_iris
from sklearn.tree import DecisionTreeClassifier

# Parameters
n_classes = 3
plot_colors = "ryb"
plot_step = 0.02

# Load data
iris = load_iris()

for pairidx, pair in enumerate([[0, 1], [0, 2], [0, 3], [1, 2], [1, 3], [2, 3]]):
    # We only take the two corresponding features
    X = iris.data[:, pair]
y = iris.target

    # Train
    clf = DecisionTreeClassifier().fit(X, y)

    # Plot the decision boundary
```

29.3. Plot the decision surface of a decision tree on the iris dataset
29.4 Understanding the decision tree structure

The decision tree structure can be analysed to gain further insight on the relation between the features and the target to predict. In this example, we show how to retrieve:

- the binary tree structure;
- the depth of each node and whether or not it’s a leaf;
- the nodes that were reached by a sample using the `decision_path` method;
- the leaf that was reached by a sample using the `apply` method;
- the rules that were used to predict a sample;
- the decision path shared by a group of samples.

Out:

```
The binary tree structure has 5 nodes and has the following tree structure:
node=0 test node: go to node 1 if X[:, 3] <= 0.800000011921 else to node 2.
    node=1 leaf node.
    node=2 test node: go to node 3 if X[:, 2] <= 4.94999980927 else to node 4.
        node=3 leaf node.
        node=4 leaf node.

Rules used to predict sample 0:
decision id node 4 : (X_test[0, 2] (= 5.1) > -2.0)
```
The following samples [0, 1] share the node [0 2] in the tree.
It is 40.0 % of all nodes.

```python
import numpy as np

from sklearn.model_selection import train_test_split
from sklearn.datasets import load_iris
from sklearn.tree import DecisionTreeClassifier

iris = load_iris()
X = iris.data
y = iris.target
X_train, X_test, y_train, y_test = train_test_split(X, y, random_state=0)

estimator = DecisionTreeClassifier(max_leaf_nodes=3, random_state=0)
estimator.fit(X_train, y_train)

# The decision estimator has an attribute called tree_ which stores the entire
# tree structure and allows access to low level attributes. The binary tree
# is represented as a number of parallel arrays. The i-th element of each
# array holds information about the node `i`. Node 0 is the tree's root. NOTE:
# Some of the arrays only apply to either leaves or split nodes, resp. In this
# case the values of nodes of the other type are arbitrary!
#
# Among those arrays, we have:
# - left_child, id of the left child of the node
# - right_child, id of the right child of the node
# - feature, feature used for splitting the node
# - threshold, threshold value at the node
#
# Using those arrays, we can parse the tree structure:

n_nodes = estimator.tree_.node_count
children_left = estimator.tree_.children_left
children_right = estimator.tree_.children_right
feature = estimator.tree_.feature
threshold = estimator.tree_.threshold

# The tree structure can be traversed to compute various properties such
# as the depth of each node and whether or not it is a leaf.
node_depth = np.zeros(shape=n_nodes, dtype=np.int64)
is_leaves = np.zeros(shape=n_nodes, dtype=bool)
stack = [(0, -1)]
# seed is the root node id and its parent depth
while len(stack) > 0:
    node_id, parent_depth = stack.pop()
    node_depth[node_id] = parent_depth + 1

    # If we have a test node
    if (children_left[node_id] != children_right[node_id]):
        stack.append((children_left[node_id], parent_depth + 1))
        stack.append((children_right[node_id], parent_depth + 1))
```

29.4. Understanding the decision tree structure
else:
    is_leaves[node_id] = True

print("The binary tree structure has %s nodes and has "
      "the following tree structure:
      " % n_nodes)
for i in range(n_nodes):
    if is_leaves[i]:
        print("%s node=%s leaf node." % (node_depth[i] * \t", i))
    else:
        print("%s node=%s test node: go to node %s if X[:, %s] <= %s else to "
              "node %s.
              " % (node_depth[i] * \t",
              1,
              children_left[i],
              feature[i],
              threshold[i],
              children_right[i],
              ))

print()

# First let’s retrieve the decision path of each sample. The decision_path
# method allows to retrieve the node indicator functions. A non zero element of
# indicator matrix at the position (i, j) indicates that the sample i goes
# through the node j.

node_indicator = estimator.decision_path(X_test)

# Similarly, we can also have the leaves ids reached by each sample.

leave_id = estimator.apply(X_test)

# Now, it’s possible to get the tests that were used to predict a sample or
# a group of samples. First, let’s make it for the sample.

sample_id = 0
node_index = node_indicator.indices[node_indicator.indptr[sample_id]:
                                       node_indicator.indptr[sample_id + 1]]

print('Rules used to predict sample %s: ' % sample_id)
for node_id in node_index:
    if leave_id[sample_id] != node_id:
        continue

    if (X_test[sample_id, feature[node_id]] <= threshold[node_id]):
        threshold_sign = "<="
    else:
        threshold_sign = "">

    print("decision id node %s : (X_test[%s, %s] (= %s) %s %s)
          % (node_id,
             sample_id,
             feature[node_id],
             X_test[sample_id, feature[node_id]],
             threshold_sign,
             threshold[node_id]))

# For a group of samples, we have the following common node.
sample_ids = [0, 1]
common_nodes = (node_indicator.toarray()[sample_ids].sum(axis=0) ==
              len(sample_ids))

common_node_id = np.arange(n_nodes)[common_nodes]

print("\nThe following samples \$s share the node \$s in the tree"
      % (sample_ids, common_node_id))
print("It is \$s \$% of all nodes." % (100 * len(common_node_id) / n_nodes,))

**Total running time of the script:** ( 0 minutes 0.004 seconds)
This is the class and function reference of scikit-learn. Please refer to the full user guide for further details, as the class and function raw specifications may not be enough to give full guidelines on their uses.

### 30.1 sklearn.base: Base classes and utility functions

Base classes for all estimators.

#### 30.1.1 Base classes

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>base.BaseEstimator</code></td>
<td>Base class for all estimators in scikit-learn</td>
</tr>
<tr>
<td><code>base.BiclusterMixin</code></td>
<td>Mixin class for all bicluster estimators in scikit-learn</td>
</tr>
<tr>
<td><code>base.ClassifierMixin</code></td>
<td>Mixin class for all classifiers in scikit-learn</td>
</tr>
<tr>
<td><code>base.ClusterMixin</code></td>
<td>Mixin class for all cluster estimators in scikit-learn.</td>
</tr>
<tr>
<td><code>base.DensityMixin</code></td>
<td>Mixin class for all density estimators in scikit-learn.</td>
</tr>
<tr>
<td><code>base.RegressorMixin</code></td>
<td>Mixin class for all regression estimators in scikit-learn.</td>
</tr>
<tr>
<td><code>base.TransformerMixin</code></td>
<td>Mixin class for all transformers in scikit-learn</td>
</tr>
</tbody>
</table>

#### sklearn.base.BaseEstimator

**class sklearn.base.BaseEstimator**

Base class for all estimators in scikit-learn

#### Notes

All estimators should specify all the parameters that can be set at the class level in their `__init__` as explicit keyword arguments (no `*args` or `**kwargs`).

#### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>__init__</code> ($self, /, *args, **kwargs)`</td>
<td>Initialize self. See help(type(self)) for accurate signature.</td>
</tr>
</tbody>
</table>
get_params (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.base.BaseEstimator

• Feature Union with Heterogeneous Data Sources

sklearn.base.BiclusterMixin

class sklearn.base.BiclusterMixin

Mixin class for all bicluster estimators in scikit-learn

Attributes

biclusters_ Convenient way to get row and column indicators together.

Methods

get_indices(i) Row and column indices of the i’th bicluster.

get_shape(i) Shape of the i’th bicluster.

get_submatrix(i, data) Returns the submatrix corresponding to bicluster i.

__init__(self, /, *args, **kwargs)

Initialize self. See help(type(self)) for accurate signature.

biclusters_ Convenient way to get row and column indicators together.

Returns the rows_ and columns_ members.

get_indices (i) Row and column indices of the i’th bicluster.

Only works if rows_ and columns_ attributes exist.

Parameters i : int
The index of the cluster.

**Returns** row_ind : np.array, dtype=np.intp

Indices of rows in the dataset that belong to the bicluster.

col_ind : np.array, dtype=np.intp

Indices of columns in the dataset that belong to the bicluster.

**get_shape**(i)

Shape of the i’th bicluster.

**Parameters**

i : int

The index of the cluster.

**Returns** shape : (int, int)

Number of rows and columns (resp.) in the bicluster.

**get_submatrix**(i, data)

Returns the submatrix corresponding to bicluster i.

**Parameters**

i : int

The index of the cluster.

data : array

The data.

**Returns** submatrix : array

The submatrix corresponding to bicluster i.

**Notes**

Works with sparse matrices. Only works if rows_ and columns_ attributes exist.

**sklearn.base.ClassifierMixin**

class sklearn.base.ClassifierMixin

Mixin class for all classifiers in scikit-learn.

**Methods**

**score**(X, y[, sample_weight])

Returns the mean accuracy on the given test data and labels.

**__init__**(self, /, *args, **kwargs)

Initialize self. See help(type(self)) for accurate signature.

**score**(X, y, sample_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

X : array-like, shape = (n_samples, n_features)
Test samples.

\[
y : \text{array-like, shape} = (n_{\text{samples}}) \text{ or } (n_{\text{samples}}, n_{\text{outputs}})
\]
True labels for X.

\[
\text{sample_weight} : \text{array-like, shape} = [n_{\text{samples}}], \text{optional}
\]
Sample weights.

**Returns** score : float
Mean accuracy of self.predict(X) wrt. y.

### sklearn.base.ClusterMixin

class sklearn.base.ClusterMixin
    Mixin class for all cluster estimators in scikit-learn.

#### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit_predict</td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td><strong>init</strong></td>
<td>Initialize self. See help(type(self)) for accurate signature.</td>
</tr>
<tr>
<td>fit_predict</td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td>Parameters X</td>
<td>ndarray, shape (n_samples, n_features)</td>
</tr>
<tr>
<td>Returns y</td>
<td>ndarray, shape (n_samples,)</td>
</tr>
<tr>
<td>cluster labels</td>
<td></td>
</tr>
</tbody>
</table>

### sklearn.base.DensityMixin

class sklearn.base.DensityMixin
    Mixin class for all density estimators in scikit-learn.

#### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>score</td>
<td>Returns the score of the model on the data X</td>
</tr>
<tr>
<td><strong>init</strong></td>
<td>Initialize self. See help(type(self)) for accurate signature.</td>
</tr>
<tr>
<td>score</td>
<td>Returns the score of the model on the data X</td>
</tr>
<tr>
<td>Parameters X</td>
<td>array-like, shape = (n_samples, n_features)</td>
</tr>
<tr>
<td>Returns score</td>
<td>float</td>
</tr>
</tbody>
</table>

sklearn.base.RegressorMixin

class sklearn.base.RegressorMixin

    Mixin class for all regression estimators in scikit-learn.

    Methods

    score(X, y[, sample_weight])

    Returns the coefficient of determination $R^2$ of the prediction.

    __init__(self, *args, **kwargs)

    Initialize self. See help(type(self)) for accurate signature.

    score(X, y, sample_weight=None)

    Returns the coefficient of determination $R^2$ of the prediction.

    The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $(y_{true} - y_{pred})^2$.sum() and $v$ is the total sum of squares $(y_{true} - y_{true}.mean())^2$.sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

    Parameters

    X : array-like, shape = (n_samples, n_features)
        Test samples.

    y : array-like, shape = (n_samples) or (n_samples, n_outputs)
        True values for X.

    sample_weight : array-like, shape = [n_samples], optional
        Sample weights.

    Returns

    score : float
        $R^2$ of self.predict(X) wrt. $y$.

sklearn.base.TransformerMixin

class sklearn.base.TransformerMixin

    Mixin class for all transformers in scikit-learn.

    Methods

    fit_transform(X[, y])

    Fit to data, then transform it.

    __init__(self, *args, **kwargs)

    Initialize self. See help(type(self)) for accurate signature.

    fit_transform(X, y=None, **fit_params)

    Fit to data, then transform it.

    Fits transformer to $X$ and $y$ with optional parameters fit_params and returns a transformed version of $X$.

    Parameters

    X : numpy array of shape [n_samples, n_features]
Training set.

\( y \) : numpy array of shape \([n_{samples}]\)

Target values.

Returns \( X_{new} \) : numpy array of shape \([n_{samples}, n_{features}_{new}]\)

Transformed array.

Examples using sklearn.base.TransformerMixin

- Feature Union with Heterogeneous Data Sources

### 30.1.2 Functions

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>base.clone(estimator[, safe])</td>
<td>Constructs a new estimator with the same parameters.</td>
</tr>
<tr>
<td>config_context(**new_config)</td>
<td>Context manager for global scikit-learn configuration</td>
</tr>
<tr>
<td>get_config()</td>
<td>Retrieve current values for configuration set by set_config</td>
</tr>
<tr>
<td>set_config([assume_finite])</td>
<td>Set global scikit-learn configuration</td>
</tr>
</tbody>
</table>

**sklearn.base.clone**

```python
sklearn.base.clone(estimator, safe=True)
```

Constructs a new estimator with the same parameters.

Clone does a deep copy of the model in an estimator without actually copying attached data. It yields a new estimator with the same parameters that has not been fit on any data.

**Parameters** 

- **estimator**: estimator object, or list, tuple or set of objects
- **safe**: boolean, optional

If safe is false, clone will fall back to a deep copy on objects that are not estimators.

**sklearn.config_context**

```python
sklearn.config_context(**new_config)
```

Context manager for global scikit-learn configuration

**Parameters** 

- **assume_finite**: bool, optional

If True, validation for finiteness will be skipped, saving time, but leading to potential crashes. If False, validation for finiteness will be performed, avoiding error.

**Notes**

All settings, not just those presently modified, will be returned to their previous values when the context manager is exited. This is not thread-safe.
Examples

```python
>>> import sklearn
>>> from sklearn.utils.validation import assert_all_finite
>>> with sklearn.config_context(assume_finite=True):
...     assert_all_finite([float('nan')])
>>> with sklearn.config_context(assume_finite=True):
...     with sklearn.config_context(assume_finite=False):
...         assert_all_finite([float('nan')])
...     Traceback (most recent call last):
...     ValueError: Input contains NaN, ...
```

sklearn.get_config

```python
sklearn.get_config()
```

Retrieve current values for configuration set by `set_config`

**Returns**

`config`: dict

Keys are parameter names that can be passed to `set_config`.

sklearn.set_config

```python
sklearn.set_config(assume_finite=None)
```

Set global scikit-learn configuration

**Parameters**

`assume_finite`: bool, optional

If True, validation for finiteness will be skipped, saving time, but leading to potential crashes. If False, validation for finiteness will be performed, avoiding error.

### 30.2 sklearn.calibration: Probability Calibration

Calibration of predicted probabilities.

**User guide:** See the Probability calibration section for further details.

```
calibration.CalibratedClassifierCV([...]) Probability calibration with isotonic regression or sigmoid.
```

#### 30.2.1 sklearn.calibration.CalibratedClassifierCV

**class** `sklearn.calibration.CalibratedClassifierCV(base_estimator=None, method='sigmoid', cv=3)`

Probability calibration with isotonic regression or sigmoid.

With this class, the base_estimator is fit on the train set of the cross-validation generator and the test set is used for calibration. The probabilities for each of the folds are then averaged for prediction. In case that cv="prefit" is passed to `__init__`, it is assumed that base_estimator has been fitted already and all data is used for calibration. Note that data for fitting the classifier and for calibrating it must be disjoint.

Read more in the User Guide.
Parameters `base_estimator`: instance BaseEstimator

The classifier whose output decision function needs to be calibrated to offer more accurate predict_proba outputs. If cv=prefit, the classifier must have been fit already on data.

`method`: ‘sigmoid’ or ‘isotonic’

The method to use for calibration. Can be ‘sigmoid’ which corresponds to Platt’s method or ‘isotonic’ which is a non-parametric approach. It is not advised to use isotonic calibration with too few calibration samples (<<1000) since it tends to overfit. Use sigmoids (Platt’s calibration) in this case.

`cv`: integer, cross-validation generator, iterable or “prefit”, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds,
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if y is binary or multiclass, `sklearn.model_selection.StratifiedKFold` is used. If y is neither binary nor multiclass, `sklearn.model_selection.KFold` is used.

Refer User Guide for the various cross-validation strategies that can be used here.

If “prefit” is passed, it is assumed that base_estimator has been fitted already and all data is used for calibration.

Attributes

<table>
<thead>
<tr>
<th>classes_</th>
<th>(array, shape (n_classes)) The class labels.</th>
</tr>
</thead>
<tbody>
<tr>
<td>calibrated_classifiers_</td>
<td>(list (len() equal to cv or 1 if cv == “prefit”) The list of calibrated classifiers, one for each validation fold, which has been fitted on all but the validation fold and calibrated on the validation fold.)</td>
</tr>
</tbody>
</table>

References

[R14], [R24], [R34], [R44]

Methods

<table>
<thead>
<tr>
<th>fit(X, y[, sample_weight])</th>
<th>Fit the calibrated model</th>
</tr>
</thead>
<tbody>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict the target of new samples.</td>
</tr>
<tr>
<td>predict_proba(X)</td>
<td>Posterior probabilities of classification</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>
__init__ (base_estimator=None, method='sigmoid', cv=3)

fit (X, y, sample_weight=) None)
    Fit the calibrated model

    Parameters X : array-like, shape (n_samples, n_features)
        Training data.
    y : array-like, shape (n_samples,)
        Target values.
    sample_weight : array-like, shape = [n_samples] or None
        Sample weights. If None, then samples are equally weighted.

    Returns self : object
        Returns an instance of self.

get_params (deep=True)
    Get parameters for this estimator.

        Parameters deep : boolean, optional
            If True, will return the parameters for this estimator and contained subobjects that are
            estimators.

        Returns params : mapping of string to any
            Parameter names mapped to their values.

predict (X)
    Predict the target of new samples. Can be different from the prediction of the uncalibrated classifier.

        Parameters X : array-like, shape (n_samples, n_features)
            The samples.

        Returns C : array, shape (n_samples,)
            The predicted class.

predict_proba (X)
    Posterior probabilities of classification

    This function returns posterior probabilities of classification according to each class on an array of test
    vectors X.

        Parameters X : array-like, shape (n_samples, n_features)
            The samples.

        Returns C : array, shape (n_samples, n_classes)
            The predicted probas.

score (X, y, sample_weight=)
    Returns the mean accuracy on the given test data and labels.

    In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each
    sample that each label set be correctly predicted.

        Parameters X : array-like, shape = (n_samples, n_features)
            Test samples.
    y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

**sample_weight**: array-like, shape = [n_samples], optional
Sample weights.

**Returns** score : float
Mean accuracy of self.predict(X) wrt. y.

**set_params**(**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns** self

**Examples using sklearn.calibration.CalibratedClassifierCV**

- Probability Calibration curves
- Probability calibration of classifiers
- Probability Calibration for 3-class classification

```
calibration.calibration_curve(y_true, y_prob)
```

Compute true and predicted probabilities for a calibration curve.

**30.2.2 sklearn.calibration.calibration_curve**

sklearn.calibration.calibration_curve (y_true, y_prob, normalize=False, n_bins=5)

Compute true and predicted probabilities for a calibration curve.

Calibration curves may also be referred to as reliability diagrams.

Read more in the *User Guide*.

**Parameters** y_true : array, shape (n_samples,)
True targets.

y_prob : array, shape (n_samples,)
Probabilities of the positive class.

normalize : bool, optional, default=False
Whether y_prob needs to be normalized into the bin [0, 1], i.e. is not a proper probability. If True, the smallest value in y_prob is mapped onto 0 and the largest one onto 1.

n_bins : int
Number of bins. A bigger number requires more data.

**Returns** prob_true : array, shape (n_bins,)
The true probability in each bin (fraction of positives).

prob_pred : array, shape (n_bins,)
The mean predicted probability in each bin.

References


Examples using sklearn.calibration.calibration_curve

- Comparison of Calibration of Classifiers
- Probability Calibration curves

30.3 sklearn.cluster: Clustering

The sklearn.cluster module gathers popular unsupervised clustering algorithms.

User guide: See the Clustering section for further details.

30.3.1 Classes

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>sklearn.cluster.AffinityPropagation</td>
<td>Perform Affinity Propagation Clustering of data.</td>
</tr>
<tr>
<td>sklearn.cluster.AgglomerativeClustering</td>
<td>Agglomerative Clustering</td>
</tr>
<tr>
<td>sklearn.cluster.Birch</td>
<td>Implements the Birch clustering algorithm.</td>
</tr>
<tr>
<td>sklearn.cluster.DBSCAN</td>
<td>Perform DBSCAN clustering from vector array or distance matrix.</td>
</tr>
<tr>
<td>sklearn.cluster.FeatureAgglomeration</td>
<td>Agglomerate features.</td>
</tr>
<tr>
<td>sklearn.cluster.KMeans</td>
<td>K-Means clustering</td>
</tr>
<tr>
<td>sklearn.cluster.MiniBatchKMeans</td>
<td>Mini-Batch K-Means clustering</td>
</tr>
<tr>
<td>sklearn.cluster.MeanShift</td>
<td>Mean shift clustering using a flat kernel.</td>
</tr>
<tr>
<td>sklearn.cluster.SpectralClustering</td>
<td>Apply clustering to a projection to the normalized laplacian.</td>
</tr>
</tbody>
</table>

sklearn.cluster.AffinityPropagation

class sklearn.cluster.AffinityPropagation (damping=0.5, max_iter=200, convergence_iter=15, copy=True, preference=None, affinity='euclidean', verbose=False)

Perform Affinity Propagation Clustering of data.

Read more in the User Guide.

Parameters damping : float, optional, default: 0.5

Damping factor (between 0.5 and 1) is the extent to which the current value is maintained relative to incoming values (weighted 1 - damping). This in order to avoid numerical oscillations when updating these values (messages).

max_iter : int, optional, default: 200
Maximum number of iterations.

**convergence_iter** : int, optional, default: 15

Number of iterations with no change in the number of estimated clusters that stops the convergence.

**copy** : boolean, optional, default: True

Make a copy of input data.

**preference** : array-like, shape (n_samples,) or float, optional

Preferences for each point - points with larger values of preferences are more likely to be chosen as exemplars. The number of exemplars, i.e., clusters, is influenced by the input preferences value. If the preferences are not passed as arguments, they will be set to the median of the input similarities.

**affinity** : string, optional, default=``euclidean``

Which affinity to use. At the moment precomputed and euclidean are supported. euclidean uses the negative squared euclidean distance between points.

**verbose** : boolean, optional, default: False

Whether to be verbose.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>cluster_centers_indices</strong></td>
<td>(array, shape (n_clusters,)) Indices of cluster centers</td>
</tr>
<tr>
<td><strong>cluster_centers</strong></td>
<td>(array, shape (n_clusters, n_features)) Cluster centers (if affinity != precomputed).</td>
</tr>
<tr>
<td><strong>labels</strong></td>
<td>(array, shape (n_samples,)) Labels of each point</td>
</tr>
<tr>
<td><strong>affinity_matrix</strong></td>
<td>(array, shape (n_samples, n_samples)) Stores the affinity matrix used in fit.</td>
</tr>
<tr>
<td><strong>n_iter</strong></td>
<td>(int) Number of iterations taken to converge.</td>
</tr>
</tbody>
</table>

### Notes

For an example, see `examples/cluster/plot_affinity_propagation.py`.

The algorithmic complexity of affinity propagation is quadratic in the number of points.

When `fit` does not converge, `cluster_centers_` becomes an empty array and all training samples will be labelled as -1. In addition, `predict` will then label every sample as -1.

When all training samples have equal similarities and equal preferences, the assignment of cluster centers and labels depends on the preference. If the preference is smaller than the similarities, `fit` will result in a single cluster center and label 0 for every sample. Otherwise, every training sample becomes its own cluster center and is assigned a unique label.

### References

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Create affinity matrix from negative euclidean distances, then apply affinity propagation clustering.</td>
</tr>
<tr>
<td><code>fit_predict(X[, y])</code></td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict the closest cluster each sample in X belongs to.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**__init__** (damping=0.5, max_iter=200, convergence_iter=15, copy=True, preference=None, affinity='euclidean', verbose=False)

**fit** (X, y=None)

Create affinity matrix from negative euclidean distances, then apply affinity propagation clustering.

**Parameters**

- **X**: array-like, shape (n_samples, n_features) or (n_samples, n_samples)
  Data matrix or, if affinity is precomputed, matrix of similarities / affinities.
- **y**: Ignored

**fit_predict** (X, y=None)

Performs clustering on X and returns cluster labels.

**Parameters**

- **X**: ndarray, shape (n_samples, n_features)
  Input data.

**Returns**

- **y**: ndarray, shape (n_samples,)
  cluster labels

**get_params** (deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**predict** (X)

Predict the closest cluster each sample in X belongs to.

**Parameters**

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  New data to predict.

**Returns**

- **labels**: array, shape (n_samples,)
  Index of the cluster each sample belongs to.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**
Examples using `sklearn.cluster.AffinityPropagation`

- Demo of affinity propagation clustering algorithm
- Comparing different clustering algorithms on toy datasets

`sklearn.cluster.AgglomerativeClustering`

class `sklearn.cluster.AgglomerativeClustering`:

```python
AgglomerativeClustering(n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func='deprecated')
```

Agglomerative Clustering

Recursively merges the pair of clusters that minimally increases a given linkage distance.


**Parameters**

- **n_clusters**: int, default=2
  The number of clusters to find.
- **affinity**: string or callable, default: “euclidean”
  Metric used to compute the linkage. Can be “euclidean”, “l1”, “l2”, “manhattan”, “cosine”, or ‘precomputed’. If linkage is “ward”, only “euclidean” is accepted.
- **memory**: None, str or object with the joblib.Memory interface, optional
  Used to cache the output of the computation of the tree. By default, no caching is done. If a string is given, it is the path to the caching directory.
- **connectivity**: array-like or callable, optional
  Connectivity matrix. Defines for each sample the neighboring samples following a given structure of the data. This can be a connectivity matrix itself or a callable that transforms the data into a connectivity matrix, such as derived from kneighbors_graph. Default is None, i.e, the hierarchical clustering algorithm is unstructured.
- **compute_full_tree**: bool or ‘auto’ (optional)
  Stop early the construction of the tree at n_clusters. This is useful to decrease computation time if the number of clusters is not small compared to the number of samples. This option is useful only when specifying a connectivity matrix. Note also that when varying the number of clusters and using caching, it may be advantageous to compute the full tree.
- **linkage**: {“ward”, “complete”, “average”}, optional, default: “ward”
  Which linkage criterion to use. The linkage criterion determines which distance to use between sets of observation. The algorithm will merge the pairs of cluster that minimize this criterion.
  - ward minimizes the variance of the clusters being merged.
  - average uses the average of the distances of each observation of the two sets.
  - complete or maximum linkage uses the maximum distances between all observations of the two sets.
- **pooling_func**: callable, default='deprecated'}
Ignoring.

Deprecation since version 0.20: pooling_func has been deprecated in 0.20 and will be removed in 0.22.

Attributes

<table>
<thead>
<tr>
<th>labels_</th>
<th>(array [n_samples]) cluster labels for each point</th>
</tr>
</thead>
<tbody>
<tr>
<td>n_leaves</td>
<td>Number of leaves in the hierarchical tree.</td>
</tr>
<tr>
<td>n_components</td>
<td>estimated number of connected components in the graph.</td>
</tr>
<tr>
<td>children_</td>
<td>(array-like, shape (n_nodes-1, 2)) The children of each non-leaf node. Values less than n_samples correspond to leaves of the tree which are the original samples. A node i greater than or equal to n_samples is a non-leaf node and has children children[i-1:n_samples]. Alternatively at the i-th iteration, children[i][0] and children[i][1] are merged to form node n_samples + i</td>
</tr>
</tbody>
</table>

Methods

<table>
<thead>
<tr>
<th>fit(X[, y])</th>
<th>Fit the hierarchical clustering on the data</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit_predict(X[, y])</td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func='deprecated')

fit (X, y=None)
Fit the hierarchical clustering on the data

Parameters

X : array-like, shape = [n_samples, n_features]
Training data. Shape [n_samples, n_features], or [n_samples, n_samples] if affinity=='precomputed'.

y : Ignored

Returns

self

fit_predict (X, y=None)
Performs clustering on X and returns cluster labels.

Parameters

X : ndarray, shape (n_samples, n_features)
Input data.

Returns

y : ndarray, shape (n_samples,)
Cluster labels

get_params (deep=True)
Get parameters for this estimator.

Parameters

deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.
Returns `params` : mapping of string to any
Parameter names mapped to their values.

`set_params (**params)`
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns `self`

Examples using `sklearn.cluster.AgglomerativeClustering`

- A demo of structured Ward hierarchical clustering on a raccoon face image
- Agglomerative clustering with and without structure
- Various Agglomerative Clustering on a 2D embedding of digits
- Hierarchical clustering: structured vs unstructured ward
- Agglomerative clustering with different metrics
- Comparing different clustering algorithms on toy datasets

`sklearn.cluster.Birch`

class `sklearn.cluster.Birch` (`threshold=0.5, branching_factor=50, n_clusters=3, compute_labels=True, copy=True`) Implements the Birch clustering algorithm.

It is a memory-efficient, online-learning algorithm provided as an alternative to `MiniBatchKMeans`. It constructs a tree data structure with the cluster centroids being read off the leaf. These can be either the final cluster centroids or can be provided as input to another clustering algorithm such as `AgglomerativeClustering`.

Read more in the User Guide.

**Parameters**

- `threshold` : float, default 0.5
  The radius of the subcluster obtained by merging a new sample and the closest subcluster should be lesser than the threshold. Otherwise a new subcluster is started. Setting this value to be very low promotes splitting and vice-versa.

- `branching_factor` : int, default 50
  Maximum number of CF subclusters in each node. If a new samples enters such that the number of subclusters exceed the branching_factor then that node is split into two nodes with the subclusters redistributed in each. The parent subcluster of that node is removed and two new subclusters are added as parents of the 2 split nodes.

- `n_clusters` : int, instance of sklearn.cluster model, default 3
  Number of clusters after the final clustering step, which treats the subclusters from the leaves as new samples.
  - `None` : the final clustering step is not performed and the subclusters are returned as they are.
• `sklearn.cluster` Estimator: If a model is provided, the model is fit treating the subclusters as new samples and the initial data is mapped to the label of the closest subcluster.

• `int`: the model fit is `AgglomerativeClustering` with `n_clusters` set to be equal to the int.

`compute_labels`: bool, default True

Whether or not to compute labels for each fit.

`copy`: bool, default True

Whether or not to make a copy of the given data. If set to False, the initial data will be overwritten.

**Attributes**

<table>
<thead>
<tr>
<th>root_ (_CFNode)</th>
<th>Root of the CFTree.</th>
</tr>
</thead>
<tbody>
<tr>
<td>dummy_leaf (_CFNode)</td>
<td>Start pointer to all the leaves.</td>
</tr>
<tr>
<td>subcluster_centers_</td>
<td>(ndarray,) Centroids of all subclusters read directly from the leaves.</td>
</tr>
<tr>
<td>subcluster_labels_</td>
<td>(ndarray,) Labels assigned to the centroids of the subclusters after they are clustered globally.</td>
</tr>
<tr>
<td>labels_</td>
<td>(ndarray, shape (n_samples,)) Array of labels assigned to the input data. If partial_fit is used instead of fit, they are assigned to the last batch of data.</td>
</tr>
</tbody>
</table>

**Notes**

The tree data structure consists of nodes with each node consisting of a number of subclusters. The maximum number of subclusters in a node is determined by the branching factor. Each subcluster maintains a linear sum, squared sum and the number of samples in that subcluster. In addition, each subcluster can also have a node as its child, if the subcluster is not a member of a leaf node.

For a new point entering the root, it is merged with the subcluster closest to it and the linear sum, squared sum and the number of samples of that subcluster are updated. This is done recursively till the properties of the leaf node are updated.

**References**


• Roberto Perdisci JBirch - Java implementation of BIRCH clustering algorithm https://code.google.com/archive/p/jbirch

**Examples**

```python
>>> from sklearn.cluster import Birch
>>> X = [[0, 1], [0.3, 1], [-0.3, 1], [0, -1], [0.3, -1], [-0.3, -1]]
>>> brc = Birch(branching_factor=50, n_clusters=None, threshold=0.5, ... compute_labels=True)
```
```python
>>> brc.fit(X)
Birch(branching_factor=50, compute_labels=True, copy=True, n_clusters=None, threshold=0.5)
>>> brc.predict(X)
array([0, 0, 0, 1, 1, 1])
```

### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Build a CF Tree for the input data.</td>
</tr>
<tr>
<td><code>fit_predict(X[, y])</code></td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>partial_fit([X, y])</code></td>
<td>Online learning.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict data using the <code>centroids_</code> of subclusters.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Transform X into subcluster centroids dimension.</td>
</tr>
</tbody>
</table>

**__init__**(threshold=0.5, branching_factor=50, n_clusters=3, compute_labels=True, copy=True)  

**fit** *(X, y=None)*  
Build a CF Tree for the input data.  

**Parameters**  
X : {array-like, sparse matrix}, shape (n_samples, n_features)  
Input data.  

y : Ignored

**fit_predict** *(X, y=None)*  
Performs clustering on X and returns cluster labels.  

**Parameters**  
X : ndarray, shape (n_samples, n_features)  
Input data.  

**Returns**  
y : ndarray, shape (n_samples,)  
cluster labels

**fit_transform** *(X, y=None, **fit_params)*  
Fit to data, then transform it.  
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.  

**Parameters**  
X : numpy array of shape [n_samples, n_features]  
Training set.  

y : numpy array of shape [n_samples]  
Target values.  

**Returns**  
X_new : numpy array of shape [n_samples, n_features_new]  
Transformed array.

**get_params**(deep=True)  
Get parameters for this estimator.  

**Parameters**  
deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns params** : mapping of string to any

Parameter names mapped to their values.

**partial_fit** (X=None, y=None)

Online learning. Prevents rebuilding of CFTree from scratch.

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features), None

Input data. If X is not provided, only the global clustering step is done.

y : Ignored

**predict** (X)

Predict data using the centroids of subclusters.

Avoid computation of the row norms of X.

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features)

Input data.

**Returns** labels : ndarray, shape(n_samples)

Labelled data.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform** (X)

Transform X into subcluster centroids dimension.

Each dimension represents the distance from the sample point to each cluster centroid.

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features)

Input data.

**Returns** X_trans : {array-like, sparse matrix}, shape (n_samples, n_clusters)

Transformed data.

---

**Examples using sklearn.cluster.Birch**

- *Compare BIRCH and MiniBatchKMeans*
- *Comparing different clustering algorithms on toy datasets*

**sklearn.cluster.DBSCAN**

class** sklearn.cluster.DBSCAN (eps=0.5, min_samples=5, metric='euclidean', metric_params=None, algorithm='auto', leaf_size=30, p=None, n_jobs=1)

Perform DBSCAN clustering from vector array or distance matrix.
DBSCAN - Density-Based Spatial Clustering of Applications with Noise. Finds core samples of high density and expands clusters from them. Good for data which contains clusters of similar density.

Read more in the User Guide.

Parameters

- **eps**: float, optional
  The maximum distance between two samples for them to be considered as in the same neighborhood.

- **min_samples**: int, optional
  The number of samples (or total weight) in a neighborhood for a point to be considered as a core point. This includes the point itself.

- **metric**: string, or callable
  The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by metrics.pairwise.calculate_distance for its metric parameter. If metric is “precomputed”, X is assumed to be a distance matrix and must be square. X may be a sparse matrix, in which case only “nonzero” elements may be considered neighbors for DBSCAN.

  New in version 0.17: metric precomputed to accept precomputed sparse matrix.

- **metric_params**: dict, optional
  Additional keyword arguments for the metric function.

  New in version 0.19.

- **algorithm**: {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional
  The algorithm to be used by the NearestNeighbors module to compute pointwise distances and find nearest neighbors. See NearestNeighbors module documentation for details.

- **leaf_size**: int, optional (default = 30)
  Leaf size passed to BallTree or cKDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

- **p**: float, optional
  The power of the Minkowski metric to be used to calculate distance between points.

- **n_jobs**: int, optional (default = 1)
  The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.

Attributes

- **core_sample_indices_**: array, shape = [n_core_samples]) Indices of core samples.

- **components_**: (array, shape = [n_core_samples, n_features]) Copy of each core sample found by training.

- **labels_**: (array, shape = [n_samples]) Cluster labels for each point in the dataset given to fit(). Noisy samples are given the label -1.
Notes

For an example, see `examples/cluster/plot_dbscan.py`.

This implementation bulk-computes all neighborhood queries, which increases the memory complexity to \(O(n.d)\) where \(d\) is the average number of neighbors, while original DBSCAN had memory complexity \(O(n)\).

Sparse neighborhoods can be precomputed using `NearestNeighbors.radius_neighbors_graph` with `mode='distance'`.

References


Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y, sample_weight])</code></td>
<td>Perform DBSCAN clustering from features or distance matrix.</td>
</tr>
<tr>
<td><code>fit_predict(X[, y, sample_weight])</code></td>
<td>Performs clustering on X and returns cluster labels.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__(eps=0.5, min_samples=5, metric='euclidean', metric_params=None, algorithm='auto', leaf_size=30, p=None, n_jobs=1)
```  
Perform DBSCAN clustering from features or distance matrix.

**Parameters**

- **X**: array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)
  
  A feature array, or array of distances between samples if `metric='precomputed'`.

- **sample_weight**: array, shape (n_samples,), optional
  
  Weight of each sample, such that a sample with a weight of at least `min_samples` is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.

- **y**: Ignored

```python
fit_predict (X, y=None, sample_weight=None)
```  
Performs clustering on X and returns cluster labels.

**Parameters**

- **X**: array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)
  
  A feature array, or array of distances between samples if `metric='precomputed'`.

- **sample_weight**: array, shape (n_samples,), optional
  
  Weight of each sample, such that a sample with a weight of at least `min_samples` is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.
y : Ignored

Returns y : ndarray, shape (n_samples,)
    cluster labels

get_params (deep=True)
    Get parameters for this estimator.

Parameters deep : boolean, optional
    If True, will return the parameters for this estimator and contained subobjects that are
    estimators.

Returns params : mapping of string to any
    Parameter names mapped to their values.

set_params (**params)
    Set the parameters of this estimator.

    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
    parameters of the form <component>__<parameter> so that it’s possible to update each component
    of a nested object.

Returns self

Examples using sklearn.cluster.DBSCAN

- Demo of DBSCAN clustering algorithm
- Comparing different clustering algorithms on toy datasets

sklearn.cluster.FeatureAgglomeration

class sklearn.cluster.FeatureAgglomeration (n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func=<function mean>)

Agglomerate features.

Similar to AgglomerativeClustering, but recursively merges features instead of samples.

Read more in the User Guide.

Parameters n_clusters : int, default 2
    The number of clusters to find.

affinity : string or callable, default “euclidean”
    Metric used to compute the linkage. Can be “euclidean”, “l1”, “l2”, “manhattan”, “cosine”, or ‘precomputed’. If linkage is ‘ward’, only “euclidean” is accepted.

memory : None, str or object with the joblib.Memory interface, optional
    Used to cache the output of the computation of the tree. By default, no caching is done. If a string is given, it is the path to the caching directory.

connectivity : array-like or callable, optional
Connectivity matrix. Defines for each feature the neighboring features following a given structure of the data. This can be a connectivity matrix itself or a callable that transforms the data into a connectivity matrix, such as derived from kneighbors_graph. Default is None, i.e., the hierarchical clustering algorithm is unstructured.

**compute_full_tree**: bool or ‘auto’, optional, default “auto”

Stop early the construction of the tree at n_clusters. This is useful to decrease computation time if the number of clusters is not small compared to the number of features. This option is useful only when specifying a connectivity matrix. Note also that when varying the number of clusters and using caching, it may be advantageous to compute the full tree.

**linkage**: {“ward”, “complete”, “average”}, optional, default “ward”

Which linkage criterion to use. The linkage criterion determines which distance to use between sets of features. The algorithm will merge the pairs of cluster that minimize this criterion.

- ward minimizes the variance of the clusters being merged.
- average uses the average of the distances of each feature of the two sets.
- complete or maximum linkage uses the maximum distances between all features of the two sets.

**pooling_func**: callable, default np.mean

This combines the values of agglomerated features into a single value, and should accept an array of shape [M, N] and the keyword argument axis=1, and reduce it to an array of size [M].

**Attributes**

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>labels_</td>
<td>(array-like, (n_features,)) cluster labels for each feature.</td>
</tr>
<tr>
<td>n_leaves_</td>
<td>(int) Number of leaves in the hierarchical tree.</td>
</tr>
<tr>
<td>n_components_</td>
<td>estimated number of connected components in the graph.</td>
</tr>
<tr>
<td>children_</td>
<td>(array-like, shape (n_nodes-1, 2)) The children of each non-leaf node. Values less than n_features correspond to leaves of the tree which are the original samples. A node i greater than or equal to n_features is a non-leaf node and has children children_[i - n_features]. Alternatively at the i-th iteration, children[i][0] and children[i][1] are merged to form node n_features + i</td>
</tr>
</tbody>
</table>

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Fit the hierarchical clustering on the data</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>inverse_transform(Xred)</td>
<td>Inverse the transformation.</td>
</tr>
<tr>
<td>pooling_func(a[, axis, dtype, out, keepdims])</td>
<td>Compute the arithmetic mean along the specified axis.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Transform a new matrix using the built clustering</td>
</tr>
</tbody>
</table>
__init__ (n_clusters=2, affinity='euclidean', memory=None, connectivity=None, compute_full_tree='auto', linkage='ward', pooling_func=<function mean>)

fit (X, y=None, **params)
Fit the hierarchical clustering on the data

Parameters X : array-like, shape = [n_samples, n_features]
The data
y : Ignored

Returns self

fit_transform (X, y=None, **fit_params)
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]
Training set.
y : numpy array of shape [n_samples]
Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]
Transformed array.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform (Xred)
Inverse the transformation. Return a vector of size nb_features with the values of Xred assigned to each group of features

Parameters Xred : array-like, shape=[n_samples, n_clusters] or [n_clusters,]
The values to be assigned to each cluster of samples

Returns X : array, shape=[n_samples, n_features] or [n_features]
A vector of size n_samples with the values of Xred assigned to each of the cluster of samples.

pooling_func (a, axis=None, dtype=None, out=None, keepdims=<class 'numpy._globals._NoValue'>)
Compute the arithmetic mean along the specified axis.

Returns the average of the array elements. The average is taken over the flattened array by default, otherwise over the specified axis. float64 intermediate and return values are used for integer inputs.

Parameters a : array like
Array containing numbers whose mean is desired. If a is not an array, a conversion is attempted.
axis : None or int or tuple of ints, optional
    Axis or axes along which the means are computed. The default is to compute the mean
    of the flattened array.
    New in version 1.7.0.
    If this is a tuple of ints, a mean is performed over multiple axes, instead of a single axis
    or all the axes as before.

dtype : data-type, optional
    Type to use in computing the mean. For integer inputs, the default is float64; for floating
    point inputs, it is the same as the input dtype.

out : ndarray, optional
    Alternate output array in which to place the result. The default is None; if provided, it
    must have the same shape as the expected output, but the type will be cast if necessary.

keepdims : bool, optional
    If this is set to True, the axes which are reduced are left in the result as dimensions with
    size one. With this option, the result will broadcast correctly against the input array.
    If the default value is passed, then keepdims will not be passed through to the mean
    method of sub-classes of ndarray, however any non-default value will be. If the sub-
    classes sum method does not implement keepdims any exceptions will be raised.

Returns m : ndarray, see dtype parameter above
    If out=None, returns a new array containing the mean values, otherwise a reference to
    the output array is returned.

See also:

average  Weighted average

std, var, nanmean, nanstd, nanvar

Notes

The arithmetic mean is the sum of the elements along the axis divided by the number of elements.
Note that for floating-point input, the mean is computed using the same precision the input has. Depending
on the input data, this can cause the results to be inaccurate, especially for float32 (see example below). Specifying a higher-precision accumulator using the dtype keyword can alleviate this issue.

By default, float16 results are computed using float32 intermediates for extra precision.

Examples

```python
>>> a = np.array([[1, 2], [3, 4]])
>>> np.mean(a)
2.5
>>> np.mean(a, axis=0)
array([ 2., 3.])
>>> np.mean(a, axis=1)
array([ 1.5, 3.5])
```
In single precision, `mean` can be inaccurate:

```python
>>> a = np.zeros((2, 512*512), dtype=np.float32)
>>> a[0, :] = 1.0
>>> a[1, :] = 0.1
>>> np.mean(a)
0.54999924
```

Computing the mean in float64 is more accurate:

```python
>>> np.mean(a, dtype=np.float64)
0.55000000074505806
```

```python
set_params (**params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

```
Returns self
```

```python
transform (X)
```

Transform a new matrix using the built clustering

```python
Parameters X : array-like, shape = [n_samples, n_features] or [n_features]
A M by N array of M observations in N dimensions or a length M array of M one-dimensional observations.
```

```
Returns Y : array, shape = [n_samples, n_clusters] or [n_clusters]
The pooled values for each feature cluster.
```

**Examples using sklearn.cluster.FeatureAgglomeration**

- Feature agglomeration
- Feature agglomeration vs. univariate selection

**sklearn.cluster.KMeans**

```python
class sklearn.cluster.KMeans(n_clusters=8, init='k-means++', n_init=10, max_iter=300, tol=0.0001, precompute_distances='auto', verbose=0, random_state=None, copy_x=True, n_jobs=1, algorithm='auto')
```

K-Means clustering

Read more in the User Guide.

**Parameters n_clusters : int, optional, default: 8**

The number of clusters to form as well as the number of centroids to generate.

**init : {'k-means++', 'random' or an ndarray}**

Method for initialization, defaults to ‘k-means++’:

‘k-means++’ : selects initial cluster centers for k-mean clustering in a smart way to speed up convergence. See section Notes in k_init for more details.
‘random’: choose k observations (rows) at random from data for the initial centroids.
If an ndarray is passed, it should be of shape (n_clusters, n_features) and gives the initial centers.

**n_init**: int, default: 10
Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n_init consecutive runs in terms of inertia.

**max_iter**: int, default: 300
Maximum number of iterations of the k-means algorithm for a single run.

**tol**: float, default: 1e-4
Relative tolerance with regards to inertia to declare convergence

**precompute_distances**: {'auto', True, False}
Precompute distances (faster but takes more memory).

‘auto’ : do not precompute distances if n_samples * n_clusters > 12 million. This corresponds to about 100MB overhead per job using double precision.

True : always precompute distances
False : never precompute distances

**verbose**: int, default 0
Verbosity mode.

**random_state**: int, RandomState instance or None, optional, default: None
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**copy_x**: boolean, default True
When pre-computing distances it is more numerically accurate to center the data first. If copy_x is True, then the original data is not modified. If False, the original data is modified, and put back before the function returns, but small numerical differences may be introduced by subtracting and then adding the data mean.

**n_jobs**: int
The number of jobs to use for the computation. This works by computing each of the n_init runs in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**algorithm**: “auto”, “full” or “elkan”, default=“auto”
K-means algorithm to use. The classical EM-style algorithm is “full”. The “elkan” variation is more efficient by using the triangle inequality, but currently doesn’t support sparse data. “auto” chooses “elkan” for dense data and “full” for sparse data.
Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>cluster_centers_</code></td>
<td>(array, [n_clusters, n_features]) Coordinates of cluster centers</td>
</tr>
<tr>
<td><code>labels_</code></td>
<td>Labels of each point</td>
</tr>
<tr>
<td><code>inertia_</code></td>
<td>(float) Sum of squared distances of samples to their closest cluster center.</td>
</tr>
</tbody>
</table>

See also:

**MiniBatchKMeans** Alternative online implementation that does incremental updates of the centers positions using mini-batches. For large scale learning (say n_samples > 10k) MiniBatchKMeans is probably much faster than the default batch implementation.

Notes

The k-means problem is solved using Lloyd’s algorithm.

The average complexity is given by O(k n T), were n is the number of samples and T is the number of iteration.

The worst case complexity is given by O(n^((k+2)/p)) with n = n_samples, p = n_features. (D. Arthur and S. Vassilvitski, ‘How slow is the k-means method?’ SoCG2006)

In practice, the k-means algorithm is very fast (one of the fastest clustering algorithms available), but it falls in local minima. That’s why it can be useful to restart it several times.

Examples

```python
>>> from sklearn.cluster import KMeans
>>> import numpy as np
>>> X = np.array([[1, 2], [1, 4], [1, 0],
...               [4, 2], [4, 4], [4, 0]])
>>> kmeans = KMeans(n_clusters=2, random_state=0).fit(X)
>>> kmeans.labels_
array([0, 0, 0, 1, 1, 1], dtype=int32)
>>> kmeans.predict([[0, 0], [4, 4]])
array([0, 1], dtype=int32)
>>> kmeans.cluster_centers_
array([[ 1.,  2.],
       [ 4.,  2.]]
```
Table 30.20 – continued from previous page

<table>
<thead>
<tr>
<th>set_params(**params)</th>
<th>Set the parameters of this estimator.</th>
</tr>
</thead>
<tbody>
<tr>
<td>transform(X)</td>
<td>Transform X to a cluster-distance space.</td>
</tr>
</tbody>
</table>

```python
__init__(n_clusters=8, init='k-means++', n_init=10, max_iter=300, tol=0.0001, precom
pute_distances='auto', verbose=0, random_state=None, copy_x=True, n_jobs=1, al
gorithm='auto')
```

```python
fit(X, y=None)

Compute k-means clustering.

Parameters
X: array-like or sparse matrix, shape=(n_samples, n_features)
Training instances to cluster.

y: Ignored
```

```python
fit_predict(X, y=None)

Compute cluster centers and predict cluster index for each sample.

Parameters
X: {array-like, sparse matrix}, shape=[n_samples, n_features]
New data to transform.

u: Ignored

Returns
labels: array, shape [n_samples,]
Index of the cluster each sample belongs to.
```

```python
fit_transform(X, y=None)

Compute clustering and transform X to cluster-distance space.

Parameters
X: {array-like, sparse matrix}, shape=[n_samples, n_features]
New data to transform.

y: Ignored

Returns
X_new: array, shape [n_samples, k]
X transformed in the new space.
```

```python
get_params(deep=True)

Get parameters for this estimator.

Parameters
deep: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns
params: mapping of string to any
Parameter names mapped to their values.
```

```python
predict(X)

Predict the closest cluster each sample in X belongs to.

In the vector quantization literature, cluster_centers_ is called the code book and each value returned by
predict is the index of the closest code in the code book.

Parameters
X: {array-like, sparse matrix}, shape=[n_samples, n_features]
```
New data to predict.

**Returns** labels : array, shape [n_samples,]

Index of the cluster each sample belongs to.

**score** *(X, y=None)*

Opposite of the value of X on the K-means objective.

**Parameters** X : {array-like, sparse matrix}, shape = [n_samples, n_features]

New data.

y : Ignored

**Returns** score : float

Opposite of the value of X on the K-means objective.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Transform X to a cluster-distance space.

In the new space, each dimension is the distance to the cluster centers. Note that even if X is sparse, the array returned by `transform` will typically be dense.

**Parameters** X : {array-like, sparse matrix}, shape = [n_samples, n_features]

New data to transform.

**Returns** X_new : array, shape [n_samples, k]

X transformed in the new space.

**Examples using sklearn.cluster.KMeans**

- Demonstration of k-means assumptions
- Vector Quantization Example
- K-means Clustering
- Color Quantization using K-Means
- Empirical evaluation of the impact of k-means initialization
- A demo of K-Means clustering on the handwritten digits data
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- Clustering text documents using k-means
**sklearn.cluster.MiniBatchKMeans**

**class sklearn.cluster.MiniBatchKMeans**

```python
MiniBatchKMeans(n_clusters=8, init='k-means++', max_iter=100, 
batch_size=100, verbose=0, compute_labels=True, 
random_state=None, tol=0.0, max_no_improvement=10, 
init_size=None, n_init=3, reassignment_ratio=0.01)
```

Mini-Batch K-Means clustering

Read more in the User Guide.

**Parameters**

**n_clusters** : int, optional, default: 8

The number of clusters to form as well as the number of centroids to generate.

**init** : {'k-means++', 'random' or an ndarray}, default: ‘k-means++’

Method for initialization, defaults to ‘k-means++’:

- ‘k-means++’ : selects initial cluster centers for k-mean clustering in a smart way to speed up convergence. See section Notes in k_init for more details.
- ‘random’ : choose k observations (rows) at random from data for the initial centroids.

If an ndarray is passed, it should be of shape (n_clusters, n_features) and gives the initial centers.

**max_iter** : int, optional

Maximum number of iterations over the complete dataset before stopping independently of any early stopping criterion heuristics.

**batch_size** : int, optional, default: 100

Size of the mini batches.

**verbose** : boolean, optional

Verbosity mode.

**compute_labels** : boolean, default=True

Compute label assignment and inertia for the complete dataset once the minibatch optimization has converged in fit.

**random_state** : int, RandomState instance or None, optional, default: None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**tol** : float, default: 0.0

Control early stopping based on the relative center changes as measured by a smoothed, variance-normalized of the mean center squared position changes. This early stopping heuristics is closer to the one used for the batch variant of the algorithms but induces a slight computational and memory overhead over the inertia heuristic.

To disable convergence detection based on normalized center change, set tol to 0.0 (default).

**max_no_improvement** : int, default: 10

Control early stopping based on the consecutive number of mini batches that does not yield an improvement on the smoothed inertia.

To disable convergence detection based on inertia, set max_no_improvement to None.
**init_size**: int, optional, default: 3 * batch_size

Number of samples to randomly sample for speeding up the initialization (sometimes at the expense of accuracy): the only algorithm is initialized by running a batch KMeans on a random subset of the data. This needs to be larger than n_clusters.

**n_init**: int, default=3

Number of random initializations that are tried. In contrast to KMeans, the algorithm is only run once, using the best of the n_init initializations as measured by inertia.

**reassignment_ratio**: float, default: 0.01

Control the fraction of the maximum number of counts for a center to be reassigned. A higher value means that low count centers are more easily reassigned, which means that the model will take longer to converge, but should converge in a better clustering.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>cluster_centers</td>
<td>(array, [n_clusters, n_features]) Coordinates of cluster centers</td>
</tr>
<tr>
<td>labels_</td>
<td>Labels of each point (if compute_labels is set to True).</td>
</tr>
<tr>
<td>inertia_</td>
<td>(float) The value of the inertia criterion associated with the chosen partition (if compute_labels is set to True). The inertia is defined as the sum of square distances of samples to their nearest neighbor.</td>
</tr>
</tbody>
</table>

**See also:**

*KMeans* The classic implementation of the clustering method based on the Lloyd’s algorithm. It consumes the whole set of input data at each iteration.

**Notes**


**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Compute the centroids on X by chunking it into mini-batches.</td>
</tr>
<tr>
<td>fit_predict(X[, y])</td>
<td>Compute cluster centers and predict cluster index for each sample.</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Compute clustering and transform X to cluster-distance space.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>partial_fit(X[, y])</td>
<td>Update k means estimate on a single mini-batch X.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict the closest cluster each sample in X belongs to.</td>
</tr>
<tr>
<td>score(X[, y])</td>
<td>Opposite of the value of X on the K-means objective.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Transform X to a cluster-distance space.</td>
</tr>
</tbody>
</table>
KMeans(kmeans)=8, init='k-means++', max_iter=100, batch_size=100, verbose=0, compute_labels=True, random_state=None, tol=0.0, max_no_improvement=10, init_size=None, n_init=3, reassignment_ratio=0.01)

fit (X, y=None)
Compute the centroids on X by chunking it into mini-batches.

Parameters X : array-like or sparse matrix, shape=(n_samples, n_features)
Training instances to cluster.

y : Ignored

fit_predict (X, y=None)
Compute cluster centers and predict cluster index for each sample.
Convenience method; equivalent to calling fit(X) followed by predict(X).

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
New data to transform.

u : Ignored

Returns labels : array, shape [n_samples,]
Index of the cluster each sample belongs to.

fit_transform (X, y=None)
Compute clustering and transform X to cluster-distance space.
Equivalent to fit(X).transform(X), but more efficiently implemented.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
New data to transform.

y : Ignored

Returns X_new : array, shape [n_samples, k]
X transformed in the new space.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

partial_fit (X, y=None)
Update k means estimate on a single mini-batch X.

Parameters X : array-like, shape = [n_samples, n_features]
Coordinates of the data points to cluster.

y : Ignored

predict (X)
Predict the closest cluster each sample in X belongs to.

In the vector quantization literature, cluster_centers_ is called the code book and each value returned by predict is the index of the closest code in the code book.
Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
    New data to predict.
Returns labels : array, shape [n_samples,]
    Index of the cluster each sample belongs to.
score (X, y=None)
    Opposite of the value of X on the K-means objective.
    Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
        New data.
    y : Ignored
    Returns score : float
        Opposite of the value of X on the K-means objective.
set_params (**params)
    Set the parameters of this estimator.
    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
    parameters of the form <component>__<parameter> so that it’s possible to update each component
    of a nested object.
    Returns self
transform (X)
    Transform X to a cluster-distance space.
    In the new space, each dimension is the distance to the cluster centers. Note that even if X is sparse, the
    array returned by transform will typically be dense.
    Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
        New data to transform.
    Returns X_new : array, shape [n_samples, k]
        X transformed in the new space.

Examples using sklearn.cluster.MiniBatchKMeans

- Biclustering documents with the Spectral Co-clustering algorithm
- Online learning of a dictionary of parts of faces
- Compare BIRCH and MiniBatchKMeans
- Empirical evaluation of the impact of k-means initialization
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- Comparing different clustering algorithms on toy datasets
- Faces dataset decompositions
- Clustering text documents using k-means
Mean shift clustering using a flat kernel.

Mean shift clustering aims to discover “blobs” in a smooth density of samples. It is a centroid-based algorithm, which works by updating candidates for centroids to be the mean of the points within a given region. These candidates are then filtered in a post-processing stage to eliminate near-duplicates to form the final set of centroids.

Seeding is performed using a binning technique for scalability.

Read more in the User Guide.

Parameters

- `bandwidth`: float, optional
  Bandwidth used in the RBF kernel.
  If not given, the bandwidth is estimated using sklearn.cluster.estimate_bandwidth; see the documentation for that function for hints on scalability (see also the Notes, below).

- `seeds`: array, shape=[n_samples, n_features], optional
  Seeds used to initialize kernels. If not set, the seeds are calculated by clustering.get_bin_seeds with bandwidth as the grid size and default values for other parameters.

- `bin_seeding`: boolean, optional
  If true, initial kernel locations are not locations of all points, but rather the location of the discretized version of points, where points are binned onto a grid whose coarseness corresponds to the bandwidth. Setting this option to True will speed up the algorithm because fewer seeds will be initialized. default value: False Ignored if seeds argument is not None.

- `min_bin_freq`: int, optional
  To speed up the algorithm, accept only those bins with at least min_bin_freq points as seeds. If not defined, set to 1.

- `cluster_all`: boolean, default True
  If true, then all points are clustered, even those orphans that are not within any kernel. Orphans are assigned to the nearest kernel. If false, then orphans are given cluster label -1.

- `n_jobs`: int
  The number of jobs to use for the computation. This works by computing each of the n_init runs in parallel.
  If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

Attributes

- `cluster_centers_` (array, [n_clusters, n_features]) Coordinates of cluster centers.
- `labels_` : Labels of each point.
Notes

Scalability:

Because this implementation uses a flat kernel and a Ball Tree to look up members of each kernel, the complexity will tend towards $O(T*n*log(n))$ in lower dimensions, with $n$ the number of samples and $T$ the number of points. In higher dimensions the complexity will tend towards $O(T*n^2)$.

Scalability can be boosted by using fewer seeds, for example by using a higher value of min_bin_freq in the get_bin_seeds function.

Note that the estimate_bandwidth function is much less scalable than the mean shift algorithm and will be the bottleneck if it is used.

References


Methods

**fit**(X[, y])  Perform clustering.

**fit_predict**(X[, y])  Performs clustering on X and returns cluster labels.

**get_params**(deep)  Get parameters for this estimator.

**predict**(X)  Predict the closest cluster each sample in X belongs to.

**set_params**(**params)  Set the parameters of this estimator.

__init__ (bandwidth=None, seeds=None, bin_seeding=False, min_bin_freq=1, cluster_all=True, n_jobs=1)

**fit**(X, y=None)  Perform clustering.

Parameters  

**X** : array-like, shape=[n_samples, n_features]  
Samples to cluster.

**y** : Ignored

**fit_predict**(X, y=None)  
Performs clustering on X and returns cluster labels.

Parameters  

**X** : ndarray, shape (n_samples, n_features)  
Input data.

Returns  

**y** : ndarray, shape (n_samples,)  
cluster labels

**get_params**(deep=True)  
Get parameters for this estimator.

Parameters  

**deep** : boolean, optional  
If True, will return the parameters for this estimator and contained subobjects that are estimators.
**Returns** params : mapping of string to any
Parameter names mapped to their values.

**predict** *(X)*
Predict the closest cluster each sample in X belongs to.

**Parameters** X : {array-like, sparse matrix}, shape=[n_samples, n_features]
New data to predict.

**Returns** labels : array, shape [n_samples,]
Index of the cluster each sample belongs to.

**set_params**(**params**)  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns** self

**Examples using sklearn.cluster.MeanShift**

- A demo of the mean-shift clustering algorithm
- Comparing different clustering algorithms on toy datasets

**sklearn.cluster.SpectralClustering**

**class sklearn.cluster.SpectralClustering**(n_clusters=8,  
eigen_solver=None,  
random_state=None,  
n_init=10,  
gamma=1.0,  
affinity='rbf',  
n_neighbors=10,  
eigen_tol=0.0,  
assign_labels='kmeans',  
degree=3,  
coef0=1,  
kernel_params=None,  
n_jobs=1)

Apply clustering to a projection to the normalized laplacian.

In practice Spectral Clustering is very useful when the structure of the individual clusters is highly non-convex or more generally when a measure of the center and spread of the cluster is not a suitable description of the complete cluster. For instance when clusters are nested circles on the 2D plan.

If affinity is the adjacency matrix of a graph, this method can be used to find normalized graph cuts.

When calling **fit**, an affinity matrix is constructed using either kernel function such the Gaussian (aka RBF) kernel of the euclidean distanced d(X, X):

```python
np.exp(-gamma * d(X,X) ** 2)
```

or a k-nearest neighbors connectivity matrix.

Alternatively, using **precomputed**, a user-provided affinity matrix can be used.

Read more in the User Guide.

**Parameters** n_clusters : integer, optional
The dimension of the projection subspace.

eigen_solver : {None, ‘arpack’, ‘lobpcg’, or ‘amg’}
Eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.

**random_state** : int, RandomState instance or None, optional, default: None
A pseudo random number generator used for the initialization of the lobpcg eigenvectors decomposition when eigen_solver == `amg` and by the K-Means initialization. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**n_init** : int, optional, default: 10
Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n_init consecutive runs in terms of inertia.

**gamma** : float, default=1.0
Kernel coefficient for rbf, poly, sigmoid, laplacian and chi2 kernels. Ignored for affinity='nearest_neighbors'.

**affinity** : string, array-like or callable, default: ‘rbf’
If a string, this may be one of ‘nearest_neighbors’, ‘precomputed’, ‘rbf’ or one of the kernels supported by sklearn.metrics.pairwise_kernels.

Only kernels that produce similarity scores (non-negative values that increase with similarity) should be used. This property is not checked by the clustering algorithm.

**n_neighbors** : integer
Number of neighbors to use when constructing the affinity matrix using the nearest neighbors method. Ignored for affinity='rbf'.

**eigen_tol** : float, optional, default: 0.0
Stopping criterion for eigendecomposition of the Laplacian matrix when using arpack eigen_solver.

**assign_labels** : {‘kmeans’, ‘discretize’}, default: ‘kmeans’
The strategy to use to assign labels in the embedding space. There are two ways to assign labels after the laplacian embedding. k-means can be applied and is a popular choice. But it can also be sensitive to initialization. Discretization is another approach which is less sensitive to random initialization.

**degree** : float, default=3
Degree of the polynomial kernel. Ignored by other kernels.

**coef0** : float, default=1
Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

**kernel_params** : dictionary of string to any, optional
Parameters (keyword arguments) and values for kernel passed as callable object. Ignored by other kernels.

**n_jobs** : int, optional (default = 1)
The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.
Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>affinity_matrix_</td>
<td>(array-like, shape (n_samples, n_samples)) Affinity matrix used for clustering. Available only if after calling fit.</td>
</tr>
<tr>
<td>labels_</td>
<td>Labels of each point</td>
</tr>
</tbody>
</table>

Notes

If you have an affinity matrix, such as a distance matrix, for which 0 means identical elements, and high values means very dissimilar elements, it can be transformed in a similarity matrix that is well suited for the algorithm by applying the Gaussian (RBF, heat) kernel:

```
np.exp(- dist_matrix ** 2 / (2. * delta ** 2))
```

Where `delta` is a free parameter representing the width of the Gaussian kernel.

Another alternative is to take a symmetric version of the `k` nearest neighbors connectivity matrix of the points.

If the pyamg package is installed, it is used: this greatly speeds up computation.

References


Methods

```
fit(X[, y])
```

Creates an affinity matrix for `X` using the selected affinity, then applies spectral clustering to this affinity matrix.

```
fit_predict(X[, y])
```

Perform clustering on `X` and returns cluster labels.

```
get_params([deep])
```

Get parameters for this estimator.

```
set_params(**params)
```

Set the parameters of this estimator.

```
__init__(n_clusters=8, eigen_solver=None, random_state=None, n_init=10, gamma=1.0, affinity='rbf', n_neighbors=10, eigen_tol=0.0, assign_labels='kmeans', degree=3, coef0=1, kernel_params=None, n_jobs=1)
```

```
fit(X, y=None)
```

Creates an affinity matrix for `X` using the selected affinity, then applies spectral clustering to this affinity matrix.

Parameters

`X` : array-like or sparse matrix, shape (n_samples, n_features)

OR, if `affinity='precomputed'`, a precomputed affinity matrix of shape (n_samples, n_samples)
y : Ignored

**fit_predict** *(X, y=None)*

Performs clustering on X and returns cluster labels.

**Parameters**

- **X** : ndarray, shape (n_samples, n_features)
  
  Input data.

- **y** : ndarray, shape (n_samples,)
  
  cluster labels

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  
  Parameter names mapped to their values.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**Examples using sklearn.cluster.SpectralClustering**

- *Comparing different clustering algorithms on toy datasets*

### 30.3.2 Functions

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**sklearn.cluster.affinity_propagation**

`sklearn.cluster.affinity_propagation(S, preference=None, convergence_iter=15, max_iter=200, damping=0.5, copy=True, verbose=False, return_n_iter=False)`

Perform Affinity Propagation Clustering of data
Parameters

- **S**: array-like, shape (n_samples, n_samples)
  Matrix of similarities between points

- **preference**: array-like, shape (n_samples,) or float, optional
  Preferences for each point - points with larger values of preferences are more likely to be chosen as exemplars. The number of exemplars, i.e. of clusters, is influenced by the input preferences value. If the preferences are not passed as arguments, they will be set to the median of the input similarities (resulting in a moderate number of clusters). For a smaller amount of clusters, this can be set to the minimum value of the similarities.

- **convergence_iter**: int, optional, default: 15
  Number of iterations with no change in the number of estimated clusters that stops the convergence.

- **max_iter**: int, optional, default: 200
  Maximum number of iterations

- **damping**: float, optional, default: 0.5
  Damping factor between 0.5 and 1.

- **copy**: boolean, optional, default: True
  If copy is False, the affinity matrix is modified inplace by the algorithm, for memory efficiency

- **verbose**: boolean, optional, default: False
  The verbosity level

- **return_n_iter**: bool, default False
  Whether or not to return the number of iterations.

Returns

- **cluster_centers_indices**: array, shape (n_clusters,)
  index of clusters centers

- **labels**: array, shape (n_samples,)
  cluster labels for each point

- **n_iter**: int
  number of iterations run. Returned only if return_n_iter is set to True.

Notes

For an example, see examples/cluster/plot_affinity_propagation.py.

When the algorithm does not converge, it returns an empty array as cluster_center_indices and -1 as label for each training sample.

When all training samples have equal similarities and equal preferences, the assignment of cluster centers and labels depends on the preference. If the preference is smaller than the similarities, a single cluster center and label 0 for every sample will be returned. Otherwise, every training sample becomes its own cluster center and is assigned a unique label.
References


Examples using `sklearn.cluster.affinity_propagation`

- Visualizing the stock market structure

`skslearn.cluster.dbscan`

`skslearn.cluster.dbscan` *(X, eps=0.5, min_samples=5, metric='minkowski', metric_params=None, algorithm='auto', leaf_size=30, p=2, sample_weight=None, n_jobs=1)*

Perform DBSCAN clustering from vector array or distance matrix.

Read more in the User Guide.

**Parameters**

* X : array or sparse (CSR) matrix of shape (n_samples, n_features), or array of shape (n_samples, n_samples)

A feature array, or array of distances between samples if metric='precomputed'.

* eps : float, optional

The maximum distance between two samples for them to be considered as in the same neighborhood.

* min_samples : int, optional

The number of samples (or total weight) in a neighborhood for a point to be considered as a core point. This includes the point itself.

* metric : string, or callable

The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by metrics.pairwise.pairwise_distances for its metric parameter. If metric is “precomputed”, X is assumed to be a distance matrix and must be square. X may be a sparse matrix, in which case only “nonzero” elements may be considered neighbors for DBSCAN.

* metric_params : dict, optional

Additional keyword arguments for the metric function.

New in version 0.19.

* algorithm : {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional

The algorithm to be used by the NearestNeighbors module to compute pointwise distances and find nearest neighbors. See NearestNeighbors module documentation for details.

* leaf_size : int, optional (default = 30)

Leaf size passed to BallTree or cKDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

* p : float, optional

The power of the Minkowski metric to be used to calculate distance between points.

* sample_weight : array, shape (n_samples,), optional
Weight of each sample, such that a sample with a weight of at least min_samples is by itself a core sample; a sample with negative weight may inhibit its eps-neighbor from being core. Note that weights are absolute, and default to 1.

**n_jobs** : int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores.

**Returns**

**core_samples** : array [n_core_samples]

Indices of core samples.

**labels** : array [n_samples]

Cluster labels for each point. Noisy samples are given the label -1.

**Notes**

For an example, see examples/cluster/plot_dbscan.py.

This implementation bulk-computes all neighborhood queries, which increases the memory complexity to O(n.d) where d is the average number of neighbors, while original DBSCAN had memory complexity O(n).

Sparse neighborhoods can be precomputed using NearestNeighbors.radius_neighbors_graph with mode='distance'.

**References**


**sklearn.cluster.estimate_bandwidth**

sklearn.cluster.estimate_bandwidth(X, quantile=0.3, n_samples=None, random_state=0, n_jobs=1)

Estimate the bandwidth to use with the mean-shift algorithm.

That this function takes time at least quadratic in n_samples. For large datasets, it’s wise to set that parameter to a small value.

**Parameters**

**X** : array-like, shape=[n_samples, n_features]

Input points.

**quantile** : float, default 0.3

should be between [0, 1] 0.5 means that the median of all pairwise distances is used.

**n_samples** : int, optional

The number of samples to use. If not given, all samples are used.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
n_jobs : int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If -1, then the number of jobs
is set to the number of CPU cores.

Returns bandwidth : float

The bandwidth parameter.

Examples using sklearn.cluster.estimate_bandwidth

- A demo of the mean-shift clustering algorithm
- Comparing different clustering algorithms on toy datasets

sklearn.cluster.k_means

sklearn.cluster.k_means(X, n_clusters, init='k-means++', precompute_distances='auto',
n_init=10, max_iter=300, verbose=False, tol=0.0001, random_state=None, copy_x=True, n_jobs=1, algorithm='auto', return_n_iter=False)

K-means clustering algorithm.

Read more in the User Guide.

Parameters X : array-like or sparse matrix, shape (n_samples, n_features)

The observations to cluster.

n_clusters : int

The number of clusters to form as well as the number of centroids to generate.

init : {'k-means++', 'random', or ndarray, or a callable}, optional

Method for initialization, default to 'k-means++':

'k-means++' : selects initial cluster centers for k-mean clustering in a smart way to
speed up convergence. See section Notes in k_init for more details.

'random': generate k centroids from a Gaussian with mean and variance estimated from
the data.

If an ndarray is passed, it should be of shape (n_clusters, n_features) and gives the initial
centers.

If a callable is passed, it should take arguments X, k and a random state and return
an initialization.

precompute_distances : {'auto', True, False}

Precompute distances (faster but takes more memory).

'auto': do not precompute distances if n_samples * n_clusters > 12 million. This
corresponds to about 100MB overhead per job using double precision.

True : always precompute distances

False : never precompute distances

n_init : int, optional, default: 10
Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n_init consecutive runs in terms of inertia.

max_iter : int, optional, default 300
Maximum number of iterations of the k-means algorithm to run.

verbose : boolean, optional
Verbosity mode.

tol : float, optional
The relative increment in the results before declaring convergence.

random_state : int, RandomState instance or None, optional, default: None
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

copy_x : boolean, optional
When pre-computing distances it is more numerically accurate to center the data first. If copy_x is True, then the original data is not modified. If False, the original data is modified, and put back before the function returns, but small numerical differences may be introduced by subtracting and then adding the data mean.

n_jobs : int
The number of jobs to use for the computation. This works by computing each of the n_init runs in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

algorithm : “auto”, “full” or “elkan”, default=”auto”
K-means algorithm to use. The classical EM-style algorithm is “full”. The “elkan” variation is more efficient by using the triangle inequality, but currently doesn’t support sparse data. “auto” chooses “elkan” for dense data and “full” for sparse data.

return_n_iter : bool, optional
Whether or not to return the number of iterations.

Returns
centroid : float ndarray with shape (k, n_features)
Centroids found at the last iteration of k-means.

label : integer ndarray with shape (n_samples,)
label[i] is the code or index of the centroid the i’th observation is closest to.

inertia : float
The final value of the inertia criterion (sum of squared distances to the closest centroid for all observations in the training set).

best_n_iter : int
Number of iterations corresponding to the best results. Returned only if return_n_iter is set to True.
scikit-learn user guide, Release 0.20.dev0

sklearn.cluster.mean_shift

sklearn.cluster.mean_shift(X, bandwidth=None, seeds=None, bin_seeding=False, min_bin_freq=1, cluster_all=True, max_iter=300, n_jobs=1)

Perform mean shift clustering of data using a flat kernel.

Read more in the User Guide.

Parameters

**X** : array-like, shape=[n_samples, n_features]

Input data.

**bandwidth** : float, optional

Kernel bandwidth.

If bandwidth is not given, it is determined using a heuristic based on the median of all pairwise distances. This will take quadratic time in the number of samples. The sklearn.cluster.estimate_bandwidth function can be used to do this more efficiently.

**seeds** : array-like, shape=[n_seeds, n_features] or None

Point used as initial kernel locations. If None and bin_seeding=False, each data point is used as a seed. If None and bin_seeding=True, see bin_seeding.

**bin_seeding** : boolean, default=False

If true, initial kernel locations are not locations of all points, but rather the location of the discretized version of points, where points are binned onto a grid whose coarseness corresponds to the bandwidth. Setting this option to True will speed up the algorithm because fewer seeds will be initialized. Ignored if seeds argument is not None.

**min_bin_freq** : int, default=1

To speed up the algorithm, accept only those bins with at least min_bin_freq points as seeds.

**cluster_all** : boolean, default True

If true, then all points are clustered, even those orphans that are not within any kernel. Orphans are assigned to the nearest kernel. If false, then orphans are given cluster label -1.

**max_iter** : int, default 300

Maximum number of iterations, per seed point before the clustering operation terminates (for that seed point), if has not converged yet.

**n_jobs** : int

The number of jobs to use for the computation. This works by computing each of the n_init runs in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_CPUs + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

New in version 0.17: Parallel Execution using **n_jobs**.

Returns

**cluster_centers** : array, shape=[n_clusters, n_features]

Coordinates of cluster centers.

**labels** : array, shape=[n_samples]

Cluster labels for each point.
Notes

For an example, see examples/cluster/plot_mean_shift.py.

sklearn.cluster.spectral_clustering

Parameters

affinity : array-like or sparse matrix, shape: (n_samples, n_samples)
The affinity matrix describing the relationship of the samples to embed. Must be symmetric.

Possible examples:

- adjacency matrix of a graph,
- heat kernel of the pairwise distance matrix of the samples,
- symmetric k-nearest neighbours connectivity matrix of the samples.

n_clusters : integer, optional
Number of clusters to extract.

n_components : integer, optional, default is n_clusters
Number of eigen vectors to use for the spectral embedding

eigen_solver : {None, ‘arpack’, ‘lobpcg’, or ‘amg’}
The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities

random_state : int, RandomState instance or None, optional, default: None
A pseudo random number generator used for the initialization of the lobpcg eigen vectors decomposition when eigen_solver == ‘amg’ and by the K-Means initialization. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

n_init : int, optional, default: 10
Number of time the k-means algorithm will be run with different centroid seeds. The final results will be the best output of n_init consecutive runs in terms of inertia.

eigen_tol : float, optional, default: 0.0
Stopping criterion for eigendecomposition of the Laplacian matrix when using arpack eigen_solver.

assign_labels : {‘kmeans’, ‘discretize’}, default: ‘kmeans’
The strategy to use to assign labels in the embedding space. There are two ways to assign labels after the laplacian embedding. k-means can be applied and is a popular choice. But it can also be sensitive to initialization. Discretization is another approach which is less sensitive to random initialization. See the ‘Multiclass spectral clustering’ paper referenced below for more details on the discretization approach.

Returns labels : array of integers, shape: n_samples

The labels of the clusters.

Notes

The graph should contain only one connect component, elsewhere the results make little sense.

This algorithm solves the normalized cut for k=2: it is a normalized spectral clustering.

References


Examples using sklearn.cluster.spectral_clustering

- Segmenting the picture of a raccoon face in regions
- Spectral clustering for image segmentation

sklearn.cluster.ward_tree

sklearn.cluster.ward_tree(X, connectivity=None, n_clusters=None, return_distance=False)

Ward clustering based on a Feature matrix.

Recursively merges the pair of clusters that minimally increases within-cluster variance.

The inertia matrix uses a Heapq-based representation.

This is the structured version, that takes into account some topological structure between samples.

Read more in the User Guide.

Parameters X : array, shape (n_samples, n_features)

feature matrix representing n_samples samples to be clustered

connectivity : sparse matrix (optional).

connectivity matrix. Defines for each sample the neighboring samples following a given structure of the data. The matrix is assumed to be symmetric and only the upper triangular half is used. Default is None, i.e, the Ward algorithm is unstructured.

n_clusters : int (optional)
Stop early the construction of the tree at n_clusters. This is useful to decrease compu-
tation time if the number of clusters is not small compared to the number of samples.
In this case, the complete tree is not computed, thus the ‘children’ output is of limited use, and the ‘parents’ output should rather be used. This option is valid only when specifying a connectivity matrix.

**return_distance** : bool (optional)

If True, return the distance between the clusters.

**Returns**

**children** : 2D array, shape (n_nodes-1, 2)

The children of each non-leaf node. Values less than n_samples correspond to leaves of the tree which are the original samples. A node i greater than or equal to n_samples is a non-leaf node and has children children[i - n_samples]. Alternatively at the i-th iteration, children[i][0] and children[i][1] are merged to form node n_samples + i

**n_components** : int

The number of connected components in the graph.

**n_leaves** : int

The number of leaves in the tree

**parents** : 1D array, shape (n_nodes, ) or None

The parent of each node. Only returned when a connectivity matrix is specified, else-
where ‘None’ is returned.

**distances** : 1D array, shape (n_nodes-1,)

Only returned if return_distance is set to True (for compatibility). The distances be-
tween the centers of the nodes. distances[i] corresponds to a weighted euclidean distance between the nodes children[i, 1] and children[i, 2]. If the nodes refer to leaves of the tree, then distances[i] is their unweighted euclidean distance. Distances are updated in the following way (from scipy.hierarchy.linkage):

The new entry \(d(u, v)\) is computed as follows,

\[
d(u, v) = \sqrt{\frac{|v| + |s|}{T}d(v, s)^2 + \frac{|v| + |t|}{T}d(v, t)^2 - \frac{|v|}{T}d(s, t)^2}
\]

where \(u\) is the newly joined cluster consisting of clusters \(s\) and \(t\), \(v\) is an unused cluster in the forest, \(T = |v| + |s| + |t|\), and \(|*|\) is the cardinality of its argument. This is also known as the incremental algorithm.

### 30.4 sklearn.cluster.bicluster: Biclustering

Spectral biclustering algorithms.

Authors : Kemal Eren License: BSD 3 clause

User guide: See the Biclustering section for further details.

### 30.4.1 Classes
Spectral biclustering (Kluger, 2003).

Partitions rows and columns under the assumption that the data has an underlying checkerboard structure. For instance, if there are two row partitions and three column partitions, each row will belong to three biclusters, and each column will belong to two biclusters. The outer product of the corresponding row and column label vectors gives this checkerboard structure.

Read more in the User Guide.

**Parameters**

- **n_clusters**: integer or tuple (n_row_clusters, n_column_clusters)
  - The number of row and column clusters in the checkerboard structure.

- **method**: string, optional, default: ‘bistochastic’
  - Method of normalizing and converting singular vectors into biclusters. May be one of ‘scale’, ‘bistochastic’, or ‘log’. The authors recommend using ‘log’. If the data is sparse, however, log normalization will not work, which is why the default is ‘bistochastic’. CAUTION: if method=’log’, the data must not be sparse.

- **n_components**: integer, optional, default: 6
  - Number of singular vectors to check.

- **n_best**: integer, optional, default: 3
  - Number of best singular vectors to which to project the data for clustering.

- **svd_method**: string, optional, default: ‘randomized’
  - Selects the algorithm for finding singular vectors. May be ‘randomized’ or ‘arpack’. If ‘randomized’, uses sklearn.utils.extmath.randomized_svd, which may be faster for large matrices. If ‘arpack’, uses scipy.sparse.linalg.svds, which is more accurate, but possibly slower in some cases.

- **n_svd_vecs**: int, optional, default: None
  - Number of vectors to use in calculating the SVD. Corresponds to ncv when svd_method=’arpack’ and n_oversamples when svd_method is ‘randomized’.

- **mini_batch**: bool, optional, default: False
  - Whether to use mini-batch k-means, which is faster but may get different results.

- **init**: (‘k-means++’, ‘random’ or an ndarray)
  - Method for initialization of k-means algorithm; defaults to ‘k-means++’.

- **n_init**: int, optional, default: 10
Number of random initializations that are tried with the k-means algorithm.

If mini-batch k-means is used, the best initialization is chosen and the algorithm runs once. Otherwise, the algorithm is run for each initialization and the best solution chosen.

**n_jobs** : int, optional, default: 1

The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n_jobs even slices and computing them in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**random_state** : int, RandomState instance or None, optional, default: None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

<table>
<thead>
<tr>
<th>rows_</th>
<th>(array-like, shape (n_row_clusters, n_rows)) Results of the clustering. rows[i, r] is True if cluster i contains row r. Available only after calling fit.</th>
</tr>
</thead>
<tbody>
<tr>
<td>columns_</td>
<td>(array-like, shape (n_column_clusters, n_columns)) Results of the clustering, like rows.</td>
</tr>
<tr>
<td>row_labels_</td>
<td>(array-like, shape (n_rows,)) Row partition labels.</td>
</tr>
<tr>
<td>column_labels_</td>
<td>(array-like, shape (n_cols,)) Column partition labels.</td>
</tr>
</tbody>
</table>

**References**

- Kluger, Yuval, et. al., 2003. *Spectral biclustering of microarray data: coclustering genes and conditions.*

**Methods**

- **fit**(X[, y])
  - Creates a biclustering for X.

- **get_indices**(i)
  - Row and column indices of the i’th bicluster.

- **get_params**(deep)
  - Get parameters for this estimator.

- **get_shape**(i)
  - Shape of the i’th bicluster.

- **get_submatrix**(i, data)
  - Returns the submatrix corresponding to bicluster i.

- **set_params**(**params)
  - Set the parameters of this estimator.

- **__init__**(n_clusters=3, method='bistochastic', n_components=6, n_best=3, svd_method='randomized', n_svd_vecs=None, mini_batch=False, init='k-means++', n_init=10, n_jobs=1, random_state=None)

- **biclusters**
  - Convenient way to get row and column indicators together.
  - Returns the rows_ and columns_ members.

- **fit**(X, y=None)
  - Creates a biclustering for X.
Parameters X : array-like, shape (n_samples, n_features)

y : Ignored

get_indices (i)
Row and column indices of the i’th bicluster.
Only works if rows_ and columns_ attributes exist.

Parameters i : int
The index of the cluster.

Returns row_ind : np.array, dtype=np.intp
Indices of rows in the dataset that belong to the bicluster.

col_ind : np.array, dtype=np.intp
Indices of columns in the dataset that belong to the bicluster.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_shape (i)
Shape of the i’th bicluster.

Parameters i : int
The index of the cluster.

Returns shape : (int, int)
Number of rows and columns (resp.) in the bicluster.

get_submatrix (i, data)
Returns the submatrix corresponding to bicluster i.

Parameters i : int
The index of the cluster.

data : array
The data.

Returns submatrix : array
The submatrix corresponding to bicluster i.

Notes
Works with sparse matrices. Only works if rows_ and columns_ attributes exist.

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns
self

**sklearn.cluster.bicluster.SpectralCoclustering**

class sklearn.cluster.bicluster.SpectralCoclustering(n_clusters=3, svd_method='randomized', n_svd_vecs=None, mini_batch=False, init='k-means++', n_init=10, n_jobs=1, random_state=None)

Spectral Co-Clustering algorithm (Dhillon, 2001).

Clusters rows and columns of an array $X$ to solve the relaxed normalized cut of the bipartite graph created from $X$ as follows: the edge between row vertex $i$ and column vertex $j$ has weight $X[i, j]$.

The resulting bicluster structure is block-diagonal, since each row and each column belongs to exactly one bicluster.

Supports sparse matrices, as long as they are nonnegative.

Read more in the User Guide.

**Parameters**

- **n_clusters** : integer, optional, default: 3
  
  The number of biclusters to find.

- **svd_method** : string, optional, default: ‘randomized’
  
  Selects the algorithm for finding singular vectors. May be ‘randomized’ or ‘arpack’. If ‘randomized’, use `sklearn.utils.extmath.randomized_svd`, which may be faster for large matrices. If ‘arpack’, use `scipy.sparse.linalg.svds`, which is more accurate, but possibly slower in some cases.

- **n_svd_vecs** : int, optional, default: None
  
  Number of vectors to use in calculating the SVD. Corresponds to $ncv$ when `svd_method=arpack` and $n_oversamples$ when `svd_method` is ‘randomized’.

- **mini_batch** : bool, optional, default: False
  
  Whether to use mini-batch k-means, which is faster but may get different results.

- **init** : {'k-means++', 'random' or an ndarray}
  
  Method for initialization of k-means algorithm; defaults to ‘k-means++’.

- **n_init** : int, optional, default: 10
  
  Number of random initializations that are tried with the k-means algorithm.

  If mini-batch k-means is used, the best initialization is chosen and the algorithm runs once. Otherwise, the algorithm is run for each initialization and the best solution chosen.

- **n_jobs** : int, optional, default: 1
  
  The number of jobs to use for the computation. This works by breaking down the pairwise matrix into $n_{jobs}$ even slices and computing them in parallel.
If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**random_state**: int, RandomState instance or None, optional, default: None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>rows_</td>
<td>(array-like, shape (n_row_clusters, n_rows)) Results of the clustering. rows[i, r] is True if cluster i contains row r. Available only after calling fit.</td>
</tr>
<tr>
<td>columns_</td>
<td>(array-like, shape (n_column_clusters, n_columns)) Results of the clustering, like rows.</td>
</tr>
<tr>
<td>row_labels_</td>
<td>(array-like, shape (n_rows,)) The bicluster label of each row.</td>
</tr>
<tr>
<td>col_labels_</td>
<td>(array-like, shape (n_cols,)) The bicluster label of each column.</td>
</tr>
</tbody>
</table>

**References**


**Methods**

- `fit(X[, y])`: Creates a biclustering for X.
- `get_indices(i)`: Row and column indices of the i'th bicluster. Only works if rows_ and columns_ attributes exist.
- `get_params([deep])`: Get parameters for this estimator.
- `get_shape(i)`: Shape of the i'th bicluster.
- `get_submatrix(i, data)`: Returns the submatrix corresponding to bicluster i.
- `set_params(**params)`: Set the parameters of this estimator.

```python
__init__(n_clusters=3, svd_method='randomized', n_svd_vecs=None, mini_batch=False, init='k-means++', n_init=10, n_jobs=1, random_state=None)
```

**biclusters**

Convenient way to get row and column indicators together.

Returns the rows_ and columns_ members.

- `fit(X, y=None)`: Creates a biclustering for X.
- `get_indices(i)`: Row and column indices of the i'th bicluster.
- `get_submatrix(i, data)`: Returns the submatrix corresponding to bicluster i.
- `set_params(**params)`: Set the parameters of this estimator.
The index of the cluster.

**Returns** row_ind : np.array, dtype=np.intp

Indices of rows in the dataset that belong to the bicluster.

col_ind : np.array, dtype=np.intp

Indices of columns in the dataset that belong to the bicluster.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are
estimators.

**Returns**

params : mapping of string to any

Parameter names mapped to their values.

**get_shape** *(i)*

Shape of the i’th bicluster.

**Parameters**

i : int

The index of the cluster.

**Returns**

shape : (int, int)

Number of rows and columns (resp.) in the bicluster.

**get_submatrix** *(i, data)*

Returns the submatrix corresponding to bicluster i.

**Parameters**

i : int

The index of the cluster.

data : array

The data.

**Returns**

submatrix : array

The submatrix corresponding to bicluster i.

**Notes**

Works with sparse matrices. Only works if rows_ and columns_ attributes exist.

**set_params** *(**params)*

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form `<component>__<parameter>` so that it’s possible to update each component
of a nested object.

**Returns**

self
## 30.5 sklearn.covariance: Covariance Estimators

The `sklearn.covariance` module includes methods and algorithms to robustly estimate the covariance of features given a set of points. The precision matrix defined as the inverse of the covariance is also estimated. Covariance estimation is closely related to the theory of Gaussian Graphical Models.

**User guide:** See the [Covariance estimation](#) section for further details.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>covariance.EmpiricalCovariance(...)</code></td>
<td>Maximum likelihood covariance estimator</td>
</tr>
<tr>
<td><code>covariance.EllipticEnvelope(...)</code></td>
<td>An object for detecting outliers in a Gaussian distributed dataset.</td>
</tr>
<tr>
<td><code>covariance.GraphLasso([alpha, mode, tol, ...])</code></td>
<td>Sparse inverse covariance estimation with an 1l-penalized estimator.</td>
</tr>
<tr>
<td><code>covariance.GraphLassoCV([alphas, ...])</code></td>
<td>Sparse inverse covariance w/ cross-validated choice of the 1l penalty</td>
</tr>
<tr>
<td><code>covariance.LedoitWolf([store_precision, ...])</code></td>
<td>LedoitWolf Estimator</td>
</tr>
<tr>
<td><code>covariance.OAS([store_precision, ...])</code></td>
<td>Oracle Approximating Shrinkage Estimator</td>
</tr>
<tr>
<td><code>covariance.ShrunkCovariance(...)</code></td>
<td>Covariance estimator with shrinkage</td>
</tr>
</tbody>
</table>

### 30.5.1 sklearn.covariance.EmpiricalCovariance

**class** `sklearn.covariance.EmpiricalCovariance(store_precision=True, assume_centered=False)`

Maximum likelihood covariance estimator

Read more in the [User Guide](#).

**Parameters**

- **store_precision** : bool
  
  Specifies if the estimated precision is stored.

- **assume_centered** : bool
  
  If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data are centered before computation.

**Attributes**

- **covariance_** (2D ndarray, shape (n_features, n_features)) Estimated covariance matrix
- **precision_** (2D ndarray, shape (n_features, n_features)) Estimated pseudo-inverse matrix. (stored only if store_precision is True)

**Methods**

- **error_norm(comp_cov[, norm, scaling, squared])** Computes the Mean Squared Error between two covariance estimators.
### Table 30.29 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Fits the Maximum Likelihood Estimator covariance model according to the given training data and parameters.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_precision()</td>
<td>Getter for the precision matrix.</td>
</tr>
<tr>
<td>mahalanobis(observations)</td>
<td>Computes the squared Mahalanobis distances of given observations.</td>
</tr>
<tr>
<td>score(X_test[, y])</td>
<td>Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

#### __init__ (store_precision=True, assume_centered=False)

#### error_norm (comp_cov, norm=’frobenius’, scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

**Parameters**

- **comp_cov**: array-like, shape = [n_features, n_features]
  
  The covariance to compare with.

- **norm**: str
  
  The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A))) where A is the error (comp_cov - self.covariance_).

- **scaling**: bool
  
  If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

- **squared**: bool
  
  Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns**

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp_cov covariance estimators.

#### fit (X, y=None)

Fits the Maximum Likelihood Estimator covariance model according to the given training data and parameters.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training data, where n_samples is the number of samples and n_features is the number of features.

- **y**: not used, present for API consistence purpose.

**Returns**

self : object

Returns self.

#### get_params (deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
   Parameter names mapped to their values.

get_precision()  
   Getter for the precision matrix.

   Returns precision_ : array-like,
   The precision matrix associated to the current covariance object.

mahalanobis(observations)  
   Computes the squared Mahalanobis distances of given observations.

   Parameters observations : array-like, shape = [n_observations, n_features]
   The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

   Returns mahalanobis_distance : array, shape = [n_observations,]
   Squared Mahalanobis distances of the observations.

score(X_test, y=None)  
   Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

   Parameters X_test : array-like, shape = [n_samples, n_features]
   Test data of which we compute the likelihood, where n_samples is the number of samples and n_features is the number of features. X_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

   y : not used, present for API consistence purpose.

   Returns res : float
   The likelihood of the data set with self.covariance_ as an estimator of its covariance matrix.

set_params(**params)  
   Set the parameters of this estimator.
   The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

   Returns self

Examples using sklearn.covariance.EmpiricalCovariance

- Robust covariance estimation and Mahalanobis distances relevance
- Robust vs Empirical covariance estimate
30.5.2 sklearn.covariance.EllipticEnvelope

class sklearn.covariance.EllipticEnvelope (store_precision=True, assume_centered=False, support_fraction=None, contamination=0.1, random_state=None)

An object for detecting outliers in a Gaussian distributed dataset.

Read more in the User Guide.

Parameters

store_precision : boolean, optional (default=True)

Specify if the estimated precision is stored.

assume_centered : boolean, optional (default=False)

If True, the support of robust location and covariance estimates is computed, and a covariance estimate is recomputed from it, without centering the data. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, the robust location and covariance are directly computed with the FastMCD algorithm without additional treatment.

support_fraction : float in (0., 1.), optional (default=None)

The proportion of points to be included in the support of the raw MCD estimate. If None, the minimum value of support_fraction will be used within the algorithm: \[\frac{n \text{ sample} + n \text{ features} + 1}{2}\].

contamination : float in (0., 0.5), optional (default=0.1)

The amount of contamination of the data set, i.e. the proportion of outliers in the data set.

random_state : int, RandomState instance or None, optional (default=None)

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>location_</td>
<td>(array-like, shape (n_features,)) Estimated robust location</td>
</tr>
<tr>
<td>covariance_</td>
<td>(array-like, shape (n_features, n_features)) Estimated robust covariance matrix</td>
</tr>
<tr>
<td>precision_</td>
<td>(array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. (stored only if store_precision is True)</td>
</tr>
<tr>
<td>support_</td>
<td>(array-like, shape (n_samples,)) A mask of the observations that have been used to compute the robust estimates of location and shape.</td>
</tr>
</tbody>
</table>

See also:

EmpiricalCovariance, MinCovDet
Notes

Outlier detection from covariance estimation may break or not perform well in high-dimensional settings. In particular, one will always take care to work with $n_{\text{samples}} > n_{\text{features}}^2$.

References

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>correct_covariance(data)</code></td>
<td>Apply a correction to raw Minimum Covariance Determinant estimates.</td>
</tr>
<tr>
<td><code>decision_function(X[, raw_values])</code></td>
<td>Compute the decision function of the given observations.</td>
</tr>
<tr>
<td><code>error_norm(comp_cov[, norm, scaling, squared])</code></td>
<td>Computes the Mean Squared Error between two covariance estimators.</td>
</tr>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Fit the EllipticEnvelope model with X.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>get_precision()</code></td>
<td>Getter for the precision matrix.</td>
</tr>
<tr>
<td><code>mahalanobis(observations)</code></td>
<td>Computes the squared Mahalanobis distances of given observations.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Outlyingness of observations in X according to the fitted model.</td>
</tr>
<tr>
<td><code>reweight_covariance(data)</code></td>
<td>Re-weight raw Minimum Covariance Determinant estimates.</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

`__init__(store_precision=True, assume_centered=False, support_fraction=None, contamination=0.1, random_state=None)`

`correct_covariance(data)`

Apply a correction to raw Minimum Covariance Determinant estimates.

Correction using the empirical correction factor suggested by Rousseeuw and Van Driessen in [RVD81120].

**Parameters**

- **data** : array-like, shape (n_samples, n_features)
  
  The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

**Returns**

- **covariance_corrected** : array-like, shape (n_features, n_features)
  
  Corrected robust covariance estimate.

**References**

[RVD81120]

`decision_function(X, raw_values=False)`

Compute the decision function of the given observations.

**Parameters**

- **X** : array-like, shape (n_samples, n_features)
**raw_values** : bool

Whether or not to consider raw Mahalanobis distances as the decision function. Must be False (default) for compatibility with the others outlier detection tools.

**Returns decision** : array-like, shape (n_samples,)

Decision function of the samples. It is equal to the Mahalanobis distances if **raw_values** is True. By default (**raw_values=False**), it is equal to the cubic root of the shifted Mahalanobis distances. In that case, the threshold for being an outlier is 0, which ensures a compatibility with other outlier detection tools such as the One-Class SVM.

**error_norm** (**comp_cov, norm=’frobenius’, scaling=True, squared=True**)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

**Parameters** **comp_cov** : array-like, shape = [n_features, n_features]

The covariance to compare with.

**norm** : str

The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A))) where A is the error (comp_cov - self.covariance_).

**scaling** : bool

If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

**squared** : bool

Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns** The Mean Squared Error (in the sense of the Frobenius norm) between **self** and **comp_cov** covariance estimators.

**fit** (**X, y=None**)

Fit the EllipticEnvelope model with X.

**Parameters** **X** : numpy array or sparse matrix of shape [n_samples, n_features]

Training data

**y** : (ignored)

**get_params** (**deep=True**)

Get parameters for this estimator.

**Parameters** **deep** : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** **params** : mapping of string to any

Parameter names mapped to their values.

**get_precision** ()

Getter for the precision matrix.

**Returns** **precision_** : array-like

The precision matrix associated to the current covariance object.
**mahalanobis** *(observations)*

Computes the squared Mahalanobis distances of given observations.

**Parameters**

- **observations**: array-like, shape = [n_observations, n_features]

  The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

**Returns**

- **mahalanobis_distance**: array, shape = [n_observations,]

  Squared Mahalanobis distances of the observations.

**predict** *(X)*

Outlyingness of observations in X according to the fitted model.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)

**Returns**

- **is_outliers**: array, shape = (n_samples, ), dtype = bool

  For each observation, tells whether or not it should be considered as an outlier according to the fitted model.

- **threshold**: float,

  The values of the less outlying point’s decision function.

**reweight_covariance** *(data)*

Re-weight raw Minimum Covariance Determinant estimates.

Re-weight observations using Rousseeuw’s method (equivalent to deleting outlying observations from the data set before computing location and covariance estimates) described in [RVDriessen91121].

**Parameters**

- **data**: array-like, shape (n_samples, n_features)

  The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

**Returns**

- **location_reweighted**: array-like, shape (n_features,)

  Re-weighted robust location estimate.

- **covariance_reweighted**: array-like, shape (n_features, n_features)

  Re-weighted robust covariance estimate.

- **support_reweighted**: array-like, type boolean, shape (n_samples,)

  A mask of the observations that have been used to compute the re-weighted robust location and covariance estimates.

**References**

[RVDriessen91121]

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)

  Test samples.

- **y**: array-like, shape = (n_samples,) or (n_samples, n_outputs)
True labels for X.

**sample_weight** : array-like, shape = (n_samples,), optional

Sample weights.

Returns **score** : float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

Examples using `sklearn.covariance.EllipticEnvelope`

- Outlier detection on a real data set
- Outlier detection with several methods.

### 30.5.3 sklearn.covariance.GraphLasso

**class sklearn.covariance.GraphLasso**(*alpha=0.01*, *mode=’cd’, *tol=0.0001*, *enet_tol=0.0001*, *max_iter=100*, *verbose=False*, *assume_centered=False*)

Sparse inverse covariance estimation with an L1-penalized estimator.

Read more in the User Guide.

**Parameters**

- **alpha** : positive float, default 0.01
  - The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.

- **mode** : {'cd', 'lars'}, default ‘cd’
  - The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.

- **tol** : positive float, default 1e-4
  - The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

- **enet_tol** : positive float, optional
  - The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode=’cd’.

- **max_iter** : integer, default 100
  - The maximum number of iterations.

- **verbose** : boolean, default False
  - If verbose is True, the objective function and dual gap are plotted at each iteration.

- **assume_centered** : boolean, default False
If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

Attributes

| covariance_ | (array-like, shape (n_features, n_features)) Estimated covariance matrix |
| precision_  | (array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. |
| n_iter_     | (int) Number of iterations run. |

See also:

graph_lasso, GraphLassoCV

Methods

error_norm(comp_cov[, norm, scaling, squared]) Computes the Mean Squared Error between two covariance estimators.

fit(X[, y]) Fits the GraphLasso model to X.

get_params([deep]) Get parameters for this estimator.

get_precision() Getter for the precision matrix.

mahalanobis(observations) Computes the squared Mahalanobis distances of given observations.

score(X_test[, y]) Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

set_params(**params) Set the parameters of this estimator.

__init__(alpha=0.01, mode='cd', tol=0.0001, enet_tol=0.0001, max_iter=100, verbose=False, assume_centered=False)

error_norm(comp_cov, norm='frobenius', scaling=True, squared=True) Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

Parameters comp_cov : array-like, shape = [n_features, n_features]

The covariance to compare with.

norm : str

The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A)) where A is the error (comp_cov - self.covariance_).

scaling : bool

If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

squared : bool

Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.
Returns The Mean Squared Error (in the sense of the Frobenius norm) between
self and comp_cov covariance estimators.

fit (X, y=None)
Fits the GraphLasso model to X.

Parameters X : ndarray, shape (n_samples, n_features)
Data from which to compute the covariance estimate
y : (ignored)

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

generate_precision()
Getter for the precision matrix.

Returns precision_ : array-like,
The precision matrix associated to the current covariance object.

mahalanobis (observations)
Computes the squared Mahalanobis distances of given observations.

Parameters observations : array-like, shape = [n_observations, n_features]
The observations, the Mahalanobis distances of the which we compute. Observations
are assumed to be drawn from the same distribution than the data used in fit.

Returns mahalanobis_distance : array, shape = [n_observations,]
Squared Mahalanobis distances of the observations.

score (X_test, y=None)
Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance
matrix.

Parameters X_test : array-like, shape = [n_samples, n_features]
Test data of which we compute the likelihood, where n_samples is the number of sam-
ple and n_features is the number of features. X_test is assumed to be drawn from
the same distribution than the data used in fit (including centering).

y : not used, present for API consistence purpose.

Returns res : float
The likelihood of the data set with self.covariance_ as an estimator of its covariance
matrix.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component of
a nested object.
Returns self

30.5.4 sklearn.covariance.GraphLassoCV

class sklearn.covariance.GraphLassoCV (alphas=4, n_refinements=4, cv=None, tol=0.0001, enet_tol=0.0001, max_iter=100, mode='cd', n_jobs=1, verbose=False, assume_centered=False)

Sparse inverse covariance w/ cross-validated choice of the 11 penalty

Read more in the User Guide.

Parameters alphas : integer, or list positive float, optional
If an integer is given, it fixes the number of points on the grids of alpha to be used. If a list is given, it gives the grid to be used. See the notes in the class docstring for more details.

n_refinements : strictly positive integer
The number of times the grid is refined. Not used if explicit values of alphas are passed.

cv : int, cross-validation generator or an iterable, optional
Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

tol : positive float, optional
The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

enet_tol : positive float, optional
The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

max_iter : integer, optional
Maximum number of iterations.

mode : {'cd', 'lars'}
The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where number of features is greater than number of samples. Elsewhere prefer cd which is more numerically stable.

n_jobs : int, optional
number of jobs to run in parallel (default=1).

verbose : boolean, optional
If verbose is True, the objective function and duality gap are printed at each iteration.
**assume_centered** : Boolean

If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>covariance_</td>
<td>(numpy.ndarray, shape (n_features, n_features)) Estimated covariance matrix.</td>
</tr>
<tr>
<td>precision_</td>
<td>(numpy.ndarray, shape (n_features, n_features)) Estimated precision matrix (inverse covariance).</td>
</tr>
<tr>
<td>alpha_</td>
<td>(float) Penalization parameter selected.</td>
</tr>
<tr>
<td>cv_alphas_</td>
<td>(list of float) All penalization parameters explored.</td>
</tr>
<tr>
<td>grid_scores_</td>
<td>(2D numpy.ndarray (n_alphas, n_folds)) Log-likelihood score on left-out data across folds.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Number of iterations run for the optimal alpha.</td>
</tr>
</tbody>
</table>

**See also:**

graph_lasso, GraphLasso

**Notes**

The search for the optimal penalization parameter (alpha) is done on an iteratively refined grid: first the cross-validated scores on a grid are computed, then a new refined grid is centered around the maximum, and so on.

One of the challenges which is faced here is that the solvers can fail to converge to a well-conditioned estimate. The corresponding values of alpha then come out as missing values, but the optimum may be close to these missing values.

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>error_norm</td>
<td>Computes the Mean Squared Error between two covariance estimators.</td>
</tr>
<tr>
<td>fit(X[, y])</td>
<td>Fits the GraphLasso covariance model to X.</td>
</tr>
<tr>
<td>get_params</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_precision</td>
<td>Getter for the precision matrix.</td>
</tr>
<tr>
<td>mahalanobis</td>
<td>Computes the squared Mahalanobis distances of given observations.</td>
</tr>
<tr>
<td>score(X_test[, y])</td>
<td>Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.</td>
</tr>
<tr>
<td>set_params</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**__init__** (alphas=4, n_refinements=4, cv=None, tol=0.0001, enet_tol=0.0001, max_iter=100, mode='cd', n_jobs=1, verbose=False, assume_centered=False)

**error_norm** (comp_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

Parameters **comp_cov** : array-like, shape = [n_features, n_features]
The covariance to compare with.

**norm** : str

The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A)) where A is the error (comp_cov - self.covariance_).

**scaling** : bool

If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

**squared** : bool

Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns** The Mean Squared Error (in the sense of the Frobenius norm) between self and comp_cov covariance estimators.

**fit**(X, y=None)

Fits the GraphLasso covariance model to X.

**Parameters**

**X** : ndarray, shape (n_samples, n_features)

Data from which to compute the covariance estimate

**y** : (ignored)

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

**deep** : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

**params** : mapping of string to any

Parameter names mapped to their values.

**get_precision**()

Getter for the precision matrix.

**Returns**

**precision_** : array-like,

The precision matrix associated to the current covariance object.

**grid_scores**

DEPRECATED: Attribute grid_scores was deprecated in version 0.19 and will be removed in 0.21. Use grid_scores_ instead

**mahalanobis**(observations)

Computes the squared Mahalanobis distances of given observations.

**Parameters**

**observations** : array-like, shape = [n_observations, n_features]

The observations, the Mahalanobis distances of which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

**Returns**

**mahalanobis_distance** : array, shape = [n_observations,]

Squared Mahalanobis distances of the observations.
**score**

Computes the log-likelihood of a Gaussian data set with `self.covariance_` as an estimator of its covariance matrix.

**Parameters**
- **X_test**: array-like, shape = [n_samples, n_features]
  Test data of which we compute the likelihood, where n_samples is the number of samples and n_features is the number of features. X_test is assumed to be drawn from the same distribution than the data used in fit (including centering).
- **y**: not used, present for API consistence purpose.

**Returns**
- **res**: float
  The likelihood of the data set with `self.covariance_` as an estimator of its covariance matrix.

**set_params**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**
- **self**

**Examples using sklearn.covariance.GraphLassoCV**

- Visualizing the stock market structure
- Sparse inverse covariance estimation

### 30.5.5 sklearn.covariance.LedoitWolf

**class sklearn.covariance.LedoitWolf**(store_precision=True, assume_centered=False, block_size=1000)

LedoitWolf Estimator


Read more in the [User Guide](#).

**Parameters**
- **store_precision**: bool, default=True
  Specify if the estimated precision is stored.
- **assume_centered**: bool, default=False
  If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data are centered before computation.
- **block_size**: int, default=1000
  Size of the blocks into which the covariance matrix will be split during its Ledoit-Wolf estimation. This is purely a memory optimization and does not affect results.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>covariance</td>
<td>(array-like, shape (n_features, n_features)) Estimated covariance matrix</td>
</tr>
<tr>
<td>precision</td>
<td>(array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. (stored only if store_precision is True)</td>
</tr>
<tr>
<td>shrinkage</td>
<td>(float, 0 &lt;= shrinkage &lt;= 1) Coefficient in the convex combination used for the computation of the shrunk estimate.</td>
</tr>
</tbody>
</table>

Notes

The regularised covariance is:

\[(1 - \text{shrinkage}) \cdot \text{cov} + \text{shrinkage} \cdot \mu \cdot \text{np.identity(n_features)}\]

where \(\mu = \text{trace(cov)} / \text{n_features}\) and shrinkage is given by the Ledoit and Wolf formula (see References)

References


Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>error_norm</td>
<td>Computes the Mean Squared Error between two covariance estimators.</td>
</tr>
<tr>
<td>fit</td>
<td>Fits the Ledoit-Wolf shrunk covariance model according to the given training data and parameters.</td>
</tr>
<tr>
<td>get_params</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_precision</td>
<td>Getter for the precision matrix.</td>
</tr>
<tr>
<td>mahalanobis</td>
<td>Computes the squared Mahalanobis distances of given observations.</td>
</tr>
<tr>
<td>score</td>
<td>Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.</td>
</tr>
<tr>
<td>set_params</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(store_precision=True, assume_centered=False, block_size=1000)

error_norm(comp_cov[, norm, scaling, squared])

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

Parameters comp_cov : array-like, shape = [n_features, n_features]

The covariance to compare with.

norm : str

The type of norm used to compute the error. Available error types: - ‘frobenius’ (de-
fault): \sqrt{\text{tr}(A^tA)} - \text{‘spectral’: } \sqrt{\text{max(eigenvalues}(A^tA))}

where A is the error \((\text{comp\_cov - self.covariance\_})\).

**scaling** : bool

If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

**squared** : bool

Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns** The Mean Squared Error (in the sense of the Frobenius norm) between self and comp_c cov covariance estimators.

**fit** \((X, y=None)\)

Fits the Ledoit-Wolf shrunk covariance model according to the given training data and parameters.

**Parameters**

- **X** : array-like, shape = \([n\_samples, n\_features]\)
  - Training data, where n_samples is the number of samples and n_features is the number of features.
- **y** : not used, present for API consistence purpose.

**Returns** self : object

Returns self.

**get_params** \((deep=True)\)

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  - Parameter names mapped to their values.

**get_precision**()

Getter for the precision matrix.

**Returns** precision_ : array-like,

The precision matrix associated to the current covariance object.

**mahalanobis** \((observations)\)

Computes the squared Mahalanobis distances of given observations.

**Parameters**

- **observations** : array-like, shape = \([n\_observations, n\_features]\)
  - The observations, the Mahalanobis distances of which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

**Returns** mahalanobis_distance : array, shape = \([n\_observations,]\)

Squared Mahalanobis distances of the observations.

**score** \((X\_test, y=None)\)

Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

**Parameters**

- **X\_test** : array-like, shape = \([n\_samples, n\_features]\)
Test data of which we compute the likelihood, where \( n_{\text{samples}} \) is the number of samples and \( n_{\text{features}} \) is the number of features. \( X_{\text{test}} \) is assumed to be drawn from the same distribution than the data used in fit (including centering).

\( y \) : not used, present for API consistence purpose.

**Returns**

res : float

The likelihood of the data set with \( \text{self.covariance}_\) as an estimator of its covariance matrix.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \( \text{<component>__<parameter>} \) so that it’s possible to update each component of a nested object.

**Returns**

self

### Examples using sklearn.covariance.LedoitWolf

- Ledoit-Wolf vs OAS estimation
- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
- Model selection with Probabilistic PCA and Factor Analysis (FA)

### 30.5.6 sklearn.covariance.MinCovDet

**class** sklearn.covariance.MinCovDet (store_precision=True, assume_centered=False, support_fraction=None, random_state=None)

Minimum Covariance Determinant (MCD): robust estimator of covariance.

The Minimum Covariance Determinant covariance estimator is to be applied on Gaussian-distributed data, but could still be relevant on data drawn from a unimodal, symmetric distribution. It is not meant to be used with multi-modal data (the algorithm used to fit a MinCovDet object is likely to fail in such a case). One should consider projection pursuit methods to deal with multi-modal datasets.

Read more in the User Guide.

**Parameters**

store_precision : bool

Specify if the estimated precision is stored.

assume_centered : Boolean

If True, the support of the robust location and the covariance estimates is computed, and a covariance estimate is recomputed from it, without centering the data. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, the robust location and covariance are directly computed with the FastMCD algorithm without additional treatment.

support_fraction : float, \( 0 < \text{support_fraction} < 1 \)

The proportion of points to be included in the support of the raw MCD estimate. Default is None, which implies that the minimum value of support_fraction will be used within the algorithm: \( \lfloor n_{\text{sample}} + n_{\text{features}} + 1 \rfloor / 2 \)

random_state : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Attributes

- **raw_location_** (array-like, shape (n_features,)) The raw robust estimated location before correction and re-weighting.
- **raw_covariance_** (array-like, shape (n_features, n_features)) The raw robust estimated covariance before correction and re-weighting.
- **raw_support_** (array-like, shape (n_samples,)) A mask of the observations that have been used to compute the raw robust estimates of location and shape, before correction and re-weighting.
- **location_** (array-like, shape (n_features,)) Estimated robust location
- **covariance_** (array-like, shape (n_features, n_features)) Estimated robust covariance matrix
- **precision_** (array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. (stored only if store_precision is True)
- **support_** (array-like, shape (n_samples,)) A mask of the observations that have been used to compute the robust estimates of location and shape.
- **dist_** (array-like, shape (n_samples,)) Mahalanobis distances of the training set (on which fit is called) observations.

References

[Rousseeuw19842329], [Rousseeuw2329], [ButlerDavies2329]

Methods

- **correct_covariance**(data) Apply a correction to raw Minimum Covariance Determinant estimates.
- **error_norm**(comp_cov[, norm, scaling, squared]) Computes the Mean Squared Error between two covariance estimators.
- **fit**(X[, y]) Fits a Minimum Covariance Determinant with the FastMCD algorithm.
- **get_params**(deep) Get parameters for this estimator.
- **get_precision**( ) Getter for the precision matrix.
- **mahalanobis**(observations) Computes the squared Mahalanobis distances of given observations.
- **reweight_covariance**(data) Re-weight raw Minimum Covariance Determinant estimates.
- **score**(X_test[, y]) Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.
- **set_params**( **params) Set the parameters of this estimator.

**__init__**(store_precision=True, assume_centered=False, support_fraction=None, random_state=None)

**correct_covariance**(data)
Apply a correction to raw Minimum Covariance Determinant estimates.

Correction using the empirical correction factor suggested by Rousseeuw and Van Driessen in [RVD262941].

**Parameters**

- **data** : array-like, shape (n_samples, n_features)
  The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

**Returns**

- **covariance_corrected** : array-like, shape (n_features, n_features)
  Corrected robust covariance estimate.

**References**

[RVD262941]

**error_norm**

(error_norm=comp_cov, norm='frobenius', scaling=True, squared=True)

Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

**Parameters**

- **comp_cov** : array-like, shape = [n_features, n_features]
  The covariance to compare with.

- **norm** : str
  The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A)) where A is the error (comp_cov - self.covariance_).

- **scaling** : bool
  If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

- **squared** : bool
  Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns**

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp_cov covariance estimators.

**fit**

(X, y=None)

Fits a Minimum Covariance Determinant with the FastMCD algorithm.

**Parameters**

- **X** : array-like, shape = [n_samples, n_features]
  Training data, where n_samples is the number of samples and n_features is the number of features.

- **y** : not used, present for API consistence purpose.

**Returns**

- **self** : object
  Returns self.

**get_params**

(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_precision ()
Getter for the precision matrix.

Returns precision_ : array-like,
The precision matrix associated to the current covariance object.

mahalanobis (observations)
Computes the squared Mahalanobis distances of given observations.

Parameters observations : array-like, shape = [n_observations, n_features]
The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

Returns mahalanobis_distance : array, shape = [n_observations,]
Squared Mahalanobis distances of the observations.

reweight_covariance (data)
Re-weight raw Minimum Covariance Determinant estimates.
Re-weight observations using Rousseeuw’s method (equivalent to deleting outlying observations from the data set before computing location and covariance estimates) described in [RVDriessen272942].

Parameters data : array-like, shape (n_samples, n_features)
The data matrix, with p features and n samples. The data set must be the one which was used to compute the raw estimates.

Returns location_reweighted : array-like, shape (n_features, )
Re-weighted robust location estimate.

covariance_reweighted : array-like, shape (n_features, n_features)
Re-weighted robust covariance estimate.

support_reweighted : array-like, type boolean, shape (n_samples,)
A mask of the observations that have been used to compute the re-weighted robust location and covariance estimates.

References

[RVDriessen272942]

score (X_test, y=None)
Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

Parameters X_test : array-like, shape = [n_samples, n_features]
Test data of which we compute the likelihood, where n_samples is the number of samples and n_features is the number of features. X_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y : not used, present for API consistence purpose.
Returns res: float

The likelihood of the data set with self.covariance_ as an estimator of its covariance matrix.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.covariance.MinCovDet

- Robust covariance estimation and Mahalanobis distances relevance
- Robust vs Empirical covariance estimate

30.5.7 sklearn.covariance.OAS

class sklearn.covariance.OAS(store_precision=True, assume_centered=False)

Oracle Approximating Shrinkage Estimator

Read more in the User Guide.


The formula used here does not correspond to the one given in the article. It has been taken from the Matlab program available from the authors’ webpage (http://tbayes.eecs.umich.edu/yilun/covestimation). In the original article, formula (23) states that 2/p is multiplied by Trace(cov*cov) in both the numerator and denominator, this operation is omitted in the author’s MATLAB program because for a large p, the value of 2/p is so small that it doesn’t affect the value of the estimator.

Parameters store_precision: bool, default=True

Specify if the estimated precision is stored.

assume_centered: bool, default=False

If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False (default), data are centered before computation.

Attributes

covariance_ (array-like, shape (n_features, n_features)) Estimated covariance matrix.

precision_ (array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. (stored only if store_precision is True)

shrinkage_ (float, 0 <= shrinkage <= 1) coefficient in the convex combination used for the computation of the shrunk estimate.
Notes

The regularised covariance is:

\[(1 - \text{shrinkage}) \times \text{cov} + \text{shrinkage} \times \mu \times \text{np.identity(n\_features)}\]

where \(\mu = \text{trace(cov)} / \text{n\_features}\) and shrinkage is given by the OAS formula (see References)

References


Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>error_norm</td>
<td>Computes the Mean Squared Error between two covariance estimators.</td>
</tr>
<tr>
<td>fit</td>
<td>Fits the Oracle Approximating Shrinkage covariance model according to the given training data and parameters.</td>
</tr>
<tr>
<td>get_params</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_precision</td>
<td>Getter for the precision matrix.</td>
</tr>
<tr>
<td>mahalanobis</td>
<td>Computes the squared Mahalanobis distances of given observations.</td>
</tr>
<tr>
<td>score</td>
<td>Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.</td>
</tr>
<tr>
<td>set_params</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

`__init__` (store_precision=True, assume_centered=False)

`error_norm (comp_c cov[, norm, scaling, squared])` Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

Parameters:
- comp_cov : array-like, shape = [n\_features, n\_features]
  The covariance to compare with.
- norm : str
  The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): \(\sqrt{\text{tr}(A^t.A)}\) - ‘spectral’: \(\sqrt{\max(\text{eigenvalues}(A^t.A))}\) where A is the error \((\text{comp_c cov} - \text{self.covariance}_).\)
- scaling : bool
  If True (default), the squared error norm is divided by n\_features. If False, the squared error norm is not rescaled.
- squared : bool
  Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.
**Returns** The Mean Squared Error (in the sense of the Frobenius norm) between `self` and `comp_cov` covariance estimators.

**fit** `(X, y=None)`
Fits the Oracle Approximating Shrinkage covariance model according to the given training data and parameters.

**Parameters**
- **X** : array-like, shape = [n_samples, n_features]
  Training data, where n_samples is the number of samples and n_features is the number of features.
- **y** : not used, present for API consistence purpose.

**Returns**
- **self** : object
  Returns self.

**get_params** `(deep=True)`
Get parameters for this estimator.

**Parameters**
- **deep** : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params** : mapping of string to any
  Parameter names mapped to their values.

**get_precision** ()
Getter for the precision matrix.

**Returns**
- **precision_** : array-like,
  The precision matrix associated to the current covariance object.

**mahalanobis** `(observations)`
Computes the squared Mahalanobis distances of given observations.

**Parameters**
- **observations** : array-like, shape = [n_observations, n_features]
  The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

**Returns**
- **mahalanobis_distance** : array, shape = [n_observations,]
  Squared Mahalanobis distances of the observations.

**score** `(X_test, y=None)`
Computes the log-likelihood of a Gaussian data set with `self.covariance_` as an estimator of its covariance matrix.

**Parameters**
- **X_test** : array-like, shape = [n_samples, n_features]
  Test data of which we compute the likelihood, where n_samples is the number of samples and n_features is the number of features. X_test is assumed to be drawn from the same distribution than the data used in fit (including centering).
- **y** : not used, present for API consistence purpose.

**Returns**
- **res** : float
  The likelihood of the data set with `self.covariance_` as an estimator of its covariance matrix.
**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  self

**Examples using sklearn.covariance.OAS**

- Ledoit-Wolf vs OAS estimation
- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood

### 30.5.8 sklearn.covariance.ShrunkCovariance

**class sklearn.covariance.ShrunkCovariance**(store_precision=True, assume_centered=False, shrinkage=0.1)

Covariance estimator with shrinkage

Read more in the User Guide.

**Parameters**

- **store_precision** : boolean, default True
  
  Specify if the estimated precision is stored

- **assume_centered** : boolean, default False
  
  If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

- **shrinkage** : float, 0 <= shrinkage <= 1, default 0.1
  
  Coefficient in the convex combination used for the computation of the shrunk estimate.

**Attributes**

<table>
<thead>
<tr>
<th>covariance_</th>
<th>(array-like, shape (n_features, n_features)) Estimated covariance matrix</th>
</tr>
</thead>
<tbody>
<tr>
<td>precision_</td>
<td>(array-like, shape (n_features, n_features)) Estimated pseudo inverse matrix. (stored only if store_precision is True)</td>
</tr>
<tr>
<td>shrinkage</td>
<td>(float, 0 &lt;= shrinkage &lt;= 1) Coefficient in the convex combination used for the computation of the shrunk estimate.</td>
</tr>
</tbody>
</table>

**Notes**

The regularized covariance is given by

\[(1 - \text{shrinkage}) \cdot \text{cov}\]

- shrinkage*mu*np.identity(n_features)

where mu = trace(cov) / n_features
Methods

**error_norm**(comp_cov[, norm, scaling, squared]) Computes the Mean Squared Error between two covariance estimators.

**fit**(X[, y]) Fits the shrunk covariance model according to the given training data and parameters.

**get_params**(deep) Get parameters for this estimator.

**get_precision**() Getter for the precision matrix.

**mahalanobis**(observations) Computes the squared Mahalanobis distances of given observations.

**score**(X_test[, y]) Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

**set_params**(**params) Set the parameters of this estimator.

___init___(store_precision=True, assume_centered=False, shrinkage=0.1)

**error_norm** (comp_cov, norm='frobenius', scaling=True, squared=True) Computes the Mean Squared Error between two covariance estimators. (In the sense of the Frobenius norm).

**Parameters**

comp_cov : array-like, shape = [n_features, n_features]

The covariance to compare with.

norm : str

The type of norm used to compute the error. Available error types: - ‘frobenius’ (default): sqrt(tr(A^t.A)) - ‘spectral’: sqrt(max(eigenvalues(A^t.A)) where A is the error (comp_cov - self.covariance_).

scaling : bool

If True (default), the squared error norm is divided by n_features. If False, the squared error norm is not rescaled.

squared : bool

Whether to compute the squared error norm or the error norm. If True (default), the squared error norm is returned. If False, the error norm is returned.

**Returns**

The Mean Squared Error (in the sense of the Frobenius norm) between self and comp_cov covariance estimators.

**fit**(X, y=None) Fits the shrunk covariance model according to the given training data and parameters.

**Parameters**

X : array-like, shape = [n_samples, n_features]

Training data, where n_samples is the number of samples and n_features is the number of features.

y : not used, present for API consistence purpose.

**Returns**

self : object

Returns self.

**get_params**(deep=True) Get parameters for this estimator.
Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

get_precision()

Getter for the precision matrix.

Returns precision_ : array-like,

The precision matrix associated to the current covariance object.

mahalanobis(observations)

Computes the squared Mahalanobis distances of given observations.

Parameters observations : array-like, shape = [n_observations, n_features]

The observations, the Mahalanobis distances of the which we compute. Observations are assumed to be drawn from the same distribution than the data used in fit.

Returns mahalanobis_distance : array, shape = [n_observations,]

Squared Mahalanobis distances of the observations.

score(X_test, y=None)

Computes the log-likelihood of a Gaussian data set with self.covariance_ as an estimator of its covariance matrix.

Parameters X_test : array-like, shape = [n_samples, n_features]

Test data of which we compute the likelihood, where n_samples is the number of samples and n_features is the number of features. X_test is assumed to be drawn from the same distribution than the data used in fit (including centering).

y : not used, present for API consistence purpose.

Returns res : float

The likelihood of the data set with self.covariance_ as an estimator of its covariance matrix.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.covariance.ShrunkCovariance

- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
- Model selection with Probabilistic PCA and Factor Analysis (FA)

| covariance.empirical_covariance(X[...]) | Computes the Maximum likelihood covariance estimator |
|covariance.graph_lasso(emp_cov, alpha[...]) | L1-penalized covariance estimator |

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<thead>
<tr>
<th>Function</th>
<th>Description</th>
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<tbody>
<tr>
<td><code>covariance.ledoit_wolf(X[, assume_centered, ...])</code></td>
<td>Estimates the shrunk Ledoit-Wolf covariance matrix.</td>
</tr>
<tr>
<td><code>covariance.oas(X[, assume_centered])</code></td>
<td>Estimate covariance with the Oracle Approximating Shrinkage algorithm.</td>
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<tr>
<td><code>covariance.shrunk_covariance(emp_cov[, ...])</code></td>
<td>Calculates a covariance matrix shrunk on the diagonal</td>
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### 30.5.9 sklearn.covariance.empirical_covariance

`sklearn.covariance.empirical_covariance(X, assume_centered=False)`

Computes the Maximum likelihood covariance estimator

**Parameters**

- **X**: ndarray, shape (n_samples, n_features)

  Data from which to compute the covariance estimate

- **assume_centered**: Boolean

  If True, data are not centered before computation. Useful when working with data whose mean is almost, but not exactly zero. If False, data are centered before computation.

**Returns**

- **covariance**: 2D ndarray, shape (n_features, n_features)

  Empirical covariance (Maximum Likelihood Estimator).

**Examples using sklearn.covariance.empirical_covariance**

- Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood

### 30.5.10 sklearn.covariance.graph_lasso

`sklearn.covariance.graph_lasso(emp_cov, alpha, cov_init=None, mode='cd', tol=0.0001, enet_tol=0.001, max_iter=100, verbose=False, return_costs=False, eps=2.220446049250313e-16, return_n_iter=False)`

l1-penalized covariance estimator

Read more in the User Guide.

**Parameters**

- **emp_cov**: 2D ndarray, shape (n_features, n_features)

  Empirical covariance from which to compute the covariance estimate.

- **alpha**: positive float

  The regularization parameter: the higher alpha, the more regularization, the sparser the inverse covariance.

- **cov_init**: 2D array (n_features, n_features), optional

  The initial guess for the covariance.

- **mode**: {'cd', 'lars'}

  The Lasso solver to use: coordinate descent or LARS. Use LARS for very sparse underlying graphs, where p > n. Elsewhere prefer cd which is more numerically stable.

- **tol**: positive float, optional
The tolerance to declare convergence: if the dual gap goes below this value, iterations are stopped.

**enet_tol**: positive float, optional

The tolerance for the elastic net solver used to calculate the descent direction. This parameter controls the accuracy of the search direction for a given column update, not of the overall parameter estimate. Only used for mode='cd'.

**max_iter**: integer, optional

The maximum number of iterations.

**verbose**: boolean, optional

If verbose is True, the objective function and dual gap are printed at each iteration.

**return_costs**: boolean, optional

If return_costs is True, the objective function and dual gap at each iteration are returned.

**eps**: float, optional

The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.

**return_n_iter**: bool, optional

Whether or not to return the number of iterations.

**Returns**

**covariance**: 2D ndarray, shape (n_features, n_features)

The estimated covariance matrix.

**precision**: 2D ndarray, shape (n_features, n_features)

The estimated (sparse) precision matrix.

**costs**: list of (objective, dual gap) pairs

The list of values of the objective function and the dual gap at each iteration. Returned only if return_costs is True.

**n_iter**: int

Number of iterations. Returned only if return_n_iter is set to True.

**See also:**

*GraphLasso, GraphLassoCV*

**Notes**

The algorithm employed to solve this problem is the GLasso algorithm, from the Friedman 2008 Biostatistics paper. It is the same algorithm as in the R *glasso* package.

One possible difference with the *glasso* R package is that the diagonal coefficients are not penalized.

### 30.5.11 sklearn.covariance.ledoit_wolf

`sklearn.covariance.ledoit_wolf(X, assume_centered=False, block_size=1000)`

Estimates the shrunk Ledoit-Wolf covariance matrix.

Read more in the *User Guide*.
Parameters `X` : array-like, shape (n_samples, n_features)

Data from which to compute the covariance estimate

**assume_centered** : boolean, default=False

If True, data are not centered before computation. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, data are centered before computation.

**block_size** : int, default=1000

Size of the blocks into which the covariance matrix will be split. This is purely a memory optimization and does not affect results.

Returns **shrunk_cov** : array-like, shape (n_features, n_features)

Shrunk covariance.

**shrinkage** : float

Coefficient in the convex combination used for the computation of the shrunk estimate.

Notes

The regularized (shrunk) covariance is:

\[(1 - \text{shrinkage}) \times \text{cov} \]

- shrinkage * mu * np.identity(n_features)

where \( \mu = \text{trace(cov)} / \text{n_features} \)

Examples using `sklearn.covariance.ledoit_wolf`

- Sparse inverse covariance estimation

30.5.12 sklearn.covariance.oas

`sklearn.covariance.oas(X, assume_centered=False)`

Estimate covariance with the Oracle Approximating Shrinkage algorithm.

Parameters `X` : array-like, shape (n_samples, n_features)

Data from which to compute the covariance estimate.

**assume_centered** : boolean

If True, data are not centered before computation. Useful to work with data whose mean is significantly equal to zero but is not exactly zero. If False, data are centered before computation.

Returns **shrunk_cov** : array-like, shape (n_features, n_features)

Shrunk covariance.

**shrinkage** : float

Coefficient in the convex combination used for the computation of the shrunk estimate.
Notes

The regularised (shrunken) covariance is:

\[(1 - \text{shrinkage}) \times \text{cov} \]

- \(\text{shrinkage} \times \mu \times \text{n} \times \text{id}(\text{n} \times \text{features})\)

where \(\mu = \text{trace} \times (\text{cov}) / \text{n} \times \text{features}\)

The formula we used to implement the OAS does not correspond to the one given in the article. It has been taken from the MATLAB program available from the author’s webpage (http://tbayes.eecs.umich.edu/yilun/covestimation).

30.5.13 sklearn.covariance.shrunk_covariance

`sklearn.covariance.shrunk_covariance(emp_cov, shrinkage=0.1)`

Calculates a covariance matrix shrunk on the diagonal

Read more in the User Guide.

**Parameters**
- `emp_cov`: array-like, shape (n_features, n_features)
  - Covariance matrix to be shrunk
- `shrinkage`: float, 0 <= shrinkage <= 1
  - Coefficient in the convex combination used for the computation of the shrunk estimate.

**Returns**
- `shrunk_cov`: array-like
  - Shrunken covariance.

Notes

The regularized (shrunken) covariance is given by

\[(1 - \text{shrinkage}) \times \text{cov} \]

- \(\text{shrinkage} \times \mu \times \text{n} \times \text{id}(\text{n} \times \text{features})\)

where \(\mu = \text{trace} \times (\text{cov}) / \text{n} \times \text{features}\)

30.6 sklearn.cross_decomposition: Cross decomposition

**User guide:** See the Cross decomposition section for further details.

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<th>cross_decomposition.CCA([n_components, ...])</th>
<th>CCA Canonical Correlation Analysis.</th>
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<tbody>
<tr>
<td>cross_decomposition.PLSCanonical([...])</td>
<td>PLSCanonical implements the 2 blocks canonical PLS of the original Wold algorithm [Tenenhaus 1998] p.204, referred as PLS-C2A in [Wegelin 2000].</td>
</tr>
<tr>
<td>cross_decomposition.PLSRegression([...])</td>
<td>PLS regression</td>
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<tr>
<td>cross_decomposition.PLSSVD([n_components, ...])</td>
<td>Partial Least Square SVD</td>
</tr>
</tbody>
</table>
30.6.1 sklearn.cross_decomposition.CCA

**class** sklearn.cross_decomposition.CCA(n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)

CCA Canonical Correlation Analysis.

CCA inherits from PLS with mode=”B” and deflation_mode=“canonical”.

Read more in the *User Guide*.

**Parameters**

- **n_components**: int, (default 2).
  
  number of components to keep.

- **scale**: boolean, (default True)
  
  whether to scale the data?

- **max_iter**: an integer, (default 500)
  
  the maximum number of iterations of the NIPALS inner loop

- **tol**: non-negative real, default 1e-06.
  
  the tolerance used in the iterative algorithm

- **copy**: boolean
  
  Whether the deflation be done on a copy. Let the default value to True unless you don’t care about side effects

**Attributes**

- **x_weights_**: (array, [p, n_components]) X block weights vectors.

- **y_weights_**: (array, [q, n_components]) Y block weights vectors.

- **x_loadings_**: (array, [p, n_components]) X block loadings vectors.

- **y_loadings_**: (array, [q, n_components]) Y block loadings vectors.

- **x_scores_**: (array, [n_samples, n_components]) X scores.

- **y_scores_**: (array, [n_samples, n_components]) Y scores.

- **x_rotations_**: (array, [p, n_components]) X block to latents rotations.

- **y_rotations_**: (array, [q, n_components]) Y block to latents rotations.

- **n_iter_**: (array-like) Number of iterations of the NIPALS inner loop for each component.

**See also:**

- PLSCanonical, PLSSVD

**Notes**

For each component k, find the weights u, v that maximizes max corr(Xk u, Yk v), such that |u| = |v| = 1

Note that it maximizes only the correlations between the scores.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current Y score.
References


Examples

```python
>>> from sklearn.cross_decomposition import CCA
>>> X = [[0., 0., 1.], [1.,0.,0.], [2.,2.,2.], [3.,5.,4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> cca = CCA(n_components=1)
>>> cca.fit(X, Y)
...
CCA(copy=True, max_iter=500, n_components=1, scale=True, tol=1e-06)
>>> X_c, Y_c = cca.transform(X, Y)
```

Methods

```python
fit(X, Y) Fit model to data.
```

```python
fit_transform(X[, y]) Learn and apply the dimension reduction on the train data.
```

```python
get_params([deep]) Get parameters for this estimator.
```

```python
predict(X[, copy]) Apply the dimension reduction learned on the train data.
```

```python
score(X, y[, sample_weight]) Returns the coefficient of determination $R^2$ of the prediction.
```

```python
set_params(**params) Set the parameters of this estimator.
```

```python
transform(X[, Y , copy]) Apply the dimension reduction learned on the train data.
```

```python
__init__(n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)
```

```python
fit (X, Y)
Fit model to data.

Parameters X : array-like, shape = [n_samples, n_features]
Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

Y : array-like, shape = [n_samples, n_targets]
Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.
```

```python
fit_transform (X, y=None)
Learn and apply the dimension reduction on the train data.

Parameters X : array-like, shape = [n_samples, n_features]
Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

y : array-like, shape = [n_samples, n_targets]
```
Target vectors, where \( n_{\text{samples}} \) is the number of samples and \( n_{\text{targets}} \) is the number of response variables.

Returns \( x_{\text{scores}} \) if \( Y \) is not given, \((x_{\text{scores}}, y_{\text{scores}})\) otherwise.

get_params \((\text{deep}=\text{True})\)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

predict \((X, \text{copy}=\text{True})\)

Apply the dimension reduction learned on the train data.

Parameters X : array-like, shape = [\( n_{\text{samples}}, n_{\text{features}} \)]

Training vectors, where \( n_{\text{samples}} \) is the number of samples and \( n_{\text{features}} \) is the number of predictors.

copy : boolean, default True

Whether to copy \( X \) and \( Y \), or perform in-place normalization.

Notes

This call requires the estimation of a \( p \times q \) matrix, which may be an issue in high dimensional space.

score \((X, y, \text{sample_weight}=\text{None})\)

Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \((1 - u/v)\), where \( u \) is the residual sum of squares \((y_{\text{true}} - y_{\text{pred}})^2\).sum() and \( v \) is the total sum of squares \((y_{\text{true}} - y_{\text{true}}.\text{mean()})^2\).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

Parameters X : array-like, shape = (\( n_{\text{samples}}, n_{\text{features}} \))

Test samples.

y : array-like, shape = (\( n_{\text{samples}} \)) or (\( n_{\text{samples}}, n_{\text{outputs}} \))

True values for \( X \).

sample_weight : array-like, shape = [\( n_{\text{samples}} \)], optional

Sample weights.

Returns score : float

\( R^2 \) of self.predict(X) wrt. \( y \).

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>_{\text{parameter}}\) so that it's possible to update each component of a nested object.

Returns self
transform \((X, Y=None, copy=True)\)
Apply the dimension reduction learned on the train data.

**Parameters**
- \(X\) : array-like, shape = \([n\_samples, n\_features]\)
  - Training vectors, where \(n\_samples\) is the number of samples and \(n\_features\) is the number of predictors.
- \(Y\) : array-like, shape = \([n\_samples, n\_targets]\)
  - Target vectors, where \(n\_samples\) is the number of samples and \(n\_targets\) is the number of response variables.
- \(copy\) : boolean, default True
  - Whether to copy \(X\) and \(Y\), or perform in-place normalization.

**Returns**
- \(x\_scores\) if \(Y\) is not given, \((x\_scores, y\_scores)\) otherwise.

**Examples using sklearn.cross_decomposition.CCA**

- Multilabel classification
- Compare cross decomposition methods

### 30.6.2 sklearn.cross_decomposition.PLSCanonical

**class** sklearn.cross_decomposition.PLSCanonical

PLSCanonical implements the 2 blocks canonical PLS of the original Wold algorithm [Tenenhaus 1998] p.204, referred as PLS-C2A in [Wegelin 2000].

This class inherits from PLS with mode=”A” and deflation_mode=”canonical”, norm_y_weights=True and algorithm=”nipals”, but svd should provide similar results up to numerical errors.

Read more in the User Guide.

**Parameters**
- \(n\_components\) : int, (default 2).
  - Number of components to keep
- \(scale\) : boolean, (default True)
  - Option to scale data
- \(algorithm\) : string, “nipals” or “svd”
  - The algorithm used to estimate the weights. It will be called \(n\_components\) times, i.e. once for each iteration of the outer loop.
- \(max\_iter\) : an integer, (default 500)
  - the maximum number of iterations of the NIPALS inner loop (used only if algorithm=”nipals”)
- \(tol\) : non-negative real, default 1e-06
  - the tolerance used in the iterative algorithm
- \(copy\) : boolean, default True
  - Whether the deflation should be done on a copy. Let the default value to True unless you don’t care about side effect
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>x_weights_</td>
<td>(array, shape = [p, n_components]) X block weights vectors.</td>
</tr>
<tr>
<td>y_weights_</td>
<td>(array, shape = [q, n_components]) Y block weights vectors.</td>
</tr>
<tr>
<td>x_loadings_</td>
<td>(array, shape = [p, n_components]) X block loadings vectors.</td>
</tr>
<tr>
<td>y_loadings_</td>
<td>(array, shape = [q, n_components]) Y block loadings vectors.</td>
</tr>
<tr>
<td>x_scores_</td>
<td>(array, shape = [n_samples, n_components]) X scores.</td>
</tr>
<tr>
<td>y_scores_</td>
<td>(array, shape = [n_samples, n_components]) Y scores.</td>
</tr>
<tr>
<td>x_rotations_</td>
<td>(array, shape = [p, n_components]) X block to latents rotations.</td>
</tr>
<tr>
<td>y_rotations_</td>
<td>(array, shape = [q, n_components]) Y block to latents rotations.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(array-like) Number of iterations of the NIPALS inner loop for each component. Not useful if the algorithm provided is “svd”.</td>
</tr>
</tbody>
</table>

See also:

CCA, PLSSVD

Notes

Matrices:

T: x_scores_
U: y_scores_
W: x_weights_
C: y_weights_
P: x_loadings_
Q: y_loadings_

Are computed such that:

\[
X = T P.T + \text{Err} \quad \text{and} \quad Y = U Q.T + \text{Err}
\]

\[
T[:, k] = X_k W[:, k] \quad \text{for} \quad k \in \text{range}(n_{\text{components}})
\]

\[
U[:, k] = Y_k C[:, k] \quad \text{for} \quad k \in \text{range}(n_{\text{components}})
\]

\[
x_{\text{rotations}}_\text{=} W (P.T W)^{-1}
\]

\[
y_{\text{rotations}}\text{=} C (Q.T C)^{-1}
\]

where X_k and Y_k are residual matrices at iteration k.

Slides explaining PLS

For each component k, find weights u, v that optimize:

\[
\max \text{ corr} (X_k u, Y_k v) \ast \text{std} (X_k u) \text{ std} (Y_k v), \quad \text{such that} \quad u \ast v = 1
\]

Note that it maximizes both the correlations between the scores and the intra-block variances.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current Y score. This performs a canonical symmetric version of the PLS regression. But slightly different than the CCA. This is mostly used for modeling.

This implementation provides the same results that the “plspm” package provided in the R language (R-project), using the function plsca(X, Y). Results are equal or collinear with the function pls(..., mode = "canonical") of the “mixOmics” package. The difference relies in the fact that mixOmics implementation does not exactly implement the Wold algorithm since it does not normalize y_weights to one.
References


Examples

```python
>>> from sklearn.cross_decomposition import PLSCanonical
>>> X = [[0., 0., 1.], [1., 0., 0.], [2., 2., 2.], [2., 5., 4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> plsca = PLSCanonical(n_components=2)
>>> plsca.fit(X, Y)
... PLSCanonical(algorithm='nipals', copy=True, max_iter=500, n_components=2, scale=True, tol=1e-06)
>>> X_c, Y_c = plsca.transform(X, Y)
```

Methods

- **fit(X, Y)**
  Fit model to data.

- **fit_transform(X[, y])**
  Learn and apply the dimension reduction on the train data.

- **get_params([deep])**
  Get parameters for this estimator.

- **predict(X[, copy])**
  Apply the dimension reduction learned on the train data.

- **score(X, y[, sample_weight])**
  Returns the coefficient of determination $R^2$ of the prediction.

- **set_params(**params)**
  Set the parameters of this estimator.

- **transform(X[, Y , copy])**
  Apply the dimension reduction learned on the train data.

**__init__**(n_components=2, scale=True, algorithm='nipals', max_iter=500, tol=1e-06, copy=True)

**fit (X, Y)**
Fit model to data.

**Parameters**
- **X** : array-like, shape = [n_samples, n_features]
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

- **Y** : array-like, shape = [n_samples, n_targets]
  Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

**fit_transform(X, y=None)**
Learn and apply the dimension reduction on the train data.

**Parameters**
- **X** : array-like, shape = [n_samples, n_features]
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

- **y** : array-like, shape = [n_samples, n_targets]
Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

**Returns** x_scores if Y is not given, (x_scores, y_scores) otherwise.

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  
  Parameter names mapped to their values.

**predict** *(X, copy=True)*
Apply the dimension reduction learned on the train data.

**Parameters**

- **X** : array-like, shape = [n_samples, n_features]
  
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

- **copy** : boolean, default True
  
  Whether to copy X and Y, or perform in-place normalization.

**Notes**

This call requires the estimation of a p x q matrix, which may be an issue in high dimensional space.

**score** *(X, y, sample_weight=None)*
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters**

- **X** : array-like, shape = (n_samples, n_features)
  
  Test samples.

- **y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
  
  True values for X.

- **sample_weight** : array-like, shape = [n_samples], optional
  
  Sample weights.

**Returns**

- **score** : float
  
  R^2 of self.predict(X) wrt. y.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**
transform \((X, Y=None, copy=True)\)

Apply the dimension reduction learned on the train data.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

- **Y**: array-like, shape = [n_samples, n_targets]
  
  Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

- **copy**: boolean, default True
  
  Whether to copy X and Y, or perform in-place normalization.

**Returns**

- **x_scores** if Y is not given, 
- **(x_scores, y_scores)** otherwise.

**Examples using** sklearn.cross_decomposition.PLSCanonical

- **Compare cross decomposition methods**

**30.6.3 sklearn.cross_decomposition.PLSRegression**

```python
class sklearn.cross_decomposition.PLSRegression(n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)
```

PLS regression

PLSRegression implements the PLS 2 blocks regression known as PLS2 or PLS1 in case of one dimensional response. This class inherits from _PLS with mode="A", deflation_mode="regression", norm_y_weights=False and algorithm="nipals".

Read more in the User Guide.

**Parameters**

- **n_components**: int, (default 2)
  
  Number of components to keep.

- **scale**: boolean, (default True)
  
  Whether to scale the data

- **max_iter**: an integer, (default 500)
  
  the maximum number of iterations of the NIPALS inner loop (used only if algorithm="nipals")

- **tol**: non-negative real
  
  Tolerance used in the iterative algorithm default 1e-06.

- **copy**: boolean, default True
  
  Whether the deflation should be done on a copy. Let the default value to True unless you don’t care about side effect
Attributes

| x_weights_ | (array, [p, n_components]) X block weights vectors. |
| y_weights_ | (array, [q, n_components]) Y block weights vectors. |
| x_loadings_ | (array, [p, n_components]) X block loadings vectors. |
| y_loadings_ | (array, [q, n_components]) Y block loadings vectors. |
| x_scores_ | (array, [n_samples, n_components]) X scores. |
| y_scores_ | (array, [n_samples, n_components]) Y scores. |
| x_rotations_ | (array, [p, n_components]) X block to latents rotations. |
| y_rotations_ | (array, [q, n_components]) Y block to latents rotations. |
| coef_ | (array, [p, q]) The coefficients of the linear model: \( Y = X \text{coef}_\) + Err |
| n_iter_ | (array-like) Number of iterations of the NIPALS inner loop for each component. |

Notes

Matrices:

| T: x_scores_ |
| U: y_scores_ |
| W: x_weights_ |
| C: y_weights_ |
| P: x_loadings_ |
| Q: y_loadings_ |

Are computed such that:

\[
X = T P . T + \text{Err} \quad \text{and} \quad Y = U Q . T + \text{Err} \\
T[:, k] = Xk W[:, k] \quad \text{for} \quad k \in \text{range}(n\_\text{components}) \\
U[:, k] = Yk C[:, k] \quad \text{for} \quad k \in \text{range}(n\_\text{components}) \\
x\_\text{rotations}_\) = W (P . T W)^(-1) \\
y\_\text{rotations}_\) = C (Q . T C)^(-1) \\
\]

where Xk and Yk are residual matrices at iteration k.

Slides explaining PLS

For each component k, find weights u, v that optimizes: \( \max \text{corr}(Xk u, Yk v) \times \text{std}(Xk u) / \text{std}(Yk u) \), such that \(|u| = 1\)

Note that it maximizes both the correlations between the scores and the intra-block variances.

The residual matrix of X (Xk+1) block is obtained by the deflation on the current X score: x_score.

The residual matrix of Y (Yk+1) block is obtained by deflation on the current X score. This performs the PLS regression known as PLS2. This mode is prediction oriented.

This implementation provides the same results that 3 PLS packages provided in the R language (R-project):

- "mixOmics" with function pls(X, Y, mode = "regression")
- "plspm" with function plsreg2(X, Y)
- "pls" with function oscorespls.fit(X, Y)
References


Examples

```python
>>> from sklearn.cross_decomposition import PLSRegression
>>> X = [[0., 0., 1.], [1.,0.,0.], [2.,2.,2.], [2.,5.,4.]]
>>> Y = [[0.1, -0.2], [0.9, 1.1], [6.2, 5.9], [11.9, 12.3]]
>>> pls2 = PLSRegression(n_components=2)
>>> pls2.fit(X, Y)
...  
>>> Y_pred = pls2.predict(X)
```

Methods

- `fit(X, Y)` Fit model to data.
- `fit_transform(X[, y])` Learn and apply the dimension reduction on the train data.
- `get_params([deep])` Get parameters for this estimator.
- `predict(X[, copy])` Apply the dimension reduction learned on the train data.
- `score(X, y[, sample_weight])` Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X[, Y , copy])` Apply the dimension reduction learned on the train data.

```python
__init__(n_components=2, scale=True, max_iter=500, tol=1e-06, copy=True)
fit (X, Y)
  Fit model to data.

Parameters

X : array-like, shape = [n_samples, n_features]
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

Y : array-like, shape = [n_samples, n_targets]
  Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.
```

```python
fit_transform(X, y=None)
  Learn and apply the dimension reduction on the train data.

Parameters

X : array-like, shape = [n_samples, n_features]
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.
```

y : array-like, shape = [n_samples, n_targets]
Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

Returns x_scores if Y is not given, (x_scores, y_scores) otherwise.

get_params (deep=True)
Get parameters for this estimator.

Parameters:
- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns:
- params : mapping of string to any
  Parameter names mapped to their values.

predict (X, copy=True)
Apply the dimension reduction learned on the train data.

Parameters:
- X : array-like, shape = [n_samples, n_features]
  Training vectors, where n_samples is the number of samples and n_features is the number of predictors.
- copy : boolean, default True
  Whether to copy X and Y, or perform in-place normalization.

Notes
This call requires the estimation of a p x q matrix, which may be an issue in high dimensional space.

score (X, y, sample_weight=None)
Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_true - y_pred)^2).sum()$ and $v$ is the total sum of squares $((y_true - y_true.mean())^2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

Parameters:
- X : array-like, shape = (n_samples, n_features)
  Test samples.
- y : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.
- sample_weight : array-like, shape = [n_samples], optional
  Sample weights.

Returns:
- score : float
  $R^2$ of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.
Returns self

transform(X, Y=None, copy=True)

Apply the dimension reduction learned on the train data.

Parameters
X : array-like, shape = [n_samples, n_features]
    Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

Y : array-like, shape = [n_samples, n_targets]
    Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

copy : boolean, default True
    Whether to copy X and Y, or perform in-place normalization.

Returns
x_scores if Y is not given, (x_scores, y_scores) otherwise.

Examples using sklearn.cross_decomposition.PLSRegression

• Compare cross decomposition methods

30.6.4 sklearn.cross_decomposition.PLSSVD

class sklearn.cross_decomposition.PLSSVD(n_components=2, scale=True, copy=True)

Partial Least Square SVD

Simply perform a svd on the crosscovariance matrix: X'Y There are no iterative deflation here.

Read more in the User Guide.

Parameters
n_components : int, default 2
    Number of components to keep.

scale : boolean, default True
    Whether to scale X and Y.

copy : boolean, default True
    Whether to copy X and Y, or perform in-place computations.

Attributes

x_weights_  (array, [p, n_components]) X block weights vectors.
y_weights_  (array, [q, n_components]) Y block weights vectors.
x_scores_  (array, [n_samples, n_components]) X scores.
y_scores_  (array, [n_samples, n_components]) Y scores.

See also:
PLSCanonical, CCA
### Methods

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<td><code>fit_transform(X[, y])</code></td>
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</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X[, Y])</code></td>
<td>Apply the dimension reduction learned on the train data.</td>
</tr>
</tbody>
</table>

```python
__init__(n_components=2, scale=True, copy=True)
```

Fit model to data.

**Parameters**

- `X`: array-like, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of predictors.
- `Y`: array-like, shape = [n_samples, n_targets]
  - Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

```python
fit_transform(X, y=None)
```

Learn and apply the dimension reduction on the train data.

**Parameters**

- `X`: array-like, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of predictors.
- `y`: array-like, shape = [n_samples, n_targets]
  - Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

**Returns**

- `x_scores` if `Y` is not given, `(x_scores, y_scores)` otherwise.

```python
get_params(deep=True)
```

Get parameters for this estimator.

**Parameters**

- `deep`: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- `params`: mapping of string to any Parameter names mapped to their values.

```python
set_params(**params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- `self`

```python
transform(X, Y=None)
```

Apply the dimension reduction learned on the train data.
Parameters $X$: array-like, shape = [n_samples, n_features]

Training vectors, where n_samples is the number of samples and n_features is the number of predictors.

$Y$: array-like, shape = [n_samples, n_targets]

Target vectors, where n_samples is the number of samples and n_targets is the number of response variables.

## 30.7 sklearn.datasets: Datasets

The **sklearn.datasets** module includes utilities to load datasets, including methods to load and fetch popular reference datasets. It also features some artificial data generators.

**User guide:** See the **Dataset loading utilities** section for further details.

### 30.7.1 Loaders

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<th>Function</th>
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<td>Delete all the content of the data home cache.</td>
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<tr>
<td><code>datasets.fetch_20newsgroups(data_home, ...)</code></td>
<td>Load the filenames and data from the 20 newsgroups dataset.</td>
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<td><code>datasets.fetch_20newsgroups_vectorized([...])</code></td>
<td>Load the 20 newsgroups dataset and transform it into tf-idf vectors.</td>
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<tr>
<td><code>datasets.fetch_california_housing([...])</code></td>
<td>Loader for the California housing dataset from StatLib.</td>
</tr>
<tr>
<td><code>datasets.fetch_covtype([data_home, ...])</code></td>
<td>Load the covertype dataset, downloading it if necessary.</td>
</tr>
<tr>
<td><code>datasets.fetch_kddcup99([subset, data_home, ...])</code></td>
<td>Load and return the kddcup99 dataset (classification).</td>
</tr>
<tr>
<td><code>datasets.fetch_lfw_pairs([subset, ...])</code></td>
<td>Loader for the Labeled Faces in the Wild (LFW) pairs dataset.</td>
</tr>
<tr>
<td><code>datasets.fetch_lfw_people([data_home, ...])</code></td>
<td>Loader for the Labeled Faces in the Wild (LFW) people dataset.</td>
</tr>
<tr>
<td><code>datasets.fetch_mldata(dataname[, ...])</code></td>
<td>Fetch an mldata.org data set.</td>
</tr>
<tr>
<td><code>datasets.fetch_olivetti_faces([data_home, ...])</code></td>
<td>Loader for the Olivetti faces data-set from AT&amp;T.</td>
</tr>
<tr>
<td><code>datasets.fetch_rcv1([data_home, subset, ...])</code></td>
<td>Load the RCV1 multilabel dataset, downloading it if necessary.</td>
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<tr>
<td><code>datasets.fetch_species_distributions([...])</code></td>
<td>Loader for species distribution dataset from Phillips et.</td>
</tr>
<tr>
<td><code>datasets.get_data_home([data_home])</code></td>
<td>Return the path of the scikit-learn data dir.</td>
</tr>
<tr>
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<td>Load and return the boston house-prices dataset (regression).</td>
</tr>
<tr>
<td><code>datasets.load_breast_cancer([return_X_y])</code></td>
<td>Load and return the breast cancer wisconsin dataset (classification).</td>
</tr>
<tr>
<td><code>datasets.load_diabetes([return_X_y])</code></td>
<td>Load and return the diabetes dataset (regression).</td>
</tr>
<tr>
<td><code>datasets.load_digits([n_class, return_X_y])</code></td>
<td>Load and return the digits dataset (classification).</td>
</tr>
<tr>
<td><code>datasets.load_files(container_path[, ...])</code></td>
<td>Load text files with categories as subfolder names.</td>
</tr>
<tr>
<td><code>datasets.load_iris([return_X_y])</code></td>
<td>Load and return the iris dataset (classification).</td>
</tr>
<tr>
<td><code>datasets.load_linnerud([return_X_y])</code></td>
<td>Load and return the linnerud dataset (multivariate regression).</td>
</tr>
</tbody>
</table>
DEPRECATED: since the http://mlcomp.org/ website will shut down in March 2017, the load_mlcomp function was deprecated in version 0.19 and will be removed in 0.21.

Datasets that provide images:

- `datasets.load_sample_image(image_name)` Load the numpy array of a single sample image.
- `datasets.load_sample_images()` Load sample images for image manipulation.

Datasets that load text-based datasets:

- `datasets.load_svmlight_file(f[, n_features,...])` Load datasets in the svmlight / libsvm format into sparse CSR matrix.
- `datasets.load_svmlight_files(files[,...])` Load dataset from multiple files in SVMlight format.
- `datasets.load_wine([return_X_y])` Load and return the wine dataset (classification).

Utilities for data manipulation:

- `sklearn.datasets.clear_data_home(data_home=None)` Delete all the content of the data home cache.
  - Parameters data_home : str | None
    - The path to scikit-learn data dir.

- `sklearn.datasets.dump_svmlight_file(X, y, f, zero_based=True, comment=None, query_id=None, multilabel=False)` Dump the dataset in svmlight / libsvm file format.
  - The first element of each line can be used to store a target variable to predict.
  - Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
    - Training vectors, where n_samples is the number of samples and n_features is the number of features.
  - y : {array-like, sparse matrix}, shape = [n_samples, n_labels]
    - Target values. Class labels must be an integer or float, or array-like objects of integer or float for multilabel classifications.
  - f : string or file-like in binary mode
    - If string, specifies the path that will contain the data. If file-like, data will be written to f. f should be opened in binary mode.
  - zero_based : boolean, optional
    - Whether column indices should be written zero-based (True) or one-based (False).
  - comment : string, optional
    - Comment to insert at the top of the file. This should be either a Unicode string, which will be encoded as UTF-8, or an ASCII byte string. If a comment is given, then it will be preceded by one that identifies the file as having been dumped by scikit-learn. Note that not all tools grok comments in SVMlight files.
  - query_id : array-like, shape = [n_samples]
    - Array containing pairwise preference constraints (qid in svmlight format).
**multilabel**: boolean, optional

Samples may have several labels each (see http://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)

New in version 0.17: parameter `multilabel` to support multilabel datasets.

**Examples using sklearn.datasets.dump_svmlight_file**

- **Libsvm GUI**

**sklearn.datasets.fetch_20newsgroups**

```python
sklearn.datasets.fetch_20newsgroups(data_home=None, subset='train', categories=None,
shuffle=True, random_state=42, remove=(), download_if_missing=True)
```

Load the filenames and data from the 20 newsgroups dataset.

Read more in the *User Guide*.

**Parameters**

**data_home**: optional, default: None

Specify a download and cache folder for the datasets. If None, all scikit-learn data is stored in `~/scikit_learn_data` subfolders.

**subset**: ‘train’ or ‘test’, ‘all’, optional

Select the dataset to load: ‘train’ for the training set, ‘test’ for the test set, ‘all’ for both, with shuffled ordering.

**categories**: None or collection of string or unicode

If None (default), load all the categories. If not None, list of category names to load (other categories ignored).

**shuffle**: bool, optional

Whether or not to shuffle the data: might be important for models that make the assumption that the samples are independent and identically distributed (i.i.d.), such as stochastic gradient descent.

**random_state**: numpy random number generator or seed integer

Used to shuffle the dataset.

**remove**: tuple

May contain any subset of (‘headers’, ‘footers’, ‘quotes’). Each of these are kinds of text that will be detected and removed from the newsgroup posts, preventing classifiers from overfitting on metadata.

‘headers’ removes newsgroup headers, ‘footers’ removes blocks at the ends of posts that look like signatures, and ‘quotes’ removes lines that appear to be quoting another post.

‘headers’ follows an exact standard; the other filters are not always correct.

**download_if_missing**: optional, True by default

If False, raise an IOError if the data is not locally available instead of trying to download the data from the source site.
Examples using `sklearn.datasets.fetch_20newsgroups`

- Feature Union with Heterogeneous Data Sources
- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Biclustering documents with the Spectral Co-clustering algorithm
- Sample pipeline for text feature extraction and evaluation
- FeatureHasher and DictVectorizer Comparison
- Clustering text documents using k-means
- Classification of text documents using sparse features

`sklearn.datasets.fetch_20newsgroups_vectorized`

```python
sklearn.datasets.fetch_20newsgroups_vectorized(subset='train', remove=(),
                                             data_home=None,
                                             download_if_missing=True)
```

Load the 20 newsgroups dataset and transform it into tf-idf vectors.

This is a convenience function; the tf-idf transformation is done using the default settings for `sklearn.feature_extraction.textVectorizer`. For more advanced usage (stopword filtering, n-gram extraction, etc.), combine fetch_20newsgroups with a custom `Vectorizer` or `CountVectorizer`.

Read more in the User Guide.

**Parameters**

- `subset` : ‘train’ or ‘test’, ‘all’, optional
  - Select the dataset to load: ‘train’ for the training set, ‘test’ for the test set, ‘all’ for both, with shuffled ordering.

- `remove` : tuple
  - May contain any subset of (‘headers’, ‘footers’, ‘quotes’). Each of these are kinds of text that will be detected and removed from the newsgroup posts, preventing classifiers from overfitting on metadata.
  - ‘headers’ removes newsgroup headers, ‘footers’ removes blocks at the ends of posts that look like signatures, and ‘quotes’ removes lines that appear to be quoting another post.

- `data_home` : optional, default: None
  - Specify an download and cache folder for the datasets. If None, all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.

- `download_if_missing` : optional, True by default
  - If False, raise an IOError if the data is not locally available instead of trying to download the data from the source site.

**Returns**

- `bunch` : Bunch object
  - `bunch.data`: sparse matrix, shape [n_samples, n_features]
  - `bunch.target`: array, shape [n_samples]
  - `bunch.target_names`: list, length [n_classes]

Examples using `sklearn.datasets.fetch_20newsgroups_vectorized`

- The Johnson-Lindenstrauss bound for embedding with random projections
• **Model Complexity Influence**

• **Multiclass sparse logistic regression on newsgroups20**

**sklearn.datasets.fetch_california_housing**

```python
sklearn.datasets.fetch_california_housing(data_home=None,
download_if_missing=True)
```

Loader for the California housing dataset from StatLib.

Read more in the User Guide.

**Parameters**

- **data_home**: optional, default: None
  
  Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit_learn_data' subfolders.

- **download_if_missing**: optional, True by default
  
  If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**Returns**

- **dataset**: dict-like object with the following attributes:
  
  - **dataset.data**: ndarray, shape [20640, 8]
    
    Each row corresponding to the 8 feature values in order.
  
  - **dataset.target**: numpy array of shape (20640,)
    
    Each value corresponds to the average house value in units of 100,000.
  
  - **dataset.feature_names**: array of length 8
    
    Array of ordered feature names used in the dataset.
  
  - **dataset.DESCR**: string
    
    Description of the California housing dataset.

**Notes**

This dataset consists of 20,640 samples and 9 features.

**Examples using sklearn.datasets.fetch_california_housing**

- **Partial Dependence Plots**

- **Compare the effect of different scalers on data with outliers**

**sklearn.datasets.fetch_covtype**

```python
sklearn.datasets.fetch_covtype(data_home=None,
download_if_missing=True,
random_state=None, shuffle=False)
```

Load the covtype dataset, downloading it if necessary.

Read more in the User Guide.

**Parameters**

- **data_home**: string, optional
Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.

**download_if_missing** : boolean, default=True

If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**random_state** : int, RandomState instance or None, optional (default=None)

Random state for shuffling the dataset. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**shuffle** : bool, default=False

Whether to shuffle dataset.

**Returns** dataset : dict-like object with the following attributes:

- **dataset.data** : numpy array of shape (581012, 54)
  - Each row corresponds to the 54 features in the dataset.

- **dataset.target** : numpy array of shape (581012,)
  - Each value corresponds to one of the 7 forest covetypes with values ranging between 1 to 7.

- **dataset.DESCR** : string
  - Description of the forest covertype dataset.

### sklearn.datasets.fetch_kddcup99

**sklearn.datasets.fetch_kddcup99**

Load and return the kddcup 99 dataset (classification).

The KDD Cup ‘99 dataset was created by processing the tcpdump portions of the 1998 DARPA Intrusion Detection System (IDS) Evaluation dataset, created by MIT Lincoln Lab [1]. The artificial data was generated using a closed network and hand-injected attacks to produce a large number of different types of attack with normal activity in the background. As the initial goal was to produce a large training set for supervised learning algorithms, there is a large proportion (80.1%) of abnormal data which is unrealistic in real world, and inappropriate for unsupervised anomaly detection which aims at detecting ‘abnormal’ data, i.e

1. qualitatively different from normal data.
2. in large minority among the observations.

We thus transform the KDD Data set into two different data sets: SA and SF.

- SA is obtained by simply selecting all the normal data, and a small proportion of abnormal data to gives an anomaly proportion of 1%.
- SF is obtained as in [2] by simply picking up the data whose attribute logged_in is positive, thus focusing on the intrusion attack, which gives a proportion of 0.3% of attack.
- http and smtp are two subsets of SF corresponding with third feature equal to ‘http’ (resp. to ‘smtp’)

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General KDD structure:

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>4898431</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>41</td>
</tr>
<tr>
<td>Features</td>
<td>discrete (int) or continuous (float)</td>
</tr>
<tr>
<td>Targets</td>
<td>str, ‘normal.’ or name of the anomaly type</td>
</tr>
</tbody>
</table>

SA structure:

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>976158</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>41</td>
</tr>
<tr>
<td>Features</td>
<td>discrete (int) or continuous (float)</td>
</tr>
<tr>
<td>Targets</td>
<td>str, ‘normal.’ or name of the anomaly type</td>
</tr>
</tbody>
</table>

SF structure:

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>699691</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>4</td>
</tr>
<tr>
<td>Features</td>
<td>discrete (int) or continuous (float)</td>
</tr>
<tr>
<td>Targets</td>
<td>str, ‘normal.’ or name of the anomaly type</td>
</tr>
</tbody>
</table>

http structure:

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>619052</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>3</td>
</tr>
<tr>
<td>Features</td>
<td>discrete (int) or continuous (float)</td>
</tr>
<tr>
<td>Targets</td>
<td>str, ‘normal.’ or name of the anomaly type</td>
</tr>
</tbody>
</table>

smtp structure:

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>95373</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>3</td>
</tr>
<tr>
<td>Features</td>
<td>discrete (int) or continuous (float)</td>
</tr>
<tr>
<td>Targets</td>
<td>str, ‘normal.’ or name of the anomaly type</td>
</tr>
</tbody>
</table>

New in version 0.18.

**Parameters**

- **subset**: None, ‘SA’, ‘SF’, ‘http’, ‘smtp’
  
  To return the corresponding classical subsets of kddcup 99. If None, return the entire kddcup 99 dataset.

- **data_home**: string, optional
  
  Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders. .. versionadded:: 0.19

- **shuffle**: bool, default=False
  
  Whether to shuffle dataset.

- **random_state**: int, RandomState instance or None, optional (default=None)
Random state for shuffling the dataset. If subset=’SA’, this random state is also used to randomly select the small proportion of abnormal samples. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

percent10 : bool, default=True
Whether to load only 10 percent of the data.

download_if_missing : bool, default=True
If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

Returns data : Bunch
Dictionary-like object, the interesting attributes are: ‘data’, the data to learn and ‘target’, the regression target for each sample.

References

[R329330], [R330330]

sklearn.datasets.fetch_lfw_pairs

sklearn.datasets.fetch_lfw_pairs(subset=’train’, data_home=None, funneled=True, resize=0.5, color=False, slice_=(slice(70, 195, None), slice(78, 172, None)), download_if_missing=True)

Loader for the Labeled Faces in the Wild (LFW) pairs dataset

This dataset is a collection of JPEG pictures of famous people collected on the internet, all details are available on the official website:

http://vis-www.cs.umass.edu/lfw/

Each picture is centered on a single face. Each pixel of each channel (color in RGB) is encoded by a float in range 0.0 - 1.0.

The task is called Face Verification: given a pair of two pictures, a binary classifier must predict whether the two images are from the same person.

In the official README.txt this task is described as the “Restricted” task. As I am not sure as to implement the “Unrestricted” variant correctly, I left it as unsupported for now.

The original images are 250 x 250 pixels, but the default slice and resize arguments reduce them to 62 x 47.

Read more in the User Guide.

Parameters subset : optional, default: ‘train’
Select the dataset to load: ‘train’ for the development training set, ‘test’ for the development test set, and ‘10_folds’ for the official evaluation set that is meant to be used with a 10-folds cross validation.

data_home : optional, default: None
Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.
funneled : boolean, optional, default: True
    Download and use the funneled variant of the dataset.

resize : float, optional, default 0.5
    Ratio used to resize the each face picture.

color : boolean, optional, default False
    Keep the 3 RGB channels instead of averaging them to a single gray level channel. If color is True the shape of the data has one more dimension than the shape with color = False.
	slice_: optional
    Provide a custom 2D slice (height, width) to extract the ‘interesting’ part of the jpeg files and avoid use statistical correlation from the background

download_if_missing : optional, True by default
    If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

Returns  The data is returned as a Bunch object with the following attributes:

data : numpy array of shape (2200, 5828). Shape depends on subset.
    Each row corresponds to 2 ravel’d face images of original size 62 x 47 pixels. Changing the slice_, resize or subset parameters will change the shape of the output.

pairs : numpy array of shape (2200, 2, 62, 47). Shape depends on subset.
    Each row has 2 face images corresponding to same or different person from the dataset containing 5749 people. Changing the slice_, resize or subset parameters will change the shape of the output.

target : numpy array of shape (2200,). Shape depends on subset.
    Labels associated to each pair of images. The two label values being different persons or the same person.

DESCR : string
    Description of the Labeled Faces in the Wild (LFW) dataset.

sklearn.datasets.fetch_lfw_people

sklearn.datasets.fetch_lfw_people(data_home=None, funneled=True, resize=0.5, min_faces_per_person=0, color=False, slice_=(slice(70, 195, None), slice(78, 172, None)), download_if_missing=True)

Loader for the Labeled Faces in the Wild (LFW) people dataset

This dataset is a collection of JPEG pictures of famous people collected on the internet, all details are available on the official website:

http://vis-www.cs.umass.edu/lfw/

Each picture is centered on a single face. Each pixel of each channel (color in RGB) is encoded by a float in range 0.0 - 1.0.
The task is called Face Recognition (or Identification): given the picture of a face, find the name of the person given a training set (gallery).

The original images are 250 x 250 pixels, but the default slice and resize arguments reduce them to 62 x 47.

**Parameters**

- **data_home**: optional, default: None
  Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in '~/scikit_learn_data' subfolders.

- **funneled**: boolean, optional, default: True
  Download and use the funneled variant of the dataset.

- **resize**: float, optional, default 0.5
  Ratio used to resize the each face picture.

- **min_faces_per_person**: int, optional, default None
  The extracted dataset will only retain pictures of people that have at least min_faces_per_person different pictures.

- **color**: boolean, optional, default False
  Keep the 3 RGB channels instead of averaging them to a single gray level channel. If color is True the shape of the data has one more dimension than the shape with color = False.

- **slice_**: optional
  Provide a custom 2D slice (height, width) to extract the ‘interesting’ part of the jpeg files and avoid use statistical correlation from the background

- **download_if_missing**: optional, True by default
  If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**Returns**

- **dataset**: dict-like object with the following attributes:
  - **dataset.data**: numpy array of shape (13233, 2914)
    Each row corresponds to a ravelled face image of original size 62 x 47 pixels. Changing the slice_ or resize parameters will change the shape of the output.
  - **dataset.images**: numpy array of shape (13233, 62, 47)
    Each row is a face image corresponding to one of the 5749 people in the dataset. Changing the slice_ or resize parameters will change the shape of the output.
  - **dataset.target**: numpy array of shape (13233,)
    Labels associated to each face image. Those labels range from 0-5748 and correspond to the person IDs.
  - **dataset.DESCR**: string
    Description of the Labeled Faces in the Wild (LFW) dataset.

**Examples using sklearn.datasets.fetch_lfw_people**

- *Faces recognition example using eigenfaces and SVMs*
Fetch an mldata.org data set

If the file does not exist yet, it is downloaded from mldata.org. 
mldata.org does not have an enforced convention for storing data or naming the columns in a data set. The default behavior of this function works well with the most common cases:

1. data values are stored in the column ‘data’, and target values in the column ‘label’
2. alternatively, the first column stores target values, and the second data values
3. the data array is stored as $n_{features} \times n_{samples}$, and thus needs to be transposed to match the scikit-learn standard

Keyword arguments allow to adapt these defaults to specific data sets (see parameters target_name, data_name, transpose_data, and the examples below).

mldata.org data sets may have multiple columns, which are stored in the Bunch object with their original name.

**Parameters**

dataname : str
    Name of the data set on mldata.org, e.g.: “leukemia”, “Whistler Daily Snowfall”, etc. The raw name is automatically converted to a mldata.org URL.

target_name : optional, default: ‘label’
    Name or index of the column containing the target values.

data_name : optional, default: ‘data’
    Name or index of the column containing the data.

transpose_data : optional, default: True
    If True, transpose the downloaded data array.

data_home : optional, default: None
    Specify another download and cache folder for the data sets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.

**Returns**

data : Bunch
    Dictionary-like object, the interesting attributes are: ‘data’, the data to learn, ‘target’, the classification labels, ‘DESCR’, the full description of the dataset, and ‘COL_NAMES’, the original names of the dataset columns.

**Examples**

Load the ‘iris’ dataset from mldata.org:

```python
>>> from sklearn.datasets.mldata import fetch_mldata
>>> import tempfile
>>> test_data_home = tempfile.mkdtemp()

>>> iris = fetch_mldata('iris', data_home=test_data_home)
>>> iris.target.shape
(150,)
```
>>> iris.data.shape
(150, 4)

Load the ‘leukemia’ dataset from mldata.org, which needs to be transposed to respects the scikit-learn axes convention:

```python
>>> leukemia = fetch_mldata('leukemia', transpose_data=True,
                          data_home=test_data_home)
>>> leukemia.data.shape
(72, 7129)
```

Load an alternative ‘iris’ dataset, which has different names for the columns:

```python
>>> iris2 = fetch_mldata('datasets-UCI iris', target_name=1,
                        data_name=0, data_home=test_data_home)
>>> iris3 = fetch_mldata('datasets-UCI iris',
                        target_name='class', data_name='double0',
                        data_home=test_data_home)
```

```python
>>> import shutil
>>> shutil.rmtree(test_data_home)
```

Examples using `sklearn.datasets.fetch_mldata`

- Gaussian process regression (GPR) on Mauna Loa CO2 data.
- MNIST classification using multinomial logistic + L1
- Classifier Chain
- Visualization of MLP weights on MNIST

`sklearn.datasets.fetch_olivetti_faces`

`sklearn.datasets.fetch_olivetti_faces(data_home=None, shuffle=False, random_state=0, download_if_missing=True)`

Loader for the Olivetti faces data-set from AT&T.

Read more in the User Guide.

**Parameters**

- `data_home`: optional, default: None
  
  Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/.scikit_learn_data’ subfolders.

- `shuffle`: boolean, optional
  
  If True the order of the dataset is shuffled to avoid having images of the same person grouped.

- `random_state`: int, RandomState instance or None, optional (default=0)
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

- `download_if_missing`: optional, True by default

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If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**Returns** An object with the following attributes:

- `data`: numpy array of shape (400, 4096)
  Each row corresponds to a ravelled face image of original size 64 x 64 pixels.
- `images`: numpy array of shape (400, 64, 64)
  Each row is a face image corresponding to one of the 40 subjects of the dataset.
- `target`: numpy array of shape (400, )
  Labels associated to each face image. Those labels are ranging from 0-39 and correspond to the Subject IDs.

- `DESCR`: string
  Description of the modified Olivetti Faces Dataset.

**Notes**

This dataset consists of 10 pictures each of 40 individuals. The original database was available from (now defunct)

http://www.cl.cam.ac.uk/research/dtg/attarchive/facedatabase.html

The version retrieved here comes in MATLAB format from the personal web page of Sam Roweis:

http://www.cs.nyu.edu/~roweis/

Examples using `sklearn.datasets.fetch_olivetti_faces`

- Face completion with a multi-output estimators
- Online learning of a dictionary of parts of faces
- Faces dataset decompositions
- Pixel importances with a parallel forest of trees

`sklearn.datasets.fetch_rcv1`

`sklearn.datasets.fetch_rcv1(data_home=None, subset='all', download_if_missing=True, random_state=None, shuffle=False)`

Load the RCV1 multilabel dataset, downloading it if necessary.

Version: RCV1-v2, vectors, full sets, topics multilabels.

<table>
<thead>
<tr>
<th>Classes</th>
<th>103</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>804414</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>47236</td>
</tr>
<tr>
<td>Features</td>
<td>real, between 0 and 1</td>
</tr>
</tbody>
</table>

Read more in the User Guide.

New in version 0.17.
Parameters  

**data_home**: string, optional

Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.

**subset**: string, ‘train’, ‘test’, or ‘all’, default=’all’

Select the dataset to load: ‘train’ for the training set (23149 samples), ‘test’ for the test set (781265 samples), ‘all’ for both, with the training samples first if shuffle is False. This follows the official LYRL2004 chronological split.

**download_if_missing**: boolean, default=True

If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

**random_state**: int, RandomState instance or None, optional (default=None)

Random state for shuffling the dataset. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**shuffle**: bool, default=False

Whether to shuffle dataset.

Returns  

**dataset**: dict-like object with the following attributes:

**dataset.data**: scipy csr array, dtype np.float64, shape (804414, 47236)

The array has 0.16% of non zero values.

**dataset.target**: scipy csr array, dtype np.uint8, shape (804414, 103)

Each sample has a value of 1 in its categories, and 0 in others. The array has 3.15% of non zero values.

**dataset.sample_id**: numpy array, dtype np.uint32, shape (804414,)

Identification number of each sample, as ordered in dataset.data.

**dataset.target_names**: numpy array, dtype object, length (103)

Names of each target (RCV1 topics), as ordered in dataset.target.

**dataset.DESCR**: string

Description of the RCV1 dataset.

References


sklearn.datasets.fetch_species_distributions

```
sklearn.datasets.fetch_species_distributions(data_home=None, download_if_missing=True)
```

Loader for species distribution dataset from Phillips et. al. (2006)

Read more in the User Guide.
Parameters data_home : optional, default: None

Specify another download and cache folder for the datasets. By default all scikit-learn data is stored in ‘~/scikit_learn_data’ subfolders.

download_if_missing : optional, True by default

If False, raise a IOError if the data is not locally available instead of trying to download the data from the source site.

Returns The data is returned as a Bunch object with the following attributes:

coverages : array, shape = [14, 1592, 1212]

These represent the 14 features measured at each point of the map grid. The latitude/longitude values for the grid are discussed below. Missing data is represented by the value -9999.

train : record array, shape = (1623,)

The training points for the data. Each point has three fields:

• train[‘species’] is the species name
• train[‘dd long’] is the longitude, in degrees
• train[‘dd lat’] is the latitude, in degrees

test : record array, shape = (619,)

The test points for the data. Same format as the training data.

Nx, Ny : integers

The number of longitudes (x) and latitudes (y) in the grid

x_left_lower_corner, y_left_lower_corner : floats

The (x,y) position of the lower-left corner, in degrees

grid_size : float

The spacing between points of the grid, in degrees

Notes

This dataset represents the geographic distribution of species. The dataset is provided by Phillips et. al. (2006).

The two species are:

• “Bradypus variegatus”, the Brown-throated Sloth.
• “Microryzomys minutus”, also known as the Forest Small Rice Rat, a rodent that lives in Peru, Colombia, Ecuador, Peru, and Venezuela.
• For an example of using this dataset with scikit-learn, see examples/applications/plot_species_distribution_modeling.py.

References

Examples using `sklearn.datasets.fetch_species_distributions`

- *Species distribution modeling*
- *Kernel Density Estimate of Species Distributions*

### sklearn.datasets.get_data_home

`sklearn.datasets.get_data_home(data_home=None)`

Return the path of the scikit-learn data dir.

This folder is used by some large dataset loaders to avoid downloading the data several times.

By default the data dir is set to a folder named ‘scikit_learn_data’ in the user home folder.

Alternatively, it can be set by the ‘SCIKIT_LEARN_DATA’ environment variable or programmatically by giving an explicit folder path. The ‘~’ symbol is expanded to the user home folder.

If the folder does not already exist, it is automatically created.

**Parameters**

- **data_home**: str | None
  - The path to scikit-learn data dir.

Examples using `sklearn.datasets.get_data_home`

- *Out-of-core classification of text documents*

### sklearn.datasets.load_boston

`sklearn.datasets.load_boston(return_X_y=False)`

Load and return the boston house-prices dataset (regression).

| Samples total | 506 |
| Dimensionality | 13 |
| Features       | real, positive |
| Targets        | real 5. - 50. |

**Parameters**

- **return_X_y**: boolean, default=False.
  - If True, returns `(data, target)` instead of a Bunch object. See below for more information about the `data` and `target` object.

**New in version 0.18.**

**Returns**

- **data**: Bunch
  - Dictionary-like object, the interesting attributes are: ‘data’, the data to learn, ‘target’, the regression targets, and ‘DESCR’, the full description of the dataset.

- **(data, target)**: tuple if `return_X_y` is True
  - New in version 0.18.
Examples

```python
>>> from sklearn.datasets import load_boston
>>> boston = load_boston()
>>> print(boston.data.shape)
(506, 13)
```

Examples using `sklearn.datasets.load_boston`

- Plotting Cross-Validated Predictions
- Imputing missing values before building an estimator
- Outlier detection on a real data set
- Model Complexity Influence
- Gradient Boosting regression
- Feature selection using SelectFromModel and LassoCV

`sklearn.datasets.load_breast_cancer`

`sklearn.datasets.load_breast_cancer(return_X_y=False)`

Load and return the breast cancer wisconsin dataset (classification).

The breast cancer dataset is a classic and very easy binary classification dataset.

<table>
<thead>
<tr>
<th>Classes</th>
<th>2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples per class</td>
<td>212(M), 357(B)</td>
</tr>
<tr>
<td>Samples total</td>
<td>569</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>30</td>
</tr>
<tr>
<td>Features</td>
<td>real, positive</td>
</tr>
</tbody>
</table>

**Parameters**

`return_X_y : boolean, default=False`

If True, returns `(data, target)` instead of a Bunch object. See below for more information about the `data` and `target` object.

New in version 0.18.

**Returns**

`data : Bunch`

Dictionary-like object, the interesting attributes are: ‘data’, the data to learn, ‘target’, the classification labels, ‘target_names’, the meaning of the labels, ‘feature_names’, the meaning of the features, and ‘DESCR’, the full description of the dataset.

`data, target : tuple if return_X_y is True`

New in version 0.18.

The copy of UCI ML Breast Cancer Wisconsin (Diagnostic) dataset is downloaded from:

https://goo.gl/U2Uwz2
Examples

Let’s say you are interested in the samples 10, 50, and 85, and want to know their class name.

```python
>>> from sklearn.datasets import load_breast_cancer
>>> data = load_breast_cancer()
>>> data.target[[10, 50, 85]]
array([0, 1, 0])
>>> list(data.target_names)
['malignant', 'benign']
```

`sklearn.datasets.load_diabetes`

`sklearn.datasets.load_diabetes (return_X_y=False)`

Load and return the diabetes dataset (regression).

<table>
<thead>
<tr>
<th>Parameters</th>
<th>Description</th>
</tr>
</thead>
</table>
| `return_X_y` | boolean, default=False.  
If True, returns `(data, target)` instead of a Bunch object. See below for more information about the `data` and `target` object.  
New in version 0.18. |

<table>
<thead>
<tr>
<th>Returns</th>
<th>Description</th>
</tr>
</thead>
</table>
| `data` | Bunch  
Dictionary-like object, the interesting attributes are: 'data', the data to learn and 'target', the regression target for each sample.  
New in version 0.18. |
| `(data, target)` | tuple if `return_X_y` is True |

Examples using `sklearn.datasets.load_diabetes`

- Cross-validation on diabetes Dataset Exercise
- Lasso path using LARS
- Linear Regression Example
- Sparsity Example: Fitting only features 1 and 2
- Lasso and Elastic Net
- Lasso model selection: Cross-Validation / AIC / BIC
sklearn.datasets.load_digits

sklearn.datasets.load_digits(n_class=10, return_X_y=False)
Load and return the digits dataset (classification).

Each datapoint is a 8x8 image of a digit.

<table>
<thead>
<tr>
<th>Classes</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples per class</td>
<td>~180</td>
</tr>
<tr>
<td>Samples total</td>
<td>1797</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>64</td>
</tr>
<tr>
<td>Features</td>
<td>integers 0-16</td>
</tr>
</tbody>
</table>

Read more in the User Guide.

**Parameters n_class**: integer, between 0 and 10, optional (default=10)
The number of classes to return.

**return_X_y**: boolean, default=False.
If True, returns (data, target) instead of a Bunch object. See below for more information about the data and target object.
New in version 0.18.

**Returns data**: Bunch
Dictionary-like object, the interesting attributes are: ‘data’, the data to learn, ‘images’, the images corresponding to each sample, ‘target’, the classification labels for each sample, ‘target_names’, the meaning of the labels, and ‘DESCR’, the full description of the dataset.

**(data, target)**: tuple if return_X_y is True
New in version 0.18.

This is a copy of the test set of the UCI ML hand-written digits datasets

**Examples**

To load the data and visualize the images:

```python
>>> from sklearn.datasets import load_digits
>>> digits = load_digits()
>>> print(digits.data.shape)
(1797, 64)
>>> import matplotlib.pyplot as plt
>>> plt.gray()
>>> plt.matshow(digits.images[0])
>>> plt.show()
```

**Examples using sklearn.datasets.load_digits**

- **Pipelining: chaining a PCA and a logistic regression**
• Selecting dimensionality reduction with Pipeline and GridSearchCV
• The Johnson-Lindenstrauss bound for embedding with random projections
• Explicit feature map approximation for RBF kernels
• Recognizing hand-written digits
• Feature agglomeration
• Various Agglomerative Clustering on a 2D embedding of digits
• A demo of K-Means clustering on the handwritten digits data
• The Digit Dataset
• Early stopping of Gradient Boosting
• Digits Classification Exercise
• Cross-validation on Digits Dataset Exercise
• Recursive feature elimination
• Comparing various online solvers
• L1 Penalty and Sparsity in Logistic Regression
• Manifold learning on handwritten digits: Locally Linear Embedding, Isomap…
• Plotting Validation Curves
• Parameter estimation using grid search with cross-validation
• Comparing randomized search and grid search for hyperparameter estimation
• Plotting Learning Curves
• Kernel Density Estimation
• Compare Stochastic learning strategies for MLPClassifier
• Restricted Boltzmann Machine features for digit classification
• Label Propagation digits: Demonstrating performance
• Label Propagation digits active learning
• SVM-Anova: SVM with univariate feature selection

sklearn.datasets.load_files

`sklearn.datasets.load_files(container_path, description=None, categories=None, load_content=True, shuffle=True, encoding=None, decode_error='strict', random_state=0)`

Load text files with categories as subfolder names.

Individual samples are assumed to be files stored a two levels folder structure such as the following:

```
  container_folder/
    category_1_folder/  file_1.txt file_2.txt ... file_42.txt
    category_2_folder/  file_43.txt file_44.txt ...
```
The folder names are used as supervised signal label names. The individual file names are not important.

This function does not try to extract features into a numpy array or scipy sparse matrix. In addition, if load_content is false it does not try to load the files in memory.

To use text files in a scikit-learn classification or clustering algorithm, you will need to use the `sklearn.feature_extraction.text` module to build a feature extraction transformer that suits your problem.

If you set load_content=True, you should also specify the encoding of the text using the ‘encoding’ parameter. For many modern text files, ‘utf-8’ will be the correct encoding. If you leave encoding equal to None, then the content will be made of bytes instead of Unicode, and you will not be able to use most functions in `sklearn.feature_extraction.text`.

Similar feature extractors should be built for other kind of unstructured data input such as images, audio, video, ...

Read more in the User Guide.

Parameters

**container_path** : string or unicode

Path to the main folder holding one subfolder per category

**description** : string or unicode, optional (default=None)

A paragraph describing the characteristic of the dataset: its source, reference, etc.

**categories** : A collection of strings or None, optional (default=None)

If None (default), load all the categories. If not None, list of category names to load (other categories ignored).

**load_content** : boolean, optional (default=True)

Whether to load or not the content of the different files. If true a ‘data’ attribute containing the text information is present in the data structure returned. If not, a filenames attribute gives the path to the files.

**shuffle** : bool, optional (default=True)

Whether or not to shuffle the data: might be important for models that make the assumption that the samples are independent and identically distributed (i.i.d.), such as stochastic gradient descent.

**encoding** : string or None (default is None)

If None, do not try to decode the content of the files (e.g. for images or other non-text content). If not None, encoding to use to decode text files to Unicode if load_content is True.

**decode_error** : {'strict', 'ignore', 'replace'}, optional

Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. Passed as keyword argument ‘errors’ to bytes.decode.

**random_state** : int, RandomState instance or None, optional (default=0)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns **data** : Bunch

Dictionary-like object, the interesting attributes are: either data, the raw text data to learn, or ‘filenames’, the files holding it, ‘target’, the classification labels (integer index),
`target_names`, the meaning of the labels, and `DESCR`, the full description of the dataset.

**`sklearn.datasets.load_iris`**

`sklearn.datasets.load_iris(return_X_y=False)`  
Load and return the iris dataset (classification).

The iris dataset is a classic and very easy multi-class classification dataset.

<table>
<thead>
<tr>
<th>Classes</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples per class</td>
<td>50</td>
</tr>
<tr>
<td>Samples total</td>
<td>150</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>4</td>
</tr>
<tr>
<td>Features</td>
<td>real, positive</td>
</tr>
</tbody>
</table>

Read more in the *User Guide*.

**Parameters**  
`return_X_y`: boolean, default=False.  
If True, returns `(data, target)` instead of a Bunch object. See below for more information about the `data` and `target` object.

New in version 0.18.

**Returns**  
`data`: Bunch  
Dictionary-like object, the interesting attributes are: `data`, the data to learn, `target`, the classification labels, `target_names`, the meaning of the labels, `feature_names`, the meaning of the features, and `DESCR`, the full description of the dataset.

`(data, target)`: tuple if `return_X_y` is True  
New in version 0.18.

**Examples**

Let’s say you are interested in the samples 10, 25, and 50, and want to know their class name.

```python
>>> from sklearn.datasets import load_iris
>>> data = load_iris()
>>> data.target[[10, 25, 50]]
array([0, 0, 1])
>>> list(data.target_names)
['setosa', 'versicolor', 'virginica']
```

**Examples using `sklearn.datasets.load_iris`**

- Concatenating multiple feature extraction methods
- Plot classification probability
- K-means Clustering
- The Iris Dataset
- PCA example with Iris Data-set
scikit-learn user guide, Release 0.20.dev0

- Incremental PCA
- Comparison of LDA and PCA 2D projection of Iris dataset
- Plot the decision boundaries of a VotingClassifier
- Early stopping of Gradient Boosting
- Plot the decision surfaces of ensembles of trees on the iris dataset
- SVM Exercise
- Test with permutations the significance of a classification score
- Univariate Feature Selection
- Gaussian process classification (GPC) on iris dataset
- Path with L1- Logistic Regression
- Logistic Regression 3-class Classifier
- Plot multi-class SGD on the iris dataset
- GMM covariances
- Receiver Operating Characteristic (ROC) with cross validation
- Confusion matrix
- Nested versus non-nested cross-validation
- Receiver Operating Characteristic (ROC)
- Precision-Recall
- Nearest Neighbors Classification
- Nearest Centroid Classification
- Compare Stochastic learning strategies for MLPClassifier
- Decision boundary of label propagation versus SVM on the Iris dataset
- SVM with custom kernel
- Plot different SVM classifiers in the iris dataset
- RBF SVM parameters
- Plot the decision surface of a decision tree on the iris dataset
- Understanding the decision tree structure

sklearn.datasets.load_linnerud

sklearn.datasets.load_linnerud(return_X_y=False)
Load and return the linnerud dataset (multivariate regression).

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples total</td>
<td>20</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>3 (for both data and target)</td>
</tr>
<tr>
<td>Features</td>
<td>integer</td>
</tr>
<tr>
<td>Targets</td>
<td>integer</td>
</tr>
</tbody>
</table>

Parameters return_X_y : boolean, default=False.
If True, returns \((data, target)\) instead of a Bunch object. See below for more information about the \(data\) and \(target\) object.

New in version 0.18.

**Returns**

**data** : Bunch

Dictionary-like object, the interesting attributes are: ‘data’ and ‘targets’, the two multivariate datasets, with ‘data’ corresponding to the exercise and ‘targets’ corresponding to the physiological measurements, as well as ‘feature_names’ and ‘target_names’.

\((data, target)\) : tuple if \(return_X_y\) is True

New in version 0.18.

### sklearn.datasets.load_mlcomp

**sklearn.datasets.load_mlcomp**

**sklearn.datasets.load_mlcomp**(*name_or_id*, *set_*= 'raw', *mlcomp_root=None*, **kwargs)

DEPRECATED: since the http://mlcomp.org/ website will shut down in March 2017, the load_mlcomp function was deprecated in version 0.19 and will be removed in 0.21.

Load a datasets as downloaded from http://mlcomp.org

**Parameters**

- **name_or_id** : the integer id or the string name metadata of the MLComp dataset to load
- **set_** : select the portion to load: ‘train’, ‘test’ or ‘raw’
- **mlcomp_root** [the filesystem path to the root folder where MLComp datasets] are stored, if mlcomp_root is None, the MLCOMP_DATASETS_HOME environment variable is looked up instead.

**kwargs** : domain specific kwargs to be passed to the dataset loader.

Read more in the User Guide.

**Returns**

**data** : Bunch

Dictionary-like object, the interesting attributes are: ‘filenames’, the files holding the raw to learn, ‘target’, the classification labels (integer index), ‘target_names’, the meaning of the labels, and ‘DESCR’, the full description of the dataset.

Note on the lookup process: depending on the type of name_or_id, will choose between integer id lookup or metadata name lookup by looking at the unzipped archives and metadata file.

TODO: implement zip dataset loading too

### sklearn.datasets.load_sample_image

**sklearn.datasets.load_sample_image**(*image_name*)

Load the numpy array of a single sample image

**Parameters**

- **image_name** : \{'china.jpg', 'flower.jpg'\}  
  The name of the sample image loaded

**Returns**

**img** : 3D array

The image as a numpy array: height x width x color
Examples

```python
>>> from sklearn.datasets import load_sample_image
>>> china = load_sample_image('china.jpg')
>>> china.dtype
dtype('uint8')
>>> china.shape
(427, 640, 3)
>>> flower = load_sample_image('flower.jpg')
>>> flower.dtype
dtype('uint8')
>>> flower.shape
(427, 640, 3)
```

Examples using `sklearn.datasets.load_sample_image`

- *Color Quantization using K-Means*

`sklearn.datasets.load_sample_images`

`sklearn.datasets.load_sample_images()`
Load sample images for image manipulation.

Loads both, `china` and `flower`.

Returns `data`: Bunch

Dictionary-like object with the following attributes: `'images'`, the two sample images, `'filenames'`, the file names for the images, and `'DESCR'` the full description of the dataset.

Examples

To load the data and visualize the images:

```python
>>> from sklearn.datasets import load_sample_images
>>> dataset = load_sample_images()
>>> len(dataset.images)
2
>>> first_img_data = dataset.images[0]
>>> first_img_data.shape
(427, 640, 3)
```

`sklearn.datasets.load_svmlight_file`

`sklearn.datasets.load_svmlight_file(f, n_features=None, dtype=<class 'numpy.float64'>, multilabel=False, zero_based='auto', query_id=False, offset=0, length=-1)`

Load datasets in the svmlight / libsvm format into sparse CSR matrix
This format is a text-based format, with one sample per line. It does not store zero valued features hence is suitable for sparse dataset.

The first element of each line can be used to store a target variable to predict.

This format is used as the default format for both svmlight and the libsvm command line programs.

Parsing a text based source can be expensive. When working on repeatedly on the same dataset, it is recommended to wrap this loader with joblib.Memory.cache to store a memmapped backup of the CSR results of the first call and benefit from the near instantaneous loading of memmapped structures for the subsequent calls.

In case the file contains a pairwise preference constraint (known as “qid” in the svmlight format) these are ignored unless the query_id parameter is set to True. These pairwise preference constraints can be used to constraint the combination of samples when using pairwise loss functions (as is the case in some learning to rank problems) so that only pairs with the same query_id value are considered.

This implementation is written in Cython and is reasonably fast. However, a faster API-compatible loader is also available at:

https://github.com/mblondel/svmlight-loader

**Parameters**

```python
f : {str, file-like, int}
```

(Path to) a file to load. If a path ends in “.gz” or “.bz2”, it will be uncompressed on the fly. If an integer is passed, it is assumed to be a file descriptor. A file-like or file descriptor will not be closed by this function. A file-like object must be opened in binary mode.

```python
n_features : int or None
```

The number of features to use. If None, it will be inferred. This argument is useful to load several files that are subsets of a bigger sliced dataset: each subset might not have examples of every feature, hence the inferred shape might vary from one slice to another. `n_features` is only required if `offset` or `length` are passed a non-default value.

```python
dtype : numpy data type, default np.float64
```

Data type of dataset to be loaded. This will be the data type of the output numpy arrays X and y.

```python
multilabel : boolean, optional, default False
```

Samples may have several labels each (see http://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)

```python
zero_based : boolean or “auto”, optional, default “auto”
```

Whether column indices in f are zero-based (True) or one-based (False). If column indices are one-based, they are transformed to zero-based to match Python/NumPy conventions. If set to “auto”, a heuristic check is applied to determine this from the file contents. Both kinds of files occur “in the wild”, but they are unfortunately not self-identifying. Using “auto” or True should always be safe when no offset or length is passed. If offset or length are passed, the “auto” mode falls back to zero_based=True to avoid having the heuristic check yield inconsistent results on different segments of the file.

```python
query_id : boolean, default False
```

If True, will return the query_id array for each file.

```python
offset : integer, optional, default 0
```
Ignore the offset first bytes by seeking forward, then discarding the following bytes up until the next new line character.

**length** : integer, optional, default -1

If strictly positive, stop reading any new line of data once the position in the file has reached the (offset + length) bytes threshold.

**Returns**

- **X** : scipy.sparse matrix of shape (n_samples, n_features)
- **y** : ndarray of shape (n_samples,), or, in the multilabel a list of tuples of length n_samples.
- **query_id** : array of shape (n_samples,)

query_id for each sample. Only returned when query_id is set to True.

**See also:**

- **load_svmlight_files** similar function for loading multiple files in this format.

**Examples**

To use joblib.Memory to cache the svmlight file:

```python
from sklearn.externals.joblib import Memory
from sklearn.datasets import load_svmlight_file
mem = Memory("./mycache")

@mem.cache
def get_data():
    data = load_svmlight_file("mysvmlightfile")
    return data[0], data[1]

X, y = get_data()
```

**sklearn.datasets.load_svmlight_files**

This function is equivalent to mapping load_svmlight_file over a list of files, except that the results are concatenated into a single, flat list and the samples vectors are constrained to all have the same number of features.

In case the file contains a pairwise preference constraint (known as “qid” in the svmlight format) these are ignored unless the query_id parameter is set to True. These pairwise preference constraints can be used to constraint the combination of samples when using pairwise loss functions (as is the case in some learning to rank problems) so that only pairs with the same query_id value are considered.

**Parameters**

- **files** : iterable over {str, file-like, int}
Paths of) files to load. If a path ends in ".gz" or ".bz2", it will be uncompressed on the fly. If an integer is passed, it is assumed to be a file descriptor. File-likes and file descriptors will not be closed by this function. File-like objects must be opened in binary mode.

**n_features**: int or None

The number of features to use. If None, it will be inferred from the maximum column index occurring in any of the files.

This can be set to a higher value than the actual number of features in any of the input files, but setting it to a lower value will cause an exception to be raised.

**dtype**: numpy data type, default np.float64

Data type of dataset to be loaded. This will be the data type of the output numpy arrays \( X \) and \( y \).

**multilabel**: boolean, optional

Samples may have several labels each (see http://www.csie.ntu.edu.tw/~cjlin/libsvmtools/datasets/multilabel.html)

**zero_based**: boolean or "auto", optional

Whether column indices in \( f \) are zero-based (True) or one-based (False). If column indices are one-based, they are transformed to zero-based to match Python/NumPy conventions. If set to "auto", a heuristic check is applied to determine this from the file contents. Both kinds of files occur “in the wild”, but they are unfortunately not self-identifying. Using “auto” or True should always be safe when no offset or length is passed. If offset or length are passed, the “auto” mode falls back to zero_based=True to avoid having the heuristic check yield inconsistent results on different segments of the file.

**query_id**: boolean, defaults to False

If True, will return the query_id array for each file.

**offset**: integer, optional, default 0

Ignore the offset first bytes by seeking forward, then discarding the following bytes up until the next new line character.

**length**: integer, optional, default -1

If strictly positive, stop reading any new line of data once the position in the file has reached the (offset + length) bytes threshold.

**Returns**

\([X_1, y_1, \ldots, X_n, y_n]\)

where each (\(X_i, y_i\)) pair is the result from \(\text{load_svmlight_file}(\text{files}[i])\).

If query_id is set to True, this will return instead \([X_1, y_1, q_1, \ldots, X_n, y_n, q_n]\) where (\(X_i, y_i, q_i\)) is the result from \(\text{load_svmlight_file}(\text{files}[i])\)

**See also:**

\(\text{load_svmlight_file}\)
Notes

When fitting a model to a matrix $X_{\text{train}}$ and evaluating it against a matrix $X_{\text{test}}$, it is essential that $X_{\text{train}}$ and $X_{\text{test}}$ have the same number of features ($X_{\text{train}}.\text{shape}[1] == X_{\text{test}}.\text{shape}[1]$). This may not be the case if you load the files individually with load_svmlight_file.

**sklearn.datasets.load_wine**

`sklearn.datasets.load_wine(return_X_y=False)`

Load and return the wine dataset (classification).

New in version 0.18.

The wine dataset is a classic and very easy multi-class classification dataset.

<table>
<thead>
<tr>
<th>Classes</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Samples per class</td>
<td>[59, 71, 48]</td>
</tr>
<tr>
<td>Samples total</td>
<td>178</td>
</tr>
<tr>
<td>Dimensionality</td>
<td>13</td>
</tr>
<tr>
<td>Features</td>
<td>real, positive</td>
</tr>
</tbody>
</table>

Read more in the *User Guide*.

**Parameters**

`return_X_y : boolean, default=False.`

If True, returns `(data, target)` instead of a Bunch object. See below for more information about the `data` and `target` object.

**Returns**

`data : Bunch`

Dictionary-like object, the interesting attributes are: `data`, the data to learn, `target`, the classification labels, `target_names`, the meaning of the labels, `feature_names`, the meaning of the features, and `DESCR`, the full description of the dataset.

`(data, target) : tuple if return_X_y is True`

The copy of UCI ML Wine Data Set dataset is downloaded and modified to fit standard format from:


**Examples**

Let’s say you are interested in the samples 10, 80, and 140, and want to know their class name.

```python
>>> from sklearn.datasets import load_wine
>>> data = load_wine()
>>> data.target[[10, 80, 140]]
array([0, 1, 2])
>>> list(data.target_names)
['class_0', 'class_1', 'class_2']
```

**Examples using sklearn.datasets.load_wine**

- *Importance of Feature Scaling*
**sklearn.datasets.mldata_filename**

sklearn.datasets.mldata_filename(dataname)

Convert a raw name for a data set in a mldata.org filename.

**Parameters**

- dataname : str
  Name of dataset

**Returns**

- fname : str
  The converted dataname.

### 30.7.2 Samples generator

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>datasets.make_biclusters(shape, n_clusters)</td>
<td>Generate an array with constant block diagonal structure for biclustering.</td>
</tr>
<tr>
<td>datasets.make_blobs([n_samples, n_features, ...])</td>
<td>Generate isotropic Gaussian blobes for clustering.</td>
</tr>
<tr>
<td>datasets.make_checkerboard(shape, n_clusters)</td>
<td>Generate an array with block checkerboard structure for biclustering.</td>
</tr>
<tr>
<td>datasets.make_circles([n_samples, shuffle, ...])</td>
<td>Make a large circle containing a smaller circle in 2d.</td>
</tr>
<tr>
<td>datasets.make_classification([n_samples, ...])</td>
<td>Generate a random n-class classification problem.</td>
</tr>
<tr>
<td>datasets.make_friedman1([n_samples, ...])</td>
<td>Generate the “Friedman #1” regression problem</td>
</tr>
<tr>
<td>datasets.make_friedman2([n_samples, noise, ...])</td>
<td>Generate the “Friedman #2” regression problem</td>
</tr>
<tr>
<td>datasets.make_friedman3([n_samples, noise, ...])</td>
<td>Generate the “Friedman #3” regression problem</td>
</tr>
<tr>
<td>datasets.make_gaussian_quantiles([mean, ...])</td>
<td>Generate isotropic Gaussian and label samples by quantile</td>
</tr>
<tr>
<td>datasets.make_hastie_10_2([n_samples, ...])</td>
<td>Generates data for binary classification used in Hastie et al.</td>
</tr>
<tr>
<td>datasets.make_low_rank_matrix([n_samples, ...])</td>
<td>Generate a mostly low rank matrix with bell-shaped singular values</td>
</tr>
<tr>
<td>datasets.make_moons([n_samples, shuffle, ...])</td>
<td>Make two interleaving half circles</td>
</tr>
<tr>
<td>datasets.make_multilabel_classification([...])</td>
<td>Generate a random multilabel classification problem.</td>
</tr>
<tr>
<td>datasets.make_regression([n_samples, ...])</td>
<td>Generate a random regression problem.</td>
</tr>
<tr>
<td>datasets.make_s_curve([n_samples, noise, ...])</td>
<td>Generate an S curve dataset.</td>
</tr>
<tr>
<td>datasets.make_sparse_coded_signal(n_samples, ...))</td>
<td>Generate a signal as a sparse combination of dictionary elements.</td>
</tr>
<tr>
<td>datasets.make_sparse_spd_matrix([dim, ...])</td>
<td>Generate a sparse symmetric definite positive matrix.</td>
</tr>
<tr>
<td>datasets.make_sparse_uncorrelated([...])</td>
<td>Generate a random regression problem with sparse uncorrelated design</td>
</tr>
<tr>
<td>datasets.make_spd_matrix(n_dim, random_state)</td>
<td>Generate a random symmetric, positive-definite matrix.</td>
</tr>
<tr>
<td>datasets.make_swiss_roll([n_samples, noise, ...])</td>
<td>Generate a swiss roll dataset.</td>
</tr>
</tbody>
</table>

**sklearn.datasets.make_biclusters**

sklearn.datasets.make_biclusters(shape, n_clusters, noise=0.0, minval=10, maxval=100, shuffle=True, random_state=None)

Generate an array with constant block diagonal structure for biclustering.

Read more in the User Guide.
Parameters  **shape** : iterable (n_rows, n_cols)

The shape of the result.

**n_clusters** : integer

The number of biclusters.

**noise** : float, optional (default=0.0)

The standard deviation of the gaussian noise.

**minval** : int, optional (default=10)

Minimum value of a bicluster.

**maxval** : int, optional (default=100)

Maximum value of a bicluster.

**shuffle** : boolean, optional (default=True)

Shuffle the samples.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

Returns  **X** : array of shape **shape**

The generated array.

**rows** : array of shape (n_clusters, X.shape[0],)

The indicators for cluster membership of each row.

**cols** : array of shape (n_clusters, X.shape[1],)

The indicators for cluster membership of each column.

See also:

*make_checkerboard*

References

[R4545]

Examples using **sklearn.datasets.make_biclusters**

- A demo of the Spectral Co-Clustering algorithm

**sklearn.datasets.make_blobs**

**sklearn.datasets.make_blobs** *(n_samples=100, n_features=2, centers=3, cluster_std=1.0, center_box=(-10.0, 10.0), shuffle=True, random_state=None)*

Generate isotropic Gaussian blobs for clustering.

Read more in the **User Guide**.

**Parameters** **n_samples** : int, optional (default=100)
The total number of points equally divided among clusters.

**n_features** : int, optional (default=2)

The number of features for each sample.

**centers** : int or array of shape [n_centers, n_features], optional

(default=3) The number of centers to generate, or the fixed center locations.

**cluster_std** : float or sequence of floats, optional (default=1.0)

The standard deviation of the clusters.

**center_box** : pair of floats (min, max), optional (default=(-10.0, 10.0))

The bounding box for each cluster center when centers are generated at random.

**shuffle** : boolean, optional (default=True)

Shuffle the samples.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**Returns**

**X**: array of shape [n_samples, n_features]

The generated samples.

**y**: array of shape [n_samples]

The integer labels for cluster membership of each sample.

See also:

`make_classification` a more intricate variant

**Examples**

```python
>>> from sklearn.datasets.samples_generator import make_blobs
>>> X, y = make_blobs(n_samples=10, centers=3, n_features=2,
...                   random_state=0)
>>> print(X.shape)
(10, 2)
>>> y
array([0, 0, 1, 0, 2, 2, 2, 1, 1, 0])
```

**Examples using sklearn.datasets.make_blobs**

- Probability calibration of classifiers
- Probability Calibration for 3-class classification
- Normal and Shrinkage Linear Discriminant Analysis for classification
- A demo of the mean-shift clustering algorithm
- Demonstration of k-means assumptions
- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Compare BIRCH and MiniBatchKMeans
- Comparison of the K-Means and MiniBatchKMeans clustering algorithms
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- Comparing different clustering algorithms on toy datasets
- Plot randomly generated classification dataset
- SGD: Maximum margin separating hyperplane
- Plot multinomial and One-vs-Rest Logistic Regression
- SVM: Maximum margin separating hyperplane

**sklearn.datasets.make_checkerboard**

`sklearn.datasets.make_checkerboard(shape, n_clusters, noise=0.0, minval=10, maxval=100, shuffle=True, random_state=None)`

Generate an array with block checkerboard structure for biclustering.

Read more in the User Guide.

**Parameters**

- **shape**: iterable (n_rows, n_cols)
  - The shape of the result.

- **n_clusters**: integer or iterable (n_row_clusters, n_column_clusters)
  - The number of row and column clusters.

- **noise**: float, optional (default=0.0)
  - The standard deviation of the gaussian noise.

- **minval**: int, optional (default=10)
  - Minimum value of a bicluster.

- **maxval**: int, optional (default=100)
  - Maximum value of a bicluster.

- **shuffle**: boolean, optional (default=True)
  - Shuffle the samples.

- **random_state**: int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**Returns**

- **X**: array of shape `shape`
  - The generated array.

- **rows**: array of shape (n_clusters, X.shape[0],)
  - The indicators for cluster membership of each row.

- **cols**: array of shape (n_clusters, X.shape[1],)
  - The indicators for cluster membership of each column.
See also:

make_biclusters

References

[R4747]

Examples using sklearn.datasets.make_checkerboard

- A demo of the Spectral Biclustering algorithm

sklearn.datasets.make_circles

sklearn.datasets.make_circles(n_samples=100, shuffle=True, noise=None, random_state=None, factor=0.8)

Make a large circle containing a smaller circle in 2d.

A simple toy dataset to visualize clustering and classification algorithms.

Read more in the User Guide.

Parameters

n_samples : int, optional (default=100)
    The total number of points generated.

shuffle : bool, optional (default=True)
    Whether to shuffle the samples.

noise : double or None (default=None)
    Standard deviation of Gaussian noise added to the data.

random_state : int, RandomState instance or None, optional (default=None)
    If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

factor : double < 1 (default=.8)
    Scale factor between inner and outer circle.

Returns

X : array of shape [n_samples, 2]
    The generated samples.

y : array of shape [n_samples]
    The integer labels (0 or 1) for class membership of each sample.

Examples using sklearn.datasets.make_circles

- Classifier comparison
- Comparing different clustering algorithms on toy datasets
- Kernel PCA
sklearn.datasets.make_classification

Generate a random n-class classification problem.

This initially creates clusters of points normally distributed (std=1) about vertices of an \( n_{\text{informative}} \)-dimensional hypercube with sides of length \( 2*\text{class} \_\text{sep} \) and assigns an equal number of clusters to each class. It introduces interdependence between these features and adds various types of further noise to the data.

Prior to shuffling, \( X \) stacks a number of these primary “informative” features, “redundant” linear combinations of these, “repeated” duplicates of sampled features, and arbitrary noise for and remaining features.

Read more in the User Guide.

**Parameters**

- **n_samples**: int, optional (default=100)

  The number of samples.

- **n_features**: int, optional (default=20)

  The total number of features. These comprise \( n_{\text{informative}} \) informative features, \( n_{\text{redundant}} \) redundant features, \( n_{\text{repeated}} \) duplicated features and \( n_{\text{features}}-n_{\text{informative}}-n_{\text{redundant}}-n_{\text{repeated}} \) useless features drawn at random.

- **n_informative**: int, optional (default=2)

  The number of informative features. Each class is composed of a number of gaussian clusters each located around the vertices of a hypercube in a subspace of dimension \( n_{\text{informative}} \). For each cluster, informative features are drawn independently from \( \text{N}(0,1) \) and then randomly linearly combined within each cluster in order to add covariance. The clusters are then placed on the vertices of the hypercube.

- **n_redundant**: int, optional (default=2)

  The number of redundant features. These features are generated as random linear combinations of the informative features.

- **n_repeated**: int, optional (default=0)

  The number of duplicated features, drawn randomly from the informative and the redundant features.

- **n_classes**: int, optional (default=2)

  The number of classes (or labels) of the classification problem.

- **n_clusters_per_class**: int, optional (default=2)

  The number of clusters per class.
weights : list of floats or None (default=None)

The proportions of samples assigned to each class. If None, then classes are balanced.
Note that if len(weights) == n_classes - 1, then the last class weight is automatically
inferred. More than n_samples samples may be returned if the sum of weights exceeds
1.

flip_y : float, optional (default=0.01)

The fraction of samples whose class are randomly exchanged. Larger values introduce
noise in the labels and make the classification task harder.

class_sep : float, optional (default=1.0)

The factor multiplying the hypercube size. Larger values spread out the clusters/classes
and make the classification task easier.

hypercube : boolean, optional (default=True)

If True, the clusters are put on the vertices of a hypercube. If False, the clusters are put
on the vertices of a random polytope.

shift : float, array of shape [n_features] or None, optional (default=0.0)

Shift features by the specified value. If None, then features are shifted by a random
value drawn in [-class_sep, class_sep].

scale : float, array of shape [n_features] or None, optional (default=1.0)

Multiply features by the specified value. If None, then features are scaled by a random
value drawn in [1, 100]. Note that scaling happens after shifting.

shuffle : boolean, optional (default=True)

Shuffle the samples and the features.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState
instance, random_state is the random number generator; If None, the random number
generator is the RandomState instance used by np.random.

Returns X : array of shape [n_samples, n_features]

The generated samples.

y : array of shape [n_samples]

The integer labels for class membership of each sample.

See also:

make_blobs simplified variant

make_multilabel_classification unrelated generator for multilabel tasks

Notes

The algorithm is adapted from Guyon [1] and was designed to generate the “Madelon” dataset.
References

[R4949]

Examples using `sklearn.datasets.make_classification`

- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Classifier comparison
- Plot randomly generated classification dataset
- Feature importances with forests of trees
- OOB Errors for Random Forests
- Feature transformations with ensembles of trees
- Pipeline Anova SVM
- Recursive feature elimination with cross-validation
- Varying regularization in Multi-layer Perceptron
- Scaling the regularization parameter for SVCs

`sklearn.datasets.make_friedman1`

`sklearn.datasets.make_friedman1(n_samples=100, n_features=10, noise=0.0, random_state=None)`

Generate the “Friedman #1” regression problem

This dataset is described in Friedman [1] and Breiman [2].

Inputs $X$ are independent features uniformly distributed on the interval $[0, 1]$. The output $y$ is created according to the formula:

$$y(X) = 10 * \sin(\pi * X[:, 0] * X[:, 1]) + 20 * (X[:, 2] - 0.5)^2 + 10 * X[:, \rightarrow 3] + 5 * X[:, 4] + \text{noise} * \mathcal{N}(0, 1).$$

Out of the $n_{\text{features}}$ features, only 5 are actually used to compute $y$. The remaining features are independent of $y$.

The number of features has to be $\geq 5$.

Read more in the User Guide.

Parameters

- `n_samples` : int, optional (default=100)
  
  The number of samples.

- `n_features` : int, optional (default=10)
  
  The number of features. Should be at least 5.

- `noise` : float, optional (default=0.0)
  
  The standard deviation of the gaussian noise applied to the output.

- `random_state` : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns

**X**: array of shape [n_samples, n_features]

The input samples.

**y**: array of shape [n_samples]

The output values.

References

[R339340], [R340340]

sklearn.datasets.make_friedman2

**sklearn.datasets.make_friedman2** *(n_samples=100, noise=0.0, random_state=None)*

Generate the “Friedman #2” regression problem

This dataset is described in Friedman [1] and Breiman [2].

Inputs X are 4 independent features uniformly distributed on the intervals:

\[
0 \leq X[:, 0] \leq 100, \\
40 \times \pi \leq X[:, 1] \leq 560 \times \pi, \\
0 \leq X[:, 2] \leq 1, \\
1 \leq X[:, 3] \leq 11.
\]

The output y is created according to the formula:

\[
y(X) = (X[:, 0] ** 2 + (X[:, 1] * X[:, 2] - 1 / (X[:, 1] * X[:, 3])) ** 2) ** 0.5 + \text{noise} \times \text{N}(0, 1).
\]

Read more in the *User Guide*.

**Parameters**

- **n_samples**: int, optional (default=100)
  The number of samples.

- **noise**: float, optional (default=0.0)
  The standard deviation of the gaussian noise applied to the output.

- **random_state**: int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **X**: array of shape [n_samples, 4]
  The input samples.

- **y**: array of shape [n_samples]
  The output values.
scikit-learn user guide, Release 0.20.dev0

References

[R343344], [R344344]

sklearn.datasets.make_friedman3

sklearn.datasets.make_friedman3(n_samples=100, noise=0.0, random_state=None)

Generate the “Friedman #3” regression problem

This dataset is described in Friedman [1] and Breiman [2].

Inputs X are 4 independent features uniformly distributed on the intervals:

\[
0 \leq X[:, 0] \leq 100,
40 \times \pi \leq X[:, 1] \leq 560 \times \pi,
0 \leq X[:, 2] \leq 1,
1 \leq X[:, 3] \leq 11.
\]

The output y is created according to the formula:

\[
y(X) = \arctan((X[:, 1] \times X[:, 2] - 1 / (X[:, 1] \times X[:, 3])) / X[:, 0]) + \text{noise} \times \mathcal{N}(0, 1).\]

Read more in the User Guide.

Parameters

**n_samples** : int, optional (default=100)

The number of samples.

**noise** : float, optional (default=0.0)

The standard deviation of the gaussian noise applied to the output.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns

**X** : array of shape [n_samples, 4]

The input samples.

**y** : array of shape [n_samples]

The output values.

References

[R347348], [R348348]

sklearn.datasets.make_gaussian_quantiles

sklearn.datasets.make_gaussian_quantiles(mean=None, cov=1.0, n_samples=100, n_features=2, n_classes=3, shuffle=True, random_state=None)

Generate isotropic Gaussian and label samples by quantile
This classification dataset is constructed by taking a multi-dimensional standard normal distribution and defining classes separated by nested concentric multi-dimensional spheres such that roughly equal numbers of samples are in each class (quantiles of the χ² distribution).

Read more in the User Guide.

**Parameters**

- **mean**: array of shape `[n_features]`, optional (default=None)
  The mean of the multi-dimensional normal distribution. If None then use the origin (0, 0, ...).

- **cov**: float, optional (default=1.)
  The covariance matrix will be this value times the unit matrix. This dataset only produces symmetric normal distributions.

- **n_samples**: int, optional (default=100)
  The total number of points equally divided among classes.

- **n_features**: int, optional (default=2)
  The number of features for each sample.

- **n_classes**: int, optional (default=3)
  The number of classes

- **shuffle**: boolean, optional (default=True)
  Shuffle the samples.

- **random_state**: int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **X**: array of shape `[n_samples, n_features]`
  The generated samples.

- **y**: array of shape `[n_samples]`
  The integer labels for quantile membership of each sample.

**Notes**

The dataset is from Zhu et al [1].

**References**

[R5151]

**Examples using sklearn.datasets.make_gaussian_quantiles**

- "Plot randomly generated classification dataset"
- "Two-class AdaBoost"
- "Multi-class AdaBoosted Decision Trees"
sklearn.datasets.make_hastie_10_2

Generates data for binary classification used in Hastie et al. 2009, Example 10.2.

The ten features are standard independent Gaussian and the target \( y \) is defined by:

\[
y[i] = 1 \text{ if } \text{np.sum}(X[i] ** 2) > 9.34 \text{ else } -1
\]

Read more in the User Guide.

Parameters

- **n_samples** : int, optional (default=12000)
  - The number of samples.

- **random_state** : int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

Returns

- **X** : array of shape [n_samples, 10]
  - The input samples.

- **y** : array of shape [n_samples]
  - The output values.

See also:

- `make_gaussian_quantiles` a generalization of this dataset approach

References

[R5353]

Examples using sklearn.datasets.make_hastie_10_2

- Gradient Boosting regularization
- Discrete versus Real AdaBoost
- Early stopping of Gradient Boosting
- Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV

sklearn.datasets.make_low_rank_matrix

Generate a mostly low rank matrix with bell-shaped singular values.

Most of the variance can be explained by a bell-shaped curve of width `effective_rank`: the low rank part of the singular values profile is:

\[(1 - \text{tail_strength}) \times \exp(-1.0 \times (i / \text{effective_rank}) ** 2)\]

The remaining singular values’ tail is fat, decreasing as:
The low rank part of the profile can be considered the structured signal part of the data while the tail can be considered the noisy part of the data that cannot be summarized by a low number of linear components (singular vectors).

This kind of singular profiles is often seen in practice, for instance:

- gray level pictures of faces
- TF-IDF vectors of text documents crawled from the web

Read more in the User Guide.

**Parameters**

- **n_samples** : int, optional (default=100)
  The number of samples.
- **n_features** : int, optional (default=100)
  The number of features.
- **effective_rank** : int, optional (default=10)
  The approximate number of singular vectors required to explain most of the data by linear combinations.
- **tail_strength** : float between 0.0 and 1.0, optional (default=0.5)
  The relative importance of the fat noisy tail of the singular values profile.
- **random_state** : int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **X** : array of shape [n_samples, n_features]
  The matrix.

**sklearn.datasets.make_moons**

Make two interleaving half circles

A simple toy dataset to visualize clustering and classification algorithms. Read more in the User Guide.

**Parameters**

- **n_samples** : int, optional (default=100)
  The total number of points generated.
- **shuffle** : bool, optional (default=True)
  Whether to shuffle the samples.
- **noise** : double or None (default=None)
  Standard deviation of Gaussian noise added to the data.
- **random_state** : int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
Returns X : array of shape [n_samples, 2]
The generated samples.
y : array of shape [n_samples]
The integer labels (0 or 1) for class membership of each sample.

Examples using sklearn.datasets.make_moons

- Classifier comparison
- Comparing different clustering algorithms on toy datasets
- Compare Stochastic learning strategies for MLPClassifier
- Varying regularization in Multi-layer Perceptron

sklearn.datasets.make_multilabel_classification

sklearn.datasets.make_multilabel_classification(n_samples=100, n_features=20, n_classes=5, n_labels=2, length=50, allow_unlabeled=True, sparse=False, return_indicator='dense', return_distributions=False, random_state=None)

Generate a random multilabel classification problem.

For each sample, the generative process is:

- pick the number of labels: n ~ Poisson(n_labels)
- n times, choose a class c: c ~ Multinomial(theta)
- pick the document length: k ~ Poisson(length)
- k times, choose a word: w ~ Multinomial(theta_c)

In the above process, rejection sampling is used to make sure that n is never zero or more than n_classes, and that the document length is never zero. Likewise, we reject classes which have already been chosen.

Read more in the User Guide.

Parameters n_samples : int, optional (default=100)
The number of samples.
n_features : int, optional (default=20)
The total number of features.
n_classes : int, optional (default=5)
The number of classes of the classification problem.
n_labels : int, optional (default=2)
The average number of labels per instance. More precisely, the number of labels per sample is drawn from a Poisson distribution with n_labels as its expected value, but samples are bounded (using rejection sampling) by n_classes, and must be nonzero if allow_unlabeled is False.
length : int, optional (default=50)
The sum of the features (number of words if documents) is drawn from a Poisson distribution with this expected value.

**allow_unlabeled** : bool, optional (default=True)

If True, some instances might not belong to any class.

**sparse** : bool, optional (default=False)

If True, return a sparse feature matrix

New in version 0.17: parameter to allow sparse output.

**return_indicator** : ‘dense’ (default) | 'sparse' | False

If dense return Y in the dense binary indicator format. If 'sparse' return Y in the sparse binary indicator format. False returns a list of lists of labels.

**return_distributions** : bool, optional (default=False)

If True, return the prior class probability and conditional probabilities of features given classes, from which the data was drawn.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns **X** : array of shape [n_samples, n_features]

The generated samples.

**Y** : array or sparse CSR matrix of shape [n_samples, n_classes]

The label sets.

**p_c** : array, shape [n_classes]

The probability of each class being drawn. Only returned if return_distributions=True.

**p_w_c** : array, shape [n_features, n_classes]

The probability of each feature being drawn given each class. Only returned if return_distributions=True.

Examples using **sklearn.datasets.make_multilabel_classification**

- **Multilabel classification**
- **Plot randomly generated multilabel dataset**

**sklearn.datasets.make_regression**

**sklearn.datasets.make_regression** (n_samples=100, n_features=100, n_informative=10, n_targets=1, bias=0.0, effective_rank=None, tail_strength=0.5, noise=0.0, shuffle=True, coef=False, random_state=None)

Generate a random regression problem.

The input set can either be well conditioned (by default) or have a low rank-fat tail singular profile. See **make_low_rank_matrix** for more details.
The output is generated by applying a (potentially biased) random linear regression model with \( n_{\text{informative}} \) nonzero regressors to the previously generated input and some gaussian centered noise with some adjustable scale.

Read more in the User Guide.

**Parameters**

- **n_samples** : int, optional (default=100)
  - The number of samples.

- **n_features** : int, optional (default=100)
  - The number of features.

- **n_informative** : int, optional (default=10)
  - The number of informative features, i.e., the number of features used to build the linear model used to generate the output.

- **n_targets** : int, optional (default=1)
  - The number of regression targets, i.e., the dimension of the y output vector associated with a sample. By default, the output is a scalar.

- **bias** : float, optional (default=0.0)
  - The bias term in the underlying linear model.

- **effective_rank** : int or None, optional (default=None)
  - if not None: The approximate number of singular vectors required to explain most of the input data by linear combinations. Using this kind of singular spectrum in the input allows the generator to reproduce the correlations often observed in practice.
  - if None: The input set is well conditioned, centered and gaussian with unit variance.

- **tail_strength** : float between 0.0 and 1.0, optional (default=0.5)
  - The relative importance of the fat noisy tail of the singular values profile if effective_rank is not None.

- **noise** : float, optional (default=0.0)
  - The standard deviation of the gaussian noise applied to the output.

- **shuffle** : boolean, optional (default=True)
  - Shuffle the samples and the features.

- **coef** : boolean, optional (default=False)
  - If True, the coefficients of the underlying linear model are returned.

- **random_state** : int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by \( \text{np.random} \).

**Returns**

- **X** : array of shape [n_samples, n_features]
  - The input samples.

- **y** : array of shape [n_samples] or [n_samples, n_targets]
  - The output values.

- **coef** : array of shape [n_features] or [n_features, n_targets], optional
The coefficient of the underlying linear model. It is returned only if coef is True.

Examples using `sklearn.datasets.make_regression`

- Prediction Latency
- Plot Ridge coefficients as a function of the L2 regularization
- Robust linear model estimation using RANSAC
- Lasso on dense and sparse data
- HuberRegressor vs Ridge on dataset with strong outliers

`sklearn.datasets.make_s_curve`

`sklearn.datasets.make_s_curve` *(n_samples=100, noise=0.0, random_state=None)*

Generate an S curve dataset.

Parameters:

- `n_samples` : int, optional (default=100)
  The number of sample points on the S curve.
- `noise` : float, optional (default=0.0)
  The standard deviation of the gaussian noise.
- `random_state` : int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

Returns:

- `X` : array of shape [n_samples, 3]
  The points.
- `t` : array of shape [n_samples]
  The univariate position of the sample according to the main dimension of the points in the manifold.

Examples using `sklearn.datasets.make_s_curve`

- Comparison of Manifold Learning methods
- t-SNE: The effect of various perplexity values on the shape

`sklearn.datasets.make_sparse_coded_signal`

`sklearn.datasets.make_sparse_coded_signal` *(n_samples, n_components, n_features, n_nonzero_coefs, random_state=None)*

Generate a signal as a sparse combination of dictionary elements.

Returns a matrix Y = DX, such as D is (n_features, n_components), X is (n_components, n_samples) and each column of X has exactly n_nonzero_coefs non-zero elements.

Read more in the User Guide.
Parameters

- **n_samples**: int
  number of samples to generate

- **n_components**: int,
  number of components in the dictionary

- **n_features**: int
  number of features of the dataset to generate

- **n_nonzero_coefs**: int
  number of active (non-zero) coefficients in each sample

- **random_state**: int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

Returns

- **data**: array of shape [n_features, n_samples]
  The encoded signal (Y).

- **dictionary**: array of shape [n_features, n_components]
  The dictionary with normalized components (D).

- **code**: array of shape [n_components, n_samples]
  The sparse code such that each column of this matrix has exactly n_nonzero_coefs non-zero items (X).

Examples using `sklearn.datasets.make_sparse_coded_signal`

- **Orthogonal Matching Pursuit**

`sklearn.datasets.make_sparse_spd_matrix`

`sklearn.datasets.make_sparse_spd_matrix(dim=1, alpha=0.95, norm_diag=False, smallest_coef=0.1, largest_coef=0.9, random_state=None)`

Generate a sparse symmetric definite positive matrix.

Read more in the User Guide.

- **Parameters**
  - **dim**: integer, optional (default=1)
    The size of the random matrix to generate.
  - **alpha**: float between 0 and 1, optional (default=0.95)
    The probability that a coefficient is zero (see notes). Larger values enforce more sparsity.
  - **norm_diag**: boolean, optional (default=False)
    Whether to normalize the output matrix to make the leading diagonal elements all 1
  - **smallest_coef**: float between 0 and 1, optional (default=0.1)
    The value of the smallest coefficient.
largest_coef : float between 0 and 1, optional (default=0.9)

The value of the largest coefficient.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns prec : sparse matrix of shape (dim, dim)

The generated matrix.

See also:

make_spd_matrix

Notes

The sparsity is actually imposed on the cholesky factor of the matrix. Thus alpha does not translate directly into the filling fraction of the matrix itself.

Examples using sklearn.datasets.make_sparse_spd_matrix

• Sparse inverse covariance estimation

sklearn.datasets.make_sparse_uncorrelated

sklearn.datasets.make_sparse_uncorrelated(n_samples=100, n_features=10, random_state=None)

Generate a random regression problem with sparse uncorrelated design

This dataset is described in Celeux et al [1]. as:

\[
\begin{align*}
X & \sim N(0, 1) \\
y(X) &= X[:, 0] + 2 \times X[:, 1] - 2 \times X[:, 2] - 1.5 \times X[:, 3]
\end{align*}
\]

Only the first 4 features are informative. The remaining features are useless.

Read more in the User Guide.

Parameters n_samples : int, optional (default=100)

The number of samples.

n_features : int, optional (default=10)

The number of features.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns X : array of shape [n_samples, n_features]

The input samples.

y : array of shape [n_samples]
The output values.

References

[R355355]

**sklearn.datasets.make_spd_matrix**

sklearn.datasets.make_spd_matrix(n_dim, random_state=None)

Generate a random symmetric, positive-definite matrix.

Read more in the User Guide.

**Parameters**

- **n_dim**: int
  
  The matrix dimension.
  
  - **random_state**: int, RandomState instance or None, optional (default=None)
    
    If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **X**: array of shape [n_dim, n_dim]

  The random symmetric, positive-definite matrix.

**See also:**

make_sparse_spd_matrix

**sklearn.datasets.make_swiss_roll**

sklearn.datasets.make_swiss_roll(n_samples=100, noise=0.0, random_state=None)

Generate a swiss roll dataset.

Read more in the User Guide.

**Parameters**

- **n_samples**: int, optional (default=100)

  The number of sample points on the S curve.

- **noise**: float, optional (default=0.0)

  The standard deviation of the gaussian noise.

- **random_state**: int, RandomState instance or None, optional (default=None)

  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **X**: array of shape [n_samples, 3]

  The points.

- **t**: array of shape [n_samples]

  The univariate position of the sample according to the main dimension of the points in the manifold.
Notes

The algorithm is from Marsland [1].

References

[R5555]

Examples using `sklearn.datasets.make_swiss_roll`

- Hierarchical clustering: structured vs unstructured ward
- Swiss Roll reduction with LLE

30.8 `sklearn.decomposition`: Matrix Decomposition

The `sklearn.decomposition` module includes matrix decomposition algorithms, including among others PCA, NMF or ICA. Most of the algorithms of this module can be regarded as dimensionality reduction techniques.

User guide: See the Decomposing signals in components (matrix factorization problems) section for further details.

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<td>Dictionary learning</td>
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<td><code>FactorAnalysis</code></td>
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<td><code>IncrementalPCA</code></td>
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<td><code>KernelPCA</code></td>
<td>Kernel Principal component analysis (KPCA)</td>
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<tr>
<td><code>LatentDirichletAllocation</code></td>
<td>Latent Dirichlet Allocation with online variational Bayes algorithm</td>
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<td><code>MiniBatchDictionaryLearning</code></td>
<td>Mini-batch dictionary learning</td>
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<td><code>PCA</code></td>
<td>Principal component analysis (PCA)</td>
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<td><code>SparsePCA</code></td>
<td>Sparse Principal Components Analysis (SparsePCA)</td>
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<td><code>SparseCoder</code></td>
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<tr>
<td><code>TruncatedSVD</code></td>
<td>Dimensionality reduction using truncated SVD (aka LSA).</td>
</tr>
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</table>
Dictionary learning

Finds a dictionary (a set of atoms) that can best be used to represent data using a sparse code.

Solves the optimization problem:

\[(U^*, V^*) = \arg\min_{(U, V)} 0.5 \| Y - U V \|_2^2 + \alpha \| U \|_1\]

with \( \| V_k \|_2 = 1 \) for all \( 0 \leq k < n\text{\_components} \)

Read more in the User Guide.

**Parameters**

**n\_components**: int,
number of dictionary elements to extract

**alpha**: float,
sparsity controlling parameter

**max\_iter**: int,
maximum number of iterations to perform

**tol**: float,
tolerance for numerical error

**fit\_algorithm**: {'lars', 'cd'}
- lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path)
- cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

New in version 0.17: cd coordinate descent method to improve speed.

**transform\_algorithm**: {'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'}
- lasso\_lars: uses Lars to compute the Lasso solution (linear_model.Lasso).
- lasso\_cd: uses Lars to solve the Lasso problem (linear_model.lars_path)
- lars\_lars: uses Lars to compute the Lasso solution (linear_model.Lasso).
- lars\_cd will be faster if the estimated components are sparse.
- omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection \( \text{dictionary} \times X' \)

New in version 0.17: lasso\_cd coordinate descent method to improve speed.

**transform\_n\_nonzero\_coefs**: int, \(0.1 \times \text{n\_features}\) by default

Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the omp case.
transform_alpha : float, 1. by default

If algorithm='lasso_lars' or algorithm='lasso_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n_nonzero_coefs.

n_jobs : int

   number of parallel jobs to run

code_init : array of shape (n_samples, n_components),

   initial value for the code, for warm restart
dict_init : array of shape (n_components, n_features),

   initial values for the dictionary, for warm restart

verbose : bool, optional (default: False)

   To control the verbosity of the procedure.
split_sign : bool, False by default

   Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.

random_state : int, RandomState instance or None, optional (default=None)

   If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Attributes

| components_ | (array, [n_components, n_features]) dictionary atoms extracted from the data |
| error_      | (array) vector of errors at each iteration |
| n_iter_     | (int) Number of iterations run. |

See also:

SparseCoder, MiniBatchDictionaryLearning, SparsePCA, MiniBatchSparsePCA

Notes

References:


Methods

fit(X[, y])  Fit the model from data in X.
fit_transform(X[, y])  Fit to data, then transform it.
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<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Encode the data as a sparse combination of the dictionary atoms.</td>
</tr>
</tbody>
</table>

```
__init__(n_components=None, alpha=1, max_iter=1000, tol=1e-08, fit_algorithm='lars', transform_algorithm='omp', transform_n_nonzero_coefs=None, transform_alpha=None, n_jobs=1, code_init=None, dict_init=None, verbose=False, split_sign=False, random_state=None)
```

```
fit (X, y=None)
```

Fit the model from data in X.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  Training vector, where n_samples in the number of samples and n_features is the number of features.

- **y**: Ignored

**Returns**

- **self**: object

  Returns the object itself

```
fit_transform (X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  
  Training set.

- **y**: numpy array of shape [n_samples]
  
  Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

```
get_params (deep=True)
```

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any

  Parameter names mapped to their values.

```
set_params (**params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

```
transform (X)
```

Encode the data as a sparse combination of the dictionary atoms.
Coding method is determined by the object parameter `transform_algorithm`.

**Parameters**

- **X**: array of shape (n_samples, n_features)
  
  Test data to be transformed, must have the same number of features as the data used to train the model.

**Returns**

- **X_new**: array, shape (n_samples, n_components)
  
  Transformed data

### 30.8.2 sklearn.decomposition.FactorAnalysis

**class sklearn.decomposition.FactorAnalysis**

```
FactorAnalysis(n_components=None, tol=0.01, copy=True, max_iter=1000, noise_variance_init=None, svd_method='randomized', iterated_power=3, random_state=0)
```

Factor Analysis (FA)

A simple linear generative model with Gaussian latent variables.

The observations are assumed to be caused by a linear transformation of lower dimensional latent factors and added Gaussian noise. Without loss of generality the factors are distributed according to a Gaussian with zero mean and unit covariance. The noise is also zero mean and has an arbitrary diagonal covariance matrix.

If we would restrict the model further, by assuming that the Gaussian noise is even isotropic (all diagonal entries are the same) we would obtain PPCA.

FactorAnalysis performs a maximum likelihood estimate of the so-called *loading* matrix, the transformation of the latent variables to the observed ones, using expectation-maximization (EM).

Read more in the User Guide.

**Parameters**

- **n_components**: int | None
  
  Dimensionality of latent space, the number of components of X that are obtained after `transform`. If None, n_components is set to the number of features.

- **tol**: float
  
  Stopping tolerance for EM algorithm.

- **copy**: bool
  
  Whether to make a copy of X. If False, the input X gets overwritten during fitting.

- **max_iter**: int
  
  Maximum number of iterations.

- **noise_variance_init**: None | array, shape=(n_features,)
  
  The initial guess of the noise variance for each feature. If None, it defaults to `np.ones(n_features)`.

- **svd_method**: {'lapack', 'randomized'}
  
  Which SVD method to use. If ‘lapack’ use standard SVD from scipy.linalg, if ‘randomized’ use fast `randomized_svd` function. Defaults to ‘randomized’. For most applications ‘randomized’ will be sufficiently precise while providing significant speed gains. Accuracy can also be improved by setting higher values for `iterated_power`. If this is not sufficient, for maximum precision you should choose ‘lapack’.

- **iterated_power**: int, optional
Number of iterations for the power method. 3 by default. Only used if **svd_method** equals ‘randomized’

**random_state** : int, RandomState instance or None, optional (default=0)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Only used when **svd_method** equals ‘randomized’.

**Attributes**

<table>
<thead>
<tr>
<th>components_</th>
<th>(array, [n_components, n_features]) Components with maximum variance.</th>
</tr>
</thead>
<tbody>
<tr>
<td>loglike_</td>
<td>(list, [n_iterations]) The log likelihood at each iteration.</td>
</tr>
<tr>
<td>noise_variance_</td>
<td>(array, shape=(n_features,)) The estimated noise variance for each feature.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Number of iterations run.</td>
</tr>
</tbody>
</table>

**See also:**

**PCA** Principal component analysis is also a latent linear variable model which however assumes equal noise variance for each feature. This extra assumption makes probabilistic PCA faster as it can be computed in closed form.

**FastICA** Independent component analysis, a latent variable model with non-Gaussian latent variables.

**References**

**Methods**

- **fit(X[, y])**  
  Fit the FactorAnalysis model to X using EM

- **fit_transform(X[, y])**  
  Fit to data, then transform it.

- **get_covariance()**  
  Compute data covariance with the FactorAnalysis model.

- **get_params([deep])**  
  Get parameters for this estimator.

- **get_precision()**  
  Compute data precision matrix with the FactorAnalysis model.

- **score(X[, y])**  
  Compute the average log-likelihood of the samples

- **score_samples(X)**  
  Compute the log-likelihood of each sample

- **set_params(**params)**  
  Set the parameters of this estimator.

- **transform(X)**  
  Apply dimensionality reduction to X using the model.

**__init__** (n_components=None, tol=0.01, copy=True, max_iter=1000, noise_variance_init=None, svd_method='randomized', iterated_power=3, random_state=0)

**fit (X, y=None)**  
Fit the FactorAnalysis model to X using EM

  **Parameters**  
  **X** : array-like, shape (n_samples, n_features)

  Training data.

  **y** : Ignored

---

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Returns self

**fit_transform**(X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  - Training set.
- **y**: numpy array of shape [n_samples]
  - Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  - Transformed array.

**get_covariance**()

Compute data covariance with the FactorAnalysis model.

\[
\text{cov} = \text{components}_\cdot^\text{T} \ast \text{components}_\cdot + \text{diag} (\text{noise}_\text{variance})
\]

**Returns**

- **cov**: array, shape (n_features, n_features)
  - Estimated covariance of data.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**get_precision**()

Compute data precision matrix with the FactorAnalysis model.

**Returns**

- **precision**: array, shape (n_features, n_features)
  - Estimated precision of data.

**score**(X, y=None)

Compute the average log-likelihood of the samples

**Parameters**

- **X**: array, shape (n_samples, n_features)
  - The data
- **y**: Ignored

**Returns**

- **ll**: float
  - Average log-likelihood of the samples under the current model

**score_samples**(X)

Compute the log-likelihood of each sample

**Parameters**

- **X**: array, shape (n_samples, n_features)
  - The data

**Returns**

- **ll**: array, shape (n_samples,)
Log-likelihood of each sample under the current model

**set_params**(**params**)  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>___<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
self

**transform**(**X**)  
Apply dimensionality reduction to X using the model.

Compute the expected mean of the latent variables. See Barber, 21.2.33 (or Bishop, 12.66).

**Parameters**  
**X**: array-like, shape (n_samples, n_features)  
Training data.

**Returns**  
**X_new**: array-like, shape (n_samples, n_components)  
The latent variables of X.

Examples using `sklearn.decomposition.FactorAnalysis`

- *Model selection with Probabilistic PCA and Factor Analysis (FA)*
- *Faces dataset decompositions*

### 30.8.3 sklearn.decomposition.FastICA

**class** `sklearn.decomposition.FastICA(n_components=None, algorithm='parallel', whiten=True, fun='logcosh', fun_args=None, max_iter=200, tol=0.0001, w_init=None, random_state=None)`

FastICA: a fast algorithm for Independent Component Analysis.

Read more in the *User Guide*.

**Parameters**  
**n_components**: int, optional  
Number of components to use. If none is passed, all are used.

**algorithm**: {'parallel', 'deflation'}  
Apply parallel or deflational algorithm for FastICA.

**whiten**: boolean, optional  
If whiten is false, the data is already considered to be whitened, and no whitening is performed.

**fun**: string or function, optional. Default: ‘logcosh’  
The functional form of the G function used in the approximation to neg-entropy. Could be either ‘logcosh’, ‘exp’, or ‘cube’. You can also provide your own function. It should return a tuple containing the value of the function, and of its derivative, in the point. Example:

```python
def my_g(x):
    return x ** 3, 3 * x ** 2
```

**fun_args**: dictionary, optional
Arguments to send to the functional form. If empty and if fun='logcosh', fun_args will take value {'alpha': 1.0}.

**max_iter** : int, optional
Maximum number of iterations during fit.

**tol** : float, optional
Tolerance on update at each iteration.

**w_init** : None of an (n_components, n_components) ndarray
The mixing matrix to be used to initialize the algorithm.

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

| components_ | (2D array, shape (n_components, n_features)) The unmixing matrix. |
| mixing_     | (array, shape (n_features, n_components)) The mixing matrix. |
| n_iter_     | (int) If the algorithm is “deflation”, n_iter is the maximum number of iterations run across all components. Else they are just the number of iterations taken to converge. |

**Notes**


**Methods**

| fit(X[, y]) | Fit the model to X. |
| fit_transform(X[, y]) | Fit the model and recover the sources from X. |
| get_params([deep]) | Get parameters for this estimator. |
| inverse_transform(X[, copy]) | Transform the sources back to the mixed data (apply mixing matrix). |
| set_params(**params) | Set the parameters of this estimator. |
| transform(X[, y, copy]) | Recover the sources from X (apply the unmixing matrix). |

**__init__**(n_components=None, algorithm='parallel', whiten=True, fun='logcosh', fun_args=None, max_iter=200, tol=0.0001, w_init=None, random_state=None)

**fit**(X, y=None)
Fit the model to X.

**Parameters**

- **X** : array-like, shape (n_samples, n_features)
Training data, where n_samples is the number of samples and n_features is the number of features.

y : Ignored

Returns self

**fit_transform** *(X, y=None)*
Fit the model and recover the sources from X.

**Parameters**
- X : array-like, shape (n_samples, n_features)
  Training data, where n_samples is the number of samples and n_features is the number of features.
- y : Ignored

**Returns**
- X_new : array-like, shape (n_samples, n_components)

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**
- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- params : mapping of string to any
  Parameter names mapped to their values.

**inverse_transform** *(X, copy=True)*
Transform the sources back to the mixed data (apply mixing matrix).

**Parameters**
- X : array-like, shape (n_samples, n_components)
  Sources, where n_samples is the number of samples and n_components is the number of components.
- copy : bool (optional)
  If False, data passed to fit are overwritten. Defaults to True.

**Returns**
- X_new : array-like, shape (n_samples, n_features)

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**
- self

**transform** *(X, y='deprecated', copy=True)*
Recover the sources from X (apply the unmixing matrix).

**Parameters**
- X : array-like, shape (n_samples, n_features)
  Data to transform, where n_samples is the number of samples and n_features is the number of features.
- y : (ignored)
  Deprecated since version 0.19: This parameter will be removed in 0.21.
- copy : bool (optional)
If False, data passed to fit are overwritten. Defaults to True.

**Returns**  
X_new : array-like, shape (n_samples, n_components)

**Examples using sklearn.decomposition.FastICA**

- Blind source separation using FastICA
- FastICA on 2D point clouds
- Faces dataset decompositions

### 30.8.4 sklearn.decomposition.IncrementalPCA

*Class sklearn.decomposition.IncrementalPCA(n_components=None, whiten=False, copy=True, batch_size=None)*

Incremental principal components analysis (IPCA).

Linear dimensionality reduction using Singular Value Decomposition of centered data, keeping only the most significant singular vectors to project the data to a lower dimensional space.

Depending on the size of the input data, this algorithm can be much more memory efficient than a PCA.

This algorithm has constant memory complexity, on the order of batch_size, enabling use of np.memmap files without loading the entire file into memory.

The computational overhead of each SVD is $O(\text{batch_size} \times n_{\text{features}}^2)$, but only $2 \times \text{batch_size}$ samples remain in memory at a time. There will be $n_{\text{samples}} / \text{batch_size}$ SVD computations to get the principal components, versus 1 large SVD of complexity $O(n_{\text{samples}} \times n_{\text{features}}^2)$ for PCA.

Read more in the User Guide.

**Parameters**

- **n_components** : int or None, (default=None)
  
  Number of components to keep. If n_components is None, then n_components is set to \(\min(n_{\text{samples}}, n_{\text{features}})\).

- **whiten** : bool, optional
  
  When True (False by default) the components_ vectors are divided by \(n_{\text{samples}} \times \text{components}_{\text{components}}\) to ensure uncorrelated outputs with unit component-wise variances.
  
  Whitening will remove some information from the transformed signal (the relative variance scales of the components) but can sometimes improve the predictive accuracy of the downstream estimators by making data respect some hard-wired assumptions.

- **copy** : bool, (default=True)
  
  If False, X will be overwritten. copy=False can be used to save memory but is unsafe for general use.

- **batch_size** : int or None, (default=None)
  
  The number of samples to use for each batch. Only used when calling fit. If batch_size is None, then batch_size is inferred from the data and set to $5 \times n_{\text{features}}$, to provide a balance between approximation accuracy and memory consumption.
Attributes

<table>
<thead>
<tr>
<th>component_</th>
<th>(array, shape (n_components, n_features)) Components with maximum variance.</th>
</tr>
</thead>
<tbody>
<tr>
<td>explained_variance_</td>
<td>(array, shape (n_components,)) Variance explained by each of the selected components.</td>
</tr>
<tr>
<td>explained_variance_ratio_</td>
<td>(array, shape (n_components,)) Percentage of variance explained by each of the selected components. The sum of explained variances is equal to 1.0.</td>
</tr>
<tr>
<td>singular_values_</td>
<td>(array, shape (n_components,)) The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n_components variables in the lower-dimensional space.</td>
</tr>
<tr>
<td>mean_</td>
<td>(array, shape (n_features,)) Per-feature empirical mean, aggregate over calls to partial_fit.</td>
</tr>
<tr>
<td>var_</td>
<td>(array, shape (n_features,)) Per-feature empirical variance, aggregate over calls to partial_fit.</td>
</tr>
<tr>
<td>n_components_</td>
<td>(int) The estimated number of components. Relevant when n_components=None.</td>
</tr>
<tr>
<td>n_samples_seen_</td>
<td>(int) The number of samples processed by the estimator. Will be reset on new calls to fit, but increments across partial_fit calls.</td>
</tr>
</tbody>
</table>

See also:

PCA, RandomizedPCA, KernelPCA, SparsePCA, TruncatedSVD

Notes


We have specifically abstained from an optimization used by authors of both papers, a QR decomposition used in specific situations to reduce the algorithmic complexity of the SVD. The source for this technique is Matrix Computations, Third Edition, G. Holub and C. Van Loan, Chapter 5, section 5.4.4, pp 252-253. This technique has been omitted because it is advantageous only when decomposing a matrix with n_samples (rows) >= 5/3 * n_features (columns), and hurts the readability of the implemented algorithm. This would be a good opportunity for future optimization, if it is deemed necessary.

References


Methods

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**init**\((n\_components=None, whiten=False, copy=True, batch\_size=None)\)

**fit** \((X, y=None)\)

Fit the model with \(X\), using minibatches of size \(\text{batch\_size}\).

**Parameters**

- \(X\) : array-like, shape \((n\_samples, n\_features)\)
  - Training data, where \(n\_samples\) is the number of samples and \(n\_features\) is the number of features.
- \(y\) : Ignored

**Returns**

- \(self\) : object
  - Returns the instance itself.

**fit\_transform** \((X, y=None, **fit\_params)\)

Fit to data, then transform it.

Fits transformer to \(X\) and \(y\) with optional parameters \(fit\_params\) and returns a transformed version of \(X\).

**Parameters**

- \(X\) : numpy array of shape \([n\_samples, n\_features]\)
  - Training set.
- \(y\) : numpy array of shape \([n\_samples]\)
  - Target values.

**Returns**

- \(X\_\text{new}\) : numpy array of shape \([n\_samples, n\_features\_new]\)
  - Transformed array.

**get\_covariance**()

Compute data covariance with the generative model.

\[
\text{cov} = \text{components\_T} \times S^{\times 2} \times \text{components\_} + \sigma^2 \times \text{eye}(n\_features)
\]

where \(S^{\times 2}\) contains the explained variances, and \(\sigma^2\) contains the noise variances.

**Returns**

- \(cov\) : array, shape \((n\_features, n\_features)\)
  - Estimated covariance of data.

**get\_params**(\text{\text{deep}=\text{True}})

Get parameters for this estimator.

**Parameters**

- \(\text{deep}\) : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_precision ()
Compute data precision matrix with the generative model.
Equals the inverse of the covariance but computed with the matrix inversion lemma for efficiency.

Returns precision : array, shape=(n_features, n_features)
Estimated precision of data.

inverse_transform (X)
Transform data back to its original space.
In other words, return an input X_original whose transform would be X.

Parameters X : array-like, shape (n_samples, n_components)
New data, where n_samples is the number of samples and n_components is the number of components.

Returns X_original array-like, shape (n_samples, n_features)

Notes
If whitening is enabled, inverse_transform will compute the exact inverse operation, which includes reversing whitening.

partial_fit (X, y=None, check_input=True)
Incremental fit with X. All of X is processed as a single batch.

Parameters X : array-like, shape (n_samples, n_features)
Training data, where n_samples is the number of samples and n_features is the number of features.

check_input : bool
Run check_array on X.

y : Ignored

Returns self : object
Returns the instance itself.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Apply dimensionality reduction to X.
X is projected on the first principal components previously extracted from a training set.
Parameters X : array-like, shape (n_samples, n_features)

New data, where n_samples is the number of samples and n_features is the number of features.

Returns X_new : array-like, shape (n_samples, n_components)

Examples

```python
>>> import numpy as np
>>> from sklearn.decomposition import IncrementalPCA
>>> X = np.array([[1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> ipca = IncrementalPCA(n_components=2, batch_size=3)
>>> ipca.fit(X)
IncrementalPCA(batch_size=3, copy=True, n_components=2, whiten=False)
>>> ipca.transform(X)
```

Examples using sklearn.decomposition.IncrementalPCA

- Incremental PCA

30.8.5 sklearn.decomposition.KernelPCA

class sklearn.decomposition.KernelPCA(n_components=None, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None, alpha=1.0, fit_inverse_transform=False, eigen_solver='auto', tol=0, max_iter=None, remove_zero_eig=False, random_state=None, copy_X=True, n_jobs=1)

Kernel Principal component analysis (KPCA)

Non-linear dimensionality reduction through the use of kernels (see Pairwise metrics, Affinities and Kernels).

Read more in the User Guide.

Parameters n_components : int, default=None

Number of components. If None, all non-zero components are kept.

kernel : “linear” | “poly” | “rbf” | “sigmoid” | “cosine” | “precomputed”

Kernel. Default=”linear”.

gamma : float, default=1/n_features

Kernel coefficient for rbf, poly and sigmoid kernels. Ignored by other kernels.

degree : int, default=3

Degree for poly kernels. Ignored by other kernels.

coef0 : float, default=1

Independent term in poly and sigmoid kernels. Ignored by other kernels.

kernel_params : mapping of string to any, default=None

Parameters (keyword arguments) and values for kernel passed as callable object. Ignored by other kernels.

alpha : int, default=1.0
Hyperparameter of the ridge regression that learns the inverse transform (when `fit_inverse_transform=True`).

**fit_inverse_transform** : bool, default=False

Learn the inverse transform for non-precomputed kernels. (i.e. learn to find the pre-image of a point)

**eigen_solver** : string [‘auto’|‘dense’|‘arpack’], default=’auto’

Select eigensolver to use. If `n_components` is much less than the number of training samples, arpack may be more efficient than the dense eigensolver.

**tol** : float, default=0

Convergence tolerance for arpack. If 0, optimal value will be chosen by arpack.

**max_iter** : int, default=None

Maximum number of iterations for arpack. If None, optimal value will be chosen by arpack.

**remove_zero_eig** : boolean, default=False

If True, then all components with zero eigenvalues are removed, so that the number of components in the output may be < `n_components` (and sometimes even zero due to numerical instability). When `n_components` is None, this parameter is ignored and components with zero eigenvalues are removed regardless.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`. Used when `eigen_solver == ‘arpack’`.

New in version 0.18.

**copy_X** : boolean, default=True

If True, input X is copied and stored by the model in the `X_fit_` attribute. If no further changes will be done to X, setting `copy_X=False` saves memory by storing a reference.

New in version 0.18.

**n_jobs** : int, default=1

The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.

New in version 0.18.
Attributes

- `lambdas_` (array, (n_components,)) Eigenvalues of the centered kernel matrix in decreasing order. If `n_components` and `remove_zero_eig` are not set, then all values are stored.
- `alphas_` (array, (n_samples, n_components)) Eigenvectors of the centered kernel matrix. If `n_components` and `remove_zero_eig` are not set, then all components are stored.
- `dual_coef_` (array, (n_samples, n_features)) Inverse transform matrix. Set if `fit_inverse_transform` is True.
- `X_transformed_` (array, (n_samples, n_components)) Projection of the fitted data on the kernel principal components.
- `X_fit_` (array, (n_samples, n_features)) The data used to fit the model. If `copy_X=False`, then `X_fit_` is a reference. This attribute is used for the calls to transform.

References


Methods

- `fit(X[, y])` Fit the model from data in X.
- `fit_transform(X[, y])` Fit the model from data in X and transform X.
- `get_params([deep])` Get parameters for this estimator.
- `inverse_transform(X)` Transform X back to original space.
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X)` Transform X.

**init**(n_components=None, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None, alpha=1.0, fit_inverse_transform=False, eigen_solver='auto', tol=0, max_iter=None, remove_zero_eig=False, random_state=None, copy_X=True, n_jobs=1)

```python
fit(X, y=None)
Fit the model from data in X.

Parameters
X : array-like, shape (n_samples, n_features)
Training vector, where n_samples in the number of samples and n_features is the number of features.

Returns
self : object
Returns the instance itself.

fit_transform(X, y=None, **params)
Fit the model from data in X and transform X.

Parameters
X : array-like, shape (n_samples, n_features)
Training vector, where n_samples in the number of samples and n_features is the number of features.

Returns
X_new : array-like, shape (n_samples, n_components)
```
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform (X)
Transform X back to original space.

Parameters X : array-like, shape (n_samples, n_components)

Returns X_new : array-like, shape (n_samples, n_features)

References


set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Transform X.

Parameters X : array-like, shape (n_samples, n_features)

Returns X_new : array-like, shape (n_samples, n_components)

Examples using sklearn.decomposition.KernelPCA

• Kernel PCA
Latent Dirichlet Allocation with online variational Bayes algorithm

New in version 0.17.

Read more in the User Guide.

**Parameters**

- **n_components**: int, optional (default=10)
  Number of topics.

- **doc_topic_prior**: float, optional (default=None)
  Prior of document topic distribution theta. If the value is None, defaults to \( \frac{1}{n\_components} \). In the literature, this is called alpha.

- **topic_word_prior**: float, optional (default=None)
  Prior of topic word distribution beta. If the value is None, defaults to \( \frac{1}{n\_components} \). In the literature, this is called eta.

- **learning_method**: ‘batch’ | ‘online’, default=’online’
  Method used to update _component. Only used in fit method. In general, if the data size is large, the online update will be much faster than the batch update. The default learning method is going to be changed to ‘batch’ in the 0.20 release. Valid options:

  - **'batch'**: Batch variational Bayes method. Use all training data in each EM update. Old 'components_' will be overwritten in each iteration.
  - **'online'**: Online variational Bayes method. In each EM update, use mini-batch of training data to update the 'components_' variable incrementally. The learning rate is controlled by the learning_decay and the learning_offset parameters.

- **learning_decay**: float, optional (default=0.7)
  It is a parameter that control learning rate in the online learning method. The value should be set between (0.5, 1.0] to guarantee asymptotic convergence. When the value is 0.0 and batch_size is n_samples, the update method is same as batch learning. In the literature, this is called kappa.
learning_offset : float, optional (default=10.)

A (positive) parameter that downweights early iterations in online learning. It should be greater than 1.0. In the literature, this is called tau_0.

max_iter : integer, optional (default=10)

The maximum number of iterations.

batch_size : int, optional (default=128)

Number of documents to use in each EM iteration. Only used in online learning.

evaluate_every : int, optional (default=0)

How often to evaluate perplexity. Only used in fit method. set it to 0 or negative number to not evaluate perplexity in training at all. Evaluating perplexity can help you check convergence in training process, but it will also increase total training time. Evaluating perplexity in every iteration might increase training time up to two-fold.

total_samples : int, optional (default=1e6)

Total number of documents. Only used in the partial_fit method.

perp_tol : float, optional (default=1e-1)

Perplexity tolerance in batch learning. Only used when evaluate_every is greater than 0.

mean_change_tol : float, optional (default=1e-3)

Stopping tolerance for updating document topic distribution in E-step.

max_doc_update_iter : int (default=100)

Max number of iterations for updating document topic distribution in the E-step.

n_jobs : int, optional (default=1)

The number of jobs to use in the E-step. If -1, all CPUs are used. For n_jobs below -1, (n_cpu + 1 + n_jobs) are used.

verbose : int, optional (default=0)

Verbosity level.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

n_topics : int, optional (default=None)

This parameter has been renamed to n_components and will be removed in version 0.21. .. deprecated:: 0.19
Attributes

- **components** (array, [n_components, n_features]) Variational parameters for topic word distribution. Since the complete conditional for topic word distribution is a Dirichlet, components_[i, j] can be viewed as pseudocount that represents the number of times word j was assigned to topic i. It can also be viewed as distribution over the words for each topic after normalization: model.components_ / model.components_.sum(axis=1)[:, np.newaxis].
- **n_batch_iter** (int) Number of iterations of the EM step.
- **n_iter** (int) Number of passes over the dataset.

References


Methods

- **fit**(X[, y]) Learn model for the data X with variational Bayes method.
- **fit_transform**(X[, y]) Fit to data, then transform it.
- **get_params**(deep) Get parameters for this estimator.
- **partial_fit**(X[, y]) Online VB with Mini-Batch update.
- **perplexity**(X[, doc_topic_distr, sub_sampling]) Calculate approximate perplexity for data X.
- **score**(X[, y]) Calculate approximate log-likelihood as score.
- **set_params**(**params) Set the parameters of this estimator.
- **transform**(X) Transform data X according to the fitted model.

- **init**(n_components=10, doc_topic_prior=None, topic_word_prior=None, learning_method=None, learning_decay=0.7, learning_offset=10.0, max_iter=10, batch_size=128, evaluate_every=-1, total_samples=1000000.0, perp_tol=0.1, mean_change_tol=0.001, max_doc_update_iter=100, n_jobs=1, verbose=0, random_state=None, n_topics=None)

- **fit**(X, y=None)
  Learn model for the data X with variational Bayes method.
  When learning_method is ‘online’, use mini-batch update. Otherwise, use batch update.

  **Parameters**
  - **X**: array-like or sparse matrix, shape=(n_samples, n_features)
    Document word matrix.
  - **y**: Ignored

  **Returns**
  - **self**

- **fit_transform**(X, y=None, **fit_params)
  Fit to data, then transform it.
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**
- **X**: numpy array of shape [n_samples, n_features]
  
  Training set.

- **y**: numpy array of shape [n_samples]
  
  Target values.

**Returns**
- **X_new**: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

**get_params**

Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any

  Parameter names mapped to their values.

**partial_fit**

Online VB with Mini-Batch update.

**Parameters**
- **X**: array-like or sparse matrix, shape=(n_samples, n_features)

  Document word matrix.

- **y**: Ignored

**Returns**
- **self**

**perplexity**

Calculate approximate perplexity for data X.

Perplexity is defined as \( \exp(-1. * \log\text{-likelihood per word}) \)

Changed in version 0.19: **doc_topic_distr** argument has been deprecated and is ignored because user no longer has access to unnormalized distribution.

**Parameters**
- **X**: array-like or sparse matrix, [n_samples, n_features]

  Document word matrix.

- **doc_topic_distr**: None or array, shape=(n_samples, n_components)

  Document topic distribution. This argument is deprecated and is currently being ignored.

  Deprecated since version 0.19.

- **sub_sampling**: bool

  Do sub-sampling or not.

**Returns**
- **score**: float

  Perplexity score.

**score**

Calculate approximate log-likelihood as score.

**Parameters**
- **X**: array-like or sparse matrix, shape=(n_samples, n_features)
Document word matrix.

\[ y \] : Ignored

**Returns** score : float

Use approximate bound as score.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>\_<\text{parameter}>\) so that it’s possible to update each component of a nested object.

**Returns** self

**transform** (X)

Transform data X according to the fitted model.

Changed in version 0.18: \( \text{doc_topic_distr} \) is now normalized

**Parameters** X : array-like or sparse matrix, shape=(n_samples, n_features)

Document word matrix.

**Returns** doc_topic_distr : shape=(n_samples, n_components)

Document topic distribution for X.

Examples using sklearn.decomposition.LatentDirichletAllocation

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation

30.8.7 sklearn.decomposition.MiniBatchDictionaryLearning

class sklearn.decomposition.MiniBatchDictionaryLearning (n_components=None, alpha=1, n_iter=1000, fit_algorithm='lars', n_jobs=1, batch_size=3, shuffle=True, dict_init=None, transform_algorithm='omp', transform_n_nonzero_coefs=None, transform_alpha=None, verbose=False, split_sign=False, random_state=None)

Mini-batch dictionary learning

Finds a dictionary (a set of atoms) that can best be used to represent data using a sparse code.

Solves the optimization problem:

\[
(U^*, V^*) = \arg\min_{U, V} \frac{1}{2} || Y - U V ||_2^2 + \alpha \sum || U ||_1
\]

with \( || V_k ||_2 = 1 \) for all \( 0 \leq k < n\_components \)

Read more in the User Guide.

**Parameters** n_components : int,
number of dictionary elements to extract

**alpha** : float,

sparsity controlling parameter

**n_iter** : int,

total number of iterations to perform

**fit_algorithm** : {'lars', 'cd'}

lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path) cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

**n_jobs** : int,

number of parallel jobs to run

**batch_size** : int,

number of samples in each mini-batch

**shuffle** : bool,

whether to shuffle the samples before forming batches

**dict_init** : array of shape (n_components, n_features),

initial value of the dictionary for warm restart scenarios

**transform_algorithm** : {'lasso_lars', 'lasso_cd', 'lars', 'omp', 'threshold'}

Algorithm used to transform the data. lars: uses the least angle regression method (linear_model.lars_path) lasso_lars: uses Lars to compute the Lasso solution lasso_cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). lasso_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection dictionary * X'

**transform_n_nonzero_coefs** : int, 0.1 * n_features by default

Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the omp case.

**transform_alpha** : float, 1. by default

If algorithm='lasso_lars' or algorithm='lasso_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n_nonzero_coefs.

**verbose** : bool, optional (default: False)

To control the verbosity of the procedure.

**split_sign** : bool, False by default

Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Attributes

| components | (array, [n_components, n_features]) components extracted from the data |
| inner_stats | (tuple of (A, B) ndarrays) Internal sufficient statistics that are kept by the algorithm. Keeping them is useful in online settings, to avoid loosing the history of the evolution, but they shouldn’t have any use for the end user. A (n_components, n_components) is the dictionary covariance matrix. B (n_features, n_components) is the data approximation matrix |
| n_iter | (int) Number of iterations run |

See also:

SparseCoder, DictionaryLearning, SparsePCA, MiniBatchSparsePCA

Notes

References:


Methods

| fit(X[, y]) | Fit the model from data in X. |
| fit_transform(X[, y]) | Fit to data, then transform it. |
| get_params([deep]) | Get parameters for this estimator. |
| partial_fit(X[, y, iter_offset]) | Updates the model using the data in X as a mini-batch. |
| set_params(**params) | Set the parameters of this estimator. |
| transform(X) | Encode the data as a sparse combination of the dictionary atoms. |

__init__(n_components=None, alpha=1, n_iter=1000, fit_algorithm='lars', n_jobs=1, batch_size=3, shuffle=True, dict_init=None, transform_algorithm='omp', transform_n_nonzero_coefs=None, transform_alpha=None, verbose=False, split_sign=False, random_state=None)

fit (X, y=None)
Fit the model from data in X.

Parameters

| X : array-like, shape (n_samples, n_features) |
| Training vector, where n_samples is the number of samples and n_features is the number of features |
| y : Ignored |

Returns

| self : object |
Returns the instance itself.

**fit_transform** *(X, y=None, **fit_params)*

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

- **Parameters**
  - **X**: numpy array of shape [n_samples, n_features]
    - Training set.
  - **y**: numpy array of shape [n_samples]
    - Target values.
  - **Returns**
    - **X_new**: numpy array of shape [n_samples, n_features_new]
      - Transformed array.

**get_params** *(deep=True)*

Get parameters for this estimator.

- **Parameters**
  - **deep**: boolean, optional
    - If True, will return the parameters for this estimator and contained subobjects that are estimators.
  - **Returns**
    - **params**: mapping of string to any
      - Parameter names mapped to their values.

**partial_fit** *(X, y=None, iter_offset=None)*

Updates the model using the data in X as a mini-batch.

- **Parameters**
  - **X**: array-like, shape (n_samples, n_features)
    - Training vector, where n_samples in the number of samples and n_features is the number of features.
  - **y**: Ignored
  - **iter_offset**: integer, optional
    - The number of iteration on data batches that has been performed before this call to partial_fit. This is optional: if no number is passed, the memory of the object is used.
  - **Returns**
    - **self**: object
      - Returns the instance itself.

**set_params** *(**params)*

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

- **Returns**
  - **self**: object

**transform** *(X)*

Encode the data as a sparse combination of the dictionary atoms.

Coding method is determined by the object parameter `transform_algorithm`.

- **Parameters**
  - **X**: array of shape (n_samples, n_features)
    - Test data to be transformed, must have the same number of features as the data used to train the model.
Returns `X_new` : array, shape (n_samples, n_components)
Transformed data

Examples using `sklearn.decomposition.MiniBatchDictionaryLearning`

- Image denoising using dictionary learning
- Faces dataset decompositions

30.8.8 `sklearn.decomposition.MiniBatchSparsePCA`

class `sklearn.decomposition.MiniBatchSparsePCA`

Mini-batch Sparse Principal Components Analysis

Finds the set of sparse components that can optimally reconstruct the data. The amount of sparseness is controllable by the coefficient of the L1 penalty, given by the parameter alpha.

Read more in the User Guide.

Parameters

`n_components` : int,
number of sparse atoms to extract

`alpha` : int,
Sparsity controlling parameter. Higher values lead to sparser components.

`ridge_alpha` : float,
Amount of ridge shrinkage to apply in order to improve conditioning when calling the transform method.

`n_iter` : int,
number of iterations to perform for each mini batch

`callback` : callable or None, optional (default: None)
callable that gets invoked every five iterations

`batch_size` : int,
the number of features to take in each mini batch

`verbose` : int
Controls the verbosity; the higher, the more messages. Defaults to 0.

`shuffle` : boolean,
whether to shuffle the data before splitting it in batches

`n_jobs` : int,
number of parallel jobs to run, or -1 to autodetect.

`method` : {‘lars’, ‘cd’}
lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path) cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>components_</td>
<td>(array, [n_components, n_features]) Sparse components extracted from the data.</td>
</tr>
<tr>
<td>error_</td>
<td>(array) Vector of errors at each iteration.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Number of iterations run.</td>
</tr>
</tbody>
</table>

**See also:**

PCA, SparsePCA, DictionaryLearning

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
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</tr>
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<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Fit the model from data in X.</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>set_params(*params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X[, ridge_alpha])</td>
<td>Least Squares projection of the data onto the sparse components.</td>
</tr>
</tbody>
</table>

**__init__**

(n_components=None, alpha=1, ridge_alpha=0.01, n_iter=100, callback=None, batch_size=3, verbose=False, shuffle=True, n_jobs=1, method='lars', random_state=None)

**fit (X, y=None)**

Fit the model from data in X.

Parameters

- **X**: array-like, shape (n_samples, n_features)
  Training vector, where n_samples in the number of samples and n_features is the number of features.
  
- **y**: Ignored

Returns

- **self**: object
  Returns the instance itself.

**fit_transform (X, y=None, **fit_params)**

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters

- **X**: numpy array of shape [n_samples, n_features]
  Training set.
  
- **y**: numpy array of shape [n_samples]
Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]
Transformed array.

going params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

going params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns self

transform (X, ridge_alpha='deprecated')
Least Squares projection of the data onto the sparse components.

To avoid instability issues in case the system is under-determined, regularization can be applied (Ridge
regression) via the ridge_alpha parameter.

Note that Sparse PCA components orthogonality is not enforced as in PCA hence one cannot use a simple
linear projection.

Parameters X : array of shape (n_samples, n_features)
Test data to be transformed, must have the same number of features as the data used to
train the model.

ridge_alpha : float, default: 0.01
Amount of ridge shrinkage to apply in order to improve conditioning.

Depreciated since version 0.19: This parameter will be removed in 0.21. Specify
ridge_alpha in the SparsePCA constructor.

Returns X_new array, shape (n_samples, n_components)
Transformed data.

Examples using sklearn.decomposition.MiniBatchSparsePCA
• Faces dataset decompositions

30.8.9 sklearn.decomposition.NMF

class sklearn.decomposition.NMF (n_components=None, init=None, solver='cd',
beta_loss='frobenius', tol=0.0001, max_iter=200, random_state=None, alpha=0.0, l1_ratio=0.0, verbose=0, shuffle=False)

Non-Negative Matrix Factorization (NMF)
Find two non-negative matrices (W, H) whose product approximates the non-negative matrix X. This factorization can be used for example for dimensionality reduction, source separation or topic extraction.

The objective function is:

\[
0.5 \times ||X - WH||_{\text{Fro}}^2 \\
+ \alpha \times \text{l1\_ratio} \times ||\text{vec}(W)||_1 \\
+ \alpha \times \text{l1\_ratio} \times ||\text{vec}(H)||_1 \\
+ 0.5 \times \alpha \times (1 - \text{l1\_ratio}) \times ||W||_{\text{Fro}}^2 \\
+ 0.5 \times \alpha \times (1 - \text{l1\_ratio}) \times ||H||_{\text{Fro}}^2
\]

Where:

\[
||A||_{\text{Fro}}^2 = \sum_{i,j} A_{ij}^2 \text{ (Frobenius norm)} \\
||\text{vec}(A)||_1 = \sum_{i,j} \text{abs}(A_{ij}) \text{ (Elementwise L1 norm)}
\]

For multiplicative-update (‘mu’) solver, the Frobenius norm (0.5 * ||X - WH||_{Fro}^2) can be changed into another beta-divergence loss, by changing the beta_loss parameter.

The objective function is minimized with an alternating minimization of W and H.

Read more in the User Guide.

**Parameters**

**n_components**: int or None

Number of components, if n_components is not set all features are kept.

**init**: ‘random’ | ‘nndsvd’ | ‘nndsvda’ | ‘nndsvdar’ | ‘custom’

Method used to initialize the procedure. Default: ‘nndsvd’ if n_components < n_features, otherwise random. Valid options:

- ‘random’: non-negative random matrices, scaled with: \(\sqrt{X.\text{mean()}} / \sqrt{n\_\text{components}}\)
- ‘nndsvd’: Nonnegative Double Singular Value Decomposition (NNDSVD) initialization (better for sparseness)
- ‘nndsvda’: NNDSVD with zeros filled with the average of X (better when sparsity is not desired)
- ‘nndsvdar’: NNDSVD with zeros filled with small random values (generally faster, less accurate alternative to NNDSVDa for when sparsity is not desired)
- ‘custom’: use custom matrices W and H

**solver**: ‘cd’ | ‘mu’

Numerical solver to use: ‘cd’ is a Coordinate Descent solver. ‘mu’ is a Multiplicative Update solver.

New in version 0.17: Coordinate Descent solver.

New in version 0.19: Multiplicative Update solver.

**beta_loss**: float or string, default ‘frobenius’

String must be in {'frobenius', 'kullback-leibler', 'itakura-saito'}. Beta divergence to be minimized, measuring the distance between X and the dot product WH. Note that values different from ‘frobenius’ (or 2) and ‘kullback-leibler’ (or 1) lead to significantly slower fits. Note that for beta_loss <= 0 (or ‘itakura-saito’), the input matrix X cannot contain zeros. Used only in ‘mu’ solver.

New in version 0.19.
tol : float, default: 1e-4
   Tolerance of the stopping condition.
max_iter : integer, default: 200
   Maximum number of iterations before timing out.
random_state : int, RandomState instance or None, optional, default: None
   If int, random_state is the seed used by the random number generator; If RandomState
   instance, random_state is the random number generator; If None, the random number
   generator is the RandomState instance used by np.random.
alpha : double, default: 0.
   Constant that multiplies the regularization terms. Set it to zero to have no regularization.
   New in version 0.17: alpha used in the Coordinate Descent solver.
l1_ratio : double, default: 0.
   The regularization mixing parameter, with 0 <= l1_ratio <= 1. For l1_ratio = 0 the
   penalty is an elementwise L2 penalty (aka Frobenius Norm). For l1_ratio = 1 it is an
   elementwise L1 penalty. For 0 < l1_ratio < 1, the penalty is a combination of L1 and
   L2.
   New in version 0.17: Regularization parameter l1_ratio used in the Coordinate Descent
   solver.
verbose : bool, default=False
   Whether to be verbose.
shuffle : boolean, default: False
   If true, randomize the order of coordinates in the CD solver.
   New in version 0.17: shuffle parameter used in the Coordinate Descent solver.

Attributes

<table>
<thead>
<tr>
<th>components_</th>
<th>(array, [n_components, n_features]) Factorization matrix, sometimes called 'dictionary'.</th>
</tr>
</thead>
<tbody>
<tr>
<td>reconstruction_err_</td>
<td>(number) Frobenius norm of the matrix difference, or beta-divergence, between the training data X and the reconstructed data WH from the fitted model.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Actual number of iterations.</td>
</tr>
</tbody>
</table>

References

Cichocki, Andrzej, and P. H. A. N. Anh-Huy. “Fast local algorithms for large scale nonnegative matrix and ten-
sor factorizations,” IEICE transactions on fundamentals of electronics, communications and computer sciences

Computation, 23(9).
Examples

```python
>>> import numpy as np
>>> X = np.array([[1, 1], [2, 1], [3, 1.2], [4, 1], [5, 0.8], [6, 1]])
>>> from sklearn.decomposition import NMF
>>> model = NMF(n_components=2, init='random', random_state=0)
>>> W = model.fit_transform(X)
>>> H = model.components_
```

Methods

- `fit(X[, y])`: Learn a NMF model for the data X.
- `fit_transform(X[, y, W, H])`: Learn a NMF model for the data X and returns the transformed data.
- `get_params([deep])`: Get parameters for this estimator.
- `inverse_transform(W)`: Transform data back to its original space.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(X)`: Transform the data X according to the fitted NMF model

```python
__init__(n_components=None, init=None, solver='cd', beta_loss='frobenius', tol=0.0001, max_iter=200, random_state=None, alpha=0.0, l1_ratio=0.0, verbose=0, shuffle=False)

fit(X, y=None, **params)
Learn a NMF model for the data X.

Parameters

X : {array-like, sparse matrix}, shape (n_samples, n_features)
Data matrix to be decomposed

y : Ignored

Returns

self

fit_transform(X, y=None, W=None, H=None)
Learn a NMF model for the data X and returns the transformed data.

This is more efficient than calling fit followed by transform.

Parameters

X : {array-like, sparse matrix}, shape (n_samples, n_features)
Data matrix to be decomposed

y : Ignored

W : array-like, shape (n_samples, n_components)
If init='custom', it is used as initial guess for the solution.

H : array-like, shape (n_components, n_features)
If init='custom', it is used as initial guess for the solution.

Returns

W : array, shape (n_samples, n_components)
Transformed data.
```

```python
get_params(deep=True)
Get parameters for this estimator.

Parameters

deep : boolean, optional
```
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

inverse_transform(W)

Transform data back to its original space.

Parameters W : {array-like, sparse matrix}, shape (n_samples, n_components)

Transformed data matrix

Returns X : {array-like, sparse matrix}, shape (n_samples, n_features)

Data matrix of original shape

New in version 0.18.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

transform(X)

Transform the data X according to the fitted NMF model

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)

Data matrix to be transformed by the model

Returns W : array, shape (n_samples, n_components)

Transformed data

Examples using sklearn.decomposition.NMF

- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Faces dataset decompositions

30.8.10 sklearn.decomposition.PCA

class sklearn.decomposition.PCA(n_components=None, copy=True, whiten=False, svd_solver='auto', tol=0.0, iterated_power='auto', random_state=None)

Principal component analysis (PCA)

Linear dimensionality reduction using Singular Value Decomposition of the data to project it to a lower dimensional space.

It uses the LAPACK implementation of the full SVD or a randomized truncated SVD by the method of Halko et al. 2009, depending on the shape of the input data and the number of components to extract.

It can also use the scipy.sparse.linalg ARPACK implementation of the truncated SVD.

Notice that this class does not support sparse input. See TruncatedSVD for an alternative with sparse data.
Parameters **n_components**: int, float, None or string

Number of components to keep. If n_components is not set all components are kept:

\[
\text{n_components} = \min(\text{n_samples}, \text{n_features})
\]

If n_components == 'mle' and svd_solver == 'full', Minka’s MLE is used to guess the dimension. Use of n_components == 'mle' will interpret svd_solver == 'auto' as svd_solver == 'full'.

If 0 < n_components < 1 and svd_solver == 'full', select the number of components such that the amount of variance that needs to be explained is greater than the percentage specified by n_components.

If svd_solver == 'arpack', the number of components must be strictly less than the minimum of n_features and n_samples.

Hence, the None case results in:

\[
\text{n_components} = \min(\text{n_samples}, \text{n_features}) - 1
\]

copy : bool (default True)

If False, data passed to fit are overwritten and running fit(X).transform(X) will not yield the expected results, use fit_transform(X) instead.

whiten : bool, optional (default False)

When True (False by default) the components vectors are multiplied by the square root of n_samples and then divided by the singular values to ensure uncorrelated outputs with unit component-wise variances.

Whitening will remove some information from the transformed signal (the relative variance scales of the components) but can sometime improve the predictive accuracy of the downstream estimators by making their data respect some hard-wired assumptions.


- **auto**: the solver is selected by a default policy based on X.shape and n_components: if the input data is larger than 500x500 and the number of components to extract is lower than 80% of the smallest dimension of the data, then the more efficient ‘randomized’ method is enabled. Otherwise the exact full SVD is computed and optionally truncated afterwards.

- **full**: run exact full SVD calling the standard LAPACK solver via scipy.linalg.svd and select the components by postprocessing

- **arpack**: run SVD truncated to n_components calling ARPACK solver via scipy.sparse.linalg.svds. It requires strictly 0 < n_components < min(X.shape)

- **randomized**: run randomized SVD by the method of Halko et al.

New in version 0.18.0.

tol : float >= 0, optional (default .0)

Tolerance for singular values computed by svd_solver == ‘arpack’.

New in version 0.18.0.

iterated_power : int >= 0, or ‘auto’, (default ‘auto’)
Number of iterations for the power method computed by svd_solver == ‘randomized’.

New in version 0.18.0.

random_state : int, RandomState instance or None, optional (default None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when svd_solver == ‘arpack’ or ‘randomized’.

New in version 0.18.0.

Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>components</td>
<td>(array, shape (n_components, n_features)) Principal axes in feature space, representing the directions of maximum variance in the data. The components are sorted by explained_variance_.</td>
</tr>
<tr>
<td>explained_variance_</td>
<td>(array, shape (n_components,)) The amount of variance explained by each of the selected components. Equal to n_components largest eigenvalues of the covariance matrix of X. .. versionadded:: 0.18</td>
</tr>
<tr>
<td>explained_variance_ratio_</td>
<td>(array, shape (n_components,)) Percentage of variance explained by each of the selected components. If n_components is not set then all components are stored and the sum of the ratios is equal to 1.0.</td>
</tr>
<tr>
<td>singular_values_</td>
<td>(array, shape (n_components,)) The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n_components variables in the lower-dimensional space.</td>
</tr>
<tr>
<td>mean_</td>
<td>(array, shape (n_features,)) Per-feature empirical mean, estimated from the training set. Equal to X.mean(axis=0).</td>
</tr>
<tr>
<td>n_components</td>
<td>The estimated number of components. When n_components is set to ‘mle’ or a number between 0 and 1 (with svd_solver == ‘full’) this number is estimated from input data. Otherwise it equals the parameter n_components, or the lesser value of n_features and n_samples if n_components is None.</td>
</tr>
<tr>
<td>noise_variance_</td>
<td>The estimated noise covariance following the Probabilistic PCA model from Tipping and Bishop 1999. See “Pattern Recognition and Machine Learning” by C. Bishop, 12.2.1 p. 574 or <a href="http://www.miketipping.com/papers/met-mppca.pdf">http://www.miketipping.com/papers/met-mppca.pdf</a>. It is required to computed the estimated data covariance and score samples. Equal to the average of (min(n_features, n_samples) - n_components) smallest eigenvalues of the covariance matrix of X.</td>
</tr>
</tbody>
</table>

See also:

KernelPCA, SparsePCA, TruncatedSVD, IncrementalPCA

References

For n_components == ‘mle’, this class uses the method of Thomas P. Minka: Automatic Choice of Dimensionality for PCA. NIPS 2000: 598-604


For svd_solver == ‘arpack’, refer to scipy.sparse.linalg.svds.

Examples

```python
>>> import numpy as np
>>> from sklearn.decomposition import PCA
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> pca = PCA(n_components=2)
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=2, random_state=None,
    svd_solver='auto', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.99244... 0.00755...]
>>> print(pca.singular_values_)
[6.30061... 0.54980...]

>>> pca = PCA(n_components=2, svd_solver='full')
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=2, random_state=None,
    svd_solver='full', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.99244... 0.00755...]
>>> print(pca.singular_values_)
[6.30061... 0.54980...]

>>> pca = PCA(n_components=1, svd_solver='arpack')
>>> pca.fit(X)
PCA(copy=True, iterated_power='auto', n_components=1, random_state=None,
    svd_solver='arpack', tol=0.0, whiten=False)
>>> print(pca.explained_variance_ratio_)
[0.99244...]
>>> print(pca.singular_values_)
[6.30061...]
```

Methods

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Fit the model with X.</td>
</tr>
<tr>
<td><code>fit_transform(X[, y])</code></td>
<td>Fit the model with X and apply the dimensionality reduction on X.</td>
</tr>
<tr>
<td><code>get_covariance()</code></td>
<td>Compute data covariance with the generative model.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>get_precision()</code></td>
<td>Compute data precision matrix with the generative model.</td>
</tr>
<tr>
<td><code>inverse_transform(X)</code></td>
<td>Transform data back to its original space.</td>
</tr>
<tr>
<td><code>score(X[, y])</code></td>
<td>Return the average log-likelihood of all samples.</td>
</tr>
<tr>
<td><code>score_samples(X)</code></td>
<td>Return the log-likelihood of each sample.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Apply dimensionality reduction to X.</td>
</tr>
</tbody>
</table>
__init__ (n_components=None, copy=True, whiten=False, svd_solver='auto', tol=0.0, iterated_power='auto', random_state=None)

fit (X, y=None)
Fit the model with X.

Parameters X : array-like, shape (n_samples, n_features)
Training data, where n_samples in the number of samples and n_features is the number of features.

y : Ignored

Returns self : object
Returns the instance itself.

fit_transform (X, y=None)
Fit the model with X and apply the dimensionality reduction on X.

Parameters X : array-like, shape (n_samples, n_features)
Training data, where n_samples is the number of samples and n_features is the number of features.

y : Ignored

Returns X_new : array-like, shape (n_samples, n_components)

get_covariance()
Compute data covariance with the generative model.

cov = components_.T * S**2 * components_ + sigma2 * eye(n_features)
where S**2 contains the explained variances, and sigma2 contains the noise variances.

Returns cov : array, shape=(n_features, n_features)
Estimated covariance of data.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_precision()
Compute data precision matrix with the generative model.

Equals the inverse of the covariance but computed with the matrix inversion lemma for efficiency.

Returns precision : array, shape=(n_features, n_features)
Estimated precision of data.

inverse_transform (X)
Transform data back to its original space.
In other words, return an input X_original whose transform would be X.

Parameters X : array-like, shape (n_samples, n_components)
New data, where n_samples is the number of samples and n_components is the number of components.

**Returns** X_original array-like, shape (n_samples, n_features)

**Notes**

If whitening is enabled, inverse_transform will compute the exact inverse operation, which includes reversing whitening.

**score** *(X, y=None)*

Return the average log-likelihood of all samples.


**Parameters**

- **X**: array, shape (n_samples, n_features)
  
  The data.

- **y**: Ignored

**Returns** **ll** : float

Average log-likelihood of the samples under the current model

**score_samples** *(X)*

Return the log-likelihood of each sample.


**Parameters**

- **X**: array, shape (n_samples, n_features)
  
  The data.

**Returns** **ll** : array, shape (n_samples,)

Log-likelihood of each sample under the current model

**set_params** *(**params**)*

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Apply dimensionality reduction to X.

X is projected on the first principal components previously extracted from a training set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)

  New data, where n_samples is the number of samples and n_features is the number of features.

**Returns** **X_new** : array-like, shape (n_samples, n_components)
Examples

```python
>>> import numpy as np
>>> from sklearn.decomposition import IncrementalPCA

>>> X = np.array([[−1, −1], [−2, −1], [−3, −2], [1, 1], [2, 1], [3, 2]])
>>> ipca = IncrementalPCA(n_components=2, batch_size=3)
>>> ipca.fit(X)
IncrementalPCA(batch_size=3, copy=True, n_components=2, whiten=False)
>>> ipca.transform(X)
```

Examples using `sklearn.decomposition.PCA`

- Concatenating multiple feature extraction methods
- Pipelining: chaining a PCA and a logistic regression
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Multilabel classification
- Explicit feature map approximation for RBF kernels
- Faces recognition example using eigenfaces and SVMs
- A demo of K-Means clustering on the handwritten digits data
- The Iris Dataset
- PCA example with Iris Data-set
- Incremental PCA
- Comparison of LDA and PCA 2D projection of Iris dataset
- Blind source separation using FastICA
- Principal components analysis (PCA)
- FastICA on 2D point clouds
- Kernel PCA
- Model selection with Probabilistic PCA and Factor Analysis (FA)
- Faces dataset decompositions
- Multi-dimensional scaling
- Kernel Density Estimation
- Using FunctionTransformer to select columns
- Importance of Feature Scaling

### 30.8.11 sklearn.decomposition.SparsePCA

class `sklearn.decomposition.SparsePCA`(n_components=None, alpha=1, ridge_alpha=0.01, max_iter=1000, tol=1e-08, method='lars', n_jobs=1, U_init=None, V_init=None, verbose=False, random_state=None)

Sparse Principal Components Analysis (SparsePCA)
Finds the set of sparse components that can optimally reconstruct the data. The amount of sparseness is controllable by the coefficient of the L1 penalty, given by the parameter alpha.

Read more in the User Guide.

Parameters:

**n_components** : int,
Number of sparse atoms to extract.

**alpha** : float,
Sparsity controlling parameter. Higher values lead to sparser components.

**ridge_alpha** : float,
Amount of ridge shrinkage to apply in order to improve conditioning when calling the transform method.

**max_iter** : int,
Maximum number of iterations to perform.

**tol** : float,
Tolerance for the stopping condition.

**method** : {'lars', 'cd'}
lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path) cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

**n_jobs** : int,
Number of parallel jobs to run.

**U_init** : array of shape (n_samples, n_components),
Initial values for the loadings for warm restart scenarios.

**V_init** : array of shape (n_components, n_features),
Initial values for the components for warm restart scenarios.

**verbose** : int
Controls the verbosity; the higher, the more messages. Defaults to 0.

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Attributes

| components_ | (array, [n_components, n_features]) Sparse components extracted from the data. |
| error_ | (array) Vector of errors at each iteration. |
| n_iter_ | (int) Number of iterations run. |

See also:

PCA, MiniBatchSparsePCA, DictionaryLearning
## Methods

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<tr>
<td><code>transform(X[, ridge_alpha])</code></td>
<td>Least Squares projection of the data onto the sparse components.</td>
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```python
__init__ (n_components=None, alpha=1, ridge_alpha=0.01, max_iter=1000, tol=1e-08, method='lars', n_jobs=1, U_init=None, V_init=None, verbose=False, random_state=None)
```

`fit (X, y=None)`
Fit the model from data in X.

**Parameters**
- `X` : array-like, shape (n_samples, n_features)
  Training vector, where n_samples in the number of samples and n_features is the number of features.
- `y` : Ignored

**Returns**
- `self` : object
  Returns the instance itself.

`fit_transform (X, y=None, **fit_params)`
Fit to data, then transform it.
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**
- `X` : numpy array of shape [n_samples, n_features]
  Training set.
- `y` : numpy array of shape [n_samples]
  Target values.

**Returns**
- `X_new` : numpy array of shape [n_samples, n_features_new]
  Transformed array.

`get_params (deep=True)`
Get parameters for this estimator.

**Parameters**
- `deep` : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- `params` : mapping of string to any
  Parameter names mapped to their values.

`set_params (**params)`
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**
- `self`
transform \((X, \text{ridge\_alpha}='\text{deprecated}')\)

Least Squares projection of the data onto the sparse components.

To avoid instability issues in case the system is under-determined, regularization can be applied (Ridge regression) via the \text{ridge\_alpha} parameter.

Note that Sparse PCA components orthogonality is not enforced as in PCA hence one cannot use a simple linear projection.

**Parameters**

- **X**: array of shape \((n\_samples, n\_features)\)
  Test data to be transformed, must have the same number of features as the data used to train the model.

- **ridge\_alpha**: float, default: 0.01
  Amount of ridge shrinkage to apply in order to improve conditioning.
  Deprecated since version 0.19: This parameter will be removed in 0.21. Specify ridge\_alpha in the SparsePCA constructor.

**Returns**

- **X\_new**: array, shape \((n\_samples, n\_components)\)
  Transformed data.

### 30.8.12 sklearn.decomposition.SparseCoder

**class** sklearn.decomposition.SparseCoder(*dictionary*, **transform\_algorithm='omp'**, **transform\_n\_nonzero\_coeffs=None**, **transform\_alpha=None**, **split\_sign=False**, **n\_jobs=1**)

Sparse coding

Finds a sparse representation of data against a fixed, precomputed dictionary.

Each row of the result is the solution to a sparse coding problem. The goal is to find a sparse array \text{code} such that:

\[
X \approx \text{code} \times \text{dictionary}
\]

Read more in the User Guide.

**Parameters**

- **dictionary**: array, \([n\_components, n\_features]\)
  The dictionary atoms used for sparse coding. Lines are assumed to be normalized to unit norm.

- **transform\_algorithm**: \{'lasso\_lars', 'lasso\_cd', 'lars', 'omp', 'threshold'\}
  Algorithm used to transform the data: lars: uses the least angle regression method (linear\_model.lars\_path) lasso\_lars: uses Lars to compute the Lasso solution lasso\_cd: uses the coordinate descent method to compute the Lasso solution (linear\_model.Lasso). lasso\_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection \text{dictionary} \times X'\`

- **transform\_n\_nonzero\_coeffs**: int, \(0.1 \times n\_features\) by default
  Number of nonzero coefficients to target in each column of the solution. This is only used by \text{algorithm}='lars' and \text{algorithm}='omp' and is overridden by alpha in the omp case.

- **transform\_alpha**: float, 1. by default
If `algorithm='lasso_lars'` or `algorithm='lasso_cd'`, `alpha` is the penalty applied to the L1 norm. If `algorithm='threshold'`, `alpha` is the absolute value of the threshold below which coefficients will be squashed to zero. If `algorithm='omp'`, `alpha` is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides `n_nonzero_coefs`.

**split_sign** : bool, False by default

Whether to split the sparse feature vector into the concatenation of its negative part and its positive part. This can improve the performance of downstream classifiers.

**n_jobs** : int,

number of parallel jobs to run

### Attributes

| components_ | (array, [n_components, n_features]) The unchanged dictionary atoms |

See also:

- DictionaryLearning
- MiniBatchDictionaryLearning
- SparsePCA
- MiniBatchSparsePCA
- sparse_encode

### Methods

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<td>fit(X[, y])</td>
<td>Do nothing and return the estimator unchanged</td>
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<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
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<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Encode the data as a sparse combination of the dictionary atoms.</td>
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**__init__**(dictionary, transform_algorithm='omp', transform_n_nonzero_coefs=None, transform_alpha=None, split_sign=False, n_jobs=1)

**fit**(X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

**Parameters**

- **X** : Ignored
- **y** : Ignored

**Returns**

- **self** : object

Returns the object itself

**fit_transform**(X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X** : numpy array of shape [n_samples, n_features]

Training set.
y: numpy array of shape [n_samples]

Target values.

Returns X_new: numpy array of shape [n_samples, n_features_new]

Transformed array.

get_params(deep=True)

Get parameters for this estimator.

Parameters:

depth: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns:

params: mapping of string to any

Parameter names mapped to their values.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns:

self

transform(X)

Encode the data as a sparse combination of the dictionary atoms.

Coding method is determined by the object parameter transform_algorithm.

Parameters:

X: array of shape (n_samples, n_features)

Test data to be transformed, must have the same number of features as the data used to
train the model.

Returns:

X_new: array, shape (n_samples, n_components)

Transformed data

Examples using sklearn.decomposition.SparseCoder

- Sparse coding with a precomputed dictionary

30.8.13 sklearn.decomposition.TruncatedSVD

class sklearn.decomposition.TruncatedSVD(n_components=2, algorithm='randomized', n_iter=5, random_state=None, tol=0.0)

Dimensionality reduction using truncated SVD (aka LSA).

This transformer performs linear dimensionality reduction by means of truncated singular value decomposition
(SVD). Contrary to PCA, this estimator does not center the data before computing the singular value decompo-
sition. This means it can work with scipy.sparse matrices efficiently.

In particular, truncated SVD works on term count/tf-idf matrices as returned by the vectorizers in
sklearn.feature_extraction.text. In that context, it is known as latent semantic analysis (LSA).

This estimator supports two algorithms: a fast randomized SVD solver, and a “naive” algorithm that uses
ARPACK as an eigensolver on (X * X.T) or (X.T * X), whichever is more efficient.
Parameters **n_components**: int, default = 2

Desired dimensionality of output data. Must be strictly less than the number of features. The default value is useful for visualisation. For LSA, a value of 100 is recommended.

**algorithm**: string, default = “randomized”

SVD solver to use. Either “arpack” for the ARPACK wrapper in SciPy (scipy.sparse.linalg.svds), or “randomized” for the randomized algorithm due to Halko (2009).

**n_iter**: int, optional (default 5)

Number of iterations for randomized SVD solver. Not used by ARPACK. The default is larger than the default in randomized_svd to handle sparse matrices that may have large slowly decaying spectrum.

**random_state**: int, RandomState instance or None, optional, default = None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**tol**: float, optional

Tolerance for ARPACK. 0 means machine precision. Ignored by randomized SVD solver.

Attributes

| components_ | (array, shape (n_components, n_features)) |
| explained_variance_ | (array, shape (n_components,)) The variance of the training samples transformed by a projection to each component. |
| explained_variance_ratio_ | (array, shape (n_components,)) Percentage of variance explained by each of the selected components. |
| singular_values_ | (array, shape (n_components,)) The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n_components variables in the lower-dimensional space. |

See also:

*PCA*, *RandomizedPCA*

Notes

SVD suffers from a problem called “sign indeterminacy”, which means the sign of the components_ and the output from transform depend on the algorithm and random state. To work around this, fit instances of this class to data once, then keep the instance around to do transformations.

References

Examples

```python
>>> from sklearn.decomposition import TruncatedSVD
>>> from sklearn.random_projection import sparse_random_matrix

>>> X = sparse_random_matrix(100, 100, density=0.01, random_state=42)
>>> svd = TruncatedSVD(n_components=5, n_iter=7, random_state=42)
>>> svd.fit(X)
TruncatedSVD(algorithm='randomized', n_components=5, n_iter=7,
            random_state=42, tol=0.0)
>>> print(svd.explained_variance_ratio_)
[ 0.0606... 0.0584... 0.0497... 0.0434... 0.0372...]
>>> print(svd.explained_variance_ratio_.sum())
0.249...
>>> print(svd.singular_values_)
[ 2.5841... 2.5245... 2.3201... 2.1753... 2.0443...]
```

Methods

- `fit(X[, y])`: Fit LSI model on training data X.
- `fit_transform(X[, y])`: Fit LSI model to X and perform dimensionality reduction on X.
- `get_params([deep])`: Get parameters for this estimator.
- `inverse_transform(X)`: Transform X back to its original space.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(X)`: Perform dimensionality reduction on X.

```python
def __init__(n_components=2, algorithm='randomized', n_iter=5, random_state=None, tol=0.0)
def fit(X, y=None)
    Fit LSI model on training data X.

    Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
        Training data.
    y : Ignored
        Returns self : object
        Returns the transformer object.

def fit_transform(X, y=None)
    Fit LSI model to X and perform dimensionality reduction on X.

    Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
        Training data.
    y : Ignored
        Returns X_new : array, shape (n_samples, n_components)
        Reduced version of X. This will always be a dense array.

def get_params(deep=True)
    Get parameters for this estimator.

    Parameters deep : boolean, optional
```

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If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any
Parameter names mapped to their values.

inverse_transform(X)
Transform X back to its original space.

Returns an array X_original whose transform would be X.

**Parameters** X : array-like, shape (n_samples, n_components)
New data.

**Returns** X_original : array, shape (n_samples, n_features)
Note that this is always a dense array.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

**Returns** self

transform(X)
Perform dimensionality reduction on X.

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features)
New data.

**Returns** X_new : array, shape (n_samples, n_components)
Reduced version of X. This will always be a dense array.

**Examples using sklearn.decomposition.TruncatedSVD**

- Feature Union with Heterogeneous Data Sources
- Hashing feature transformation using Totally Random Trees
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
- Clustering text documents using k-means

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<td>decomposition.fastica(X[, n_components, ...])</td>
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30.8.14 sklearn.decomposition.dict_learning

sklearn.decomposition.dict_learning(X, n_components, alpha, max_iter=100, tol=1e-08, method='lars', n_jobs=1, dict_init=None, code_init=None, callback=None, verbose=False, random_state=None, return_n_iter=False)

Solves a dictionary learning matrix factorization problem.

Finds the best dictionary and the corresponding sparse code for approximating the data matrix X by solving:

\[(U^*, V^*) = \arg\min_{(U,V)} 0.5 \| X - UV \|_2^2 + \alpha \| U \|_1\]

with \| V_k \|_2 = 1 for all 0 <= k < n_components

where V is the dictionary and U is the sparse code.

Read more in the User Guide.

Parameters

- X : array of shape (n_samples, n_features)
  Data matrix.

- n_components : int,
  Number of dictionary atoms to extract.

- alpha : int,
  Sparsity controlling parameter.

- max_iter : int,
  Maximum number of iterations to perform.

- tol : float,
  Tolerance for the stopping condition.

- method : {'lars', 'cd'}
  lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path) cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

- n_jobs : int,
  Number of parallel jobs to run, or -1 to autodetect.

- dict_init : array of shape (n_components, n_features),
  Initial value for the dictionary for warm restart scenarios.

- code_init : array of shape (n_samples, n_components),
  Initial value for the sparse code for warm restart scenarios.

- callback : callable or None, optional (default: None)
  Callable that gets invoked every five iterations

- verbose : bool, optional (default: False)
  To control the verbosity of the procedure.

- random_state : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

:return_n_iter : bool
   Whether or not to return the number of iterations.

Returns

code : array of shape (n_samples, n_components)
   The sparse code factor in the matrix factorization.

dictionary : array of shape (n_components, n_features),
   The dictionary factor in the matrix factorization.

ersors : array
   Vector of errors at each iteration.

n_iter : int
   Number of iterations run. Returned only if return_n_iter is set to True.

See also:

dict_learning_online, DictionaryLearning, MiniBatchDictionaryLearning, SparsePCA, MiniBatchSparsePCA

30.8.15 sklearn.decomposition.dict_learning_online

sklearn.decomposition.dict_learning_online(X, n_components=2, alpha=1, n_iter=100, return_code=True, dict_init=None, callback=None, batch_size=3, verbose=False, shuffle=True, n_jobs=1, method='lars', return_n_iter=False)

Solves a dictionary learning matrix factorization problem online.

Finds the best dictionary and the corresponding sparse code for approximating the data matrix X by solving:

\[(U^*, V^*) = \arg\min_{(U,V)} 0.5 \| X - U V \|^2_2 + \alpha \| U \|_1 \]

with \| V_k \|^2_2 = 1 for all 0 \leq k < n_components

where V is the dictionary and U is the sparse code. This is accomplished by repeatedly iterating over mini-batches by slicing the input data.

Read more in the User Guide.

Parameters

X : array of shape (n_samples, n_features)
   Data matrix.

n_components : int,
   Number of dictionary atoms to extract.

alpha : float,
   Sparsity controlling parameter.

n_iter : int,
Number of iterations to perform.

\texttt{return\_code} : boolean,

Whether to also return the code \(U\) or just the dictionary \(V\).

\texttt{dict\_init} : array of shape (\(n\_components, n\_features\)),

Initial value for the dictionary for warm restart scenarios.

\texttt{callback} : callable or None, optional (default: None)

callable that gets invoked every five iterations

\texttt{batch\_size} : int,

The number of samples to take in each batch.

\texttt{verbose} : bool, optional (default: False)

To control the verbosity of the procedure.

\texttt{shuffle} : boolean,

Whether to shuffle the data before splitting it in batches.

\texttt{n\_jobs} : int,

Number of parallel jobs to run, or -1 to autodetect.

\texttt{method} : {'lars', 'cd'}

lars: uses the least angle regression method to solve the lasso problem (linear_model.lars_path) cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). Lars will be faster if the estimated components are sparse.

\texttt{iter\_offset} : int, default 0

Number of previous iterations completed on the dictionary used for initialization.

\texttt{random\_state} : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by \texttt{np.random}.

\texttt{return\_inner\_stats} : boolean, optional

Return the inner statistics \(A\) (dictionary covariance) and \(B\) (data approximation). Useful to restart the algorithm in an online setting. If \texttt{return\_inner\_stats} is True, \texttt{return\_code} is ignored.

\texttt{inner\_stats} : tuple of (\(A\), \(B\)) ndarrays

Inner sufficient statistics that are kept by the algorithm. Passing them at initialization is useful in online settings, to avoid loosing the history of the evolution. \(A\) (\(n\_components, n\_components\)) is the dictionary covariance matrix. \(B\) (\(n\_features, n\_components\)) is the data approximation matrix.

\texttt{return\_n\_iter} : bool

Whether or not to return the number of iterations.

\textbf{Returns} 

\texttt{code} : array of shape (\(n\_samples, n\_components\)),

the sparse code (only returned if \texttt{return\_code}=True)

\texttt{dictionary} : array of shape (\(n\_components, n\_features\)),

30.8. \texttt{sklearn.decomposition}: Matrix Decomposition
the solutions to the dictionary learning problem

n_iter : int

Number of iterations run. Returned only if return_n_iter is set to True.

See also:

dict_learning, DictionaryLearning, MiniBatchDictionaryLearning, SparsePCA, MiniBatchSparsePCA

30.8.16 sklearn.decomposition.fastica

sklearn.decomposition.fastica(X, n_components=None, algorithm='parallel', whiten=True, fun='logcosh', fun_args=None, max_iter=200, tol=0.0001, w_init=None, random_state=None, return_X_mean=False, compute_sources=True, return_n_iter=False)

Perform Fast Independent Component Analysis.

Read more in the User Guide.

Parameters

X : array-like, shape (n_samples, n_features)

Training vector, where n_samples is the number of samples and n_features is the number of features.

n_components : int, optional

Number of components to extract. If None no dimension reduction is performed.

algorithm : {'parallel', 'deflation'}, optional

Apply a parallel or deflational FASTICA algorithm.

whiten : boolean, optional

If True perform an initial whitening of the data. If False, the data is assumed to have already been preprocessed: it should be centered, normed and white. Otherwise you will get incorrect results. In this case the parameter n_components will be ignored.

fun : string or function, optional. Default: ‘logcosh’

The functional form of the G function used in the approximation to neg-entropy. Could be either ‘logcosh’, ‘exp’, or ‘cube’. You can also provide your own function. It should return a tuple containing the value of the function, and of its derivative, in the point. Example:

def my_g(x): return x ** 3, 3 * x ** 2

fun_args : dictionary, optional

Arguments to send to the functional form. If empty or None and if fun=’logcosh’, fun_args will take value {'alpha': 1.0}

max_iter : int, optional

Maximum number of iterations to perform.

tol : float, optional

A positive scalar giving the tolerance at which the un-mixing matrix is considered to have converged.

w_init : (n_components, n_components) array, optional
Initial un-mixing array of dimension \((n\text{.comp}, n\text{.comp})\). If None (default) then an array of normal r.v.'s is used.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by \(np\text{.random}\).

**return_X_mean** : bool, optional

If True, \(X\text{.mean}\) is returned too.

**compute_sources** : bool, optional

If False, sources are not computed, but only the rotation matrix. This can save memory when working with big data. Defaults to True.

**return_n_iter** : bool, optional

Whether or not to return the number of iterations.

**Returns**

\(K\) : array, shape \((n\text{.components}, n\text{.features})\) | None.

If whiten is ‘True’, \(K\) is the pre-whitening matrix that projects data onto the first \(n\text{.components}\) principal components. If whiten is ‘False’, \(K\) is ‘None’.

\(W\) : array, shape \((n\text{.components}, n\text{.components})\)

Estimated un-mixing matrix. The mixing matrix can be obtained by:

\[
\begin{align*}
    w &= np\text{.dot}(W, K\text{.T}) \\
    A &= w\text{.T} + (w \times w\text{.T}) \times I
\end{align*}
\]

\(S\) : array, shape \((n\text{.samples}, n\text{.components})\) | None

Estimated source matrix

\(X\text{.mean}\) : array, shape \((n\text{.features}, )\)

The mean over features. Returned only if return_X_mean is True.

\(n\text{.iter}\) : int

If the algorithm is “deflation”, \(n\text{.iter}\) is the maximum number of iterations run across all components. Else they are just the number of iterations taken to converge. This is returned only when return_n_iter is set to True.

**Notes**

The data matrix \(X\) is considered to be a linear combination of non-Gaussian (independent) components i.e. \(X = AS\) where columns of \(S\) contain the independent components and \(A\) is a linear mixing matrix. In short ICA attempts to \(un\text{-mix}‘ the data by estimating an un-mixing matrix \(W\) where ‘\(S = WKX\).’

This implementation was originally made for data of shape \([n\text{.features}, n\text{.samples}]\). Now the input is transposed before the algorithm is applied. This makes it slightly faster for Fortran-ordered input.

Sparse coding

Each row of the result is the solution to a sparse coding problem. The goal is to find a sparse array `code` such that:

\[ X \approx code \times \text{dictionary} \]

Read more in the User Guide.

**Parameters**

- **X**: array of shape (n_samples, n_features)
  - Data matrix

- **dictionary**: array of shape (n_components, n_features)
  - The dictionary matrix against which to solve the sparse coding of the data. Some of the algorithms assume normalized rows for meaningful output.

- **gram**: array, shape=(n_components, n_components)
  - Precomputed Gram matrix, dictionary * dictionary'

- **cov**: array, shape=(n_components, n_samples)
  - Precomputed covariance, dictionary' * X

- **algorithm**: {'lasso_lars', 'lasso_cd', 'lars', 'omp', 'threshold'}
  - lars: uses the least angle regression method (linear_model.lars_path) lasso_lars: uses Lars to compute the Lasso solution lasso_cd: uses the coordinate descent method to compute the Lasso solution (linear_model.Lasso). lasso_lars will be faster if the estimated components are sparse. omp: uses orthogonal matching pursuit to estimate the sparse solution threshold: squashes to zero all coefficients less than alpha from the projection dictionary * X'

- **n_nonzero_coefs**: int, 0.1 * n_features by default
  - Number of nonzero coefficients to target in each column of the solution. This is only used by algorithm='lars' and algorithm='omp' and is overridden by alpha in the omp case.

- **alpha**: float, 1. by default
  - If algorithm='lasso_lars' or algorithm='lasso_cd', alpha is the penalty applied to the L1 norm. If algorithm='threshold', alpha is the absolute value of the threshold below which coefficients will be squashed to zero. If algorithm='omp', alpha is the tolerance parameter: the value of the reconstruction error targeted. In this case, it overrides n_nonzero_coefs.

- **copy_cov**: boolean, optional
  - Whether to copy the precomputed covariance matrix; if False, it may be overwritten.

- **init**: array of shape (n_samples, n_components)
  - Initialization value of the sparse codes. Only used if algorithm='lasso_cd'.

- **max_iter**: int, 1000 by default
Maximum number of iterations to perform if `algorithm='lasso_cd'`.

**n_jobs**: int, optional

Number of parallel jobs to run.

**check_input**: boolean, optional

If False, the input arrays X and dictionary will not be checked.

**verbose**: int, optional

Controls the verbosity; the higher, the more messages. Defaults to 0.

**Returns**

- **code**: array of shape (n_samples, n_components)
  The sparse codes

**See also:**

- `sklearn.linear_model.lars_path`, `sklearn.linear_model.orthogonal_mp`, `sklearn.linear_model.Lasso`, `SparseCoder`

## 30.9 sklearn.discriminant_analysis: Discriminant Analysis

Linear Discriminant Analysis and Quadratic Discriminant Analysis

**User guide**: See the Linear and Quadratic Discriminant Analysis section for further details.

```
<table>
<thead>
<tr>
<th>discriminant_analysis.</th>
<th>Linear Discriminant Analysis</th>
</tr>
</thead>
<tbody>
<tr>
<td>LinearDiscriminantAnalysis([...])</td>
<td></td>
</tr>
<tr>
<td>discriminant_analysis.</td>
<td>Quadratic Discriminant Analysis</td>
</tr>
<tr>
<td>QuadraticDiscriminantAnalysis([...])</td>
<td></td>
</tr>
</tbody>
</table>
```

### 30.9.1 sklearn.discriminant_analysis.LinearDiscriminantAnalysis

**class sklearn.discriminant_analysis.LinearDiscriminantAnalysis (solver='svd', shrinkage=None, priors=None, n_components=None, store_covariance=False, tol=0.0001)**

Linear Discriminant Analysis

A classifier with a linear decision boundary, generated by fitting class conditional densities to the data and using Bayes’ rule.

The model fits a Gaussian density to each class, assuming that all classes share the same covariance matrix.

The fitted model can also be used to reduce the dimensionality of the input by projecting it to the most discriminative directions.

New in version 0.17: `LinearDiscriminantAnalysis`.

Read more in the User Guide.

**Parameters**

- **solver**: string, optional

  Solver to use, possible values:
• ‘svd’: Singular value decomposition (default). Does not compute the covariance matrix, therefore this solver is recommended for data with a large number of features.
• ‘lsqr’: Least squares solution, can be combined with shrinkage.
• ‘eigen’: Eigenvalue decomposition, can be combined with shrinkage.

shrinkage : string or float, optional

Shrinkage parameter, possible values:
• None: no shrinkage (default).
• ‘auto’: automatic shrinkage using the Ledoit-Wolf lemma.
• float between 0 and 1: fixed shrinkage parameter.

Note that shrinkage works only with ‘lsqr’ and ‘eigen’ solvers.
priors : array, optional, shape (n_classes,)

Class priors.
n_components : int, optional

Number of components (< n_classes - 1) for dimensionality reduction.
store_covariance : bool, optional

Additionally compute class covariance matrix (default False), used only in ‘svd’ solver.

tol : float, optional, (default 1.0e-4)

Threshold used for rank estimation in SVD solver.

Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape (n_features,) or (n_classes, n_features)) Weight vector(s).</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape (n_features,)) Intercept term.</td>
</tr>
<tr>
<td>covariance_</td>
<td>(array-like, shape (n_features, n_features)) Covariance matrix (shared by all classes).</td>
</tr>
<tr>
<td>explained_variance_</td>
<td>(array, shape (n_components,)) Percentage of variance explained by each of the selected components. If n_components is not set then all components are stored and the sum of explained variances is equal to 1.0. Only available when eigen or svd solver is used.</td>
</tr>
<tr>
<td>means_</td>
<td>(array-like, shape (n_classes, n_features)) Class means.</td>
</tr>
<tr>
<td>priors_</td>
<td>(array-like, shape (n_classes,)) Class priors (sum to 1).</td>
</tr>
<tr>
<td>scalings_</td>
<td>(array-like, shape (rank, n_classes - 1)) Scaling of the features in the space spanned by the class centroids.</td>
</tr>
<tr>
<td>xbar_</td>
<td>(array-like, shape (n_features,)) Overall mean.</td>
</tr>
<tr>
<td>classes_</td>
<td>(array-like, shape (n_classes,)) Unique class labels.</td>
</tr>
</tbody>
</table>

See also:

sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis Quadratic Discriminant Analysis
Notes

The default solver is ‘svd’. It can perform both classification and transform, and it does not rely on the calculation of the covariance matrix. This can be an advantage in situations where the number of features is large. However, the ‘svd’ solver cannot be used with shrinkage.

The ‘lsqr’ solver is an efficient algorithm that only works for classification. It supports shrinkage.

The ‘eigen’ solver is based on the optimization of the between class scatter to within class scatter ratio. It can be used for both classification and transform, and it supports shrinkage. However, the ‘eigen’ solver needs to compute the covariance matrix, so it might not be suitable for situations with a high number of features.

Examples

```python
>>> import numpy as np
>>> from sklearn.discriminant_analysis import LinearDiscriminantAnalysis
>>> X = np.array([[1, 1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])
>>> clf = LinearDiscriminantAnalysis()
>>> clf.fit(X, y)
LinearDiscriminantAnalysis(n_components=None, priors=None, shrinkage=None,
                           solver='svd', store_covariance=False, tol=0.0001)
>>> print(clf.predict([[0, 1], [0, 0]]))
[1]
```

Methods

- `decision_function(X)` Predict confidence scores for samples.
- `fit(X, y)` Fit LinearDiscriminantAnalysis model according to the given training data and parameters.
- `fit_transform(X[, y])` Fit to data, then transform it.
- `get_params([deep])` Get parameters for this estimator.
- `predict(X)` Predict class labels for samples in X.
- `predict_log_proba(X)` Estimate log probability.
- `predict_proba(X)` Estimate probability.
- `score(X, y[, sample_weight])` Returns the mean accuracy on the given test data and labels.
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X)` Project data to maximize class separation.

__init__(solver='svd', shrinkage=None, priors=None, n_components=None, store_covariance=False, tol=0.0001)

decision_function (X)

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

Parameters

- `X` : array-like, sparse matrix, shape = (n_samples, n_features)
  - Samples.

Returns

- array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
Confidence scores per (sample, class) combination. In the binary case, confidence score for `self.classes_[1]` where >0 means this class would be predicted.

**fit** \((X, y)\)

Fit LinearDiscriminantAnalysis model according to the given training data and parameters.

Changed in version 0.19: `store_covariance` has been moved to main constructor.

Parameters

- **X**: array-like, shape (n_samples, n_features)
  - Training data.

- **y**: array, shape (n_samples,)
  - Target values.

**fit_transform** \((X, y=None, **fit_params)\)

Fit to data, then transform it.

Fits transformer to \(X\) and \(y\) with optional parameters `fit_params` and returns a transformed version of \(X\).

Parameters

- **X**: numpy array of shape \([n_samples, n_features]\)
  - Training set.

- **y**: numpy array of shape \([n_samples]\)
  - Target values.

Returns

- **X_new**: numpy array of shape \([n_samples, n_features_new]\)
  - Transformed array.

**get_params** \((deep=True)\)

Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**predict** \((X)\)

Predict class labels for samples in \(X\).

Parameters

- **X**: {array-like, sparse matrix}, shape \([n_samples, n_features]\)
  - Samples.

Returns

- **C**: array, shape \([n_samples]\)
  - Predicted class label per sample.

**predict_log_proba** \((X)\)

Estimate log probability.

Parameters

- **X**: array-like, shape \((n_samples, n_features)\)
  - Input data.

Returns

- **C**: array, shape \((n_samples, n_classes)\)
Estimated log probabilities.

**predict_proba** *(X)*
Estimate probability.

**Parameters**

X : array-like, shape (n_samples, n_features)
Input data.

**Returns**

C : array, shape (n_samples, n_classes)
Estimated probabilities.

**score** *(X, y, sample_weight=None)*
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

**Returns**

score : float
Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

self

**transform** *(X)*
Project data to maximize class separation.

**Parameters**

X : array-like, shape (n_samples, n_features)
Input data.

**Returns**

X_new : array, shape (n_samples, n_components)
Transformed data.

**Examples using** sklearn.discriminant_analysis.LinearDiscriminantAnalysis

- Normal and Shrinkage Linear Discriminant Analysis for classification
- Linear and Quadratic Discriminant Analysis with covariance ellipsoid
- Comparison of LDA and PCA 2D projection of Iris dataset
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
30.9.2 `sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis`

**class** `sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis` *(priors=None, reg_param=0.0, store_covariance=False, tol=0.0001, store_covariances=None)*

Quadratic Discriminant Analysis

A classifier with a quadratic decision boundary, generated by fitting class conditional densities to the data and using Bayes’ rule.

The model fits a Gaussian density to each class.

New in version 0.17: *QuadraticDiscriminantAnalysis*

Read more in the *User Guide*.

**Parameters**

- `priors`: array, optional, shape = [n_classes]
  - Priors on classes

- `reg_param`: float, optional
  - Regularizes the covariance estimate as $(1-reg_param)\times\Sigma + reg_param\times np.eye(n_features)$

- `store_covariance`: boolean
  - If True the covariance matrices are computed and stored in the `self.covariance_` attribute.

  - New in version 0.17.

- `tol`: float, optional, default 1.0e-4
  - Threshold used for rank estimation.

  - New in version 0.17.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>covariance_</td>
<td>(list of array-like, shape = [n_features, n_features]) Covariance matrices of each class.</td>
</tr>
<tr>
<td>means</td>
<td>(array-like, shape = [n_classes, n_features]) Class means.</td>
</tr>
<tr>
<td>priors</td>
<td>(array-like, shape = [n_classes]) Class priors (sum to 1).</td>
</tr>
<tr>
<td>rotations</td>
<td>(list of arrays) For each class k an array of shape [n_features, n_k], with n_k = min(n_features, number of elements in class k) It is the rotation of the Gaussian distribution, i.e. its principal axis.</td>
</tr>
<tr>
<td>scalings</td>
<td>(list of arrays) For each class k an array of shape [n_k]. It contains the scaling of the Gaussian distributions along its principal axes, i.e. the variance in the rotated coordinate system.</td>
</tr>
</tbody>
</table>

**See also:**

`sklearn.discriminant_analysis.LinearDiscriminantAnalysis` Linear Discriminant Analysis
Examples

```python
>>> from sklearn.discriminant_analysis import QuadraticDiscriminantAnalysis
>>> import numpy as np

>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])
>>> clf = QuadraticDiscriminantAnalysis()
>>> clf.fit(X, y)
... QuadraticDiscriminantAnalysis(priors=None, reg_param=0.0,
                              store_covariance=False,
                              store_covariances=None, tol=0.0001)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

Methods

- `decision_function(X)`  
  Apply decision function to an array of samples.

- `fit(X, y)`  
  Fit the model according to the given training data and parameters.

- `get_params([deep])`  
  Get parameters for this estimator.

- `predict(X)`  
  Perform classification on an array of test vectors X.

- `predict_log_proba(X)`  
  Return posterior probabilities of classification.

- `predict_proba(X)`  
  Return posterior probabilities of classification.

- `score(X, y[, sample_weight])`  
  Returns the mean accuracy on the given test data and labels.

- `set_params(**params)`  
  Set the parameters of this estimator.

- `__init__(priors=None, reg_param=0.0, store_covariance=False, store_covariances=None, tol=0.0001)`

```python
DEPRECATED: Attribute covariances_ was deprecated in version 0.19 and will be removed in 0.21. Use covariance_ instead
```

- `decision_function(X)`  
  Apply decision function to an array of samples.

  **Parameters**
  
  - X : array-like, shape = [n_samples, n_features]

    Array of samples (test vectors).

  **Returns**
  
  - C : array, shape = [n_samples, n_classes] or [n_samples,]

    Decision function values related to each class, per sample. In the two-class case, the shape is [n_samples,], giving the log likelihood ratio of the positive class.

- `fit(X, y)`  
  Fit the model according to the given training data and parameters.

  **Changed in version 0.19:**

  - store_covariances has been moved to main constructor as store_covariance

  **Changed in version 0.19:**

  - tol has been moved to main constructor.

  **Parameters**

  - X : array-like, shape = [n_samples, n_features]
Training vector, where \( n_{\text{samples}} \) is the number of samples and \( n_{\text{features}} \) is the number of features.

\[ y : \text{array, shape} = [n_{\text{samples}}] \]

Target values (integers)

**get_params** (*deep=True*)

Get parameters for this estimator.

**Parameters** deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**predict** (*X*)

Perform classification on an array of test vectors \( X \).

The predicted class \( C \) for each sample in \( X \) is returned.

**Parameters** X : array-like, shape = \([n_{\text{samples}}, n_{\text{features}}]\)

**Returns** C : array, shape = \([n_{\text{samples}}]\)

**predict_log_proba** (*X*)

Return posterior probabilities of classification.

**Parameters** X : array-like, shape = \([n_{\text{samples}}, n_{\text{features}}]\)

Array of samples/test vectors.

**Returns** C : array, shape = \([n_{\text{samples}}, n_{\text{classes}}]\)

Posterior log-probabilities of classification per class.

**predict_proba** (*X*)

Return posterior probabilities of classification.

**Parameters** X : array-like, shape = \([n_{\text{samples}}, n_{\text{features}}]\)

Array of samples/test vectors.

**Returns** C : array, shape = \([n_{\text{samples}}, n_{\text{classes}}]\)

Posterior probabilities of classification per class.

**score** (*X, y, sample_weight=None*)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters** X : array-like, shape = \((n_{\text{samples}}, n_{\text{features}})\)

Test samples.

y : array-like, shape = \((n_{\text{samples}})\) or \((n_{\text{samples}}, n_{\text{outputs}})\)

True labels for \( X \).

**sample_weight** : array-like, shape = \([n_{\text{samples}}]\), optional

Sample weights.
Returns score: float
Mean accuracy of self.predict(X) wrt. y.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

Examples using sklearn.discriminant_analysis.QuadraticDiscriminantAnalysis

- Classifier comparison
- Linear and Quadratic Discriminant Analysis with covariance ellipsoid

30.10 sklearn.dummy: Dummy estimators

User guide: See the Model evaluation: quantifying the quality of predictions section for further details.

dummy.DummyClassifier([strategy, ...])
DummyClassifier is a classifier that makes predictions using simple rules.
dummy.DummyRegressor([strategy, constant, ...])
DummyRegressor is a regressor that makes predictions using simple rules.

30.10.1 sklearn.dummy.DummyClassifier

class sklearn.dummy.DummyClassifier(strategy='stratified', random_state=None, constant=None)
DummyClassifier is a classifier that makes predictions using simple rules.

This classifier is useful as a simple baseline to compare with other (real) classifiers. Do not use it for real problems.

Read more in the User Guide.

Parameters strategy: str, default=’stratified’
Strategy to use to generate predictions.
- “stratified”: generates predictions by respecting the training set’s class distribution.
- “most_frequent”: always predicts the most frequent label in the training set.
- “prior”: always predicts the class that maximizes the class prior (like “most_frequent”) and predict_proba returns the class prior.
- “uniform”: generates predictions uniformly at random.
- “constant”: always predicts a constant label that is provided by the user. This is useful for metrics that evaluate a non-majority class

New in version 0.17: Dummy Classifier now supports prior fitting strategy using parameter prior.

random_state: int, RandomState instance or None, optional, default=None
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**constant** : int or str or array of shape = [n_outputs]

The explicit constant as predicted by the “constant” strategy. This parameter is useful only for the “constant” strategy.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>classes_</code></td>
<td>(array or list of array of shape = [n_classes]) Class labels for each output.</td>
</tr>
<tr>
<td><code>n_classes_</code></td>
<td>(array or list of array of shape = [n_classes]) Number of label for each output.</td>
</tr>
<tr>
<td><code>class_prior_</code></td>
<td>(array or list of array of shape = [n_classes]) Probability of each class for each output.</td>
</tr>
<tr>
<td><code>n_outputs_</code></td>
<td>(int,) Number of outputs.</td>
</tr>
<tr>
<td><code>outputs_2d_</code></td>
<td>(bool,) True if the output at fit is 2d, else false.</td>
</tr>
<tr>
<td><code>sparse_output_</code></td>
<td>(bool,) True if the array returned from predict is to be in sparse CSC format. Is automatically set to True if the input y is passed in sparse format.</td>
</tr>
</tbody>
</table>

### Methods

- **`fit(X, y[, sample_weight])`**
  Fit the random classifier.

- **`get_params([deep])`**
  Get parameters for this estimator.

- **`predict(X)`**
  Perform classification on test vectors X.

- **`predict_log_proba(X)`**
  Return log probability estimates for the test vectors X.

- **`predict_proba(X)`**
  Return probability estimates for the test vectors X.

- **`score(X, y[, sample_weight])`**
  Returns the mean accuracy on the given test data and labels.

- **`set_params(**params)`**
  Set the parameters of this estimator.

```python
__init__(strategy='stratified', random_state=None, constant=None)
```

Fit the random classifier.

**Parameters**

- `X`: {array-like, sparse matrix}, shape = [n_samples, n_features]  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

- `y`: array-like, shape = [n_samples] or [n_samples, n_outputs]  
  Target values.

- `sample_weight`: array-like of shape = [n_samples], optional  
  Sample weights.

**Returns**

- `self`: object  
  Returns self.

```python
get_params (deep=True)
```

Get parameters for this estimator.
scikit-learn user guide, Release 0.20.dev0

**Parameters** `deep` : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** `params` : mapping of string to any

Parameter names mapped to their values.

`predict(X)`

Perform classification on test vectors X.

**Parameters** `X` : {array-like, sparse matrix}, shape = [n_samples, n_features]

Input vectors, where n_samples is the number of samples and n_features is the number of features.

**Returns** `y` : array, shape = [n_samples] or [n_samples, n_outputs]

Predicted target values for X.

`predict_log_proba(X)`

Return log probability estimates for the test vectors X.

**Parameters** `X` : {array-like, sparse matrix}, shape = [n_samples, n_features]

Input vectors, where n_samples is the number of samples and n_features is the number of features.

**Returns** `P` : array-like or list of array-like of shape = [n_samples, n_classes]

Returns the log probability of the sample for each class in the model, where classes are ordered arithmetically for each output.

`predict_proba(X)`

Return probability estimates for the test vectors X.

**Parameters** `X` : {array-like, sparse matrix}, shape = [n_samples, n_features]

Input vectors, where n_samples is the number of samples and n_features is the number of features.

**Returns** `P` : array-like or list of array-like of shape = [n_samples, n_classes]

Returns the probability of the sample for each class in the model, where classes are ordered arithmetically, for each output.

`slove(X, y, sample_weight=None)`

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters** `X` : array-like, shape = (n_samples, n_features)

Test samples.

`y` : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

`sample_weight` : array-like, shape = [n_samples], optional

Sample weights.

**Returns** `score` : float

Mean accuracy of self.predict(X) wrt. y.
**set_params(****params***)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

## 30.10.2 sklearn.dummy.DummyRegressor

class sklearn.dummy.DummyRegressor (strategy='mean', constant=None, quantile=None)

DummyRegressor is a regressor that makes predictions using simple rules.

This regressor is useful as a simple baseline to compare with other (real) regressors. Do not use it for real problems.

Read more in the User Guide.

Parameters

- **strategy**: str
  Strategy to use to generate predictions.
  - “mean”: always predicts the mean of the training set
  - “median”: always predicts the median of the training set
  - “quantile”: always predicts a specified quantile of the training set, provided with the quantile parameter.
  - “constant”: always predicts a constant value that is provided by the user.

- **constant**: int or float or array of shape = [n_outputs]
  The explicit constant as predicted by the “constant” strategy. This parameter is useful only for the “constant” strategy.

- **quantile**: float in [0.0, 1.0]
  The quantile to predict using the “quantile” strategy. A quantile of 0.5 corresponds to the median, while 0.0 to the minimum and 1.0 to the maximum.

Attributes

- **constant_** (float or array of shape [n_outputs]) Mean or median or quantile of the training targets or constant value given by the user.
- **n_outputs_** (int) Number of outputs.
- **outputs_2d_** (bool) True if the output at fit is 2d, else false.

Methods

- **fit(X, y[, sample_weight])**  
  Fit the random regressor.
- **get_params([deep])**  
  Get parameters for this estimator.
- **predict(X)**  
  Perform classification on test vectors X.

Continued on next page
Table 30.65 – continued from previous page

**score**(*X, y[, sample_weight])  Returns the coefficient of determination R^2 of the prediction.

**set_params**(**params)  Set the parameters of this estimator.

```
__init__(strategy='mean', constant=None, quantile=None)
```

```
fit (X, y, sample_weight=None)
Fit the random regressor.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Training vectors, where n_samples is the number of samples and n_features is the number of features.

y : array-like, shape = [n_samples] or [n_samples, n_outputs]
Target values.

sample_weight : array-like of shape = [n_samples], optional
Sample weights.

Returns self : object
Returns self.
```

```
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.
```

```
predict (X)
Perform classification on test vectors X.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Input vectors, where n_samples is the number of samples and n_features is the number of features.

Returns y : array, shape = [n_samples] or [n_samples, n_outputs]
Predicted target values for X.
```

```
score (X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.
```

30.10. sklearn.dummy: Dummy estimators
**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.

**Returns** score : float

$R^2$ of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

---

### 30.11 sklearn.ensemble: Ensemble Methods

The `sklearn.ensemble` module includes ensemble-based methods for classification, regression and anomaly detection.

**User guide:** See the *Ensemble methods* section for further details.

<table>
<thead>
<tr>
<th>Class Name</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td><code>ensemble.BaggingClassifier([base_estimator, ...])</code></td>
<td>A Bagging classifier.</td>
</tr>
<tr>
<td><code>ensemble.BaggingRegressor([base_estimator, ...])</code></td>
<td>A Bagging regressor.</td>
</tr>
<tr>
<td><code>ensemble.ExtraTreesClassifier([...])</code></td>
<td>An extra-trees classifier.</td>
</tr>
<tr>
<td><code>ensemble.GradientBoostingClassifier([loss, ...])</code></td>
<td>Gradient Boosting for classification.</td>
</tr>
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<td><code>ensemble.GradientBoostingRegressor([loss, ...])</code></td>
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<td><code>ensemble.IsolationForest([n_estimators, ...])</code></td>
<td>Isolation Forest Algorithm</td>
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<td><code>ensemble.RandomForestClassifier([...])</code></td>
<td>A random forest classifier.</td>
</tr>
<tr>
<td><code>ensemble.RandomForestRegressor([...])</code></td>
<td>A random forest regressor.</td>
</tr>
</tbody>
</table>

#### 30.11.1 sklearn.ensemble.AdaBoostClassifier

**class** `sklearn.ensemble.AdaBoostClassifier` *(base_estimator=\texttt{None}, n_estimators=50, learning_rate=1.0, algorithm=‘SAMME.R’, random_state=\texttt{None})*

An AdaBoost classifier.

An AdaBoost [1] classifier is a meta-estimator that begins by fitting a classifier on the original dataset and then fits additional copies of the classifier on the same dataset but where the weights of incorrectly classified instances
are adjusted such that subsequent classifiers focus more on difficult cases.
This class implements the algorithm known as AdaBoost-SAMME [2].
Read more in the User Guide.

Parameters

**base_estimator** : object, optional (default=DecisionTreeClassifier)
The base estimator from which the boosted ensemble is built. Support for sample
weighting is required, as well as proper `classes_` and `n_classes_` attributes.

**n_estimators** : integer, optional (default=50)
The maximum number of estimators at which boosting is terminated. In case of perfect
fit, the learning procedure is stopped early.

**learning_rate** : float, optional (default=1.)
Learning rate shrinks the contribution of each classifier by `learning_rate`. There
is a trade-off between learning_rate and n_estimators.

**algorithm** : {'SAMME', 'SAMME.R'}, optional (default='SAMME.R')
If ‘SAMME.R’ then use the SAMME.R real boosting algorithm. `base_estimator`
must support calculation of class probabilities. If ‘SAMME’ then use the SAMME
discrete boosting algorithm. The SAMME.R algorithm typically converges faster than
SAMME, achieving a lower test error with fewer boosting iterations.

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState
instance, random_state is the random number generator; If None, the random number
generator is the RandomState instance used by `np.random`

Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>feature_importances_</td>
<td>Return the feature importances (the higher, the more important the feature).</td>
</tr>
<tr>
<td>estimators_</td>
<td>(list of classifiers) The collection of fitted sub-estimators.</td>
</tr>
<tr>
<td>classes_</td>
<td>(array of shape = [n_classes]) The classes labels.</td>
</tr>
<tr>
<td>n_classes_</td>
<td>(int) The number of classes.</td>
</tr>
<tr>
<td>estimator_weights_</td>
<td>(array of floats) Weights for each estimator in the boosted ensemble.</td>
</tr>
<tr>
<td>estimator_errors_</td>
<td>(array of floats) Classification error for each estimator in the boosted ensemble.</td>
</tr>
</tbody>
</table>

See also:


References

*R5758*, R5858

Methods
decision_function(X) Compute the decision function of X.

fit(X, y[, sample_weight]) Build a boosted classifier from the training set (X, y).

get_params([deep]) Get parameters for this estimator.

predict(X) Predict classes for X.

predict_log_proba(X) Predict class log-probabilities for X.

predict_proba(X) Predict class probabilities for X.

score(X, y[, sample_weight]) Returns the mean accuracy on the given test data and labels.

set_params(**params) Set the parameters of this estimator.

staged_decision_function(X) Compute decision function of X for each boosting iteration.

staged_predict(X) Return staged predictions for X.

staged_predict_proba(X) Predict class probabilities for X.

staged_score(X, y[, sample_weight]) Return staged scores for X, y.

__init__(base_estimator=None, n_estimators=50, learning_rate=1.0, algorithm='SAMME.R', random_state=None)

decision_function(X) Compute the decision function of X.

Parameters X : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

Returns score : array, shape = [n_samples, k]

The decision function of the input samples. The order of outputs is the same of that of the classes_ attribute. Binary classification is a special cases with k == 1, otherwise k==n_classes. For binary classification, values closer to -1 or 1 mean more like the first or second class in classes_, respectively.

feature_importances_ Return the feature importances (the higher, the more important the feature).

Returns feature_importances_ : array, shape = [n_features]

fit(X, y, sample_weight=None) Build a boosted classifier from the training set (X, y).

Parameters X : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

y : array-like of shape = [n_samples]

The target values (class labels).

sample_weight : array-like of shape = [n_samples], optional

Sample weights. If None, the sample weights are initialized to 1 / n_samples.

Returns self : object

Returns self.

get_params (deep=True) Get parameters for this estimator.
Parameters `deep` : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns `params` : mapping of string to any

Parameter names mapped to their values.

**predict** *(X)*

Predict classes for X.

The predicted class of an input sample is computed as the weighted mean prediction of the classifiers in the ensemble.

**Parameters** `X` : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

Returns `y` : array of shape = [n_samples]

The predicted classes.

**predict_log_proba** *(X)*

Predict class log-probabilities for X.

The predicted class log-probabilities of an input sample is computed as the weighted mean predicted class log-probabilities of the classifiers in the ensemble.

**Parameters** `X` : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

Returns `p` : array of shape = [n_samples]

The class probabilities of the input samples. The order of outputs is the same of that of the `classes_` attribute.

**predict_proba** *(X)*

Predict class probabilities for X.

The predicted class probabilities of an input sample is computed as the weighted mean predicted class probabilities of the classifiers in the ensemble.

**Parameters** `X` : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

Returns `p` : array of shape = [n_samples]

The class probabilities of the input samples. The order of outputs is the same of that of the `classes_` attribute.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters** `X` : array-like, shape = (n_samples, n_features)

Test samples.

`y` : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.

**Returns score** : float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**staged_decision_function** (X)

Compute decision function of X for each boosting iteration.

This method allows monitoring (i.e. determine error on testing set) after each boosting iteration.

**Parameters** X : {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

**Returns** score : generator of array, shape = [n_samples, k]

The decision function of the input samples. The order of outputs is the same of that of the `classes_` attribute. Binary classification is a special cases with k == 1, otherwise k==n_classes. For binary classification, values closer to -1 or 1 mean more like the first or second class in `classes_`, respectively.

**staged_predict** (X)

Return staged predictions for X.

The predicted class of an input sample is computed as the weighted mean prediction of the classifiers in the ensemble.

This generator method yields the ensemble prediction after each iteration of boosting and therefore allows monitoring, such as to determine the prediction on a test set after each boost.

**Parameters** X : array-like of shape = [n_samples, n_features]

The input samples.

**Returns** y : generator of array, shape = [n_samples]

The predicted classes.

**staged_predict_proba** (X)

Predict class probabilities for X.

The predicted class probabilities of an input sample is computed as the weighted mean predicted class probabilities of the classifiers in the ensemble.

This generator method yields the ensemble predicted class probabilities after each iteration of boosting and therefore allows monitoring, such as to determine the predicted class probabilities on a test set after each boost.

**Parameters** X : {array-like, sparse matrix} of shape = [n_samples, n_features]
The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

**Returns p**: generator of array, shape = [n_samples]

The class probabilities of the input samples. The order of outputs is the same of that of the `classes_` attribute.

**staged_score** *(X, y, sample_weight=None)*

Return staged scores for X, y.

This generator method yields the ensemble score after each iteration of boosting and therefore allows monitoring, such as to determine the score on a test set after each boost.

**Parameters X**: {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

**y**: array-like, shape = [n_samples]

Labels for X.

**sample_weight**: array-like, shape = [n_samples], optional

Sample weights.

**Returns z**: float

Examples using `sklearn.ensemble.AdaBoostClassifier`

- Classifier comparison
- Two-class AdaBoost
- Discrete versus Real AdaBoost
- Multi-class AdaBoosted Decision Trees
- Plot the decision surfaces of ensembles of trees on the iris dataset

### 30.11.2 sklearn.ensemble.AdaBoostRegressor

```python
class sklearn.ensemble.AdaBoostRegressor
```

An AdaBoost regressor.

An AdaBoost [1] regressor is a meta-estimator that begins by fitting a regressor on the original dataset and then fits additional copies of the regressor on the same dataset but where the weights of instances are adjusted according to the error of the current prediction. As such, subsequent regressors focus more on difficult cases.

This class implements the algorithm known as AdaBoost.R2 [2].

Read more in the [User Guide](#).

**Parameters base_estimator**: object, optional (default=DecisionTreeRegressor)

The base estimator from which the boosted ensemble is built. Support for sample weighting is required.

**n_estimators**: integer, optional (default=50)

The maximum number of estimators at which boosting is terminated. In case of perfect fit, the learning procedure is stopped early.
**learning_rate** : float, optional (default=1.)

Learning rate shrinks the contribution of each regressor by learning_rate. There is a trade-off between learning_rate and n_estimators.

**loss** : {'linear', 'square', 'exponential'}, optional (default='linear')

The loss function to use when updating the weights after each boosting iteration.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; if RandomState instance, random_state is the random number generator; if None, the random number generator is the RandomState instance used by np.random.

**Attributes**

- **feature_importances_**
  Return the feature importances (the higher, the more important the feature).

- **estimators_**
  (list of classifiers) The collection of fitted sub-estimators.

- **estimator_weights_**
  (array of floats) Weights for each estimator in the boosted ensemble.

- **estimator_errors_**
  (array of floats) Regression error for each estimator in the boosted ensemble.

**See also:**

AdaBoostClassifier, GradientBoostingRegressor, DecisionTreeRegressor

**References**

[R6162], [R6262]

**Methods**

- **fit(X, y, sample_weight)**
  Build a boosted regressor from the training set (X, y).

- **get_params**(deep)
  Get parameters for this estimator.

- **predict**(X)
  Predict regression value for X.

- **score(X, y, sample_weight)**
  Returns the coefficient of determination R^2 of the prediction.

- **set_params**(**params)
  Set the parameters of this estimator.

- **staged_predict**(X)
  Return staged predictions for X.

- **staged_score**(X, y, sample_weight)
  Return staged scores for X, y.

**__init__**(base_estimator=None, n_estimators=50, learning_rate=1.0, loss='linear', random_state=None)

**feature_importances_**

Return the feature importances (the higher, the more important the feature).

**Returns**

feature_importances_ : array, shape = [n_features]
**fit** *(X, y, sample_weight=None)*
Build a boosted regressor from the training set (X, y).

**Parameters**

- **X**: array-like, sparse matrix of shape = [n_samples, n_features]
  The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.
- **y**: array-like of shape = [n_samples]
  The target values (real numbers).
- **sample_weight**: array-like of shape = [n_samples], optional
  Sample weights. If None, the sample weights are initialized to 1 / n_samples.

**Returns**

- **self**: object
  Returns self.

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**predict** *(X)*
Predict regression value for X.

The predicted regression value of an input sample is computed as the weighted median prediction of the classifiers in the ensemble.

**Parameters**

- **X**: array-like, sparse matrix of shape = [n_samples, n_features]
  The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

**Returns**

- **y**: array of shape = [n_samples]
  The predicted regression values.

**score** *(X, y, sample_weight=None)*
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- **score**: float
  Returns score.
R^2 of self.predict(X) wrt. y.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

**staged_predict** (X)
Return staged predictions for X.

The predicted regression value of an input sample is computed as the weighted median prediction of the classifiers in the ensemble.

This generator method yields the ensemble prediction after each iteration of boosting and therefore allows monitoring, such as to determine the prediction on a test set after each boost.

Parameters X : {array-like, sparse matrix} of shape = [n_samples, n_features]
The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

Returns y : generator of array, shape = [n_samples]
The predicted regression values.

**staged_score** (X, y, sample_weight=None)
Return staged scores for X, y.

This generator method yields the ensemble score after each iteration of boosting and therefore allows monitoring, such as to determine the score on a test set after each boost.

Parameters X : {array-like, sparse matrix} of shape = [n_samples, n_features]
The training input samples. Sparse matrix can be CSC, CSR, COO, DOK, or LIL. DOK and LIL are converted to CSR.

y : array-like, shape = [n_samples]
Labels for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns z : float

Examples using sklearn.ensemble.AdaBoostRegressor

- Decision Tree Regression with AdaBoost

30.11.3 sklearn.ensemble.BaggingClassifier

class sklearn.ensemble.BaggingClassifier (base_estimator=None, n_estimators=10, max_samples=1.0, max_features=1.0, bootstrap=True, bootstrap_features=False, oob_score=False, warm_start=False, n_jobs=1, random_state=None, verbose=0)

A Bagging classifier.
A **Bagging** classifier is an ensemble meta-estimator that fits base classifiers each on random subsets of the original dataset and then aggregate their individual predictions (either by voting or by averaging) to form a final prediction. Such a meta-estimator can typically be used as a way to reduce the variance of a black-box estimator (e.g., a decision tree), by introducing randomization into its construction procedure and then making an ensemble out of it.

This algorithm encompasses several works from the literature. When random subsets of the dataset are drawn as random subsets of the samples, then this algorithm is known as Pasting [R371374]. If samples are drawn with replacement, then the method is known as Bagging [R372374]. When random subsets of the dataset are drawn as random subsets of the features, then the method is known as Random Subspaces [R373374]. Finally, when base estimators are built on subsets of both samples and features, then the method is known as Random Patches [R374374].

Read more in the [User Guide](#).

**Parameters**

**base_estimator** : object or None, optional (default=None)

The base estimator to fit on random subsets of the dataset. If None, then the base estimator is a decision tree.

**n_estimators** : int, optional (default=10)

The number of base estimators in the ensemble.

**max_samples** : int or float, optional (default=1.0)

The number of samples to draw from X to train each base estimator.

- If int, then draw `max_samples` samples.
- If float, then draw `max_samples * X.shape[0]` samples.

**max_features** : int or float, optional (default=1.0)

The number of features to draw from X to train each base estimator.

- If int, then draw `max_features` features.
- If float, then draw `max_features * X.shape[1]` features.

**bootstrap** : boolean, optional (default=True)

Whether samples are drawn with replacement.

**bootstrap_features** : boolean, optional (default=False)

Whether features are drawn with replacement.

**oob_score** : bool

Whether to use out-of-bag samples to estimate the generalization error.

**warm_start** : bool, optional (default=False)

When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new ensemble.

New in version 0.17: `warm_start` constructor parameter.

**n_jobs** : int, optional (default=1)

The number of jobs to run in parallel for both `fit` and `predict`. If -1, then the number of jobs is set to the number of cores.

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**verbose** : int, optional (default=0)

Controls the verbosity of the building process.

**Attributes**

- **estimators_samples_**
  The subset of drawn samples for each base estimator.

- **base_estimator** (estimator) The base estimator from which the ensemble is grown.

- **estimators_** (list of estimators) The collection of fitted base estimators.

- **estimators_features_** (list of arrays) The subset of drawn features for each base estimator.

- **classes_** (array of shape = [n_classes]) The classes labels.

- **n_classes_** (int or list) The number of classes.

- **oob_score_** (float) Score of the training dataset obtained using an out-of-bag estimate.

- **oob_decision_function_** (array of shape = [n_samples, n_classes]) Decision function computed with out-of-bag estimate on the training set. If n_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob_decision_function_ might contain NaN.

**References**

[R371374], [R372374], [R373374], [R374374]

**Methods**

- **decision_function(X)** Average of the decision functions of the base classifiers.

- **fit(X, y[, sample_weight])** Build a Bagging ensemble of estimators from the training set (X, y).

- **get_params([deep])** Get parameters for this estimator.

- **predict(X)** Predict class for X.

- **predict_log_proba(X)** Predict class log-probabilities for X.

- **predict_proba(X)** Predict class probabilities for X.

- **score(X, y[, sample_weight])** Returns the mean accuracy on the given test data and labels.

- **set_params(**params)** Set the parameters of this estimator.

**__init__**(base_estimator=None, n_estimators=10, max_samples=1.0, max_features=1.0, bootstrap=True, bootstrap_features=False, oob_score=False, warm_start=False, n_jobs=1, random_state=None, verbose=0)

**decision_function(X)**

Average of the decision functions of the base classifiers.

**Parameters**

- **X** : {array-like, sparse matrix} of shape = [n_samples, n_features]
The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns score**: array, shape = [n_samples, k]

The decision function of the input samples. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`. Regression and binary classification are special cases with k == 1, otherwise k==n_classes.

**estimators_samples_**

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of boolean masks identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.

Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.

**fit (X, y, sample_weight=None)**

Build a Bagging ensemble of estimators from the training set (X, y).

**Parameters X**: {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

y : array-like, shape = [n_samples]

The target values (class labels in classification, real numbers in regression).

sample_weight : array-like, shape = [n_samples] or None

Sample weights. If None, then samples are equally weighted. Note that this is supported only if the base estimator supports sample weighting.

**Returns self**: object

Returns self.

**get_params (deep=True)**

Get parameters for this estimator.

**Parameters deep**: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns params**: mapping of string to any

Parameter names mapped to their values.

**predict (X)**

Predict class for X.

The predicted class of an input sample is computed as the class with the highest mean predicted probability. If base estimators do not implement a `predict_proba` method, then it resorts to voting.

**Parameters X**: {array-like, sparse matrix} of shape = [n_samples, n_features]

The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns y**: array of shape = [n_samples]

The predicted classes.
**predict_log_proba** *(X)*

Predict class log-probabilities for *X*.

The predicted class log-probabilities of an input sample is computed as the log of the mean predicted class probabilities of the base estimators in the ensemble.

**Parameters**

- **X**: array-like, sparse matrix of shape = [n_samples, n_features]
  - The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns**

- **p**: array of shape = [n_samples, n_classes]
  - The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute `classes_`.

**predict_proba** *(X)*

Predict class probabilities for *X*.

The predicted class probabilities of an input sample is computed as the mean predicted class probabilities of the base estimators in the ensemble. If base estimators do not implement a `predict_proba` method, then it resorts to voting and the predicted class probabilities of an input sample represents the proportion of estimators predicting each class.

**Parameters**

- **X**: array-like, sparse matrix of shape = [n_samples, n_features]
  - The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns**

- **p**: array of shape = [n_samples, n_classes]
  - The class probabilities of the input samples. The order of the classes corresponds to that in the attribute `classes_`.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for *X*.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**

- **score**: float
  - Mean accuracy of `self.predict(X)` wrt. *y*.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**
A Bagging regressor.

A Bagging regressor is an ensemble meta-estimator that fits base regressors each on random subsets of the original dataset and then aggregate their individual predictions (either by voting or by averaging) to form a final prediction. Such a meta-estimator can typically be used as a way to reduce the variance of a black-box estimator (e.g., a decision tree), by introducing randomization into its construction procedure and then making an ensemble out of it.

This algorithm encompasses several works from the literature. When random subsets of the dataset are drawn as random subsets of the samples, then this algorithm is known as Pasting [R6568]. If samples are drawn with replacement, then the method is known as Bagging [R6668]. When random subsets of the dataset are drawn as random subsets of the features, then the method is known as Random Subspaces [R6768]. Finally, when base estimators are built on subsets of both samples and features, then the method is known as Random Patches [R6868].

Read more in the User Guide.

**Parameters**

- **base_estimator**: object or None, optional (default=None)
  The base estimator to fit on random subsets of the dataset. If None, then the base estimator is a decision tree.

- **n_estimators**: int, optional (default=10)
  The number of base estimators in the ensemble.

- **max_samples**: int or float, optional (default=1.0)
  The number of samples to draw from X to train each base estimator.
  - If int, then draw `max_samples` samples.
  - If float, then draw `max_samples * X.shape[0]` samples.

- **max_features**: int or float, optional (default=1.0)
  The number of features to draw from X to train each base estimator.
  - If int, then draw `max_features` features.
  - If float, then draw `max_features * X.shape[1]` features.

- **bootstrap**: boolean, optional (default=True)
  Whether samples are drawn with replacement.

- **bootstrap_features**: boolean, optional (default=False)
  Whether features are drawn with replacement.

- **oob_score**: bool
  Whether to use out-of-bag samples to estimate the generalization error.

- **warm_start**: bool, optional (default=False)
  When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new ensemble.
**n_jobs** : int, optional (default=1)

The number of jobs to run in parallel for both fit and predict. If -1, then the number of jobs is set to the number of cores.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**verbose** : int, optional (default=0)

Controls the verbosity of the building process.

### Attributes

<table>
<thead>
<tr>
<th><strong>estimators_samples_</strong></th>
<th>The subset of drawn samples for each base estimator.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>estimators_</strong></th>
<th>(list of estimators) The collection of fitted sub-estimators.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>estimators_features_</strong></th>
<th>(list of arrays) The subset of drawn features for each base estimator.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>oob_score_</strong></th>
<th>(float) Score of the training dataset obtained using an out-of-bag estimate.</th>
</tr>
</thead>
</table>

| **oob_prediction_** | (array of shape = [n_samples]) Prediction computed with out-of-bag estimate on the training set. If n_estimators is small it might be possible that a data point was never left out during the bootstrap. In this case, oob_prediction_ might contain NaN. |

### References

[R6568], [R6668], [R6768], [R6868]

### Methods

<table>
<thead>
<tr>
<th><strong>fit(X, y[, sample_weight])</strong></th>
<th>Build a Bagging ensemble of estimators from the training set (X, y).</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>get_params([deep])</strong></th>
<th>Get parameters for this estimator.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>predict(X)</strong></th>
<th>Predict regression target for X.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th><strong>score(X, y[, sample_weight])</strong></th>
<th>Returns the coefficient of determination R^2 of the prediction.</th>
</tr>
</thead>
</table>

<table>
<thead>
<tr>
<th>**set_params(<strong>params)</strong></th>
<th>Set the parameters of this estimator.</th>
</tr>
</thead>
</table>

**__init__**(base_estimator=None, n_estimators=10, max_samples=1.0, max_features=1.0, bootstrap=True, bootstrap_features=False, oob_score=False, warm_start=False, n_jobs=1, random_state=None, verbose=0)

**estimators_samples_**

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of boolean masks identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.
Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.

**fit** *(X, y, sample_weight=None)*  
Build a Bagging ensemble of estimators from the training set *(X, y).*

**Parameters**  
- **X**: {array-like, sparse matrix} of shape = [n_samples, n_features]  
The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.
- **y**: array-like, shape = [n_samples]  
The target values (class labels in classification, real numbers in regression).
- **sample_weight**: array-like, shape = [n_samples] or None  
Sample weights. If None, then samples are equally weighted. Note that this is supported only if the base estimator supports sample weighting.

**Returns**  
- **self**: object  
Returns self.

**get_params** *(deep=True)*  
Get parameters for this estimator.

**Parameters**  
- **deep**: boolean, optional  
If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**  
- **params**: mapping of string to any  
Parameter names mapped to their values.

**predict** *(X)*  
Predict regression target for X.

The predicted regression target of an input sample is computed as the mean predicted regression targets of the estimators in the ensemble.

**Parameters**  
- **X**: {array-like, sparse matrix} of shape = [n_samples, n_features]  
The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns**  
- **y**: array of shape = [n_samples]  
The predicted values.

**score** *(X, y, sample_weight=None)*  
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters**  
- **X**: array-like, shape = (n_samples, n_features)  
Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.

**sample_weight** : array-like, shape = [n_samples], optional
Sample weights.

Returns **score** : float
R^2 of self.predict(X) wrt. y.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

Examples using `sklearn.ensemble.BaggingRegressor`

- Single estimator versus bagging: bias-variance decomposition

### 30.11.5 sklearn.ensemble.IsolationForest

**class** `sklearn.ensemble.IsolationForest` (n_estimators=100, max_samples='auto', contamination=0.1, max_features=1.0, bootstrap=False, n_jobs=1, random_state=None, verbose=0)

Isolation Forest Algorithm

Return the anomaly score of each sample using the IsolationForest algorithm

The IsolationForest ‘isolates’ observations by randomly selecting a feature and then randomly selecting a split value between the maximum and minimum values of the selected feature.

Since recursive partitioning can be represented by a tree structure, the number of splittings required to isolate a sample is equivalent to the path length from the root node to the terminating node.

This path length, averaged over a forest of such random trees, is a measure of normality and our decision function.

Random partitioning produces noticeably shorter paths for anomalies. Hence, when a forest of random trees collectively produce shorter path lengths for particular samples, they are highly likely to be anomalies.

Read more in the User Guide.

New in version 0.18.

**Parameters**

- **n_estimators** : int, optional (default=100)
  The number of base estimators in the ensemble.

- **max_samples** : int or float, optional (default=”auto”)
  The number of samples to draw from X to train each base estimator.
  - If int, then draw `max_samples` samples.
  - If float, then draw `max_samples` * X.shape[0] samples.
  - If “auto”, then `max_samples`=min(256, n_samples).

If max_samples is larger than the number of samples provided, all samples will be used for all trees (no sampling).
contamination : float in (0., 0.5), optional (default=0.1)

The amount of contamination of the data set, i.e. the proportion of outliers in the data set. Used when fitting to define the threshold on the decision function.

max_features : int or float, optional (default=1.0)

The number of features to draw from X to train each base estimator.

- If int, then draw max_features features.
- If float, then draw max_features * X.shape[1] features.

bootstrap : boolean, optional (default=False)

If True, individual trees are fit on random subsets of the training data sampled with replacement. If False, sampling without replacement is performed.

n_jobs : integer, optional (default=1)

The number of jobs to run in parallel for both fit and predict. If -1, then the number of jobs is set to the number of cores.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

verbose : int, optional (default=0)

Controls the verbosity of the tree building process.

Attributes

estimators_samples_ The subset of drawn samples for each base estimator.

estimators_ (list of DecisionTreeClassifier) The collection of fitted sub-estimators.

max_samples_ (integer) The actual number of samples

References

[R7778], [R7878]

Methods

decision_function(X) Average anomaly score of X of the base classifiers.

fit(X[, y, sample_weight]) Fit estimator.

get_params([deep]) Get parameters for this estimator.

predict(X) Predict if a particular sample is an outlier or not.

set_params(**params) Set the parameters of this estimator.

__init__ (n_estimators=100, max_samples='auto', contamination=0.1, max_features=1.0, bootstrap=False, n_jobs=1, random_state=None, verbose=0)
**decision_function** *(X)*

Average anomaly score of X of the base classifiers.

The anomaly score of an input sample is computed as the mean anomaly score of the trees in the forest.

The measure of normality of an observation given a tree is the depth of the leaf containing this observation, which is equivalent to the number of splittings required to isolate this point. In case of several observations n_left in the leaf, the average path length of a n_left samples isolation tree is added.

**Parameters**

* X : {array-like, sparse matrix}, shape (n_samples, n_features)

  The training input samples. Sparse matrices are accepted only if they are supported by the base estimator.

**Returns**

* scores : array of shape (n_samples,)

  The anomaly score of the input samples. The lower, the more abnormal.

**estimators_samples_**

The subset of drawn samples for each base estimator.

Returns a dynamically generated list of boolean masks identifying the samples used for fitting each member of the ensemble, i.e., the in-bag samples.

*Note: the list is re-created at each call to the property in order to reduce the object memory footprint by not storing the sampling data. Thus fetching the property may be slower than expected.*

**fit** *(X, y=None, sample_weight=None)*

Fit estimator.

**Parameters**

* X : array-like or sparse matrix, shape (n_samples, n_features)

  The input samples. Use `dtype=np.float32` for maximum efficiency. Sparse matrices are also supported, use sparse `csc_matrix` for maximum efficiency.

* sample_weight : array-like, shape = [n_samples] or None

  Sample weights. If None, then samples are equally weighted.

**Returns**

* self : object

  Returns self.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

* deep : boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

* params : mapping of string to any

  Parameter names mapped to their values.

**predict** *(X)*

Predict if a particular sample is an outlier or not.

**Parameters**

* X : array-like or sparse matrix, shape (n_samples, n_features)

  The input samples. Internally, it will be converted to `dtype=np.float32` and if a sparse matrix is provided to a sparse `csr_matrix`.

**Returns**

* is_inlier : array, shape (n_samples,)

  For each observations, tells whether or not (+1 or -1) it should be considered as an inlier according to the fitted model.
set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns self

Examples using sklearn.ensemble.IsolationForest

• Outlier detection with several methods.
• IsolationForest example

30.11.6 sklearn.ensemble.RandomTreesEmbedding

class sklearn.ensemble.RandomTreesEmbedding (n_estimators=10, max_depth=5,
 min_samples_split=2, min_samples_leaf=1,
 min_weight_fraction_leaf=0.0,
 max_leaf_nodes=None,
 min_impurity_decrease=0.0,
 min_impurity_split=None, sparse_output=True,
 n_jobs=1, random_state=None, verbose=0,
 warm_start=False)

An ensemble of totally random trees.

An unsupervised transformation of a dataset to a high-dimensional sparse representation. A datapoint is coded
according to which leaf of each tree it is sorted into. Using a one-hot encoding of the leaves, this leads to a
binary coding with as many ones as there are trees in the forest.

The dimensionality of the resulting representation is n_out <= n_estimators * max_leaf_nodes. If
max_leaf_nodes == None, the number of leaf nodes is at most n_estimators * 2 **
max_depth.

Read more in the User Guide.

Parameters n_estimators : integer, optional (default=10)

Number of trees in the forest.

max_depth : integer, optional (default=5)

The maximum depth of each tree. If None, then nodes are expanded until all leaves are
pure or until all leaves contain less than min_samples_split samples.

min_samples_split : int, float, optional (default=2)

The minimum number of samples required to split an internal node:

• If int, then consider min_samples_split as the minimum number.

• If float, then min_samples_split is a percentage and ceil(min_samples_split *
n_samples) is the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

min_samples_leaf : int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

• If int, then consider min_samples_leaf as the minimum number.
• If float, then \textit{min\_samples\_leaf} is a percentage and \textit{cei}(min\_samples\_leaf \times n\_samples) is the minimum number of samples for each node.

  Changed in version 0.18: Added float values for percentages.

\textbf{min\_weight\_fraction\_leaf} : float, optional (default=0.)

  The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

\textbf{max\_leaf\_nodes} : int or None, optional (default=None)

  Grow trees with \textit{max\_leaf\_nodes} in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

\textbf{min\_impurity\_split} : float,

  Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

  Deprecated since version 0.19: \textit{min\_impurity\_split} has been deprecated in favor of \textit{min\_impurity\_decrease} in 0.19 and will be removed in 0.21. Use \textit{min\_impurity\_decrease} instead.

\textbf{min\_impurity\_decrease} : float, optional (default=0.)

  A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

  The weighted impurity decrease equation is the following:

  \[
  \frac{N_t}{N} \times (\text{impurity} - \frac{N_{t\_R}}{N_t} \times \text{right\_impurity} - \frac{N_{t\_L}}{N_t} \times \text{left\_impurity})
  \]

  where \(N\) is the total number of samples, \(N_t\) is the number of samples at the current node, \(N_{t\_L}\) is the number of samples in the left child, and \(N_{t\_R}\) is the number of samples in the right child.

  \(N, N_t, N_{t\_R}\) and \(N_{t\_L}\) all refer to the weighted sum, if sample_weight is passed.

  New in version 0.19.

\textbf{bootstrap} : boolean, optional (default=True)

  Whether bootstrap samples are used when building trees.

\textbf{sparse\_output} : bool, optional (default=True)

  Whether or not to return a sparse CSR matrix, as default behavior, or to return a dense array compatible with dense pipeline operators.

\textbf{n\_jobs} : integer, optional (default=1)

  The number of jobs to run in parallel for both \textit{fit} and \textit{predict}. If -1, then the number of jobs is set to the number of cores.

\textbf{random\_state} : int, RandomState instance or None, optional (default=None)

  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by \textit{np.random}.

\textbf{verbose} : int, optional (default=0)
Controls the verbosity of the tree building process.

**warm_start** : bool, optional (default=False)

When set to True, reuse the solution of the previous call to fit and add more estimators to the ensemble, otherwise, just fit a whole new forest.

**Attributes**

| estimators_ | (list of DecisionTreeClassifier) The collection of fitted sub-estimators. |

**References**

[R8586], [R8686]

**Methods**

- **apply**(X)
  Apply trees in the forest to X, return leaf indices.

- **decision_path**(X)
  Return the decision path in the forest

- **fit**(X[, y, sample_weight])
  Fit estimator.

- **fit_transform**(X[, y, sample_weight])
  Fit estimator and transform dataset.

- **get_params**(deep=False)
  Get parameters for this estimator.

- **set_params**(**params)
  Set the parameters of this estimator.

- **transform**(X)
  Transform dataset.

**__init__**(n_estimators=10, max_depth=5, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, sparse_output=True, n_jobs=1, random_state=None, verbose=0, warm_start=False)

**apply**(X)
Apply trees in the forest to X, return leaf indices.

**Parameters** X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns** X_leaves : array_like, shape = [n_samples, n_estimators]

For each datapoint x in X and for each tree in the forest, return the index of the leaf x ends up in.

**decision_path**(X)
Return the decision path in the forest

New in version 0.18.

**Parameters** X : array-like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, its dtype will be converted to dtype=np.float32. If a sparse matrix is provided, it will be converted into a sparse csr_matrix.

**Returns** indicator : sparse csr array, shape = [n_samples, n_nodes]
Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**n_nodes_ptr** : array of size (n_estimators + 1, )

The columns from indicator[n_nodes_ptr[i]:n_nodes_ptr[i+1]] gives the indicator value for the i-th estimator.

**feature_importances_**

Return the feature importances (the higher, the more important the feature).

Returns **feature_importances_** : array, shape = [n_features]

**fit** *(X, y=None, sample_weight=None)*

Fit estimator.

**Parameters**

- **X** : array-like or sparse matrix, shape=(n_samples, n_features)
  
The input samples. Use `dtype=np.float32` for maximum efficiency. Sparse matrices are also supported, use sparse `csc_matrix` for maximum efficiency.

- **sample_weight** : array-like, shape = [n_samples] or None
  
  Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

Returns **self** : object

Returns self.

**fit_transform** *(X, y=None, sample_weight=None)*

Fit estimator and transform dataset.

**Parameters**

- **X** : array-like or sparse matrix, shape=(n_samples, n_features)
  
  Input data used to build forests. Use `dtype=np.float32` for maximum efficiency.

- **sample_weight** : array-like, shape = [n_samples] or None
  
  Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. In the case of classification, splits are also ignored if they would result in any single class carrying a negative weight in either child node.

Returns **X_transformed** : sparse matrix, shape=(n_samples, n_out)

Transformed dataset.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns **params** : mapping of string to any

Parameter names mapped to their values.
**set_params(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

**transform**(X)

Transform dataset.

Parameters X : array-like or sparse matrix, shape=(n_samples, n_features)

Input data to be transformed. Use dtype=np.float32 for maximum efficiency.
Sparse matrices are also supported, use sparse csr_matrix for maximum efficiency.

Returns X_transformed : sparse matrix, shape=(n_samples, n_out)

Transformed dataset.

Examples using sklearn.ensemble.RandomTreesEmbedding

- Hashing feature transformation using Totally Random Trees
- Feature transformations with ensembles of trees
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

30.11.7 sklearn.ensemble.VotingClassifier

class sklearn.ensemble.VotingClassifier(**estimators**, voting='hard', weights=None, n_jobs=1, flatten_transform=None)

Soft Voting/Majority Rule classifier for unfitted estimators.
New in version 0.17.

Read more in the User Guide.

Parameters estimators : list of (string, estimator) tuples

Invoking the fit method on the VotingClassifier will fit clones of those original estimators that will be stored in the class attribute self.estimators_. An estimator can be set to None using set_params.

voting : str, {‘hard’, ‘soft’} (default=’hard’)

If ‘hard’, uses predicted class labels for majority rule voting. Else if ‘soft’, predicts the class label based on the argmax of the sums of the predicted probabilities, which is recommended for an ensemble of well-calibrated classifiers.

weights : array-like, shape = [n_classifiers], optional (default=’None’)

Sequence of weights (float or int) to weight the occurrences of predicted class labels (hard voting) or class probabilities before averaging (soft voting). Uses uniform weights if None.

n_jobs : int, optional (default=1)

The number of jobs to run in parallel for fit. If -1, then the number of jobs is set to the number of cores.

flatten_transform : bool, optional (default=None)
Affects shape of transform output only when voting='soft' If voting='soft' and flatten_transform=True, transform method returns matrix with shape (n_samples, n_classifiers * n_classes). If flatten_transform=False, it returns (n_classifiers, n_samples, n_classes).

**Attributes**

<table>
<thead>
<tr>
<th><strong>estimators_</strong></th>
<th>(list of classifiers) The collection of fitted sub-estimators as defined in estimators that are not None.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>named_estimators</strong></td>
<td>(Bunch object, a dictionary with attribute access) Attribute to access any fitted sub-estimators by name. .. versionadded:: 0.20</td>
</tr>
<tr>
<td><strong>classes_</strong></td>
<td>(array-like, shape = [n_predictions]) The classes labels.</td>
</tr>
</tbody>
</table>

**Examples**

```python
>>> import numpy as np
>>> from sklearn.linear_model import LogisticRegression
>>> from sklearn.naive_bayes import GaussianNB
>>> from sklearn.ensemble import RandomForestClassifier, VotingClassifier

>>> clf1 = LogisticRegression(random_state=1)
>>> clf2 = RandomForestClassifier(random_state=1)
>>> clf3 = GaussianNB()

>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
>>> y = np.array([1, 1, 1, 2, 2, 2])

>>> eclf1 = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)], voting='hard')
>>> eclf1 = eclf1.fit(X, y)
>>> print(eclf1.predict(X))
[1 1 1 2 2 2]
>>> np.array_equal(eclf1.named_estimators_.lr.predict(X), eclf1.named_estimators_['lr'].predict(X))
True

>>> eclf2 = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)], voting='soft')
>>> eclf2 = eclf2.fit(X, y)
>>> print(eclf2.predict(X))
[1 1 1 2 2 2]

>>> eclf3 = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2), ('gnb', clf3)],
... voting='soft', weights=[2, 1, 1],
... flatten_transform=True)
>>> eclf3 = eclf3.fit(X, y)
>>> print(eclf3.predict(X))
[1 1 1 2 2 2]

>>> print(eclf3.transform(X).shape)
(6, 6)
```

**Methods**
**VotingClassifier**

Parameters:
- **estimators**: list of estimators of shape 
  
  ```python
  [estimator1, estimator2, ..., estimatorM]
  ```
  where `M` is the number of estimators.

  Each estimator in the list must provide methods `fit` and `predict`.

- **voting**: string, default='hard'
  - 'hard': Use hard voting. The predicted class is the argmax of the predicted probabilities.
  - 'soft': Use soft voting. The predicted class probabilities are averaged.

- **weights**: array of shape `[M]`, default=None
  - Weights for the individual classifiers. If None, all classifiers are equally weighted.

- **n_jobs**: int, default=1
  - Number of jobs to run in parallel. Setting to None runs in one job.

- **flatten_transform**: bool, default=None
  - Whether to call `transform` as `transform(X)` or just `transform`.

**Methods**

- __init__
  ```python
  (estimators, voting='hard', weights=None, n_jobs=1, flatten_transform=None)
  ```

- `fit(X, y[, sample_weight])`
  - Fit the estimators.
  ```
  Parameters
  X : {array-like, sparse matrix}, shape = [n_samples, n_features]
      Training vectors, where n_samples is the number of samples and
      n_features is the number of features.
  
  y : array-like, shape = [n_samples]
      Target values.
  
  Returns
  self : object
  ```

- `fit_transform(X[, y])`
  - Fit to data, then transform it.
  ```
  Parameters
  X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  ```

- `get_params([deep])`
  - Get the parameters of the VotingClassifier
  ```
  Parameters
  deep : bool
      Setting it to True gets the various classifiers and the parameters of the classifiers as well
  ```

- `predict(X)`
  - Predict class labels for X.
  ```
  Parameters
  X : {array-like, sparse matrix}, shape = [n_samples, n_features]
      Training vectors, where n_samples is the number of samples and n_features is the number of features.
  ```

- `score(X, y[, sample_weight])`
  - Returns the mean accuracy on the given test data and labels.
  ```
  Parameters
  X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  y : array-like, shape = [n_samples]
  ```

- `set_params(**params)`
  - Setting the parameters for the voting classifier

- `transform(X)`
  - Return class labels or probabilities for X for each estimator.
  ```
  Parameters
  X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  ```

---

**sklearn.ensemble**: Ensemble Methods

30.11.
Predicted class labels.

**predict_proba**
Compute probabilities of possible outcomes for samples in X.

**Parameters**
- **X**: {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of features.

**Returns**
- **avg**: array-like, shape = [n_samples, n_classes]
  - Weighted average probability for each class per sample.

**score** *(X, y, sample_weight=None)*
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**
- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**
- **score**: float
  - Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)
Setting the parameters for the voting classifier

Valid parameter keys can be listed with get_params().

**Parameters**
- **params**: keyword arguments
  - Specific parameters using e.g. set_params(parameter_name=new_value) In addition, to setting the parameters of the VotingClassifier, the individual classifiers of the VotingClassifier can also be set or replaced by setting them to None.

**Examples**

# In this example, the RandomForestClassifier is removed
clf1 = LogisticRegression()
clf2 = RandomForestClassifier()
eclf = VotingClassifier(estimators=[('lr', clf1), ('rf', clf2)])
eclf.set_params(rf=None)

**transform** *(X)*
Return class labels or probabilities for X for each estimator.

**Parameters**
- **X**: {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of features.

**Returns**
- If `voting='soft'` and `flatten_transform=True`:
  - array-like = (n_classifiers, n_samples * n_classes) otherwise array-like = (n_classifiers, n_samples, n_classes)
Class probabilities calculated by each classifier.

If `voting='hard'`:  

array-like = [n_samples, n_classifiers] Class labels predicted by each classifier.

Examples using `sklearn.ensemble.VotingClassifier`

- Plot the decision boundaries of a VotingClassifier
- Plot class probabilities calculated by the VotingClassifier

## 30.11.8 partial dependence

Partial dependence plots for tree ensembles.

```
ensemble.partial_dependence.
partial_dependence(...)  # Partial dependence of target_variables.

ensemble.partial_dependence.
plot_partial_dependence(...)  # Partial dependence plots for features.
```

```
sklearn.ensemble.partial_dependence.partial_dependence
gbrt, target_variables,  # Partial dependence of target_variables.
grid=None, X=None,  # Partial dependence plots show the dependence between the joint values of the target_variables and the
percentiles=(0.05, 0.95),  # function represented by the gbrt.
grid_resolution=100  # Read more in the User Guide.
```

**Parameters**

- **gbrt**: BaseGradientBoosting  
  A fitted gradient boosting model.
- **target_variables**: array-like, dtype=int  
  The target features for which the partial dependency should be computed (size should be smaller than 3 for visual renderings).
- **grid**: array-like, shape=(n_points, len(target_variables))  
  The grid of target_variables values for which the partial dependency should be evaluated (either grid or X must be specified).
- **X**: array-like, shape=(n_samples, n_features)  
  The data on which gbrt was trained. It is used to generate a grid for the target_variables. The grid comprises grid_resolution equally spaced points between the two percentiles.
- **percentiles**: (low, high), default=(0.05, 0.95)
The lower and upper percentile used create the extreme values for the grid. Only if \( X \) is not None.

**grid_resolution** : int, default=100

The number of equally spaced points on the grid.

**Returns pdp** : array, shape=(n_classes, n_points)

The partial dependence function evaluated on the grid. For regression and binary classification \( n_{classes}=1 \).

**axes** : seq of ndarray or None

The axes with which the grid has been created or None if the grid has been given.

**Examples**

```python
gbrt = GradientBoostingClassifier(random_state=0).fit(samples, labels)
gbrt.partial_dependence(X=samples, percentiles=(0, 1), grid_resolution=2)
```

**Examples using sklearn.ensemble.partial_dependence.partial_dependence**

- Partial Dependence Plots

**sklearn.ensemble.partial_dependence.plot_partial_dependence**

```python
sklearn.ensemble.partial_dependence.plot_partial_dependence(gbrt, X, features, feature_names=None, label=None, n_cols=3, grid_resolution=100, percentiles=(0.05, 0.95), n_jobs=1, verbose=0, ax=None, line_kw=None, contour_kw=None, **fig_kw)
```

Partial dependence plots for features.

The len(features) plots are arranged in a grid with n_cols columns. Two-way partial dependence plots are plotted as contour plots.

Read more in the User Guide.

**Parameters gbrt** : BaseGradientBoosting

A fitted gradient boosting model.

**X** : array-like, shape=(n_samples, n_features)

The data on which \( gbrt \) was trained.
features: seq of ints, strings, or tuples of ints or strings

If seq[i] is an int or a tuple with one int value, a one-way PDP is created; if seq[i] is a tuple of two ints, a two-way PDP is created. If feature_names is specified and seq[i] is an int, seq[i] must be < len(feature_names). If seq[i] is a string, feature_names must be specified, and seq[i] must be in feature_names.

feature_names: seq of str

Name of each feature; feature_names[i] holds the name of the feature with index i.

label: object

The class label for which the PDPs should be computed. Only if gbdt is a multi-class model. Must be in gbdt.classes_.

n_cols: int

The number of columns in the grid plot (default: 3).

percentiles: (low, high), default=(0.05, 0.95)

The lower and upper percentile used to create the extreme values for the PDP axes.

grid_resolution: int, default=100

The number of equally spaced points on the axes.

n_jobs: int

The number of CPUs to use to compute the PDs. -1 means ‘all CPUs’. Defaults to 1.

verbose: int

Verbose output during PD computations. Defaults to 0.

ax: Matplotlib axis object, default None

An axis object onto which the plots will be drawn.

line_kw: dict

Dict with keywords passed to the matplotlib.pyplot.plot call. For one-way partial dependence plots.

contour_kw: dict

Dict with keywords passed to the matplotlib.pyplot.plot call. For two-way partial dependence plots.

fig_kw: dict

Dict with keywords passed to the figure() call. Note that all keywords not recognized above will be automatically included here.

Returns:

fig: figure

The Matplotlib Figure object.

axs: seq of Axis objects

A seq of Axis objects, one for each subplot.
Examples

```python
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.ensemble import GradientBoostingRegressor
>>> X, y = make_friedman1()
>>> clf = GradientBoostingRegressor(n_estimators=10).fit(X, y)
>>> fig, axs = plot_partial_dependence(clf, X, [0, (0, 1)])
...```

Examples using `sklearn.ensemble.partial_dependence.plot_partial_dependence`

- **Partial Dependence Plots**

## 30.12 `sklearn.exceptions`: Exceptions and warnings

The `sklearn.exceptions` module includes all custom warnings and error classes used across scikit-learn.

### 30.12.1 `sklearn.exceptions.ChangedBehaviorWarning`

**class sklearn.exceptions.ChangedBehaviorWarning**

Warning class used to notify the user of any change in the behavior.

Changed in version 0.18: Moved from `sklearn.base`.

**Attributes**

<table>
<thead>
<tr>
<th>Name</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>args</code></td>
</tr>
</tbody>
</table>

**Methods**
### 30.12.2 sklearn.exceptions.ConvergenceWarning

#### class sklearn.exceptions.ConvergenceWarning
Custom warning to capture convergence problems

Changed in version 0.18: Moved from sklearn.utils.

**Attributes**

- `args`

**Methods**

- `with_traceback`

```python
with_traceback()  
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

### 30.12.3 sklearn.exceptions.DataConversionWarning

#### class sklearn.exceptions.DataConversionWarning
Warning used to notify implicit data conversions happening in the code.

This warning occurs when some input data needs to be converted or interpreted in a way that may not match the user’s expectations.

**For example, this warning may occur when the user**

- passes an integer array to a function which expects float input and will convert the input
- requests a non-copying operation, but a copy is required to meet the implementation’s data-type expectations;
- passes an input whose shape can be interpreted ambiguously.

Changed in version 0.18: Moved from sklearn.utils.validation.

**Attributes**

- `args`
Methods

**with_traceback**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

**with_traceback()**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

### 30.12.4 sklearn.exceptions.DataDimensionalityWarning

class sklearn.exceptions.DataDimensionalityWarning

Custom warning to notify potential issues with data dimensionality.

For example, in random projection, this warning is raised when the number of components, which quantifies the dimensionality of the target projection space, is higher than the number of features, which quantifies the dimensionality of the original source space, to imply that the dimensionality of the problem will not be reduced.

Changed in version 0.18: Moved from sklearn.utils.

**Attributes**

**args**

**Methods**

**with_traceback**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

**with_traceback()**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

### 30.12.5 sklearn.exceptions.EfficiencyWarning

class sklearn.exceptions.EfficiencyWarning

Warning used to notify the user of inefficient computation.

This warning notifies the user that the efficiency may not be optimal due to some reason which may be included as a part of the warning message. This may be subclassed into a more specific Warning class.

New in version 0.18.

**Attributes**

**args**
Methods

**with_traceback**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

**with_traceback()**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

### 30.12.6 sklearn.exceptions.FitFailedWarning

class sklearn.exceptions.FitFailedWarning

Warning class used if there is an error while fitting the estimator.

This Warning is used in meta estimators GridSearchCV and RandomizedSearchCV and the cross-validation helper function cross_val_score to warn when there is an error while fitting the estimator.

**Attributes**

*args*

**Examples**

```python
>>> from sklearn.model_selection import GridSearchCV
>>> from sklearn.svm import LinearSVC
>>> from sklearn.exceptions import FitFailedWarning
>>> import warnings

>>> warnings.simplefilter('always', FitFailedWarning)

>>> gs = GridSearchCV(LinearSVC(), {'C': [-1, -2]}, error_score=0)
>>> X, y = [[1, 2], [3, 4], [5, 6], [7, 8], [8, 9]], [0, 0, 0, 1, 1]
>>> with warnings.catch_warnings(record=True) as w:
... try:
...     gs.fit(X, y)  # This will raise a ValueError since C is < 0
... except ValueError:
...     pass
...     print(repr(w[-1].message))
...
FitFailedWarning("Classifier fit failed. The score on this train-test partition for these parameters will be set to 0.000000. Details:\n\nValueError('Penalty term must be positive; got (C=-2)'\n")
```

Changed in version 0.18: Moved from sklearn.cross_validation.

### Methods

**with_traceback**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.

**with_traceback()**

Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
30.12.7 sklearn.exceptions.NotFittedError

class sklearn.exceptions.NotFittedError
Exception class to raise if estimator is used before fitting.

This class inherits from both ValueError and AttributeError to help with exception handling and backward compatibility.

Attributes

- **args**

Examples

```python
>>> from sklearn.svm import LinearSVC
>>> from sklearn.exceptions import NotFittedError
>>> try:
...    LinearSVC().predict([[1, 2], [2, 3], [3, 4]])
... except NotFittedError as e:
...    print(repr(e))
...NotFittedError('This LinearSVC instance is not fitted yet',)
```

Changed in version 0.18: Moved from sklearn.utils.validation.

Methods

- **with_traceback**

```python
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

```
with_traceback()
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

30.12.8 sklearn.exceptions.NonBLASDotWarning

class sklearn.exceptions.NonBLASDotWarning
Warning used when the dot operation does not use BLAS.

This warning is used to notify the user that BLAS was not used for dot operation and hence the efficiency may be affected.

Changed in version 0.18: Moved from sklearn.utils.validation, extends EfficiencyWarning.

Attributes

- **args**
Methods

```
with_traceback
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

```
with_traceback()
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

### 30.12.9 `sklearn.exceptions.UndefinedMetricWarning`

#### class `sklearn.exceptions.UndefinedMetricWarning`

Warning used when the metric is invalid

Changed in version 0.18: Moved from sklearn.base.

Attributes

```
args
```

Methods

```
with_traceback
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

```
with_traceback()
Exception.with_traceback(tb) – set self.__traceback__ to tb and return self.
```

### 30.13 `sklearn.feature_extraction`: Feature Extraction

The `sklearn.feature_extraction` module deals with feature extraction from raw data. It currently includes methods to extract features from text and images.

**User guide:** See the Feature extraction section for further details.

```
feature_extraction.DictVectorizer([dtype,
...])
```

```
feature_extraction.FeatureHasher([...])
```

Implement feature hashing, aka the hashing trick.

#### 30.13.1 `sklearn.feature_extraction.DictVectorizer`

#### class `sklearn.feature_extraction.DictVectorizer` (`dtyper=class ‘numpy.float64’, separator=‘ ‘, sparse=True, sort=NotImplementedType)```

Transforms lists of feature-value mappings to vectors.

This transformer turns lists of mappings (dict-like objects) of feature names to feature values into Numpy arrays or scipy.sparse matrices for use with scikit-learn estimators.
When feature values are strings, this transformer will do a binary one-hot (aka one-of-K) coding: one boolean-valued feature is constructed for each of the possible string values that the feature can take on. For instance, a feature “f” that can take on the values “ham” and “spam” will become two features in the output, one signifying “f=ham”, the other “f=spam”.

However, note that this transformer will only do a binary one-hot encoding when feature values are of type string. If categorical features are represented as numeric values such as int, the DictVectorizer can be followed by OneHotEncoder to complete binary one-hot encoding.

Features that do not occur in a sample (mapping) will have a zero value in the resulting array/matrix.

Read more in the User Guide.

**Parameters**

- **dtype** : callable, optional
  The type of feature values. Passed to Numpy array/scipy.sparse matrix constructors as the dtype argument.
- **separator** : string, optional
  Separator string used when constructing new features for one-hot coding.
- **sparse** : boolean, optional.
  Whether transform should produce scipy.sparse matrices. True by default.
- **sort** : boolean, optional.
  Whether feature_names_ and vocabulary_ should be sorted when fitting. True by default.

**Attributes**

- **vocabulary_** : (dict) A dictionary mapping feature names to feature indices.
- **feature_names_** : (list) A list of length n_features containing the feature names (e.g., “f=ham” and “f=spam”).

See also:

- **FeatureHasher** performs vectorization using only a hash function.
- **sklearn.preprocessing.OneHotEncoder** handles nominal/categorical features encoded as columns of integers.

**Examples**

```python
>>> from sklearn.feature_extraction import DictVectorizer
>>> v = DictVectorizer(sparse=False)
>>> D = [{'foo': 1, 'bar': 2}, {'foo': 3, 'baz': 1}]
>>> X = v.fit_transform(D)
>>> X
array([[ 2.,  0.,  1.],
       [ 0.,  1.,  3.]])
>>> v.inverse_transform(X) == [{'bar': 2.0, 'foo': 1.0}, {'baz': 1.0, 'foo': 3.0}]
True
>>> v.transform({'foo': 4, 'unseen_feature': 3})
array([[ 0.,  0.,  4.]])
```
Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Learn a list of feature name -&gt; indices mappings.</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Learn a list of feature name -&gt; indices mappings and transform X.</td>
</tr>
<tr>
<td>get_feature_names()</td>
<td>Returns a list of feature names, ordered by their indices.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>inverse_transform(X[, dict_type])</td>
<td>Transform array or sparse matrix X back to feature mappings.</td>
</tr>
<tr>
<td>restrict(support[, indices])</td>
<td>Restrict the features to those in support using feature selection.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Transform feature-&gt;value dicts to array or sparse matrix.</td>
</tr>
</tbody>
</table>

__init__ (dtype=<class 'numpy.float64'>, separator='=', sparse=True, sort=True)

fit (X, y=None)
Learn a list of feature name -> indices mappings.

Parameters X : Mapping or iterable over Mappings

- Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values (strings or convertible to dtype).
- y : (ignored)

Returns self

fit_transform (X, y=None)
Learn a list of feature name -> indices mappings and transform X.

Like fit(X) followed by transform(X), but does not require materializing X in memory.

Parameters X : Mapping or iterable over Mappings

- Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values (strings or convertible to dtype).
- y : (ignored)

Returns Xa : {array, sparse matrix}

Feature vectors; always 2-d.

generate_feature_names ()
Returns a list of feature names, ordered by their indices.

If one-of-K coding is applied to categorical features, this will include the constructed feature names but not the original ones.

generate_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.
**Returns** params : mapping of string to any
Parameter names mapped to their values.

**inverse_transform** *(X, dict_type=class 'dict'>)*
Transform array or sparse matrix X back to feature mappings.

X must have been produced by this DictVectorizer’s transform or fit_transform method; it may only have passed through transformers that preserve the number of features and their order.

In the case of one-hot/one-of-K coding, the constructed feature names and values are returned rather than the original ones.

**Parameters** X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Sample matrix.

dict_type : callable, optional
Constructor for feature mappings. Must conform to the collections.Mapping API.

**Returns** D : list of dict_type objects, length = n_samples
Feature mappings for the samples in X.

**restrict** *(support, indices=False)*
Restrict the features to those in support using feature selection.
This function modifies the estimator in-place.

**Parameters** support : array-like
Boolean mask or list of indices (as returned by the get_support member of feature selectors).

indices : boolean, optional
Whether support is a list of indices.

**Returns** self

**Examples**

```python
>>> from sklearn.feature_extraction import DictVectorizer
>>> from sklearn.feature_selection import SelectKBest, chi2
>>> v = DictVectorizer()
>>> D = [{'foo': 1, 'bar': 2}, {'foo': 3, 'baz': 1}]
>>> X = v.fit_transform(D)
>>> support = SelectKBest(chi2, k=2).fit(X, [0, 1])
>>> v.get_feature_names()
['bar', 'baz', 'foo']
>>> v.restrict(support.get_support())
DictVectorizer(dtype=..., separator='=', sort=True, sparse=True)
>>> v.get_feature_names()
['bar', 'foo']
```

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>_<parameter>` so that it’s possible to update each component of a nested object.
Returns self
transform(X)
    Transform feature->value dicts to array or sparse matrix.
    Named features not encountered during fit or fit_transform will be silently ignored.

Parameters X : Mapping or iterable over Mappings, length = n_samples
    Dict(s) or Mapping(s) from feature names (arbitrary Python objects) to feature values
    (strings or convertible to dtype).
Returns Xa : {array, sparse matrix}
    Feature vectors; always 2-d.

Examples using sklearn.feature_extraction.DictVectorizer

• Feature Union with Heterogeneous Data Sources
• FeatureHasher and DictVectorizer Comparison

30.13.2 sklearn.feature_extraction.FeatureHasher
class sklearn.feature_extraction.FeatureHasher (n_features=1048576, input_type='dict',
dtype=<class 'numpy.float64'>, alternate_sign=True, non_negative=False)

Implements feature hashing, aka the hashing trick.
This class turns sequences of symbolic feature names (strings) into scipy.sparse matrices, using a hash function to compute the matrix column corresponding to a name. The hash function employed is the signed 32-bit version of Murmurhash3.
Feature names of type byte string are used as-is. Unicode strings are converted to UTF-8 first, but no Unicode normalization is done. Feature values must be (finite) numbers.
This class is a low-memory alternative to DictVectorizer and CountVectorizer, intended for large-scale (online) learning and situations where memory is tight, e.g. when running prediction code on embedded devices.
Read more in the User Guide.

Parameters n_features : integer, optional
    The number of features (columns) in the output matrices. Small numbers of features are likely to cause hash collisions, but large numbers will cause larger coefficient dimensions in linear learners.

input_type : string, optional, default “dict”
    Either “dict” (the default) to accept dictionaries over (feature_name, value); “pair” to accept pairs of (feature_name, value); or “string” to accept single strings. feature_name should be a string, while value should be a number. In the case of “string”, a value of 1 is implied. The feature_name is hashed to find the appropriate column for the feature. The value’s sign might be flipped in the output (but see non_negative, below).

dtype : numpy type, optional, default np.float64
    The type of feature values. Passed to scipy.sparse matrix constructors as the dtype argument. Do not set this to bool, np.boolean or any unsigned integer type.

alternate_sign : boolean, optional, default True
When True, an alternating sign is added to the features as to approximately conserve the inner product in the hashed space even for small n_features. This approach is similar to sparse random projection.

**non_negative** : boolean, optional, default False

When True, an absolute value is applied to the features matrix prior to returning it. When used in conjunction with alternate_sign=True, this significantly reduces the inner product preservation property.

Deprecated since version 0.19: This option will be removed in 0.21.

See also:

*DictVectorizer* vectorizes string-valued features using a hash table.

*sklearn.preprocessing.OneHotEncoder* handles nominal/categorical features encoded as columns of integers.

**Examples**

```python
>>> from sklearn.feature_extraction import FeatureHasher
>>> h = FeatureHasher(n_features=10)
>>> D = [{'dog': 1, 'cat':2, 'elephant':4},{'dog': 2, 'run': 5}]
>>> f = h.transform(D)
>>> f.toarray()
array([[ 0., 0., -4., -1., 0., 0., 0., 0., 0., 2.],
       [ 0., 0., 0., -2., -5., 0., 0., 0., 0., 0.]])
```

**Methods**

**fit** *(X, y)*

No-op.

**fit_transform** *(X[, y]*)

Fit to data, then transform it.

**get_params** *(**deep**)*

Get parameters for this estimator.

**set_params** *(**params]*)

Set the parameters of this estimator.

**transform** *(raw_X)*

Transform a sequence of instances to a scipy.sparse matrix.

___init___ *(n_features=1048576, input_type='dict', dtype=numpy.float64, alternate_sign=True, non_negative=False)*

**fit** *(X=None, y=None)*

No-op.

This method doesn’t do anything. It exists purely for compatibility with the scikit-learn transformer API.

**Parameters**

* X : array-like

**Returns**

* self : FeatureHasher

**fit_transform** *(X, y=None, **fit_params)*

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

* X : numpy array of shape [n_samples, n_features]
Training set.

\[ y \]: numpy array of shape \([n_{\text{samples}}]\)

Target values.

**Returns** \(X_{\text{new}}\): numpy array of shape \([n_{\text{samples}}, n_{\text{features\_new}}]\)

Transformed array.

**get_params** *(deep=\text{True})*

Get parameters for this estimator.

**Parameters** deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params: mapping of string to any

Parameter names mapped to their values.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_\_<parameter> so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(raw\_X)*

Transform a sequence of instances to a scipy.sparse matrix.

**Parameters** raw\_X: iterable over iterable over raw features, length = n\_samples

Samples. Each sample must be iterable an (e.g., a list or tuple) containing/generating feature names (and optionally values, see the input_type constructor argument) which will be hashed. raw\_X need not support the len function, so it can be the result of a generator; n\_samples is determined on the fly.

**Returns** X: scipy.sparse matrix, shape = (n\_samples, self.n\_features)

Feature matrix, for use with estimators or further transformers.

**Examples using** sklearn.feature_extraction.FeatureHasher

- FeatureHasher and DictVectorizer Comparison

**30.13.3 From images**

The sklearn.feature_extraction.image submodule gathers utilities to extract features from images.

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**sklearn.feature_extraction.image.extract_patches_2d**

Reshape a 2D image into a collection of patches.

The resulting patches are allocated in a dedicated array.

Read more in the [User Guide](#).

**Parameters**

- `image` : array, shape = (image_height, image_width) or (image_height, image_width, n_channels) The original image data. For color images, the last dimension specifies the channel: a RGB image would have n_channels=3.
- `patch_size` : tuple of ints (patch_height, patch_width) the dimensions of one patch
- `max_patches` : integer or float, optional default is None The maximum number of patches to extract. If max_patches is a float between 0 and 1, it is taken to be a proportion of the total number of patches.
- `random_state` : int, RandomState instance or None, optional (default=None) Pseudo number generator state used for random sampling to use if max_patches is not None. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- `patches` : array, shape = (n_patches, patch_height, patch_width) or (n_patches, patch_height, patch_width, n_channels) The collection of patches extracted from the image, where n_patches is either max_patches or the total number of patches that can be extracted.

**Examples**

```python
>>> from sklearn.feature_extraction import image
>>> one_image = np.arange(16).reshape((4, 4))
>>> one_image
array([[ 0,  1,  2,  3],
       [ 4,  5,  6,  7],
       [ 8,  9, 10, 11],
       [12, 13, 14, 15]])
>>> patches = image.extract_patches_2d(one_image, (2, 2))
>>> print(patches.shape)
(9, 2, 2)
>>> patches[0]
array([[0, 1],
       [4, 5]])
```
Examples using `sklearn.feature_extraction.image.extract_patches_2d`

- Online learning of a dictionary of parts of faces
- Image denoising using dictionary learning

`sklearn.feature_extraction.image.grid_to_graph`

`sklearn.feature_extraction.image.grid_to_graph(n_x, n_y, n_z=1, mask=None, return_as=<class 'scipy.sparse.coo.coo_matrix'>, dtype=<class 'int'>)`

Graph of the pixel-to-pixel connections

Edges exist if 2 voxels are connected.

Parameters

- **n_x**: int
  - Dimension in x axis
- **n_y**: int
  - Dimension in y axis
- **n_z**: int, optional, default 1
  - Dimension in z axis
- **mask**: ndarray of booleans, optional
  - An optional mask of the image, to consider only part of the pixels.
- **return_as**: np.ndarray or a sparse matrix class, optional
  - The class to use to build the returned adjacency matrix.
- **dtype**: dtype, optional, default int
  - The data of the returned sparse matrix. By default it is int

Notes

For scikit-learn versions 0.14.1 and prior, return_as=np.ndarray was handled by returning a dense np.matrix instance. Going forward, np.ndarray returns an np.ndarray, as expected.

For compatibility, user code relying on this method should wrap its calls in `np.asarray` to avoid type issues.
Graph of the pixel-to-pixel gradient connections
Edges are weighted with the gradient values.
Read more in the User Guide.

Parameters

- **img**: ndarray, 2D or 3D
  
  2D or 3D image

- **mask**: ndarray of booleans, optional
  
  An optional mask of the image, to consider only part of the pixels.

- **return_as**: np.ndarray or a sparse matrix class, optional
  
  The class to use to build the returned adjacency matrix.

- **dtype**: None or dtype, optional
  
  The data of the returned sparse matrix. By default it is the dtype of img

Notes

For scikit-learn versions 0.14.1 and prior, return_as=np.ndarray was handled by returning a dense np.matrix instance. Going forward, np.ndarray returns an np.ndarray, as expected.

For compatibility, user code relying on this method should wrap its calls in np.asarray to avoid type issues.

Reconstruct the image from all of its patches.

Patches are assumed to overlap and the image is constructed by filling in the patches from left to right, top to bottom, averaging the overlapping regions.

Read more in the User Guide.

Parameters

- **patches**: array, shape = (n_patches, patch_height, patch_width) or
  
  (n_patches, patch_height, patch_width, n_channels) The complete set of patches. If the patches contain colour information, channels are indexed along the last dimension: RGB patches would have n_channels=3.

- **image_size**: tuple of ints (image_height, image_width) or
  
  (image_height, image_width, n_channels) the size of the image that will be reconstructed

Returns

- **image**: array, shape = image_size
  
  the reconstructed image
Examples using `sklearn.feature_extraction.image.reconstruct_from_patches_2d`

- *Image denoising using dictionary learning*

`sklearn.feature_extraction.image.PatchExtractor`

class `sklearn.feature_extraction.image.PatchExtractor`(patch_size=None, max_patches=None, random_state=None)

Extracts patches from a collection of images

Read more in the *User Guide*.

**Parameters**

- patch_size : tuple of ints (patch_height, patch_width)
  the dimensions of one patch

- max_patches : integer or float, optional default is None
  The maximum number of patches per image to extract. If max_patches is a float in (0, 1), it is taken to mean a proportion of the total number of patches.

- random_state : int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**Methods**

- `fit(X[, y])` Do nothing and return the estimator unchanged
- `get_params([deep])` Get parameters for this estimator.
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X)` Transforms the image samples in X into a matrix of patch data.

__init__ (patch_size=None, max_patches=None, random_state=None)

`fit`(X, y=None)

Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

`get_params`(deep=True)

Get parameters for this estimator.

**Parameters**

- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- params : mapping of string to any
  Parameter names mapped to their values.

`set_params` (**params)

Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Transforms the image samples in X into a matrix of patch data.

**Parameters**

- **X** : array, shape = (n_samples, image_height, image_width) or (n_samples, image_height, image_width, n_channels) Array of images from which to extract patches. For color images, the last dimension specifies the channel: a RGB image would have `n_channels=3`.

**Returns**

- **patches** : array, shape = (n_patches, patch_height, patch_width) or (n_patches, patch_height, patch_width, n_channels) The collection of patches extracted from the images, where `n_patches` is either `n_samples * max_patches` or the total number of patches that can be extracted.

### 30.13.4 From text

The `sklearn.feature_extraction.text` submodule gathers utilities to build feature vectors from text documents.

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**sklearn.feature_extraction.text.CountVectorizer**

*class* `sklearn.feature_extraction.text.CountVectorizer`(input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), analyzer='word', max_df=1.0, min_df=1, max_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>)

Convert a collection of text documents to a matrix of token counts

This implementation produces a sparse representation of the counts using scipy.sparse.csr_matrix.

If you do not provide an a-priori dictionary and you do not use an analyzer that does some kind of feature selection then the number of features will be equal to the vocabulary size found by analyzing the data.
Read more in the *User Guide*.

**Parameters**

**input** : string \{‘filename’, ‘file’, ‘content’

If ‘filename’, the sequence passed as an argument to fit is expected to be a list of filenames that need reading to fetch the raw content to analyze.

If ‘file’, the sequence items must have a ‘read’ method (file-like object) that is called to fetch the bytes in memory.

Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.

**encoding** : string, ‘utf-8’ by default.

If bytes or files are given to analyze, this encoding is used to decode.

**decode_error** : \{'strict’, ‘ignore’, ‘replace’

Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given *encoding*. By default, it is ‘strict’, meaning that a UnicodeDecodeError will be raised. Other values are ‘ignore’ and ‘replace’.

**strip_accents** : \{‘ascii’, ‘unicode’, None\}

Remove accents during the preprocessing step. ‘ascii’ is a fast method that only works on characters that have an direct ASCII mapping. ‘unicode’ is a slightly slower method that works on any characters. None (default) does nothing.

**analyzer** : string, \{‘word’, ‘char’, ‘char_wb’\} or callable

Whether the feature should be made of word or character n-grams. Option ‘char_wb’ creates character n-grams only from text inside word boundaries; n-grams at the edges of words are padded with space.

If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.

**preprocessor** : callable or None (default)

Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.

**tokenizer** : callable or None (default)

Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if *analyzer* == ‘word’.

**ngram_range** : tuple \(\text{min}_n, \text{max}_n\)

The lower and upper boundary of the range of n-values for different n-grams to be extracted. All values of \(n\) such that \(\text{min}_n \leq n \leq \text{max}_n\) will be used.

**stop_words** : string \{‘english’\}, list, or None (default)

If ‘english’, a built-in stop word list for English is used.

If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if *analyzer* == ‘word’.

If None, no stop words will be used. max_df can be set to a value in the range \([0.7, 1.0)\) to automatically detect and filter stop words based on intra corpus document frequency of terms.

**lowercase** : boolean, True by default
Convert all characters to lowercase before tokenizing.

**token_pattern**: string

Regular expression denoting what constitutes a “token”, only used if `analyzer == 'word'`. The default regexp select tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).

**max_df**: float in range [0.0, 1.0] or int, default=1.0

When building the vocabulary ignore terms that have a document frequency strictly higher than the given threshold (corpus-specific stop words). If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

**min_df**: float in range [0.0, 1.0] or int, default=1

When building the vocabulary ignore terms that have a document frequency strictly lower than the given threshold. This value is also called cut-off in the literature. If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

**max_features**: int or None, default=None

If not None, build a vocabulary that only consider the top max_features ordered by term frequency across the corpus.

This parameter is ignored if vocabulary is not None.

**vocabulary**: Mapping or iterable, optional

Either a Mapping (e.g., a dict) where keys are terms and values are indices in the feature matrix, or an iterable over terms. If not given, a vocabulary is determined from the input documents. Indices in the mapping should not be repeated and should not have any gap between 0 and the largest index.

**binary**: boolean, default=False

If True, all non zero counts are set to 1. This is useful for discrete probabilistic models that model binary events rather than integer counts.

**dtype**: type, optional

Type of the matrix returned by `fit_transform()` or `transform()`.

### Attributes

| Vocabulary | (dict) A mapping of terms to feature indices. |
| Stop Words | Terms that were ignored because they either: - occurred in too many documents (max_df) - occurred in too few documents (min_df) - were cut off by feature selection (max_features). This is only available if no vocabulary was given. |

See also:

- `HashingVectorizer`
- `TfidfVectorizer`
Notes

The `stop_words_` attribute can get large and increase the model size when pickling. This attribute is provided only for introspection and can be safely removed using delattr or set to None before pickling.

Methods

- `build_analyzer()` Return a callable that handles preprocessing and tokenization
- `build_preprocessor()` Return a function to preprocess the text before tokenization
- `build_tokenizer()` Return a function that splits a string into a sequence of tokens
- `decode(doc)` Decode the input into a string of unicode symbols
- `fit(raw_documents[, y])` Learn a vocabulary dictionary of all tokens in the raw documents.
- `fit_transform(raw_documents[, y])` Learn the vocabulary dictionary and return term-document matrix.
- `get_feature_names()` Array mapping from feature integer indices to feature name
- `get_params([deep])` Get parameters for this estimator.
- `get_stop_words()` Build or fetch the effective stop words list
- `inverse_transform(X)` Return terms per document with nonzero entries in X.
- `set_params(**params)` Set the parameters of this estimator.

```python
__init__(input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), analyzer='word', max_df=1.0, min_df=1, max_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>)
```

- `build_analyzer()` Return a callable that handles preprocessing and tokenization
- `build_preprocessor()` Return a function to preprocess the text before tokenization
- `build_tokenizer()` Return a function that splits a string into a sequence of tokens
- `decode(doc)` Decode the input into a string of unicode symbols
  - The decoding strategy depends on the vectorizer parameters.
- `fit(raw_documents, y=None)` Learn a vocabulary dictionary of all tokens in the raw documents.
  - Parameters `raw_documents` : iterable
    - An iterable which yields either str, unicode or file objects.
  - Returns `self`
**fit_transform** *(raw_documents, y=None)*

Learn the vocabulary dictionary and return term-document matrix.

This is equivalent to fit followed by transform, but more efficiently implemented.

**Parameters**

- **raw_documents**: iterable
  An iterable which yields either str, unicode or file objects.

**Returns**

- **X**: array, [n_samples, n_features]

**get_feature_names** *

Array mapping from feature integer indices to feature name

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**get_stop_words** *

Build or fetch the effective stop words list

**inverse_transform** *(X)*

Return terms per document with nonzero entries in X.

**Parameters**

- **X**: {array, sparse matrix}, shape = [n_samples, n_features]

**Returns**

- **X_inv**: list of arrays, len = n_samples
  List of arrays of terms.

**set_params** *(**params)*

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**transform** *(raw_documents)*

Transform documents to document-term matrix.

Extract token counts out of raw text documents using the vocabulary fitted with fit or the one provided to the constructor.

**Parameters**

- **raw_documents**: iterable
  An iterable which yields either str, unicode or file objects.

**Returns**

- **X**: sparse matrix, [n_samples, n_features]
Examples using `sklearn.feature_extraction.text.CountVectorizer`

- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Sample pipeline for text feature extraction and evaluation

`sklearn.feature_extraction.text.HashingVectorizer`

```python
class sklearn.feature_extraction.text.HashingVectorizer(input='content',
    encoding='utf-8', decode_error='strict',
    strip_accents=None, lowercase=True, preprocessor=None,
    tokenizer=None, stop_words=None, token_pattern='(?u)\b\w\w+\b',
    ngram_range=(1, 1), analyzer='word', n_features=1048576, binary=False,
    norm='l2', alternate_sign=True, non_negative=False,
    dtype=<class 'numpy.float64'>)
```

Convert a collection of text documents to a matrix of token occurrences

It turns a collection of text documents into a scipy.sparse matrix holding token occurrence counts (or binary occurrence information), possibly normalized as token frequencies if norm='l1' or projected on the euclidean unit sphere if norm='l2'.

This text vectorizer implementation uses the hashing trick to find the token string name to feature integer index mapping.

This strategy has several advantages:

- it is very low memory scalable to large datasets as there is no need to store a vocabulary dictionary in memory
- it is fast to pickle and un-pickle as it holds no state besides the constructor parameters
- it can be used in a streaming (partial fit) or parallel pipeline as there is no state computed during fit.

There are also a couple of cons (vs using a CountVectorizer with an in-memory vocabulary):

- there is no way to compute the inverse transform (from feature indices to string feature names) which can be a problem when trying to introspect which features are most important to a model.
- there can be collisions: distinct tokens can be mapped to the same feature index. However in practice this is rarely an issue if n_features is large enough (e.g. 2 ** 18 for text classification problems).
- no IDF weighting as this would render the transformer stateful.

The hash function employed is the signed 32-bit version of Murmurhash3.

Read more in the User Guide.

**Parameters**

- `input` : string {'filename', 'file', 'content'}

  If 'filename', the sequence passed as an argument to fit is expected to be a list of filenames that need reading to fetch the raw content to analyze.
If ‘file’, the sequence items must have a ‘read’ method (file-like object) that is called to fetch the bytes in memory.

Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.

**encoding**: string, default='utf-8'

If bytes or files are given to analyze, this encoding is used to decode.

**decode_error**: {'strict', 'ignore', 'replace'}

Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given `encoding`. By default, it is ‘strict’, meaning that a UnicodeDecodeError will be raised. Other values are ‘ignore’ and ‘replace’.

**strip_accents**: {'ascii', 'unicode', None}

Remove accents during the preprocessing step. ‘ascii’ is a fast method that only works on characters that have a direct ASCII mapping. ‘unicode’ is a slightly slower method that works on any characters. None (default) does nothing.

**analyzer**: string, {'word', 'char', 'char_wb'} or callable

Whether the feature should be made of word or character n-grams. Option ‘char_wb’ creates character n-grams only from text inside word boundaries; n-grams at the edges of words are padded with space.

If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.

**preprocessor**: callable or None (default)

Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.

**tokenizer**: callable or None (default)

Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if `analyzer == 'word'`.

**ngram_range**: tuple (min_n, max_n), default=(1, 1)

The lower and upper boundary of the range of n-values for different n-grams to be extracted. All values of n such that min_n <= n <= max_n will be used.

**stop_words**: string {'english'}, list, or None (default)

If ‘english’, a built-in stop word list for English is used.

If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if `analyzer == 'word'`.

**lowercase**: boolean, default=True

Convert all characters to lowercase before tokenizing.

**token_pattern**: string

Regular expression denoting what constitutes a “token”, only used if `analyzer == 'word'`. The default regexp selects tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).

**n_features**: integer, default=(2 ** 20)
The number of features (columns) in the output matrices. Small numbers of features are likely to cause hash collisions, but large numbers will cause larger coefficient dimensions in linear learners.

**norm**: ‘l1’, ‘l2’ or None, optional
Norm used to normalize term vectors. None for no normalization.

**binary**: boolean, default=False.
If True, all non zero counts are set to 1. This is useful for discrete probabilistic models that model binary events rather than integer counts.

**dtype**: type, optional
Type of the matrix returned by fit_transform() or transform().

**alternate_sign**: boolean, optional, default True
When True, an alternating sign is added to the features as to approximately conserve the inner product in the hashed space even for small n_features. This approach is similar to sparse random projection.

New in version 0.19.

**non_negative**: boolean, optional, default False
When True, an absolute value is applied to the features matrix prior to returning it. When used in conjunction with alternate_sign=True, this significantly reduces the inner product preservation property.

Deprecated since version 0.19: This option will be removed in 0.21.

See also:
CountVectorizer, TfidfVectorizer

**Methods**

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<th>Method</th>
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<td><strong>build_analyzer()</strong></td>
<td>Return a callable that handles preprocessing and tokenization</td>
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<tr>
<td><strong>build_preprocessor()</strong></td>
<td>Return a function to preprocess the text before tokenization</td>
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<td><strong>build_tokenizer()</strong></td>
<td>Return a function that splits a string into a sequence of tokens</td>
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<td><strong>decode(doc)</strong></td>
<td>Decode the input into a string of unicode symbols</td>
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<td><strong>fit(X[, y])</strong></td>
<td>Does nothing: this transformer is stateless.</td>
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<tr>
<td><strong>fit_transform(X[, y])</strong></td>
<td>Fit to data, then transform it.</td>
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<td><strong>get_params([deep])</strong></td>
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<td><strong>get_stop_words()</strong></td>
<td>Build or fetch the effective stop words list</td>
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<tr>
<td><strong>partial_fit(X[, y])</strong></td>
<td>Does nothing: this transformer is stateless.</td>
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<td>**set_params(<strong>params)</strong></td>
<td>Set the parameters of this estimator.</td>
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<tr>
<td><strong>transform(X)</strong></td>
<td>Transform a sequence of documents to a document-term matrix.</td>
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</table>
__init__(input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), analyzer='word', n_features=1048576, binary=False, norm='l2', alternate_sign=True, non_negative=False, dtype=<class 'numpy.float64'>)

build_analyzer()
Return a callable that handles preprocessing and tokenization

build_preprocessor()
Return a function to preprocess the text before tokenization

build_tokenizer()
Return a function that splits a string into a sequence of tokens

decode(doc)
Decode the input into a string of unicode symbols

The decoding strategy depends on the vectorizer parameters.

fit(X, y=None)
Does nothing: this transformer is stateless.

fit_transform(X, y=None, **fit_params)
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]
Training set.

y : numpy array of shape [n_samples]
Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]
Transformed array.

get_params(deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_stop_words()
Build or fetch the effective stop words list

partial_fit(X, y=None)
Does nothing: this transformer is stateless.

This method is just there to mark the fact that this transformer can work in a streaming setup.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>.__<parameter> so that it's possible to update each component of a nested object.
Returns self

transform(X)
Transform a sequence of documents to a document-term matrix.

Parameters X : iterable over raw text documents, length = n_samples
Samples. Each sample must be a text document (either bytes or unicode strings, file
name or file object depending on the constructor argument) which will be tokenized and
hashed.

Returns X : scipy.sparse matrix, shape = (n_samples, self.n_features)

Examples using sklearn.feature_extraction.text.HashingVectorizer

• Out-of-core classification of text documents
• Clustering text documents using k-means
• Classification of text documents using sparse features

sklearn.feature_extraction.text.TfidfTransformer
class sklearn.feature_extraction.text.TfidfTransformer(norm='l2', use_idf=True,
smooth_idf=True, sublinear_tf=False)
Transform a count matrix to a normalized tf or tf-idf representation

Tf means term-frequency while tf-idf means term-frequency times inverse document-frequency. This is a com-
mon term weighting scheme in information retrieval, that has also found good use in document classification.

The goal of using tf-idf instead of the raw frequencies of occurrence of a token in a given document is to scale
down the impact of tokens that occur very frequently in a given corpus and that are hence empirically less
informative than features that occur in a small fraction of the training corpus.

The formula that is used to compute the tf-idf of term t is tf-idf(d, t) = tf(t) * idf(d, t), and the idf is computed
as idf(d, t) = log [ n / df(d, t) ] + 1 (if smooth_idf=False), where n is the total number of documents and
df(d, t) is the document frequency; the document frequency is the number of documents d that contain term t.
The effect of adding “1” to the idf in the equation above is that terms with zero idf, i.e., terms that occur in
all documents in a training set, will not be entirely ignored. (Note that the idf formula above differs from the
standard textbook notation that defines the idf as idf(d, t) = log [ n / (df(d, t) + 1) ].

If smooth_idf=True (the default), the constant “1” is added to the numerator and denominator of the idf
as if an extra document was seen containing every term in the collection exactly once, which prevents zero
divisions: idf(d, t) = log [ (1 + n) / (1 + df(d, t)) ] + 1.

Furthermore, the formulas used to compute tf and idf depend on parameter settings that correspond to the
SMART notation used in IR as follows:

Tf is “n” (natural) by default, “l” (logarithmic) when sublinear_tf=True. Idf is “t” when use_idf is given,
“n” (none) otherwise. Normalization is “c” (cosine) when norm='l2', “n” (none) when norm=None.

Read more in the User Guide.

Parameters norm : ‘l1’, ‘l2’ or None, optional
Norm used to normalize term vectors. None for no normalization.

use_idf : boolean, default=True
Enable inverse-document-frequency reweighting.

**smooth_idf** : boolean, default=True

Smooth idf weights by adding one to document frequencies, as if an extra document was seen containing every term in the collection exactly once. Prevents zero divisions.

**sublinear_tf** : boolean, default=False

Apply sublinear tf scaling, i.e. replace tf with 1 + log(tf).

**Attributes**

**idf_**

**References**

[Yates20118890], [MRS20088890]

**Methods**

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<tr>
<td>fit(X, y=None)</td>
<td>Learn the idf vector (global term weights)</td>
</tr>
<tr>
<td>fit_transform(X, y=None, **fit_params)</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params()</td>
<td>Get parameters for this estimator.</td>
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<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X[, copy])</td>
<td>Transform a count matrix to a tf or tf-idf representation</td>
</tr>
</tbody>
</table>

**__init__** (norm='l2', use_idf=True, smooth_idf=True, sublinear_tf=False)

**fit** (X, y=None)

Learn the idf vector (global term weights)

**Parameters**

X : sparse matrix, [n_samples, n_features]

a matrix of term/token counts

**fit_transform** (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

**Returns**

X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.

**get_params** (deep=True)

Get parameters for this estimator.

**Parameters**

depth : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X, copy=True)
Transform a count matrix to a tf or tf-idf representation

Parameters X : sparse matrix, [n_samples, n_features]
a matrix of term/token counts
copy : boolean, default True
Whether to copy X and operate on the copy or perform in-place operations.

Returns vectors : sparse matrix, [n_samples, n_features]

Examples using sklearn.feature_extraction.text.TfidfTransformer

• Sample pipeline for text feature extraction and evaluation
• Clustering text documents using k-means

sklearn.feature_extraction.text.TfidfVectorizer

class sklearn.feature_extraction.text.TfidfVectorizer(input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, analyzer='word', stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), max_df=1.0, min_df=1, max_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>, norm='l2', smooth_idf=True, sublinear_tf=False)

Convert a collection of raw documents to a matrix of TF-IDF features.
Equivalent to CountVectorizer followed by TfidfTransformer.
Read more in the User Guide.

Parameters input : string {'filename', 'file', 'content'}
If ‘filename’, the sequence passed as an argument to fit is expected to be a list of file-names that need reading to fetch the raw content to analyze.

If ‘file’, the sequence items must have a ‘read’ method (file-like object) that is called to fetch the bytes in memory.

Otherwise the input is expected to be the sequence strings or bytes items are expected to be analyzed directly.

**encoding** : string, ‘utf-8’ by default.
If bytes or files are given to analyze, this encoding is used to decode.

**decode_error** : {'strict', ‘ignore’, ‘replace’}
Instruction on what to do if a byte sequence is given to analyze that contains characters not of the given encoding. By default, it is ‘strict’, meaning that a UnicodeDecodeError will be raised. Other values are ‘ignore’ and ‘replace’.

**strip_accents** : {'ascii', ‘unicode’, None}
Remove accents during the preprocessing step. ‘ascii’ is a fast method that only works on characters that have an direct ASCII mapping. ‘unicode’ is a slightly slower method that works on any characters. None (default) does nothing.

**analyzer** : string, {'word’, ‘char’} or callable
Whether the feature should be made of word or character n-grams.
If a callable is passed it is used to extract the sequence of features out of the raw, unprocessed input.

**preprocessor** : callable or None (default)
Override the preprocessing (string transformation) stage while preserving the tokenizing and n-grams generation steps.

**tokenizer** : callable or None (default)
Override the string tokenization step while preserving the preprocessing and n-grams generation steps. Only applies if analyzer == ‘word’.

**ngram_range** : tuple (min_n, max_n)
The lower and upper boundary of the range of n-values for different n-grams to be extracted. All values of n such that min_n <= n <= max_n will be used.

**stop_words** : string {'english'}, list, or None (default)
If a string, it is passed to _check_stop_list and the appropriate stop list is returned. ‘english’ is currently the only supported string value.
If a list, that list is assumed to contain stop words, all of which will be removed from the resulting tokens. Only applies if analyzer == ‘word’.
If None, no stop words will be used. max_df can be set to a value in the range [0.7, 1.0) to automatically detect and filter stop words based on intra corpus document frequency of terms.

**lowercase** : boolean, default True
Convert all characters to lowercase before tokenizing.

**token_pattern** : string
Regular expression denoting what constitutes a “token”, only used if `analyzer == 'word'`. The default regexp selects tokens of 2 or more alphanumeric characters (punctuation is completely ignored and always treated as a token separator).

**max_df**: float in range [0.0, 1.0] or int, default=1.0

When building the vocabulary ignore terms that have a document frequency strictly higher than the given threshold (corpus-specific stop words). If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

**min_df**: float in range [0.0, 1.0] or int, default=1

When building the vocabulary ignore terms that have a document frequency strictly lower than the given threshold. This value is also called cut-off in the literature. If float, the parameter represents a proportion of documents, integer absolute counts. This parameter is ignored if vocabulary is not None.

**max_features**: int or None, default=None

If not None, build a vocabulary that only consider the top max_features ordered by term frequency across the corpus.

This parameter is ignored if vocabulary is not None.

**vocabulary**: Mapping or iterable, optional

Either a Mapping (e.g., a dict) where keys are terms and values are indices in the feature matrix, or an iterable over terms. If not given, a vocabulary is determined from the input documents.

**binary**: boolean, default=False

If True, all non-zero term counts are set to 1. This does not mean outputs will have only 0/1 values, only that the tf term in tf-idf is binary. (Set idf and normalization to False to get 0/1 outputs.)

**dtype**: type, optional

Type of the matrix returned by `fit_transform()` or `transform()`.

**norm**: ‘l1’, ‘l2’ or None, optional

Norm used to normalize term vectors. None for no normalization.

**use_idf**: boolean, default=True

Enable inverse-document-frequency reweighting.

**smooth_idf**: boolean, default=True

Smooth idf weights by adding one to document frequencies, as if an extra document was seen containing every term in the collection exactly once. Prevents zero divisions.

**sublinear_tf**: boolean, default=False

Apply sublinear tf scaling, i.e. replace tf with 1 + log(tf).
Attributes

| vo-         | (dict) A mapping of terms to feature indices. |
| cab-        |                                               |
| u-lary_     |                                               |
| idf_        | (array, shape = [n_features], or None) The learned idf vector (global term weights) when use_idf is set to True, None otherwise. |
| stop_words_ | Terms that were ignored because they either: - occurred in too many documents (max_df) - occurred in too few documents (min_df) - were cut off by feature selection (max_features). This is only available if no vocabulary was given. |

See also:

**CountVectorizer** Tokenize the documents and count the occurrences of token and return them as a sparse matrix

**TfidfTransformer** Apply Term Frequency Inverse Document Frequency normalization to a sparse matrix of occurrence counts.

Notes

The `stop_words_` attribute can get large and increase the model size when pickling. This attribute is provided only for introspection and can be safely removed using delattr or set to None before pickling.

Methods

| build_analyzer()     | Return a callable that handles preprocessing and tokenization |
| build_preprocessor() | Return a function to preprocess the text before tokenization |
| build_tokenizer()    | Return a function that splits a string into a sequence of tokens |
| decode(doc)          | Decode the input into a string of unicode symbols |
| fit(raw_documents[, y]) | Learn vocabulary and idf from training set. |
| fit_transform(raw_documents[, y]) | Learn vocabulary and idf, return term-document matrix. |
| get_feature_names()  | Array mapping from feature integer indices to feature name |
| get_params([deep])   | Get parameters for this estimator. |
| get_stop_words()     | Build or fetch the effective stop words list |
| inverse_transform(X) | Return terms per document with nonzero entries in X. |
| set_params(**params) | Set the parameters of this estimator. |
| transform(raw_documents[, copy]) | Transform documents to document-term matrix. |
| __init__ | (input='content', encoding='utf-8', decode_error='strict', strip_accents=None, lowercase=True, preprocessor=None, tokenizer=None, analyzer='word', stop_words=None, token_pattern='(?u)\b\w\w+\b', ngram_range=(1, 1), max_df=1.0, min_df=1, max_features=None, vocabulary=None, binary=False, dtype=<class 'numpy.int64'>, norm='l2', use_idf=True, smooth_idf=True, sublinear_tf=False) |
build_analyzer()
   Return a callable that handles preprocessing and tokenization

build_preprocessor()
   Return a function to preprocess the text before tokenization

build_tokenizer()
   Return a function that splits a string into a sequence of tokens

decode
   Decode the input into a string of unicode symbols
   The decoding strategy depends on the vectorizer parameters.

fit (raw_documents, y=None)
   Learn vocabulary and idf from training set.
   Parameters raw_documents : iterable
      an iterable which yields either str, unicode or file objects
   Returns self : TfidfVectorizer

fit_transform (raw_documents, y=None)
   Learn vocabulary and idf, return term-document matrix.
   This is equivalent to fit followed by transform, but more efficiently implemented.
   Parameters raw_documents : iterable
      an iterable which yields either str, unicode or file objects
   Returns X : sparse matrix, [n_samples, n_features]

generate_stop_words
   Build or fetch the effective stop words list

inverse_transform (X)
   Return terms per document with nonzero entries in X.
   Parameters X : {array, sparse matrix}, shape = [n_samples, n_features]
   Returns X_inv : list of arrays, len = n_samples
      List of arrays of terms.

set_params (**params)
   Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(raw_documents, copy=True)*

Transform documents to document-term matrix.

Uses the vocabulary and document frequencies (df) learned by fit (or fit_transform).

**Parameters**

`raw_documents`: iterable

An iterable which yields either str, unicode or file objects

`copy`: boolean, default True

Whether to copy X and operate on the copy or perform in-place operations.

**Returns**

`X`: sparse matrix, `[n_samples, n_features]`


**Examples using** `sklearn.feature_extraction.text.TfidfVectorizer`

- Feature Union with Heterogeneous Data Sources
- Topic extraction with Non-negative Matrix Factorization and Latent Dirichlet Allocation
- Biclustering documents with the Spectral Co-clustering algorithm
- Clustering text documents using k-means
- Classification of text documents using sparse features

### 30.14 sklearn.feature_selection: Feature Selection

The `sklearn.feature_selection` module implements feature selection algorithms. It currently includes univariate filter selection methods and the recursive feature elimination algorithm.

**User guide:** See the Feature selection section for further details.

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<td>Univariate feature selector with configurable strategy.</td>
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<td><code>feature_selection.SelectPercentile(...)</code></td>
<td>Select features according to a percentile of the highest scores.</td>
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<td><code>feature_selection.SelectKBest((score_func, k))</code></td>
<td>Select features according to the k highest scores.</td>
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<tr>
<td><code>feature_selection.SelectFpr((score_func, alpha))</code></td>
<td>Filter: Select the p-values below alpha based on a FPR test.</td>
</tr>
<tr>
<td><code>feature_selection.SelectFdr((score_func, alpha))</code></td>
<td>Filter: Select the p-values for an estimated false discovery rate.</td>
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<tr>
<td><code>feature_selection.SelectFromModel(estimator)</code></td>
<td>Meta-transformer for selecting features based on importance weights.</td>
</tr>
<tr>
<td><code>feature_selection.SelectFwe((score_func, alpha))</code></td>
<td>Filter: Select the p-values corresponding to Family-wise error rate.</td>
</tr>
<tr>
<td><code>feature_selection.RFE(estimator[, ...])</code></td>
<td>Feature ranking with recursive feature elimination.</td>
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| `feature_selection.RFECV` (estimator[, step, ...]) | Feature ranking with recursive feature elimination and cross-validated selection of the best number of features. |
| `feature_selection.VarianceThreshold` ([threshold]) | Feature selector that removes all low-variance features. |

### 30.14.1 `sklearn.feature_selection.GenericUnivariateSelect`

class `sklearn.feature_selection.GenericUnivariateSelect`

Univariate feature selector with configurable strategy.

Read more in the User Guide.

**Parameters**

- `score_func`: callable
  
  Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). For modes ‘percentile’ or ‘k_best’ it can return a single array scores.

- `mode`: {'percentile', 'k_best', 'fpr', 'fdr', ‘fwe’}
  
  Feature selection mode.

- `param`: float or int depending on the feature selection mode

  Parameter of the corresponding mode.

**Attributes**

| `scores_` | (array-like, shape=(n_features,)) Scores of features. |
| `pvalues_` | (array-like, shape=(n_features,)) p-values of feature scores, None if `score_func` returned scores only. |

See also:

- `f_classif` ANOVA F-value between label/feature for classification tasks.
- `mutual_info_classif` Mutual information for a discrete target.
- `chi2` Chi-squared stats of non-negative features for classification tasks.
- `f_regression` F-value between label/feature for regression tasks.
- `mutual_info_regression` Mutual information for a continuous target.
- `SelectPercentile` Select features based on percentile of the highest scores.
- `SelectKBest` Select features based on the k highest scores.
- `SelectFpr` Select features based on a false positive rate test.
- `SelectFdr` Select features based on an estimated false discovery rate.
- `SelectFwe` Select features based on family-wise error rate.
## Methods

<table>
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<tr>
<th>Method</th>
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<tr>
<td><code>fit(X, y)</code></td>
<td>Run score function on ((X, y)) and get the appropriate features.</td>
</tr>
<tr>
<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>get_support([indices])</code></td>
<td>Get a mask, or integer index, of the features selected.</td>
</tr>
<tr>
<td><code>inverse_transform(X)</code></td>
<td>Reverse the transformation operation.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Reduce (X) to the selected features.</td>
</tr>
</tbody>
</table>

### __init__

```
__init__ (score_func=<function f_classif>, mode='percentile', param=1e-05)
```

**fit** \((X, y)\)

Run score function on \((X, y)\) and get the appropriate features.

**Parameters**

- **X**: array-like, shape \(= [n\_samples, n\_features]\)
  
The training input samples.
- **y**: array-like, shape \(= [n\_samples]\)
  
The target values (class labels in classification, real numbers in regression).

**Returns**

- **self**: object
  
  Returns self.

**fit_transform** \((X, y=None, **fit_params)\)

Fit to data, then transform it.

Fits transformer to \(X\) and \(y\) with optional parameters fit_params and returns a transformed version of \(X\).

**Parameters**

- **X**: numpy array of shape \(= [n\_samples, n\_features]\)
  
  Training set.
- **y**: numpy array of shape \(= [n\_samples]\)
  
  Target values.

**Returns**

- **X\_new**: numpy array of shape \(= [n\_samples, n\_features\_new]\)
  
  Transformed array.

### get_params

```
get_params (deep=True)
```

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  
  Parameter names mapped to their values.

### get_support

```
get_support (indices=False)
```

Get a mask, or integer index, of the features selected.

**Parameters**

- **indices**: boolean (default False)
  
  If True, the return value will be an array of integers, rather than a boolean mask.
Returns support: array

An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [output features] whose values are indices into the input feature vector.

inverse_transform(X)
Reverse the transformation operation

Parameters X: array of shape [n_samples, n_selected_features]

The input samples.

Returns X_r: array of shape [n_samples, n_original_features]

X with columns of zeros inserted where features would have been removed by transform.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

transform(X)
Reduce X to the selected features.

Parameters X: array of shape [n_samples, n_features]

The input samples.

Returns X_r: array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

30.14.2 sklearn.feature_selection.SelectPercentile

class sklearn.feature_selection.SelectPercentile(score_func=function f_classif, percentile=10)

Select features according to a percentile of the highest scores.

Read more in the User Guide.

Parameters score_func: callable

Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues) or a single array with scores. Default is f_classif (see below “See also”). The default function only works with classification tasks.

percentile: int, optional, default=10

Percent of features to keep.
Attributes

| scores_   | (array-like, shape=(n_features,)) Scores of features. |
| pvalues_  | (array-like, shape=(n_features,)) p-values of feature scores, None if score_func returned only scores. |

See also:

- `f_classif` ANOVA F-value between label/feature for classification tasks.
- `mutual_info_classif` Mutual information for a discrete target.
- `chi2` Chi-squared stats of non-negative features for classification tasks.
- `f_regression` F-value between label/feature for regression tasks.
- `mutual_info_regression` Mutual information for a continuous target.
- `SelectKBest` Select features based on the k highest scores.
- `SelectFpr` Select features based on a false positive rate test.
- `SelectFdr` Select features based on an estimated false discovery rate.
- `SelectFwe` Select features based on family-wise error rate.
- `GenericUnivariateSelect` Univariate feature selector with configurable mode.

Notes

Ties between features with equal scores will be broken in an unspecified way.

Methods

- `__init__(score_func=<function f_classif>, percentile=10)`
- `fit(X, y)` Run score function on (X, y) and get the appropriate features.
- `fit_transform(X[, y])` Fit to data, then transform it.
- `get_params([deep])` Get parameters for this estimator.
- `get_support([indices])` Get a mask, or integer index, of the features selected
- `inverse_transform(X)` Reverse the transformation operation
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X)` Reduce X to the selected features.

```python
__init__(score_func=<function f_classif>, percentile=10)

fit(X, y)
Run score function on (X, y) and get the appropriate features.

Parameters

  X: array-like, shape=[n_samples, n_features]
    The training input samples.

  y: array-like, shape=[n_samples]
    The target values (class labels in classification, real numbers in regression).

Returns

  self: object
```
Returns self.

**fit_transform** *(X, y=\texttt{None}, **fit_params)*

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape \([n\_samples, n\_features]\)
  - Training set.
- **y**: numpy array of shape \([n\_samples]\)
  - Target values.

**Returns**

- **X\_new**: numpy array of shape \([n\_samples, n\_features\_new]\)
  - Transformed array.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**get_support**(indices=False)

Get a mask, or integer index, of the features selected

**Parameters**

- **indices**: boolean (default False)
  - If True, the return value will be an array of integers, rather than a boolean mask.

**Returns**

- **support**: array
  - An index that selects the retained features from a feature vector. If \(indices\) is False, this is a boolean array of shape \([\# input features]\), in which an element is True iff its corresponding feature is selected for retention. If \(indices\) is True, this is an integer array of shape \([\# output features]\) whose values are indices into the input feature vector.

**inverse_transform** *(X)*

Reverse the transformation operation

**Parameters**

- **X**: array of shape \([n\_samples, n\_selected\_features]\)
  - The input samples.

**Returns**

- **X\_r**: array of shape \([n\_samples, n\_original\_features]\)
  - \(X\) with columns of zeros inserted where features would have been removed by \(transform\).

**set_params**(**params)**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<component>\_\_<parameter>\) so that it’s possible to update each component of a nested object.

**Returns**

- **self**
transform($X$)

Reduce X to the selected features.

**Parameters**

$X$: array of shape [n_samples, n_features]

The input samples.

**Returns**

$X_r$: array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

Examples using `sklearn.feature_selection.SelectPercentile`

- Feature agglomeration vs. univariate selection
- Univariate Feature Selection
- SVM-ANOVA: SVM with univariate feature selection

30.14.3 `sklearn.feature_selection.SelectKBest`

class `sklearn.feature_selection.SelectKBest(score_func=<function f_classif>, k=10)`

Select features according to the k highest scores.

Read more in the User Guide.

**Parameters**

`score_func`: callable

Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues) or a single array with scores. Default is f_classif (see below “See also”). The default function only works with classification tasks.

`k`: int or “all”, optional, default=10

Number of top features to select. The “all” option bypasses selection, for use in a parameter search.

**Attributes**

<table>
<thead>
<tr>
<th>scores_</th>
<th>(array-like, shape=(n_features,)) Scores of features.</th>
</tr>
</thead>
<tbody>
<tr>
<td>pval-</td>
<td>(array-like, shape=(n_features,)) p-values of feature scores, None if score_func returned only</td>
</tr>
</tbody>
</table>

See also:

- `f_classif` ANOVA F-value between label/feature for classification tasks.
- `mutual_info_classif` Mutual information for a discrete target.
- `chi2` Chi-squared stats of non-negative features for classification tasks.
- `f_regression` F-value between label/feature for regression tasks.
- `mutual_info_regression` Mutual information for a continuous target.
- `SelectPercentile` Select features based on percentile of the highest scores.
- `SelectFpr` Select features based on a false positive rate test.
SelectFdr Select features based on an estimated false discovery rate.

SelectFwe Select features based on family-wise error rate.

GenericUnivariateSelect Univariate feature selector with configurable mode.

Notes

Ties between features with equal scores will be broken in an unspecified way.

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y)</td>
<td>Run score function on (X, y) and get the appropriate features.</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_support([indices])</td>
<td>Get a mask, or integer index, of the features selected</td>
</tr>
<tr>
<td>inverse_transform(X)</td>
<td>Reverse the transformation operation</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Reduce X to the selected features.</td>
</tr>
</tbody>
</table>

__init__ (score_func=<function f_classif>, k=10)

fit (X, y)

Run score function on (X, y) and get the appropriate features.

Parameters X : array-like, shape = [n_samples, n_features]

The training input samples.

y : array-like, shape = [n_samples]

The target values (class labels in classification, real numbers in regression).

Returns self : object

Returns self.

fit_transform (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.

get_params (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns **params** : mapping of string to any

Parameter names mapped to their values.

get_support(indices=False)

Get a mask, or integer index, of the features selected

Parameters **indices** : boolean (default False)

If True, the return value will be an array of integers, rather than a boolean mask.

Returns **support** : array

An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

inverse_transform(X)

Reverse the transformation operation

Parameters **X** : array of shape [n_samples, n_selected_features]

The input samples.

Returns **X_r** : array of shape [n_samples, n_original_features]

X with columns of zeros inserted where features would have been removed by transform.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns **self**

transform(X)

Reduce X to the selected features.

Parameters **X** : array of shape [n_samples, n_features]

The input samples.

Returns **X_r** : array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

Examples using sklearn.feature_selection.SelectKBest

- Concatenating multiple feature extraction methods
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Pipeline Anova SVM
- Classification of text documents using sparse features
30.14.4 sklearn.feature_selection.SelectFpr

**class** sklearn.feature_selection.SelectFpr(score_func=f_classif, alpha=0.05)

Filter: Select the pvalues below alpha based on a FPR test.

FPR test stands for False Positive Rate test. It controls the total amount of false detections.

Read more in the User Guide.

**Parameters**

- **score_func**: callable
  Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues).
  Default is f_classif (see below “See also”). The default function only works with classification tasks.

- **alpha**: float, optional
  The highest p-value for features to be kept.

**Attributes**

- **scores_**: (array-like, shape=(n_features,)) Scores of features.
- **pvalues_**: (array-like, shape=(n_features,)) p-values of feature scores.

**See also:**

- **f_classif** ANOVA F-value between label/feature for classification tasks.
- **chi2** Chi-squared stats of non-negative features for classification tasks.
- **mutual_info_classif**
- **f_regression** F-value between label/feature for regression tasks.
- **mutual_info_regression** Mutual information between features and the target.
- **SelectPercentile** Select features based on percentile of the highest scores.
- **SelectKBest** Select features based on the k highest scores.
- **SelectFdr** Select features based on an estimated false discovery rate.
- **SelectFwe** Select features based on family-wise error rate.
- **GenericUnivariateSelect** Univariate feature selector with configurable mode.

**Methods**

- **fit**(X, y) Run score function on (X, y) and get the appropriate features.
- **fit_transform**(X[, y]) Fit to data, then transform it.
- **get_params**(deep) Get parameters for this estimator.
- **get_support**(indices) Get a mask, or integer index, of the features selected
- **inverse_transform**(X) Reverse the transformation operation
- **set_params**(**params) Set the parameters of this estimator.
- **transform**(X) Reduce X to the selected features.
__init__(score_func=<function f_classif>, alpha=0.05)

fit(X, y)
   Run score function on (X, y) and get the appropriate features.
   
   Parameters X : array-like, shape = [n_samples, n_features]
      The training input samples.
   y : array-like, shape = [n_samples]
      The target values (class labels in classification, real numbers in regression).
   
   Returns self : object
      Returns self.

fit_transform(X, y=None, **fit_params)
   Fit to data, then transform it.
   
   Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.
   
   Parameters X : numpy array of shape [n_samples, n_features]
      Training set.
   y : numpy array of shape [n_samples]
      Target values.
   
   Returns X_new : numpy array of shape [n_samples, n_features_new]
      Transformed array.

get_params(deep=True)
   Get parameters for this estimator.
   
   Parameters deep : boolean, optional
      If True, will return the parameters for this estimator and contained subobjects that are estimators.
   
   Returns params : mapping of string to any
      Parameter names mapped to their values.

get_support(indices=False)
   Get a mask, or integer index, of the features selected
   
   Parameters indices : boolean (default False)
      If True, the return value will be an array of integers, rather than a boolean mask.
   
   Returns support : array
      An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

inverse_transform(X)
   Reverse the transformation operation
   
   Parameters X : array of shape [n_samples, n_selected_features]
      The input samples.
   
   Returns X_r : array of shape [n_samples, n_original_features]
X with columns of zeros inserted where features would have been removed by `transform`.

```python
set_params(**params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

```python
transform(X)
```

Reduce X to the selected features.

**Parameters**

- `X`: array of shape [n_samples, n_features]
  
The input samples.

**Returns**

- `X_r`: array of shape [n_samples, n_selected_features]
  
The input samples with only the selected features.

### 30.14.5 sklearn.feature_selection.SelectFdr

```python
class sklearn.feature_selection.SelectFdr(score_func=<function f_classif>, alpha=0.05)
```

Filter: Select the p-values for an estimated false discovery rate

This uses the Benjamini-Hochberg procedure. alpha is an upper bound on the expected false discovery rate.

Read more in the User Guide.

**Parameters**

- `score_func`: callable
  
  Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). Default is `f_classif` (see below “See also”). The default function only works with classification tasks.

- `alpha`: float, optional
  
  The highest uncorrected p-value for features to keep.

**Attributes**

- `scores_` (array-like, shape=(n_features,)) Scores of features.
- `pvalues_` (array-like, shape=(n_features,)) p-values of feature scores.

**See also:**

- `f_classif` ANOVA F-value between label/feature for classification tasks.
- `mutual_info_classif` Mutual information for a discrete target.
- `chi2` Chi-squared stats of non-negative features for classification tasks.
- `f_regression` F-value between label/feature for regression tasks.
- `mutual_info_regression` Mutual information for a continuous target.
- `SelectPercentile` Select features based on percentile of the highest scores.
SelectKBest  Select features based on the k highest scores.

SelectFpr  Select features based on a false positive rate test.

SelectFwe  Select features based on family-wise error rate.

GenericUnivariateSelect  Univariate feature selector with configurable mode.

References

https://en.wikipedia.org/wiki/False_discovery_rate

Methods

**fit**(X, y)  Run score function on (X, y) and get the appropriate features.

**fit_transform**(X[, y])  Fit to data, then transform it.

**get_params**(deep)  Get parameters for this estimator.

**get_support**(indices)  Get a mask, or integer index, of the features selected

**inverse_transform**(X)  Reverse the transformation operation

**set_params**(**params)  Set the parameters of this estimator.

**transform**(X)  Reduce X to the selected features.

**__init__**(score_func=<function f_classif>, alpha=0.05)

**fit**(X, y)  Run score function on (X, y) and get the appropriate features.

Parameters  

X : array-like, shape = [n_samples, n_features]

The training input samples.

y : array-like, shape = [n_samples]

The target values (class labels in classification, real numbers in regression).

Returns  

self : object

Returns self.

**fit_transform**(X, y=None, **fit_params)  Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters  

X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns  

X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.

**get_params**(deep=True)  Get parameters for this estimator.

Parameters  

depth : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

get_support(indices=False)
Get a mask, or integer index, of the features selected

Parameters indices : boolean (default False)

If True, the return value will be an array of integers, rather than a boolean mask.

Returns support : array

An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

inverse_transform(X)
Reverse the transformation operation

Parameters X : array of shape [n_samples, n_selected_features]

The input samples.

Returns X_r : array of shape [n_samples, n_original_features]

X with columns of zeros inserted where features would have been removed by transform.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform(X)
Reduce X to the selected features.

Parameters X : array of shape [n_samples, n_features]

The input samples.

Returns X_r : array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

30.14.6 sklearn.feature_selection.SelectFromModel

class sklearn.feature_selection.SelectFromModel(estimator, threshold=None, prefit=False, norm_order=1)

Meta-transformer for selecting features based on importance weights.

New in version 0.17.

Parameters estimator : object
The base estimator from which the transformer is built. This can be both a fitted (if `prefit` is set to True) or a non-fitted estimator. The estimator must have either a `feature_importances_` or `coef_` attribute after fitting.

**threshold**: string, float, optional default None

The threshold value to use for feature selection. Features whose importance is greater or equal are kept while the others are discarded. If “median” (resp. “mean”), then the threshold value is the median (resp. the mean) of the feature importances. A scaling factor (e.g., “1.25*mean”) may also be used. If None and if the estimator has a parameter penalty set to l1, either explicitly or implicitly (e.g, Lasso), the threshold used is 1e-5. Otherwise, “mean” is used by default.

**prefit**: bool, default False

Whether a prefit model is expected to be passed into the constructor directly or not. If True, `transform` must be called directly and `SelectFromModel` cannot be used with `cross_val_score`, `GridSearchCV` and similar utilities that clone the estimator. Otherwise train the model using `fit` and then `transform` to do feature selection.

**norm_order**: non-zero int, inf, -inf, default 1

Order of the norm used to filter the vectors of coefficients below `threshold` in the case where the `coef_` attribute of the estimator is of dimension 2.

### Attributes

<table>
<thead>
<tr>
<th>estimator_</th>
<th>(an estimator) The base estimator from which the transformer is built. This is stored only when a non-fitted estimator is passed to the <code>SelectFromModel</code>, i.e when <code>prefit</code> is False.</th>
</tr>
</thead>
<tbody>
<tr>
<td>threshold_</td>
<td>(float) The threshold value used for feature selection.</td>
</tr>
</tbody>
</table>

### Methods

```python
fit(X[, y]) Fit the SelectFromModel meta-transformer.
fit_transform(X[, y]) Fit to data, then transform it.
get_params([deep]) Get parameters for this estimator.
get_support([indices]) Get a mask, or integer index, of the features selected
inverse_transform(X) Reverse the transformation operation
partial_fit(X[, y]) Fit the SelectFromModel meta-transformer only once.
set_params(**params) Set the parameters of this estimator.
transform(X) Reduce X to the selected features.
```

__init__ (estimator, threshold=None, prefit=False, norm_order=1)

**fit** (X, y=None, **fit_params)

Fit the SelectFromModel meta-transformer.

**Parameters**

- **X**: array-like of shape (n_samples, n_features)
  - The training input samples.
- **y**: array-like, shape (n_samples,)
The target values (integers that correspond to classes in classification, real numbers in regression).

**fit_params** : Other estimator specific parameters

Returns self : object

Returns self.

**fit_transform** (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.

g**et_params** (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

**get_support** (indices=False)

Get a mask, or integer index, of the features selected.

Parameters indices : boolean (default False)

If True, the return value will be an array of integers, rather than a boolean mask.

Returns support : array

An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

**inverse_transform** (X)

Reverse the transformation operation.

Parameters X : array of shape [n_samples, n_selected_features]

The input samples.

Returns X_r : array of shape [n_samples, n_original_features]

X with columns of zeros inserted where features would have been removed by transform.

**partial_fit** (X, y=None, **fit_params)

Fit the SelectFromModel meta-transformer only once.

Parameters X : array-like of shape (n_samples, n_features)
The training input samples.

\( y \): array-like, shape (n_samples,)

The target values (integers that correspond to classes in classification, real numbers in regression).

**fit_params**: Other estimator specific parameters

Returns `self` : object

Returns `self`.

`set_params(**params)`

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns `self`

`transform(X)`

Reduce X to the selected features.

Parameters

\( X \): array of shape [n_samples, n_features]

The input samples.

Returns \( X_r \): array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

Examples using `sklearn.feature_selection.SelectFromModel`

- Feature selection using SelectFromModel and LassoCV
- Classification of text documents using sparse features

### 30.14.7 `sklearn.feature_selection.SelectFwe`

**class sklearn.feature_selection.SelectFwe(score_func=<function f_classif>, alpha=0.05)**

Filter: Select the p-values corresponding to Family-wise error rate

Read more in the User Guide.

Parameters

`score_func` : callable

Function taking two arrays X and y, and returning a pair of arrays (scores, pvalues). Default is `f_classif` (see below “See also”). The default function only works with classification tasks.

`alpha` : float, optional

The highest uncorrected p-value for features to keep.

Attributes

<table>
<thead>
<tr>
<th><code>scores_</code></th>
<th>(array-like, shape=(n_features,)) Scores of features.</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>pvalues_</code></td>
<td>(array-like, shape=(n_features,)) p-values of feature scores.</td>
</tr>
</tbody>
</table>
See also:

- **f_classif** ANOVA F-value between label/feature for classification tasks.
- **chi2** Chi-squared stats of non-negative features for classification tasks.
- **f_regression** F-value between label/feature for regression tasks.
- **SelectPercentile** Select features based on percentile of the highest scores.
- **SelectKBest** Select features based on the k highest scores.
- **SelectFpr** Select features based on a false positive rate test.
- **SelectFdr** Select features based on an estimated false discovery rate.
- **GenericUnivariateSelect** Univariate feature selector with configurable mode.

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y)</td>
<td>Run score function on (X, y) and get the appropriate features.</td>
</tr>
<tr>
<td>fit_transform(X, y)</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params()</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>get_support()</td>
<td>Get a mask, or integer index, of the features selected</td>
</tr>
<tr>
<td>inverse_transform(X)</td>
<td>Reverse the transformation operation</td>
</tr>
<tr>
<td>set_params()</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Reduce X to the selected features.</td>
</tr>
</tbody>
</table>

__init__(score_func=<function f_classif>, alpha=0.05)

**fit** (X, y)

Run score function on (X, y) and get the appropriate features.

**Parameters**

- **X** : array-like, shape = [n_samples, n_features]
  The training input samples.
- **y** : array-like, shape = [n_samples]
  The target values (class labels in classification, real numbers in regression).

**Returns**

- **self** : object
  Returns self.

**fit_transform** (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X** : numpy array of shape [n_samples, n_features]
  Training set.
- **y** : numpy array of shape [n_samples]
  Target values.

**Returns**

- **X_new** : numpy array of shape [n_samples, n_features_new]
  Transformed array.
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

get_support (indices=False)
Get a mask, or integer index, of the features selected

Parameters indices : boolean (default False)
If True, the return value will be an array of integers, rather than a boolean mask.

Returns support : array
An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

inverse_transform (X)
Reverse the transformation operation

Parameters X : array of shape [n_samples, n_selected_features]
The input samples.

Returns X_r : array of shape [n_samples, n_original_features]
X with columns of zeros inserted where features would have been removed by transform.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Reduce X to the selected features.

Parameters X : array of shape [n_samples, n_features]
The input samples.

Returns X_r : array of shape [n_samples, n_selected_features]
The input samples with only the selected features.

30.14.8 sklearn.feature_selection.RFE

class sklearn.feature_selection.RFE (estimator, n_features_to_select=None, step=1, verbose=0)
Feature ranking with recursive feature elimination.

Given an external estimator that assigns weights to features (e.g., the coefficients of a linear model), the goal of recursive feature elimination (RFE) is to select features by recursively considering smaller and smaller sets of
features. First, the estimator is trained on the initial set of features and the importance of each feature is obtained either through a \texttt{coef\_} attribute or through a \texttt{feature\_importances\_} attribute. Then, the least important features are pruned from current set of features. That procedure is recursively repeated on the pruned set until the desired number of features to select is eventually reached.

Read more in the \textit{User Guide}.

**Parameters**

- \texttt{estimator} : object
  
  A supervised learning estimator with a \texttt{fit} method that provides information about feature importance either through a \texttt{coef\_} attribute or through a \texttt{feature\_importances\_} attribute.

- \texttt{n\_features\_to\_select} : int or None (default=None)
  
  The number of features to select. If \texttt{None}, half of the features are selected.

- \texttt{step} : int or float, optional (default=1)
  
  If greater than or equal to 1, then \texttt{step} corresponds to the (integer) number of features to remove at each iteration. If within \((0.0, 1.0)\), then \texttt{step} corresponds to the percentage (rounded down) of features to remove at each iteration.

- \texttt{verbose} : int, default=0
  
  Controls verbosity of output.

**Attributes**

- \texttt{n\_features\_} (int) The number of selected features.

- \texttt{support\_} (array of shape [\texttt{n\_features\_}]) The mask of selected features.

- \texttt{ranking\_} (array of shape [\texttt{n\_features\_}]) The feature ranking, such that \texttt{ranking\_[i]} corresponds to the ranking position of the \texttt{i}-th feature. Selected (i.e., estimated best) features are assigned rank 1.

- \texttt{estimator\_} (object) The external estimator fit on the reduced dataset.

See also:

- \textit{RFECV}  Recursive feature elimination with built-in cross-validated selection of the best number of features

**References**

[R9393]

**Examples**

The following example shows how to retrieve the 5 right informative features in the Friedman #1 dataset.

```python
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.feature_selection import RFE
>>> from sklearn.svm import SVR
>>> X, y = make_friedman1(n_samples=50, n_features=10, random_state=0)
>>> estimator = SVR(kernel="linear")
```
>>> selector = RFE(estimator, 5, step=1)
>>> selector = selector.fit(X, y)
>>> selector.support_
array([ True, True, True, True, True, False, False, False, False, False], dtype=bool)
>>> selector.ranking_
array([1, 1, 1, 1, 1, 6, 4, 3, 2, 5])

Methods

decision_function(X)  
fit(X, y)  
fit_transform(X[, y])  
get_params([deep])  
get_support([indices])  
inverse_transform(X)  
predict(X)  
predict_log_proba(X)  
predict_proba(X)  
score(X, y)  
set_params(**params)  
transform(X)

__init__(estimator, n_features_to_select=None, step=1, verbose=0)

fit(X, y)

Fit the RFE model and then the underlying estimator on the selected features.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]

The training input samples.

y : array-like, shape = [n_samples]

The target values.

fit_transform(X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.
get_params (deep=True)
Get parameters for this estimator.

Parameters  
- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns  
- **params**: mapping of string to any
  
  Parameter names mapped to their values.

get_support (indices=False)
Get a mask, or integer index, of the features selected

Parameters  
- **indices**: boolean (default False)
  
  If True, the return value will be an array of integers, rather than a boolean mask.

Returns  
- **support**: array
  
  An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

inverse_transform (X)
Reverse the transformation operation

Parameters  
- **X**: array of shape [n_samples, n_selected_features]
  
  The input samples.

Returns  
- **X_r**: array of shape [n_samples, n_original_features]
  
  X with columns of zeros inserted where features would have been removed by transform.

predict (X)
Reduce X to the selected features and then predict using the underlying estimator.

Parameters  
- **X**: array of shape [n_samples, n_features]
  
  The input samples.

Returns  
- **y**: array of shape [n_samples]
  
  The predicted target values.

score (X, y)
Reduce X to the selected features and then return the score of the underlying estimator.

Parameters  
- **X**: array of shape [n_samples, n_features]
  
  The input samples.

- **y**: array of shape [n_samples]
  
  The target values.

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Reduce X to the selected features.

**Parameters** `X` : array of shape [n_samples, n_features]

The input samples.

**Returns** `X_r` : array of shape [n_samples, n_selected_features]

The input samples with only the selected features.

**Examples using sklearn.feature_selection.RFE**

- Recursive feature elimination

**30.14.9 sklearn.feature_selection.RFECV**

class `sklearn.feature_selection.RFECV` *(estimator, step=1, cv=None, scoring=None, verbose=0, n_jobs=1)*

Feature ranking with recursive feature elimination and cross-validated selection of the best number of features.

Read more in the *User Guide*.

**Parameters** `estimator` : object

A supervised learning estimator with a `fit` method that provides information about feature importance either through a `coef_` attribute or through a `feature_importances_` attribute.

`step` : int or float, optional (default=1)

If greater than or equal to 1, then `step` corresponds to the (integer) number of features to remove at each iteration. If within (0.0, 1.0), then `step` corresponds to the percentage (rounded down) of features to remove at each iteration.

`cv` : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for `cv` are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds,
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if `y` is binary or multiclass, `sklearn.model_selection.StratifiedKFold` is used. If the estimator is a classifier or if `y` is neither binary nor multiclass, `sklearn.model_selection.KFold` is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

`scoring` : string, callable or None, optional, default: None
A string (see model evaluation documentation) or a scorer callable object / function with signature `scorer(estimator, X, y)`.

**verbose** : int, default=0

Controls verbosity of output.

**n_jobs** : int, default 1

Number of cores to run in parallel while fitting across folds. Defaults to 1 core. If `n_jobs=-1`, then number of jobs is set to number of cores.

### Attributes

<table>
<thead>
<tr>
<th><strong>n_features</strong>&lt;br&gt;int</th>
<th>The number of selected features with cross-validation.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>support_</strong>&lt;br&gt;(array of shape [n_features])</td>
<td>The mask of selected features.</td>
</tr>
<tr>
<td><strong>ranking_</strong>&lt;br&gt;(array of shape [n_features])</td>
<td>The feature ranking, such that <code>ranking_[i]</code> corresponds to the ranking position of the i-th feature. Selected (i.e., estimated best) features are assigned rank 1.</td>
</tr>
<tr>
<td><strong>grid_scores_</strong>&lt;br&gt;(array of shape [n_subsets_of_features])</td>
<td>The cross-validation scores such that <code>grid_scores_[i]</code> corresponds to the CV score of the i-th subset of features.</td>
</tr>
<tr>
<td><strong>estimator_</strong>&lt;br&gt;(object)</td>
<td>The external estimator fit on the reduced dataset.</td>
</tr>
</tbody>
</table>

**See also:**

*RFE* Recursive feature elimination

**Notes**

The size of `grid_scores_` is equal to `ceil((n_features - 1) / step) + 1`, where step is the number of features removed at each iteration.

**References**

[R9595]

**Examples**

The following example shows how to retrieve the a-priori not known 5 informative features in the Friedman #1 dataset.

```python
>>> from sklearn.datasets import make_friedman1
>>> from sklearn.feature_selection import RFECV
>>> from sklearn.svm import SVR

>>> X, y = make_friedman1(n_samples=50, n_features=10, random_state=0)
>>> estimator = SVR(kernel="linear")
>>> selector = RFECV(estimator, step=1, cv=5)
>>> selector = selector.fit(X, y)
>>> selector.support_
array([ True,  True,  True,  True,  True,
        False, False, False, False, False])
```
Methods

- decision_function(X)
  Fit the RFE model and automatically tune the number of selected features.

- fit(X, y)
  Fit the RFE model and automatically tune the number of selected features.

- fit_transform(X[, y])
  Fit to data, then transform it.

- get_params([deep])
  Get parameters for this estimator.

- get_support([indices])
  Get a mask, or integer index, of the features selected.

- inverse_transform(X)
  Reverse the transformation operation.

- predict(X)
  Reduce X to the selected features and then predict using the underlying estimator.

- predict_log_proba(X)
  
- predict_proba(X)
  
- score(X, y)
  Reduce X to the selected features and then return the score of the underlying estimator.

- set_params(**params)
  Set the parameters of this estimator.

- transform(X)
  Reduce X to the selected features.

__init__ (estimator, step=1, cv=None, scoring=None, verbose=0, n_jobs=1)

fit (X, y)

Fit the RFE model and automatically tune the number of selected features.

**Parameters**

- **X** : {array-like, sparse matrix}, shape = [n_samples, n_features]
  Training vector, where n_samples is the number of samples and n_features is the total number of features.
- **y** : array-like, shape = [n_samples]
  Target values (integers for classification, real numbers for regression).

fit_transform (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X** : numpy array of shape [n_samples, n_features]
  Training set.
- **y** : numpy array of shape [n_samples]
  Target values.

**Returns**

- **X_new** : numpy array of shape [n_samples, n_features_new]
  Transformed array.

get_params (deep=True)

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**get_support**(indices=False)

Get a mask, or integer index, of the features selected

**Parameters** indices : boolean (default False)

If True, the return value will be an array of integers, rather than a boolean mask.

**Returns** support : array

An index that selects the retained features from a feature vector. If indices is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If indices is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

**inverse_transform**(X)

Reverse the transformation operation

**Parameters** X : array of shape [n_samples, n_selected_features]

The input samples.

**Returns** X_r : array of shape [n_samples, n_original_features]

X with columns of zeros inserted where features would have been removed by transform.

**predict**(X)

Reduce X to the selected features and then predict using the underlying estimator.

**Parameters** X : array of shape [n_samples, n_features]

The input samples.

**Returns** y : array of shape [n_samples]

The predicted target values.

**score**(X, y)

Reduce X to the selected features and then return the score of the underlying estimator.

**Parameters** X : array of shape [n_samples, n_features]

The input samples.

y : array of shape [n_samples]

The target values.

**set_params**(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns** self
transform(X)
Reduce X to the selected features.

Parameters  

X : array of shape [n_samples, n_features]
The input samples.

Returns  

X_r : array of shape [n_samples, n_selected_features]
The input samples with only the selected features.

Examples using sklearn.feature_selection.RFECV

• Recursive feature elimination with cross-validation


class sklearn.feature_selection.VarianceThreshold(threshold=0.0)
Feature selector that removes all low-variance features.
This feature selection algorithm looks only at the features (X), not the desired outputs (y), and can thus be used for unsupervised learning.

Read more in the User Guide.

Parameters  

threshold : float, optional
Features with a training-set variance lower than this threshold will be removed. The default is to keep all features with non-zero variance, i.e. remove the features that have the same value in all samples.

Attributes

variances_  
(array, shape (n_features,)) Variances of individual features.

Examples

The following dataset has integer features, two of which are the same in every sample. These are removed with the default setting for threshold:

```python
>>> X = [[0, 2, 0, 3], [0, 1, 4, 3], [0, 1, 1, 3]]
>>> selector = VarianceThreshold()
>>> selector.fit_transform(X)
array([[2, 0],
       [1, 4],
       [1, 1]])
```

Methods

fit(X[, y]) Learn empirical variances from X.

fit_transform(X[, y]) Fit to data, then transform it.
Table 30.122 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>get_params</code>([<code>deep</code>])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>get_support</code>([<code>indices</code>])</td>
<td>Get a mask, or integer index, of the features selected</td>
</tr>
<tr>
<td><code>inverse_transform(X)</code></td>
<td>Reverse the transformation operation</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Reduce X to the selected features.</td>
</tr>
</tbody>
</table>

__init__(threshold=0.0)

`fit(X, y=None)`
Learn empirical variances from X.

**Parameters**
- `X`: {array-like, sparse matrix}, shape (n_samples, n_features)
  Sample vectors from which to compute variances.
- `y`: any
  Ignored. This parameter exists only for compatibility with sklearn.pipeline.Pipeline.

**Returns**
- `self`

`fit_transform(X, y=None, **fit_params)`
Fit to data, then transform it.
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**
- `X`: numpy array of shape [n_samples, n_features]
  Training set.
- `y`: numpy array of shape [n_samples]
  Target values.

**Returns**
- `X_new`: numpy array of shape [n_samples, n_features_new]
  Transformed array.

`get_params(deep=True)`
Get parameters for this estimator.

**Parameters**
- `deep`: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- `params`: mapping of string to any
  Parameter names mapped to their values.

`get_support(indices=False)`
Get a mask, or integer index, of the features selected

**Parameters**
- `indices`: boolean (default False)
  If True, the return value will be an array of integers, rather than a boolean mask.

**Returns**
- `support`: array
  An index that selects the retained features from a feature vector. If `indices` is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If `indices` is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.
**inverse_transform** *(X)*
Reverse the transformation operation

**Parameters**

- **X**: array of shape [n_samples, n_selected_features]
  
The input samples.

**Returns**

- **X_r**: array of shape [n_samples, n_original_features]
  
  X with columns of zeros inserted where features would have been removed by transformation.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**transform** *(X)*
Reduce X to the selected features.

**Parameters**

- **X**: array of shape [n_samples, n_features]
  
The input samples.

**Returns**

- **X_r**: array of shape [n_samples, n_selected_features]
  
The input samples with only the selected features.

---

**feature_selection.chi2(X, y)**
Compute chi-squared stats between each non-negative feature and class.

**feature_selection.f_classif(X, y)**
Compute the ANOVA F-value for the provided sample.

**feature_selection.f_regression(X, y, center)**
Univariate linear regression tests.

**feature_selection.mutual_info_classif(X, y)**
Estimate mutual information for a discrete target variable.

**feature_selection.mutual_info_regression(X, y)**
Estimate mutual information for a continuous target variable.

---

### 30.14.11 sklearn.feature_selection.chi2

**sklearn.feature_selection.chi2**(X, y)
Compute chi-squared stats between each non-negative feature and class.

This score can be used to select the n_features features with the highest values for the test chi-squared statistic from X, which must contain only non-negative features such as booleans or frequencies (e.g., term counts in document classification), relative to the classes.

Recall that the chi-square test measures dependence between stochastic variables, so using this function “weeds out” the features that are the most likely to be independent of class and therefore irrelevant for classification.


**Parameters**

- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features_in)
  
  Sample vectors.

- **y**: array-like, shape = (n_samples,)
Target vector (class labels).

**Returns**  
*chi2* : array, shape = (n_features,)  
chi2 statistics of each feature.  
*pval* : array, shape = (n_features,)  
p-values of each feature.

**See also:**

- **f_classif**  
  ANOVA F-value between label/feature for classification tasks.  
- **f_regression**  
  F-value between label/feature for regression tasks.

**Notes**

Complexity of this algorithm is $O(n_{classes} \times n_{features})$.

**Examples using sklearn.feature_selection.chi2**
- *Selecting dimensionality reduction with Pipeline and GridSearchCV*  
- *Classification of text documents using sparse features*

### 30.14.12 sklearn.feature_selection.f_classif

sklearn.feature_selection.f_classif(X, y)  
Compute the ANOVA F-value for the provided sample.

Parameters  
- **X** : {array-like, sparse matrix} shape = [n_samples, n_features]  
The set of regressors that will be tested sequentially.  
- **y** : array of shape(n_samples)  
The data matrix.

**Returns**  
- **F** : array, shape = [n_features,]  
The set of F values.  
- **pval** : array, shape = [n_features,]  
The set of p-values.

**See also:**  
- **chi2**  
  Chi-squared stats of non-negative features for classification tasks.  
- **f_regression**  
  F-value between label/feature for regression tasks.

**Examples using sklearn.feature_selection.f_classif**
- *Univariate Feature Selection*  
- *SVM-Anova: SVM with univariate feature selection*
sklearn.feature_selection.f_regression

sklearn.feature_selection.f_regression(X, y, center=True)

Univariate linear regression tests.

Linear model for testing the individual effect of each of many regressors. This is a scoring function to be used in a feature selection procedure, not a free standing feature selection procedure.

This is done in 2 steps:

1. The correlation between each regressor and the target is computed, that is, \(((X[:, i] - \text{mean}(X[:, i])) * (y - \text{mean}_y) / (\text{std}(X[:, i]) * \text{std}(y)).\)

2. It is converted to an F score then to a p-value.

For more on usage see the User Guide.

**Parameters**

- **X**: {array-like, sparse matrix} shape = (n_samples, n_features)
  The set of regressors that will be tested sequentially.

- **y**: array of shape(n_samples).
  The data matrix.

- **center**: True, bool,
  If true, X and y will be centered.

**Returns**

- **F**: array, shape=(n_features,)
  F values of features.

- **pval**: array, shape=(n_features,)
  p-values of F-scores.

**See also:**

- mutual_info_regression  Mutual information for a continuous target.
- f_classif  ANOVA F-value between label/feature for classification tasks.
- chi2  Chi-squared stats of non-negative features for classification tasks.
- SelectKBest  Select features based on the k highest scores.
- SelectFpr  Select features based on a false positive rate test.
- SelectFdr  Select features based on an estimated false discovery rate.
- SelectFwe  Select features based on family-wise error rate.
- SelectPercentile  Select features based on percentile of the highest scores.

**Examples using sklearn.feature_selection.f_regression**

- Feature agglomeration vs. univariate selection
- Comparison of F-test and mutual information
- Pipeline Anova SVM
Estimate mutual information for a discrete target variable.

Mutual information (MI) \([R411414]\) between two random variables is a non-negative value, which measures the dependency between the variables. It is equal to zero if and only if two random variables are independent, and higher values mean higher dependency.

The function relies on nonparametric methods based on entropy estimation from k-nearest neighbors distances as described in \([R412414]\) and \([R413414]\). Both methods are based on the idea originally proposed in \([R414414]\).

It can be used for univariate features selection, read more in the User Guide.

**Parameters**

- **X**: array_like or sparse matrix, shape (n_samples, n_features)
  
  Feature matrix.

- **y**: array_like, shape (n_samples,)
  
  Target vector.

- **discrete_features**: {'auto', bool, array_like}, default ‘auto’
  
  If bool, then determines whether to consider all features discrete or continuous. If array, then it should be either a boolean mask with shape (n_features,) or array with indices of discrete features. If ‘auto’, it is assigned to False for dense X and to True for sparse X.

- **n_neighbors**: int, default 3
  
  Number of neighbors to use for MI estimation for continuous variables, see \([R412414]\) and \([R413414]\). Higher values reduce variance of the estimation, but could introduce a bias.

- **copy**: bool, default True
  
  Whether to make a copy of the given data. If set to False, the initial data will be overwritten.

- **random_state**: int, RandomState instance or None, optional, default None
  
  The seed of the pseudo random number generator for adding small noise to continuous variables in order to remove repeated values. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **mi**: ndarray, shape (n_features,)
  
  Estimated mutual information between each feature and the target.

**Notes**

1. The term “discrete features” is used instead of naming them “categorical”, because it describes the essence more accurately. For example, pixel intensities of an image are discrete features (but hardly categorical) and you will get better results if mark them as such. Also note, that treating a continuous variable as discrete and vice versa will usually give incorrect results, so be attentive about that.

2. True mutual information can’t be negative. If its estimate turns out to be negative, it is replaced by zero.
Estimate mutual information for a continuous target variable.

Mutual information (MI) [R97100] between two random variables is a non-negative value, which measures the dependency between the variables. It is equal to zero if and only if two random variables are independent, and higher values mean higher dependency.

The function relies on nonparametric methods based on entropy estimation from k-nearest neighbors distances as described in [R98100] and [R99100]. Both methods are based on the idea originally proposed in [R100100].

It can be used for univariate features selection, read more in the User Guide.

**Parameters**

- **X**: array_like or sparse matrix, shape (n_samples, n_features)
  Feature matrix.

- **y**: array_like, shape (n_samples,)
  Target vector.

- **discrete_features**: {'auto', bool, array_like}, default 'auto'
  If bool, then determines whether to consider all features discrete or continuous. If array, then it should be either a boolean mask with shape (n_features,) or array with indices of discrete features. If ‘auto’, it is assigned to False for dense X and to True for sparse X.

- **n_neighbors**: int, default 3
  Number of neighbors to use for MI estimation for continuous variables, see [R98100] and [R99100]. Higher values reduce variance of the estimation, but could introduce a bias.

- **copy**: bool, default True
  Whether to make a copy of the given data. If set to False, the initial data will be overwritten.

- **random_state**: int, RandomState instance or None, optional, default None
  The seed of the pseudo random number generator for adding small noise to continuous variables in order to remove repeated values. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Returns**

- **mi**: ndarray, shape (n_features,)
  Estimated mutual information between each feature and the target.

**Notes**

1. The term “discrete features” is used instead of naming them “categorical”, because it describes the essence more accurately. For example, pixel intensities of an image are discrete features (but hardly categorical)
and you will get better results if mark them as such. Also note, that treating a continuous variable as
discrete and vice versa will usually give incorrect results, so be attentive about that.

2. True mutual information can’t be negative. If its estimate turns out to be negative, it is replaced by zero.

References

[R97100], [R98100], [R99100], [R100100]

Examples using `sklearn.feature_selection.mutual_info_regression`

- Comparison of F-test and mutual information

30.15 `sklearn.gaussian_process`: Gaussian Processes

The `sklearn.gaussian_process` module implements Gaussian Process based regression and classification.

User guide: See the Gaussian Processes section for further details.

Gaussian process classification (GPC) based on Laplace approximation.

Gaussian process regression (GPR).

30.15.1 `sklearn.gaussian_process.GaussianProcessClassifier`

class `sklearn.gaussian_process.GaussianProcessClassifier`:

Gaussian process classification (GPC) based on Laplace approximation.

The implementation is based on Algorithm 3.1, 3.2, and 5.1 of Gaussian Processes for Machine Learning
(GPML) by Rasmussen and Williams.

Internally, the Laplace approximation is used for approximating the non-Gaussian posterior by a Gaussian.

Currently, the implementation is restricted to using the logistic link function. For multi-class classification,
several binary one-versus rest classifiers are fitted. Note that this class thus does not implement a true multi-
class Laplace approximation.

Parameters:

- `kernel`: kernel object
  - The kernel specifying the covariance function of the GP. If None is passed, the kernel
    “1.0 * RBF(1.0)" is used as default. Note that the kernel’s hyperparameters are opti-
    mized during fitting.

- `optimizer`: string or callable, optional (default: “fmin_l_bfgs_b")
Can either be one of the internally supported optimizers for optimizing the kernel’s parameters, specified by a string, or an externally defined optimizer passed as a callable. If a callable is passed, it must have the signature:

```python
def optimizer(obj_func, initial_theta, bounds):
    # * 'obj_func' is the objective function to be maximized,
    # which
    # takes the hyperparameters theta as parameter and an
    # optional flag eval_gradient, which determines if the
    # gradient is returned additionally to the function value
    # * 'initial_theta': the initial value for theta, which can
    # be
    # used by local optimizers
    # * 'bounds': the bounds on the values of theta
    ...
    # Returned are the best found hyperparameters theta and
    # the corresponding value of the target function.
    return theta_opt, func_min
```

Per default, the ‘fmin_l_bfgs_b’ algorithm from scipy.optimize is used. If None is passed, the kernel’s parameters are kept fixed. Available internal optimizers are:

- 'fmin_l_bfgs_b'

**n_restarts_optimizer** : int, optional (default: 0)

The number of restarts of the optimizer for finding the kernel’s parameters which maximize the log-marginal likelihood. The first run of the optimizer is performed from the kernel’s initial parameters, the remaining ones (if any) from thetas sampled log-uniform randomly from the space of allowed theta-values. If greater than 0, all bounds must be finite. Note that n_restarts_optimizer=0 implies that one run is performed.

**max_iter_predict** : int, optional (default: 100)

The maximum number of iterations in Newton’s method for approximating the posterior during predict. Smaller values will reduce computation time at the cost of worse results.

**warm_start** : bool, optional (default: False)

If warm-starts are enabled, the solution of the last Newton iteration on the Laplace approximation of the posterior mode is used as initialization for the next call of _posterior_mode(). This can speed up convergence when _posterior_mode is called several times on similar problems as in hyperparameter optimization.

**copy_X_train** : bool, optional (default: True)

If True, a persistent copy of the training data is stored in the object. Otherwise, just a reference to the training data is stored, which might cause predictions to change if the data is modified externally.

**random_state** : int, RandomState instance or None, optional (default: None)

The generator used to initialize the centers. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**multi_class** : string, default

Specifies how multi-class classification problems are handled. Supported are “one_vs_rest” and “one_vs_one”. In “one_vs_rest”, one binary Gaussian process class-
**n_jobs**: int, optional, default: 1

The number of jobs to use for the computation. If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>kernel_</strong></td>
<td>(kernel object) The kernel used for prediction. In case of binary classification, the structure of the kernel is the same as the one passed as parameter but with optimized hyperparameters. In case of multi-class classification, a CompoundKernel is returned which consists of the different kernels used in the one-versus-rest classifiers.</td>
</tr>
<tr>
<td><strong>log_marginal_likelihood_</strong></td>
<td>The log-marginal-likelihood of self.kernel_.theta</td>
</tr>
<tr>
<td><strong>classes_</strong></td>
<td>(array-like, shape = (n_classes,)) Unique class labels.</td>
</tr>
<tr>
<td><strong>n_classes_</strong></td>
<td>(int) The number of classes in the training data</td>
</tr>
</tbody>
</table>

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>fit(X, y)</strong></td>
<td>Fit Gaussian process classification model</td>
</tr>
<tr>
<td><strong>get_params([deep])</strong></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><strong>log_marginal_likelihood([theta, eval_gradient])</strong></td>
<td>Returns log-marginal likelihood of theta for training data.</td>
</tr>
<tr>
<td><strong>predict(X)</strong></td>
<td>Perform classification on an array of test vectors X.</td>
</tr>
<tr>
<td><strong>predict_proba(X)</strong></td>
<td>Return probability estimates for the test vector X.</td>
</tr>
<tr>
<td><strong>score(X, y[, sample_weight])</strong></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>**set_params(<strong>params)</strong></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**__init__** *(kernel=None, optimizer='fmin_l_bfgs_b', n_restarts_optimizer=0, max_iter_predict=100, warm_start=False, copy_X_train=True, random_state=None, multi_class='one_vs_rest', n_jobs=1)*

**fit (X, y)**

Fit Gaussian process classification model

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  
  Training data

- **y**: array-like, shape = (n_samples,)
  
  Target values, must be binary

**Returns**

**self**: returns an instance of self.
get_params (deep=True)
Get parameters for this estimator.

Parameters:
- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are
  estimators.

Returns:
- params : mapping of string to any
  Parameter names mapped to their values.

log_marginal_likelihood (theta=None, eval_gradient=False)
Returns log-marginal likelihood of theta for training data.
In the case of multi-class classification, the mean log-marginal likelihood of the one-versus-rest classifiers
are returned.

Parameters:
- theta : array-like, shape = (n_kernel_params,) or none
  Kernel hyperparameters for which the log-marginal likelihood is evaluated. In the case of
  multi-class classification, theta may be the hyperparameters of the compound kernel
  or of an individual kernel. In the latter case, all individual kernel get assigned the same
  theta values. If None, the precomputed log_marginal_likelihood of self.kernel_.
  theta is returned.
- eval_gradient : bool, default: False
  If True, the gradient of the log-marginal likelihood with respect to the kernel hyperpa-
  rameters at position theta is returned additionally. Note that gradient computation is not
  supported for non-binary classification. If True, theta must not be None.

Returns:
- log_likelihood : float
  Log-marginal likelihood of theta for training data.
- log_likelihood_gradient : array, shape = (n_kernel_params,), optional
  Gradient of the log-marginal likelihood with respect to the kernel hyperparameters at
  position theta. Only returned when eval_gradient is True.

predict (X)
Perform classification on an array of test vectors X.

Parameters:
- X : array-like, shape = (n_samples, n_features)

Returns:
- C : array, shape = (n_samples,)
  Predicted target values for X, values are from classes_.

predict_proba (X)
Return probability estimates for the test vector X.

Parameters:
- X : array-like, shape = (n_samples, n_features)

Returns:
- C : array-like, shape = (n_samples, n_classes)
  Returns the probability of the samples for each class in the model. The columns corre-
  spond to the classes in sorted order, as they appear in the attribute classes_.

score (X, y, sample_weight=None)
Returns the mean accuracy on the given test data and labels.
In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each
sample that each label set be correctly predicted.
Parameters

X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns

score : float
Mean accuracy of self.predict(X) wrt. y.

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it's possible to update each component
of a nested object.

Returns
self

Examples using sklearn.gaussian_process.GaussianProcessClassifier

• Plot classification probability
• Classifier comparison
• Illustration of Gaussian process classification (GPC) on the XOR dataset
• Gaussian process classification (GPC) on iris dataset
• Iso-probability lines for Gaussian Processes classification (GPC)
• Probabilistic predictions with Gaussian process classification (GPC)

30.15.2 sklearn.gaussian_process.GaussianProcessRegressor
class sklearn.gaussian_process.GaussianProcessRegressor(kernel=None, alpha=1e-10,
optimizer='fmin_l_bfgs_b',
n_restarts_optimizer=0,
normalize_y=False,
copy_X_train=True, random_state=None)

Gaussian process regression (GPR).

The implementation is based on Algorithm 2.1 of Gaussian Processes for Machine Learning (GPML) by Ras-
mussen and Williams.

In addition to standard scikit-learn estimator API, GaussianProcessRegressor:
• allows prediction without prior fitting (based on the GP prior)
• provides an additional method sample_y(X), which evaluates samples drawn from the GPR (prior or pos-
terior) at given inputs
• exposes a method log_marginal_likelihood(theta), which can be used externally for other ways of selecting
hyperparameters, e.g., via Markov chain Monte Carlo.
Read more in the User Guide.
New in version 0.18.

Parameters kernel : kernel object

The kernel specifying the covariance function of the GP. If None is passed, the kernel “1.0 * RBF(1.0)” is used as default. Note that the kernel’s hyperparameters are optimized during fitting.

alpha : float or array-like, optional (default: 1e-10)

Value added to the diagonal of the kernel matrix during fitting. Larger values correspond to increased noise level in the observations. This can also prevent a potential numerical issue during fitting, by ensuring that the calculated values form a positive definite matrix. If an array is passed, it must have the same number of entries as the data used for fitting and is used as datapoint-dependent noise level. Note that this is equivalent to adding a WhiteKernel with c=alpha. Allowing to specify the noise level directly as a parameter is mainly for convenience and for consistency with Ridge.

optimizer : string or callable, optional (default: “fmin_l_bfgs_b”)

Can either be one of the internally supported optimizers for optimizing the kernel’s parameters, specified by a string, or an externally defined optimizer passed as a callable. If a callable is passed, it must have the signature:

```python
def optimizer(obj_func, initial_theta, bounds):
    # * 'obj_func' is the objective function to be maximized,
    #   which
    #   takes the hyperparameters theta as parameter and an
    #   optional flag eval_gradient, which determines if the
    #   gradient is returned additionally to the function value
    # * 'initial_theta': the initial value for theta, which can
    #   be
    #   used by local optimizers
    # * 'bounds': the bounds on the values of theta
    ....
    # Returned are the best found hyperparameters theta and
    # the corresponding value of the target function.
    return theta_opt, func_min
```

Per default, the ‘fmin_l_bfgs_b’ algorithm from scipy.optimize is used. If None is passed, the kernel’s parameters are kept fixed. Available internal optimizers are:

'fmin_l_bfgs_b'

n_restarts_optimizer : int, optional (default: 0)

The number of restarts of the optimizer for finding the kernel’s parameters which maximize the log-marginal likelihood. The first run of the optimizer is performed from the kernel’s initial parameters, the remaining ones (if any) from thetas sampled log-uniform randomly from the space of allowed theta-values. If greater than 0, all bounds must be finite. Note that n_restarts_optimizer == 0 implies that one run is performed.

normalize_y : boolean, optional (default: False)

Whether the target values y are normalized, i.e., the mean of the observed target values become zero. This parameter should be set to True if the target values’ mean is expected to differ considerable from zero. When enabled, the normalization effectively modifies the GP’s prior based on the data, which contradicts the likelihood principle; normalization is thus disabled per default.
**copy_X_train**: bool, optional (default: True)

If True, a persistent copy of the training data is stored in the object. Otherwise, just a reference to the training data is stored, which might cause predictions to change if the data is modified externally.

**random_state**: int, RandomState instance or None, optional (default: None)

The generator used to initialize the centers. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
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</tr>
</thead>
<tbody>
<tr>
<td>X_train_</td>
<td>(array-like, shape = (n_samples, n_features)) Feature values in training data (also required for prediction)</td>
</tr>
<tr>
<td>y_train_</td>
<td>(array-like, shape = (n_samples, [n_output_dims])) Target values in training data (also required for prediction)</td>
</tr>
<tr>
<td>kernel_</td>
<td>(kernel object) The kernel used for prediction. The structure of the kernel is the same as the one passed as parameter but with optimized hyperparameters</td>
</tr>
<tr>
<td>L_</td>
<td>(array-like, shape = (n_samples, n_samples)) Lower-triangular Cholesky decomposition of the kernel in X_train_</td>
</tr>
<tr>
<td>alpha_</td>
<td>(array-like, shape = (n_samples,)) Dual coefficients of training data points in kernel space</td>
</tr>
<tr>
<td>log_marginal_likelihood_value</td>
<td>log-marginal-likelihood of self.kernel_.theta</td>
</tr>
</tbody>
</table>

### Methods

<table>
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<td>fit(X, y)</td>
<td>Fit Gaussian process regression model.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>log_marginal_likelihood([theta, eval_gradient])</td>
<td>Returns log-marginal likelihood of theta for training data.</td>
</tr>
<tr>
<td>predict(X[, return_std, return_cov])</td>
<td>Predict using the Gaussian process regression model</td>
</tr>
<tr>
<td>sample_y(X[, n_samples, random_state])</td>
<td>Draw samples from Gaussian process and evaluate at X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction. (set_params(**params))</td>
</tr>
</tbody>
</table>

**__init__**(kernel=None, alpha=1e-10, optimizer='fmin_l_bfgs_b', n_restarts_optimizer=0, normalize_y=False, copy_X_train=True, random_state=None)

**fit**(X, y)

Fit Gaussian process regression model.

**Parameters**

**X**: array-like, shape = (n_samples, n_features)

Training data

**y**: array-like, shape = (n_samples, [n_output_dims])

Target values

**Returns**

self: returns an instance of self.
get_params (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

log_marginal_likelihood (theta=None, eval_gradient=False)

Returns log-marginal likelihood of theta for training data.

Parameters theta : array-like, shape = (n_kernel_params,) or None

Kernel hyperparameters for which the log-marginal likelihood is evaluated. If None, the
precomputed log_marginal_likelihood of self.kernel_.theta is returned.

eval_gradient : bool, default: False

If True, the gradient of the log-marginal likelihood with respect to the kernel hyperpa-
rameters at position theta is returned additionally. If True, theta must not be None.

Returns log_likelihood : float

Log-marginal likelihood of theta for training data.

log_likelihood_gradient : array, shape = (n_kernel_params,), optional

Gradient of the log-marginal likelihood with respect to the kernel hyperparameters at
position theta. Only returned when eval_gradient is True.

predict (X, return_std=False, return_cov=False)

Predict using the Gaussian process regression model

We can also predict based on an unfitted model by using the GP prior. In addition to the mean of the pre-
dictive distribution, also its standard deviation (return_std=True) or covariance (return_cov=True). Note
that at most one of the two can be requested.

Parameters X : array-like, shape = (n_samples, n_features)

Query points where the GP is evaluated

return_std : bool, default: False

If True, the standard-deviation of the predictive distribution at the query points is re-
turned along with the mean.

return_cov : bool, default: False

If True, the covariance of the joint predictive distribution at the query points is returned
along with the mean

Returns y_mean : array, shape = (n_samples, [n_output_dims])

Mean of predictive distribution a query points

y_std : array, shape = (n_samples,), optional

Standard deviation of predictive distribution at query points. Only returned when re-
turn_std is True.

y_cov : array, shape = (n_samples, n_samples), optional
Covariance of joint predictive distribution a query points. Only returned when return_cov is True.

**rng**

DEPRECATED: Attribute rng was deprecated in version 0.19 and will be removed in 0.21.

**sample_y** \( (X, n_{samples}=1, \text{random\_state}=0) \)

Draw samples from Gaussian process and evaluate at X.

Parameters:
- **X**: array-like, shape = (n_samples_X, n_features)
  - Query points where the GP samples are evaluated
- **n_samples**: int, default: 1
  - The number of samples drawn from the Gaussian process
- **random_state**: int, RandomState instance or None, optional (default=0)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

Returns:
- **y_samples**: array, shape = (n_samples_X, [n_output_dims], n_samples)
  - Values of n_samples samples drawn from Gaussian process and evaluated at query points.

**score** \( (X, y, \text{sample\_weight}=\text{None}) \)

Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \( 1 - u/v \), where \( u \) is the residual sum of squares \( ((y_{true} - y_{pred})^2) \) and \( v \) is the total sum of squares \( ((y_{true} - y_{true.mean})^2) \). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

Parameters:
- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True values for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

Returns:
- **score**: float
  - \( R^2 \) of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns:
- **self**

**y_train_mean**

DEPRECATED: Attribute `y_train_mean` was deprecated in version 0.19 and will be removed in 0.21.
**Examples using sklearn.gaussian_process.GaussianProcessRegressor**

- Comparison of kernel ridge and Gaussian process regression
- Gaussian process regression (GPR) on Mauna Loa CO2 data.
- Illustration of prior and posterior Gaussian process for different kernels
- Gaussian process regression (GPR) with noise-level estimation
- Gaussian Processes regression: basic introductory example

Kernels:

<table>
<thead>
<tr>
<th>Kernel</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>gaussian_process.kernels.CompoundKernel(kernels)</code></td>
<td>Kernel which is composed of a set of other kernels.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.ConstantKernel()</code></td>
<td>Constant kernel.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Exponentiation()</code></td>
<td>Exponentiate kernel by given exponent.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Hyperparameter</code></td>
<td>A kernel hyperparameter’s specification in form of a namedtuple.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Kernel</code></td>
<td>Base class for all kernels.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Matern()</code></td>
<td>Matern kernel.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.PairwiseKernel()</code></td>
<td>Wrapper for kernels in sklearn.metrics.pairwise.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Product(k1, k2)</code></td>
<td>Product-kernel $k1 \times k2$ of two kernels $k1$ and $k2$.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.RBF([length_scale, ...])</code></td>
<td>Radial-basis function kernel (aka squared-exponential kernel).</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.RationalQuadratic()</code></td>
<td>Rational Quadratic kernel.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.Sum(k1, k2)</code></td>
<td>Sum-kernel $k1 + k2$ of two kernels $k1$ and $k2$.</td>
</tr>
<tr>
<td><code>gaussian_process.kernels.WhiteKernel()</code></td>
<td>White kernel.</td>
</tr>
</tbody>
</table>

### 30.15.3 sklearn.gaussian_process.kernels.CompoundKernel

**class** sklearn.gaussian_process.kernels.CompoundKernel(kernels)

Kernel which is composed of a set of other kernels.

New in version 0.18.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>bounds</code></td>
<td>Returns the log-transformed bounds on the theta.</td>
</tr>
<tr>
<td><code>hyperparameters</code></td>
<td>Returns a list of all hyperparameter specifications.</td>
</tr>
<tr>
<td><code>n_dims</code></td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
</tbody>
</table>

Continued on next page
theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Methods

__call__(X[, Y, eval_gradient])
Return the kernel k(X, Y) and optionally its gradient.

clone_with_theta(theta)
Returns a clone of self with given hyperparameters theta.

diag(X)
Returns the diagonal of the kernel k(X, X).

get_params([deep])
Get parameters of this kernel.

is_stationary()
Returns whether the kernel is stationary.

set_params(**params)
Set the parameters of this kernel.

__init__(kernels)
__call__(X=Y=None, eval_gradient=False)
Return the kernel k(X, Y) and optionally its gradient.

Note that this compound kernel returns the results of all simple kernel stacked along an additional axis.

Parameters

X : array, shape (n_samples_X, n_features)
Left argument of the returned kernel k(X, Y)

Y : array, shape (n_samples_Y, n_features), (optional, default=None)
Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

eval_gradient : bool (optional, default=False)
Determines whether the gradient with respect to the kernel hyperparameter is determined.

Returns

K : array, shape (n_samples_X, n_samples_Y, n_kernels)
Kernel k(X, Y)

K_gradient : array, shape (n_samples_X, n_samples_X, n_dims, n_kernels)
The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

bounds

Returns the log-transformed bounds on the theta.

Returns bounds : array, shape (n_dims, 2)
The log-transformed bounds on the kernel’s hyperparameters theta

clone_with_theta(theta)
Returns a clone of self with given hyperparameters theta.

diag(X)
Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

Parameters

X : array, shape (n_samples_X, n_features)
Left argument of the returned kernel k(X, Y)
Returns `K_diag`: array, shape (n_samples_X, n_kernels)

Diagonal of kernel k(X, X)

**get_params**(deep=True)

Get parameters of this kernel.

**Parameters**

- **deep**: boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any

  Parameter names mapped to their values.

**hyperparameters**

Returns a list of all hyperparameter specifications.

**is_stationary**()

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params**(**params**)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**: 

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns**

- **theta**: array, shape (n_dims,)

  The non-fixed, log-transformed hyperparameters of the kernel.

### 30.15.4 `sklearn.gaussian_process.kernels.ConstantKernel`

**class** `sklearn.gaussian_process.kernels.ConstantKernel`(constant_value=1.0, constant_value_bounds=(1e-05, 100000.0))

Constant kernel.

Can be used as part of a product-kernel where it scales the magnitude of the other factor (kernel) or as part of a sum-kernel, where it modifies the mean of the Gaussian process.

k(x_1, x_2) = constant_value for all x_1, x_2

New in version 0.18.

**Parameters**

- **constant_value**: float, default: 1.0

  The constant value which defines the covariance: k(x_1, x_2) = constant_value

- **constant_value Bounds**: pair of floats >= 0, default: (1e-5, 1e5)

  The lower and upper bound on constant_value
Attributes

- **bounds**
  Returns the log-transformed bounds on the theta.

- **hyperparameter_constant_value**
  Returns a list of all hyperparameter specifications.

- **hyperparameters**
  Returns the number of non-fixed hyperparameters of the kernel.

- **theta**
  Returns the (flattened, log-transformed) non-fixed hyperparameters.

Methods

- **__call__(X[, Y, eval_gradient])**
  Return the kernel k(X, Y) and optionally its gradient.

- **clone_with_theta(theta)**
  Returns a clone of self with given hyperparameters theta.

- **diag(X)**
  Returns the diagonal of the kernel k(X, X).

- **get_params(**deep**)**
  Get parameters of this kernel.

- **is_stationary()**
  Returns whether the kernel is stationary.

- **set_params(**params)**
  Set the parameters of this kernel.

**__init__**(constant_value=1.0, constant_value_bounds=(1e-05, 100000.0))

**__call__**(X, Y=None, eval_gradient=False)
  Return the kernel k(X, Y) and optionally its gradient.

  Parameters

  - **X** : array, shape (n_samples_X, n_features)
    Left argument of the returned kernel k(X, Y)

  - **Y** : array, shape (n_samples_Y, n_features), (optional, default=None)
    Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

  - **eval_gradient** : bool (optional, default=False)
    Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

  Returns

  - **K** : array, shape (n_samples_X, n_samples_Y)
    Kernel k(X, Y)

  - **K_gradient** : array (opt.), shape (n_samples_X, n_samples_X, n_dims)
    The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

- **bounds**
  Returns the log-transformed bounds on the theta.

  Returns **bounds** : array, shape (n_dims, 2)
  The log-transformed bounds on the kernel’s hyperparameters theta

- **clone_with_theta(theta)**
  Returns a clone of self with given hyperparameters theta.

- **diag(X)**
  Returns the diagonal of the kernel k(X, X).
The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

**Parameters**

- **X** : array, shape (n_samples_X, n_features)

  Left argument of the returned kernel k(X, Y)

**Returns**

- **K_diag** : array, shape (n_samples_X,)

  Diagonal of kernel k(X, X)

**get_params**(deep=True)

Get parameters of this kernel.

**Parameters**

- **deep** : boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any

  Parameter names mapped to their values.

**hyperparameters**

Returns a list of all hyperparameter specifications.

**is_stationary**()

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params**(**params**)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns**

- **theta** : array, shape (n_dims,)

  The non-fixed, log-transformed hyperparameters of the kernel

---

**Examples using sklearn.gaussian_process.kernels.ConstantKernel**

- *Illustration of prior and posterior Gaussian process for different kernels*
- *Iso-probability lines for Gaussian Processes classification (GPC)*
- *Gaussian Processes regression: basic introductory example*
30.15.5 sklearn.gaussian_process.kernels.DotProduct

class sklearn.gaussian_process.kernels.DotProduct (sigma_0=1.0, sigma_0_bounds=(1e-05, 100000.0))

Dot-Product kernel.

The DotProduct kernel is non-stationary and can be obtained from linear regression by putting \( N(0, 1) \) priors on the coefficients of \( x_d \) (\( d = 1, \ldots, D \)) and a prior of \( N(0, \sigma_0^2) \) on the bias. The DotProduct kernel is invariant to a rotation of the coordinates about the origin, but not translations. It is parameterized by a parameter \( \sigma_0^2 \). For \( \sigma_0^2 = 0 \), the kernel is called the homogeneous linear kernel, otherwise it is inhomogeneous. The kernel is given by

\[
k(x_i, x_j) = \sigma_0^2 + x_i \cdot x_j
\]

The DotProduct kernel is commonly combined with exponentiation.

New in version 0.18.

Parameters

- **sigma_0** : float \( >= 0 \), default: 1.0
  Parameter controlling the inhomogeneity of the kernel. If \( \sigma_0=0 \), the kernel is homogeneous.

- **sigma_0_bounds** : pair of floats \( >= 0 \), default: (1e-5, 1e5)
  The lower and upper bound on \( \sigma_0 \).

Attributes

- **bounds**
  Returns the log-transformed bounds on the theta.

- **hyperparameter_sigma_0**
  Returns a list of all hyperparameter specifications.

- **n_dims**
  Returns the number of non-fixed hyperparameters of the kernel.

- **theta**
  Returns the (flattened, log-transformed) non-fixed hyperparameters.

Methods

- **__call__(X[, Y, eval_gradient])**
  Return the kernel \( k(X, Y) \) and optionally its gradient.

- **clone_with_theta(theta)**
  Returns a clone of self with given hyperparameters theta.

- **diag(X)**
  Returns the diagonal of the kernel \( k(X, X) \).

- **get_params([deep])**
  Get parameters of this kernel.

- **is_stationary()**
  Returns whether the kernel is stationary.

- **set_params(**params)**
  Set the parameters of this kernel.

__init__(sigma_0=1.0, sigma_0_bounds=(1e-05, 100000.0))

__call__(X, Y=None, eval_gradient=False)
Return the kernel \( k(X, Y) \) and optionally its gradient.

Parameters

- **X** : array, shape \( (n_samples_X, n_features) \)
  Left argument of the returned kernel \( k(X, Y) \)
Y : array, shape (n_samples_Y, n_features), (optional, default=None)
    Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

eval_gradient : bool (optional, default=False)
    Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

Returns K : array, shape (n_samples_X, n_samples_Y)
    Kernel k(X, Y)

K_gradient : array (opt.), shape (n_samples_X, n_samples_X, n_dims)
    The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

bounds
    Returns the log-transformed bounds on the theta.

    Returns bounds : array, shape (n_dims, 2)
        The log-transformed bounds on the kernel’s hyperparameters theta

close_with_theta(theta)
    Returns a clone of self with given hyperparameters theta.

diag(X)
    Returns the diagonal of the kernel k(X, X).

    The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

    Parameters X : array, shape (n_samples_X, n_features)
        Left argument of the returned kernel k(X, Y)

    Returns K_diag : array, shape (n_samples_X,)
        Diagonal of kernel k(X, X)

get_params(deep=True)
    Get parameters of this kernel.

    Parameters deep : boolean, optional
        If True, will return the parameters for this estimator and contained subobjects that are estimators.

    Returns params : mapping of string to any
        Parameter names mapped to their values.

hyperparameters
    Returns a list of all hyperparameter specifications.

is_stationary()
    Returns whether the kernel is stationary.

n_dims
    Returns the number of non-fixed hyperparameters of the kernel.

set_params(**params)
    Set the parameters of this kernel.
The method works on simple kernels as well as on nested kernels. The latter have parameters of the form component__parameter so that it's possible to update each component of a nested object.

Returns: self

theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

Returns: theta : array, shape (n_dims,)

The non-fixed, log-transformed hyperparameters of the kernel

Examples using sklearn.gaussian_process.kernels.DotProduct

- Illustration of Gaussian process classification (GPC) on the XOR dataset
- Illustration of prior and posterior Gaussian process for different kernels
- Iso-probability lines for Gaussian Processes classification (GPC)

30.15.6 sklearn.gaussian_process.kernels.ExpSineSquared

class sklearn.gaussian_process.kernels.ExpSineSquared(length_scale=1.0, periodicity=1.0, length_scale_bounds=(1e-05, 100000.0), periodicity_bounds=(1e-05, 100000.0))

Exp-Sine-Squared kernel.

The ExpSineSquared kernel allows modeling periodic functions. It is parameterized by a length-scale parameter length_scale>0 and a periodicity parameter periodicity>0. Only the isotropic variant where l is a scalar is supported at the moment. The kernel given by:

k(x_i, x_j) = \exp(-2 \sin(\pi / periodicity * d(x_i, x_j)) / length_scale)^2)

New in version 0.18.

Parameters:

length_scale : float > 0, default: 1.0

The length scale of the kernel.

periodicity : float > 0, default: 1.0

The periodicity of the kernel.

length_scale_bounds : pair of floats >= 0, default: (1e-5, 1e5)

The lower and upper bound on length_scale

periodicity_bounds : pair of floats >= 0, default: (1e-5, 1e5)

The lower and upper bound on periodicity

Attributes
bounds
Returns the log-transformed bounds on the theta.

hyperparameter_length_scale
hyperparameter_periodicity

hyperparameters
Returns a list of all hyperparameter specifications.

n_dims
Returns the number of non-fixed hyperparameters of the kernel.

theta
Returns the (flattened, log-transformed) non-fixed hyperparameters.

Methods

__call__(X[, Y , eval_gradient])
Return the kernel k(X, Y) and optionally its gradient.

Parameters X: array, shape (n_samples_X, n_features)
Left argument of the returned kernel k(X, Y)

Y: array, shape (n_samples_Y, n_features), (optional, default=None)
Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

eval_gradient: bool (optional, default=False)
Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

Returns K: array, shape (n_samples_X, n_samples_Y)
Kernel k(X, Y)

K_gradient: array (opt.), shape (n_samples_X, n_samples_X, n_dims)
The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

bounds
Returns the log-transformed bounds on the theta.

Returns bounds: array, shape (n_dims, 2)
The log-transformed bounds on the kernel’s hyperparameters theta

close_with_theta(theta)
Returns a clone of self with given hyperparameters theta.

diag(X)
Returns the diagonal of the kernel k(X, X).
The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

**Parameters**

- **X**: array, shape (n_samples_X, n_features)
  
  Left argument of the returned kernel k(X, Y)

**Returns**

- **K_diag**: array, shape (n_samples_X,)
  
  Diagonal of kernel k(X, X)

**get_params** *(deep=True)*

Get parameters of this kernel.

- **Parameters**
  
  - **deep**: boolean, optional
    
    If True, will return the parameters for this estimator and contained subobjects that are estimators.

- **Returns**
  
  - **params**: mapping of string to any
    
    Parameter names mapped to their values.

** hyperparameters**

Returns a list of all hyperparameter specifications.

**is_stationary**

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params** *(**params)*

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns**

- **theta**: array, shape (n_dims,)
  
  The non-fixed, log-transformed hyperparameters of the kernel

**Examples using sklearn.gaussian_process.kernels.ExpSineSquared**

- *Comparison of kernel ridge and Gaussian process regression*
- *Gaussian process regression (GPR) on Mauna Loa CO2 data.*
- *Illustration of prior and posterior Gaussian process for different kernels*
30.15.7 sklearn.gaussian_process.kernels.Exponentiation

class sklearn.gaussian_process.kernels.Exponentiation(kernel, exponent)

Exponentiate kernel by given exponent.

The resulting kernel is defined as k_exp(X, Y) = k(X, Y) ** exponent

New in version 0.18.

Parameters

kernel : Kernel object

The base kernel

exponent : float

The exponent for the base kernel

Attributes

bounds

Returns the log-transformed bounds on the theta.

hyperparameters

Returns a list of all hyperparameters.

n_dims

Returns the number of non-fixed hyperparameters of the kernel.

theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Methods

__call__(X[, Y, eval_gradient])

Return the kernel k(X, Y) and optionally its gradient.

Parameters

X : array, shape (n_samples_X, n_features)

Left argument of the returned kernel k(X, Y)

Y : array, shape (n_samples_Y, n_features), (optional, default=None)

Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

eval_gradient : bool (optional, default=False)

Determines whether the gradient with respect to the kernel hyperparameter is determined.

Returns

K : array, shape (n_samples_X, n_samples_Y)

Kernel k(X, Y)
**K_gradient**: array (opt.), shape (n_samples_X, n_samples_X, n_dims)

The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

**bounds**

Returns the log-transformed bounds on the theta.

*Returns bounds*: array, shape (n_dims, 2)

The log-transformed bounds on the kernel’s hyperparameters theta.

**clone_with_theta**(theta)

Returns a clone of self with given hyperparameters theta.

**diag**(X)

Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

*Parameters X*: array, shape (n_samples_X, n_features)

Left argument of the returned kernel k(X, Y)

*Returns K_diag*: array, shape (n_samples_X,)

Diagonal of kernel k(X, X)

**get_params**(deep=True)

Get parameters of this kernel.

*Parameters deep*: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

*Returns params*: mapping of string to any

Parameter names mapped to their values.

**hyperparameters**

Returns a list of all hyperparameter.

**is_stationary**()

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params**(**params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

*Returns self*

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

*Returns theta*: array, shape (n_dims,)

---

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The non-fixed, log-transformed hyperparameters of the kernel

### 30.15.8 sklearn.gaussian_process.kernels.Hyperparameter

class sklearn.gaussian_process.kernels.Hyperparameter
A kernel hyperparameter’s specification in form of a namedtuple.

New in version 0.18.

#### Attributes

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>name</td>
<td>Alias for field number 0</td>
</tr>
<tr>
<td>value_type</td>
<td>Alias for field number 1</td>
</tr>
<tr>
<td>bounds</td>
<td>Alias for field number 2</td>
</tr>
<tr>
<td>n_elements</td>
<td>Alias for field number 3</td>
</tr>
<tr>
<td>fixed</td>
<td>Alias for field number 4</td>
</tr>
</tbody>
</table>

#### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>count(...)</td>
<td>Return number of occurrences of value</td>
</tr>
<tr>
<td>index(...)</td>
<td>Return first index of value. Raises ValueError if not present.</td>
</tr>
</tbody>
</table>

__init__(self, *args, **kwargs)
Initialize self. See help(type(self)) for accurate signature.

__call__(self, *args, **kwargs)
Call self as a function.

bounds
Alias for field number 2

count(value) → integer
Return number of occurrences of value.

fixed
Alias for field number 4

index(value, [start, stop]) → integer
Return first index of value. Raises ValueError if not present.

n_elements
Alias for field number 3

name
Alias for field number 0

value_type
Alias for field number 1

### 30.15.9 sklearn.gaussian_process.kernels.Kernel

class sklearn.gaussian_process.kernels.Kernel
Base class for all kernels.

New in version 0.18.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>bounds</td>
<td>Returns the log-transformed bounds on the theta.</td>
</tr>
<tr>
<td>hyperparameters</td>
<td>Returns a list of all hyperparameter specifications.</td>
</tr>
<tr>
<td>n_dims</td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
<tr>
<td>theta</td>
<td>Returns the (flattened, log-transformed) non-fixed hyperparameters.</td>
</tr>
</tbody>
</table>

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>call</strong></td>
<td>Evaluate the kernel.</td>
</tr>
<tr>
<td>clone_with_theta(theta)</td>
<td>Returns a clone of self with given hyperparameters theta.</td>
</tr>
<tr>
<td>diag(X)</td>
<td>Returns the diagonal of the kernel k(X, X).</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters of this kernel.</td>
</tr>
<tr>
<td>is_stationary()</td>
<td>Returns whether the kernel is stationary.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this kernel.</td>
</tr>
</tbody>
</table>

__init__($self, /, *args, **kwargs)
Initialize self. See help(type(self)) for accurate signature.

__call__ (X, Y=None, eval_gradient=False)
Evaluate the kernel.

bounds
Returns the log-transformed bounds on the theta.

Returns bounds : array, shape (n_dims, 2)

The log-transformed bounds on the kernel’s hyperparameters theta

clonewiththeta(theta)
Returns a clone of self with given hyperparameters theta.

diag(X)
Returns the diagonal of the kernel k(X, X).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

Parameters X : array, shape (n_samples_X, n_features)
Left argument of the returned kernel k(X, Y)

Returns K_diag : array, shape (n_samples_X,)
Diagonal of kernel k(X, X)

get_params (deep=True)
Get parameters of this kernel.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

**hyperparameters**
Returns a list of all hyperparameter specifications.

**is_stationary()**
Returns whether the kernel is stationary.

**n_dims**
Returns the number of non-fixed hyperparameters of the kernel.

**set_params(**params**)**
Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**theta**
Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns** theta : array, shape (n_dims,)

The non-fixed, log-transformed hyperparameters of the kernel

### 30.15.10 sklearn.gaussian_process.kernels.Matern

class sklearn.gaussian_process.kernels.Matern(length_scale=1.0, length_scale_bounds=(1e-05, 100000.0), nu=1.5)

Matern kernel.

The class of Matern kernels is a generalization of the RBF and the absolute exponential kernel parameterized by an additional parameter nu. The smaller nu, the less smooth the approximated function is. For nu=inf, the kernel becomes equivalent to the RBF kernel and for nu=0.5 to the absolute exponential kernel. Important intermediate values are nu=1.5 (once differentiable functions) and nu=2.5 (twice differentiable functions).

See Rasmussen and Williams 2006, pp84 for details regarding the different variants of the Matern kernel.

New in version 0.18.

**Parameters**

**length_scale** : float or array with shape (n_features,), default: 1.0

The length scale of the kernel. If a float, an isotropic kernel is used. If an array, an anisotropic kernel is used where each dimension of l defines the length-scale of the respective feature dimension.

**length_scale_bounds** : pair of floats >= 0, default: (1e-5, 1e5)

The lower and upper bound on length_scale

**nu** : float, default: 1.5

The parameter nu controlling the smoothness of the learned function. The smaller nu, the less smooth the approximated function is. For nu=inf, the kernel becomes equivalent to the RBF kernel and for nu=0.5 to the absolute exponential kernel. Important intermediate values are nu=1.5 (once differentiable functions) and nu=2.5 (twice differentiable functions). Note that values of nu not in [0.5, 1.5, 2.5, inf] incur a considerably higher computational cost (appr. 10 times higher) since they require to evaluate the modified
Bessel function. Furthermore, in contrast to l, nu is kept fixed to its initial value and not optimized.

Attributes

- anisotropic
- bounds
- hyperparameter_length_scale
- hyperparameters
- n_dims
- theta

Methods

- __call__(X[, Y, eval_gradient]) Return the kernel k(X, Y) and optionally its gradient.
- clone_with_theta(theta) Returns a clone of self with given hyperparameters theta.
- diag(X) Returns the diagonal of the kernel k(X, X).
- get_params([deep]) Get parameters of this kernel.
- is_stationary() Returns whether the kernel is stationary.
- set_params(**params) Set the parameters of this kernel.

__init__ (length_scale=1.0, length_scale_bounds=(1e-05, 100000.0), nu=1.5)
__call__ (X, Y=None, eval_gradient=False)

Return the kernel k(X, Y) and optionally its gradient.

**Parameters**

- X : array, shape (n_samples_X, n_features)
  - Left argument of the returned kernel k(X, Y)
- Y : array, shape (n_samples_Y, n_features), (optional, default=None)
  - Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.
- eval_gradient : bool (optional, default=False)
  - Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

**Returns**

- K : array, shape (n_samples_X, n_samples_Y)
  - Kernel k(X, Y)
- K_gradient : array (opt.), shape (n_samples_X, n_samples_X, n_dims)
  - The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

**bounds**

Returns the log-transformed bounds on the theta.

**Returns**

- bounds : array, shape (n_dims, 2)
  - The log-transformed bounds on the kernel’s hyperparameters theta
clone_with_theta(theta)
  Returns a clone of self with given hyperparameters theta.

diag(X)
  Returns the diagonal of the kernel k(X, X).
  The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

  Parameters X : array, shape (n_samples_X, n_features)
      Left argument of the returned kernel k(X, Y)

  Returns K_diag : array, shape (n_samples_X,)
      Diagonal of kernel k(X, X)

get_params(deep=True)
  Get parameters of this kernel.

  Parameters deep : boolean, optional
      If True, will return the parameters for this estimator and contained subobjects that are estimators.

  Returns params : mapping of string to any
      Parameter names mapped to their values.

hyperparameters
  Returns a list of all hyperparameter specifications.

is_stationary()
  Returns whether the kernel is stationary.

n_dims
  Returns the number of non-fixed hyperparameters of the kernel.

set_params(**params)
  Set the parameters of this kernel.

  The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

  Returns self

theta
  Returns the (flattened, log-transformed) non-fixed hyperparameters.

  Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

  Returns theta : array, shape (n_dims,)
      The non-fixed, log-transformed hyperparameters of the kernel

Examples using sklearn.gaussian_process.kernels.Matern

  • Illustration of prior and posterior Gaussian process for different kernels
**30.15.11 sklearn.gaussian_process.kernels.PairwiseKernel**

class sklearn.gaussian_process.kernels.PairwiseKernel (gamma=1.0, gamma_bounds=(1e-05, 100000.0), metric='linear', pairwise_kernels_kwargs=None)

Wrapper for kernels in sklearn.metrics.pairwise.

A thin wrapper around the functionality of the kernels in sklearn.metrics.pairwise.

**Note:** Evaluation of eval_gradient is not analytic but numeric and all kernels support only isotropic distances. The parameter gamma is considered to be a hyperparameter and may be optimized. The other kernel parameters are set directly at initialization and are kept fixed.

New in version 0.18.

**Parameters**

gamma: float >= 0, default: 1.0

Parameter gamma of the pairwise kernel specified by metric

**gamma_bounds**: pair of floats >= 0, default: (1e-5, 1e5)

The lower and upper bound on gamma

metric: string, or callable, default: “linear”

The metric to use when calculating kernel between instances in a feature array. If metric is a string, it must be one of the metrics in pairwise.PAIRWISE_KERNEL_FUNCTIONS. If metric is “precomputed”, X is assumed to be a kernel matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

**pairwise_kernels_kwargs**: dict, default: None

All entries of this dict (if any) are passed as keyword arguments to the pairwise kernel function.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>bounds</td>
<td>Returns the log-transformed bounds on the theta.</td>
</tr>
<tr>
<td>hyperparameter_gamma</td>
<td>Returns a list of all hyperparameter specifications.</td>
</tr>
<tr>
<td>hyperparameters</td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
<tr>
<td>n_dims</td>
<td>Returns the (flattened, log-transformed) non-fixed hyperparameters.</td>
</tr>
<tr>
<td>theta</td>
<td></td>
</tr>
</tbody>
</table>

**Methods**

__call__(X[, Y, eval_gradient])

Return the kernel k(X, Y) and optionally its gradient.

close_with_theta(theta)

Returns a clone of self with given hyperparameters theta.

diag(X)

Returns the diagonal of the kernel k(X, X).

get_params([deep])

Get parameters of this kernel.

Continued on next page
Table 30.145 – continued from previous page

<table>
<thead>
<tr>
<th>method</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>is_stationary()</code></td>
<td>Returns whether the kernel is stationary.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this kernel.</td>
</tr>
</tbody>
</table>

```python
__init__(gamma=1.0, gamma_bounds=(1e-05, 100000.0), metric='linear', pairwise_kernels_kwargs=None)
```

Return the kernel \( k(X, Y) \) and optionally its gradient.

**Parameters**

- **X**: array, shape (n_samples_X, n_features)
  
  Left argument of the returned kernel \( k(X, Y) \)

- **Y**: array, shape (n_samples_Y, n_features), (optional, default=None)
  
  Right argument of the returned kernel \( k(X, Y) \). If None, \( k(X, X) \) if evaluated instead.

- **eval_gradient**: bool (optional, default=False)
  
  Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

**Returns**

- **K**: array, shape (n_samples_X, n_samples_Y)
  
  Kernel \( k(X, Y) \)

- **K_gradient**: array (opt.), shape (n_samples_X, n_samples_X, n_dims)
  
  The gradient of the kernel \( k(X, X) \) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

```python
bounds
```

Returns the log-transformed bounds on the theta.

**Returns**

- **bounds**: array, shape (n_dims, 2)
  
  The log-transformed bounds on the kernel’s hyperparameters theta

```python
clone_with_theta(theta)
```

Returns a clone of self with given hyperparameters theta.

```python
diag(X)
```

Returns the diagonal of the kernel \( k(X, X) \).

The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

**Parameters**

- **X**: array, shape (n_samples_X, n_features)
  
  Left argument of the returned kernel \( k(X, Y) \)

**Returns**

- **K_diag**: array, shape (n_samples_X,)
  
  Diagonal of kernel \( k(X, X) \)

```python
get_params (deep=True)
```

Get parameters of this kernel.

**Parameters**

- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  
  Parameter names mapped to their values.
hyperparameters
Returns a list of all hyperparameter specifications.

is_stationary()
Returns whether the kernel is stationary.

n_dims
Returns the number of non-fixed hyperparameters of the kernel.

set_params(**params)
Set the parameters of this kernel.
The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

theta
Returns the (flattened, log-transformed) non-fixed hyperparameters.
Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

Returns theta : array, shape (n_dims,)
The non-fixed, log-transformed hyperparameters of the kernel

30.15.12 sklearn.gaussian_process.kernels.Product

class sklearn.gaussian_process.kernels.Product(kl, k2)
Product-kernel kl * k2 of two kernels kl and k2.
The resulting kernel is defined as k_prod(X, Y) = kl(X, Y) * k2(X, Y)
New in version 0.18.

Parameters kl : Kernel object
The first base-kernel of the product-kernel

k2 : Kernel object
The second base-kernel of the product-kernel

Attributes

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>bounds</td>
<td>Returns the log-transformed bounds on the theta.</td>
</tr>
<tr>
<td>hyperparameters</td>
<td>Returns a list of all hyperparameter.</td>
</tr>
<tr>
<td>n_dims</td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
<tr>
<td>theta</td>
<td>Returns the (flattened, log-transformed) non-fixed hyperparameters.</td>
</tr>
</tbody>
</table>

Methods
<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>call</strong>()</td>
<td>Return the kernel $k(X, Y)$ and optionally its gradient.</td>
</tr>
<tr>
<td>clone_with_theta(theta)</td>
<td>Returns a clone of self with given hyperparameters theta.</td>
</tr>
<tr>
<td>diag(X)</td>
<td>Returns the diagonal of the kernel $k(X, X)$.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters of this kernel.</td>
</tr>
<tr>
<td>is_stationary()</td>
<td>Returns whether the kernel is stationary.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this kernel.</td>
</tr>
<tr>
<td><strong>init</strong>(k1, k2)</td>
<td><strong>call</strong>(X, Y=None, eval_gradient=False) Return the kernel $k(X, Y)$ and optionally its gradient.</td>
</tr>
</tbody>
</table>

**Parameters**

- **X**: array, shape (n_samples_X, n_features)
  - Left argument of the returned kernel $k(X, Y)$
- **Y**: array, shape (n_samples_Y, n_features), (optional, default=None)
  - Right argument of the returned kernel $k(X, Y)$. If None, $k(X, X)$ if evaluated instead.
- **eval_gradient**: bool (optional, default=False)
  - Determines whether the gradient with respect to the kernel hyperparameter is determined.

**Returns**

- **K**: array, shape (n_samples_X, n_samples_Y)
  - Kernel $k(X, Y)$
- **K_gradient**: array (opt.), shape (n_samples_X, n_samples_X, ndims)
  - The gradient of the kernel $k(X, X)$ with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

**bounds**

- Returns **bounds**: array, shape (ndims, 2)
  - The log-transformed bounds on the kernel’s hyperparameters theta

**clone_with_theta(theta)**

- Returns a clone of self with given hyperparameters theta.

**diag(X)**

- Returns the diagonal of the kernel $k(X, X)$.
  - The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

**Parameters**

- **X**: array, shape (n_samples_X, n_features)
  - Left argument of the returned kernel $k(X, Y)$

**Returns**

- **K_diag**: array, shape (n_samples_X,)
  - Diagonal of kernel $k(X, X)$

**get_params**(deep=True)

- Get parameters of this kernel.

**Parameters**

- **deep**: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

hyperparameters
Returns a list of all hyperparameter.

is_stationary()
Returns whether the kernel is stationary.

n_dims
Returns the number of non-fixed hyperparameters of the kernel.

set_params(**params)
Set the parameters of this kernel.
The method works on simple kernels as well as on nested kernels. The latter have parameters of the form
<component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

theta
Returns the (flattened, log-transformed) non-fixed hyperparameters.
Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representa-
tion of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales
naturally live on a log-scale.

Returns theta : array, shape (n_dims,)
The non-fixed, log-transformed hyperparameters of the kernel

30.15.13 sklearn.gaussian_process.kernels.RBF

class sklearn.gaussian_process.kernels.RBF (length_scale=1.0, length_scale_bounds=(1e-05, 100000.0))
Radial-basis function kernel (aka squared-exponential kernel).
The RBF kernel is a stationary kernel. It is also known as the “squared exponential” kernel. It is parameterized
by a length-scale parameter length_scale>0, which can either be a scalar (isotropic variant of the kernel) or a
vector with the same number of dimensions as the inputs X (anisotropic variant of the kernel). The kernel is
given by:
k(x_i, x_j) = exp(-1 / 2 d(x_i / length_scale, x_j / length_scale)^2)
This kernel is infinitely differentiable, which implies that GPs with this kernel as covariance function have mean
square derivatives of all orders, and are thus very smooth.
New in version 0.18.

Parameters length_scale : float or array with shape (n_features,), default: 1.0
The length scale of the kernel. If a float, an isotropic kernel is used. If an array, an
anisotropic kernel is used where each dimension of l defines the length-scale of the
respective feature dimension.

length_scale_bounds : pair of floats >= 0, default: (1e-5, 1e5)
The lower and upper bound on length_scale
Attributes

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>anisotropic</td>
<td></td>
</tr>
<tr>
<td>bounds</td>
<td>Returns the log-transformed bounds on the theta.</td>
</tr>
<tr>
<td>hyperparameter_length_scale</td>
<td>Returns a list of all hyperparameter specifications.</td>
</tr>
<tr>
<td>hyperparameters</td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
<tr>
<td>n_dims</td>
<td>Returns the (flattened, log-transformed) non-fixed hyperparameters.</td>
</tr>
<tr>
<td>theta</td>
<td></td>
</tr>
</tbody>
</table>

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>__call__</code>(X[, Y, eval_gradient])</td>
<td>Return the kernel k(X, Y) and optionally its gradient.</td>
</tr>
<tr>
<td><code>clone_with_theta</code>(theta)</td>
<td>Returns a clone of self with given hyperparameters theta.</td>
</tr>
<tr>
<td><code>diag</code>(X)</td>
<td>Returns the diagonal of the kernel k(X, X).</td>
</tr>
<tr>
<td><code>get_params</code>([deep])</td>
<td>Get parameters of this kernel.</td>
</tr>
<tr>
<td><code>is_stationary</code>()</td>
<td>Returns whether the kernel is stationary.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this kernel.</td>
</tr>
</tbody>
</table>

`__init__`(length_scale=1.0, length_scale_bounds=(1e-05, 100000.0))

Return the kernel k(X, Y) and optionally its gradient.

Parameters

- **X**: array, shape (n_samples_X, n_features)
  
  Left argument of the returned kernel k(X, Y)

- **Y**: array, shape (n_samples_Y, n_features), (optional, default=None)
  
  Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

- **eval_gradient**: bool (optional, default=False)
  
  Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

Returns

- **K**: array, shape (n_samples_X, n_samples_Y)
  
  Kernel k(X, Y)

- **K_gradient**: array (opt.), shape (n_samples_X, n_samples_X, n_dims)
  
  The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

`bounds`

Returns the log-transformed bounds on the theta.

Returns **bounds**: array, shape (n_dims, 2)

The log-transformed bounds on the kernel’s hyperparameters theta

`clone_with_theta`(theta)

Returns a clone of self with given hyperparameters theta.
\texttt{diag}(X)

Returns the diagonal of the kernel \(k(X, X)\).

The result of this method is identical to \texttt{np.diag(self(X))}; however, it can be evaluated more efficiently since only the diagonal is evaluated.

\textbf{Parameters} \(X\): array, shape (\textit{n}\_\textit{samples}\_\textit{X}, \textit{n}\_\textit{features})

Left argument of the returned kernel \(k(X, Y)\)

\textbf{Returns} \(K\_\text{diag}\): array, shape (\textit{n}\_\textit{samples}\_\textit{X},)

Diagonal of kernel \(k(X, X)\)

\texttt{get_params}(\textit{deep}=True)

Get parameters of this kernel.

\textbf{Parameters} \textit{deep}: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

\textbf{Returns} \textit{params}: mapping of string to any

Parameter names mapped to their values.

\textbf{hyperparameters}

Returns a list of all hyperparameter specifications.

\texttt{is\_stationary}()

Returns whether the kernel is stationary.

\textbf{n\_dims}

Returns the number of non-fixed hyperparameters of the kernel.

\texttt{set\_params}(**\textit{params})

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form \texttt{<component>\_<parameter>} so that it’s possible to update each component of a nested object.

\textbf{Returns} \textit{self}

\textbf{theta}

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that \textit{theta} are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

\textbf{Returns} \textit{theta}: array, shape (\textit{n}\_\textit{dims},)

The non-fixed, log-transformed hyperparameters of the kernel

\textbf{Examples using} \texttt{sklearn.gaussian_process.kernels.RBF}

- \textit{Plot classification probability}
- \textit{Classifier comparison}
- \textit{Illustration of Gaussian process classification (GPC) on the XOR dataset}
- \textit{Gaussian process classification (GPC) on iris dataset}
- \textit{Gaussian process regression (GPR) on Mauna Loa CO2 data}. 
• Illustration of prior and posterior Gaussian process for different kernels
• Probabilistic predictions with Gaussian process classification (GPC)
• Gaussian process regression (GPR) with noise-level estimation
• Gaussian Processes regression: basic introductory example

30.15.14 sklearn.gaussian_process.kernels.RationalQuadratic

class sklearn.gaussian_process.kernels.RationalQuadratic(length_scale=1.0, alpha=1.0, length_scale_bounds=(1e-05, 100000.0), alpha_bounds=(1e-05, 100000.0))

Rational Quadratic kernel.

The RationalQuadratic kernel can be seen as a scale mixture (an infinite sum) of RBF kernels with different characteristic length-scales. It is parameterized by a length-scale parameter length_scale>0 and a scale mixture parameter alpha>0. Only the isotropic variant where length_scale is a scalar is supported at the moment. The kernel given by:

\[ k(x_i, x_j) = \left(1 + \frac{d(x_i, x_j)^2}{2*alpha * length_scale^2}\right)^{-alpha} \]

New in version 0.18.

**Parameters**

- **length_scale**: float > 0, default: 1.0
  
  The length scale of the kernel.

- **alpha**: float > 0, default: 1.0
  
  Scale mixture parameter

- **length_scale_bounds**: pair of floats >= 0, default: (1e-5, 1e5)
  
  The lower and upper bound on length_scale

- **alpha_bounds**: pair of floats >= 0, default: (1e-5, 1e5)
  
  The lower and upper bound on alpha

**Attributes**

- **bounds**: Returns the log-transformed bounds on the theta.
- **hyperparameter_alpha**:
- **hyperparameter_length_scale**:
- **hyperparameters**: Returns a list of all hyperparameter specifications.
- **n_dims**: Returns the number of non-fixed hyperparameters of the kernel.
- **theta**: Returns the (flattened, log-transformed) non-fixed hyperparameters.

**Methods**
__call__(X[, Y, eval_gradient]) Return the kernel k(X, Y) and optionally its gradient.

clone_with_theta(theta) Returns a clone of self with given hyperparameters theta.

diag(X) Returns the diagonal of the kernel k(X, X).

get_params([deep]) Get parameters of this kernel.

is_stationary() Returns whether the kernel is stationary.

set_params(**params) Set the parameters of this kernel.

__init__(length_scale=1.0, alpha=1.0, length_scale_bounds=(1e-05, 100000.0), alpha_bounds=(1e-05, 100000.0))

__call__(X, Y=None, eval_gradient=False) Return the kernel k(X, Y) and optionally its gradient.

Parameters
X : array, shape (n_samples_X, n_features)
    Left argument of the returned kernel k(X, Y)

Y : array, shape (n_samples_Y, n_features), (optional, default=None)
    Right argument of the returned kernel k(X, Y). If None, k(X, X) if evaluated instead.

eval_gradient : bool (optional, default=False)
    Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

Returns
K : array, shape (n_samples_X, n_samples_Y)
    Kernel k(X, Y)

K_gradient : array (opt.), shape (n_samples_X, n_samples_X, n_dims)
    The gradient of the kernel k(X, X) with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

bounds
    Returns the log-transformed bounds on the theta.

Returns bounds : array, shape (n_dims, 2)
    The log-transformed bounds on the kernel’s hyperparameters theta

clonewiththeta(theta)
    Returns a clone of self with given hyperparameters theta.

diag(X)
    Returns the diagonal of the kernel k(X, X).

    The result of this method is identical to np.diag(self(X)); however, it can be evaluated more efficiently since only the diagonal is evaluated.

Parameters
X : array, shape (n_samples_X, n_features)
    Left argument of the returned kernel k(X, Y)

Returns K_diag : array, shape (n_samples_X,)
    Diagonal of kernel k(X, X)

get_params(deep=True)
    Get parameters of this kernel.

Parameters
deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**hyperparameters**

Returns a list of all hyperparameter specifications.

**is_stationary()**

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params(**params)**

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

**Returns** self

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel's hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns** theta : array, shape (n_dims,)

The non-fixed, log-transformed hyperparameters of the kernel

**Examples using sklearn.gaussian_process.kernels.RationalQuadratic**

- Gaussian process regression (GPR) on Mauna Loa CO2 data.
- Illustration of prior and posterior Gaussian process for different kernels

**30.15.15 sklearn.gaussian_process.kernels.Sum**

**class** sklearn.gaussian_process.kernels.Sum(k1, k2)

Sum-kernel k1 + k2 of two kernels k1 and k2.

The resulting kernel is defined as k_sum(X, Y) = k1(X, Y) + k2(X, Y)

New in version 0.18.

**Parameters** k1 : Kernel object

The first base-kernel of the sum-kernel

k2 : Kernel object

The second base-kernel of the sum-kernel

**Attributes**
**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>call</strong> (X[, Y, \text{eval_gradient}])</td>
<td>Return the kernel (k(X, Y)) and optionally its gradient.</td>
</tr>
<tr>
<td>clone_with_theta (\text{theta})</td>
<td>Returns a clone of self with given hyperparameters (\text{theta}).</td>
</tr>
<tr>
<td>diag (X)</td>
<td>Returns the diagonal of the kernel (k(X, X)).</td>
</tr>
<tr>
<td>get_params ([\text{deep}])</td>
<td>Get parameters of this kernel.</td>
</tr>
<tr>
<td>is_stationary ()</td>
<td>Returns whether the kernel is stationary.</td>
</tr>
<tr>
<td>set_params (**\text{params})</td>
<td>Set the parameters of this kernel.</td>
</tr>
</tbody>
</table>

**__init__ \((k1, k2)\)**

**__call__ \((X, Y=\text{None}, \text{eval\_gradient}=\text{False})\)**

Return the kernel \(k(X, Y)\) and optionally its gradient.

**Parameters**
- \(X\) : array, shape \((n\_samples\_X, n\_features)\)
  - Left argument of the returned kernel \(k(X, Y)\)
- \(Y\) : array, shape \((n\_samples\_Y, n\_features)\), (optional, default=\(\text{None}\))
  - Right argument of the returned kernel \(k(X, Y)\). If \(\text{None}\), \(k(X, X)\) if evaluated instead.
- \(\text{eval\_gradient}\) : bool (optional, default=\(\text{False}\))
  - Determines whether the gradient with respect to the kernel hyperparameter is determined.

**Returns**
- \(K\) : array, shape \((n\_samples\_X, n\_samples\_Y)\)
  - Kernel \(k(X, Y)\)
- \(K\_\text{gradient}\) : array (opt.), shape \((n\_samples\_X, n\_samples\_X, n\_d dims)\)
  - The gradient of the kernel \(k(X, X)\) with respect to the hyperparameter of the kernel. Only returned when \(\text{eval\_gradient}\) is \(\text{True}\).

**bounds**

Returns the log-transformed bounds on the theta.

**Returns bounds** : array, shape \((n\_dims, 2)\)

The log-transformed bounds on the kernel’s hyperparameters theta

**clone_with_theta \((\text{theta})\)**

Returns a clone of self with given hyperparameters \(\text{theta}\).

**diag \((X)\)**

Returns the diagonal of the kernel \(k(X, X)\).

The result of this method is identical to \(\text{np.diag(self}(X))\); however, it can be evaluated more efficiently since only the diagonal is evaluated.
Parameters $X$: array, shape (n_samples_X, n_features)

Left argument of the returned kernel $k(X, Y)$

Returns $K_{\text{diag}}$: array, shape (n_samples_X,)

Diagonal of kernel $k(X, X)$

get_params ($deep=True$)

Get parameters of this kernel.

Parameters $deep$: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns $params$: mapping of string to any

Parameter names mapped to their values.

hyperparameters

Returns a list of all hyperparameter.

is_stationary()

Returns whether the kernel is stationary.

n_dims

Returns the number of non-fixed hyperparameters of the kernel.

set_params (**params)

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form $<\text{component}>_{__}<\text{parameter}>$ so that it’s possible to update each component of a nested object.

Returns self

theta

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

Returns $theta$: array, shape (n_dims,)

The non-fixed, log-transformed hyperparameters of the kernel

30.15.16 sklearn.gaussian_process.kernels.WhiteKernel

class sklearn.gaussian_process.kernels.WhiteKernel ($noise_level=1.0$, $noise_level_bounds=(1e-05, 100000.0)$)

White kernel.

The main use-case of this kernel is as part of a sum-kernel where it explains the noise-component of the signal. Tuning its parameter corresponds to estimating the noise-level.

$k(x_1, x_2) = noise\_level$ if $x_1 == x_2$ else $0$

New in version 0.18.

Parameters $noise\_level$: float, default: 1.0

Parameter controlling the noise level
noise_level_bounds : pair of floats $\geq 0$, default: $(1e-5, 1e5)$

The lower and upper bound on noise_level

Attributes

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</tr>
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<td>hyperparameter_noise_level</td>
<td>Returns a list of all hyperparameter specifications.</td>
</tr>
<tr>
<td>hyperparameters</td>
<td>Returns the number of non-fixed hyperparameters of the kernel.</td>
</tr>
<tr>
<td>theta</td>
<td>Returns the (flattened, log-transformed) non-fixed hyperparameters.</td>
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Methods

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<td><strong>call</strong> (X[, Y, eval_gradient])</td>
<td>Return the kernel $k(X, Y)$ and optionally its gradient.</td>
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<td>clone_with_theta(θ)</td>
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<td>Returns the diagonal of the kernel $k(X, X)$.</td>
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<td>get_params([deep])</td>
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<td>set_params(**params)</td>
<td>Set the parameters of this kernel.</td>
</tr>
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</table>

__init__(noise_level=1.0, noise_level_bounds=(1e-05, 100000.0))

__call__(X, Y=None, eval_gradient=False)

Return the kernel $k(X, Y)$ and optionally its gradient.

**Parameters**

- **X** : array, shape (n_samples_X, n_features)
  - Left argument of the returned kernel $k(X, Y)$

- **Y** : array, shape (n_samples_Y, n_features), (optional, default=None)
  - Right argument of the returned kernel $k(X, Y)$. If None, $k(X, X)$ if evaluated instead.

- **eval_gradient** : bool (optional, default=False)
  - Determines whether the gradient with respect to the kernel hyperparameter is determined. Only supported when Y is None.

**Returns**

- **K** : array, shape (n_samples_X, n_samples_Y)
  - Kernel $k(X, Y)$

- **K_gradient** : array (opt.), shape (n_samples_X, n_samples_X, n_dims)
  - The gradient of the kernel $k(X, Y)$ with respect to the hyperparameter of the kernel. Only returned when eval_gradient is True.

**bounds**

Returns the log-transformed bounds on the theta.

**Returns**

- **bounds** : array, shape (n_dims, 2)
  - The log-transformed bounds on the kernel’s hyperparameters theta
**clone_with_theta** *(theta)*

Returns a clone of self with given hyperparameters theta.

**diag** *(X)*

Returns the diagonal of the kernel \( k(X, X) \).

The result of this method is identical to `np.diag(self(X))`; however, it can be evaluated more efficiently since only the diagonal is evaluated.

**Parameters**

\- **X** : array, shape (n_samples_X, n_features)
  
  Left argument of the returned kernel \( k(X, Y) \)

**Returns**

\- **K_diag** : array, shape (n_samples_X,)
  
  Diagonal of kernel \( k(X, X) \)

**get_params** *(deep=True)*

Get parameters of this kernel.

**Parameters**

\- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

\- **params** : mapping of string to any
  
  Parameter names mapped to their values.

**hyperparameters**

Returns a list of all hyperparameter specifications.

**is_stationary** *

Returns whether the kernel is stationary.

**n_dims**

Returns the number of non-fixed hyperparameters of the kernel.

**set_params** *(**params)*

Set the parameters of this kernel.

The method works on simple kernels as well as on nested kernels. The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

**theta**

Returns the (flattened, log-transformed) non-fixed hyperparameters.

Note that theta are typically the log-transformed values of the kernel’s hyperparameters as this representation of the search space is more amenable for hyperparameter search, as hyperparameters like length-scales naturally live on a log-scale.

**Returns**

\- **theta** : array, shape (n_dims,)
  
  The non-fixed, log-transformed hyperparameters of the kernel

**Examples using sklearn.gaussian_process.kernels.WhiteKernel**

- *Comparison of kernel ridge and Gaussian process regression*
- *Gaussian process regression (GPR) on Mauna Loa CO2 data.*
- *Gaussian process regression (GPR) with noise-level estimation*
30.16 sklearn.isotonic: Isotonic regression

User guide: See the Isotonic regression section for further details.

```
isotonic.IsotonicRegression([y_min,  y_max,  Isotonic regression model.  ...
```

30.16.1 sklearn.isotonic.IsotonicRegression

class sklearn.isotonic.IsotonicRegression(y_min=None,  y_max=None,  increasing=True,  `out_of_bounds='nan'`)

Isotonic regression model.

The isotonic regression optimization problem is defined by:

```
min sum w_i (y[i] - y_[i]) ** 2
subject to y_[i] <= y[j] whenever X[i] <= X[j]  
and min(y_) = y_min,  max(y_) = y_max
```

where:

- y[i] are inputs (real numbers)
- y_[i] are fitted
- X specifies the order. If X is non-decreasing then y_ is non-decreasing.
- w[i] are optional strictly positive weights (default to 1.0)

Read more in the User Guide.

**Parameters**

- **y_min**: optional, default: None
  If not None, set the lowest value of the fit to y_min.
- **y_max**: optional, default: None
  If not None, set the highest value of the fit to y_max.
- **increasing**: boolean or string, optional, default: True
  If boolean, whether or not to fit the isotonic regression with y increasing or decreasing.
  The string value “auto” determines whether y should increase or decrease based on the Spearman correlation estimate’s sign.
- **out_of_bounds**: string, optional, default: “nan”
  The out_of_bounds parameter handles how x-values outside of the training domain are handled. When set to “nan”, predicted y-values will be NaN. When set to “clip”, predicted y-values will be set to the value corresponding to the nearest train interval endpoint. When set to “raise”, allow interp1d to throw ValueError.

...
Attributes

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<tr>
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<tbody>
<tr>
<td>X_min</td>
<td>(float) Minimum value of input array X for left bound.</td>
</tr>
<tr>
<td>X_max</td>
<td>(float) Maximum value of input array X for right bound.</td>
</tr>
<tr>
<td>f_</td>
<td>(function) The stepwise interpolating function that covers the domain X.</td>
</tr>
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Notes

Ties are broken using the secondary method from Leeuw, 1977.

References

Isotone Optimization in R : Pool-Adjacent-Violators Algorithm (PAVA) and Active Set Methods Leeuw, Hornik, Mair Journal of Statistical Software 2009
Correctness of Kruskal’s algorithms for monotone regression with ties Leeuw, Psychometrica, 1977

Methods

- `fit(X, y[, sample_weight])`: Fit the model using X, y as training data.
- `fit_transform(X[, y])`: Fit to data, then transform it.
- `get_params([deep])`: Get parameters for this estimator.
- `predict(T)`: Predict new data by linear interpolation.
- `score(X, y[, sample_weight])`: Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(T)`: Transform new data by linear interpolation.

```
__init__(y_min=None, y_max=None, increasing=True, out_of_bounds='nan')
```

`X_`

DEPRECATED: Attribute $X_\$ is deprecated in version 0.18 and will be removed in version 0.20.

```
fit (X, y, sample_weight=None)
```

Fit the model using X, y as training data.

**Parameters**

- $X_\$: array-like, shape=(n_samples,)
  
  Training data.

- $y_\$: array-like, shape=(n_samples,)
  
  Training target.

- `sample_weight`: array-like, shape=(n_samples,), optional, default: None
  
  Weights. If set to None, all weights will be set to 1 (equal weights).

**Returns**

- `self`: object
  
  Returns an instance of self.
Notes

X is stored for future use, as transform needs X to interpolate new input data.

**fit_transform**(X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X** : numpy array of shape [n_samples, n_features]
  Training set.
- **y** : numpy array of shape [n_samples]
  Target values.

**Returns**

- **X_new** : numpy array of shape [n_samples, n_features_new]
  Transformed array.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  Parameter names mapped to their values.

**predict**(T)

Predict new data by linear interpolation.

**Parameters**

- **T** : array-like, shape=(n_samples,)
  Data to transform.

**Returns**

- **T_** : array, shape=(n_samples,)
  Transformed data.

**score**(X, y, sample_weight=None)

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters**

- **X** : array-like, shape = (n_samples, n_features)
  Test samples.
- **y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.
- **sample_weight** : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- **score** : float
  R^2 of self.predict(X) wrt. y.
**set_params(**params)**
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns: self

**transform**(T)
Transform new data by linear interpolation

Parameters:

- **T**: array-like, shape=(n_samples,)
  Data to transform.

Returns:

- **T_**: array, shape=(n_samples,)
  The transformed data

**y_**
DEPRECATED: Attribute `y_` is deprecated in version 0.18 and will be removed in version 0.20.

**Examples using sklearn.isotonic.IsotonicRegression**

- **Isotonic Regression**

  isotonic.check_increasing(x, y)  
  Determine whether y is monotonically correlated with x.

  isotonic.isotonic_regression(y[, ...])  
  Solve the isotonic regression model:

**30.16.2 sklearn.isotonic.check_increasing**

**sklearn.isotonic.check_increasing**(x, y)

Determine whether y is monotonically correlated with x.

y is found increasing or decreasing with respect to x based on a Spearman correlation test.

Parameters:

- **x**: array-like, shape=(n_samples,)
  Training data.

- **y**: array-like, shape=(n_samples,)
  Training target.

Returns:

- **increasing_bool**: boolean
  Whether the relationship is increasing or decreasing.

Notes

The Spearman correlation coefficient is estimated from the data, and the sign of the resulting estimate is used as the result.

In the event that the 95% confidence interval based on Fisher transform spans zero, a warning is raised.
30.16.3 sklearn.isotonic.isotonic_regression

The `sklearn.isotonic.isotonic_regression` function solves the isotonic regression model:

\[
\min \sum w[i] (y[i] - y_\text{[i]})^2
\]

subject to \(y\_\text{min} = y_\text{[1]} \leq y_\text{[2]} \ldots \leq y_\text{n} = y_\text{max}\)

where:

- \(y[i]\) are inputs (real numbers)
- \(y_\text{[i]}\) are fitted
- \(w[i]\) are optional strictly positive weights (default to 1.0)


**Parameters**

- \(y\) : iterable of floating-point values
  - The data.
- \(sample\_weight\) : iterable of floating-point values, optional, default: None
  - Weights on each point of the regression. If None, weight is set to 1 (equal weights).
- \(y\_\text{min}\) : optional, default: None
  - If not None, set the lowest value of the fit to \(y\_\text{min}\).
- \(y\_\text{max}\) : optional, default: None
  - If not None, set the highest value of the fit to \(y\_\text{max}\).
- \(increasing\) : boolean, optional, default: True
  - Whether to compute \(y\) is increasing (if set to True) or decreasing (if set to False)

**Returns**

- \(y\) : list of floating-point values
  - Isotonic fit of \(y\).

**References**

"Active set algorithms for isotonic regression; A unifying framework" by Michael J. Best and Nilotpal Chakravarti, section 3.

30.17 sklearn.kernel_approximation Kernel Approximation

The `sklearn.kernel_approximation` module implements several approximate kernel feature maps base on Fourier transforms.
User guide: See the Kernel Approximation section for further details.

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<td>Approximate feature map for additive chi2 kernel.</td>
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<td><code>Nystroem</code></td>
<td>Approximate a kernel map using a subset of the training data.</td>
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<td><code>RBFSampler</code></td>
<td>Approximates feature map of an RBF kernel by Monte Carlo approximation of its Fourier transform.</td>
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<td><code>SkewedChi2Sampler</code></td>
<td>Approximates feature map of the “skewed chi-squared” kernel by Monte Carlo approximation of its Fourier transform.</td>
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# 30.17.1 sklearn.kernel_approximation.AdditiveChi2Sampler

class `sklearn.kernel_approximation.AdditiveChi2Sampler` (sample_steps=2, sample_interval=None)

Approximate feature map for additive chi2 kernel.

Uses sampling the fourier transform of the kernel characteristic at regular intervals.

Since the kernel that is to be approximated is additive, the components of the input vectors can be treated separately. Each entry in the original space is transformed into 2*sample_steps+1 features, where sample_steps is a parameter of the method. Typical values of sample_steps include 1, 2 and 3.

Optimal choices for the sampling interval for certain data ranges can be computed (see the reference). The default values should be reasonable.

Read more in the User Guide.

**Parameters**

- `sample_steps`: int, optional
  
  Gives the number of (complex) sampling points.
  
- `sample_interval`: float, optional
  
  Sampling interval. Must be specified when sample_steps not in \{1,2,3\}.

**See also**

- `SkewedChi2Sampler` A Fourier-approximation to a non-additive variant of the chi squared kernel.
- `sklearn.metrics.pairwise.chi2_kernel` The exact chi squared kernel.
- `sklearn.metrics.pairwise.additive_chi2_kernel` The exact additive chi squared kernel.

**Notes**

This estimator approximates a slightly different version of the additive chi squared kernel then `metric.additive_chi2` computes.

**References**

See “Efficient additive kernels via explicit feature maps” A. Vedaldi and A. Zisserman, Pattern Analysis and Machine Intelligence, 2011
Methods

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<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Apply approximate feature map to X.</td>
</tr>
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</table>

```python
__init__(sample_steps=2, sample_interval=None)
```

```python
fit (X, y=None)
Set parameters.
```

```python
fit_transform (X, y=None, **fit_params)
Fit to data, then transform it.
```

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**
- **X**: numpy array of shape [n_samples, n_features]
  
  Training set.

- **y**: numpy array of shape [n_samples]
  
  Target values.

**Returns**
- **X_new**: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

```python
get_params (deep=True)
Get parameters for this estimator.
```

```python
Parameters deep : boolean, optional
```

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  
  Parameter names mapped to their values.

```python
set_params (**params)
Set the parameters of this estimator.
```

```python
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.
```

**Returns**
- **self**: object

```python
transform (X)
Apply approximate feature map to X.
```

**Parameters**
- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)

**Returns**
- **X_new**: {array, sparse matrix}, shape = (n_samples, n_features * (2*sample_steps + 1))
  
  Whether the return value is an array of sparse matrix depends on the type of the input X.
Approximate a kernel map using a subset of the training data.

Constructs an approximate feature map for an arbitrary kernel using a subset of the data as basis.

Read more in the User Guide.

**Parameters**

- **kernel** : string or callable, default="rbf"
  - Kernel map to be approximated. A callable should accept two arguments and the keyword arguments passed to this object as kernel_params, and should return a floating point number.

- **n_components** : int
  - Number of features to construct. How many data points will be used to construct the mapping.

- **gamma** : float, default=None
  - Gamma parameter for the RBF, laplacian, polynomial, exponential chi2 and sigmoid kernels. Interpretation of the default value is left to the kernel; see the documentation for sklearn.metrics.pairwise. Ignored by other kernels.

- **degree** : float, default=None
  - Degree of the polynomial kernel. Ignored by other kernels.

- **coef0** : float, default=None
  - Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

- **kernel_params** : mapping of string to any, optional
  - Additional parameters (keyword arguments) for kernel function passed as callable object.

- **random_state** : int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

- **components_** : (array, shape (n_components, n_features)) Subset of training points used to construct the feature map.

- **component_indices_** : (array, shape (n_components)) Indices of components in the training set.

- **normalization_** : (array, shape (n_components, n_components)) Normalization matrix needed for embedding. Square root of the kernel matrix on components_.

**See also:**

- **RBFSampler** An approximation to the RBF kernel using random Fourier features.

- **sklearn.metrics.pairwise.kernel_metrics** List of built-in kernels.
**References**

- Williams, C.K.I. and Seeger, M. “Using the Nystroem method to speed up kernel machines”, Advances in neural information processing systems 2001

**Methods**

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<td><code>fit(X[, y])</code></td>
<td>Fit estimator to data.</td>
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<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Apply feature map to X.</td>
</tr>
</tbody>
</table>

```python
__init__(kernel='rbf', gamma=None, coef0=None, degree=None, kernel_params=None, n_components=100, random_state=None)
```

- `fit (X, y=None)`
  - Fit estimator to data.
  - Samples a subset of training points, computes kernel on these and computes normalization matrix.
  - **Parameters**
    - `X`: array-like, shape=(n_samples, n_feature)
      - Training data.
    - `y`: None

- `fit_transform (X, y=None, **fit_params)`
  - Fit to data, then transform it.
  - Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.
  - **Parameters**
    - `X`: numpy array of shape [n_samples, n_features]
      - Training set.
    - `y`: numpy array of shape [n_samples]
      - Target values.
  - **Returns**
    - `X_new`: numpy array of shape [n_samples, n_features_new]
      - Transformed array.

```python
get_params (deep=True)
```

- Get parameters for this estimator.
  - **Parameters**
    - `deep`: boolean, optional
      - If True, will return the parameters for this estimator and contained subobjects that are estimators.
  - **Returns**
    - `params`: mapping of string to any
      - Parameter names mapped to their values.

```python
set_params (**params)
```

- Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Apply feature map to X.

Computes an approximate feature map using the kernel between some training points and X.

**Parameters**

- **X**: array-like, shape=(n_samples, n_features)
  Data to transform.

**Returns**

- **X_transformed**: array, shape=(n_samples, n_components)
  Transformed data.

**Examples using** `sklearn.kernel_approximation.Nystroem`

- *Explicit feature map approximation for RBF kernels*

**30.17.3 sklearn.kernel_approximation.RBFSampler**

**class** `sklearn.kernel_approximation.RBFSampler`(gamma=1.0, n_components=100, random_state=None)

Approximates feature map of an RBF kernel by Monte Carlo approximation of its Fourier transform.

It implements a variant of Random Kitchen Sinks.[1]

Read more in the [User Guide](#).

**Parameters**

- **gamma**: float
  Parameter of RBF kernel: exp(-gamma * x^2)

- **n_components**: int
  Number of Monte Carlo samples per original feature. Equals the dimensionality of the computed feature space.

- **random_state**: int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Notes**

See “Random Features for Large-Scale Kernel Machines” by A. Rahimi and Benjamin Recht.


**Methods**
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<th>Method</th>
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<tr>
<td>fit(X[, y])</td>
<td>Fit the model with X.</td>
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<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
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<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Apply the approximate feature map to X.</td>
</tr>
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</table>

**__init__ (gamma=1.0, n_components=100, random_state=None)**

```python
def fit(self, X, y=None):
    # Fit the model with X.
    # Samples random projection according to n_features.
    #
    # Parameters
    # X : {array-like, sparse matrix}, shape (n_samples, n_features)
    # Training data, where n_samples in the number of samples and n_features is the number of features.
    #
    # Returns
    # self : object
    # Returns the transformer.
```

```python
def fit_transform(self, X, y=None, **fit_params):
    # Fit to data, then transform it.
    # Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.
    #
    # Parameters
    # X : numpy array of shape [n_samples, n_features]
    # Training set.
    # y : numpy array of shape [n_samples]
    # Target values.
    #
    # Returns
    # X_new : numpy array of shape [n_samples, n_features_new]
    # Transformed array.
```

```python
def get_params(self, deep=True):
    # Get parameters for this estimator.
    #
    # Parameters
    # deep : boolean, optional
    # If True, will return the parameters for this estimator and contained subobjects that are estimators.
    #
    # Returns
    # params : mapping of string to any
    # Parameter names mapped to their values.
```

```python
def set_params(**params):
    # Set the parameters of this estimator.
    # The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.
    #
    # Returns
    # self
```

```python
def transform(self, X):
    # Apply the approximate feature map to X.
    #
    # Parameters
    # X : {array-like, sparse matrix}, shape (n_samples, n_features)
```

30.17. sklearn.kernel_approximation Kernel Approximation
New data, where n_samples in the number of samples and n_features is the number of features.

Returns **X_new**: array-like, shape (n_samples, n_components)

Examples using `sklearn.kernel_approximation.RBFSampler`

- Explicit feature map approximation for RBF kernels

### 30.17.4 sklearn.kernel_approximation.SkewedChi2Sampler

class `sklearn.kernel_approximation.SkewedChi2Sampler` *(skewedness=1.0, n_components=100, random_state=None)*

Approximates feature map of the “skewed chi-squared” kernel by Monte Carlo approximation of its Fourier transform.

Read more in the User Guide.

**Parameters**

- **skewedness**: float
  
  “skewedness” parameter of the kernel. Needs to be cross-validated.

- **n_components**: int
  
  number of Monte Carlo samples per original feature. Equals the dimensionality of the computed feature space.

- **random_state**: int, RandomState instance or None, optional (default=None)
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

See also:

- **AdditiveChi2Sampler** A different approach for approximating an additive variant of the chi squared kernel.

- **sklearn.metrics.pairwise.chi2_kernel** The exact chi squared kernel.

**References**

See “Random Fourier Approximations for Skewed Multiplicative Histogram Kernels” by Fuxin Li, Catalin Ionescu and Cristian Sminchisescu.

**Methods**

- **fit(X[, y])**  
  
  Fit the model with X.

- **fit_transform(X[, y])**  
  
  Fit to data, then transform it.

- **get_params([deep])**  
  
  Get parameters for this estimator.

- **set_params(**params)**  
  
  Set the parameters of this estimator.

- **transform(X)**  
  
  Apply the approximate feature map to X.
__init__(skewedness=1.0, n_components=100, random_state=None)

fit(X, y=None)

Fit the model with X.

Parameters

X : array-like, shape (n_samples, n_features)

Training data, where n_samples in the number of samples and n_features is the number of features.

Returns

self : object

Returns the transformer.

fit_transform(X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters

X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns

X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.

get_params(deep=True)

Get parameters for this estimator.

Parameters

deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

params : mapping of string to any

Parameter names mapped to their values.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns

self

transform(X)

Apply the approximate feature map to X.

Parameters

X : array-like, shape (n_samples, n_features)

New data, where n_samples in the number of samples and n_features is the number of features. All values of X must be strictly greater than “-skewedness”.

Returns

X_new : array-like, shape (n_samples, n_components)
30.18 sklearn.kernel_ridge Kernel Ridge Regression

Module sklearn.kernel_ridge implements kernel ridge regression.

User guide: See the Kernel ridge regression section for further details.


30.18.1 sklearn.kernel_ridge.KernelRidge

class sklearn.kernel_ridge.KernelRidge (alpha=1, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None)

Kernel ridge regression.

Kernel ridge regression (KRR) combines ridge regression (linear least squares with l2-norm regularization) with the kernel trick. It thus learns a linear function in the space induced by the respective kernel and the data. For non-linear kernels, this corresponds to a non-linear function in the original space.

The form of the model learned by KRR is identical to support vector regression (SVR). However, different loss functions are used: KRR uses squared error loss while support vector regression uses epsilon-insensitive loss, both combined with l2 regularization. In contrast to SVR, fitting a KRR model can be done in closed-form and is typically faster for medium-sized datasets. On the other hand, the learned model is non-sparse and thus slower than SVR, which learns a sparse model for epsilon > 0, at prediction-time.

This estimator has built-in support for multi-variate regression (i.e., when y is a 2d-array of shape [n_samples, n_targets]).

Read more in the User Guide.

Parameters

alpha : {float, array-like}, shape = [n_targets]

Small positive values of alpha improve the conditioning of the problem and reduce the variance of the estimates. Alpha corresponds to \((2+C)^{-1}\) in other linear models such as LogisticRegression or LinearSVC. If an array is passed, penalties are assumed to be specific to the targets. Hence they must correspond in number.

kernel : string or callable, default="linear"

Kernel mapping used internally. A callable should accept two arguments and the keyword arguments passed to this object as kernel_params, and should return a floating point number.

gamma : float, default=None

Gamma parameter for the RBF, laplacian, polynomial, exponential chi2 and sigmoid kernels. Interpretation of the default value is left to the kernel; see the documentation for sklearn.metrics.pairwise. Ignored by other kernels.

degree : float, default=3

Degree of the polynomial kernel. Ignored by other kernels.

coef0 : float, default=1

Zero coefficient for polynomial and sigmoid kernels. Ignored by other kernels.

kernel_params : mapping of string to any, optional

Additional parameters (keyword arguments) for kernel function passed as callable object.
Attributes

<table>
<thead>
<tr>
<th>dual_coef_</th>
<th>(array, shape = [n_samples] or [n_samples, n_targets]) Representation of weight vector(s) in kernel space</th>
</tr>
</thead>
<tbody>
<tr>
<td>X_fit_</td>
<td>([array-like, sparse matrix], shape = [n_samples, n_features]) Training data, which is also required for prediction</td>
</tr>
</tbody>
</table>

See also:

- `sklearn.linear_model.Ridge` Linear ridge regression.
- `sklearn.svm.SVR` Support Vector Regression implemented using libsvm.

References


Examples

```python
>>> from sklearn.kernel_ridge import KernelRidge
>>> import numpy as np

>>> n_samples, n_features = 10, 5
>>> rng = np.random.RandomState(0)
>>> y = rng.randn(n_samples)
>>> X = rng.randn(n_samples, n_features)
>>> clf = KernelRidge(alpha=1.0)
>>> clf.fit(X, y)
KernelRidge(alpha=1.0, coef0=1, degree=3, gamma=None, kernel='linear', kernel_params=None)
```

Methods

```python
fit(X[, y, sample_weight]) Fit Kernel Ridge regression model
get_params([deep]) Get parameters for this estimator.
predict(X) Predict using the kernel ridge model
score(X, y[, sample_weight]) Returns the coefficient of determination R^2 of the prediction.
set_params(**params) Set the parameters of this estimator.

__init__ (alpha=1, kernel='linear', gamma=None, degree=3, coef0=1, kernel_params=None) Fit Kernel Ridge regression model

Parameters

- X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  Training data
- y : array-like, shape = [n_samples] or [n_samples, n_targets]
```
Target values

**sample_weight**: float or array-like of shape [n_samples]

Individual weights for each sample, ignored if None is passed.

**Returns** self : returns an instance of self.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters** deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**predict** *(X)*

Predict using the kernel ridge model

**Parameters** X : {array-like, sparse matrix}, shape = [n_samples, n_features]

Samples.

**Returns** C : array, shape = [n_samples] or [n_samples, n_targets]

Returns predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters** X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.

**Returns** score : float

R^2 of self.predict(X) wrt. y.

**set_params** *(**params)*

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self
Examples using `sklearn.kernel_ridge.KernelRidge`

- Comparison of kernel ridge regression and SVR
- Comparison of kernel ridge and Gaussian process regression

30.19 sklearn.linear_model: Generalized Linear Models

The `sklearn.linear_model` module implements generalized linear models. It includes Ridge regression, Bayesian Regression, Lasso and Elastic Net estimators computed with Least Angle Regression and coordinate descent. It also implements Stochastic Gradient Descent related algorithms.

**User guide:** See the Generalized Linear Models section for further details.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>linear_model.ARDRegression(n_iter, tol, ...)</code></td>
<td>Bayesian ARD regression.</td>
</tr>
<tr>
<td><code>linear_model.BayesianRidge(n_iter, tol, ...)</code></td>
<td>Bayesian ridge regression.</td>
</tr>
<tr>
<td><code>linear_model.ElasticNet(alpha, l1_ratio, ...)</code></td>
<td>Linear regression with combined L1 and L2 priors as regularizer.</td>
</tr>
<tr>
<td><code>linear_model.ElasticNetCV(Il1_ratio, eps, ...)</code></td>
<td>Elastic Net model with iterative fitting along a regularization path.</td>
</tr>
<tr>
<td><code>linear_model.HuberRegressor(epsilon, ...)</code></td>
<td>Linear regression model that is robust to outliers.</td>
</tr>
<tr>
<td><code>linear_model.Lars(fit_intercept, verbose, ...)</code></td>
<td>Least Angle Regression model a.k.a.</td>
</tr>
<tr>
<td><code>linear_model.LarsCV(fit_intercept, ...)</code></td>
<td>Cross-validated Least Angle Regression model</td>
</tr>
<tr>
<td><code>linear_model.Lasso(alpha, fit_intercept, ...)</code></td>
<td>Linear Model trained with L1 prior as regularizer (aka the Lasso)</td>
</tr>
<tr>
<td><code>linear_model.LassoCV(eps, n_alphas, ...)</code></td>
<td>Lasso linear model with iterative fitting along a regularization path.</td>
</tr>
<tr>
<td><code>linear_model.LassoLars(alpha, ...)</code></td>
<td>Lasso model fit with Least Angle Regression a.k.a.</td>
</tr>
<tr>
<td><code>linear_model.LassoLarsCV(fit_intercept, ...)</code></td>
<td>Cross-validated Lasso, using the LARS algorithm</td>
</tr>
<tr>
<td><code>linear_model.BayesianRidge(epsilon, ...)</code></td>
<td>Linear regression model that is robust to outliers.</td>
</tr>
<tr>
<td><code>linear_model.LinearRegression(...)</code></td>
<td>Ordinary least squares Linear Regression.</td>
</tr>
<tr>
<td><code>linear_model.LogisticRegression(penalty, ...)</code></td>
<td>Logistic Regression (aka logit, MaxEnt) classifier.</td>
</tr>
<tr>
<td><code>linear_model.LogisticRegressionCV(Cs, ...)</code></td>
<td>Logistic Regression CV (aka logit, MaxEnt) classifier.</td>
</tr>
<tr>
<td><code>linear_model.MultiTaskLasso(alpha, ...)</code></td>
<td>Multi-task Lasso model trained with L1/L2 mixed-norm as regularizer</td>
</tr>
<tr>
<td><code>linear_model.MultiTaskElasticNet(alpha, ...)</code></td>
<td>Multi-task ElasticNet model trained with L1/L2 mixed-norm as regularizer</td>
</tr>
<tr>
<td><code>linear_model.MultiTaskLassoCV(epsilon, ...)</code></td>
<td>Multi-task L1/L2 Lasso with built-in cross-validation.</td>
</tr>
<tr>
<td><code>linear_model.OrthogonalMatchingPursuit(...)</code></td>
<td>Orthogonal Matching Pursuit model (OMP)</td>
</tr>
<tr>
<td><code>linear_model.OrthogonalMatchingPursuitCV(...)</code></td>
<td>Cross-validated Orthogonal Matching Pursuit model (OMP)</td>
</tr>
<tr>
<td><code>linear_model.PassiveAggressiveClassifier(...)</code></td>
<td>Passive Aggressive Classifier</td>
</tr>
<tr>
<td><code>linear_model.PassiveAggressiveRegressor(...)</code></td>
<td>Passive Aggressive Regressor</td>
</tr>
<tr>
<td><code>linear_model.Perceptron(penalty, alpha, ...)</code></td>
<td>Read more in the User Guide.</td>
</tr>
<tr>
<td><code>linear_model.RANSACRegressor(...)</code></td>
<td>RANSAC (RAndom SAmple Consensus) algorithm.</td>
</tr>
<tr>
<td><code>linear_model.Ridge(alpha, fit_intercept, ...)</code></td>
<td>Linear least squares with l2 regularization.</td>
</tr>
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</table>
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<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>linear_model.RidgeClassifier</code></td>
<td>Classifier using Ridge regression.</td>
</tr>
<tr>
<td><code>linear_model.RidgeClassifierCV</code></td>
<td>Ridge classifier with built-in cross-validation.</td>
</tr>
<tr>
<td><code>linear_model.RidgeCV</code></td>
<td>Ridge regression with built-in cross-validation.</td>
</tr>
<tr>
<td><code>linear_model.SGDClassifier</code></td>
<td>Linear classifiers (SVM, logistic regression, a.o.) with SGD training.</td>
</tr>
<tr>
<td><code>linear_model.SGDRegressor</code></td>
<td>Linear model fitted by minimizing a regularized empirical loss with SGD</td>
</tr>
</tbody>
</table>

### 30.19.1 `sklearn.linear_model.ARDRegression`

**class** `sklearn.linear_model.ARDRegression` *(n_iter=300, tol=0.001, alpha_1=1e-06, alpha_2=1e-06, lambda_1=1e-06, lambda_2=1e-06, compute_score=False, threshold_lambda=10000.0, fit_intercept=True, normalize=False, copy_X=True, verbose=False)*

Bayesian ARD regression.

Fit the weights of a regression model, using an ARD prior. The weights of the regression model are assumed to be in Gaussian distributions. Also estimate the parameters lambda (precisions of the distributions of the weights) and alpha (precision of the distribution of the noise). The estimation is done by an iterative procedures (Evidence Maximization)

Read more in the [User Guide](#).

**Parameters**

- `n_iter` : int, optional

  Maximum number of iterations. Default is 300

- `tol` : float, optional

  Stop the algorithm if w has converged. Default is 1.e-3.

- `alpha_1` : float, optional

  Hyper-parameter : shape parameter for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.

- `alpha_2` : float, optional

  Hyper-parameter : inverse scale parameter (rate parameter) for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.

- `lambda_1` : float, optional

  Hyper-parameter : shape parameter for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.

- `lambda_2` : float, optional

  Hyper-parameter : inverse scale parameter (rate parameter) for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.

- `compute_score` : boolean, optional

  If True, compute the objective function at each step of the model. Default is False.

- `threshold_lambda` : float, optional
threshold for removing (pruning) weights with high precision from the computation. Default is 1.e+4.

**fit_intercept** : boolean, optional

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered). Default is True.

**normalize** : boolean, optional, default False

This parameter is ignored when `fit_intercept` is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use `sklearn.preprocessing.StandardScaler` before calling fit on an estimator with `normalize=False`.

**copy_X** : boolean, optional, default True.

If True, X will be copied; else, it may be overwritten.

**verbose** : boolean, optional, default False

Verbose mode when fitting the model.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape = (n_features)) Coefficients of the regression model (mean of distribution)</td>
</tr>
<tr>
<td>alpha_</td>
<td>(float) estimated precision of the noise.</td>
</tr>
<tr>
<td>lambda_</td>
<td>(array, shape = (n_features)) estimated precisions of the weights.</td>
</tr>
<tr>
<td>sigma_</td>
<td>(array, shape = (n_features, n_features)) estimated variance-covariance matrix of the weights</td>
</tr>
<tr>
<td>scores_</td>
<td>(float) if computed, value of the objective function (to be maximized)</td>
</tr>
</tbody>
</table>

**Notes**

For an example, see `examples/linear_model/plot_ard.py`.

**References**

D. J. C. MacKay, Bayesian nonlinear modeling for the prediction competition, ASHRAE Transactions, 1994.

R. Salakhutdinov, Lecture notes on Statistical Machine Learning, http://www.utstat.toronto.edu/~rsalakhut/sta4273/notes/Lecture2.pdf#page=15 Their beta is our `self.alpha_` Their alpha is our `self.lambda_` ARD is a little different than the slide: only dimensions/features for which `self.lambda_ < self.threshold_lambda` are kept and the rest are discarded.

**Examples**

```python
>>> from sklearn import linear_model
>>> clf = linear_model.ARDRegression()
>>> clf.fit([[0, 0], [1, 1], [2, 2]], [0, 1, 2])
```

...
Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y)</td>
<td>Fit the ARDRegression model according to the given training data and parameters.</td>
</tr>
<tr>
<td>get_params(deep)</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X, return_std)</td>
<td>Predict using the linear model.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(n_iter=300, tol=0.001, alpha_1=1e-06, alpha_2=1e-06, lambda_1=1e-06, lambda_2=1e-06, compute_score=False, threshold_lambda=10000.0, fit_intercept=True, normalize=False, copy_X=True, verbose=False)

fit(X, y)
Fit the ARDRegression model according to the given training data and parameters.

Iterative procedure to maximize the evidence

**Parameters**
- X: array-like, shape = [n_samples, n_features]  
  Training vector, where n_samples in the number of samples and n_features is the number of features.
- y: array, shape = [n_samples]  
  Target values (integers). Will be cast to X’s dtype if necessary

**Returns**
- self: returns an instance of self.

get_params(deep=True)
Get parameters for this estimator.

**Parameters**
- deep: boolean, optional  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- params: mapping of string to any  
  Parameter names mapped to their values.

predict(X, return_std=False)
Predict using the linear model.

In addition to the mean of the predictive distribution, also its standard deviation can be returned.

**Parameters**
- X: {array-like, sparse matrix}, shape = (n_samples, n_features)  
  Samples.
- return_std: boolean, optional  
  Whether to return the standard deviation of posterior prediction.

**Returns**
- y_mean: array, shape = (n_samples,)
Mean of predictive distribution of query points.

\( y_{\text{std}} \): array, shape = (n_samples,)

Standard deviation of predictive distribution of query points.

**score** \((X, y, \text{sample_weight=None})\)

Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \( (1 - \frac{u}{v}) \), where \( u \) is the residual sum of squares \( ((y_{\text{true}} - y_{\text{pred}})^2) \).sum() and \( v \) is the total sum of squares \( ((y_{\text{true}} - \text{y_true.mean()})^2) \).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

**Parameters**

\( X \): array-like, shape = (n_samples, n_features)

Test samples.

\( y \): array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for \( X \).

\( \text{sample_weight} \): array-like, shape = [n_samples], optional

Sample weights.

**Returns**

\( \text{score} \): float

\( R^2 \) of self.predict(\( X \)) wrt. \( y \).

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<component>__<parameter>\) so that it’s possible to update each component of a nested object.

**Sets**

\( \text{self} \)

---

**Examples using sklearn.linear_model.ARDRegression**

- **Automatic Relevance Determination Regression (ARD)**

**30.19.2 sklearn.linear_model.BayesianRidge**

**Class**

\( \text{sklearn.linear_model.BayesianRidge}(n_{\text{iter}}=300, tol=0.001, \text{alpha}_1=1e-06, \text{alpha}_2=1e-06, \text{lambda}_1=1e-06, \text{lambda}_2=1e-06, \text{compute_score}=\text{False}, \text{fit_intercept}=\text{True}, \text{normalize}=\text{False}, \text{copy_X}=\text{True}, \text{verbose}=\text{False}) \)

Bayesian ridge regression

Fit a Bayesian ridge model and optimize the regularization parameters lambda (precision of the weights) and alpha (precision of the noise).

Read more in the **User Guide**.

**Parameters**

\( \text{n_iter} \): int, optional

Maximum number of iterations. Default is 300.

\( \text{tol} \): float, optional

Stop the algorithm if \( w \) has converged. Default is 1.e-3.
alpha_1 : float, optional
    Hyper-parameter : shape parameter for the Gamma distribution prior over the alpha parameter. Default is 1.e-6

alpha_2 : float, optional
    Hyper-parameter : inverse scale parameter (rate parameter) for the Gamma distribution prior over the alpha parameter. Default is 1.e-6.

lambda_1 : float, optional
    Hyper-parameter : shape parameter for the Gamma distribution prior over the lambda parameter. Default is 1.e-6.

lambda_2 : float, optional
    Hyper-parameter : inverse scale parameter (rate parameter) for the Gamma distribution prior over the lambda parameter. Default is 1.e-6

compute_score : boolean, optional
    If True, compute the objective function at each step of the model. Default is False

fit_intercept : boolean, optional
    whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered). Default is True.

normalize : boolean, optional, default False
    This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

copy_X : boolean, optional, default True
    If True, X will be copied; else, it may be overwritten.

verbose : boolean, optional, default False
    Verbose mode when fitting the model.

Attributes

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<thead>
<tr>
<th></th>
<th>Description</th>
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<tbody>
<tr>
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<td>(array, shape = (n_features)) Coefficients of the regression model (mean of distribution)</td>
</tr>
<tr>
<td>alpha_</td>
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</tr>
<tr>
<td>lambda_</td>
<td>(float) estimated precision of the weights.</td>
</tr>
<tr>
<td>sigma_</td>
<td>(array, shape = (n_features, n_features)) estimated variance-covariance matrix of the weights</td>
</tr>
<tr>
<td>scores_</td>
<td>(float) if computed, value of the objective function (to be maximized)</td>
</tr>
</tbody>
</table>

Notes

For an example, see examples/linear_model/plot_bayesian_ridge.py.
References


R. Salakhutdinov. Lecture notes on Statistical Machine Learning, http://www.utstat.toronto.edu/~rsalakhu/sta4273/notes/Lecture2.pdf#page=15 Their beta is our self.alpha_ Their alpha is our self.lambda_

Examples

```
>>> from sklearn import linear_model
>>> clf = linear_model.BayesianRidge()
>>> clf.fit([[0,0], [1, 1], [2, 2]], [0, 1, 2])
... BayesianRidge(alpha_1=1e-06, alpha_2=1e-06, compute_score=False,
... copy_X=True, fit_intercept=True, lambda_1=1e-06, lambda_2=1e-06,
... n_iter=300, normalize=False, tol=0.001, verbose=False)
>>> clf.predict([[1, 1]])
array([[1.]])
```

Methods

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__init__(n_iter=300, tol=0.001, alpha_1=1e-06, alpha_2=1e-06, lambda_1=1e-06, lambda_2=1e-06, compute_score=False, fit_intercept=True, normalize=False, copy_X=True, verbose=False)

fit(X, y)

Fit the model

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  - Training data
- **y**: numpy array of shape [n_samples]
  - Target values. Will be cast to X’s dtype if necessary

**Returns**

- **self**: returns an instance of self.

get_params(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.
predict \( (X, \text{return\_std}=False) \)
Predict using the linear model.
In addition to the mean of the predictive distribution, also its standard deviation can be returned.

**Parameters**

- **X** : {array-like, sparse matrix}, shape = (n_samples, n_features)
  Samples.
- **return\_std** : boolean, optional
  Whether to return the standard deviation of posterior prediction.

**Returns**

- **y\_mean** : array, shape = (n_samples,)
  Mean of predictive distribution of query points.
- **y\_std** : array, shape = (n_samples,)
  Standard deviation of predictive distribution of query points.

score \( (X, y, \text{sample\_weight}=\text{None}) \)
Returns the coefficient of determination \( R^2 \) of the prediction.
The coefficient \( R^2 \) is defined as \( (1 - u/v) \), where \( u \) is the residual sum of squares \( ((y\_true - y\_pred) ** 2).sum() \) and \( v \) is the total sum of squares \( ((y\_true - y\_true\_mean) ** 2).sum() \). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

**Parameters**

- **X** : array-like, shape = (n_samples, n_features)
  Test samples.
- **y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.
- **sample\_weight** : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- **score** : float
  \( R^2 \) of self.predict(X) wrt. \( y \).

set_params (**params**)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns**

- **self**

Examples using sklearn.linear_model.BayesianRidge

- Feature agglomeration vs. univariate selection
- Bayesian Ridge Regression
30.19.3 sklearn.linear_model.ElasticNet

class sklearn.linear_model.ElasticNet (alpha=1.0, l1_ratio=0.5, fit_intercept=True, normalize=False, precompute=False, max_iter=1000, copy_X=True, tol=0.0001, warm_start=False, positive=False, random_state=None, selection='cyclic')

Linear regression with combined L1 and L2 priors as regularizer.

Minimizes the objective function:

\[
1 / (2 \times n_{\text{samples}}) \times ||y - Xw||^2_2 \\
+ \alpha \times l1_{\text{ratio}} \times ||w||_1 \\
+ 0.5 \times \alpha \times (1 - l1_{\text{ratio}}) \times ||w||^2_2
\]

If you are interested in controlling the L1 and L2 penalty separately, keep in mind that this is equivalent to:

\[
a \times L1 + b \times L2
\]

where:

\[
\alpha = a + b \quad \text{and} \quad l1_{\text{ratio}} = a / (a + b)
\]

The parameter l1_ratio corresponds to alpha in the glmnet R package while alpha corresponds to the lambda parameter in glmnet. Specifically, l1_ratio = 1 is the lasso penalty. Currently, l1_ratio <= 0.01 is not reliable, unless you supply your own sequence of alpha.

Read more in the User Guide.

Parameters

- **alpha** : float, optional

  Constant that multiplies the penalty terms. Defaults to 1.0. See the notes for the exact mathematical meaning of this parameter. \(\alpha = 0\) is equivalent to an ordinary least square, solved by the LinearRegression object. For numerical reasons, using \(\alpha = 0\) with the Lasso object is not advised. Given this, you should use the LinearRegression object.

- **l1_ratio** : float

  The ElasticNet mixing parameter, with \(0 \leq l1_{\text{ratio}} \leq 1\). For \(l1_{\text{ratio}} = 0\) the penalty is an L2 penalty. For \(l1_{\text{ratio}} = 1\) it is an L1 penalty. For \(0 < l1_{\text{ratio}} < 1\), the penalty is a combination of L1 and L2.

- **fit_intercept** : bool

  Whether the intercept should be estimated or not. If False, the data is assumed to be already centered.

- **normalize** : boolean, optional, default False

  This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

- **precompute** : True | False | array-like

  Whether to use a precomputed Gram matrix to speed up calculations. The Gram matrix can also be passed as argument. For sparse input this option is always True to preserve sparsity.

- **max_iter** : int, optional
The maximum number of iterations

**copy_X** : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**tol** : float, optional

The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.

**warm_start** : bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**positive** : bool, optional

When set to True, forces the coefficients to be positive.

**random_state** : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’.

**selection** : str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’) often leads to significantly faster convergence especially when tol is higher than 1e-4.

**Attributes**

| sparse_coef_ | sparse representation of the fitted **coef** |

| **coef** | (array, shape (n_features,) | (n_targets, n_features)) parameter vector (w in the cost function formula) |
| **intercept** | (float | array, shape (n_targets,)) independent term in decision function. |
| **n_iter** | (array-like, shape (n_targets,)) number of iterations run by the coordinate descent solver to reach the specified tolerance. |

**See also:**

- **ElasticNetCV** Elastic net model with best model selection by cross-validation.
- **SGDRegressor** implements elastic net regression with incremental training.
- **SGDClassifier** implements logistic regression with elastic net penalty (SGDClassifier(loss="log", penalty="elasticnet").)
Notes

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Examples

```python
>>> from sklearn.linear_model import ElasticNet
>>> from sklearn.datasets import make_regression

>>> X, y = make_regression(n_features=2, random_state=0)
>>> regr = ElasticNet(random_state=0)
>>> regr.fit(X, y)
ElasticNet(alpha=1.0, copy_X=True, fit_intercept=True, l1_ratio=0.5,
           max_iter=1000, normalize=False, positive=False, precompute=False,
           random_state=0, selection='cyclic', tol=0.0001, warm_start=False)

>>> print(regr.coef_)
[ 18.83816048  64.55968825]
>>> print(regr.intercept_)
1.45126075617
>>> print(regr.predict([[0, 0]]))
[ 1.45126076]
```

Methods

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<td>fit(X, y, check_input]</td>
<td>Fit model with coordinate descent.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
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<tr>
<td>path(X, y[, l1_ratio, eps, n_alphas, ...])</td>
<td>Compute elastic net path with coordinate descent</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R**2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
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</table>

```python
__init__(alpha=1.0, l1_ratio=0.5, fit_intercept=True, normalize=False, precompute=False,
         max_iter=1000, copy_X=True, tol=0.0001, warm_start=False, positive=False,
         random_state=None, selection='cyclic')
```

```python
fit(X, y, check_input=True)
```

Fit model with coordinate descent.

**Parameters**

- X : ndarray or scipy.sparse matrix, (n_samples, n_features)
  
  Data

- y : ndarray, shape (n_samples,) or (n_samples, n_targets)
  
  Target. Will be cast to X’s dtype if necessary

- check_input : boolean, (default=True)
  
  Allow to bypass several input checking. Don’t use this parameter unless you know what you do.
Notes

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

static path (X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto',
Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)
Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{(2 \times n_{samples})} \times ||y - Xw||^2_2 \\
+ \alpha l_1 \text{ratio} \times ||w||_1 \\
+ 0.5 \times \alpha (1 - l_1 \text{ratio}) \times ||w||^2_2
\]

For multi-output tasks it is:

\[
\frac{1}{(2 \times n_{samples})} \times ||Y - XW||_{\text{Fro}}^2 \\
+ \alpha l_1 \text{ratio} \times ||W||_{21} \\
+ 0.5 \times \alpha (1 - l_1 \text{ratio}) \times ||W||_{\text{Fro}}^2
\]

Where:

\[||W||_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}\]

i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters X : {array-like}, shape (n_samples, n_features)

Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

y : ndarray, shape (n_samples,) or (n_samples, n_outputs)

Target values

l1_ratio : float, optional

float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1_ratio=0 corresponds to the Lasso

eps : float

Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3
n_alphas : int, optional
    Number of alphas along the regularization path

alphas : ndarray, optional
    List of alphas where to compute the models. If None alphas are set automatically

precompute : True | False | ‘auto’ | array-like
    Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto'
    let us decide. The Gram matrix can also be passed as argument.

Xy : array-like, optional
    Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is
    precomputed.

copy_X : boolean, optional, default True
    If True, X will be copied; else, it may be overwritten.

coeff_init : array, shape (n_features,) | None
    The initial values of the coefficients.

verbose : bool or integer
    Amount of verbosity.

return_n_iter : bool
    whether to return the number of iterations or not.

positive : bool, default False
    If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

check_input : bool, default True
    Skip input validation checks, including the Gram matrix when provided assuming there
    are handled by the caller when check_input=False.

**params : kwargs
    keyword arguments passed to the coordinate descent solver.

Returns

alphas : array, shape (n_alphas,)
    The alphas along the path where models are computed.

coeffs : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)
    Coefficients along the path.

dual_gaps : array, shape (n_alphas,)
    The dual gaps at the end of the optimization for each alpha.

n_iters : array-like, shape (n_alphas,)
    The number of iterations taken by the coordinate descent optimizer to reach the specified
    tolerance for each alpha. (Is returned when return_n_iter is set to True).

See also:

MultiTaskElasticNet, MultiTaskElasticNetCV, ElasticNet, ElasticNetCV
Notes

For an example, see examples/linear_model/plot_lasso_coordinate_descent_path.py.

predict(X)

Predict using the linear model

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

Returns C : array, shape = (n_samples,)

Returns predicted values.

score(X, y, sample_weight=None)

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) **
2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score
is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always
predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

Returns score : float

R^2 of self.predict(X) wrt. y.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns self

sparse_coef_

sparse representation of the fitted coef_

Examples using sklearn.linear_model.ElasticNet

• Lasso and Elastic Net for Sparse Signals
• Train error vs Test error

30.19.4 sklearn.linear_model.HuberRegressor

class sklearn.linear_model.HuberRegressor(epsilon=1.35, max_iter=100, alpha=0.0001,
warm_start=False, fit_intercept=True, tol=1e-05)

Linear regression model that is robust to outliers.
The Huber Regressor optimizes the squared loss for the samples where \(|(y - X'w) / \sigma| < \varepsilon\) and the absolute loss for the samples where \(|(y - X'w) / \sigma| > \varepsilon\), where \(w\) and \(\sigma\) are parameters to be optimized. The parameter \(\sigma\) makes sure that if \(y\) is scaled up or down by a certain factor, one does not need to rescale \(\varepsilon\) to achieve the same robustness. Note that this does not take into account the fact that the different features of \(X\) may be of different scales.

This makes sure that the loss function is not heavily influenced by the outliers while not completely ignoring their effect.

Read more in the User Guide

New in version 0.18.

Parameters epsilon : float, greater than 1.0, default 1.35

The parameter epsilon controls the number of samples that should be classified as outliers. The smaller the epsilon, the more robust it is to outliers.

max_iter : int, default 100

Maximum number of iterations that scipy.optimize.fmin_l_bfgs_b should run for.

alpha : float, default 0.0001

Regularization parameter.

warm_start : bool, default False

This is useful if the stored attributes of a previously used model has to be reused. If set to False, then the coefficients will be rewritten for every call to fit.

fit_intercept : bool, default True

Whether or not to fit the intercept. This can be set to False if the data is already centered around the origin.

tol : float, default 1e-5

The iteration will stop when \(\max\{|\text{proj g}_i| \mid i = 1, \ldots, n\} \leq \text{tol}\) where \(\text{pg}_i\) is the \(i\)-th component of the projected gradient.

Attributes

| coef_     | (array, shape (n_features,)) Features got by optimizing the Huber loss. |
| intercept_| (float) Bias. |
| scale_    | (float) The value by which \(|y - X'w - c|\) is scaled down. |
| n_iter_   | (int) Number of iterations that fmin_l_bfgs_b has run for. Not available if SciPy version is 0.9 and below. |
| outliers_ | (array, shape (n_samples,)) A boolean mask which is set to True where the samples are identified as outliers. |

References

[R105106], [R106106]
Methods

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<td>Fit the model according to the given training data.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
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<td>predict(X)</td>
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<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
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</table>

`__init__` (epsilon=1.35, max_iter=100, alpha=0.0001, warm_start=False, fit_intercept=True, tol=1e-05)

`fit (X, y, sample_weight=None)`
Fit the model according to the given training data.

**Parameters**
- X: array-like, shape (n_samples, n_features)
  Training vector, where n_samples in the number of samples and n_features is the number of features.
- y: array-like, shape (n_samples,)
  Target vector relative to X.
- sample_weight: array-like, shape (n_samples,)
  Weight given to each sample.

**Returns**
- self: object
  Returns self.

`get_params (deep=True)`
Get parameters for this estimator.

**Parameters**
- deep: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- params: mapping of string to any
  Parameter names mapped to their values.

`predict (X)`
Predict using the linear model

**Parameters**
- X: {array-like, sparse matrix}, shape = (n_samples, n_features)
  Samples.

**Returns**
- C: array, shape = (n_samples,)
  Returns predicted values.

`score (X, y, sample_weight=None)`
Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_true - y_pred)^{**2}).sum()$ and $v$ is the total sum of squares $((y_true - y_true.mean())^{**2}).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.
**Parameters**

* X : array-like, shape = (n_samples, n_features)
  Test samples.

* y : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for X.

* sample_weight : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

* score : float
  \( R^2 \) of self.predict(X) wrt. y.

**set_params**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

* self

**Examples using sklearn.linear_model.HuberRegressor**

- *HuberRegressor vs Ridge on dataset with strong outliers*
- *Robust linear estimator fitting*

### 30.19.5 sklearn.linear_model.Lars

**class** sklearn.linear_model.Lars

*fit_intercept=True, verbose=False, normalize=True, precompute='auto', n_nonzero_coefs=500, eps=2.2204460492503131e-16, copy_X=True, fit_path=True, positive=False*

Least Angle Regression model a.k.a. LAR

Read more in the *User Guide.*

**Parameters**

* fit_intercept : boolean
  Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

* verbose : boolean or integer, optional
  Sets the verbosity amount

* normalize : boolean, optional, default True
  This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

* precompute : True | False | 'auto' | array-like
  Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

* n_nonzero_coefs : int, optional
  Target number of non-zero coefficients. Use np.inf for no limit.
eps : float, optional
    The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the tol parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.

copy_X : boolean, optional, default True
    If True, X will be copied; else, it may be overwritten.

fit_path : boolean
    If True the full path is stored in the coef_path_ attribute. If you compute the solution for a large problem or many targets, setting fit_path to False will lead to a speedup, especially with a small alpha.

positive : boolean (default=False)
    Restrict coefficients to be >= 0. Be aware that you might want to remove fit_intercept which is set True by default.

Attributes

| alphphas_ | (array, shape (n_alphas + 1) | list of n_targets such arrays) Maximum of covariances (in absolute value) at each iteration. n_alphas is either n_nonzero_coefs or n_features, whichever is smaller. |
| active_ | (list, length = n_alphas | list of n_targets such lists) Indices of active variables at the end of the path. |
| coef_path_ | (array, shape (n_features, n_alphas + 1) | list of n_targets such arrays) The varying values of the coefficients along the path. It is not present if the fit_path parameter is False. |
| coef_ | (array, shape (n_features,) or (n_targets, n_features)) Parameter vector (w in the formulation formula). |
| intercept_ | (float | array, shape (n_targets,)) Independent term in decision function. |
| n_iter_ | (array-like or int) The number of iterations taken by lars_path to find the grid of alphas for each target. |

See also:

larss_path, LarsCV, sklearn.decomposition.sparse_encode

Examples

```python
>>> from sklearn import linear_model
>>> reg = linear_model.Lars(n_nonzero_coefs=1)
>>> reg.fit([[1, 0, 0], [0, 1, 0], [0, 0, 1]], [-1.1111, 0, -1.1111])
... Lars(copy_X=True, eps=..., fit_intercept=True, fit_path=True,
... n_nonzero_coefs=1, normalize=True, positive=False, precompute='auto',
... verbose=False)
>>> print(reg.coef_)
[0. -1.11...]
```
### Methods

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<td><strong>fit</strong>(X, y[, Xy])</td>
<td>Fit the model using X, y as training data.</td>
</tr>
<tr>
<td><strong>get_params</strong>(deep)</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><strong>predict</strong>(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td><strong>score</strong>(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td><strong>set_params</strong>(<strong>params</strong>)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

#### __init__ (fit_intercept=True, verbose=False, normalize=True, precompute='auto', n_nonzero_coefs=500, eps=2.2204460492503131e-16, copy_X=True, fit_path=True, positive=False)

**fit**(X, y, Xy=None)

Fit the model using X, y as training data.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  - Training data.
- **y**: array-like, shape (n_samples,) or (n_samples, n_targets)
  - Target values.
- **Xy**: array-like, shape (n_samples,) or (n_samples, n_targets), optional
  - $Xy = \text{np.dot}(X.T, y)$ that can be precomputed. It is useful only when the Gram matrix is precomputed.

**Returns**

- **self**: object
  - returns an instance of self.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**predict**(X)

Predict using the linear model

**Parameters**

- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Samples.

**Returns**

- **C**: array, shape = (n_samples,)
  - Returns predicted values.

**score**(X, y, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred}) ** 2).\text{sum()}$ and $v$ is the total sum of squares $((y_{true} - y_{true}.\text{mean()}) ** 2).\text{sum()}$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.
Parameters X: array-like, shape = (n_samples, n_features)

Test samples.

y: array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight: array-like, shape = [n_samples], optional

Sample weights.

Returns score: float

R^2 of self.predict(X) wrt. y.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

30.19.6 sklearn.linear_model.Lasso

class sklearn.linear_model.Lasso(alpha=1.0, fit_intercept=True, normalize=False, precompute=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, positive=False, random_state=None, selection='cyclic')

Linear Model trained with L1 prior as regularizer (aka the Lasso)

The optimization objective for Lasso is:

\[
\frac{1}{(2 \times n_samples)} \times ||y - Xw||^2_2 + \alpha \times ||w||_1
\]

Technically the Lasso model is optimizing the same objective function as the Elastic Net with l1_ratio=1.0 (no L2 penalty).

Read more in the User Guide.

Parameters alpha: float, optional

Constant that multiplies the L1 term. Defaults to 1.0. alpha = 0 is equivalent to an ordinary least square, solved by the LinearRegression object. For numerical reasons, using alpha = 0 with the Lasso object is not advised. Given this, you should use the LinearRegression object.

fit_intercept: boolean

whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize: boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing. StandardScaler before calling fit on an estimator with normalize=False.

precompute: True | False | array-like, default=False
Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument. For sparse input this option is always True to preserve sparsity.

**copy_X** : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**max_iter** : int, optional

The maximum number of iterations

**tol** : float, optional

The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.

**warm_start** : bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**positive** : bool, optional

When set to True, forces the coefficients to be positive.

**random_state** : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == 'random'.

**selection** : str, default 'cyclic'

If set to 'random', a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to 'random') often leads to significantly faster convergence especially when tol is higher than 1e-4.

### Attributes

**sparse_coef_**

sparse representation of the fitted coef_

<table>
<thead>
<tr>
<th>coef_</th>
<th>(array, shape (n_features,)</th>
<th>l (n_targets, n_features)) parameter vector (w in the cost function formula)</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(float l array, shape (n_targets,)) independent term in decision function.</td>
<td></td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int l array-like, shape (n_targets,)) number of iterations run by the coordinate descent solver to reach the specified tolerance.</td>
<td></td>
</tr>
</tbody>
</table>

See also:

lars_path, lasso_path, LassoLars, LassoCV, LassoLarsCV, sklearn.decomposition. sparse_encode
Notes

The algorithm used to fit the model is coordinate descent.
To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Examples

```python
>>> from sklearn import linear_model
>>> clf = linear_model.Lasso(alpha=0.1)
>>> clf.fit([[0,0], [1, 1], [2, 2]], [0, 1, 2])
Lasso(alpha=0.1, copy_X=True, fit_intercept=True, max_iter=1000,
     normalize=False, positive=False, precompute=False, random_state=None,
     selection='cyclic', tol=0.0001, warm_start=False)
>>> print(clf.coef_)
[ 0.85 0. ]
>>> print(clf.intercept_)
0.15
```

Methods

- `fit(X, y[, check_input])` Fit model with coordinate descent.
- `get_params([deep])` Get parameters for this estimator.
- `path(X, y[, l1_ratio, eps, n_alphas, ...])` Compute elastic net path with coordinate descent
- `predict(X)` Predict using the linear model
- `score(X, y[, sample_weight])` Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)` Set the parameters of this estimator.

```python
def __init__(alpha=1.0, fit_intercept=True, normalize=False, precompute=False, copy_X=True,
             max_iter=1000, tol=0.0001, warm_start=False, positive=False, random_state=None,
             selection='cyclic')

fit(X, y[, check_input=True])

Fit model with coordinate descent.

Parameters

- **X**: ndarray or scipy.sparse matrix; (n_samples, n_features)
  Data
- **y**: ndarray, shape (n_samples,) or (n_samples, n_targets)
  Target. Will be cast to X’s dtype if necessary
- **check_input**: boolean, (default=True)
  Allow to bypass several input checking. Don’t use this parameter unless you know what
  you do.

Notes

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.
To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

**get_params**(deep=True)
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  Parameter names mapped to their values.

**static path**(X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)
Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{(2 \times \text{n\_samples})} \times ||y - Xw||^2_2 + \alpha \times l1\_ratio \times ||w||_1 + 0.5 \times \alpha \times (1 - l1\_ratio) \times ||w||^2_2
\]

For multi-output tasks it is:

\[
\frac{1}{(2 \times \text{n\_samples})} \times ||Y - XW||_{\text{Fro}}^2 + \alpha \times l1\_ratio \times ||W||_21 + 0.5 \times \alpha \times (1 - l1\_ratio) \times ||W||_{\text{Fro}}^2
\]

Where:

\[
||W||_21 = \sum_i \sqrt{\sum_j w_{ij}^2}
\]
i.e. the sum of norm of each row.

Read more in the User Guide.

**Parameters**
- **X**: array-like, shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- **y**: ndarray, shape (n_samples,) or (n_samples, n_outputs)
  Target values
- **l1_ratio**: float, optional
  float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1_ratio=1 corresponds to the Lasso
- **eps**: float
  Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3
- **n_alphas**: int, optional
  Number of alphas along the regularization path
- **alphas**: ndarray, optional
  List of alphas where to compute the models. If None alphas are set automatically
**precompute** : True | False | 'auto' | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

**Xy** : array-like, optional

Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

**copy_X** : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**coef_init** : array, shape (n_features,) | None

The initial values of the coefficients.

**verbose** : bool or integer

Amount of verbosity.

**return_n_iter** : bool

whether to return the number of iterations or not.

**positive** : bool, default False

If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check_input** : bool, default True

Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params** : kwargs

keyword arguments passed to the coordinate descent solver.

**Returns**

**alphas** : array, shape (n_alphas,)

The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iters** : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

See also:

`MultiTaskElasticNet`, `MultiTaskElasticNetCV`, `ElasticNet`, `ElasticNetCV`

**Notes**

For an example, see `examples/linear_model/plot_lasso_coordinate_descent_path.py`.

**predict** *(X)*

Predict using the linear model
Parameters X: {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.
Returns C: array, shape = (n_samples,)
Returns predicted values.
score (X, y, sample_weight=None)
Returns the coefficient of determination $R^2$ of the prediction.
The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares ($(y_{true} - y_{pred})^2$).sum() and $v$ is the total sum of squares ($(y_{true} - y_{true}.mean())^2$).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.
Parameters X: array-like, shape = (n_samples, n_features)
Test samples.
y: array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.
sample_weight: array-like, shape = [n_samples], optional
Sample weights.
Returns score: float
$R^2$ of self.predict(X) wrt. y.
set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.
Returns self
sparse_coef_
sparse representation of the fitted coef_

Examples using sklearn.linear_model.Lasso

- Compressive sensing: tomography reconstruction with L1 prior (Lasso)
- Cross-validation on diabetes Dataset Exercise
- Lasso on dense and sparse data
- Joint feature selection with multi-task Lasso
- Lasso and Elastic Net for Sparse Signals

30.19.7 sklearn.linear_model.LassoLars

class sklearn.linear_model.LassoLars (alpha=1.0, fit_intercept=True, verbose=False, normalize=True, precompute='auto', max_iter=500, eps=2.2204460492503131e-16, copy_X=True, fit_path=True, positive=False)

Lasso model fit with Least Angle Regression a.k.a. Lars
It is a Linear Model trained with an L1 prior as regularizer.

The optimization objective for Lasso is:

\[
(\frac{1}{(2 \times n_{\text{samples}})}) \times \|y - Xw\|^2_2 + \alpha \times \|w\|_1
\]

Read more in the User Guide.

**Parameters**

- **alpha** : float
  
  Constant that multiplies the penalty term. Defaults to 1.0. alpha = 0 is equivalent to an ordinary least square, solved by LinearRegression. For numerical reasons, using alpha = 0 with the LassoLars object is not advised and you should prefer the LinearRegression object.

- **fit_intercept** : boolean
  
  Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

- **verbose** : boolean or integer, optional
  
  Sets the verbosity amount

- **normalize** : boolean, optional, default True
  
  This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

- **precompute** : True | False | ‘auto’ | array-like
  
  Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

- **max_iter** : integer, optional
  
  Maximum number of iterations to perform.

- **eps** : float, optional
  
  The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the tol parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.

- **copy_X** : boolean, optional, default True
  
  If True, X will be copied; else, it may be overwritten.

- **fit_path** : boolean
  
  If True the full path is stored in the coef_path_ attribute. If you compute the solution for a large problem or many targets, setting fit_path to False will lead to a speedup, especially with a small alpha.

- **positive** : boolean (default=False)
  
  Restrict coefficients to be >= 0. Be aware that you might want to remove fit_intercept which is set True by default. Under the positive restriction the model coefficients will not converge to the ordinary-least-squares solution for small values of alpha. Only coefficients up to the smallest alpha value (alphas_[alphas_ > 0.].min() when fit_path=True) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent Lasso estimator.
Attributes

- `alphas_`: (array, shape (n_alphas + 1) | list of n_targets such arrays) Maximum of covariances (in absolute value) at each iteration. n_alphas is either max_iter, n_features, or the number of nodes in the path with correlation greater than alpha, whichever is smaller.
- `active_`: (list, length = n_alphas | list of n_targets such lists) Indices of active variables at the end of the path.
- `coef_path_`: (array, shape (n_features, n_alphas + 1) or list) If a list is passed it's expected to be one of n_targets such arrays. The varying values of the coefficients along the path. It is not present if the fit_path parameter is False.
- `coef_`: (array, shape (n_features,) or (n_targets, n_features)) Parameter vector (w in the formulation formula).
- `intercept_`: (float | array, shape (n_targets,)) Independent term in decision function.
- `n_iter_`: (array-like or int.) The number of iterations taken by lars_path to find the grid of alphas for each target.

See also:

lars_path, lasso_path, Lasso, LassoCV, LassoLarsCV, LassoLarsIC, sklearn.decomposition.sparse_encode

Examples

```python
>>> from sklearn import linear_model
>>> reg = linear_model.LassoLars(alpha=0.01)
>>> reg.fit([[-1, 1], [0, 0], [1, 1]], [-1, 0, -1])
... LassoLars(alpha=0.01, copy_X=True, eps=..., fit_intercept=True,
             fit_path=True, max_iter=500, normalize=True, positive=False,
             precompute='auto', verbose=False)
>>> print(reg.coef_)
[ 0. -0.963257...]
```

Methods

- `fit(X, y[, Xy])`: Fit the model using X, y as training data.
- `get_params([deep])`: Get parameters for this estimator.
- `predict(X)`: Predict using the linear model.
- `score(X, y[, sample_weight])`: Returns the coefficient of determination R^2 of the prediction.
- `set_params(**params)`: Set the parameters of this estimator.

```python
>>> __init__(alpha=1.0, fit_intercept=True, verbose=False, normalize=True, precompute='auto',
             max_iter=500, eps=2.2204460492503131e-16, copy_X=True, fit_path=True, posi-
tive=False)
```

```python
>>> fit(X, y, Xy=None)
Fit the model using X, y as training data.
```
Parameters X: array-like, shape (n_samples, n_features)
   Training data.

y: array-like, shape (n_samples, ) or (n_samples, n_targets)
   Target values.

Xy: array-like, shape (n_samples, ) or (n_samples, n_targets), optional
   Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is
   precomputed.

Returns self: object
   returns an instance of self.

get_params (deep=True)
   Get parameters for this estimator.

   Parameters deep: boolean, optional
      If True, will return the parameters for this estimator and contained subobjects that are
      estimators.

   Returns params: mapping of string to any
      Parameter names mapped to their values.

predict (X)
   Predict using the linear model

   Parameters X: {array-like, sparse matrix}, shape = (n_samples, n_features)
      Samples.

   Returns C: array, shape = (n_samples,)
      Returns predicted values.

score (X, y, sample_weight=None)
   Returns the coefficient of determination R^2 of the prediction.

   The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) **
   2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score
   is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always
   predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

   Parameters X: array-like, shape = (n_samples, n_features)
      Test samples.

   y: array-like, shape = (n_samples) or (n_samples, n_outputs)
      True values for X.

   sample_weight: array-like, shape = [n_samples], optional
      Sample weights.

   Returns score: float
      R^2 of self.predict(X) wrt. y.

set_params (**params)
   Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

30.19.8 sklearn.linear_model.LinearRegression

class sklearn.linear_model.LinearRegression (fit_intercept=True, 
normalize=False, 
copy_X=True, n_jobs=1)

Ordinary least squares Linear Regression.

Parameters

fit_intercept : boolean, optional, default True

Whether to calculate the intercept for this model. If set to False, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

copy_X : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

n_jobs : int, optional, default 1

The number of jobs to use for the computation. If -1 all CPUs are used. This will only provide speedup for n_targets > 1 and sufficient large problems.

Attributes

<table>
<thead>
<tr>
<th><strong>coef</strong></th>
<th>(array, shape (n_features,) or (n_targets, n_features)) Estimated coefficients for the linear regression problem. If multiple targets are passed during the fit (y 2D), this is a 2D array of shape (n_targets, n_features), while if only one target is passed, this is a 1D array of length n_features.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>intercept</strong></td>
<td>(array) Independent term in the linear model.</td>
</tr>
</tbody>
</table>

Notes

From the implementation point of view, this is just plain Ordinary Least Squares (scipy.linalg.lstsq) wrapped as a predictor object.

Methods

| **fit**(X, y[, sample_weight]) | Fit linear model. |
| **get_params**(deep) | Get parameters for this estimator. |
| **predict**(X) | Predict using the linear model |

Continued on next page
Table 30.176 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**init** (fit_intercept=True, normalize=False, copy_X=True, n_jobs=1)

**fit** (X, y, sample_weight=None)
Fit linear model.

**Parameters**
- **X**: numpy array or sparse matrix of shape [n_samples, n_features]
  - Training data
- **y**: numpy array of shape [n_samples, n_targets]
  - Target values. Will be cast to X's dtype if necessary
- **sample_weight**: numpy array of shape [n_samples]
  - Individual weights for each sample
  - New in version 0.17: parameter sample_weight support to LinearRegression.

**Returns**
- **self**: returns an instance of self.

**get_params**(deep=True)
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  - Parameter names mapped to their values.

**predict**(X)
Predict using the linear model

**Parameters**
- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Samples.

**Returns**
- **C**: array, shape = (n_samples,)
  - Returns predicted values.

**score**(X, y, sample_weight=None)
Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares \(((y_{true} - y_{pred}) ** 2).sum()\) and $v$ is the total sum of squares \(((y_{true} - y_{true.mean()}) ** 2).sum()\). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**
- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True values for X.
- **sample_weight**: array-like, shape = [n_samples], optional
Sample weights.

**Returns**

-score : float

R^2 of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

**Returns**

self

**Examples using sklearn.linear_model.LogisticRegression**

- Plotting Cross-Validated Predictions
- Isotonic Regression
- Face completion with a multi-output estimators
- Ordinary Least Squares and Ridge Regression Variance
- Logistic function
- Linear Regression Example
- Robust linear model estimation using RANSAC
- Sparsity Example: Fitting only features 1 and 2
- Theil-Sen Regression
- Robust linear estimator fitting
- Automatic Relevance Determination Regression (ARD)
- Bayesian Ridge Regression
- Underfitting vs. Overfitting

**30.19.9 sklearn.linear_model.LogisticRegression**

```python
class sklearn.linear_model.LogisticRegression(penalty='l2', dual=False, tol=0.0001, C=1.0, fit_intercept=True, intercept_scaling=1, class_weight=None, random_state=None, solver='liblinear', max_iter=100, multi_class='ovr', verbose=0, warm_start=False, n_jobs=1)
```

Logistic Regression (aka logit, MaxEnt) classifier.

In the multiclass case, the training algorithm uses the one-vs-rest (OvR) scheme if the ‘multi_class’ option is set to ‘ovr’, and uses the cross-entropy loss if the ‘multi_class’ option is set to ‘multinomial’. (Currently the ‘multinomial’ option is supported only by the ‘lbfgs’, ‘sag’ and ‘newton-cg’ solvers.)

This class implements regularized logistic regression using the ‘liblinear’ library, ‘newton-cg’, ‘sag’ and ‘lbfgs’ solvers. It can handle both dense and sparse input. Use C-ordered arrays or CSR matrices containing 64-bit floats for optimal performance; any other input format will be converted (and copied).

The ‘newton-cg’, ‘sag’, and ‘lbfgs’ solvers support only L2 regularization with primal formulation. The ‘liblinear’ solver supports both L1 and L2 regularization, with a dual formulation only for the L2 penalty.
Read more in the User Guide.

Parameters

penalty : str, ‘l1’ or ‘l2’, default: ‘l2’

Used to specify the norm used in the penalization. The ‘newton-cg’, ‘sag’ and ‘lbfgs’ solvers support only l2 penalties.

New in version 0.19: l1 penalty with SAGA solver (allowing ‘multinomial’ + L1)

dual : bool, default: False

Dual or primal formulation. Dual formulation is only implemented for l2 penalty with liblinear solver. Prefer dual=False when n_samples > n_features.

tol : float, default: 1e-4

Tolerance for stopping criteria.

C : float, default: 1.0

Inverse of regularization strength; must be a positive float. Like in support vector machines, smaller values specify stronger regularization.

fit_intercept : bool, default: True

Specifies if a constant (a.k.a. bias or intercept) should be added to the decision function.

intercept_scaling : float, default 1.

Useful only when the solver ‘liblinear’ is used and self.fit_intercept is set to True. In this case, x becomes [x, self.intercept_scaling], i.e. a “synthetic” feature with constant value equal to intercept_scaling is appended to the instance vector. The intercept becomes intercept_scaling * synthetic_feature_weight.

Note! the synthetic feature weight is subject to l1/l2 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept_scaling has to be increased.

class_weight : dict or ‘balanced’, default: None

Weights associated with classes in the form {class_label: weight}. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as n_samples / (n_classes * np.bincount(y)).

Note that these weights will be multiplied with sample_weight (passed through the fit method) if sample_weight is specified.

New in version 0.17: class_weight=’balanced’

random_state : int, RandomState instance or None, optional, default: None

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == ‘sag’ or ‘liblinear’.


default: ‘liblinear’ Algorithm to use in the optimization problem.

• For small datasets, ‘liblinear’ is a good choice, whereas ‘sag’ and ‘saga’ are faster for large ones.
- For multiclass problems, only ‘newton-cg’, ‘sag’, ‘saga’ and ‘lbfgs’ handle multinomial loss; ‘liblinear’ is limited to one-versus-rest schemes.

- ‘newton-cg’, ‘lbfgs’ and ‘sag’ only handle L2 penalty, whereas ‘liblinear’ and ‘saga’ handle L1 penalty.

Note that ‘sag’ and ‘saga’ fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

**max_iter**: int, default: 100

Useful only for the newton-cg, sag and lbfgs solvers. Maximum number of iterations taken for the solvers to converge.

**multi_class**: str, {'ovr', 'multinomial'}, default: 'ovr'

Multiclass option can be either ‘ovr’ or ‘multinomial’. If the option chosen is ‘ovr’, then a binary problem is fit for each label. Else the loss minimised is the multinomial loss fit across the entire probability distribution. Does not work for liblinear solver.

New in version 0.18: Stochastic Average Gradient descent solver for ‘multinomial’ case.

**verbose**: int, default: 0

For the liblinear and lbfgs solvers set verbose to any positive number for verbosity.

**warm_start**: bool, default: False

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution. Useless for liblinear solver.

New in version 0.17: warm_start to support lbfgs, newton-cg, sag, saga solvers.

**n_jobs**: int, default: 1

Number of CPU cores used when parallelizing over classes if multi_class='ovr'”. This parameter is ignored when the “solver” is set to ‘liblinear’ regardless of whether ‘multi_class’ is specified or not. If given a value of -1, all cores are used.

### Attributes

<table>
<thead>
<tr>
<th>coef_</th>
<th>(array, shape (1, n_features) or (n_classes, n_features)) Coefficient of the features in the decision function. coef_ is of shape (1, n_features) when the given problem is binary.</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(array, shape (1,) or (n_classes,)) Intercept (a.k.a. bias) added to the decision function. If fit_intercept is set to False, the intercept is set to zero. intercept_ is of shape(1,) when the problem is binary.</td>
</tr>
<tr>
<td>n_iter</td>
<td>(array, shape (n_classes,) or (1, )) Actual number of iterations for all classes. If binary or multinomial, it returns only 1 element. For liblinear solver, only the maximum number of iteration across all classes is given.</td>
</tr>
</tbody>
</table>

**See also:**

*SGDClassifier* incrementally trained logistic regression (when given the parameter **loss**="log").
sklearn.svm.LinearSVC learns SVM models using the same algorithm.

LogisticRegressionCV Logistic regression with built-in cross validation

Notes

The underlying C implementation uses a random number generator to select features when fitting the model. It is thus not uncommon, to have slightly different results for the same input data. If that happens, try with a smaller tol parameter.

Predict output may not match that of standalone liblinear in certain cases. See differences from liblinear in the narrative documentation.

References

LIBLINEAR – A Library for Large Linear Classification http://www.csie.ntu.edu.tw/~cjlin/liblinear/

SAG – Mark Schmidt, Nicolas Le Roux, and Francis Bach Minimizing Finite Sums with the Stochastic Average Gradient https://hal.inria.fr/hal-00860051/document


Methods

```
<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
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<td>decision_function(X)</td>
<td>Predict confidence scores for samples.</td>
</tr>
<tr>
<td>densify()</td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit the model according to the given training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict class labels for samples in X.</td>
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<tr>
<td>predict_log_proba(X)</td>
<td>Log of probability estimates.</td>
</tr>
<tr>
<td>predict_proba(X)</td>
<td>Probability estimates.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>sparsify()</td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>
```

__init__(penalty='l2', dual=False, tol=0.0001, C=1.0, fit_intercept=True, intercept_scaling=1, class_weight=None, random_state=None, solver='liblinear', max_iter=100, multi_class='ovr', verbose=0, warm_start=False, n_jobs=1)

decision_function(X)

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

Returns array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

**densify()**
Convert coefficient matrix to dense array format.

Converts the coef_ member (back) to a numpy.ndarray. This is the default format of coef_ and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

**Returns**
self : estimator

**fit (X, y, sample_weight=None)**
Fit the model according to the given training data.

**Parameters**

- **X** : {array-like, sparse matrix}, shape (n_samples, n_features)
  Training vector, where n_samples is the number of samples and n_features is the number of features.

- **y** : array-like, shape (n_samples,)
  Target vector relative to X.

- **sample_weight** : array-like, shape (n_samples,) optional
  Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

**New in version 0.17:** sample_weight support to LogisticRegression.

**Returns**
self : object

Returns self.

**get_params (deep=True)**
Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
params : mapping of string to any
Parameter names mapped to their values.

**predict (X)**
Predict class labels for samples in X.

**Parameters**

- **X** : {array-like, sparse matrix}, shape = [n_samples, n_features]
  Samples.

**Returns**
C : array, shape = [n_samples]
Predicted class label per sample.

**predict_log_proba (X)**
Log of probability estimates.

The returned estimates for all classes are ordered by the label of classes.

**Parameters**

- **X** : array-like, shape = [n_samples, n_features]

**Returns**
T : array-like, shape = [n_samples, n_classes]
Returns the log-probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`.

**predict_proba** *(X)*

Probability estimates.

The returned estimates for all classes are ordered by the label of classes.

For a multi_class problem, if multi_class is set to be “multinomial” the softmax function is used to find the predicted probability of each class. Else use a one-vs-rest approach, i.e calculate the probability of each class assuming it to be positive using the logistic function. and normalize these values across all the classes.

**Parameters**
- **X**: array-like, shape = [n_samples, n_features]

**Returns**
- **T**: array-like, shape = [n_samples, n_classes]

Returns the probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**
- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**
- **score**: float
  - Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**
- **self**: estimator

**sparsify** *

Convert coefficient matrix to sparse format.

Converts the `coef_` member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The `intercept_` member is not converted.

**Returns**
- **self**: estimator
Notes

For non-sparse models, i.e. when there are not many zeros in `coef_`, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with `(coef_ == 0).sum()`, must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

Examples using `sklearn.linear_model.LogisticRegression`

- Pipelining: chaining a PCA and a logistic regression
- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Plot classification probability
- Plot class probabilities calculated by the VotingClassifier
- Feature transformations with ensembles of trees
- Digits Classification Exercise
- Path with L1- Logistic Regression
- Logistic function
- Logistic Regression 3-class Classifier
- Comparing various online solvers
- MNIST classification using multinomial logistic + L1
- L1 Penalty and Sparsity in Logistic Regression
- Plot multinomial and One-vs-Rest Logistic Regression
- Multiclass sparse logistic regression on newsgroups20
- Classifier Chain
- Restricted Boltzmann Machine features for digit classification

30.19.10 `sklearn.linear_model.MultiTaskLasso`

```python
class sklearn.linear_model.MultiTaskLasso(alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, random_state=None, selection='cyclic')
```

Multi-task Lasso model trained with L1/L2 mixed-norm as regularizer

The optimization objective for Lasso is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \|Y - XW\|_2^2 + \alpha \|W\|_{2,1}
\]

Where:

\[
\|W\|_{2,1} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]
i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters

**alpha** : float, optional

Constant that multiplies the L1/L2 term. Defaults to 1.0

**fit_intercept** : boolean

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**normalize** : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the L2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

**copy_X** : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**max_iter** : int, optional

The maximum number of iterations

**tol** : float, optional

The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.

**warm_start** : bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**random_state** : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’.

**selection** : str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’) often leads to significantly faster convergence especially when tol is higher than 1e-4

Attributes

<table>
<thead>
<tr>
<th><strong>coef_</strong></th>
<th>(array, shape (n_tasks, n_features)) Parameter vector ((\hat{W}) in the cost function formula). Note that coef_ stores the transpose of (\hat{W})'s transpose.</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>intercept_</strong></td>
<td>(array, shape (n_tasks,)) independent term in decision function.</td>
</tr>
<tr>
<td><strong>n_iter_</strong></td>
<td>(int) number of iterations run by the coordinate descent solver to reach the specified tolerance.</td>
</tr>
</tbody>
</table>

See also:
**MultiTaskLasso**  Multi-task L1/L2 Lasso with built-in cross-validation

*Lasso, MultiTaskElasticNet*

**Notes**

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

**Examples**

```python
>>> from sklearn import linear_model
>>> clf = linear_model.MultiTaskLasso(alpha=0.1)
>>> clf.fit([[0,0], [1, 1], [2, 2]], [[0, 0], [1, 1], [2, 2]])
MultiTaskLasso(alpha=0.1, copy_X=True, fit_intercept=True, max_iter=1000,
               normalize=False, random_state=None, selection='cyclic', tol=0.0001,
               warm_start=False)
>>> print(clf.coef_)
[[ 0.89393398  0.        ]
 [ 0.89393398  0.        ]]  
>>> print(clf.intercept_)
[ 0.10606602  0.10606602]
```

**Methods**

- `fit(X, y)` Fit MultiTaskElasticNet model with coordinate descent
- `get_params([deep])` Get parameters for this estimator.
- `path(X, y[, l1_ratio, eps, n_alphas, ...])` Compute elastic net path with coordinate descent
- `predict(X)` Predict using the linear model
- `score(X, y[, sample_weight])` Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)` Set the parameters of this estimator.

**__init__**(alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=1000,
           tol=0.0001, warm_start=False, random_state=None, selection='cyclic')

**fit**(X, y)

Fit MultiTaskElasticNet model with coordinate descent

**Parameters**

- **X**: ndarray, shape (n_samples, n_features)
  
  Data

- **y**: ndarray, shape (n_samples, n_tasks)
  
  Target. Will be cast to X’s dtype if necessary
Notes

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

get_params (deep=True)
Get parameters for this estimator.

Parameters  
- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns  
- params : mapping of string to any
  Parameter names mapped to their values.

path (X, y, 11_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)
Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{(2 \times n\_samples)} \times ||y - Xw||^2_2 \\
+ \alpha \times 11\_ratio \times ||w||_1 \\
+ 0.5 \times \alpha \times (1 - 11\_ratio) \times ||w||^2_2
\]

For multi-output tasks it is:

\[
(1 / (2 \times n\_samples)) \times ||Y - XW||^\text{Fro}_2 \\
\times \alpha \times 11\_ratio \times ||W||_21 \\
\times 0.5 \times \alpha \times (1 - 11\_ratio) \times ||W||_\text{Fro}^2
\]

Where:

\[
||W||_21 = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters  
- X : [array-like], shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

- y : ndarray, shape (n_samples,) or (n_samples, n_outputs)
  Target values

- 11_ratio : float, optional
  float between 0 and 1 passed to elastic net (scaling between 11 and 12 penalties).
  11_ratio=1 corresponds to the Lasso

- eps : float
  Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3
**n_alphas**: int, optional

Number of alphas along the regularization path

**alphas**: ndarray, optional

List of alphas where to compute the models. If None alphas are set automatically

**precompute**: True | False | ‘auto’ | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

**Xy**: array-like, optional

Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

**copy_X**: boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**coef_init**: array, shape (n_features,) | None

The initial values of the coefficients.

**verbose**: bool or integer

Amount of verbosity.

**return_n_iter**: bool

whether to return the number of iterations or not.

**positive**: bool, default False

If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check_input**: bool, default True

Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params**: kwargs

keyword arguments passed to the coordinate descent solver.

**Returns**

**alphas**: array, shape (n_alphas,)

The alphas along the path where models are computed.

**coefs**: array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps**: array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iters**: array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

**See also:**

MultiTaskElasticNet, MultiTaskElasticNetCV, ElasticNet, ElasticNetCV
Notes

For an example, see examples/linear_model/plot_lasso_coordinate_descent_path.py.

**predict** *(X)*

Predict using the linear model

**Parameters**  
`X` : {array-like, sparse matrix}, shape = (n_samples, n_features)

  Samples.

**Returns**  
`C` : array, shape = (n_samples,)

  Returns predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred})^2).sum()$ and $v$ is the total sum of squares $((y_{true} - y_{true}.mean())^2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**  
`X` : array-like, shape = (n_samples, n_features)

  Test samples.

`y` : array-like, shape = (n_samples) or (n_samples, n_outputs)

  True values for X.

`samp"e_weight` : array-like, shape = [n_samples], optional

  Sample weights.

**Returns**  
`score` : float

  $R^2$ of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
`self`

**sparse_coef**

  sparse representation of the fitted `coef_`

Examples using `sklearn.linear_model.MultiTaskLasso`

- Joint feature selection with multi-task Lasso
Multi-task ElasticNet model trained with L1/L2 mixed-norm as regularizer

The optimization objective for MultiTaskElasticNet is:

\[
\frac{1}{(2 \times n\_samples)} \times ||Y - XW||^2_{\text{Fro}} + \alpha \times l1\_ratio \times ||W||_{21} + 0.5 \times \alpha \times (1 - l1\_ratio) \times ||W||^2_{\text{Fro}}
\]

Where:

\[
||W||_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters

alpha : float, optional
Constant that multiplies the L1/L2 term. Defaults to 1.0

l1_ratio : float
The ElasticNet mixing parameter, with 0 < l1_ratio <= 1. For l1_ratio = 1 the penalty is an L1/L2 penalty. For l1_ratio = 0 it is an L2 penalty. For 0 < l1_ratio < 1, the penalty is a combination of L1/L2 and L2.

fit_intercept : boolean
whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False
This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the L2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

copy_X : boolean, optional, default True
If True, X will be copied; else, it may be overwritten.

max_iter : int, optional
The maximum number of iterations

tol : float, optional
The tolerance for the optimization: if the updates are smaller than tol, the optimization code checks the dual gap for optimality and continues until it is smaller than tol.

warm_start : bool, optional
When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

random_state : int, RandomState instance or None, optional, default None
The seed of the pseudo random number generator that selects a random feature to update. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when selection == ‘random’.

**selection :** str, default ‘cyclic’

If set to ‘random’, a random coefficient is updated every iteration rather than looping over features sequentially by default. This (setting to ‘random’) often leads to significantly faster convergence especially when tol is higher than 1e-4.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>intercept</strong></td>
<td>(array, shape (n_tasks,)) Independent term in decision function.</td>
</tr>
<tr>
<td><strong>coef</strong></td>
<td>(array, shape (n_tasks, n_features)) Parameter vector (W in the cost function formula). If a 1D y is passed in at fit (non multi-task usage), coef_ is then a 1D array. Note that coef_ stores the transpose of W, W.T.</td>
</tr>
<tr>
<td><strong>n_iter</strong></td>
<td>(int) number of iterations run by the coordinate descent solver to reach the specified tolerance.</td>
</tr>
</tbody>
</table>

### See also:

- **MultiTaskElasticNet** Multi-task L1/L2 ElasticNet with built-in cross-validation.

- ElasticNet, MultiTaskLasso

### Notes

The algorithm used to fit the model is coordinate descent.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

### Examples

```python
>>> from sklearn import linear_model
>>> clf = linear_model.MultiTaskElasticNet(alpha=0.1)
>>> clf.fit([[0, 0], [1, 1], [2, 2]], [[0, 0], [1, 1], [2, 2]])
...
MultiTaskElasticNet(alpha=0.1, copy_X=True, fit_intercept=True,
                   il_ratio=0.5, max_iter=1000, normalize=False, random_state=None,
                   selection='cyclic', tol=0.0001, warm_start=False)
>>> print(clf.coef_)
[[ 0.45663524  0.45612256]
 [ 0.45663524  0.45612256]]
>>> print(clf.intercept_)
[ 0.0872422  0.0872422]
```
Methods

**fit**(X, y)  
Fit MultiTaskElasticNet model with coordinate descent

**get_params**(deep)  
Get parameters for this estimator.

**path**(X, y[, l1_ratio, eps, n_alphas, ...])  
Compute elastic net path with coordinate descent

**predict**(X)  
Predict using the linear model

**score**(X, y[, sample_weight])  
Returns the coefficient of determination $R^2$ of the prediction.

**set_params**(**params**)  
Set the parameters of this estimator.

__init__(alpha=1.0, l1_ratio=0.5, fit_intercept=True, normalize=False, copy_X=True, max_iter=1000, tol=0.0001, warm_start=False, random_state=None, selection='cyclic')

**fit**(X, y)  
Fit MultiTaskElasticNet model with coordinate descent

**Parameters**

X : ndarray, shape (n_samples, n_features)  
Data

y : ndarray, shape (n_samples, n_tasks)  
Target. Will be cast to X’s dtype if necessary

**Notes**

Coordinate descent is an algorithm that considers each column of data at a time hence it will automatically convert the X input as a Fortran-contiguous numpy array if necessary.

To avoid memory re-allocation it is advised to allocate the initial data in memory directly using that format.

**get_params**(deep=True)  
Get parameters for this estimator.

**Parameters**

deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

params : mapping of string to any

Parameter names mapped to their values.

**path**(X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute=’auto’, Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)  
Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

$$\frac{1}{2 \times n_{\text{samples}}} \times ||y - Xw||^2_2 + \alpha \times l1_{\text{ratio}} \times ||w||_1 + 0.5 \times \alpha \times (1 - l1_{\text{ratio}}) \times ||w||^2_2$$

For multi-output tasks it is:
\[
\frac{1}{2n_{\text{samples}}} \|Y - XW\|^2_{\text{Fro}} + \alpha \cdot l1_{\text{ratio}} \cdot \|W\|_{21} + 0.5 \cdot \alpha \cdot (1 - l1_{\text{ratio}}) \cdot \|W\|^2_{\text{Fro}}
\]

Where:

\[
\|W\|_{21} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

- **y**: ndarray, shape (n_samples,) or (n_samples, n_outputs)
  Target values

- **l1_ratio**: float, optional
  float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1_ratio=1 corresponds to the Lasso

- **eps**: float
  Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3

- **n_alphas**: int, optional
  Number of alphas along the regularization path

- **alphas**: ndarray, optional
  List of alphas where to compute the models. If None alphas are set automatically

- **precompute**: True | False | 'auto' | array-like
  Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto' let us decide. The Gram matrix can also be passed as argument.

- **Xy**: array-like, optional
  Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.

- **copy_X**: boolean, optional, default True
  If True, X will be copied; else, it may be overwritten.

- **coef_init**: array, shape (n_features,) | None
  The initial values of the coefficients.

- **verbose**: bool or integer
  Amount of verbosity.

- **return_n_iter**: bool
  whether to return the number of iterations or not.

- **positive**: bool, default False
  If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).
**check_input** : bool, default True

Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params** : kwargs

Keyword arguments passed to the coordinate descent solver.

Returns:

**alphas** : array, shape (n_alphas,)

The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iters** : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

See also:

*MultiTaskElasticNet*, *MultiTaskElasticNetCV*, *ElasticNet*, *ElasticNetCV*

Notes

For an example, see *examples/linear_model/plot_lasso_coordinate_descent_path.py*.

**predict** *(X)*

Predict using the linear model

**Parameters**

**X** : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

**Returns**

**C** : array, shape = (n_samples,)

Returns predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares ($(y_{true} - y_{pred})^2).sum()$ and $v$ is the total sum of squares ($(y_{true} - y_{true}.mean())^2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

**X** : array-like, shape = (n_samples, n_features)

Test samples.

**y** : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for $X$.

**sample_weight** : array-like, shape = [n_samples], optional

Sample weights.

**Returns**

**score** : float
R^2 of self.predict(X) wrt. y.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**sparse_coef_**
sparse representation of the fitted coef_

### 30.19.12 sklearn.linear_model.OrthogonalMatchingPursuit

**class** sklearn.linear_model.OrthogonalMatchingPursuit (n_nonzero_coefs=None,

  tol=None, fit_intercept=True, normalize=True, precompute='auto')

Orthogonal Matching Pursuit model (OMP)

Read more in the User Guide.

**Parameters**

**n_nonzero_coefs** : int, optional
Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n_features.

**tol** : float, optional
Maximum norm of the residual. If not None, overrides n_nonzero_coefs.

**fit_intercept** : boolean, optional
whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**normalize** : boolean, optional, default True
This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

**precompute** : {True, False, ‘auto’}, default ‘auto’
Whether to use a precomputed Gram and Xy matrix to speed up calculations. Improves performance when n_targets or n_samples is very large. Note that if you already have such matrices, you can pass them directly to the fit method.

**Attributes**

<table>
<thead>
<tr>
<th>coef_</th>
<th>(array, shape (n_features,) or (n_targets, n_features)) parameter vector (w in the formula)</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(float or array, shape (n_targets,)) independent term in decision function.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int or array-like) Number of active features across every target.</td>
</tr>
</tbody>
</table>

See also:
orthogonal_mp, orthogonal_mp_gram, lars_path, Lars, LassoLars, decomposition.
sparse_encode, OrthogonalMatchingPursuitCV

Notes

Orthogonal matching pursuit was introduced in G. Mallat, Z. Zhang, Matching pursuits with time-frequency
(http://blanche.polytechnique.fr/~mallat/papiers/MallatPursuit93.pdf)

This implementation is based on Rubinstein, R., Zibulevsky, M. and Elad, M., Efficient Implementation of
http://www.cs.technion.ac.il/~ronrubin/Publications/KSVD-OMP-v2.pdf

Methods

<table>
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<tr>
<th>Method</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td>fit(X, y)</td>
<td>Fit the model using X, y as training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination ( R^2 ) of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(n_nonzero_coefs=None, tol=None, fit_intercept=True, normalize=True, precompute='auto')

fit (X, y)
Fit the model using X, y as training data.

Parameters

- **X**: array-like, shape (n_samples, n_features)
  Training data.
- **y**: array-like, shape (n_samples,) or (n_samples, n_targets)
  Target values. Will be cast to X's dtype if necessary

Returns

- **self**: object
  returns an instance of self.

get_params (deep=True)
Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  Parameter names mapped to their values.

predict (X)
Predict using the linear model

Parameters

- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  Samples.
Returns $C$ : array, shape = (n_samples,)

Returns predicted values.

score $(X, y, \text{sample\_weight}=None)$

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $=((y_{true} - y_{pred})^2).\text{sum()}$ and $v$ is the total sum of squares $=((y_{true} - y_{true}.\text{mean()}^2).\text{sum()}$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

Parameters $X$ : array-like, shape = (n_samples, n_features)

Test samples.

$y$ : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for $X$.

$\text{sample\_weight}$ : array-like, shape = [n_samples], optional

Sample weights.

Returns $score$ : float

$R^2$ of self.predict($X$) wrt. $y$.

set_params (**$params$)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form $<\text{component}>__<\text{parameter}>$ so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.linear_model.OrthogonalMatchingPursuit

- Orthogonal Matching Pursuit

30.19.13 sklearn.linear_model.PassiveAggressiveClassifier

class sklearn.linear_model.PassiveAggressiveClassifier ($C=1.0$, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, loss='hinge', n_jobs=1, random_state=None, warm_start=False, class_weight=None, average=False, n_iter=None)

Passive Aggressive Classifier

Read more in the User Guide.

Parameters $C$ : float

Maximum step size (regularization). Defaults to 1.0.

fit_intercept : bool, default=False
Whether the intercept should be estimated or not. If False, the data is assumed to be already centered.

**max_iter** : int, optional

The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the `fit` method, and not the `partial_fit`. Defaults to 5. Defaults to 1000 from 0.21, or if tol is not None.

New in version 0.19.

**tol** : float or None, optional

The stopping criterion. If it is not None, the iterations will stop when `(loss > previous_loss - tol)`. Defaults to None. Defaults to `1e-3` from 0.21.

New in version 0.19.

**shuffle** : bool, default=True

Whether or not the training data should be shuffled after each epoch.

**verbose** : integer, optional

The verbosity level

**loss** : string, optional

The loss function to be used: `hinge`: equivalent to PA-I in the reference paper. `squared_hinge`: equivalent to PA-II in the reference paper.

**n_jobs** : integer, optional

The number of CPUs to use to do the OVA (One Versus All, for multi-class problems) computation. `-1` means ‘all CPUs’. Defaults to 1.

**random_state** : int, RandomState instance or None, optional, default=None

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**warm_start** : bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**class_weight** : dict, `{class_label: weight}` or “balanced” or None, optional

Preset for the `class_weight` fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of `y` to automatically adjust weights inversely proportional to class frequencies in the input data as `n_samples / (n_classes * np.bincount(y))`

New in version 0.17: parameter `class_weight` to automatically weight samples.

**average** : bool or int, optional

When set to True, computes the averaged SGD weights and stores the result in the `coef_` attribute. If set to an int greater than 1, averaging will begin once the total
number of samples seen reaches average. So average=10 will begin averaging after seeing 10 samples.

New in version 0.19: parameter average to use weights averaging in SGD

n_iter : int, optional

The number of passes over the training data (aka epochs). Defaults to None. Deprecated, will be removed in 0.21.

Changed in version 0.19: Deprecated

Attributes

<table>
<thead>
<tr>
<th>coef_</th>
<th>(array, shape = [1, n_features] if n_classes == 2 else [n_classes, n_features]) Weights assigned to the features.</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(array, shape = [1] if n_classes == 2 else [n_classes]) Constants in decision function.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) The actual number of iterations to reach the stopping criterion. For multiclass fits, it is the maximum over every binary fit.</td>
</tr>
</tbody>
</table>

See also:

SGDClassifier, Perceptron

References


Examples

```python
>>> from sklearn.linear_model import PassiveAggressiveClassifier
>>> from sklearn.datasets import make_classification

>>> X, y = make_classification(n_features=4, random_state=0)
>>> clf = PassiveAggressiveClassifier(random_state=0)
>>> clf.fit(X, y)
PassiveAggressiveClassifier(C=1.0, average=False, class_weight=None,
                               fit_intercept=True, loss='hinge', max_iter=None, n_iter=None,
                               n_jobs=1, random_state=0, shuffle=True, tol=None, verbose=0,
                               warm_start=False)

>>> print(clf.coef_)
[[ 0.49324685  1.0552176  1.49519589  1.33798314]]

>>> print(clf.intercept_)
[ 2.18438388]

>>> print(clf.predict([[0, 0, 0, 0]]))
[1]
```

Methods
<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tr>
<td><code>decision_function(X)</code></td>
<td>Predict confidence scores for samples.</td>
</tr>
<tr>
<td><code>densify()</code></td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td><code>fit(X, y[, coef_init, intercept_init])</code></td>
<td>Fit linear model with Passive Aggressive algorithm.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>partial_fit(X, y[, classes])</code></td>
<td>Fit linear model with Passive Aggressive algorithm.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict class labels for samples in X.</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(*args, **kwargs)</code></td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>

__init__(C=1.0, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, loss='hinge', n_jobs=1, random_state=None, warm_start=False, class_weight=None, average=False, n_iter=None)

`decision_function(X)`

Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

**Parameters**

- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Samples.

**Returns**

- array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
  - Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

`densify()`

Convert coefficient matrix to dense array format.

Converts the `coef_` member (back) to a numpy.ndarray. This is the default format of `coef_` and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

**Returns**

- `self`: estimator

`fit(X, y, coef_init=None, intercept_init=None)`

Fit linear model with Passive Aggressive algorithm.

**Parameters**

- **X**: {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training data
- **y**: numpy array of shape [n_samples]
  - Target values
- **coef_init**: array, shape = [n_classes, n_features]
  - The initial coefficients to warm-start the optimization.
- **intercept_init**: array, shape = [n_classes]
  - The initial intercept to warm-start the optimization.

**Returns**

- `self`: returns an instance of self.

`get_params(deep=True)`

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any  
Parameter names mapped to their values.

loss_function  
DEPRECATED: Attribute loss_function was deprecated in version 0.19 and will be removed in 0.21. Use loss_function_ instead

partial_fit (X, y, classes=None)  
Fit linear model with Passive Aggressive algorithm.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]  
Subset of the training data
y : numpy array of shape [n_samples]  
Subset of the target values
classes : array, shape = [n_classes]  
Classes across all calls to partial_fit. Can be obtained by via np.unique(y_all), where y_all is the target vector of the entire dataset. This argument is required for the first call to partial_fit and can be omitted in the subsequent calls. Note that y doesn’t need to contain all labels in classes.

Returns self : returns an instance of self.

predict (X)  
Predict class labels for samples in X.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]  
Samples.

Returns C : array, shape = [n_samples]  
Predicted class label per sample.

score (X, y, sample_weight=None)  
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters X : array-like, shape = (n_samples, n_features)  
Test samples.
y : array-like, shape = (n_samples) or (n_samples, n_outputs)  
True labels for X.

sample_weight : array-like, shape = [n_samples], optional  
Sample weights.

Returns score : float  
Mean accuracy of self.predict(X) wrt. y.

sparsify ()  
Convert coefficient matrix to sparse format.
Converts the `coef_` member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The `intercept_` member is not converted.

Returns self : estimator

Notes

For non-sparse models, i.e. when there are not many zeros in `coef_`, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with `(coef_ == 0).sum()`, must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the `partial_fit` method (if any) will not work until you call `densify`.

Examples using `sklearn.linear_model.PassiveAggressiveClassifier`

- Out-of-core classification of text documents
- Comparing various online solvers
- Classification of text documents using sparse features

30.19.14 `sklearn.linear_model.PassiveAggressiveRegressor`

class `sklearn.linear_model.PassiveAggressiveRegressor`(C=1.0, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, loss='epsilon_insensitive', epsilon=0.1, random_state=None, warm_start=False, average=False, n_iter=None)

Passive Aggressive Regressor

Read more in the User Guide.

Parameters C : float

Maximum step size (regularization). Defaults to 1.0.

fit_intercept : bool

Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.

max_iter : int, optional

The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the `fit` method, and not the `partial_fit`. Defaults to 5. Defaults to 1000 from 0.21, or if `tol` is not None.

New in version 0.19.

tol : float or None, optional

The stopping criterion. If it is not None, the iterations will stop when (loss > previous_loss - tol). Defaults to None. Defaults to 1e-3 from 0.21.

New in version 0.19.
shuffle : bool, default=True
Whether or not the training data should be shuffled after each epoch.

verbose : integer, optional
The verbosity level

loss : string, optional
The loss function to be used: epsilon_insensitive: equivalent to PA-I in the reference paper. squared_epsilon_insensitive: equivalent to PA-II in the reference paper.

epsilon : float
If the difference between the current prediction and the correct label is below this threshold, the model is not updated.

random_state : int, RandomState instance or None, optional, default=None
The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

warm_start : bool, optional
When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

average : bool or int, optional
When set to True, computes the averaged SGD weights and stores the result in the coef_ attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So average=10 will begin averaging after seeing 10 samples.

New in version 0.19: parameter average to use weights averaging in SGD

n_iter : int, optional
The number of passes over the training data (aka epochs). Defaults to None. Deprecated, will be removed in 0.21.

Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape = [1, n_features] if n_classes == 2 else [n_classes, n_features]) Weights assigned to the features.</td>
</tr>
<tr>
<td>intercep_</td>
<td>(array, shape = [1] if n_classes == 2 else [n_classes]) Constants in decision function.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) The actual number of iterations to reach the stopping criterion.</td>
</tr>
</tbody>
</table>

See also:

SGDRegressor
References


Examples

```python
>>> from sklearn.linear_model import PassiveAggressiveRegressor
>>> from sklearn.datasets import make_regression

>>> X, y = make_regression(n_features=4, random_state=0)
>>> regr = PassiveAggressiveRegressor(random_state=0)
>>> regr.fit(X, y)
PassiveAggressiveRegressor(C=1.0, average=False, epsilon=0.1,
                          fit_intercept=True, loss='epsilon_insensitive',
                          max_iter=None, n_iter=None, random_state=0, shuffle=True,
                          tol=None, verbose=0, warm_start=False)

>>> print(regr.coef_)
[ 20.48736655  34.18818427  67.59122734  87.94731329]

>>> print(regr.intercept_)
-0.02306214

>>> print(regr.predict([[0, 0, 0, 0]]))
[-0.02306214]
```

Methods

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<th>Method</th>
<th>Description</th>
</tr>
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<tbody>
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<td>densify()</td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td>fit(X, y[, coef_init, intercept_init])</td>
<td>Fit linear model with Passive Aggressive algorithm.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>partial_fit(X, y)</td>
<td>Fit linear model with Passive Aggressive algorithm.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(*args, **kwargs)</td>
<td></td>
</tr>
<tr>
<td>sparsify()</td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>

```python
>>> __init__(C=1.0, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, loss='epsilon_insensitive', epsilon=0.1, random_state=None, warm_start=False, average=False, n_iter=None)

```

Convert coefficient matrix to dense array format.

Converts the coef member (back) to a numpy.ndarray. This is the default format of coef_ and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

Returns self : estimator

```python
>>> fit(X, y[, coef_init=None, intercept_init=None])
Fit linear model with Passive Aggressive algorithm.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Training data

\( y \) : numpy array of shape [n_samples]

Target values

\( \text{coef\_init} \) : array, shape = [n_features]

The initial coefficients to warm-start the optimization.

\( \text{intercept\_init} \) : array, shape = [1]

The initial intercept to warm-start the optimization.

\textbf{Returns self} : returns an instance of self.

\textbf{get\_params} (\textit{deep=\text{True}})

Get parameters for this estimator.

\textbf{Parameters} \textit{deep} : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

\textbf{Returns} \textit{params} : mapping of string to any

Parameter names mapped to their values.

\textbf{partial\_fit} \((X, y)\)

Fit linear model with Passive Aggressive algorithm.

\textbf{Parameters} \textit{X} : \{array-like, sparse matrix\}, shape = [n_samples, n_features]

Subset of training data

\( y \) : numpy array of shape [n_samples]

Subset of target values

\textbf{Returns} \textit{self} : returns an instance of self.

\textbf{predict} \((X)\)

Predict using the linear model

\textbf{Parameters} \textit{X} : \{array-like, sparse matrix\}, shape (n_samples, n_features)

\textbf{Returns} \textit{array}, shape (n_samples,)

Predicted target values per element in X.

\textbf{score} \((X, y, \textit{sample\_weight=\text{None}})\)

Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \((1 - \frac{u}{v})\), where \( u \) is the residual sum of squares ((\textit{y\_true} - \textit{y\_pred}) ** 2).sum() and \( v \) is the total sum of squares ((\textit{y\_true} - \textit{y\_true}.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

\textbf{Parameters} \textit{X} : array-like, shape = (n_samples, n_features)

Test samples.

\( y \) : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for \( X \).

\textit{sample\_weight} : array-like, shape = [n_samples], optional

Sample weights.
**Returns score**: float

R^2 of self.predict(X) wrt. y.

**sparsify()**

Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

**Returns self**: estimator

**Notes**

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef_ == 0).sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

### 30.19.15 sklearn.linear_model.Perceptron

**class sklearn.linear_model.Perceptron**

```
penalty=None, alpha=0.0001, fit_intercept=True,
max_iter=None, tol=None, shuffle=True, verbose=0, eta0=1.0, n_jobs=1, random_state=0,
class_weight=None, warm_start=False, n_iter=None)
```

Read more in the *User Guide*.

**Parameters penalty**: None, ‘l2’ or ‘l1’ or ‘elasticnet’

The penalty (aka regularization term) to be used. Defaults to None.

**alpha**: float

Constant that multiplies the regularization term if regularization is used. Defaults to 0.0001

**fit_intercept**: bool

Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.

**max_iter**: int, optional

The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial_fit. Defaults to 5. Defaults to 1000 from 0.21, or if tol is not None.

New in version 0.19.

**tol**: float or None, optional

The stopping criterion. If it is not None, the iterations will stop when (loss > previous_loss - tol). Defaults to None. Defaults to 1e-3 from 0.21.

New in version 0.19.

**shuffle**: bool, optional, default True
Whether or not the training data should be shuffled after each epoch.

**verbose** : integer, optional

The verbosity level

**eta0** : double

Constant by which the updates are multiplied. Defaults to 1.

**n_jobs** : integer, optional

The number of CPUs to use to do the OVA (One Versus All, for multi-class problems) computation. -1 means ‘all CPUs’. Defaults to 1.

**random_state** : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**class_weight** : dict, {class_label: weight} or “balanced” or None, optional

Preset for the class_weight fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as \( n_{\text{samples}} / (n_{\text{classes}} \times \text{np.bincount}(y)) \)

**warm_start** : bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**n_iter** : int, optional

The number of passes over the training data (aka epochs). Defaults to None. Deprecated, will be removed in 0.21.

Changed in version 0.19: Deprecated

### Attributes

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape = [1, n_features] if n_classes == 2 else [n_classes, n_features]) Weights assigned to the features.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [1] if n_classes == 2 else [n_classes]) Constants in decision function.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) The actual number of iterations to reach the stopping criterion. For multiclass fits, it is the maximum over every binary fit.</td>
</tr>
</tbody>
</table>

See also:

`SGDClassifier`
Notes

Perceptron and SGDClassifier share the same underlying implementation. In fact, Perceptron() is equivalent to SGDClassifier(loss="perceptron", eta0=1, learning_rate="constant", penalty=None).

References


Methods

decision_function(X)  
Predict confidence scores for samples.

densify()  
Convert coefficient matrix to dense array format.

fit(X, y[, coef_init, intercept_init, ...])  
Fit linear model with Stochastic Gradient Descent.

get_params([deep])  
Get parameters for this estimator.

partial_fit(X, y[, classes, sample_weight])  
Fit linear model with Stochastic Gradient Descent.

predict(X)  
Predict class labels for samples in X.

score(X, y[, sample_weight])  
Returns the mean accuracy on the given test data and labels.

set_params(*args, **kwargs)  
Convert coefficient matrix to sparse format.

__init__(penalty=None, alpha=0.0001, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, eta0=1.0, n_jobs=1, random_state=0, class_weight=None, warm_start=False, n_iter=None)

decision_function(X)  
Predict confidence scores for samples.

Parameters

X : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

Returns

array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)

Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

densify()  
Convert coefficient matrix to dense array format.

Parameters

self : estimator

Returns

self

fit(X, y, coef_init=None, intercept_init=None, sample_weight=None)  
Fit linear model with Stochastic Gradient Descent.

Parameters

X : {array-like, sparse matrix}, shape (n_samples, n_features)

Training data

y : numpy array, shape (n_samples,)
Target values

**coef_init** : array, shape (n_classes, n_features)

The initial coefficients to warm-start the optimization.

**intercept_init** : array, shape (n_classes,)

The initial intercept to warm-start the optimization.

**sample_weight** : array-like, shape (n_samples,), optional

Weights applied to individual samples. If not provided, uniform weights are assumed. These weights will be multiplied with class_weight (passed through the constructor) if class_weight is specified.

**Returns** self : returns an instance of self.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters** deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**loss_function**

DEPRECATED: Attribute loss_function was deprecated in version 0.19 and will be removed in 0.21. Use loss_function instead

**partial_fit** *(X, y, classes=None, sample_weight=None)*

Fit linear model with Stochastic Gradient Descent.

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features)

Subset of the training data

y : numpy array, shape (n_samples,)

Subset of the target values

classes : array, shape (n_classes,)

Classes across all calls to partial_fit. Can be obtained by via np.unique(y_all), where y_all is the target vector of the entire dataset. This argument is required for the first call to partial_fit and can be omitted in the subsequent calls. Note that y doesn’t need to contain all labels in classes.

**sample_weight** : array-like, shape (n_samples,), optional

Weights applied to individual samples. If not provided, uniform weights are assumed.

**Returns** self : returns an instance of self.

**predict** *(X)*

Predict class labels for samples in X.

**Parameters** X : {array-like, sparse matrix}, shape = [n_samples, n_features]

Samples.

**Returns** C : array, shape = [n_samples]

Predicted class label per sample.
score \((X, y, \text{sample\_weight}={\text{None}})\)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X** : array-like, shape = (n_samples, n_features)
  Test samples.
- **y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True labels for X.
- **sample\_weight** : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- **score** : float
  Mean accuracy of self.predict(X) wrt. y.

sparsify()

Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

**Returns**

- **self** : estimator

**Notes**

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef_ == 0).sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

**Examples using sklearn.linear_model.Perceptron**

- Out-of-core classification of text documents
- Comparing various online solvers
- Classification of text documents using sparse features

**30.19.16 sklearn.linear_model.RANSACRegressor**

class sklearn.linear_model.RANSACRegressor

RANSAC (RANdom SAmple Consensus) algorithm.
RANSAC is an iterative algorithm for the robust estimation of parameters from a subset of inliers from the complete data set. More information can be found in the general documentation of linear models.

A detailed description of the algorithm can be found in the documentation of the `linear_model` sub-package. Read more in the *User Guide*.

**Parameters**

- `base_estimator` : object, optional
  
  Base estimator object which implements the following methods:
  
  - `fit(X, y)`: Fit model to given training data and target values.
  
  - `score(X, y)`: Returns the mean accuracy on the given test data, which is used for the stop criterion defined by `stop_score`. Additionally, the score is used to decide which of two equally large consensus sets is chosen as the better one.

  If `base_estimator` is None, then `base_estimator=sklearn.linear_model.LinearRegression()` is used for target values of dtype float.

  Note that the current implementation only supports regression estimators.

- `min_samples` : int (\( \geq 1 \)) or float ([0, 1]), optional
  
  Minimum number of samples chosen randomly from original data. Treated as an absolute number of samples for `min_samples` \( \geq 1 \), treated as a relative number `ceil(min_samples * X.shape[0])` for `min_samples` \(< 1\). This is typically chosen as the minimal number of samples necessary to estimate the given `base_estimator`. By default a `sklearn.linear_model.LinearRegression()` estimator is assumed and `min_samples` is chosen as `X.shape[1] + 1`.

- `residual_threshold` : float, optional
  
  Maximum residual for a data sample to be classified as an inlier. By default the threshold is chosen as the MAD (median absolute deviation) of the target values `y`.

- `is_data_valid` : callable, optional
  
  This function is called with the randomly selected data before the model is fitted to it: `is_data_valid(X, y)`. If its return value is False the current randomly chosen sub-sample is skipped.

- `is_model_valid` : callable, optional
  
  This function is called with the estimated model and the randomly selected data: `is_model_valid(model, X, y)`. If its return value is False the current randomly chosen sub-sample is skipped. Rejecting samples with this function is computationally costlier than with `is_data_valid`. `is_model_valid` should therefore only be used if the estimated model is needed for making the rejection decision.

- `max_trials` : int, optional
  
  Maximum number of iterations for random sample selection.

- `max_skips` : int, optional
  
  Maximum number of iterations that can be skipped due to finding zero inliers or invalid data defined by `is_data_valid` or invalid models defined by `is_model_valid`.

  New in version 0.19.

- `stop_n_inliers` : int, optional
  
  Stop iteration if at least this number of inliers are found.

- `stop_score` : float, optional
Stop iteration if score is greater equal than this threshold.

**stop_probability** : float in range [0, 1], optional

RANSAC iteration stops if at least one outlier-free set of the training data is sampled in RANSAC. This requires to generate at least N samples (iterations):

\[
N \geq \frac{\log(1 - \text{probability})}{\log(1 - e^{-m})}
\]

where the probability (confidence) is typically set to high value such as 0.99 (the default) and e is the current fraction of inliers w.r.t. the total number of samples.

**residual_metric** : callable, optional

Metric to reduce the dimensionality of the residuals to 1 for multi-dimensional target values \(y\.shape[1] > 1\). By default the sum of absolute differences is used:

\[
\text{lambda} \ dy: \ \text{np.sum} (\text{np.abs} (dy), \ \text{axis}=1)
\]

Deprecated since version 0.18: **residual_metric** is deprecated from 0.18 and will be removed in 0.20. Use **loss** instead.

**loss** : string, callable, optional, default “absolute_loss”

String inputs, “absolute_loss” and “squared_loss” are supported which find the absolute loss and squared loss per sample respectively.

If **loss** is a callable, then it should be a function that takes two arrays as inputs, the true and predicted value and returns a 1-D array with the i-th value of the array corresponding to the loss on \(X[i]\).

If the loss on a sample is greater than the **residual_threshold**, then this sample is classified as an outlier.

**random_state** : int, RandomState instance or None, optional, default None

The generator used to initialize the centers. If int, **random_state** is the seed used by the random number generator; If RandomState instance, **random_state** is the random number generator; If None, the random number generator is the RandomState instance used by **np.random**.

### Attributes

<table>
<thead>
<tr>
<th><strong>estimator</strong>_</th>
<th>(object) Best fitted model (copy of the base_estimator object).</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>n_trials</strong>_</td>
<td>(int) Number of random selection trials until one of the stop criteria is met. It is always &lt;= max_trials.</td>
</tr>
<tr>
<td><strong>inlier_mask</strong>_</td>
<td>(bool array of shape [n_samples]) Boolean mask of inliers classified as True.</td>
</tr>
<tr>
<td><strong>n_skips_no_inliers</strong></td>
<td>(int) Number of iterations skipped due to finding zero inliers. .. versionadded:: 0.19</td>
</tr>
<tr>
<td><strong>n_skips_invalid_data</strong></td>
<td>(int) Number of iterations skipped due to invalid data defined by is_data_valid. .. versionadded:: 0.19</td>
</tr>
<tr>
<td><strong>n_skips_invalid_model</strong></td>
<td>(int) Number of iterations skipped due to an invalid model defined by is_model_valid. .. versionadded:: 0.19</td>
</tr>
</tbody>
</table>

### References

[R109][11], [R110][11], [R111][11]

30.19. **sklearn.linear_model: Generalized Linear Models**
Methods

<table>
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<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit estimator using RANSAC algorithm.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the estimated model.</td>
</tr>
<tr>
<td>score(X, y)</td>
<td>Returns the score of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__ (base_estimator=None, min_samples=None, residual_threshold=None, is_data_valid=None, is_model_valid=None, max_trials=100, max_skips=inf, stop_n_inliers=inf, stop_score=inf, stop_probability=0.99, residual_metric=None, loss='absolute_loss', random_state=None)

**fit (X, y, sample_weight=None)**
Fit estimator using RANSAC algorithm.

**Parameters**
- **X**: array-like or sparse matrix, shape [n_samples, n_features]
  - Training data.
- **y**: array-like, shape = [n_samples] or [n_samples, n_targets]
  - Target values.
- **sample_weight**: array-like, shape = [n_samples]
  - Individual weights for each sample raises error if sample_weight is passed and base_estimator fit method does not support it.

**Raises** `ValueError`
If no valid consensus set could be found. This occurs if **is_data_valid** and **is_model_valid** return False for all **max_trials** randomly chosen sub-samples.

**get_params (deep=True)**
Get parameters for this estimator.

**Parameters**
- **deep** : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params** : mapping of string to any
  - Parameter names mapped to their values.

**predict (X)**
Predict using the estimated model.

**Parameters**
- **X** : numpy array of shape [n_samples, n_features]

**Returns**
- **y** : array, shape = [n_samples] or [n_samples, n_targets]
  - Returns predicted values.

**score (X, y)**
Returns the score of the prediction.

**Parameters**
- **X** : numpy array or sparse matrix of shape [n_samples, n_features]
Training data.

\[ y : \text{array, shape = \([n_{samples}\)] or \([n_{samples}, n_{targets}\])} \]

Target values.

Returns \( z \): float

Score of the prediction.

\[ \text{set_params (**params)} \]

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>__<\text{parameter}>\) so that it's possible to update each component of a nested object.

Returns self

Examples using sklearn.linear_model.RANSACRegressor

- Robust linear model estimation using RANSAC
- Theil-Sen Regression
- Robust linear estimator fitting

30.19.17 sklearn.linear_model.Ridge

class sklearn.linear_model.Ridge \((alpha=1.0, \text{ fit_intercept=True, \ normalize=False, } \text{ copy_X=True, max_iter=None, tol=0.001, solver='auto', random_state=None})\)

Linear least squares with l2 regularization.

Minimizes the objective function:

\[ ||y - Xw||^2_2 + \alpha \times ||w||^2_2 \]

This model solves a regression model where the loss function is the linear least squares function and regularization is given by the l2-norm. Also known as Ridge Regression or Tikhonov regularization. This estimator has built-in support for multi-variate regression (i.e., when \(y\) is a 2d-array of shape \([n_{samples}, n_{targets}]\)).

Read more in the User Guide.

Parameters alpha : \{float, array-like\}, shape \((n_{targets})\)

Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to \(C^{-1}\) in other linear models such as LogisticRegression or LinearSVC. If an array is passed, penalties are assumed to be specific to the targets. Hence they must correspond in number.

fit_intercept : boolean

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False
This parameter is ignored when `fit_intercept` is set to False. If True, the regres-
sors X will be normalized before regression by subtracting the mean and dividing by
the l2-norm. If you wish to standardize, please use `sklearn.preprocessing.
StandardScaler` before calling `fit` on an estimator with `normalize=False`.

copy_X : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

max_iter : int, optional

Maximum number of iterations for conjugate gradient solver. For ‘sparse_cg’ and ‘lsqr’
solvers, the default value is determined by scipy.sparse.linalg. For ‘sag’ solver, the
default value is 1000.

tol : float

Precision of the solution.


Solver to use in the computational routines:

• ‘auto’ chooses the solver automatically based on the type of data.

• ‘svd’ uses a Singular Value Decomposition of X to compute the Ridge coefficients.
  More stable for singular matrices than ‘cholesky’.

• ‘cholesky’ uses the standard scipy.linalg.solve function to obtain a closed-form solu-
tion.

• ‘sparse_cg’ uses the conjugate gradient solver as found in scipy.sparse.linalg.cg. As
  an iterative algorithm, this solver is more appropriate than ‘cholesky’ for large-scale
data (possibility to set `tol` and `max_iter`).

• ‘lsqr’ uses the dedicated regularized least-squares routine scipy.sparse.linalg.lsqr. It
  is the fastest but may not be available in old scipy versions. It also uses an iterative
  procedure.

• ‘sag’ uses a Stochastic Average Gradient descent, and ‘saga’ uses its improved, unbi-
ased version named SAGA. Both methods also use an iterative procedure, and are of-
ten faster than other solvers when both n_samples and n_features are large. Note that
  ‘sag’ and ‘saga’ fast convergence is only guaranteed on features with approximately
  the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

All last five solvers support both dense and sparse data. However, only ‘sag’ and ‘saga’
supports sparse input when `fit_intercept` is True.

New in version 0.17: Stochastic Average Gradient descent solver.

New in version 0.19: SAGA solver.

random_state : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator to use when shuffling the data. If
int, `random_state` is the seed used by the random number generator; If RandomState
instance, `random_state` is the random number generator; If None, the random number
generator is the RandomState instance used by `np.random`. Used when `solver ==`
‘sag’.

New in version 0.17: `random_state` to support Stochastic Average Gradient.
Attributes

| **coef_** | (array, shape (n_features,) or (n_targets, n_features)) Weight vector(s). |
| **intercept_** | (float | array, shape = (n_targets,)) Independent term in decision function. Set to 0.0 if fit_intercept = False. |
| **n_iter_** | (array or None, shape (n_targets,)) Actual number of iterations for each target. Available only for sag and lsqr solvers. Other solvers will return None. .. versionadded:: 0.17 |

See also:

**RidgeClassifier** Ridge classifier

**RidgeCV** Ridge regression with built-in cross validation

**sklearn.kernel_ridge.KernelRidge** Kernel ridge regression combines ridge regression with the kernel trick

Examples

```python
>>> from sklearn.linear_model import Ridge
>>> import numpy as np

>>> n_samples, n_features = 10, 5
>>> np.random.seed(0)

>>> y = np.random.randn(n_samples)

>>> X = np.random.randn(n_samples, n_features)

>>> clf = Ridge(alpha=1.0)

>>> clf.fit(X, y)
Ridge(alpha=1.0, copy_X=True, fit_intercept=True, max_iter=None, normalize=False, random_state=None, solver='auto', tol=0.001)
```

Methods

| **fit(X, y[, sample_weight])** | Fit Ridge regression model |
| **get_params**(deep) | Get parameters for this estimator. |
| **predict**(X) | Predict using the linear model |
| **score**(X, y[, sample_weight]) | Returns the coefficient of determination R^2 of the prediction. |
| **set_params**(**params) | Set the parameters of this estimator. |

```python
__init__(alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=None, tol=0.001, solver='auto', random_state=None)

fit (X, y[, sample_weight=none])
Fit Ridge regression model

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Training data

y : array-like, shape = [n_samples] or [n_samples, n_targets]
Target values
```
sample_weight : float or numpy array of shape [n_samples]

Individual weights for each sample

Returns self : returns an instance of self.

get_params (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

predict (X)

Predict using the linear model

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

Returns C : array, shape = (n_samples,)

Returns predicted values.

score (X, y, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares \(((y_{true} - y_{pred}) ** 2).sum()\) and $v$ is the total sum of squares \(((y_{true} - y_{true}.mean()) ** 2).sum()\). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

Parameters X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

Returns score : float

$R^2$ of self.predict(X) wrt. y.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

Examples using sklearn.linear_model.Ridge

- Compressive sensing: tomography reconstruction with L1 prior (Lasso)
• Prediction Latency
• Plot Ridge coefficients as a function of the regularization
• Plot Ridge coefficients as a function of the L2 regularization
• Ordinary Least Squares and Ridge Regression Variance
• Polynomial interpolation
• HuberRegressor vs Ridge on dataset with strong outliers

30.19.18 sklearn.linear_model.RidgeClassifier

class sklearn.linear_model.RidgeClassifier(alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=None, tol=0.001, class_weight=None, solver='auto', random_state=None)

Classifier using Ridge regression.

Read more in the User Guide.

Parameters

alpha : float

Regularization strength; must be a positive float. Regularization improves the conditioning of the problem and reduces the variance of the estimates. Larger values specify stronger regularization. Alpha corresponds to $C^{-1}$ in other linear models such as LogisticRegression or LinearSVC.

fit_intercept : boolean

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

normalize : boolean, optional, default False

This parameter is ignored when fit_intercept is set to False. If True, the regressors X will be normalized before regression by subtracting the mean and dividing by the l2-norm. If you wish to standardize, please use sklearn.preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

copy_X : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

max_iter : int, optional

Maximum number of iterations for conjugate gradient solver. The default value is determined by scipy.sparse.linalg.

tol : float

Precision of the solution.

class_weight : dict or ‘balanced’, optional

Weights associated with classes in the form {class_label: weight}. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as $n_{samples} / (n_{classes} * \text{np.bincount}(y))$

Solver to use in the computational routines:

- ‘auto’ chooses the solver automatically based on the type of data.
- ‘cholesky’ uses the standard scipy.linalg.solve function to obtain a closed-form solution.
- ‘sparse_cg’ uses the conjugate gradient solver as found in scipy.sparse.linalg.cg. As an iterative algorithm, this solver is more appropriate than ‘cholesky’ for large-scale data (possibility to set tol and max_iter).
- ‘lsqr’ uses the dedicated regularized least-squares routine scipy.sparse.linalg.lsqr. It is the fastest but may not be available in old scipy versions. It also uses an iterative procedure.
- ‘sag’ uses a Stochastic Average Gradient descent, and ‘saga’ uses its unbiased and more flexible version named SAGA. Both methods use an iterative procedure, and are often faster than other solvers when both n_samples and n_features are large. Note that ‘sag’ and ‘saga’ fast convergence is only guaranteed on features with approximately the same scale. You can preprocess the data with a scaler from sklearn.preprocessing.

New in version 0.17: Stochastic Average Gradient descent solver.
New in version 0.19: SAGA solver.

random_state : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == ‘sag’.

Attributes

<table>
<thead>
<tr>
<th>coef_</th>
<th>(array, shape (n_features,) or (n_classes, n_features)) Weight vector(s).</th>
</tr>
</thead>
<tbody>
<tr>
<td>intercept_</td>
<td>(float</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(array or None, shape (n_targets,)) Actual number of iterations for each target. Available only for sag and lsqr solvers. Other solvers will return None.</td>
</tr>
</tbody>
</table>

See also:

Ridge Ridge regression

RidgeClassifierCV Ridge classifier with built-in cross validation

Notes

For multi-class classification, n_class classifiers are trained in a one-versus-all approach. Concretely, this is implemented by taking advantage of the multi-variate response support in Ridge.
Methods

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<tr>
<td>decision_function(X)</td>
<td>Predict confidence scores for samples.</td>
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<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit Ridge regression model.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict class labels for samples in X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__ (alpha=1.0, fit_intercept=True, normalize=False, copy_X=True, max_iter=None, tol=0.001, class_weight=None, solver='auto', random_state=None)

decision_function (X)
Predict confidence scores for samples.

Parameters X: {array-like, sparse matrix}, shape = (n_samples, n_features)

Samples.

Returns array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)

Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

fit (X, y, sample_weight=None)
Fit Ridge regression model.

Parameters X: {array-like, sparse matrix}, shape = [n_samples, n_features]
Training data

y: array-like, shape = [n_samples]
Target values

sample_weight: float or numpy array of shape (n_samples,)
Sample weight.

New in version 0.17: sample_weight support to Classifier.

Returns self: returns an instance of self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any

Parameter names mapped to their values.

predict (X)
Predict class labels for samples in X.

Parameters X: {array-like, sparse matrix}, shape = [n_samples, n_features]
Samples.
**Returns**  
\[ C : \text{array, shape = [n_samples]} \]  
Predicted class label per sample.

**score** \((X, y, \text{sample_weight=\text{None}})\)
Returns the mean accuracy on the given test data and labels.
In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**  
\[ X : \text{array-like, shape = (n_samples, n_features)} \]  
Test samples.
\[ y : \text{array-like, shape = (n_samples)} \text{ or (n_samples, n_outputs)} \]  
True labels for X.
\[ \text{sample_weight} : \text{array-like, shape = [n_samples]}, \text{optional} \]  
Sample weights.

**Returns**  
\[ \text{score} : \text{float} \]  
Mean accuracy of `self.predict(X)` wrt. y.

**set_params** \((**params\))
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
\[ \text{self} \]

**Examples using `sklearn.linear_model.RidgeClassifier`**

- Classification of text documents using sparse features

**30.19.19 sklearn.linear_model.SGDClassifier**

class sklearn.linear_model.SGDClassifier \((\text{loss='hinge'}, \text{ penalty='l2'}, \text{ alpha=0.0001}, \\text{ll\_ratio=0.15, fit\_intercept=True, max\_iter=None}, \text{tol=0.0, shuffle=True, verbose=0, epsilon=0.1, n\_jobs=1, random\_state=None, learning\_rate='optimal', eta0=0.0, power\_t=0.5, class\_weight=None, warm\_start=False, average=False, n\_iter=None)}\)

Linear classifiers (SVM, logistic regression, a.o.) with SGD training.

This estimator implements regularized linear models with stochastic gradient descent (SGD) learning: the gradient of the loss is estimated each sample at a time and the model is updated along the way with a decreasing strength schedule (aka learning rate). SGD allows minibatch (online/out-of-core) learning, see the partial_fit method. For best results using the default learning rate schedule, the data should have zero mean and unit variance.

This implementation works with data represented as dense or sparse arrays of floating point values for the features. The model it fits can be controlled with the loss parameter; by default, it fits a linear support vector machine (SVM).
The regularizer is a penalty added to the loss function that shrinks model parameters towards the zero vector using either the squared euclidean norm L2 or the absolute norm L1 or a combination of both (Elastic Net). If the parameter update crosses the 0.0 value because of the regularizer, the update is truncated to 0.0 to allow for learning sparse models and achieve online feature selection.

Read more in the User Guide.

**Parameters**

- **loss**: str, default: ‘hinge’
  
  The loss function to be used. Defaults to ‘hinge’, which gives a linear SVM.

- **penalty**: str, ‘none’, ‘l2’, ‘l1’, or ‘elasticnet’
  
  The penalty (aka regularization term) to be used. Defaults to ‘l2’ which is the standard regularizer for linear SVM models. ‘l1’ and ‘elasticnet’ might bring sparsity to the model (feature selection) not achievable with ‘l2’.

- **alpha**: float
  
  Constant that multiplies the regularization term. Defaults to 0.0001 Also used to compute learning_rate when set to ‘optimal’.

- **l1_ratio**: float
  
  The Elastic Net mixing parameter, with 0 <= l1_ratio <= 1. l1_ratio=0 corresponds to L2 penalty, l1_ratio=1 to L1. Defaults to 0.15.

- **fit_intercept**: bool
  
  Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.

- **max_iter**: int, optional
  
  The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the fit method, and not the partial_fit. Defaults to 5. Defaults to 1000 from 0.21, or if tol is not None.

- **tol**: float or None, optional
  
  The stopping criterion. If it is not None, the iterations will stop when (loss > previous_loss - tol). Defaults to None. Defaults to 1e-3 from 0.21.

- **shuffle**: bool, optional
  
  Whether or not the training data should be shuffled after each epoch. Defaults to True.

- **verbose**: integer, optional
  
  The verbosity level

- **epsilon**: float
Epsilon in the epsilon-insensitive loss functions; only if loss is ‘huber’, ‘epsilon_insensitive’, or ‘squared_epsilon_insensitive’. For ‘huber’, determines the threshold at which it becomes less important to get the prediction exactly right. For epsilon-insensitive, any differences between the current prediction and the correct label are ignored if they are less than this threshold.

**n_jobs**: integer, optional

The number of CPUs to use to do the OVA (One Versus All, for multi-class problems) computation. -1 means ‘all CPUs’. Defaults to 1.

**random_state**: int, RandomState instance or None, optional (default=None)

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**learning_rate**: string, optional

The learning rate schedule:
- ‘constant’: \( \text{eta} = \text{eta0} \)
- ‘optimal’: \( \text{eta} = \frac{1.0}{\alpha (t + t0)} \) [default]
- ‘invscaling’: \( \text{eta} = \frac{\text{eta0}}{\text{pow}(t, \text{power_t})} \)

where \( t0 \) is chosen by a heuristic proposed by Leon Bottou.

**eta0**: double

The initial learning rate for the ‘constant’ or ‘invscaling’ schedules. The default value is 0.0 as eta0 is not used by the default schedule ‘optimal’.

**power_t**: double

The exponent for inverse scaling learning rate [default 0.5].

**class_weight**: dict, {class_label: weight} or “balanced” or None, optional

Preset for the class_weight fit parameter.

Weights associated with classes. If not given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as \( \frac{n\_samples}{n\_classes \times \text{np.bincount}(y)} \)

**warm_start**: bool, optional

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**average**: bool or int, optional

When set to True, computes the averaged SGD weights and stores the result in the coef_ attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So average=10 will begin averaging after seeing 10 samples.

**n_iter**: int, optional
The number of passes over the training data (aka epochs). Defaults to None. Deprecated, will be removed in 0.21.

Changed in version 0.19: Deprecated

Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>coef_</td>
<td>(array, shape (1, n_features) if n_classes == 2 else (n_classes, n_features)) Weights assigned to the features.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape (1,) if n_classes == 2 else (n_classes,)) Constants in decision function.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) The actual number of iterations to reach the stopping criterion. For multiclass fits, it is the maximum over every binary fit.</td>
</tr>
<tr>
<td>loss_function_</td>
<td>(concrete LossFunction)</td>
</tr>
</tbody>
</table>

See also:

LinearSVC, LogisticRegression, Perceptron

Examples

```python
>>> import numpy as np
>>> from sklearn import linear_model
>>> X = np.array([[-1, -1], [-2, -1], [1, 1], [2, 1]])
>>> Y = np.array([1, 1, 2, 2])
>>> clf = linear_model.SGDClassifier()
>>> clf.fit(X, Y)
...
SGDClassifier(alpha=0.0001, average=False, class_weight=None, epsilon=0.1,
              eta0=0.0, fit_intercept=True, l1_ratio=0.15,
              learning_rate='optimal', loss='hinge', max_iter=None, n_iter=None,
              n_jobs=1, penalty='l2', power_t=0.5, random_state=None,
              shuffle=True, tol=None, verbose=0, warm_start=False)

>>> print(clf.predict([[-0.8, -1]]))
[1]
```

Methods

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<tr>
<td>decision_function(X)</td>
<td>Predict confidence scores for samples.</td>
</tr>
<tr>
<td>densify()</td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td>fit(X, y[, coef_init, intercept_init, ...])</td>
<td>Fit linear model with Stochastic Gradient Descent.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>partial_fit(X, y[, classes, sample_weight])</td>
<td>Fit linear model with Stochastic Gradient Descent.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict class labels for samples in X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(*args, **kwargs)</td>
<td></td>
</tr>
<tr>
<td>sparsify()</td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>
__init__ (loss='hinge', penalty='l2', alpha=0.0001, l1_ratio=0.15, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, epsilon=0.1, n_jobs=1, random_state=None, learning_rate='optimal', eta0=0.0, power_t=0.5, class_weight=None, warm_start=False, average=False, n_iter=None)

decision_function (X)
Predict confidence scores for samples.

The confidence score for a sample is the signed distance of that sample to the hyperplane.

Parameters X : {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.

Returns array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
Confidence scores per (sample, class) combination. In the binary case, confidence score
for self.classes_[1] where >0 means this class would be predicted.

densify ()
Convert coefficient matrix to dense array format.

Converts the coef_ member (back) to a numpy.ndarray. This is the default format of coef_ and is
required for fitting, so calling this method is only required on models that have previously been sparsified;
otherwise, it is a no-op.

Returns self : estimator

fit (X, y, coef_init=None, intercept_init=None, sample_weight=None)
Fit linear model with Stochastic Gradient Descent.

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
Training data

y : numpy array, shape (n_samples,)
Target values

coef_init : array, shape (n_classes, n_features)
The initial coefficients to warm-start the optimization.

intercept_init : array, shape (n_classes,)
The initial intercept to warm-start the optimization.

sample_weight : array-like, shape (n_samples,), optional
Weights applied to individual samples. If not provided, uniform weights are assumed.
These weights will be multiplied with class_weight (passed through the constructor) if
class_weight is specified.

Returns self : returns an instance of self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.
loss_function
DEPRECATED: Attribute loss_function was deprecated in version 0.19 and will be removed in 0.21. Use loss_function_ instead

partial_fit (X, y, classes=None, sample_weight=None)
Fit linear model with Stochastic Gradient Descent.

Parameters
X : {array-like, sparse matrix}, shape (n_samples, n_features)
Subset of the training data

y : numpy array, shape (n_samples,)
Subset of the target values

classes : array, shape (n_classes,)
Classes across all calls to partial_fit. Can be obtained by via np.unique(y_all), where y_all is the target vector of the entire dataset. This argument is required for the first call to partial_fit and can be omitted in the subsequent calls. Note that y doesn’t need to contain all labels in classes.

sample_weight : array-like, shape (n_samples,), optional
Weights applied to individual samples. If not provided, uniform weights are assumed.

Returns
self : returns an instance of self.

predict (X)
Predict class labels for samples in X.

Parameters
X : {array-like, sparse matrix}, shape = [n_samples, n_features]
Samples.

Returns
C : array, shape = [n_samples]
Predicted class label per sample.

predict_log_proba
Log of probability estimates.

This method is only available for log loss and modified Huber loss.

When loss=”modified_huber”, probability estimates may be hard zeros and ones, so taking the logarithm is not possible.

See predict_proba for details.

Parameters
X : array-like, shape (n_samples, n_features)

Returns
T : array-like, shape (n_samples, n_classes)
Returns the log-probability of the sample for each class in the model, where classes are ordered as they are in self.classes_.

predict_proba
Probability estimates.

This method is only available for log loss and modified Huber loss.

Multiclass probability estimates are derived from binary (one-vs.-rest) estimates by simple normalization, as recommended by Zadrozny and Elkan.

Binary probability estimates for loss=”modified_huber” are given by (clip(decision_function(X), -1, 1) + 1) / 2. For other loss functions it is necessary to perform proper probability calibration by wrapping the classifier with sklearn.calibration.CalibratedClassifierCV instead.
Parameters $X$ : {array-like, sparse matrix}, shape (n_samples, n_features)

Returns array, shape (n_samples, n_classes)

Returns the probability of the sample for each class in the model, where classes are ordered as they are in self.classes_.

References


The justification for the formula in the loss=’modified_huber’ case is in the appendix B in: http://jmlr.csail.mit.edu/papers/volume2/zhang02c/zhang02c.pdf

score$(X, y, sample_weight=None)$

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters $X$ : array-like, shape = (n_samples, n_features)

Test samples.

$y$ : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

Returns score : float

Mean accuracy of self.predict(X) wrt. y.

sparsify()  

Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

Returns self : estimator

Notes

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef_ == 0).sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

Examples using sklearn.linear_model.SGDClassifier

• Model Complexity Influence
• Out-of-core classification of text documents
• SGD: Maximum margin separating hyperplane
• SGD: Weighted samples
• Comparing various online solvers
• Plot multi-class SGD on the iris dataset
• Sample pipeline for text feature extraction and evaluation
• Classification of text documents using sparse features

30.19.20 sklearn.linear_model.SGDRegressor

```python
class sklearn.linear_model.SGDRegressor(loss='squared_loss', penalty='l2', alpha=0.0001, l1_ratio=0.15, fit_intercept=True, max_iter=None, tol=None, shuffle=True, verbose=0, epsilon=0.1, random_state=None, learning_rate='invscaling', eta0=0.01, power_t=0.25, warm_start=False, average=False, n_iter=None)
```

Linear model fitted by minimizing a regularized empirical loss with SGD

SGD stands for Stochastic Gradient Descent: the gradient of the loss is estimated each sample at a time and the model is updated along the way with a decreasing strength schedule (aka learning rate).

The regularizer is a penalty added to the loss function that shrinks model parameters towards the zero vector using either the squared euclidean norm L2 or the absolute norm L1 or a combination of both (Elastic Net). If the parameter update crosses the 0.0 value because of the regularizer, the update is truncated to 0.0 to allow for learning sparse models and achieve online feature selection.

This implementation works with data represented as dense numpy arrays of floating point values for the features.

Read more in the User Guide.

**Parameters**

- **loss** : str, default: ‘squared_loss’
  
  The loss function to be used. The possible values are ‘squared_loss’, ‘huber’, ‘epsilon_insensitive’, or ‘squared_epsilon_insensitive’

  The ‘squared_loss’ refers to the ordinary least squares fit. ‘huber’ modifies ‘squared_loss’ to focus less on getting outliers correct by switching from squared to linear loss past a distance of epsilon. ‘epsilon_insensitive’ ignores errors less than epsilon and is linear past that; this is the loss function used in SVR. ‘squared_epsilon_insensitive’ is the same but becomes squared loss past a tolerance of epsilon.

- **penalty** : str, ‘none’, ‘l2’, ‘l1’, or ‘elasticnet’

  The penalty (aka regularization term) to be used. Defaults to ‘l2’ which is the standard regularizer for linear SVM models. ‘l1’ and ‘elasticnet’ might bring sparsity to the model (feature selection) not achievable with ‘l2’.

- **alpha** : float

  Constant that multiplies the regularization term. Defaults to 0.0001 Also used to compute learning_rate when set to ‘optimal’.

- **l1_ratio** : float

  The Elastic Net mixing parameter, with 0 <= l1_ratio <= 1. l1_ratio=0 corresponds to L2 penalty, l1_ratio=1 to L1. Defaults to 0.15.

- **fit_intercept** : bool
Whether the intercept should be estimated or not. If False, the data is assumed to be already centered. Defaults to True.

**max_iter** : int, optional
The maximum number of passes over the training data (aka epochs). It only impacts the behavior in the `fit` method, and not the `partial_fit`. Defaults to 5. Defaults to 1000 from 0.21, or if tol is not None.

New in version 0.19.

**tol** : float or None, optional
The stopping criterion. If it is not None, the iterations will stop when (loss > previous_loss - tol). Defaults to None. Defaults to 1e-3 from 0.21.

New in version 0.19.

**shuffle** : bool, optional
Whether or not the training data should be shuffled after each epoch. Defaults to True.

**verbose** : integer, optional
The verbosity level.

**epsilon** : float
Epsilon in the epsilon-insensitive loss functions; only if `loss` is ‘huber’, ‘epsilon_insensitive’, or ‘squared_epsilon_insensitive’. For ‘huber’, determines the threshold at which it becomes less important to get the prediction exactly right. For epsilon-insensitive, any differences between the current prediction and the correct label are ignored if they are less than this threshold.

**random_state** : int, RandomState instance or None, optional (default=None)
The seed of the pseudo random number generator to use when shuffling the data. If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**learning_rate** : string, optional
The learning rate schedule:

- ‘constant’: \( \eta = \eta_0 \)
- ‘optimal’: \( \eta = 1.0 / (\alpha (t + t_0)) \)
- ‘invscaling’: \( \eta = \eta_0 / \text{pow}(t, \text{power}_t) \) [default]

where \( t_0 \) is chosen by a heuristic proposed by Leon Bottou.

**eta0** : double, optional
The initial learning rate [default 0.01].

**power_t** : double, optional
The exponent for inverse scaling learning rate [default 0.25].

**warm_start** : bool, optional
When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**average** : bool or int, optional
When set to True, computes the averaged SGD weights and stores the result in the `coef_` attribute. If set to an int greater than 1, averaging will begin once the total number of samples seen reaches average. So `average=10` will begin averaging after seeing 10 samples.

**n_iter** : int, optional

The number of passes over the training data (aka epochs). Defaults to None. Deprecated, will be removed in 0.21.

Changed in version 0.19: Deprecated

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>coef_</code></td>
<td>(array, shape (n_features,)) Weights assigned to the features.</td>
</tr>
<tr>
<td><code>intercept_</code></td>
<td>(array, shape (1,)) The intercept term.</td>
</tr>
<tr>
<td><code>average_coef_</code></td>
<td>(array, shape (n_features,)) Averaged weights assigned to the features.</td>
</tr>
<tr>
<td><code>average_intercept_</code></td>
<td>(array, shape (1,)) The averaged intercept term.</td>
</tr>
<tr>
<td><code>n_iter_</code></td>
<td>(int) The actual number of iterations to reach the stopping criterion.</td>
</tr>
</tbody>
</table>

**See also:**

`Ridge`, `ElasticNet`, `Lasso`, `SVR`

**Examples**

```python
>>> import numpy as np
>>> from sklearn import linear_model
>>> n_samples, n_features = 10, 5
>>> np.random.seed(0)
>>> y = np.random.randn(n_samples)
>>> X = np.random.randn(n_samples, n_features)
>>> clf = linear_model.SGDRegressor()
>>> clf.fit(X, y)
... SGDRegressor(alpha=0.0001, average=False, epsilon=0.1, eta0=0.01,
              fit_intercept=True, l1_ratio=0.15, learning_rate='invscaling',
              loss='squared_loss', max_iter=None, n_iter=None, penalty='l2',
              power_t=0.25, random_state=None, shuffle=True, tol=None,
              verbose=0, warm_start=False)
```

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td><code>densify()</code></td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td><code>fit(X, y[, coef_init, intercept_init, ...])</code></td>
<td>Fit linear model with Stochastic Gradient Descent.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>partial_fit(X, y[, sample_weight])</code></td>
<td>Fit linear model with Stochastic Gradient Descent.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
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</table>

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<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td>set_params(*)</td>
<td>set_params(**kwargs)</td>
</tr>
<tr>
<td>sparsify()</td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>

__init__

```
(loss='squared_loss', penalty='l2', alpha=0.0001, l1_ratio=0.15, fit_intercept=True,
 max_iter=None, tol=None, shuffle=True, verbose=0, epsilon=0.1, random_state=None,
 learning_rate='invscaling', eta0=0.01, power_t=0.25, warm_start=False, average=False,
 n_iter=None)
```

densify()

Converts the `coef_` member (back) to a numpy.ndarray. This is the default format of `coef_` and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

Returns

`self` : estimator

fit(X, y, coef_init=None, intercept_init=None, sample_weight=None)

Fit linear model with Stochastic Gradient Descent.

Parameters

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  - Training data
- **y**: numpy array, shape (n_samples,)
  - Target values
- **coef_init**: array, shape (n_features,)
  - The initial coefficients to warm-start the optimization.
- **intercept_init**: array, shape (1,)
  - The initial intercept to warm-start the optimization.
- **sample_weight**: array-like, shape (n_samples,), optional
  - Weights applied to individual samples (1. for unweighted).

Returns

`self` : returns an instance of self.

get_params(deep=True)

Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

`params` : mapping of string to any
- Parameter names mapped to their values.

partial_fit(X, y, sample_weight=None)

Fit linear model with Stochastic Gradient Descent.

Parameters

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  - Subset of training data
- **y**: numpy array of shape (n_samples,)
  - Subset of target values
- **sample_weight**: array-like, shape (n_samples,), optional
  - Weights applied to individual samples (1. for unweighted).
Weights applied to individual samples. If not provided, uniform weights are assumed.

**Returns** self : returns an instance of self.

**predict** *(X)*
Predict using the linear model

**Parameters** X : {array-like, sparse matrix}, shape (n_samples, n_features)

**Returns** array, shape (n_samples,)
Predicted target values per element in X.

**score** *(X, y, sample_weight=None)*
Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred}) \times 2).sum()$ and $v$ is the total sum of squares $((y_{true} - y_{true}.mean()) \times 2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters** X : array-like, shape = (n_samples, n_features)
Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True values for X.

**sample_weight** : array-like, shape = [n_samples], optional
Sample weights.

**Returns** score : float
$R^2$ of self.predict(X) wrt. $y$.

**sparsify** *
Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

**Returns** self : estimator

**Notes**

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with (coef_ == 0).sum(), must be more than 50% for this to provide significant benefits.

After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

**Examples using sklearn.linear_model.SGDRegressor**

- Prediction Latency
**30.19.21 sklearn.linear_model.TheilSenRegressor**

```python
class sklearn.linear_model.TheilSenRegressor(fit_intercept=True, copy_X=True, max_subpopulation=1e4, n_subsamples=None, max_iter=300, tol=0.001, random_state=None, n_jobs=1, verbose=False)
```

Theil-Sen Estimator: robust multivariate regression model.

The algorithm calculates least square solutions on subsets with size n_subsamples of the samples in X. Any value of n_subsamples between the number of features and samples leads to an estimator with a compromise between robustness and efficiency. Since the number of least square solutions is “n_samples choose n_subsamples”, it can be extremely large and can therefore be limited with max_subpopulation. If this limit is reached, the subsets are chosen randomly. In a final step, the spatial median (or L1 median) is calculated of all least square solutions. Read more in the User Guide.

**Parameters**

- `fit_intercept` : boolean, optional, default True
  Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations.

- `copy_X` : boolean, optional, default True
  If True, X will be copied; else, it may be overwritten.

- `max_subpopulation` : int, optional, default 1e4
  Instead of computing with a set of cardinality ‘n choose k’, where n is the number of samples and k is the number of subsamples (at least number of features), consider only a stochastic subpopulation of a given maximal size if ‘n choose k’ is larger than max_subpopulation. For other than small problem sizes this parameter will determine memory usage and runtime if n_subsamples is not changed.

- `n_subsamples` : int, optional, default None
  Number of samples to calculate the parameters. This is at least the number of features (plus 1 if fit_intercept=True) and the number of samples as a maximum. A lower number leads to a higher breakdown point and a low efficiency while a high number leads to a low breakdown point and a high efficiency. If None, take the minimum number of subsamples leading to maximal robustness. If n_subsamples is set to n_samples, Theil-Sen is identical to least squares.

- `max_iter` : int, optional, default 300
  Maximum number of iterations for the calculation of spatial median.

- `tol` : float, optional, default 1.e-3
  Tolerance when calculating spatial median.

- `random_state` : int, RandomState instance or None, optional, default None
  A random number generator instance to define the state of the random permutations generator. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

- `n_jobs` : integer, optional, default 1
  Number of CPUs to use during the cross validation. If -1, use all the CPUs.

- `verbose` : boolean, optional, default False
Verbose mode when fitting the model.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>coef</strong></td>
<td>(array, shape = (n_features)) Coefficients of the regression model (median of distribution).</td>
</tr>
<tr>
<td><strong>intercept</strong></td>
<td>(float) Estimated intercept of regression model.</td>
</tr>
<tr>
<td><strong>breakdown</strong></td>
<td>(float) Approximated breakdown point.</td>
</tr>
<tr>
<td><strong>n_iter</strong></td>
<td>(int) Number of iterations needed for the spatial median.</td>
</tr>
<tr>
<td><strong>n_subpopulation</strong></td>
<td>Number of combinations taken into account from ‘n choose k’, where n is the number of samples and k is the number of subsamples.</td>
</tr>
</tbody>
</table>

**References**


**Methods**

- **fit(X, y)** Fit linear model.
- **get_params([deep])** Get parameters for this estimator.
- **predict(X)** Predict using the linear model.
- **score(X, y[, sample_weight])** Returns the coefficient of determination $R^2$ of the prediction.
- **set_params(**params**)** Set the parameters of this estimator.

**init**(fit_intercept=True, copy_X=True, max_subpopulation=10000.0, n_subsamples=None, max_iter=300, tol=0.001, random_state=None, n_jobs=1, verbose=False)

**fit**(X, y)
Fit linear model.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  - Training data
- **y**: numpy array of shape [n_samples]
  - Target values

**Returns**

- **self**: returns an instance of self.

**get_params**(deep=True)
Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.
predict \((X)\)
Predict using the linear model

**Parameters**
- \(X\) : {array-like, sparse matrix}, shape \(=(n_{\text{samples}}, n_{\text{features}})\)
  - Samples.

**Returns**
- \(C\) : array, shape \(=(n_{\text{samples}},)\)
  - Returns predicted values.

score \((X, y, \text{sample\_weight}={\text{None}})\)
Returns the coefficient of determination \(R^2\) of the prediction.

The coefficient \(R^2\) is defined as \(1 - \frac{u}{v}\), where \(u\) is the residual sum of squares \(\sum((y_{\text{true}} - y_{\text{pred}})^2)\) and \(v\) is the total sum of squares \(\sum((y_{\text{true}} - y_{\text{true}}.\text{mean})^2)\). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \(y\), disregarding the input features, would get a \(R^2\) score of 0.0.

**Parameters**
- \(X\) : array-like, shape \(=(n_{\text{samples}}, n_{\text{features}})\)
  - Test samples.
- \(y\) : array-like, shape \(=(n_{\text{samples}})\) or \(=(n_{\text{samples}}, n_{\text{outputs}})\)
  - True values for \(X\).
- \(\text{sample\_weight}\) : array-like, shape \(=[n_{\text{samples}}]\), optional
  - Sample weights.

**Returns**
- score : float
  - \(R^2\) of \(\text{self.predict}(X)\) wrt. \(y\).

set_params (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>__<\text{parameter}>\) so that it’s possible to update each component of a nested object.

**Returns**
- self

Examples using `sklearn.linear_model.TheilSenRegressor`

- **Theil-Sen Regression**
- **Robust linear estimator fitting**

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>linear_model.elnet_path(X, y[, l1_ratio, ...])</code></td>
<td>Compute elastic net path with coordinate descent</td>
</tr>
<tr>
<td><code>linear_model.lars_path(X, y[, Xy, Gram, ...])</code></td>
<td>Compute Least Angle Regression or Lasso path using LARS algorithm [1]</td>
</tr>
<tr>
<td><code>linear_model.lasso_path(X, y[, eps, ...])</code></td>
<td>Compute Lasso path with coordinate descent</td>
</tr>
<tr>
<td><code>linear_model.lasso_stability_path(X, y[, ...])</code></td>
<td>DEPRECATED: The function lasso_stability_path is deprecated in 0.19 and will be removed in 0.21.</td>
</tr>
<tr>
<td><code>linear_model.logistic_regression_path(X, y)</code></td>
<td>Compute a Logistic Regression model for a list of regularization parameters.</td>
</tr>
<tr>
<td><code>linear_model.orthogonal_mp(X[, y[, ...]])</code></td>
<td>Orthogonal Matching Pursuit (OMP)</td>
</tr>
<tr>
<td><code>linear_model.orthogonal_mp_gram(Gram, Xy[, ...])</code></td>
<td>Gram Orthogonal Matching Pursuit (OMP)</td>
</tr>
</tbody>
</table>
**30.19.22 sklearn.linear_model.enet_path**

sklearn.linear_model.enet_path(X, y, l1_ratio=0.5, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, check_input=True, **params)

Compute elastic net path with coordinate descent

The elastic net optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{(2 \times n_{samples})} \times ||y - Xw||^2_2
+ \alpha \times l1\_ratio \times ||w||_1
+ 0.5 \times \alpha \times (1 - l1\_ratio) \times ||w||^2_2
\]

For multi-output tasks it is:

\[
\frac{1}{(2 \times n_{samples})} \times ||Y - XW||^\text{Fro}_2
+ \alpha \times l1\_ratio \times ||W||_21
+ 0.5 \times \alpha \times (1 - l1\_ratio) \times ||W||_\text{Fro}^2
\]

Where:

\[||W||_21 = \sum_i \sqrt{\sum_j w_{ij}^2}\]

i.e. the sum of norm of each row.

Read more in the User Guide.

**Parameters**

X : {array-like}, shape (n_samples, n_features)

Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.

y : ndarray, shape (n_samples,) or (n_samples, n_outputs)

Target values

l1_ratio : float, optional

float between 0 and 1 passed to elastic net (scaling between l1 and l2 penalties). l1_ratio=1 corresponds to the Lasso

eps : float

Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3

n_alphas : int, optional

Number of alphas along the regularization path

alphas : ndarray, optional

List of alphas where to compute the models. If None alphas are set automatically

precompute : True | False | 'auto' | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to 'auto', let us decide. The Gram matrix can also be passed as argument.

Xy : array-like, optional

Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.
**copy_X** : boolean, optional, default True

If True, X will be copied; else, it may be overwritten.

**coef_init** : array, shape (n_features,) | None

The initial values of the coefficients.

**verbose** : bool or integer

Amount of verbosity.

**return_n_iter** : bool

whether to return the number of iterations or not.

**positive** : bool, default False

If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**check_input** : bool, default True

Skip input validation checks, including the Gram matrix when provided assuming there are handled by the caller when check_input=False.

**params** : kwargs

keyword arguments passed to the coordinate descent solver.

**Returns**

**alphas** : array, shape (n_alphas,)

The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iter**s : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha. (Is returned when return_n_iter is set to True).

**See also:**

`MultiTaskElasticNet`, `MultiTaskElasticNetCV`, `ElasticNet`, `ElasticNetCV`

**Notes**

For an example, see `examples/linear_model/plot_lasso_coordinate_descent_path.py`.

**Examples using `sklearn.linear_model.enet_path`**

- *Lasso and Elastic Net*
**30.19.23 sklearn.linear_model.lars_path**

```python
sklearn.linear_model.lars_path(X, y, Xy=None, Gram=None, max_iter=500, alpha_min=0,
method='lar', copy_X=True, eps=2.220446049250313e-16, copy_Gram=True, verbose=0, return_path=True, return_n_iter=False, positive=False)
```

Compute Least Angle Regression or Lasso path using LARS algorithm [1]

The optimization objective for the case method='lasso' is:

\[ \frac{1}{2n} ||y - Xw||^2_2 + \alpha ||w||_1 \]

in the case of method='lar', the objective function is only known in the form of an implicit equation (see discussion in [1])

Read more in the User Guide.

**Parameters**

- **X**: array, shape: (n_samples, n_features)
  - Input data.
- **y**: array, shape: (n_samples)
  - Input targets.
- **Xy**: array-like, shape (n_samples,) or (n_samples, n_targets), optional
  - Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.
- **Gram**: None, ‘auto’, array, shape: (n_features, n_features), optional
  - Precomputed Gram matrix (X' * X), if ‘auto’, the Gram matrix is precomputed from the given X, if there are more samples than features.
- **max_iter**: integer, optional (default=500)
  - Maximum number of iterations to perform, set to infinity for no limit.
- **alpha_min**: float, optional (default=0)
  - Minimum correlation along the path. It corresponds to the regularization parameter alpha parameter in the Lasso.
- **method**: {'lar', 'lasso'}, optional (default='lar')
  - Specifies the returned model. Select 'lar' for Least Angle Regression, 'lasso' for the Lasso.
- **copy_X**: bool, optional (default=True)
  - If False, X is overwritten.
- **eps**: float, optional (default='np.finfo(np.float).eps')
  - The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems.
- **copy_Gram**: bool, optional (default=True)
  - If False, Gram is overwritten.
- **verbose**: int (default=0)
  - Controls output verbosity.
- **return_path**: bool, optional (default=True)
If `return_path==True` returns the entire path, else returns only the last point of the path.

**return_n_iter:** bool, optional (default=False)

Whether to return the number of iterations.

**positive:** boolean (default=False)

Restrict coefficients to be \( \geq 0 \). When using this option together with method ‘lasso’ the model coefficients will not converge to the ordinary-least-squares solution for small values of alpha (neither will they when using method ‘lar’ ..). Only coefficients up to the smallest alpha value \( \text{alphas}_{[\text{alphas}_ > 0.].\text{min()}} \) reached by the stepwise Lars-Lasso algorithm are typically in congruence with the solution of the coordinate descent lasso_path function.

**Returns**

**alphas:** array, shape: \([n\_alphas + 1]\)

Maximum of covariances (in absolute value) at each iteration. \( n\_alphas \) is either \( \text{max\_iter}, \text{n\_features} \) or the number of nodes in the path with \( \alpha \geq \alpha_{\text{min}} \), whichever is smaller.

**active:** array, shape \([n\_alphas]\)

Indices of active variables at the end of the path.

**coefs:** array, shape \((\text{n\_features, n\_alphas} + 1)\)

Coefficients along the path

**n_iter:** int

Number of iterations run. Returned only if return_n_iter is set to True.

See also:

- lasso_path
- LassoLars
- Lars
- LassoLarsCV
- LarsCV
- sklearn.decomposition.sparse_encode

References

[R115117], [R116117], [R117117]

**Examples using sklearn.linear_model.lars_path**

- Lasso path using LARS

30.19.24 sklearn.linear_model.lasso_path

sklearn.linear_model.lasso_path(X, y, eps=0.001, n_alphas=100, alphas=None, precompute='auto', Xy=None, copy_X=True, coef_init=None, verbose=False, return_n_iter=False, positive=False, **params)

Compute Lasso path with coordinate descent

The Lasso optimization function varies for mono and multi-outputs.

For mono-output tasks it is:

\[
\frac{1}{2n_{\text{samples}}} \times ||y - Xw||^2_2 + \alpha \times ||w||_1
\]
For multi-output tasks it is:

\[
\frac{1}{(2 \times n_{\text{samples}})} \times ||Y - XW||^2_{\text{Fro}} + \alpha \times ||W||_{2,1}
\]

Where:

\[
||W||_{2,1} = \sum_i \sqrt{\sum_j w_{ij}^2}
\]

i.e. the sum of norm of each row.

Read more in the User Guide.

Parameters

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  - Training data. Pass directly as Fortran-contiguous data to avoid unnecessary memory duplication. If y is mono-output then X can be sparse.
- **y**: ndarray, shape (n_samples,), or (n_samples, n_outputs)
  - Target values
- **eps**: float, optional
  - Length of the path. eps=1e-3 means that alpha_min / alpha_max = 1e-3
- **n_alphas**: int, optional
  - Number of alphas along the regularization path
- **alphas**: ndarray, optional
  - List of alphas where to compute the models. If None alphas are set automatically
- **precompute**: True | False | ‘auto’ | array-like
  - Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix can also be passed as argument.
- **Xy**: array-like, optional
  - Xy = np.dot(X.T, y) that can be precomputed. It is useful only when the Gram matrix is precomputed.
- **copy_X**: boolean, optional, default True
  - If True, X will be copied; else, it may be overwritten.
- **coef_init**: array, shape (n_features,) | None
  - The initial values of the coefficients.
- **verbose**: bool or integer
  - Amount of verbosity.
- **return_n_iter**: bool
  - whether to return the number of iterations or not.
- **positive**: bool, default False
  - If set to True, forces coefficients to be positive. (Only allowed when y.ndim == 1).

**params**: kwargs
- keyword arguments passed to the coordinate descent solver.

Returns

- **alphas**: array, shape (n_alphas,)
The alphas along the path where models are computed.

**coefs** : array, shape (n_features, n_alphas) or (n_outputs, n_features, n_alphas)

Coefficients along the path.

**dual_gaps** : array, shape (n_alphas,)

The dual gaps at the end of the optimization for each alpha.

**n_iters** : array-like, shape (n_alphas,)

The number of iterations taken by the coordinate descent optimizer to reach the specified tolerance for each alpha.

See also:

*lars_path*, *Lasso*, *LassoLars*, *LassoCV*, *LassoLarsCV*, *sklearn.decomposition.sparse_encode*

Notes

For an example, see `examples/linear_model/plot_lasso_coordinate_descent_path.py`.

To avoid unnecessary memory duplication the X argument of the fit method should be directly passed as a Fortran-contiguous numpy array.

Note that in certain cases, the Lars solver may be significantly faster to implement this functionality. In particular, linear interpolation can be used to retrieve model coefficients between the values output by lars_path.

Examples

Comparing lasso_path and lars_path with interpolation:

```python
>>> X = np.array([[1, 2, 3.1], [2.3, 5.4, 4.3]]).T
>>> y = np.array([1, 2, 3.1])
>>> # Use lasso_path to compute a coefficient path
>>> _, coef_path, _ = lasso_path(X, y, alphas=[5., 1., .5])
>>> print(coef_path)
[[ 0. 0. 0.46874778]
 [ 0.2159048 0.4425765 0.23689075]]
>>> # Now use lars_path and 1D linear interpolation to compute the
>>> # same path
>>> from sklearn.linear_model import lars_path
>>> from scipy import interpolate
>>> alphas, active, coef_path_lars = lars_path(X, y, method='lasso')
>>> coef_path_continuous = interpolate.interp1d(alphas[::-1],
...     coef_path_lars[:, ::-1])
>>> print(coef_path_continuous([5., 1., .5]))
[[ 0. 0. 0.46915237]
 [ 0.2159048 0.4425765 0.23668876]]
```

Examples using `sklearn.linear_model.lasso_path`

- *Lasso and Elastic Net*
30.19.25 sklearn.linear_model.lasso_stability_path

sklearn.linear_model.lasso_stability_path(X, y, scaling=0.5, random_state=None, n_resampling=200, n_grid=100, sample_fraction=0.75, eps=8.881784197001252e-16, n_jobs=1, verbose=False)

DEPRECATED: The function lasso_stability_path is deprecated in 0.19 and will be removed in 0.21.

Stability path based on randomized Lasso estimates

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training data.

- **y**: array-like, shape = [n_samples] target values.

- **scaling**: [float, optional, default=0.5] The alpha parameter in the stability selection article used to randomly scale the features. Should be between 0 and 1.

- **random_state**: [int, RandomState instance or None, optional, default=None] The generator used to randomize the design. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

- **n_resampling**: [int, optional, default=200] Number of randomized models.

- **n_grid**: [int, optional, default=100] Number of grid points. The path is linearly interpolated on a grid between 0 and 1 before computing the scores.

- **sample_fraction**: [float, optional, default=0.75] The fraction of samples to be used in each randomized design. Should be between 0 and 1. If 1, all samples are used.

- **eps**: [float, optional] Smallest value of alpha / alpha_max considered

- **n_jobs**: [integer, optional] Number of CPUs to use during the resampling. If ‘-1’, use all the CPUs

- **verbose**: [boolean or integer, optional] Sets the verbosity amount

**Returns**

- **alphas_grid**: array, shape ~ [n_grid]
  
  The grid points between 0 and 1: alpha/alpha_max

- **scores_path**: [array, shape = [n_features, n_grid]] The scores for each feature along the path.

30.19. sklearn.linear_model: Generalized Linear Models
30.19.26 sklearn.linear_model.logistic_regression_path

**sklearn.linear_model.logistic_regression_path** *(X, y, pos_class=None, Cs=10, fit_intercept=True, max_iter=100, tol=0.0001, verbose=0, solver='lbfgs', coef=None, class_weight=None, dual=False, penalty='l2', intercept_scaling=1.0, multi_class='ovr', random_state=None, check_input=True, max_squared_sum=None, sample_weight=None)*

Compute a Logistic Regression model for a list of regularization parameters.

This is an implementation that uses the result of the previous model to speed up computations along the set of solutions, making it faster than sequentially calling LogisticRegression for the different parameters. Note that there will be no speedup with liblinear solver, since it does not handle warm-starting.

Read more in the *User Guide*.

**Parameters**

- **X**: array-like or sparse matrix, shape (n_samples, n_features)
  - Input data.

- **y**: array-like, shape (n_samples,)
  - Input data, target values.

- **pos_class**: int, None
  - The class with respect to which we perform a one-vs-all fit. If None, then it is assumed that the given problem is binary.

- **Cs**: int | array-like, shape (n_cs,)
  - List of values for the regularization parameter or integer specifying the number of regularization parameters that should be used. In this case, the parameters will be chosen in a logarithmic scale between 1e-4 and 1e4.

- **fit_intercept**: bool
  - Whether to fit an intercept for the model. In this case the shape of the returned array is (n_cs, n_features + 1).

- **max_iter**: int
  - Maximum number of iterations for the solver.

- **tol**: float
  - Stopping criterion. For the newton-cg and lbfgs solvers, the iteration will stop when \( \max\{|g_i| \mid i = 1, \ldots, n\} \leq tol \) where \( g_i \) is the i-th component of the gradient.

- **verbose**: int
  - For the liblinear and lbfgs solvers set verbose to any positive number for verbosity.

- **solver**: {'lbfgs', 'newton-cg', 'liblinear', 'sag', 'saga'}
  - Numerical solver to use.

- **coef**: array-like, shape (n_features,), default None
  - Initialization value for coefficients of logistic regression. Useless for liblinear solver.

- **class_weight**: dict or ‘balanced’, optional
Weights associated with classes in the form {class_label: weight}. If not
given, all classes are supposed to have weight one.

The “balanced” mode uses the values of y to automatically adjust weights inversely
proportional to class frequencies in the input data as n_samples / (n_classes
* np.bincount(y)).

Note that these weights will be multiplied with sample_weight (passed through the fit
method) if sample_weight is specified.

dual : bool

Dual or primal formulation. Dual formulation is only implemented for l2 penalty with
liblinear solver. Prefer dual=False when n_samples > n_features.

penalty : str, ‘l1’ or ‘l2’

Used to specify the norm used in the penalization. The ‘newton-cg’, ‘sag’ and ‘lbfgs’
solvers support only l2 penalties.

intercept_scaling : float, default 1.

Useful only when the solver ‘liblinear’ is used and self.fit_intercept is set to True. In this
case, x becomes [x, self.intercept_scaling], i.e. a “synthetic” feature with constant value
equal to intercept_scaling is appended to the instance vector. The intercept becomes
intercept_scaling * synthetic_feature_weight.

Note! the synthetic feature weight is subject to l1/l2 regularization as all other features.
To lessen the effect of regularization on synthetic feature weight (and therefore on the
intercept) intercept_scaling has to be increased.

multi_class : str, {'ovr', 'multinomial'}

Multiclass option can be either ‘ovr’ or ‘multinomial’. If the option chosen is ‘ovr’, then
a binary problem is fit for each label. Else the loss minimised is the multinomial loss
fit across the entire probability distribution. Works only for the ‘lbfgs’ and ‘newton-cg’
solvers.

random_state : int, RandomState instance or None, optional, default None

The seed of the pseudo random number generator to use when shuffling the data. If
int, random_state is the seed used by the random number generator; If RandomState
instance, random_state is the random number generator; If None, the random number
generator is the RandomState instance used by np.random. Used when solver ==
’sag’ or ‘liblinear’.

check_input : bool, default True

If False, the input arrays X and y will not be checked.

max_squared_sum : float, default None

Maximum squared sum of X over samples. Used only in SAG solver. If None, it will
be computed, going through all the samples. The value should be precomputed to speed
up cross validation.

sample_weight : array-like, shape(n_samples,) optional

Array of weights that are assigned to individual samples. If not provided, then each
sample is given unit weight.

Returns coefs : ndarray, shape (n_cs, n_features) or (n_cs, n_features + 1)
List of coefficients for the Logistic Regression model. If fit_intercept is set to True then the second dimension will be n_features + 1, where the last item represents the intercept.

Cs : ndarray
Grid of Cs used for cross-validation.

n_iter : array, shape (n_cs,)
Actual number of iteration for each Cs.

**Notes**

You might get slightly different results with the solver liblinear than with the others since this uses LIBLINEAR which penalizes the intercept.

Changed in version 0.19: The "copy" parameter was removed.

### 30.19.27 sklearn.linear_model.orthogonal_mp

**sklearn.linear_model.orthogonal_mp** *(X, y, n_nonzero_coefs=None, tol=None, precompute=False, copy_X=True, return_path=False, return_n_iter=False)*

Orthogonal Matching Pursuit (OMP)

Solves n_targets Orthogonal Matching Pursuit problems. An instance of the problem has the form:

When parametrized by the number of non-zero coefficients using n_nonzero_coefs: argmin ||y - Xgamma||^2 subject to ||gamma||_0 <= n_{nonzero coefs}

When parametrized by error using the parameter tol: argmin ||gamma||_0 subject to ||y - Xgamma||^2 <= tol

Read more in the *User Guide*.

**Parameters**

- **X** : array, shape (n_samples, n_features)
  
  Input data. Columns are assumed to have unit norm.

- **y** : array, shape (n_samples,) or (n_samples, n_targets)
  
  Input targets

- **n_nonzero_coefs** : int
  
  Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n_features.

- **tol** : float
  
  Maximum norm of the residual. If not None, overrides n_nonzero_coefs.

- **precompute** : {True, False, ‘auto’},
  
  Whether to perform precomputations. Improves performance when n_targets or n_samples is very large.

- **copy_X** : bool, optional
  
  Whether the design matrix X must be copied by the algorithm. A false value is only helpful if X is already Fortran-ordered, otherwise a copy is made anyway.

- **return_path** : bool, optional. Default: False
Whether to return every value of the nonzero coefficients along the forward path. Useful for cross-validation.

**return_n_iter**: bool, optional default False

Whether or not to return the number of iterations.

**Returns coef**: array, shape (n_features,) or (n_features, n_targets)

Coefficients of the OMP solution. If *return_path=True*, this contains the whole coefficient path. In this case its shape is (n_features, n_features) or (n_features, n_targets, n_features) and iterating over the last axis yields coefficients in increasing order of active features.

**n_iter**: array-like or int

Number of active features across every target. Returned only if *return_n_iter* is set to True.

**See also:**

OrthogonalMatchingPursuit, orthogonal_mp_gram, lars_path, decomposition, sparse_encode

**Notes**


**30.19.28 sklearn.linear_model.orthogonal_mp_gram**

sklearn.linear_model.orthogonal_mp_gram(Gram, Xy, n_nonzero_coefs=None, tol=None, norms_squared=None, copy_Gram=True, copy_Xy=True, return_path=False, return_n_iter=False)

Gram Orthogonal Matching Pursuit (OMP)

Solves n_targets Orthogonal Matching Pursuit problems using only the Gram matrix X.T * X and the product X.T * y.

Read more in the User Guide.

**Parameters Gram**: array, shape (n_features, n_features)

Gram matrix of the input data: X.T * X

**Xy**: array, shape (n_features,) or (n_features, n_targets)

Input targets multiplied by X: X.T * y

**n_nonzero_coefs**: int

Desired number of non-zero entries in the solution. If None (by default) this value is set to 10% of n_features.

**tol**: float
Maximum norm of the residual. If not None, overrides n_nonzero_coefs.

define parameters:
- **norms_squared**: array-like, shape (n_targets,)
  Squared L2 norms of the lines of y. Required if tol is not None.
- **copy_Gram**: bool, optional
  Whether the gram matrix must be copied by the algorithm. A false value is only helpful if it is already Fortran-ordered, otherwise a copy is made anyway.
- **copy_Xy**: bool, optional
  Whether the covariance vector Xy must be copied by the algorithm. If False, it may be overwritten.
- **return_path**: bool, optional. Default: False
  Whether to return every value of the nonzero coefficients along the forward path. Useful for cross-validation.
- **return_n_iter**: bool, optional default False
  Whether or not to return the number of iterations.

Returns **coef**: array, shape (n_features,) or (n_features, n_targets)

Coefficients of the OMP solution. If return_path=True, this contains the whole coefficient path. In this case its shape is (n_features, n_features) or (n_features, n_targets, n_features) and iterating over the last axis yields coefficients in increasing order of active features.

**n_iters**: array-like or int

Number of active features across every target. Returned only if return_n_iter is set to True.

See also:
OrthogonalMatchingPursuit, orthogonal_mp, lars_path, decomposition, sparse_encode

Notes


30.20 sklearn.manifold: Manifold Learning

The sklearn.manifold module implements data embedding techniques.

User guide: See the Manifold learning section for further details.

[manifold.Isomap](#) Isomap Embedding
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### 30.20.1 sklearn.manifold.Isomap

Class `sklearn.manifold.Isomap` (n_neighbors=5, n_components=2, eigen_solver='auto', tol=0, max_iter=None, path_method='auto', neighbors_algorithm='auto', n_jobs=1)

Isomap Embedding
Non-linear dimensionality reduction through Isometric Mapping
Read more in the User Guide.

**Parameters**

- **n_neighbors**: integer
  - number of neighbors to consider for each point.

- **n_components**: integer
  - number of coordinates for the manifold

- **eigen_solver**: ['auto'|'arpack'|'dense']
  - ‘auto’: Attempt to choose the most efficient solver for the given problem.
  - ‘arpack’: Use Arnoldi decomposition to find the eigenvalues and eigenvectors.
  - ‘dense’: Use a direct solver (i.e. LAPACK) for the eigenvalue decomposition.

- **tol**: float
  - Convergence tolerance passed to arpack or lobpcg. not used if eigen_solver == ‘dense’.

- **max_iter**: integer
  - Maximum number of iterations for the arpack solver. not used if eigen_solver == ‘dense’.

- **path_method**: string ['auto'|'FW'|'D']
  - Method to use in finding shortest path.
  - ‘auto’: attempt to choose the best algorithm automatically.
  - ‘FW’: Floyd-Warshall algorithm.
  - ‘D’: Dijkstra’s algorithm.

- **neighbors_algorithm**: string ['auto'|'brute'|'kd_tree'|'ball_tree']
  - Algorithm to use for nearest neighbors search, passed to neighbors.NearestNeighbors instance.

- **n_jobs**: int, optional (default = 1)
  - The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.
Attributes

| embed-     | (array-like, shape (n_samples, n_components)) Stores the embedding vectors. |
| dding_     |                                                                         |
| kernel_pca | (object) KernelPCA object used to implement the embedding.              |
| train-     | (array-like, shape (n_samples, n_features)) Stores the training data. |
| ing_data_  |                                                                         |
| nbrs_      | (sklearn.neighbors.NearestNeighbors instance) Stores nearest neighbors instance, including |
|           | BallTree or KDtree if applicable.                                      |
| dist_matrix| (array-like, shape (n_samples, n_samples)) Stores the geodesic distance matrix of training |
|           | data.                                                                  |

References

[R121121]

Methods

fit(X[, y])
Compute the embedding vectors for data X

fit_transform(X[, y])
Fit the model from data in X and transform X.

get_params([deep])
Get parameters for this estimator.

reconstruction_error()
Compute the reconstruction error for the embedding.

set_params(**params)
Set the parameters of this estimator.

transform(X)
Transform X.

__init__(n_neighbors=5, n_components=2, eigen_solver='auto', tol=0, max_iter=None, path_method='auto', neighbors_algorithm='auto', n_jobs=1)

fit (X, y=None)
Compute the embedding vectors for data X

Parameters X : {array-like, sparse matrix, BallTree, KDTre, NearestNeighbors}

Sample data, shape = (n_samples, n_features), in the form of a numpy array, precomputed tree, or NearestNeighbors object.

y: Ignored

Returns self : returns an instance of self.

fit_transform (X, y=None)
Fit the model from data in X and transform X.

Parameters X : {array-like, sparse matrix, BallTree, KDTre}

Training vector, where n_samples in the number of samples and n_features is the number of features.

y: Ignored

Returns X_new : array-like, shape (n_samples, n_components)

get_params (deep=True)
Get parameters for this estimator.
Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

reconstruction_error()

Compute the reconstruction error for the embedding.

Returns reconstruction_error : float

Notes

The cost function of an isomap embedding is

\[ E = \frac{\text{frobenius_norm}[K(D) - K(D_{\text{fit})}]}{\text{n_samples}} \]

Where \( D \) is the matrix of distances for the input data \( X \), \( D_{\text{fit}} \) is the matrix of distances for the output embedding \( X_{\text{fit}} \), and \( K \) is the isomap kernel:

\[ K(D) = -0.5 \times (I - 1/n_{\text{samples}}) \times D^2 \times (I - 1/n_{\text{samples}}) \]

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>._{\text{parameter}}\) so that it’s possible to update each component of a nested object.

Returns self

transform(X)

Transform X.

This is implemented by linking the points X into the graph of geodesic distances of the training data. First the \( n_{\text{neighbors}} \) nearest neighbors of X are found in the training data, and from these the shortest geodesic distances from each point in X to each point in the training data are computed in order to construct the kernel. The embedding of X is the projection of this kernel onto the embedding vectors of the training set.

Parameters X : array-like, shape (n_samples, n_features)

Returns X_new : array-like, shape (n_samples, n_components)

Examples using sklearn.manifold.Isomap

- Comparison of Manifold Learning methods
- Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...
30.20.2 `sklearn.manifold.LocallyLinearEmbedding`

```python
class sklearn.manifold.LocallyLinearEmbedding(n_neighbors=5,
                                           n_components=2,
                                           reg=0.001,
                                           eigen_solver='auto',
                                           tol=1e-06,
                                           max_iter=100,
                                           method='standard',
                                           hessian_tol=0.0001,
                                           modified_tol=1e-12,
                                           neighbors_algorithm='auto',
                                           random_state=None,
                                           n_jobs=1)
```

Locally Linear Embedding

Read more in the *User Guide.*

**Parameters**

- **n_neighbors**: integer
  
  number of neighbors to consider for each point.

- **n_components**: integer
  
  number of coordinates for the manifold

- **reg**: float
  
  regularization constant, multiplies the trace of the local covariance matrix of the distances.

- **eigen_solver**: string, (`'auto'`, `'arpack'`, `'dense'`)
  
  auto : algorithm will attempt to choose the best method for input data

  arpack [use arnoldi iteration in shift-invert mode.] For this method, M may be a dense matrix, sparse matrix, or general linear operator. Warning: ARPACK can be unstable for some problems. It is best to try several random seeds in order to check results.

  dense [use standard dense matrix operations for the eigenvalue] decomposition. For this method, M must be an array or matrix type. This method should be avoided for large problems.

- **tol**: float, optional
  
  Tolerance for `'arpack'` method Not used if eigen_solver==’dense’.

- **max_iter**: integer
  
  maximum number of iterations for the arpack solver. Not used if eigen_solver==’dense’.

- **method**: string (‘standard’, ‘hessian’, ‘modified’ or ‘ltsa’)
  
  standard [use the standard locally linear embedding algorithm. see] reference [1]

  hessian [use the Hessian eigenmap method. This method requires] n_neighbors > n_components * (1 + (n_components + 1) / 2 see reference [2]

  modified [use the modified locally linear embedding algorithm.] see reference [3]

  ltsa [use local tangent space alignment algorithm] see reference [4]

- **hessian_tol**: float, optional
  
  Tolerance for Hessian eigenmapping method. Only used if method == 'hessian'

- **modified_tol**: float, optional
  
  Tolerance for modified LLE method. Only used if method == 'modified'

- **neighbors_algorithm**: string [‘auto’]’l’brute’l’kd_tree’l’ball_tree’]
algorithm to use for nearest neighbors search, passed to neighbors.NearestNeighbors instance

**random_state** : int, RandomState instance or None, optional (default=None)
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when eigen_solver == ‘arpack’.

**n_jobs** : int, optional (default = 1)
The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.

**Attributes**

| embedding_ | (array-like, shape [n_samples, n_components]) Stores the embedding vectors |
| reconstruc-
| tion_error_ | (float) Reconstruction error associated with embedding_ |
| nbrs_ | (NearestNeighbors object) Stores nearest neighbors instance, including BallTree or KDtree if applicable. |

**References**

[R123126], [R124126], [R125126], [R126126]

**Methods**

| fit(X[, y]) | Compute the embedding vectors for data X |
| fit_transform(X[, y]) | Compute the embedding vectors for data X and transform X. |
| get_params([deep]) | Get parameters for this estimator. |
| set_params(**params) | Set the parameters of this estimator. |
| transform(X) | Transform new points into embedding space. |

```python
__init__(n_neighbors=5, n_components=2, reg=0.001, eigen_solver='auto', tol=1e-06, max_iter=100, method='standard', hessian_tol=0.0001, modified_tol=1e-12, neighbors_algorithm='auto', random_state=None, n_jobs=1)
```

**fit**(X, y=None)
Compute the embedding vectors for data X

**Parameters** X : array-like of shape [n_samples, n_features]
training set.

y: Ignored

**Returns** self : returns an instance of self.

**fit_transform**(X, y=None)
Compute the embedding vectors for data X and transform X.
Parameters X : array-like of shape [n_samples, n_features]
    training set.

y: Ignored

Returns X_new : array-like, shape (n_samples, n_components)

get_params (deep=True)
    Get parameters for this estimator.

Parameters deep : boolean, optional
    If True, will return the parameters for this estimator and contained subobjects that are
    estimators.

Returns params : mapping of string to any
    Parameter names mapped to their values.

set_params (**params)
    Set the parameters of this estimator.

    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
    parameters of the form <component>__<parameter> so that it’s possible to update each component
    of a nested object.

Returns self

transform(X)
    Transform new points into embedding space.

Parameters X : array-like, shape = [n_samples, n_features]

Returns X_new : array, shape = [n_samples, n_components]

Notes

Because of scaling performed by this method, it is discouraged to use it together with methods that are not
scale-invariant (like SVMs)

Examples using sklearn.manifold.LocallyLinearEmbedding

- Visualizing the stock market structure
- Comparison of Manifold Learning methods
- Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

30.20.3 sklearn.manifold.MDS

class sklearn.manifold.MDS (n_components=2, metric=True, n_init=4, max_iter=300, verbose=0,
    eps=0.001, n_jobs=1, random_state=None, dissimilarity= ‘euclidean’)

    Multidimensional scaling

    Read more in the User Guide.

Parameters n_components : int, optional, default: 2
    Number of dimensions in which to immerse the dissimilarities.
metric : boolean, optional, default: True

If True, perform metric MDS; otherwise, perform nonmetric MDS.

n_init : int, optional, default: 4

Number of times the SMACOF algorithm will be run with different initializations. The final results will be the best output of the runs, determined by the run with the smallest final stress.

max_iter : int, optional, default: 300

Maximum number of iterations of the SMACOF algorithm for a single run.

verbose : int, optional, default: 0

Level of verbosity.

eps : float, optional, default: 1e-3

Relative tolerance with respect to stress at which to declare convergence.

n_jobs : int, optional, default: 1

The number of jobs to use for the computation. If multiple initializations are used (n_init), each run of the algorithm is computed in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

random_state : int, RandomState instance or None, optional, default: None

The generator used to initialize the centers. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

dissimilarity : 'euclidean' | 'precomputed', optional, default: 'euclidean'

Dissimilarity measure to use:

- 'euclidean': Pairwise Euclidean distances between points in the dataset.
- 'precomputed': Pre-computed dissimilarities are passed directly to fit and fit_transform.

Attributes

| embedding | (array-like, shape (n_components, n_samples)) Stores the position of the dataset in the embedding space. |
| stress_  | (float) The final value of the stress (sum of squared distance of the disparities and the distances for all constrained points). |

References


“Nonmetric multidimensional scaling: a numerical method” Kruskal, J. Psychometrika, 29 (1964)
“Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis” Kruskal, J. Psychometrika, 29, (1964)

Methods

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<td>fit(X[, y, init])</td>
<td>Computes the position of the points in the embedding space</td>
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<tr>
<td>fit_transform(X[, y, init])</td>
<td>Fit the data from X, and returns the embedded coordinates</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
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</table>

__init__ (n_components=2, metric=True, n_init=4, max_iter=300, verbose=0, eps=0.001, n_jobs=1, random_state=None, dissimilarity='euclidean')

fit (X, y=None, init=None)
Computes the position of the points in the embedding space

Parameters

X : array, shape (n_samples, n_features) or (n_samples, n_samples)
Input data. If dissimilarity=='precomputed', the input should be the dissimilarity matrix.

y : Ignored

init : ndarray, shape (n_samples,), optional, default: None
Starting configuration of the embedding to initialize the SMACOF algorithm. By default, the algorithm is initialized with a randomly chosen array.

fit_transform (X, y=None, init=None)
Fit the data from X, and returns the embedded coordinates

Parameters

X : array, shape (n_samples, n_features) or (n_samples, n_samples)
Input data. If dissimilarity=='precomputed', the input should be the dissimilarity matrix.

y : Ignored

init : ndarray, shape (n_samples,), optional, default: None
Starting configuration of the embedding to initialize the SMACOF algorithm. By default, the algorithm is initialized with a randomly chosen array.

get_params (deep=True)
Get parameters for this estimator.

Parameters

depth : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

params : mapping of string to any
Parameter names mapped to their values.

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**Examples using sklearn.manifold.MDS**

- Multi-dimensional scaling
- Comparison of Manifold Learning methods
- Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

### 30.20.4 sklearn.manifold.SpectralEmbedding

**class sklearn.manifold.SpectralEmbedding**

```python
class sklearn.manifold.SpectralEmbedding(n_components=2, affinity='nearest_neighbors', gamma=None, random_state=None, eigen_solver=None, n_neighbors=None, n_jobs=1)
```

Spectral embedding for non-linear dimensionality reduction.

Forms an affinity matrix given by the specified function and applies spectral decomposition to the corresponding graph laplacian. The resulting transformation is given by the value of the eigenvectors for each data point.

Note: Laplacian Eigenmaps is the actual algorithm implemented here.

Read more in the User Guide.

**Parameters**

- `n_components`: integer, default: 2
  
The dimension of the projected subspace.

- `affinity`: string or callable, default
  
  How to construct the affinity matrix.

  - 'nearest_neighbors': construct affinity matrix by knn graph
  - 'rbf': construct affinity matrix by rbf kernel
  - 'precomputed': interpret X as precomputed affinity matrix
  - callable: use passed in function as affinity the function takes in data matrix (n_samples, n_features) and return affinity matrix (n_samples, n_samples).

- `gamma`: float, optional, default
  
  Kernel coefficient for rbf kernel.

- `random_state`: int, RandomState instance or None, optional, default: None
  
  A pseudo random number generator used for the initialization of the lobpcg eigenvectors. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == 'amg'.

- `eigen_solver`: [None, ‘arpack’, ‘lobpcg’, or ‘amg’]
  
  The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.
n_neighbors : int, default

Number of nearest neighbors for nearest_neighbors graph building.

n_jobs : int, optional (default = 1)

The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.

Attributes

embedding_ (array, shape = (n_samples, n_components)) Spectral embedding of the training matrix.

affinity_matrix_ (array, shape = (n_samples, n_samples)) Affinity_matrix constructed from samples or pre-computed.

References


Methods

fit(X[, y]) Fit the model from data in X.

fit_transform(X[, y]) Fit the model from data in X and transform X.

get_params([deep]) Get parameters for this estimator.

set_params(**params) Set the parameters of this estimator.

__init__(n_components=2, affinity='nearest_neighbors', gamma=None, random_state=None, eigen_solver=None, n_neighbors=None, n_jobs=1)

fit (X, y=None)

Fit the model from data in X.

Parameters X : array-like, shape (n_samples, n_features)

Training vector, where n_samples is the number of samples and n_features is the number of features.

If affinity is “precomputed” X : array-like, shape (n_samples, n_samples), Interpret X as precomputed adjacency graph computed from samples.

Y: Ignored

Return self : object

Returns the instance itself.

fit_transform (X, y=None)

Fit the model from data in X and transform X.
Parameters X : array-like, shape (n_samples, n_features)

Training vector, where n_samples is the number of samples and n_features is the number of features.

If affinity is “precomputed” X : array-like, shape (n_samples, n_samples), Interpret X as precomputed adjacency graph computed from samples.

Y: Ignored

Returns X_new : array-like, shape (n_samples, n_components)

get_params (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.manifold.SpectralEmbedding

- Various Agglomerative Clustering on a 2D embedding of digits
- Comparison of Manifold Learning methods
- Manifold Learning methods on a severed sphere
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

30.20.5 sklearn.manifold.TSNE

class sklearn.manifold.TSNE (n_components=2, perplexity=30.0, early_exaggeration=12.0,
learning_rate=200.0, n_iter=1000, n_iter_without_progress=300,
min_grad_norm=1e-07, metric='euclidean', init='random', verbose=0,
random_state=None, method='barnes_hut', angle=0.5)

t-distributed Stochastic Neighbor Embedding.

t-SNE [1] is a tool to visualize high-dimensional data. It converts similarities between data points to joint probabilities and tries to minimize the Kullback-Leibler divergence between the joint probabilities of the low-dimensional embedding and the high-dimensional data. t-SNE has a cost function that is not convex, i.e. with different initializations we can get different results.

It is highly recommended to use another dimensionality reduction method (e.g. PCA for dense data or TruncatedSVD for sparse data) to reduce the number of dimensions to a reasonable amount (e.g. 50) if the number of features is very high. This will suppress some noise and speed up the computation of pairwise distances between samples. For more tips see Laurens van der Maaten’s FAQ [2].

Read more in the User Guide.
Parameters n_components : int, optional (default: 2)

Dimension of the embedded space.

perplexity : float, optional (default: 30)

The perplexity is related to the number of nearest neighbors that is used in other man-
ifold learning algorithms. Larger datasets usually require a larger perplexity. Consider selecting a value between 5 and 50. The choice is not extremely critical since t-SNE is quite insensitive to this parameter.

early_exaggeration : float, optional (default: 12.0)

Controls how tight natural clusters in the original space are in the embedded space and how much space will be between them. For larger values, the space between natural clusters will be larger in the embedded space. Again, the choice of this parameter is not very critical. If the cost function increases during initial optimization, the early exaggeration factor or the learning rate might be too high.

learning_rate : float, optional (default: 200.0)

The learning rate for t-SNE is usually in the range [10.0, 1000.0]. If the learning rate is too high, the data may look like a ‘ball’ with any point approximately equidistant from its nearest neighbours. If the learning rate is too low, most points may look compressed in a dense cloud with few outliers. If the cost function gets stuck in a bad local minimum increasing the learning rate may help.

n_iter : int, optional (default: 1000)

Maximum number of iterations for the optimization. Should be at least 250.

n_iter_without_progress : int, optional (default: 300)

Maximum number of iterations without progress before we abort the optimization, used after 250 initial iterations with early exaggeration. Note that progress is only checked every 50 iterations so this value is rounded to the next multiple of 50.

New in version 0.17: parameter n_iter_without_progress to control stopping criteria.

min_grad_norm : float, optional (default: 1e-7)

If the gradient norm is below this threshold, the optimization will be stopped.

metric : string or callable, optional

The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pair-
wise.PAIRWISE_DISTANCE_FUNCTIONS. If metric is “precomputed”, X is assumed to be a distance matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them. The default is “euclidean” which is interpreted as squared euclidean distance.

init : string or numpy array, optional (default: “random”)

Initialization of embedding. Possible options are ‘random’, ‘pca’, and a numpy array of shape (n_samples, n_components). PCA initialization cannot be used with precomputed distances and is usually more globally stable than random initialization.

verbose : int, optional (default: 0)

Verbosity level.
random_state : int, RandomState instance or None, optional (default: None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Note that different initializations might result in different local minima of the cost function.

method : string (default: ‘barnes_hut’)

By default the gradient calculation algorithm uses Barnes-Hut approximation running in O(NlogN) time. method=’exact’ will run on the slower, but exact, algorithm in O(N^2) time. The exact algorithm should be used when nearest-neighbor errors need to be better than 3%. However, the exact method cannot scale to millions of examples.

New in version 0.17: Approximate optimization method via the Barnes-Hut.

angle : float (default: 0.5)

Only used if method=’barnes_hut’ This is the trade-off between speed and accuracy for Barnes-Hut T-SNE. ‘angle’ is the angular size (referred to as theta in [3]) of a distant node as measured from a point. If this size is below ‘angle’ then it is used as a summary node of all points contained within it. This method is not very sensitive to changes in this parameter in the range of 0.2 - 0.8. Angle less than 0.2 has quickly increasing computation time and angle greater 0.8 has quickly increasing error.

Attributes

| embedding_ | (array-like, shape (n_samples, n_components)) Stores the embedding vectors. |
| kl_divergence_ | (float) Kullback-Leibler divergence after optimization. |
| n_iter_ | (int) Number of iterations run. |

References


Examples

```python
>>> import numpy as np
>>> from sklearn.manifold import TSNE
>>> X = np.array([[0, 0, 0], [0, 1, 1], [1, 0, 1], [1, 1, 1]])
>>> X_embedded = TSNE(n_components=2).fit_transform(X)
>>> X_embedded.shape
(4, 2)
```
Methods

%code

```python
Methods

fit(X[, y])  Fit X into an embedded space.

fit_transform(X[, y])  Fit X into an embedded space and return that transformed output.

get_params([deep])  Get parameters for this estimator.

set_params(**params)  Set the parameters of this estimator.
```

\[\textit{__init__}(\text{n\_components}=2, \text{perplexity}=30.0, \text{early\_exaggeration}=12.0, \text{learning\_rate}=200.0,\]
\[\text{n\_iter}=1000, \text{n\_iter\_without\_progress}=300, \text{min\_grad\_norm}=1e-07, \text{metric}=\text{euclidean},\]
\[\text{init}=\text{random}, \text{verbose}=0, \text{random\_state}=\text{None}, \text{method}=\text{barnes\_hut}, \text{angle}=0.5)\]

\text{fit}(X, y=\text{None})

Fit X into an embedded space.

\textbf{Parameters}
\textbf{X} : array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)

If the metric is ‘precomputed’ X must be a square distance matrix. Otherwise it contains a sample per row.

\textbf{y} : Ignored

\text{fit\_transform}(X, y=\text{None})

Fit X into an embedded space and return that transformed output.

\textbf{Parameters}
\textbf{X} : array, shape (n\_samples, n\_features) or (n\_samples, n\_samples)

If the metric is ‘precomputed’ X must be a square distance matrix. Otherwise it contains a sample per row.

\textbf{y} : Ignored

\textbf{Returns}
\textbf{X\_new} : array, shape (n\_samples, n\_components)

Embedding of the training data in low-dimensional space.

\text{get\_params}(\text{deep}=\text{True})

Get parameters for this estimator.

\textbf{Parameters}
\textbf{deep} : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

\textbf{Returns}
\textbf{params} : mapping of string to any

Parameter names mapped to their values.

\text{n\_iter\_final}

DEPRECATED: Attribute n\_iter\_final was deprecated in version 0.19 and will be removed in 0.21. Use n\_iter\_ instead

\text{set\_params}(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>\_<parameter> so that it's possible to update each component of a nested object.

\textbf{Returns}
\textbf{self}
### Examples using `sklearn.manifold.TSNE`

- **Comparison of Manifold Learning methods**
- **t-SNE: The effect of various perplexity values on the shape**
- **Manifold Learning methods on a severed sphere**
- **Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...**

```python
manifold.locally_linear_embedding(X, ...[, n_neighbors, n_components, reg=0.001, eigen_solver='auto', tol=1e-06, max_iter=100, method='standard', hessian_tol=0.0001, modified_tol=1e-12, random_state=None, n_jobs=1])
```

Perform a Locally Linear Embedding analysis on the data.


**Parameters**

- **X** : [array-like, sparse matrix, BallTree, KDTree, NearestNeighbors]
  
  Sample data, shape = (n_samples, n_features), in the form of a numpy array, sparse array, precomputed tree, or NearestNeighbors object.

- **n_neighbors** : integer
  
  number of neighbors to consider for each point.

- **n_components** : integer
  
  number of coordinates for the manifold.

- **reg** : float
  
  regularization constant, multiplies the trace of the local covariance matrix of the distances.

- **eigen_solver** : string, [‘auto’, ‘arpack’, ‘dense’]
  
  auto : algorithm will attempt to choose the best method for input data

  arpack : [use arnoldi iteration in shift-invert mode.] For this method, M may be a dense matrix, sparse matrix, or general linear operator. Warning: ARPACK can be unstable for some problems. It is best to try several random seeds in order to check results.

  dense : [use standard dense matrix operations for the eigenvalue] decomposition. For this method, M must be an array or matrix type. This method should be avoided for large problems.

- **tol** : float, optional
  
  Tolerance for ‘arpack’ method Not used if eigen_solver=='dense'.
max_iter : integer
    maximum number of iterations for the arpack solver.
method : {'standard', 'hessian', 'modified', 'ltsa'}
    standard [use the standard locally linear embedding algorithm.] see reference [R131134]
    hessian [use the Hessian eigenmap method. This method requires] n_neighbors > n_components * (1 + (n_components + 1) / 2. see reference [R132134]
    modified [use the modified locally linear embedding algorithm.] see reference [R133134]
    ltsa [use local tangent space alignment algorithm] see reference [R134134]

hessian_tol : float, optional
    Tolerance for Hessian eigenmapping method. Only used if method == ‘hessian’

modified_tol : float, optional
    Tolerance for modified LLE method. Only used if method == ‘modified’

random_state : int, RandomState instance or None, optional (default=None)
    If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == ‘arpack’.

n_jobs : int, optional (default = 1)
    The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores.

Returns Y : array-like, shape [n_samples, n_components]
    Embedding vectors.

squared_error : float
    Reconstruction error for the embedding vectors. Equivalent to norm(Y - W Y, 'fro')**2, where W are the reconstruction weights.

References

[R131134], [R132134], [R133134], [R134134]

Examples using sklearn.manifold.locally_linear_embedding

- Swiss Roll reduction with LLE

30.20.7 sklearn.manifold.smacof

sklearn.manifold.smacof(dissimilarities, metric=True, n_components=2, init=None, n_init=8, n_jobs=1, max_iter=300, verbose=0, eps=0.001, random_state=None, return_n_iter=False)
    Computes multidimensional scaling using the SMACOF algorithm.
The SMACOF (Scaling by MAjorizing a COmplicated Function) algorithm is a multidimensional scaling algorithm which minimizes an objective function (the stress) using a majorization technique. Stress majorization, also known as the Guttman Transform, guarantees a monotone convergence of stress, and is more powerful than traditional techniques such as gradient descent.

The SMACOF algorithm for metric MDS can summarized by the following steps:

1. Set an initial start configuration, randomly or not.
2. Compute the stress
3. Compute the Guttman Transform
4. Iterate 2 and 3 until convergence.

The nonmetric algorithm adds a monotonic regression step before computing the stress.

**Parameters**

- **dissimilarities**: ndarray, shape (n_samples, n_samples)
  
  Pairwise dissimilarities between the points. Must be symmetric.

- **metric**: boolean, optional, default: True
  
  Compute metric or nonmetric SMACOF algorithm.

- **n_components**: int, optional, default: 2
  
  Number of dimensions in which to immerse the dissimilarities. If an init array is provided, this option is overridden and the shape of init is used to determine the dimensionality of the embedding space.

- **init**: ndarray, shape (n_samples, n_components), optional, default: None
  
  Starting configuration of the embedding to initialize the algorithm. By default, the algorithm is initialized with a randomly chosen array.

- **n_init**: int, optional, default: 8
  
  Number of times the SMACOF algorithm will be run with different initializations. The final results will be the best output of the runs, determined by the run with the smallest final stress. If init is provided, this option is overridden and a single run is performed.

- **n_jobs**: int, optional, default: 1
  
  The number of jobs to use for the computation. If multiple initializations are used (n_init), each run of the algorithm is computed in parallel.
  
  If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpu + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

- **max_iter**: int, optional, default: 300
  
  Maximum number of iterations of the SMACOF algorithm for a single run.

- **verbose**: int, optional, default: 0
  
  Level of verbosity.

- **eps**: float, optional, default: 1e-3
  
  Relative tolerance with respect to stress at which to declare convergence.

- **random_state**: int, RandomState instance or None, optional, default: None
The generator used to initialize the centers. If int, random_state is the seed used by
the random number generator; If RandomState instance, random_state is the random
number generator; If None, the random number generator is the RandomState instance
used by np.random.

return_n_iter : bool, optional, default: False
Whether or not to return the number of iterations.

Returns X : ndarray, shape (n_samples, n_components)
Coordinates of the points in a n_components-space.

stress : float
The final value of the stress (sum of squared distance of the disparities and the distances
for all constrained points).

n_iter : int
The number of iterations corresponding to the best stress. Returned only if
return_n_iter is set to True.

Notes

“Modern Multidimensional Scaling - Theory and Applications” Borg, I.; Groenen P. Springer Series in Statistics
(1997)
“Nonmetric multidimensional scaling: a numerical method” Kruskal, J. Psychometrika, 29 (1964)
“Multidimensional scaling by optimizing goodness of fit to a nonmetric hypothesis” Kruskal, J. Psychometrika,
29, (1964)

30.20.8 sklearn.manifold.spectral_embedding

sklearn.manifold.spectral_embedding(adjacency, n_components=8, eigen_solver=None, random_state=None, eigen_tol=0.0, norm_laplacian=True, drop_first=True)

Project the sample on the first eigenvectors of the graph Laplacian.

The adjacency matrix is used to compute a normalized graph Laplacian whose spectrum (especially the eigen-
 vectors associated to the smallest eigenvalues) has an interpretation in terms of minimal number of cuts neces-
sary to split the graph into comparably sized components.

This embedding can also ‘work’ even if the adjacency variable is not strictly the adjacency matrix of a graph
but more generally an affinity or similarity matrix between samples (for instance the heat kernel of a euclidean
distance matrix or a k-NN matrix).

However care must taken to always make the affinity matrix symmetric so that the eigenvector decomposition
works as expected.

Note : Laplacian Eigenmaps is the actual algorithm implemented here.

Read more in the User Guide.

Parameters adjacency : array-like or sparse matrix, shape: (n_samples, n_samples)
The adjacency matrix of the graph to embed.

n_components : integer, optional, default 8
The dimension of the projection subspace.
**eigen_solver** : {None, ‘arpack’, ‘lobpcg’, or ‘amg’}, default None

The eigenvalue decomposition strategy to use. AMG requires pyamg to be installed. It can be faster on very large, sparse problems, but may also lead to instabilities.

**random_state** : int, RandomState instance or None, optional, default: None

A pseudo random number generator used for the initialization of the lobpcg eigenvectors decomposition. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when solver == ‘amg’.

**eigen_tol** : float, optional, default=0.0

Stopping criterion for eigendecomposition of the Laplacian matrix when using arpack eigen_solver.

**norm_laplacian** : bool, optional, default=True

If True, then compute normalized Laplacian.

**drop_first** : bool, optional, default=True

Whether to drop the first eigenvector. For spectral embedding, this should be True as the first eigenvector should be constant vector for connected graph, but for spectral clustering, this should be kept as False to retain the first eigenvector.

**Returns**  
**embedding** : array, shape=(n_samples, n_components)

The reduced samples.

**Notes**

Spectral Embedding (Laplacian Eigenmaps) is most useful when the graph has one connected component. If there graph has many components, the first few eigenvectors will simply uncover the connected components of the graph.

**References**

- Toward the Optimal Preconditioned Eigensolver: Locally Optimal Block Preconditioned Conjugate Gradient Method Andrew V. Knyazev http://dx.doi.org/10.1137%2FS1064827500366124

### 30.21 sklearn.metrics: Metrics

See the Model evaluation: quantifying the quality of predictions section and the Pairwise metrics, Affinities and Kernels section of the user guide for further details. The sklearn.metrics module includes score functions, performance metrics and pairwise metrics and distance computations.

#### 30.21.1 Model Selection Interface

See the The scoring parameter: defining model evaluation rules section of the user guide for further details.
metrics.get_scorer(scoring) Get a scorer from string
metrics.make_scorer(score_func[, ...]) Make a scorer from a performance metric or loss function.

sklearn.metrics.get_scorer

sklearn.metrics.get_scorer (scoring)
Get a scorer from string

Parameters scoring : str | callable
scoring method as string. If callable it is returned as is.

Returns scorer : callable
The scorer.

sklearn.metrics.make_scorer

sklearn.metrics.make_scorer (score_func, greater_is_better=True, needs_proba=False, needs_threshold=False, **kwargs)
Make a scorer from a performance metric or loss function.

This factory function wraps scoring functions for use in GridSearchCV and cross_val_score. It takes a score function, such as accuracy_score, mean_squared_error, adjusted_rand_index or average_precision and returns a callable that scores an estimator’s output.

Parameters score_func : callable,
Score function (or loss function) with signature score_func(y, y_pred, **kwargs).

greater_is_better : boolean, default=True
Whether score_func is a score function (default), meaning high is good, or a loss function, meaning low is good. In the latter case, the scorer object will sign-flip the outcome of the score_func.

needs_proba : boolean, default=False
Whether score_func requires predict_proba to get probability estimates out of a classifier.

needs_threshold : boolean, default=False
Whether score_func takes a continuous decision certainty. This only works for binary classification using estimators that have either a decision_function or predict_proba method.

For example average_precision or the area under the roc curve can not be computed using discrete predictions alone.

**kwargs : additional arguments
Additional parameters to be passed to score_func.

Returns scorer : callable
Callable object that returns a scalar score; greater is better.
Examples

```python
>>> from sklearn.metrics import fbeta_score, make_scorer
>>> ftwo_scorer = make_scorer(fbeta_score, beta=2)
>>> ftwo_scorer
make_scorer(fbeta_score, beta=2)
```

Examples using sklearn.metrics.make_scorer

- Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV

### 30.21.2 Classification metrics

See the Classification metrics section of the user guide for further details.

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>metrics.accuracy_score(y_true, y_pred[, ...])</code></td>
<td>Accuracy classification score.</td>
</tr>
<tr>
<td><code>metrics.auc(x, y[, reorder])</code></td>
<td>Compute Area Under the Curve (AUC) using the trapezoidal rule.</td>
</tr>
<tr>
<td><code>metrics.average_precision_score(y_true, y_score)</code></td>
<td>Compute average precision (AP) from prediction scores.</td>
</tr>
<tr>
<td><code>metrics.balanced_accuracy_score(y_true, y_pred)</code></td>
<td>Compute the balanced accuracy.</td>
</tr>
<tr>
<td><code>metrics.brier_score_loss(y_true, y_prob[, ...])</code></td>
<td>Compute the Brier score.</td>
</tr>
<tr>
<td><code>metrics.classification_report(y_true, y_pred)</code></td>
<td>Build a text report showing the main classification metrics.</td>
</tr>
<tr>
<td><code>metrics.cohen_kappa_score(y1, y2[, labels, ...])</code></td>
<td>Cohen’s kappa: a statistic that measures inter-annotator agreement.</td>
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<td><code>metrics.confusion_matrix(y_true, y_pred[, ...])</code></td>
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<td><code>metrics.matthews_corrcoef(y_true, y_pred[, ...])</code></td>
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<td>Compute Area Under the Receiver Operating Characteristic Curve (ROC AUC) from prediction scores.</td>
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**sklearn.metrics.accuracy_score**

`sklearn.metrics.accuracy_score(y_true, y_pred, normalize=True, sample_weight=None)`

Accuracy classification score.

In multilabel classification, this function computes subset accuracy: the set of labels predicted for a sample must exactly match the corresponding set of labels in `y_true`.

Read more in the *User Guide*.

**Parameters**

- `y_true` : 1d array-like, or label indicator array / sparse matrix
  
  Ground truth (correct) labels.

- `y_pred` : 1d array-like, or label indicator array / sparse matrix
  
  Predicted labels, as returned by a classifier.

- `normalize` : bool, optional (default=True)
  
  If `False`, return the number of correctly classified samples. Otherwise, return the fraction of correctly classified samples.

- `sample_weight` : array-like of shape = `[n_samples]`, optional
  
  Sample weights.

**Returns**

- `score` : float
  
  If `normalize == True`, return the correctly classified samples (float), else it returns the number of correctly classified samples (int).

  The best performance is 1 with `normalize == True` and the number of samples with `normalize == False`.

**See also:**

`jaccard_similarity_score`, `hamming_loss`, `zero_one_loss`

**Notes**

In binary and multiclass classification, this function is equal to the `jaccard_similarity_score` function.

**Examples**

```python
>>> import numpy as np
>>> from sklearn.metrics import accuracy_score
>>> y_pred = [0, 2, 1, 3]
>>> y_true = [0, 1, 2, 3]
>>> accuracy_score(y_true, y_pred)
0.5
>>> accuracy_score(y_true, y_pred, normalize=False)
2
```
In the multilabel case with binary label indicators:

```python
>>> from sklearn.metrics import accuracy_score
>>> accuracy_score(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
```

Examples using `sklearn.metrics.accuracy_score`

- Multi-class AdaBoosted Decision Trees
- Probabilistic predictions with Gaussian process classification (GPC)
- Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV
- Importance of Feature Scaling
- Classification of text documents using sparse features

`sklearn.metrics.auc`

`sklearn.metrics.auc(x, y, reorder='deprecated')`

Compute Area Under the Curve (AUC) using the trapezoidal rule

This is a general function, given points on a curve. For computing the area under the ROC-curve, see `roc_auc_score`. For an alternative way to summarize a precision-recall curve, see `average_precision_score`.

**Parameters**

- `x` : array, shape = [n]
  x coordinates. These must be either monotonic increasing or monotonic decreasing.

- `y` : array, shape = [n]
  y coordinates.

- `reorder` : boolean, optional (default='deprecated')
  Whether to sort x before computing. If False, assume that x must be either monotonic increasing or monotonic decreasing. If True, y is used to break ties when sorting x. Make sure that y has a monotonic relation to x when setting reorder to True.

  Deprecated since version 0.20: Parameter `reorder` has been deprecated in version 0.20 and will be removed in 0.22. It’s introduced for roc_auc_score (not for general use) and is no longer used there. What’s more, the result from auc will be significantly influenced if x is sorted unexpectedly due to slight floating point error (See issue #9786). Future (and default) behavior is equivalent to `reorder=False`.

**Returns**

- `auc` : float

See also:

- `roc_auc_score` Compute the area under the ROC curve
- `average_precision_score` Compute average precision from prediction scores
- `precision_recall_curve` Compute precision-recall pairs for different probability thresholds
Examples

```python
>>> import numpy as np
>>> from sklearn import metrics

>>> y = np.array([1, 1, 2, 2])
>>> pred = np.array([0.1, 0.4, 0.35, 0.8])
>>> fpr, tpr, thresholds = metrics.roc_curve(y, pred, pos_label=2)
>>> metrics.auc(fpr, tpr)
0.75
```

Examples using sklearn.metrics.auc

- Species distribution modeling
- Receiver Operating Characteristic (ROC) with cross validation
- Receiver Operating Characteristic (ROC)

sklearn.metrics.average_precision_score

```python
def sklearn.metrics.average_precision_score(y_true, y_score, average='macro', sample_weight=None):
    Compute average precision (AP) from prediction scores

    AP summarizes a precision-recall curve as the weighted mean of precisions achieved at each threshold, with the increase in recall from the previous threshold used as the weight:

    \[ AP = \sum_n (R_n - R_{n-1})P_n \]

    where \( P_n \) and \( R_n \) are the precision and recall at the \( n \)th threshold [R147147]. This implementation is not interpolated and is different from computing the area under the precision-recall curve with the trapezoidal rule, which uses linear interpolation and can be too optimistic.

    Note: this implementation is restricted to the binary classification task or multilabel classification task.

    Read more in the User Guide.

    Parameters
    0. y_true : array, shape = [n_samples] or [n_samples, n_classes]
        True binary labels (either {0, 1} or {-1, 1}).
    1. y_score : array, shape = [n_samples] or [n_samples, n_classes]
        Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision_function” on some classifiers).
    2. average : string, [None, ‘micro’, ‘macro’ (default), ‘samples’, ‘weighted’]
        If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

        - ‘micro’: Calculate metrics globally by considering each element of the label indicator matrix as a label.
        - ‘macro’: Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
```

Parameters

- `y_true` : array, shape = [n_samples] or [n_samples, n_classes]
  True binary labels (either {0, 1} or {-1, 1}).
- `y_score` : array, shape = [n_samples] or [n_samples, n_classes]
  Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision_function” on some classifiers).
- `average` : string, [None, ‘micro’, ‘macro’ (default), ‘samples’, ‘weighted’]
  If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

  - ‘micro’: Calculate metrics globally by considering each element of the label indicator matrix as a label.
  - ‘macro’: Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label).

'samples': Calculate metrics for each instance, and find their average.

sample_weight : array-like of shape = [n_samples], optional
    Sample weights.

Returns average_precision : float

See also:

roc_auc_score  Compute the area under the ROC curve
precision_recall_curve  Compute precision-recall pairs for different probability thresholds

References

[R147147]

Examples

>>> import numpy as np
>>> from sklearn.metrics import average_precision_score
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> average_precision_score(y_true, y_scores)
0.83...

Examples using sklearn.metrics.average_precision_score

• Precision-Recall

sklearn.metrics.balanced_accuracy_score

sklearn.metrics.balanced_accuracy_score(y_true, y_pred, sample_weight=None)
    Compute the balanced accuracy

    The balanced accuracy is used in binary classification problems to deal with imbalanced datasets. It is defined as the arithmetic mean of sensitivity (true positive rate) and specificity (true negative rate), or the average recall obtained on either class. It is also equal to the ROC AUC score given binary inputs.

    The best value is 1 and the worst value is 0.

    Read more in the User Guide.

    Parameters y_true : 1d array-like
        Ground truth (correct) target values.

    y_pred : 1d array-like
        Estimated targets as returned by a classifier.

    sample_weight : array-like of shape = [n_samples], optional
Sample weights.

Returns balanced_accuracy : float.

The average of sensitivity and specificity

See also:

recall_score, roc_auc_score

References

[R475475]

Examples

```python
>>> from sklearn.metrics import balanced_accuracy_score
>>> y_true = [0, 1, 0, 0, 1, 0]
>>> y_pred = [0, 1, 0, 0, 0, 1]
>>> balanced_accuracy_score(y_true, y_pred)
0.625
```

sklearn.metrics.brier_score_loss

sklearn.metrics.brier_score_loss(y_true, y_prob, sample_weight=None, pos_label=None)

Compute the Brier score.

The smaller the Brier score, the better, hence the naming with “loss”.

Across all items in a set N predictions, the Brier score measures the mean squared difference between (1) the predicted probability assigned to the possible outcomes for item i, and (2) the actual outcome. Therefore, the lower the Brier score is for a set of predictions, the better the predictions are calibrated. Note that the Brier score always takes on a value between zero and one, since this is the largest possible difference between a predicted probability (which must be between zero and one) and the actual outcome (which can take on values of only 0 and 1).

The Brier score is appropriate for binary and categorical outcomes that can be structured as true or false, but is inappropriate for ordinal variables which can take on three or more values (this is because the Brier score assumes that all possible outcomes are equivalently “distant” from one another). Which label is considered to be the positive label is controlled via the parameter pos_label, which defaults to 1.

Read more in the User Guide.

Parameters y_true : array, shape (n_samples,)

True targets.

y_prob : array, shape (n_samples,)

Probabilities of the positive class.

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

pos_label : int or str, default=None

Label of the positive class. If None, the maximum label is used as positive class
Returns score : float

Brier score

References

[R149149]

Examples

```python
>>> import numpy as np
>>> from sklearn.metrics import brier_score_loss
>>> y_true = np.array([0, 1, 1, 0])
>>> y_true_categorical = np.array(['spam', 'ham', 'ham', 'spam'])
>>> y_prob = np.array([0.1, 0.9, 0.8, 0.3])
>>> brier_score_loss(y_true, y_prob)
0.037...
>>> brier_score_loss(y_true, 1-y_prob, pos_label=0)
0.037...
>>> brier_score_loss(y_true_categorical, y_prob, pos_label='ham')
0.037...
>>> brier_score_loss(y_true, np.array(y_prob) > 0.5)
0.0
```

Examples using sklearn.metrics.brier_score_loss

- Probability Calibration curves
- Probability calibration of classifiers

sklearn.metrics.classification_report

sklearn.metrics.classification_report (y_true, y_pred, labels=None, target_names=None, sample_weight=None, digits=2)

Build a text report showing the main classification metrics

Read more in the User Guide.

Parameters

- **y_true** : 1d array-like, or label indicator array / sparse matrix
  Ground truth (correct) target values.
- **y_pred** : 1d array-like, or label indicator array / sparse matrix
  Estimated targets as returned by a classifier.
- **labels** : array, shape = [n_labels]
  Optional list of label indices to include in the report.
- **target_names** : list of strings
  Optional display names matching the labels (same order).
- **sample_weight** : array-like of shape = [n_samples], optional
Sample weights.

```python
digits : int
```

Number of digits for formatting output floating point values

**Returns**

`report : string`

Text summary of the precision, recall, F1 score for each class.

The reported averages are a prevalence-weighted macro-average across classes (equivalent to `precision_recall_fscore_support` with `average='weighted'`).

Note that in binary classification, recall of the positive class is also known as “sensitivity”; recall of the negative class is “specificity”.

**Examples**

```python
>>> from sklearn.metrics import classification_report

>>> y_true = [0, 1, 2, 2, 2]

>>> y_pred = [0, 0, 2, 2, 1]

>>> target_names = ['class 0', 'class 1', 'class 2']

>>> print(classification_report(y_true, y_pred, target_names=target_names))

<table>
<thead>
<tr>
<th></th>
<th>precision</th>
<th>recall</th>
<th>f1-score</th>
<th>support</th>
</tr>
</thead>
<tbody>
<tr>
<td>class 0</td>
<td>0.50</td>
<td>1.00</td>
<td>0.67</td>
<td>1</td>
</tr>
<tr>
<td>class 1</td>
<td>0.00</td>
<td>0.00</td>
<td>0.00</td>
<td>1</td>
</tr>
<tr>
<td>class 2</td>
<td>1.00</td>
<td>0.67</td>
<td>0.80</td>
<td>3</td>
</tr>
</tbody>
</table>

avg / total 0.70 0.60 0.61 5
```

**Examples using `sklearn.metrics.classification_report`**

- Feature Union with Heterogeneous Data Sources
- Faces recognition example using eigenfaces and SVMs
- Recognizing hand-written digits
- Pipeline Anova SVM
- Parameter estimation using grid search with cross-validation
- Restricted Boltzmann Machine features for digit classification
- Label Propagation digits: Demonstrating performance
- Label Propagation digits active learning
- Classification of text documents using sparse features

**sklearn.metrics.cohen_kappa_score**

```python
sklearn.metrics.cohen_kappa_score(y1, y2, labels=None, weights=None, sample_weight=None)
```

Cohen’s kappa: a statistic that measures inter-annotator agreement.
This function computes Cohen’s kappa [R481483], a score that expresses the level of agreement between two annotators on a classification problem. It is defined as

\[ \kappa = \frac{p_o - p_e}{1 - p_e} \]

where \( p_o \) is the empirical probability of agreement on the label assigned to any sample (the observed agreement ratio), and \( p_e \) is the expected agreement when both annotators assign labels randomly. \( p_e \) is estimated using a per-annotator empirical prior over the class labels [R482483].

Read more in the User Guide.

**Parameters**
- \( y_1 \) : array, shape = [n_samples]
  - Labels assigned by the first annotator.
- \( y_2 \) : array, shape = [n_samples]
  - Labels assigned by the second annotator. The kappa statistic is symmetric, so swapping \( y_1 \) and \( y_2 \) doesn’t change the value.
- \( \text{labels} \) : array, shape = [n_classes], optional
  - List of labels to index the matrix. This may be used to select a subset of labels. If None, all labels that appear at least once in \( y_1 \) or \( y_2 \) are used.
- \( \text{weights} \) : str, optional
  - List of weighting type to calculate the score. None means no weighted; “linear” means linear weighted; “quadratic” means quadratic weighted.
- \( \text{sample_weight} \) : array-like of shape = [n_samples], optional
  - Sample weights.

**Returns**
- \( \kappa \) : float
  - The kappa statistic, which is a number between -1 and 1. The maximum value means complete agreement; zero or lower means chance agreement.

**References**

[R481483], [R482483], [R483483]

**sklearn.metrics.confusion_matrix**

**sklearn.metrics.confusion_matrix**(\( y_{\text{true}}, y_{\text{pred}}, \text{labels}=\text{None}, \text{sample_weight}=\text{None} \))

Compute confusion matrix to evaluate the accuracy of a classification

By definition a confusion matrix \( C \) is such that \( C_{i,j} \) is equal to the number of observations known to be in group \( i \) but predicted to be in group \( j \).

Thus in binary classification, the count of true negatives is \( C_{0,0} \), false negatives is \( C_{1,0} \), true positives is \( C_{1,1} \) and false positives is \( C_{0,1} \).

Read more in the User Guide.

**Parameters**
- \( y_{\text{true}} \) : array, shape = [n_samples]
  - Ground truth (correct) target values.
- \( y_{\text{pred}} \) : array, shape = [n_samples]
  - Estimated targets as returned by a classifier.
labels : array, shape = [n_classes], optional

List of labels to index the matrix. This may be used to reorder or select a subset of labels. If none is given, those that appear at least once in y_true or y_pred are used in sorted order.

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

Returns C : array, shape = [n_classes, n_classes]

Confusion matrix

References

[R153153]

Examples

```python
>>> from sklearn.metrics import confusion_matrix
>>> y_true = [2, 0, 2, 2, 0, 1]
>>> y_pred = [0, 0, 2, 2, 0, 2]
>>> confusion_matrix(y_true, y_pred)
array([[2, 0, 0],
       [0, 0, 1],
       [1, 0, 2]])

>>> y_true = ['cat', 'ant', 'cat', 'cat', 'ant', 'bird']
>>> y_pred = ['ant', 'ant', 'cat', 'cat', 'ant', 'cat']
>>> confusion_matrix(y_true, y_pred, labels=['ant', 'bird', 'cat'])
array([[2, 0, 0],
       [0, 0, 1],
       [1, 0, 2]])
```

In the binary case, we can extract true positives, etc as follows:

```python
>>> tn, fp, fn, tp = confusion_matrix([0, 1, 0, 1], [1, 1, 1, 0]).ravel()
>>> (tn, fp, fn, tp)
(0, 2, 1, 1)
```

Examples using sklearn.metrics.confusion_matrix

- Faces recognition example using eigenfaces and SVMs
- Recognizing hand-written digits
- Confusion matrix
- Label Propagation digits: Demonstrating performance
- Label Propagation digits active learning
- Classification of text documents using sparse features
sklearn.metrics.f1_score

sklearn.metrics.f1_score(y_true, y_pred, labels=None, pos_label=1, average='binary', sample_weight=None)

Compute the F1 score, also known as balanced F-score or F-measure

The F1 score can be interpreted as a weighted average of the precision and recall, where an F1 score reaches its best value at 1 and worst score at 0. The relative contribution of precision and recall to the F1 score are equal. The formula for the F1 score is:

\[
F1 = \frac{2 \times (\text{precision} \times \text{recall})}{\text{precision} + \text{recall}}
\]

In the multi-class and multi-label case, this is the weighted average of the F1 score of each class.

Read more in the User Guide.

**Parameters**

- `y_true` : 1d array-like, or label indicator array / sparse matrix
  
  Ground truth (correct) target values.

- `y_pred` : 1d array-like, or label indicator array / sparse matrix
  
  Estimated targets as returned by a classifier.

- `labels` : list, optional
  
  The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y_true and y_pred are used in sorted order.

  Changed in version 0.17: parameter labels improved for multiclass problem.

- `pos_label` : str or int, 1 by default
  
  The class to report if average='binary' and the data is binary. If the data are multiclass or multilabel, this will be ignored; setting labels=[pos_label] and average != 'binary' will report scores for that label only.

  
  This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

  - ‘binary’: Only report results for the class specified by pos_label. This is applicable only if targets (y_{true,pred}) are binary.
  
  - ‘micro’: Calculate metrics globally by counting the total true positives, false negatives and false positives.
  
  - ‘macro’: Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  
  - ‘weighted’: Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label). This alters ‘macro’ to account for label imbalance; it can result in an F-score that is not between precision and recall.
  
  - ‘samples’: Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy_score).

- `sample_weight` : array-like of shape = [n_samples], optional
Sample weights.

Returns **f1_score** : float or array of float, shape = [n_unique_labels]

F1 score of the positive class in binary classification or weighted average of the F1 scores of each class for the multiclass task.

**References**

[R155155]

**Examples**

```python
>>> from sklearn.metrics import f1_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> f1_score(y_true, y_pred, average='macro')
0.26...
>>> f1_score(y_true, y_pred, average='micro')
0.33...
>>> f1_score(y_true, y_pred, average='weighted')
0.26...
>>> f1_score(y_true, y_pred, average=None)
array([ 0.8,  0. ,  0. ])
```

**Examples using sklearn.metrics.f1_score**

- Probability Calibration curves

**sklearn.metrics.fbeta_score**

```
sklearn.metrics.fbeta_score(y_true, y_pred, beta, labels=None, pos_label=1, average='binary', sample_weight=None)
```

Compute the F-beta score

The F-beta score is the weighted harmonic mean of precision and recall, reaching its optimal value at 1 and its worst value at 0.

The **beta** parameter determines the weight of precision in the combined score. **beta < 1** lends more weight to precision, while **beta > 1** favors recall (**beta -> 0** considers only precision, **beta -> inf** only recall).

Read more in the User Guide.

**Parameters**

- **y_true** : 1d array-like, or label indicator array / sparse matrix
  
  Ground truth (correct) target values.

- **y_pred** : 1d array-like, or label indicator array / sparse matrix
  
  Estimated targets as returned by a classifier.

- **beta** : float
  
  Weight of precision in harmonic mean.

- **labels** : list, optional
The set of labels to include when `average != 'binary'`, and their order if `average is None`. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in `y_true` and `y_pred` are used in sorted order.

Changed in version 0.17: parameter `labels` improved for multiclass problem.

**pos_label**: str or int, 1 by default

The class to report if `average='binary'` and the data is binary. If the data are multiclass or multilabel, this will be ignored; setting `labels=[pos_label]` and `average != 'binary'` will report scores for that label only.

**average**: string, [None, ‘binary’ (default), ‘micro’, ‘macro’, ‘samples’, ‘weighted’]

This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

'binary': Only report results for the class specified by `pos_label`. This is applicable only if targets (`y_{true,pred}`) are binary.

'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.

'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.

'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label). This alters ‘macro’ to account for label imbalance; it can result in an F-score that is not between precision and recall.

'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy_score).

**sample_weight**: array-like of shape = [n_samples], optional

Sample weights.

Returns **fbeta_score**: float (if average is not None) or array of float, shape = [n_unique_labels]

F-beta score of the positive class in binary classification or weighted average of the F-beta score of each class for the multiclass task.

References

[R495496], [R496496]

Examples

```python
>>> from sklearn.metrics import fbeta_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> fbeta_score(y_true, y_pred, average='macro', beta=0.5)
... 0.23...
>>> fbeta_score(y_true, y_pred, average='micro', beta=0.5)
```
sklearn.metrics.hamming_loss

```
sklearn.metrics.hamming_loss(y_true, y_pred, labels=None, sample_weight=None, classes=None)
```

Compute the average Hamming loss.

The Hamming loss is the fraction of labels that are incorrectly predicted.

Read more in the `User Guide`.

**Parameters**

- **y_true**: 1d array-like, or label indicator array / sparse matrix
  - Ground truth (correct) labels.

- **y_pred**: 1d array-like, or label indicator array / sparse matrix
  - Predicted labels, as returned by a classifier.

- **labels**: array, shape = [n_labels], optional (default=None)
  - Integer array of labels. If not provided, labels will be inferred from y_true and y_pred.
  - New in version 0.18.

- **sample_weight**: array-like of shape = [n_samples], optional
  - Sample weights.
  - New in version 0.18.

- **classes**: array, shape = [n_labels], optional
  - Integer array of labels.
  - Deprecated since version 0.18: This parameter has been deprecated in favor of labels in version 0.18 and will be removed in 0.20. Use labels instead.

**Returns**

- **loss**: float or int,
  - Return the average Hamming loss between element of y_true and y_pred.

**See also**

- `accuracy_score`
- `jaccard_similarity_score`
- `zero_one_loss`

**Notes**

In multiclass classification, the Hamming loss correspond to the Hamming distance between y_true and y_pred which is equivalent to the subset zero_one_loss function.

In multilabel classification, the Hamming loss is different from the subset zero-one loss. The zero-one loss considers the entire set of labels for a given sample incorrect if it does entirely match the true set of labels. Hamming loss is more forgiving in that it penalizes the individual labels.
The Hamming loss is upperbounded by the subset zero-one loss. When normalized over samples, the Hamming loss is always between 0 and 1.

References

[R157158], [R158158]

Examples

```python
>>> from sklearn.metrics import hamming_loss

>>> y_pred = [1, 2, 3, 4]
>>> y_true = [2, 2, 3, 4]
>>> hamming_loss(y_true, y_pred)
0.25
```

In the multilabel case with binary label indicators:

```python
>>> hamming_loss(np.array([[0, 1], [1, 1]]), np.zeros((2, 2)))
0.75
```

Examples using `sklearn.metrics.hamming_loss`

- **Model Complexity Influence**

`sklearn.metrics.hinge_loss`

`sklearn.metrics.hinge_loss` *(y_true, pred_decision, labels=None, sample_weight=None)*

Average hinge loss (non-regularized)

In binary class case, assuming labels in `y_true` are encoded with +1 and -1, when a prediction mistake is made, `margin = y_true * pred_decision` is always negative (since the signs disagree), implying `1 - margin` is always greater than 1. The cumulated hinge loss is therefore an upper bound of the number of mistakes made by the classifier.

In multiclass case, the function expects that either all the labels are included in `y_true` or an optional labels argument is provided which contains all the labels. The multilabel margin is calculated according to Crammer-Singer’s method. As in the binary case, the cumulated hinge loss is an upper bound of the number of mistakes made by the classifier.

Read more in the `User Guide`.

**Parameters**

- `y_true` : array, shape=[n_samples]
  
  True target, consisting of integers of two values. The positive label must be greater than the negative label.

- `pred_decision` : array, shape=[n_samples] or [n_samples, n_classes]
  
  Predicted decisions, as output by decision_function (floats).

- `labels` : array, optional, default None
  
  Contains all the labels for the problem. Used in multiclass hinge loss.

- `sample_weight` : array-like of shape=[n_samples], optional
Sample weights.

Returns **loss**: float

References

[R507509], [R508509], [R509509]

Examples

```python
>>> from sklearn import svm
>>> from sklearn.metrics import hinge_loss
>>> X = [[0], [1]]
>>> y = [-1, 1]
>>> est = svm.LinearSVC(random_state=0)
>>> est.fit(X, y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
intercept_scaling=1, loss='squared_hinge', max_iter=1000,
multi_class='ovr', penalty='l2', random_state=0, tol=0.0001,
verbose=0)
>>> pred_decision = est.decision_function([-2], [3], [0.5])
>>> pred_decision
array([-2.18..., 2.36..., 0.09...
>>> hinge_loss([-1, 1, 1], pred_decision)
0.30...

In the multiclass case:

```python
>>> X = np.array([[0], [1], [2], [3]])
>>> Y = np.array([0, 1, 2, 3])
>>> labels = np.array([0, 1, 2, 3])
>>> est = svm.LinearSVC()
>>> est.fit(X, Y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
intercept_scaling=1, loss='squared_hinge', max_iter=1000,
multi_class='ovr', penalty='l2', random_state=None, tol=0.0001,
verbose=0)
>>> pred_decision = est.decision_function([-1], [2], [3])
>>> y_true = [0, 2, 3]
>>> hinge_loss(y_true, pred_decision, labels)
0.56...
```

sklearn.metrics.jaccard_similarity_score

**sklearn.metrics.jaccard_similarity_score***(y_true, y_pred, normalize=True, sample_weight=None)***

Jaccard similarity coefficient score

The Jaccard index [1], or Jaccard similarity coefficient, defined as the size of the intersection divided by the size of the union of two label sets, is used to compare set of predicted labels for a sample to the corresponding set of labels in *y_true*.

Read more in the *User Guide*.

**Parameters**

- **y_true**: 1d array-like, or label indicator array / sparse matrix
Ground truth (correct) labels.

**y_pred**: 1d array-like, or label indicator array / sparse matrix

Predicted labels, as returned by a classifier.

**normalize**: bool, optional (default=True)

If False, return the sum of the Jaccard similarity coefficient over the sample set. Otherwise, return the average of Jaccard similarity coefficient.

**sample_weight**: array-like of shape = [n_samples], optional

Sample weights.

**Returns score**: float

If normalize == True, return the average Jaccard similarity coefficient, else it returns the sum of the Jaccard similarity coefficient over the sample set.

The best performance is 1 with normalize == True and the number of samples with normalize == False.

**See also:**

accuracy_score, hamming_loss, zero_one_loss

**Notes**

In binary and multiclass classification, this function is equivalent to the accuracy_score. It differs in the multilabel classification problem.

**References**

[R163163]

**Examples**

```python
>>> import numpy as np
>>> from sklearn.metrics import jaccard_similarity_score
>>> y_pred = [0, 2, 1, 3]
>>> y_true = [0, 1, 2, 3]
>>> jaccard_similarity_score(y_true, y_pred)
0.5
>>> jaccard_similarity_score(y_true, y_pred, normalize=False)
2
```

In the multilabel case with binary label indicators:

```python
>>> jaccard_similarity_score(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.75
```

**Examples using sklearn.metrics.jaccard_similarity_score**

- **Classifier Chain**
Log loss, aka logistic loss or cross-entropy loss. This is the loss function used in (multinomial) logistic regression and extensions of it such as neural networks, defined as the negative log-likelihood of the true labels given a probabilistic classifier’s predictions. The log loss is only defined for two or more labels. For a single sample with true label $y_t$ in $\{0,1\}$ and estimated probability $y_p$ that $y_t = 1$, the log loss is

$$-\log P(y_t|y_p) = -(y_t \log(y_p) + (1 - y_t) \log(1 - y_p))$$

Read more in the User Guide.

**Parameters**

- **y_true**: array-like or label indicator matrix
  - Ground truth (correct) labels for n_samples samples.

- **y_pred**: array-like of float, shape = (n_samples, n_classes) or (n_samples,)
  - Predicted probabilities, as returned by a classifier’s predict_proba method. If y_pred.
    - shape = (n_samples, ) the probabilities provided are assumed to be that of the positive class. The labels in y_pred are assumed to be ordered alphabetically, as done by preprocessing.LabelBinarizer.

- **eps**: float
  - Log loss is undefined for $p=0$ or $p=1$, so probabilities are clipped to max(eps, min(1 - eps, p)).

- **normalize**: bool, optional (default=True)
  - If true, return the mean loss per sample. Otherwise, return the sum of the per-sample losses.

- **sample_weight**: array-like of shape = [n_samples], optional
  - Sample weights.

- **labels**: array-like, optional (default=None)
  - If not provided, labels will be inferred from y_true. If labels is None and y_pred has shape (n_samples,) the labels are assumed to be binary and are inferred from y_true. .. versionadded:: 0.18

**Returns**

- **loss**: float

**Notes**

The logarithm used is the natural logarithm (base-e).

**References**

Examples using `sklearn.metrics.log_loss`

- Probability Calibration for 3-class classification
- Probabilistic predictions with Gaussian process classification (GPC)

**sklearn.metrics.matthews_corrcoef**

`sklearn.metrics.matthews_corrcoef(y_true, y_pred, sample_weight=None)`

Compute the Matthews correlation coefficient (MCC)

The Matthews correlation coefficient is used in machine learning as a measure of the quality of binary (two-class) classifications. It takes into account true and false positives and negatives and is generally regarded as a balanced measure which can be used even if the classes are of very different sizes. The MCC is in essence a correlation coefficient value between -1 and +1. A coefficient of +1 represents a perfect prediction, 0 an average random prediction and -1 an inverse prediction. The statistic is also known as the phi coefficient. [source: Wikipedia]

Binary and multiclass labels are supported. Only in the binary case does this relate to information about true and false positives and negatives. See references below.

Read more in the User Guide.

**Parameters**

- `y_true` : array, shape = [n_samples]
  
  Ground truth (correct) target values.

- `y_pred` : array, shape = [n_samples]
  
  Estimated targets as returned by a classifier.

- `sample_weight` : array-like of shape = [n_samples], default None
  
  Sample weights.

**Returns**

- `mcc` : float
  
  The Matthews correlation coefficient (+1 represents a perfect prediction, 0 an average random prediction and -1 and inverse prediction).

**References**

[R519522], [R520522], [R521522], [R522522]

**Examples**
>>> from sklearn.metrics import matthews_corrcoef
>>> y_true = [+1, +1, +1, -1]
>>> y_pred = [+1, -1, +1, +1]
>>> matthews_corrcoef(y_true, y_pred)
-0.33...

sklearn.metrics.precision_recall_curve

sklearn.metrics.precision_recall_curve(y_true, probas_pred, pos_label=None, sample_weight=None)

Compute precision-recall pairs for different probability thresholds

Note: this implementation is restricted to the binary classification task.

The precision is the ratio \( \frac{tp}{tp + fp} \) where \( tp \) is the number of true positives and \( fp \) the number of false positives. The precision is intuitively the ability of the classifier not to label as positive a sample that is negative.

The recall is the ratio \( \frac{tp}{tp + fn} \) where \( tp \) is the number of true positives and \( fn \) the number of false negatives. The recall is intuitively the ability of the classifier to find all the positive samples.

The last precision and recall values are 1. and 0. respectively and do not have a corresponding threshold. This ensures that the graph starts on the y axis.

Read more in the User Guide.

Parameters

- **y_true**: array, shape = [n_samples]
  True targets of binary classification in range {-1, 1} or {0, 1}.

- **probas_pred**: array, shape = [n_samples]
  Estimated probabilities or decision function.

- **pos_label**: int or str, default=None
  The label of the positive class

- **sample_weight**: array-like of shape = [n_samples], optional
  Sample weights.

Returns

- **precision**: array, shape = [n_thresholds + 1]
  Precision values such that element i is the precision of predictions with score \( \geq \) thresholds[i] and the last element is 1.

- **recall**: array, shape = [n_thresholds + 1]
  Decreasing recall values such that element i is the recall of predictions with score \( \geq \) thresholds[i] and the last element is 0.

- **thresholds**: array, shape = [n_thresholds <= len(np.unique(probas_pred))]
  Increasing thresholds on the decision function used to compute precision and recall.

See also:

- **average_precision_score**: Compute average precision from prediction scores
- **roc_curve**: Compute Receiver operating characteristic (ROC) curve
Examples

```python
>>> import numpy as np
>>> from sklearn.metrics import precision_recall_curve
>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> precision, recall, thresholds = precision_recall_curve(y_true, y_scores)
>>> precision
array([ 0.66..., 0.5 , 1. , 1. ])
>>> recall
array([ 1. , 0.5, 0.5, 0. ])
>>> thresholds
array([ 0.35, 0.4 , 0.8 ])
```
labels : list, optional

The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y_true and y_pred are used in sorted order.

pos_label : str or int, 1 by default

The class to report if average='binary' and the data is binary. If the data are multiclass or multilabel, this will be ignored; setting labels=[pos_label] and average != 'binary' will report scores for that label only.

average : string, [None (default), 'binary', 'micro', 'macro', 'samples', 'weighted']

If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

'binary': Only report results for the class specified by pos_label. This is applicable only if targets (y_{true, pred}) are binary.
'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.
'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.
'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy_score).

warn_for : tuple or set, for internal use

This determines which warnings will be made in the case that this function is being used to return only one of its metrics.

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

Returns precision : float (if average is not None) or array of float, shape = [n_unique_labels]
recall : float (if average is not None) or array of float, , shape = [n_unique_labels]
fbeta_score : float (if average is not None) or array of float, shape = [n_unique_labels]
support : int (if average is not None) or array of int, shape = [n_unique_labels]

The number of occurrences of each label in y_true.

References

[R527529], [R528529], [R529529]
Examples

```python
>>> from sklearn.metrics import precision_recall_fscore_support
>>> y_true = np.array(['cat', 'dog', 'pig', 'cat', 'dog', 'pig'])
>>> y_pred = np.array(['cat', 'pig', 'dog', 'cat', 'cat', 'dog'])
>>> precision_recall_fscore_support(y_true, y_pred, average='macro')
...  (0.22..., 0.33..., 0.26..., None)
>>> precision_recall_fscore_support(y_true, y_pred, average='micro')
...  (0.33..., 0.33..., 0.33..., None)
>>> precision_recall_fscore_support(y_true, y_pred, average='weighted')
...  (0.22..., 0.33..., 0.26..., None)
```

It is possible to compute per-label precisions, recalls, F1-scores and supports instead of averaging:

```python
>>> precision_recall_fscore_support(y_true, y_pred, average=None, labels=['pig', 'dog', 'cat']) # doctest: +ELLIPSIS,+NORMALIZE_WHITESPACE
(array([ 0. , 0. , 0.66...]), array([ 0., 0., 1.]), array([ 0. , 0. , 0.8]), array([2, 2, 2]))
```

**sklearn.metrics.precision_score**

`sklearn.metrics.precision_score(y_true, y_pred, labels=None, pos_label=1, average='binary', sample_weight=None)`

Compute the precision

The precision is the ratio $\frac{tp}{tp + fp}$ where $tp$ is the number of true positives and $fp$ the number of false positives. The precision is intuitively the ability of the classifier not to label as positive a sample that is negative.

The best value is 1 and the worst value is 0.


**Parameters**

- `y_true`: 1d array-like, or label indicator array / sparse matrix
  
  Ground truth (correct) target values.

- `y_pred`: 1d array-like, or label indicator array / sparse matrix
  
  Estimated targets as returned by a classifier.

- `labels`: list, optional
  
  The set of labels to include when `average != 'binary'`, and their order if `average` is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in `y_true` and `y_pred` are used in sorted order.

  Changed in version 0.17: parameter `labels` improved for multiclass problem.

- `pos_label`: str or int, 1 by default
  
  The class to report if `average='binary'` and the data is binary. If the data are multiclass or multilabel, this will be ignored; setting `labels=[pos_label]` and `average != 'binary'` will report scores for that label only.

This parameter is required for multiclass/multilabel targets. If None, the scores for each
class are returned. Otherwise, this determines the type of averaging performed on the
data:

'binary': Only report results for the class specified by pos_label. This is applicable
only if targets (y_true, y_pred) are binary.

'micro': Calculate metrics globally by counting the total true positives, false
negatives and false positives.

'macro': Calculate metrics for each label, and find their unweighted mean. This does
not take label imbalance into account.

'weighted': Calculate metrics for each label, and find their average, weighted by
support (the number of true instances for each label). This alters ‘macro’ to account
for label imbalance; it can result in an F-score that is not between precision and recall.

'samples': Calculate metrics for each instance, and find their average (only mean-
ingful for multilabel classification where this differs from accuracy_score).

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

Returns precision : float (if average is not None) or array of float, shape = [n_unique_labels]

Precision of the positive class in binary classification or weighted average of the pre-
cision of each class for the multiclass task.

Examples

```python
>>> from sklearn.metrics import precision_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> precision_score(y_true, y_pred, average='macro')
0.22...
>>> precision_score(y_true, y_pred, average='micro')
0.33...
>>> precision_score(y_true, y_pred, average='weighted')
...
0.22...
```

Examples using sklearn.metrics.precision_score

- Probability Calibration curves

sklearn.metrics.recall_score

```python
sklearn.metrics.recall_score (y_true, y_pred, labels=None, pos_label=1, average='binary', sample_weight=None)
```

Compute the recall

The recall is the ratio tp / (tp + fn) where tp is the number of true positives and fn the number of false
negatives. The recall is intuitively the ability of the classifier to find all the positive samples.
The best value is 1 and the worst value is 0.

Read more in the User Guide.

Parameters y_true : 1d array-like, or label indicator array / sparse matrix

Ground truth (correct) target values.

y_pred : 1d array-like, or label indicator array / sparse matrix

Estimated targets as returned by a classifier.

labels : list, optional

The set of labels to include when average != 'binary', and their order if average is None. Labels present in the data can be excluded, for example to calculate a multiclass average ignoring a majority negative class, while labels not present in the data will result in 0 components in a macro average. For multilabel targets, labels are column indices. By default, all labels in y_true and y_pred are used in sorted order.

Changed in version 0.17: parameter labels improved for multiclass problem.

pos_label : str or int, 1 by default

The class to report if average='binary' and the data is binary. If the data are multiclass or multilabel, this will be ignored; setting labels=[pos_label] and average != 'binary' will report scores for that label only.

average : string, [None, 'binary' (default), 'micro', 'macro', 'samples', 'weighted']

This parameter is required for multiclass/multilabel targets. If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

'binary': Only report results for the class specified by pos_label. This is applicable only if targets (y_true,pred) are binary.

'micro': Calculate metrics globally by counting the total true positives, false negatives and false positives.

'macro': Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.

'weighted': Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label). This alters 'macro' to account for label imbalance; it can result in an F-score that is not between precision and recall.

'samples': Calculate metrics for each instance, and find their average (only meaningful for multilabel classification where this differs from accuracy_score).

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

Returns recall : float (if average is not None) or array of float, shape = [n_unique_labels]

Recall of the positive class in binary classification or weighted average of the recall of each class for the multiclass task.
Examples

```python
>>> from sklearn.metrics import recall_score
>>> y_true = [0, 1, 2, 0, 1, 2]
>>> y_pred = [0, 2, 1, 0, 0, 1]
>>> recall_score(y_true, y_pred, average='macro')
0.33...
>>> recall_score(y_true, y_pred, average='micro')
0.33...
>>> recall_score(y_true, y_pred, average='weighted')
0.33...
>>> recall_score(y_true, y_pred, average=None)
array([ 1., 0., 0.])
```

Examples using `sklearn.metrics.recall_score`

- *Probability Calibration curves*

`sklearn.metrics.roc_auc_score`

`sklearn.metrics.roc_auc_score(y_true, y_score, average='macro', sample_weight=None)`

Compute Area Under the Receiver Operating Characteristic Curve (ROC AUC) from prediction scores.

Note: this implementation is restricted to the binary classification task or multilabel classification task in label indicator format.

Read more in the User Guide.

**Parameters**

- **y_true** : array, shape = [n_samples] or [n_samples, n_classes]
  True binary labels or binary label indicators.

- **y_score** : array, shape = [n_samples] or [n_samples, n_classes]
  Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision_function” on some classifiers). For binary y_true, y_score is supposed to be the score of the class with greater label.

- **average** : string, [None, ‘micro’, ‘macro’ (default), ‘samples’, ‘weighted’]
  If None, the scores for each class are returned. Otherwise, this determines the type of averaging performed on the data:

  - ‘micro’: Calculate metrics globally by considering each element of the label indicator matrix as a label.
  - ‘macro’: Calculate metrics for each label, and find their unweighted mean. This does not take label imbalance into account.
  - ‘weighted’: Calculate metrics for each label, and find their average, weighted by support (the number of true instances for each label).
  - ‘samples’: Calculate metrics for each instance, and find their average.

- **sample_weight** : array-like of shape = [n_samples], optional
  Sample weights.

**Returns**

- **auc** : float
See also:

- `average_precision_score`: Area under the precision-recall curve
- `roc_curve`: Compute Receiver operating characteristic (ROC) curve

References

[R535535]

Examples

```python
>>> import numpy as np
>>> from sklearn.metrics import roc_auc_score

>>> y_true = np.array([0, 0, 1, 1])
>>> y_scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> roc_auc_score(y_true, y_scores)
0.75
```

**sklearn.metrics.roc_curve**

`sklearn.metrics.roc_curve(y_true, y_score, pos_label=None, sample_weight=None, drop_intermediate=True)`  
Compute Receiver operating characteristic (ROC)  

Note: this implementation is restricted to the binary classification task.  

Read more in the *User Guide*.

**Parameters**

- `y_true`: array, shape = [n_samples]  
  True binary labels. If labels are not either {-1, 1} or {0, 1}, then `pos_label` should be explicitly given.

- `y_score`: array, shape = [n_samples]  
  Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision_function” on some classifiers).

- `pos_label`: int or str, default=None  
  Label considered as positive and others are considered negative.

- `sample_weight`: array-like of shape = [n_samples], optional  
  Sample weights.

- `drop_intermediate`: boolean, optional (default=True)  
  Whether to drop some suboptimal thresholds which would not appear on a plotted ROC curve. This is useful in order to create lighter ROC curves.  
  New in version 0.17: parameter `drop_intermediate`.

**Returns**

- `fpr`: array, shape = [>2]  
  Increasing false positive rates such that element i is the false positive rate of predictions with score >= thresholds[i].
tpr : array, shape = [>2]
Increasing true positive rates such that element i is the true positive rate of predictions
with score >= thresholds[i].

thresholds : array, shape = [n_thresholds]
Decreasing thresholds on the decision function used to compute fpr and tpr. thresholds[0]
represents no instances being predicted and is arbitrarily set to max(y_score) + 1.

See also:

roc_auc_score Compute the area under the ROC curve

Notes

Since the thresholds are sorted from low to high values, they are reversed upon returning them to ensure they
 correspond to both fpr and tpr, which are sorted in reversed order during their calculation.

References

[R167167]

Examples

```python
>>> import numpy as np
>>> from sklearn import metrics
>>> y = np.array([1, 1, 2, 2])
>>> scores = np.array([0.1, 0.4, 0.35, 0.8])
>>> fpr, tpr, thresholds = metrics.roc_curve(y, scores, pos_label=2)
>>> fpr
array([ 0. , 0.5, 0.5, 1. ])
>>> tpr
array([ 0.5, 0.5, 1. , 1. ])
>>> thresholds
array([ 0.8 , 0.4 , 0.35, 0.1 ])
```

Examples using sklearn.metrics.roc_curve

- Species distribution modeling
- Feature transformations with ensembles of trees
- Receiver Operating Characteristic (ROC) with cross validation
- Receiver Operating Characteristic (ROC)

sklearn.metrics.zero_one_loss

sklearn.metrics.zero_one_loss(y_true, y_pred, normalize=True, sample_weight=None)
Zero-one classification loss.
If normalize is True, return the fraction of misclassifications (float), else it returns the number of misclassifications (int). The best performance is 0.

Read more in the User Guide.

Parameters

- **y_true**: 1d array-like, or label indicator array / sparse matrix
  Ground truth (correct) labels.

- **y_pred**: 1d array-like, or label indicator array / sparse matrix
  Predicted labels, as returned by a classifier.

- **normalize**: bool, optional (default=True)
  If False, return the number of misclassifications. Otherwise, return the fraction of misclassifications.

- **sample_weight**: array-like of shape = [n_samples], optional
  Sample weights.

Returns** loss**: float or int,

- If normalize == True, return the fraction of misclassifications (float), else it returns the number of misclassifications (int).

See also:

accuracy_score, hamming_loss, jaccard_similarity_score

Notes

In multilabel classification, the zero_one_loss function corresponds to the subset zero-one loss: for each sample, the entire set of labels must be correctly predicted, otherwise the loss for that sample is equal to one.

Examples

```python
>>> from sklearn.metrics import zero_one_loss
>>> y_pred = [1, 2, 3, 4]
>>> y_true = [2, 2, 3, 4]
>>> zero_one_loss(y_true, y_pred)
0.25
>>> zero_one_loss(y_true, y_pred, normalize=False)
1
```

In the multilabel case with binary label indicators:

```python
>>> zero_one_loss(np.array([[0, 1], [1, 1]]), np.ones((2, 2)))
0.5
```

Examples using **sklearn.metrics.zero_one_loss**

- **Discrete versus Real AdaBoost**

30.21. sklearn.metrics: Metrics 1717
30.21.3 Regression metrics

See the Regression metrics section of the user guide for further details.

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**sklearn.metrics.explained_variance_score**

```
sklearn.metrics.explained_variance_score(y_true, y_pred, sample_weight=None, multioutput='uniform_average')
```

Explained variance regression score function

Best possible score is 1.0, lower values are worse.

Read more in the User Guide.

**Parameters**

- **y_true**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Ground truth (correct) target values.

- **y_pred**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Estimated target values.

- **sample_weight**: array-like of shape = (n_samples), optional
  Sample weights.

- **multioutput**: string in ['raw_values', 'uniform_average', 'variance_weighted'] or array-like of shape (n_outputs)
  Defines aggregating of multiple output scores. Array-like value defines weights used to average scores.

  - ‘raw_values’: Returns a full set of scores in case of multioutput input.
  - ‘uniform_average’: Scores of all outputs are averaged with uniform weight.
  - ‘variance_weighted’: Scores of all outputs are averaged, weighted by the variances of each individual output.

**Returns**

- **score**: float or ndaray of floats
  The explained variance or ndarray if ‘multioutput’ is ‘raw_values’.

**Notes**

This is not a symmetric function.
Examples

```python
>>> from sklearn.metrics import explained_variance_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> explained_variance_score(y_true, y_pred)
0.957...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> explained_variance_score(y_true, y_pred, multioutput='uniform_average')
... 0.983...
```

`scklearn.metrics.mean_absolute_error`

`scklearn.metrics.mean_absolute_error`(y_true, y_pred, sample_weight=None, multioutput='uniform_average')

Mean absolute error regression loss

Read more in the `User Guide`

Parameters:
- `y_true`: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Ground truth (correct) target values.
- `y_pred`: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Estimated target values.
- `sample_weight`: array-like of shape = (n_samples), optional
  Sample weights.
- `multioutput`: string in ['raw_values', 'uniform_average']
  or array-like of shape (n_outputs) Defines aggregating of multiple output values. Arraylike value defines weights used to average errors.
  - 'raw_values': Returns a full set of errors in case of multioutput input.
  - 'uniform_average': Errors of all outputs are averaged with uniform weight.

Returns:
- `loss`: float or ndarray of floats
  If multioutput is ‘raw_values’, then mean absolute error is returned for each output separately. If multioutput is ‘uniform_average’ or an ndarray of weights, then the weighted average of all output errors is returned.
  MAE output is non-negative floating point. The best value is 0.0.

Examples

```python
>>> from sklearn.metrics import mean_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> mean_absolute_error(y_true, y_pred)
0.5
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
```
```python
>>> mean_absolute_error(y_true, y_pred)
0.75
>>> mean_absolute_error(y_true, y_pred, multioutput='raw_values')
array([ 0.5, 1. ])
>>> mean_absolute_error(y_true, y_pred, multioutput=[0.3, 0.7])
... 0.849...
```

**sklearn.metrics.mean_squared_error**


**Parameters**

- **y_true**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Ground truth (correct) target values.
- **y_pred**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  Estimated target values.
- **sample_weight**: array-like of shape = (n_samples), optional
  Sample weights.
- **multioutput**: string in ['raw_values', 'uniform_average']
  or array-like of shape (n_outputs) Defines aggregating of multiple output values. Array-like value defines weights used to average errors.
  - 'raw_values': Returns a full set of errors in case of multioutput input.
  - 'uniform_average': Errors of all outputs are averaged with uniform weight.

**Returns**

- **loss**: float or ndarray of floats
  A non-negative floating point value (the best value is 0.0), or an array of floating point values, one for each individual target.

**Examples**

```python
>>> from sklearn.metrics import mean_squared_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> mean_squared_error(y_true, y_pred)
0.375
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> mean_squared_error(y_true, y_pred)
0.708...
>>> mean_squared_error(y_true, y_pred, multioutput='raw_values')
... array([ 0.416..., 1. ])
>>> mean_squared_error(y_true, y_pred, multioutput=[0.3, 0.7])
... 0.824...
```
Examples using sklearn.metrics.mean_squared_log_error

- Model Complexity Influence
- Gradient Boosting regression
- Plot Ridge coefficients as a function of the L2 regularization
- Linear Regression Example
- Robust linear estimator fitting

sklearn.metrics.mean_squared_log_error

sklearn.metrics.mean_squared_log_error(y_true, y_pred, sample_weight=None, multioutput='uniform_average')

Mean squared logarithmic error regression loss

Read more in the User Guide.

Parameters

- y_true : array-like of shape = (n_samples) or (n_samples, n_outputs)
  Ground truth (correct) target values.
- y_pred : array-like of shape = (n_samples) or (n_samples, n_outputs)
  Estimated target values.
- sample_weight : array-like of shape = (n_samples), optional
  Sample weights.
- multioutput : string in ['raw_values', 'uniform_average'] or array-like of shape = (n_outputs)
  Defines aggregating of multiple output values. Array-like value defines weights used to
  average errors.

- 'raw_values': Returns a full set of errors when the input is of multioutput format.
- 'uniform_average': Errors of all outputs are averaged with uniform weight.

Returns

- loss : float or ndarray of floats
  A non-negative floating point value (the best value is 0.0), or an array of floating point
  values, one for each individual target.

Examples

```python
>>> from sklearn.metrics import mean_squared_log_error
>>> y_true = [3, 5, 2.5, 7]
>>> y_pred = [2.5, 5, 4, 8]
>>> mean_squared_log_error(y_true, y_pred)
0.039...
>>> y_true = [[0.5, 1], [1, 2], [7, 6]]
>>> y_pred = [[0.5, 2], [1, 2.5], [8, 8]]
>>> mean_squared_log_error(y_true, y_pred)
0.044...
>>> mean_squared_log_error(y_true, y_pred, multioutput='raw_values')
...
array([ 0.004..., 0.083...])
>>> mean_squared_log_error(y_true, y_pred, multioutput=[0.3, 0.7])
```
sklearn.metrics.median_absolute_error

**sklearn.metrics.median_absolute_error** *(y_true, y_pred)*

Median absolute error regression loss

Read more in the *User Guide*.

**Parameters**

- **y_true**: array-like of shape = (n_samples)
  - Ground truth (correct) target values.
- **y_pred**: array-like of shape = (n_samples)
  - Estimated target values.

**Returns**

- **loss**: float
  - A positive floating point value (the best value is 0.0).

**Examples**

```python
>>> from sklearn.metrics import median_absolute_error
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> median_absolute_error(y_true, y_pred)
0.5
```

sklearn.metrics.r2_score

**sklearn.metrics.r2_score** *(y_true, y_pred, sample_weight=None, multioutput=’uniform_average’)*

$R^2$ (coefficient of determination) regression score function.

Best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a $R^2$ score of 0.0.

Read more in the *User Guide*.

**Parameters**

- **y_true**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  - Ground truth (correct) target values.
- **y_pred**: array-like of shape = (n_samples) or (n_samples, n_outputs)
  - Estimated target values.
- **sample_weight**: array-like of shape = (n_samples), optional
  - Sample weights.
- **multioutput**: string in [‘raw_values’, ‘uniform_average’, ‘variance_weighted’] or None or array-like of shape (n_outputs)
  - Defines aggregating of multiple output scores. Array-like value defines weights used to average scores. Default is “uniform_average”.
  - **raw_values**: Returns a full set of scores in case of multioutput input.
scikit-learn user guide, Release 0.20.dev0

'uniform_average': Scores of all outputs are averaged with uniform weight.

'veariance_weighted': Scores of all outputs are averaged, weighted by the variances of each individual output.

Changed in version 0.19: Default value of multioutput is 'uniform_average'.

Returns z: float or ndarray of floats

The R^2 score or ndarray of scores if multioutput is 'raw_values'.

Notes

This is not a symmetric function.

Unlike most other scores, R^2 score may be negative (it need not actually be the square of a quantity R).

References

[R165165]

Examples

```python
>>> from sklearn.metrics import r2_score
>>> y_true = [3, -0.5, 2, 7]
>>> y_pred = [2.5, 0.0, 2, 8]
>>> r2_score(y_true, y_pred)
0.948...
>>> y_true = [[0.5, 1], [-1, 1], [7, -6]]
>>> y_pred = [[0, 2], [-1, 2], [8, -5]]
>>> r2_score(y_true, y_pred, multioutput='variance_weighted')
... 0.938...
>>> y_true = [1, 2, 3]
>>> y_pred = [1, 2, 3]
>>> r2_score(y_true, y_pred)
1.0
>>> y_true = [1, 2, 3]
>>> y_pred = [2, 2, 2]
>>> r2_score(y_true, y_pred)
0.0
>>> y_true = [1, 2, 3]
>>> y_pred = [3, 2, 1]
>>> r2_score(y_true, y_pred)
-3.0
```

Examples using sklearn.metrics.r2_score

- Linear Regression Example
- Lasso and Elastic Net for Sparse Signals
30.21.4 Multilabel ranking metrics

See the Multilabel ranking metrics section of the user guide for further details.

metrics.coverage_error(y_true, y_score[, ...]) Coverage error measure

metrics.label_ranking_average_precision_score(...) Compute ranking-based average precision

metrics.label_ranking_loss(y_true, y_score) Compute Ranking loss measure

sklearn.metrics.coverage_error

sklearn.metrics.coverage_error(y_true, y_score, sample_weight=None)

Coverage error measure

Compute how far we need to go through the ranked scores to cover all true labels. The best value is equal to the average number of labels in y_true per sample.

Ties in y_scores are broken by giving maximal rank that would have been assigned to all tied values.

Note: Our implementation’s score is 1 greater than the one given in Tsoumakas et al., 2010. This extends it to handle the degenerate case in which an instance has 0 true labels.

Read more in the User Guide.

Parameters y_true : array, shape = [n_samples, n_labels]

True binary labels in binary indicator format.

y_score : array, shape = [n_samples, n_labels]

Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision_function” on some classifiers).

sample_weight : array-like of shape = [n_samples], optional

Sample weights.

Returns coverage_error : float

References

[R491491]

sklearn.metrics.label_ranking_average_precision_score

sklearn.metrics.label_ranking_average_precision_score(y_true, y_score)

Compute ranking-based average precision

Label ranking average precision (LRAP) is the average over each ground truth label assigned to each sample, of the ratio of true vs. total labels with lower score.

This metric is used in multilabel ranking problem, where the goal is to give better rank to the labels associated to each sample.

The obtained score is always strictly greater than 0 and the best value is 1.

Read more in the User Guide.

Parameters y_true : array or sparse matrix, shape = [n_samples, n_labels]
True binary labels in binary indicator format.

\texttt{y\_score} : array, shape = [n\_samples, n\_labels]

Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision\_function” on some classifiers).

**Returns** score : float

**Examples**

```python
>>> import numpy as np
>>> from sklearn.metrics import label_ranking_average_precision_score
>>> y_true = np.array([[1, 0, 0], [0, 0, 1]])
>>> y_score = np.array([[0.75, 0.5, 1], [1, 0.2, 0.1]])
>>> label_ranking_average_precision_score(y_true, y_score)
0.416...
```

**sklearn.metrics.label_ranking_loss**

sklearn.metrics.label_ranking_loss (y_true, y_score, sample_weight=None)

Compute Ranking loss measure

Compute the average number of label pairs that are incorrectly ordered given y\_score weighted by the size of the label set and the number of labels not in the label set.

This is similar to the error set size, but weighted by the number of relevant and irrelevant labels. The best performance is achieved with a ranking loss of zero.

Read more in the User Guide.

New in version 0.17: A function label\_ranking\_loss

**Parameters**

- **y_true** : array or sparse matrix, shape = [n\_samples, n\_labels]
  
  True binary labels in binary indicator format.
  
  **y\_score** : array, shape = [n\_samples, n\_labels]
  
  Target scores, can either be probability estimates of the positive class, confidence values, or non-thresholded measure of decisions (as returned by “decision\_function” on some classifiers).
  
  **sample_weight** : array-like of shape = [n\_samples], optional
  
  Sample weights.

**Returns** loss : float

**References**

[R517517]
30.21.5 Clustering metrics

See the Clustering performance evaluation section of the user guide for further details. The sklearn.metrics.cluster submodule contains evaluation metrics for cluster analysis results. There are two forms of evaluation:

- supervised, which uses a ground truth class values for each sample.
- unsupervised, which does not and measures the ‘quality’ of the model itself.

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<td>V-measure cluster labeling given a ground truth.</td>
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**sklearn.metrics.adjusted_mutual_info_score**

Adjusted Mutual Information between two clusterings.

Adjusted Mutual Information (AMI) is an adjustment of the Mutual Information (MI) score to account for chance. It accounts for the fact that the MI is generally higher for two clusterings with a larger number of clusters, regardless of whether there is actually more information shared. For two clusterings $U$ and $V$, the AMI is given as:

$$AMI(U, V) = \frac{MI(U, V) - E(MI(U, V))}{\max(H(U), H(V)) - E(MI(U, V))}$$

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score value in any way.

This metric is furthermore symmetric: switching label_true with label_pred will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Be mindful that this function is an order of magnitude slower than other metrics, such as the Adjusted Rand Index.

Read more in the User Guide.

**Parameters**

- **labels_true** : int array, shape = [n_samples]
  
  A clustering of the data into disjoint subsets.

- **labels_pred** : array, shape = [n_samples]
A clustering of the data into disjoint subsets.

**Returns**  
ami: float (upperlimited by 1.0)

The AMI returns a value of 1 when the two partitions are identical (ie perfectly matched). Random partitions (independent labellings) have an expected AMI around 0 on average hence can be negative.

See also:

- `adjusted_rand_score`  Adjusted Rand Index
- `mutual_information_score`  Mutual Information (not adjusted for chance)

**References**

[R139140], [R140140]

**Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```python
>>> from sklearn.metrics.cluster import adjusted_mutual_info_score
>>> adjusted_mutual_info_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> adjusted_mutual_info_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

If classes members are completely split across different clusters, the assignment is totally in-complete, hence the AMI is null:

```python
>>> adjusted_mutual_info_score([0, 0, 0, 0], [0, 1, 2, 3])
0.0
```

**Examples using sklearn.metrics.adjusted_mutual_info_score**

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data

**sklearn.metrics.adjusted_rand_score**

```python
sklearn.metrics.adjusted_rand_score(labels_true, labels_pred)
```

Rand index adjusted for chance.

The Rand Index computes a similarity measure between two clusterings by considering all pairs of samples and counting pairs that are assigned in the same or different clusters in the predicted and true clusterings.

The raw RI score is then “adjusted for chance” into the ARI score using the following scheme:
The adjusted Rand index is thus ensured to have a value close to 0.0 for random labeling independently of the number of clusters and samples and exactly 1.0 when the clusterings are identical (up to a permutation).

ARI is a symmetric measure:

\[
\text{adjusted_rand_score}(a, b) = \frac{\text{ARI}(a, b)}{\text{ARI}(b, a)}
\]

Read more in the User Guide.

**Parameters**

- **labels_true**: int array, shape = [n_samples]
  Ground truth class labels to be used as a reference

- **labels_pred**: array, shape = [n_samples]
  Cluster labels to evaluate

**Returns**

- **ari**: float
  Similarity score between -1.0 and 1.0. Random labelings have an ARI close to 0.0. 1.0 stands for perfect match.

See also:

- `adjusted_mutual_info_score` Adjusted Mutual Information

**Examples**

Perfectly matching labelings have a score of 1 even

```python
>>> from sklearn.metrics.cluster import adjusted_rand_score
>>> adjusted_rand_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> adjusted_rand_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Labelings that assign all classes members to the same clusters are complete but not always pure, hence penalized:

```python
>>> adjusted_rand_score([0, 0, 1, 2], [0, 0, 1, 1])
0.57...
```

ARI is symmetric, so labelings that have pure clusters with members coming from the same classes but unnecessary splits are penalized:

```python
>>> adjusted_rand_score([0, 0, 1, 1], [0, 0, 1, 2])
0.57...
```

If classes members are completely split across different clusters, the assignment is totally incomplete, hence the ARI is very low:
Examples using `sklearn.metrics.adjusted_rand_score`

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

`sklearn.metrics.calinski_harabaz_score`

`sklearn.metrics.calinski_harabaz_score(X, labels)`

Compute the Calinski and Harabaz score.

The score is defined as ratio between the within-cluster dispersion and the between-cluster dispersion.

Read more in the User Guide.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  List of n_features-dimensional data points. Each row corresponds to a single data point.

- **labels**: array-like, shape (n_samples,)
  
  Predicted labels for each sample.

**Returns**

- **score**: float
  
  The resulting Calinski-Harabaz score.

**References**

[R479479]

`sklearn.metrics.completeness_score`

`sklearn.metrics.completeness_score(labels_true, labels_pred)`

Completeness metric of a cluster labeling given a ground truth.

A clustering result satisfies completeness if all the data points that are members of a given class are elements of the same cluster.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won't change the score value in any way.

This metric is not symmetric: switching `label_true` with `label_pred` will return the `homogeneity_score` which will be different in general.

Read more in the User Guide.

**Parameters**

- **labels_true**: int array, shape = [n_samples]
ground truth class labels to be used as a reference

labels_pred : array, shape = [n_samples]
cluster labels to evaluate

Returns completeness : float
score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

See also:
homogeneity_score, v_measure_score

References

[R151151]

Examples

Perfect labelings are complete:

```python
>>> from sklearn.metrics.cluster import completeness_score
>>> completeness_score([[0, 0, 1, 1], [1, 1, 0, 0]])
1.0
```

Non-perfect labelings that assign all classes members to the same clusters are still complete:

```python
>>> print(completeness_score([[0, 0, 1, 1], [0, 0, 0, 0]]))
1.0
>>> print(completeness_score([[0, 1, 2, 3], [0, 0, 1, 1]]))
1.0
```

If classes members are split across different clusters, the assignment cannot be complete:

```python
>>> print(completeness_score([[0, 0, 1, 1], [0, 1, 0, 1]]))
0.0
>>> print(completeness_score([[0, 0, 0, 0], [0, 1, 2, 3]]))
0.0
```

Examples using sklearn.metrics.completeness_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

sklearn.metrics.fowlkes_mallows_score

sklearn.metrics.fowlkes_mallows_score (labels_true, labels_pred, sparse=False)
Measure the similarity of two clusterings of a set of points.

The Fowlkes-Mallows index (FMI) is defined as the geometric mean between of the precision and recall:
FMI = TP / sqrt((TP + FP) * (TP + FN))

Where TP is the number of True Positive (i.e. the number of pair of points that belongs in the same clusters in both labels_true and labels_pred), FP is the number of False Positive (i.e. the number of pair of points that belongs in the same clusters in labels_true and not in labels_pred) and FN is the number of False Negative (i.e. the number of pair of points that belongs in the same clusters in labels_pred and not in labels_true).

The score ranges from 0 to 1. A high value indicates a good similarity between two clusters.

Read more in the User Guide.

Parameters

labels_true : int array, shape = (n_samples,)
A clustering of the data into disjoint subsets.

labels_pred : array, shape = (n_samples,)
A clustering of the data into disjoint subsets.

sparse : bool
Compute contingency matrix internally with sparse matrix.

Returns

score : float
The resulting Fowlkes-Mallows score.

References

[R499500], [R500500]

Examples

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```python
>>> from sklearn.metrics.cluster import fowlkes_mallows_score
>>> fowlkes_mallows_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> fowlkes_mallows_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

If classes members are completely split across different clusters, the assignment is totally random, hence the FMI is null:

```python
>>> fowlkes_mallows_score([0, 0, 0, 0], [0, 1, 2, 3])
0.0
```

**sklearn.metrics.homogeneity_completeness_v_measure**

`sklearn.metrics.homogeneity_completeness_v_measure(labels_true, labels_pred)`

Compute the homogeneity and completeness and V-Measure scores at once.

Those metrics are based on normalized conditional entropy measures of the clustering labeling to evaluate given the knowledge of a Ground Truth class labels of the same samples.
A clustering result satisfies homogeneity if all of its clusters contain only data points which are members of a single class.

A clustering result satisfies completeness if all the data points that are members of a given class are elements of the same cluster.

Both scores have positive values between 0.0 and 1.0, larger values being desirable.

Those 3 metrics are independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score values in any way.

V-Measure is furthermore symmetric: swapping \texttt{labels_true} and \texttt{label_pred} will give the same score. This does not hold for homogeneity and completeness.

Read more in the \texttt{User Guide}.

\textbf{Parameters} \texttt{labels\_true} : int array, shape = [n\_samples]

\begin{verbatim}
ground truth class labels to be used as a reference
\end{verbatim}

\texttt{labels\_pred} : array, shape = [n\_samples]

\begin{verbatim}
cluster labels to evaluate
\end{verbatim}

\textbf{Returns} \texttt{homogeneity} : float

\begin{verbatim}
score between 0.0 and 1.0. 1.0 stands for perfectly homogeneous labeling
\end{verbatim}

\texttt{completeness} : float

\begin{verbatim}
score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling
\end{verbatim}

\texttt{v\_measure} : float

\begin{verbatim}
harmonic mean of the first two
\end{verbatim}

\textbf{See also:}

\texttt{homogeneity\_score, completeness\_score, v\_measure\_score}

\textbf{sklearn.metrics.homogeneity\_score}

\texttt{sklearn.metrics.homogeneity\_score(labels\_true, labels\_pred)}

Homogeneity metric of a cluster labeling given a ground truth.

A clustering result satisfies homogeneity if all of its clusters contain only data points which are members of a single class.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score value in any way.

This metric is not symmetric: switching \texttt{label\_true} with \texttt{label\_pred} will return the \texttt{completeness\_score} which will be different in general.

Read more in the \texttt{User Guide}.

\textbf{Parameters} \texttt{labels\_true} : int array, shape = [n\_samples]

\begin{verbatim}
ground truth class labels to be used as a reference
\end{verbatim}

\texttt{labels\_pred} : array, shape = [n\_samples]

\begin{verbatim}
cluster labels to evaluate
\end{verbatim}

\textbf{Returns} \texttt{homogeneity} : float

\begin{verbatim}
score between 0.0 and 1.0. 1.0 stands for perfectly homogeneous labeling
\end{verbatim}
See also:

completeness_score, v_measure_score

References

[R161161]

Examples

Perfect labelings are homogeneous:

```python
>>> from sklearn.metrics.cluster import homogeneity_score
>>> homogeneity_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Non-perfect labelings that further split classes into more clusters can be perfectly homogeneous:

```python
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 0, 1, 2]))
... 1.0...
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 1, 2, 3]))
... 1.0...
```

Clusters that include samples from different classes do not make for an homogeneous labeling:

```python
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 1, 0, 1]))
... 0.0...
>>> print("%.6f" % homogeneity_score([0, 0, 1, 1], [0, 0, 0, 0]))
... 0.0...
```

Examples using sklearn.metrics.homogeneity_score

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

sklearn.metrics.mutual_info_score

sklearn.metrics.mutual_info_score(labels_true, labels_pred, contingency=None)

Mutual Information between two clusterings.

The Mutual Information is a measure of the similarity between two labels of the same data. Where \(|U_i|\) is the number of the samples in cluster \(U_i\) and \(|V_j|\) is the number of the samples in cluster \(V_j\), the Mutual Information
between clusterings \( U \) and \( V \) is given as:

\[
MI(U, V) = \sum_{i=1}^{U} \sum_{j=1}^{V} \frac{|U_i \cap V_j|}{N} \log \frac{N|U_i \cap V_j|}{|U_i||V_j|}
\]

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score value in any way.

This metric is furthermore symmetric: switching \( \text{label\_true} \) with \( \text{label\_pred} \) will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Read more in the User Guide.

**Parameters**

- **labels\_true**: int array, shape = [n_samples]
  - A clustering of the data into disjoint subsets.

- **labels\_pred**: array, shape = [n_samples]
  - A clustering of the data into disjoint subsets.

- **contingency**: \{None, array, sparse matrix\}, shape = [n_classes\_true, n_classes\_pred]
  - A contingency matrix given by the \text{contingency\_matrix} function. If value is None, it will be computed, otherwise the given value is used, with \text{labels\_true} and \text{labels\_pred} ignored.

**Returns**

- **mi**: float
  - Mutual information, a non-negative value

**See also:**

- \text{adjusted\_mutual\_info\_score} Adjusted against chance Mutual Information
- \text{normalized\_mutual\_info\_score} Normalized Mutual Information

**Examples using sklearn.metrics.mutual_info_score**

- \text{sklearn.metrics.mutual_info_score}
  - \text{sklearn.metrics.normalized\_mutual\_info\_score} Normalized Mutual Information between two clusterings.

\text{sklearn.metrics.normalized\_mutual\_info\_score}(labels\_true, labels\_pred)

Normalized Mutual Information (NMI) is an normalization of the Mutual Information (MI) score to scale the results between 0 (no mutual information) and 1 (perfect correlation). In this function, mutual information is normalized by \( \sqrt{H(\text{labels\_true}) \ast H(\text{labels\_pred})} \)

This measure is not adjusted for chance. Therefore \text{adjusted\_mustual\_info\_score} might be preferred.

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score value in any way.

This metric is furthermore symmetric: switching \text{label\_true} with \text{label\_pred} will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.
Read more in the *User Guide*.

**Parameters**

labels_true : int array, shape = [n_samples]
   A clustering of the data into disjoint subsets.

labels_pred : array, shape = [n_samples]
   A clustering of the data into disjoint subsets.

**Returns**

nmi : float
   score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

See also:

*adjusted_rand_score* Adjusted Rand Index

*adjusted_mutual_info_score* Adjusted Mutual Information (adjusted against chance)

**Examples**

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```python
>>> from sklearn.metrics.cluster import normalized_mutual_info_score
>>> normalized_mutual_info_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> normalized_mutual_info_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

If classes members are completely split across different clusters, the assignment is totally in-complete, hence the NMI is null:

```python
>>> normalized_mutual_info_score([0, 0, 0, 0], [0, 1, 2, 3])
0.0
```

```
sklearn.metrics.silhouette_score
```

*sklearn.metrics.silhouette_score*(X, labels, metric='euclidean', sample_size=None, random_state=None, **kwds)

Compute the mean Silhouette Coefficient of all samples.

The Silhouette Coefficient is calculated using the mean intra-cluster distance (a) and the mean nearest-cluster distance (b) for each sample. The Silhouette Coefficient for a sample is \( \frac{b - a}{\max(a, b)} \). To clarify, \( b \) is the distance between a sample and the nearest cluster that the sample is not a part of. Note that Silhouette Coefficient is only defined if number of labels is \( 2 \leq n_{labels} \leq n_{samples} - 1 \).

This function returns the mean Silhouette Coefficient over all samples. To obtain the values for each sample, use *silhouette_samples*.

The best value is 1 and the worst value is -1. Values near 0 indicate overlapping clusters. Negative values generally indicate that a sample has been assigned to the wrong cluster, as a different cluster is more similar.

Read more in the *User Guide*.

**Parameters**

X : array [n_samples_a, n_samples_a] if metric == “precomputed”, or, [n_samples_a, n_features] otherwise
   Array of pairwise distances between samples, or a feature array.
**labels**: array, shape = [n_samples]

Predicted labels for each sample.

**metric**: string, or callable

The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by `metrics.pairwise.pairwise_distances`. If X is the distance array itself, use metric="precomputed".

**sample_size**: int or None

The size of the sample to use when computing the Silhouette Coefficient on a random subset of the data. If sample_size is None, no sampling is used.

**random_state**: int, RandomState instance or None, optional (default=None)

The generator used to randomly select a subset of samples. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when sample_size is not None.

**kwds**: optional keyword parameters

Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

Returns **silhouette**: float

Mean Silhouette Coefficient for all samples.

**References**

[R173174], [R174174]

**Examples using sklearn.metrics.silhouette_score**

- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- A demo of K-Means clustering on the handwritten digits data
- Selecting the number of clusters with silhouette analysis on KMeans clustering
- Clustering text documents using k-means

**sklearn.metrics.silhouette_samples**

`sklearn.metrics.silhouette_samples(X, labels, metric='euclidean', **kwds)`

Compute the Silhouette Coefficient for each sample.

The Silhouette Coefficient is a measure of how well samples are clustered with samples that are similar to themselves. Clustering models with a high Silhouette Coefficient are said to be dense, where samples in the same cluster are similar to each other, and well separated, where samples in different clusters are not very similar to each other.
The Silhouette Coefficient is calculated using the mean intra-cluster distance \( (a) \) and the mean nearest-cluster distance \( (b) \) for each sample. The Silhouette Coefficient for a sample is \( \frac{(b - a)}{\max(a, b)} \). Note that Silhouette Coefficient is only defined if number of labels is \( 2 \leq n_{\text{labels}} \leq n_{\text{samples}} - 1 \).

This function returns the Silhouette Coefficient for each sample.

The best value is 1 and the worst value is -1. Values near 0 indicate overlapping clusters.

Read more in the User Guide.

**Parameters**

- **X**: array [n_samples_a, n_samples_a] if metric == “precomputed”, or, [n_samples_a, n_features] otherwise
  
  Array of pairwise distances between samples, or a feature array.

- **labels**: array, shape = [n_samples]
  
  label values for each sample

- **metric**: string, or callable
  
  The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by `sklearn.metrics.pairwise.pairwise_distances`. If X is the distance array itself, use “precomputed” as the metric.

- ****kwds**: optional keyword parameters
  
  Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

**Returns**

- **silhouette**: array, shape = [n_samples]
  
  Silhouette Coefficient for each samples.

**References**

[R169170], [R170170]

**Examples using** `sklearn.metrics.silhouette_samples`

- Selecting the number of clusters with silhouette analysis on KMeans clustering

**sklearn.metrics.v_measure_score**

`sklearn.metrics.v_measure_score(labels_true, labels_pred)`

V-measure cluster labeling given a ground truth.

This score is identical to `normalized_mutual_info_score`.

The V-measure is the harmonic mean between homogeneity and completeness:

\[
\nu = \frac{2 \times (\text{homogeneity} \times \text{completeness})}{(\text{homogeneity} + \text{completeness})}
\]

This metric is independent of the absolute values of the labels: a permutation of the class or cluster label values won’t change the score value in any way.
This metric is furthermore symmetric: switching `label_true` with `label_pred` will return the same score value. This can be useful to measure the agreement of two independent label assignments strategies on the same dataset when the real ground truth is not known.

Read more in the User Guide.

Parameters

- **labels_true** : int array, shape = [n_samples]
  - ground truth class labels to be used as a reference
- **labels_pred** : array, shape = [n_samples]
  - cluster labels to evaluate

Returns

- **v_measure** : float
  - score between 0.0 and 1.0. 1.0 stands for perfectly complete labeling

See also:

- `homogeneity_score`
- `completeness_score`

References

[R177177]

Examples

Perfect labelings are both homogeneous and complete, hence have score 1.0:

```python
>>> from sklearn.metrics.cluster import v_measure_score
>>> v_measure_score([0, 0, 1, 1], [0, 0, 1, 1])
1.0
>>> v_measure_score([0, 0, 1, 1], [1, 1, 0, 0])
1.0
```

Labelings that assign all classes members to the same clusters are complete but not homogeneous, hence penalized:

```python
>>> print("%.6f" % v_measure_score([0, 0, 1, 2], [0, 0, 1, 1]))
... 0.8...
>>> print("%.6f" % v_measure_score([0, 1, 2, 3], [0, 0, 1, 1]))
... 0.66...
```

Labelings that have pure clusters with members coming from the same classes are homogeneous but unnecessary splits harms completeness and thus penalize V-measure as well:

```python
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 0, 1, 2]))
... 0.8...
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 1, 2, 3]))
... 0.66...
```

If classes members are completely split across different clusters, the assignment is totally incomplete, hence the V-Measure is null:
>>> print("%.6f" % v_measure_score([0, 0, 0, 0], [0, 1, 2, 3]))
... 0.0...

Clusters that include samples from totally different classes totally destroy the homogeneity of the labeling, hence:

```python
>>> print("%.6f" % v_measure_score([0, 0, 1, 1], [0, 0, 0, 0]))
... 0.0...
```  

Examples using `sklearn.metrics.v_measure_score`:

- Biclustering documents with the Spectral Co-clustering algorithm
- Demo of affinity propagation clustering algorithm
- Demo of DBSCAN clustering algorithm
- Adjustment for chance in clustering performance evaluation
- A demo of K-Means clustering on the handwritten digits data
- Clustering text documents using k-means

### 30.21.6 Biclustering metrics

See the Biclustering evaluation section of the user guide for further details.

```python
metrics.consensus_score(a, b[, similarity])
```

The similarity of two sets of biclusters.

**sklearn.metrics.consensus_score**

```python
sklearn.metrics.consensus_score(a, b, similarity='jaccard')
```

The similarity of two sets of biclusters.

Similarity between individual biclusters is computed. Then the best matching between sets is found using the Hungarian algorithm. The final score is the sum of similarities divided by the size of the larger set.

Read more in the User Guide.

**Parameters**

- `a` : (rows, columns)
  
  Tuple of row and column indicators for a set of biclusters.

- `b` : (rows, columns)
  
  Another set of biclusters like a.

- `similarity` : string or function, optional, default: “jaccard”
  
  May be the string “jaccard” to use the Jaccard coefficient, or any function that takes four arguments, each of which is a 1d indicator vector: (a_rows, a_columns, b_rows, b_columns).
30.21.7 Pairwise metrics

See the *Pairwise metrics, Affinities and Kernels* section of the user guide for further details.

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<th>Function</th>
<th>Description</th>
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</thead>
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<td>Computes the additive chi-squared kernel between observations in X and Y.</td>
</tr>
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<td><code>metrics.pairwise.chi2_kernel(X, Y, gamma)</code></td>
<td>Computes the exponential chi-squared kernel X and Y.</td>
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<td><code>metrics.pairwise.cosine_similarity(X, Y)</code></td>
<td>Compute cosine similarity between samples in X and Y.</td>
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<td><code>metrics.pairwise.manhattan_distances(X, Y, ...)</code></td>
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<tr>
<td><code>metrics.pairwise.pairwise_distances(X, Y, ...)</code></td>
<td>Compute the distance matrix from a vector array X and optional Y.</td>
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<tr>
<td><code>metrics.pairwise.pairwise_kernels(X, Y, ...)</code></td>
<td>Compute the kernel between arrays X and optional array Y.</td>
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<td><code>metrics.pairwise.polynomial_kernel(X, Y, ...)</code></td>
<td>Compute the polynomial kernel between X and Y.</td>
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<td><code>metrics.pairwise.rbf_kernel(X, Y, gamma)</code></td>
<td>Compute the rbf (gaussian) kernel between X and Y.</td>
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<td><code>metrics.pairwise.sigmoid_kernel(X, Y, ...)</code></td>
<td>Compute the sigmoid kernel between X and Y.</td>
</tr>
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<td><code>metrics.pairwise.paired_distances(X, Y)</code></td>
<td>Computes the paired euclidean distances between X and Y.</td>
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<tr>
<td><code>metrics.pairwise.paired_euclidean_distances(X, Y)</code></td>
<td>Compute the L1 distances between the vectors in X and Y.</td>
</tr>
<tr>
<td><code>metrics.pairwise.paired_manhattan_distances(X, Y)</code></td>
<td>Compute the paired euclidean distances between X and Y.</td>
</tr>
<tr>
<td><code>metrics.pairwise.paired_cosine_distances(X, Y)</code></td>
<td>Computes the paired cosine distances between X and Y.</td>
</tr>
<tr>
<td><code>metrics.pairwise.pairwise_distances_argmin(X, Y, metric)</code></td>
<td>Computes the paired euclidean distances between X and Y.</td>
</tr>
<tr>
<td><code>metrics.pairwise_distances(X, Y, metric, ...)</code></td>
<td>Computes the distance matrix from a vector array X and optional Y.</td>
</tr>
<tr>
<td><code>metrics.pairwise_distances_argmin(X, Y, metric, ...)</code></td>
<td>Compute minimum distances between one point and a set of points.</td>
</tr>
</tbody>
</table>

Continued on next page
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metrics.pairwise_distances_argmin_min(X, Y)

Compute minimum distances between one point and a set of points.

sklearn.metrics.pairwise.additive_chi2_kernel

sklearn.metrics.pairwise.additive_chi2_kernel(X, Y=None)

Computes the additive chi-squared kernel between observations in X and Y.

The chi-squared kernel is computed between each pair of rows in X and Y. X and Y have to be non-negative. This kernel is most commonly applied to histograms.

The chi-squared kernel is given by:

$$k(x, y) = -\sum \left(\frac{(x - y)^2}{x + y}\right)$$

It can be interpreted as a weighted difference per entry.

Parameters

- X : array-like of shape (n_samples_X, n_features)
- Y : array of shape (n_samples_Y, n_features)

Returns

- kernel_matrix : array of shape (n_samples_X, n_samples_Y)

See also:

- chi2_kernel The exponentiated version of the kernel, which is usually preferable.
- sklearn.kernel_approximation.AdditiveChi2Sampler A Fourier approximation to this kernel.

Notes

As the negative of a distance, this kernel is only conditionally positive definite.

References


sklearn.metrics.pairwise.chi2_kernel

sklearn.metrics.pairwise.chi2_kernel(X, Y=None, gamma=1.0)

Computes the exponential chi-squared kernel X and Y.

The chi-squared kernel is computed between each pair of rows in X and Y. X and Y have to be non-negative. This kernel is most commonly applied to histograms.

The chi-squared kernel is given by:

$$k(x, y) = \exp(-\gamma \sum (x - y)^2 / (x + y))$$
It can be interpreted as a weighted difference per entry.

Read more in the User Guide.

**Parameters**

- **X**: array-like of shape (n_samples_X, n_features)
- **Y**: array of shape (n_samples_Y, n_features)
- **gamma**: float, default=1.

Scaling parameter of the chi2 kernel.

**Returns**

- **kernel_matrix**: array of shape (n_samples_X, n_samples_Y)

See also:

- **additive_chi2_kernel**: The additive version of this kernel
- **sklearn.kernel_approximation.AdditiveChi2Sampler**: A Fourier approximation to the additive version of this kernel.

**References**


---

**sklearn.metrics.pairwise.cosine_similarity**

Compute cosine similarity between samples in X and Y.

Cosine similarity, or the cosine kernel, computes similarity as the normalized dot product of X and Y:

\[ K(X, Y) = \frac{\langle X, Y \rangle}{\|X\| \cdot \|Y\|} \]

On L2-normalized data, this function is equivalent to linear_kernel.

Read more in the User Guide.

**Parameters**

- **X**: ndarray or sparse array, shape: (n_samples_X, n_features)
  Input data.

- **Y**: ndarray or sparse array, shape: (n_samples_Y, n_features)
  Input data. If None, the output will be the pairwise similarities between all samples in X.

- **dense_output**: boolean (optional), default True
  Whether to return dense output even when the input is sparse. If False, the output is sparse if both input arrays are sparse.

**Returns**

- **kernel_matrix**: array
  An array with shape (n_samples_X, n_samples_Y).
sklearn.metrics.pairwise.cosine_distances

sklearn.metrics.pairwise.cosine_distances(X, Y=None)

Compute cosine distance between samples in X and Y.
Cosine distance is defined as 1.0 minus the cosine similarity.

Read more in the User Guide.

Parameters:
- X : array_like, sparse matrix
  with shape (n_samples_X, n_features).
- Y : array_like, sparse matrix (optional)
  with shape (n_samples_Y, n_features).

Returns:
- distance matrix : array
  An array with shape (n_samples_X, n_samples_Y).

See also:
- sklearn.metrics.pairwise.cosine_similarity
- scipy.spatial.distance.cosine

sklearn.metrics.pairwise.distance_metrics

sklearn.metrics.pairwise.distance_metrics()

Valid metrics for pairwise_distances.

This function simply returns the valid pairwise distance metrics. It exists to allow for a description of the mapping for each of the valid strings.

The valid distance metrics, and the function they map to, are:

<table>
<thead>
<tr>
<th>metric</th>
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</tr>
<tr>
<td>'l1'</td>
<td>metrics.pairwise.manhattan_distances</td>
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<td>'l2'</td>
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<tr>
<td>'manhattan'</td>
<td>metrics.pairwise.manhattan_distances</td>
</tr>
</tbody>
</table>

Read more in the User Guide.

sklearn.metrics.pairwise.euclidean_distances

sklearn.metrics.pairwise.euclidean_distances(X, Y=None, Y_norm_squared=None, squared=False, X_norm_squared=None)

Considering the rows of X (and Y=X) as vectors, compute the distance matrix between each pair of vectors.

For efficiency reasons, the euclidean distance between a pair of row vector x and y is computed as:

\[ \text{dist}(x, y) = \sqrt{\text{dot}(x, x) - 2 \times \text{dot}(x, y) + \text{dot}(y, y)} \]

This formulation has two advantages over other ways of computing distances. First, it is computationally efficient when dealing with sparse data. Second, if one argument varies but the other remains unchanged, then \( \text{dot}(x, x) \) and/or \( \text{dot}(y, y) \) can be pre-computed.
However, this is not the most precise way of doing this computation, and the distance matrix returned by this function may not be exactly symmetric as required by, e.g., scipy.spatial.distance functions.

Read more in the User Guide.

Parameters

- `X` : {array-like, sparse matrix}, shape (n_samples_1, n_features)
- `Y` : {array-like, sparse matrix}, shape (n_samples_2, n_features)
- `Y_norm_squared` : array-like, shape (n_samples_2, ), optional
  Pre-computed dot-products of vectors in Y (e.g., $(Y**2).sum(axis=1)$)
- `squared` : boolean, optional
  Return squared Euclidean distances.
- `X_norm_squared` : array-like, shape = [n_samples_1], optional
  Pre-computed dot-products of vectors in X (e.g., $(X**2).sum(axis=1)$)

Returns

- `distances` : {array, sparse matrix}, shape (n_samples_1, n_samples_2)

See also:

- paired_distances distances between pairs of elements of X and Y.

Examples

```python
>>> from sklearn.metrics.pairwise import euclidean_distances
>>> X = [[0, 1], [1, 1]]
>>> # distance between rows of X
>>> euclidean_distances(X, X)
array([[ 0., 1.],
       [ 1., 0.]])
>>> # get distance to origin
>>> euclidean_distances(X, [[0, 0]])
array([[ 1.41421356]])
```

sklearn.metrics.pairwise.kernel_metrics

Valid metrics for pairwise_kernels

This function simply returns the valid pairwise distance metrics. It exists, however, to allow for a verbose description of the mapping for each of the valid strings.

The valid distance metrics, and the function they map to, are:
<table>
<thead>
<tr>
<th>metric</th>
<th>Function</th>
</tr>
</thead>
<tbody>
<tr>
<td>'additive_chi2'</td>
<td>sklearn.pairwise.additive_chi2_kernel</td>
</tr>
<tr>
<td>'chi2'</td>
<td>sklearn.pairwise.chi2_kernel</td>
</tr>
<tr>
<td>'linear'</td>
<td>sklearn.pairwise.linear_kernel</td>
</tr>
<tr>
<td>'poly'</td>
<td>sklearn.pairwise.polynomial_kernel</td>
</tr>
<tr>
<td>'polynomial'</td>
<td>sklearn.pairwise.polynomial_kernel</td>
</tr>
<tr>
<td>'rbf'</td>
<td>sklearn.pairwise.rbf_kernel</td>
</tr>
<tr>
<td>'laplacian'</td>
<td>sklearn.pairwise.laplacian_kernel</td>
</tr>
<tr>
<td>'sigmoid'</td>
<td>sklearn.pairwise.sigmoid_kernel</td>
</tr>
<tr>
<td>'cosine'</td>
<td>sklearn.pairwise.cosine_similarity</td>
</tr>
</tbody>
</table>

Read more in the *User Guide*.

**sklearn.metrics.pairwise.laplacian_kernel**

sklearn.metrics.pairwise.laplacian_kernel(X, Y=None, gamma=None)

Compute the laplacian kernel between X and Y.

The laplacian kernel is defined as:

\[
K(x, y) = \exp(-\gamma ||x-y||_1)
\]

for each pair of rows x in X and y in Y. Read more in the *User Guide*.

New in version 0.17.

**Parameters**

- **X**: array of shape (n_samples_X, n_features)
- **Y**: array of shape (n_samples_Y, n_features)
- **gamma**: float, default None
  - If None, defaults to 1.0 / n_features

**Returns**

- **kernel_matrix**: array of shape (n_samples_X, n_samples_Y)

**sklearn.metrics.pairwise.linear_kernel**

sklearn.metrics.pairwise.linear_kernel(X, Y=None)

Compute the linear kernel between X and Y.

Read more in the *User Guide*.

**Parameters**

- **X**: array of shape (n_samples_1, n_features)
- **Y**: array of shape (n_samples_2, n_features)

**Returns**

- **Gram matrix**: array of shape (n_samples_1, n_samples_2)

**sklearn.metrics.pairwise.manhattan_distances**

sklearn.metrics.pairwise.manhattan_distances(X, Y=None, sum_over_features=True, size_threshold=None)

Compute the L1 distances between the vectors in X and Y.

With sum_over_features equal to False it returns the componentwise distances.

Read more in the *User Guide*.
Parameters X : array_like
    An array with shape (n_samples_X, n_features).

Y : array_like, optional
    An array with shape (n_samples_Y, n_features).

sum_over_features : bool, default=True
    If True the function returns the pairwise distance matrix else it returns the component-wise L1 pairwise-distances. Not supported for sparse matrix inputs.

size_threshold : int, default=5e8
    Unused parameter.

Returns D : array
    If sum_over_features is False shape is (n_samples_X * n_samples_Y, n_features) and D contains the componentwise L1 pairwise-distances (ie. absolute difference), else shape is (n_samples_X, n_samples_Y) and D contains the pairwise L1 distances.

Examples

```python
>>> from sklearn.metrics.pairwise import manhattan_distances
>>> manhattan_distances([[3]], [[3]])
array([[0.]])
>>> manhattan_distances([[3]], [[2]])
array([[1.]])
>>> manhattan_distances([[2]], [[3]])
array([[1.]])
>>> manhattan_distances([[1, 2], [3, 4]], [[1, 2], [0, 3]])
array([[0., 2.],
       [1., 1.]])
>>> import numpy as np
>>> X = np.ones((1, 2))
>>> y = 2 * np.ones((2, 2))
>>> manhattan_distances(X, y, sum_over_features=False)
array([[1., 1.],
       [1., 1.]])
```

sklearn.metrics.pairwise.pairwise_distances

sklearn.metrics.pairwise.pairwise_distances (X, Y=None, metric='euclidean', n_jobs=1, **kwds)

Compute the distance matrix from a vector array X and optional Y.

This method takes either a vector array or a distance matrix, and returns a distance matrix. If the input is a vector array, the distances are computed. If the input is a distances matrix, it is returned instead.

This method provides a safe way to take a distance matrix as input, while preserving compatibility with many other algorithms that take a vector array.

If Y is given (default is None), then the returned matrix is the pairwise distance between the arrays from both X and Y.

Valid values for metric are:
• From scikit-learn: ['cityblock', 'cosine', 'euclidean', 'l1', 'l2', 'manhattan']. These metrics support sparse matrix inputs.

• From scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule'] See the documentation for scipy.spatial.distance for details on these metrics. These metrics do not support sparse matrix inputs.

Note that in the case of ‘cityblock’, ‘cosine’ and ‘euclidean’ (which are valid scipy.spatial.distance metrics), the scikit-learn implementation will be used, which is faster and has support for sparse matrices (except for ‘cityblock’). For a verbose description of the metrics from scikit-learn, see the __doc__ of the sklearn.pairwise.distance_metrics function.

Read more in the User Guide.

**Parameters**

X : array [n_samples_a, n_samples_a] if metric == “precomputed”, or, [n_samples_a, n_features] otherwise

Array of pairwise distances between samples, or a feature array.

Y : array [n_samples_b, n_features], optional

An optional second feature array. Only allowed if metric != “precomputed”.

metric : string, or callable

The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pairwise.PAIRWISE_DISTANCE_FUNCTIONS. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

n_jobs : int

The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n_jobs even slices and computing them in parallel.

If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**kwds : optional keyword parameters

Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

**Returns**

D : array [n_samples_a, n_samples_a] or [n_samples_a, n_samples_b]

A distance matrix D such that D[i, j] is the distance between the ith and jth vectors of the given matrix X, if Y is None. If Y is not None, then D[i, j] is the distance between the ith array from X and the jth array from Y.

sklearn.metrics.pairwise.pairwise_kernels

sklearn.metrics.pairwise.pairwise_kernels(X, Y=None, metric='linear', filter_params=False, n_jobs=1, **kwds)

Compute the kernel between arrays X and optional array Y.
This method takes either a vector array or a kernel matrix, and returns a kernel matrix. If the input is a vector array, the kernels are computed. If the input is a kernel matrix, it is returned instead.

This method provides a safe way to take a kernel matrix as input, while preserving compatibility with many other algorithms that take a vector array.

If Y is given (default is None), then the returned matrix is the pairwise kernel between the arrays from both X and Y.

Valid values for metric are:: ['rbf', 'sigmoid', 'polynomial', 'poly', 'linear', 'cosine']

Read more in the User Guide.

Parameters

- **X** : array [n_samples_a, n_samples_a] if metric == “precomputed”, or, [n_samples_a, n_features] otherwise
  
  Array of pairwise kernels between samples, or a feature array.

- **Y** : array [n_samples_b, n_features]
  
  A second feature array only if X has shape [n_samples_a, n_features].

- **metric** : string, or callable
  
  The metric to use when calculating kernel between instances in a feature array. If metric is a string, it must be one of the metrics in pairwise.PAIRWISE_KERNEL_FUNCTIONS. If metric is “precomputed”, X is assumed to be a kernel matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

- **filter_params** : boolean
  
  Whether to filter invalid parameters or not.

- **n_jobs** : int
  
  The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n_jobs even slices and computing them in parallel.

  If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

- ****kwds : optional keyword parameters
  
  Any further parameters are passed directly to the kernel function.

Returns

- **K** : array [n_samples_a, n_samples_a] or [n_samples_a, n_samples_b]
  
  A kernel matrix K such that K_{i, j} is the kernel between the ith and jth vectors of the given matrix X, if Y is None. If Y is not None, then K_{i, j} is the kernel between the ith array from X and the jth array from Y.

Notes

If metric is ‘precomputed’, Y is ignored and X is returned.
**sklearn.metrics.pairwise.polynomial_kernel**

*sklearn.metrics.pairwise.polynomial_kernel*(X, Y=None, degree=3, gamma=None, coef0=1)

Compute the polynomial kernel between X and Y:

\[ K(X, Y) = (\gamma \langle X, Y \rangle + \text{coef0})^\text{degree} \]

Read more in the *User Guide*.

**Parameters**
- **X**: ndarray of shape (n_samples_1, n_features)
- **Y**: ndarray of shape (n_samples_2, n_features)
- **degree**: int, default 3
- **gamma**: float, default None
  - If None, defaults to 1.0 / n_features
- **coef0**: int, default 1

**Returns**
- **Gram matrix**: array of shape (n_samples_1, n_samples_2)

**sklearn.metrics.pairwise.rbf_kernel**

*sklearn.metrics.pairwise.rbf_kernel*(X, Y=None, gamma=None)

Compute the rbf (gaussian) kernel between X and Y:

\[ K(x, y) = \exp\left(-\gamma \|x-y\|^2\right) \]

for each pair of rows x in X and y in Y.

Read more in the *User Guide*.

**Parameters**
- **X**: array of shape (n_samples_X, n_features)
- **Y**: array of shape (n_samples_Y, n_features)
- **gamma**: float, default None
  - If None, defaults to 1.0 / n_features

**Returns**
- **kernel_matrix**: array of shape (n_samples_X, n_samples_Y)

**sklearn.metrics.pairwise.sigmoid_kernel**

*sklearn.metrics.pairwise.sigmoid_kernel*(X, Y=None, gamma=None, coef0=1)

Compute the sigmoid kernel between X and Y:

\[ K(X, Y) = \tanh(\gamma \langle X, Y \rangle + \text{coef0}) \]

Read more in the *User Guide*.

**Parameters**
- **X**: ndarray of shape (n_samples_1, n_features)
- **Y**: ndarray of shape (n_samples_2, n_features)
- **gamma**: float, default None
  - If None, defaults to 1.0 / n_features
- **coef0**: int, default 1
Returns Gram matrix: array of shape (n_samples_1, n_samples_2)

sklearn.metrics.pairwise.paired_euclidean_distances

sklearn.metrics.pairwise.paired_euclidean_distances(X, Y)
Computes the paired euclidean distances between X and Y.
Read more in the User Guide.
Parameters X : array-like, shape (n_samples, n_features)
    Y : array-like, shape (n_samples, n_features)
Returns distances : ndarray (n_samples, )

sklearn.metrics.pairwise.paired_manhattan_distances

sklearn.metrics.pairwise.paired_manhattan_distances(X, Y)
Compute the L1 distances between the vectors in X and Y.
Read more in the User Guide.
Parameters X : array-like, shape (n_samples, n_features)
    Y : array-like, shape (n_samples, n_features)
Returns distances : ndarray (n_samples, )

sklearn.metrics.pairwise.paired_cosine_distances

sklearn.metrics.pairwise.paired_cosine_distances(X, Y)
Computes the paired cosine distances between X and Y.
Read more in the User Guide.
Parameters X : array-like, shape (n_samples, n_features)
    Y : array-like, shape (n_samples, n_features)
Returns distances : ndarray, shape (n_samples, )

Notes

The cosine distance is equivalent to the half the squared euclidean distance if each sample is normalized to unit norm

sklearn.metrics.pairwise.paired_distances

sklearn.metrics.pairwise.paired_distances(X, Y, metric='euclidean', **kwds)
Computes the paired distances between X and Y.
Computes the distances between (X[0], Y[0]), (X[1], Y[1]), etc...
Read more in the User Guide.
Parameters X : ndarray (n_samples, n_features)
    Array 1 for distance computation.
Y : ndarray (n_samples, n_features)
    Array 2 for distance computation.

metric : string or callable
    The metric to use when calculating distance between instances in a feature array. If
    metric is a string, it must be one of the options specified in PAIRED_DISTANCES,
    including “euclidean”, “manhattan”, or “cosine”. Alternatively, if metric is a callable
    function, it is called on each pair of instances (rows) and the resulting value recorded.
    The callable should take two arrays from X as input and return a value indicating the
    distance between them.

Returns distances : ndarray (n_samples, )
    See also:
    pairwise_distances pairwise distances.

Examples

```python
>>> from sklearn.metrics.pairwise import paired_distances
>>> X = [[0, 1], [1, 1]]
>>> Y = [[0, 1], [2, 1]]
>>> paired_distances(X, Y)
array([[0., 1.])
```

sklearn.metrics.pairwise_distances

sklearn.metrics.pairwise_distances(X, Y=None, metric='euclidean', n_jobs=1, **kwds)
    Compute the distance matrix from a vector array X and optional Y.

    This method takes either a vector array or a distance matrix, and returns a distance matrix. If the input is a vector
    array, the distances are computed. If the input is a distances matrix, it is returned instead.

    This method provides a safe way to take a distance matrix as input, while preserving compatibility with many
    other algorithms that take a vector array.

    If Y is given (default is None), then the returned matrix is the pairwise distance between the arrays from both X
    and Y.

    Valid values for metric are:

    - From scikit-learn: ['cityblock', 'cosine', 'euclidean', 'l1', 'l2', 'manhattan']. These metrics support sparse
      matrix inputs.

    - From scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jacc-
      card', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmich-
      ener', 'sokalsneath', 'sqeuclidean', 'yule'] See the documentation for scipy.spatial.distance for details on
      these metrics. These metrics do not support sparse matrix inputs.

    Note that in the case of ‘cityblock’, ‘cosine’ and ‘euclidean’ (which are valid scipy.spatial.distance met-
    rics), the scikit-learn implementation will be used, which is faster and has support for sparse matrices (ex-
    cept for ‘cityblock’). For a verbose description of the metrics from scikit-learn, see the __doc__ of the
    sklearn.pairwise.distance_metrics function.

    Read more in the User Guide.
Parameters

- **X**: array [n_samples_a, n_samples_a] if metric == “precomputed”, or, [n_samples_a, n_features] otherwise
  
  Array of pairwise distances between samples, or a feature array.

- **Y**: array [n_samples_b, n_features], optional
  
  An optional second feature array. Only allowed if metric != “precomputed”.

- **metric**: string, or callable
  
  The metric to use when calculating distance between instances in a feature array. If metric is a string, it must be one of the options allowed by scipy.spatial.distance.pdist for its metric parameter, or a metric listed in pairwise.PAIRWISE_DISTANCE_FUNCTIONS. If metric is “precomputed”, X is assumed to be a distance matrix. Alternatively, if metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays from X as input and return a value indicating the distance between them.

- **n_jobs**: int
  
  The number of jobs to use for the computation. This works by breaking down the pairwise matrix into n_jobs even slices and computing them in parallel.

  If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

- **kwds**: optional keyword parameters
  
  Any further parameters are passed directly to the distance function. If using a scipy.spatial.distance metric, the parameters are still metric dependent. See the scipy docs for usage examples.

Returns

- **D**: array [n_samples_a, n_samples_a] or [n_samples_a, n_samples_b]
  
  A distance matrix D such that D_{i, j} is the distance between the ith and jth vectors of the given matrix X, if Y is None. If Y is not None, then D_{i, j} is the distance between the ith array from X and the jth array from Y.

Examples using sklearn.metrics.pairwise_distances

- Agglomerative clustering with different metrics

sklearn.metrics.pairwise_distances_argmin

sklearn.metrics.pairwise_distances_argmin(X, Y, axis=1, metric=’euclidean’, batch_size=500, metric_kws=’None’)

Compute minimum distances between one point and a set of points.

This function computes for each row in X, the index of the row of Y which is closest (according to the specified distance).

This is mostly equivalent to calling:

pairwise_distances(X, Y=Y, metric=metric).argmin(axis=axis)

but uses much less memory, and is faster for large arrays.

This function works with dense 2D arrays only.
Parameters

X : array-like
Arrays containing points. Respective shapes (n_samples1, n_features) and (n_samples2, n_features)

Y : array-like
Arrays containing points. Respective shapes (n_samples1, n_features) and (n_samples2, n_features)

axis : int, optional, default 1
Axis along which the argmin and distances are to be computed.

metric : string or callable
metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy’s metrics, but is less efficient than passing the metric name as a string.

Distance matrices are not supported.

Valid values for metric are:

• from scikit-learn: ['cityblock', 'cosine', 'euclidean', 'l1', 'l2', 'manhattan']
• from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

batch_size : integer
To reduce memory consumption over the naive solution, data are processed in batches, comprising batch_size rows of X and batch_size rows of Y. The default value is quite conservative, but can be changed for fine-tuning. The larger the number, the larger the memory usage.

metric_kwargs : dict
keyword arguments to pass to specified metric function.

Returns

argmin : numpy.ndarray
Y[argmin[i], :] is the row in Y that is closest to X[i, :].

See also:
sklearn.metrics.pairwise_distances, sklearn.metrics.pairwise_distances_argmin_min

Examples using sklearn.metrics.pairwise_distances_argmin

• Color Quantization using K-Means
• Comparison of the K-Means and MiniBatchKMeans clustering algorithms
This function computes for each row in X, the index of the row of Y which is closest (according to the specified distance). The minimal distances are also returned.

This is mostly equivalent to calling:

```python
(pairwise_distances(X, Y=Y, metric=metric).argmin(axis=axis),
 pairwise_distances(X, Y=Y, metric=metric).min(axis=axis))
```

but uses much less memory, and is faster for large arrays.

**Parameters**

- **X**: {array-like, sparse matrix}, shape (n_samples1, n_features)
  
  Array containing points.

- **Y**: {array-like, sparse matrix}, shape (n_samples2, n_features)
  
  Arrays containing points.

- **axis**: int, optional, default 1
  
  Axis along which the argmin and distances are to be computed.

- **metric**: string or callable, default ‘euclidean’
  
  Metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

  If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy’s metrics, but is less efficient than passing the metric name as a string.

  Distance matrices are not supported.

  Valid values for metric are:


  See the documentation for scipy.spatial.distance for details on these metrics.

- **batch_size**: integer
  
  To reduce memory consumption over the naive solution, data are processed in batches, comprising batch_size rows of X and batch_size rows of Y. The default value is quite conservative, but can be changed for fine-tuning. The larger the number, the larger the memory usage.

- **metric_kwargs**: dict, optional
  
  Keyword arguments to pass to specified metric function.

**Returns**

- **argmin**: numpy.ndarray
  
  Y[argmin[i], :] is the row in Y that is closest to X[i, :].

- **distances**: numpy.ndarray
distances[i] is the distance between the i-th row in X and the argmin[i]-th row in Y.

See also:

sklearn.metrics.pairwise_distances, sklearn.metrics.pairwise_distances_argmin

30.22 sklearn.mixture: Gaussian Mixture Models

The sklearn.mixture module implements mixture modeling algorithms.

User guide: See the Gaussian mixture models section for further details.

| sklearn.mixture.BayesianGaussianMixture([...]) | Variational Bayesian estimation of a Gaussian mixture. |
| sklearn.mixture.GaussianMixture([n_components, ...]) | Gaussian Mixture. |

30.22.1 sklearn.mixture.BayesianGaussianMixture

class sklearn.mixture.BayesianGaussianMixture (n_components=1, covariance_type='full', tol=0.001, reg_covar=1e-06, max_iter=100, n_init=1, init_params='kmeans', weight_concentration_prior_type='dirichlet_process', weight_concentration_prior=None, mean_precision_prior=None, mean_prior=None, degrees_of_freedom_prior=None, covariance_prior=None, warm_start=False, verbose=0, verbose_interval=10)

Variational Bayesian estimation of a Gaussian mixture.

This class allows to infer an approximate posterior distribution over the parameters of a Gaussian mixture distribution. The effective number of components can be inferred from the data.

This class implements two types of prior for the weights distribution: a finite mixture model with Dirichlet distribution and an infinite mixture model with the Dirichlet Process. In practice Dirichlet Process inference algorithm is approximated and uses a truncated distribution with a fixed maximum number of components (called the Stick-breaking representation). The number of components actually used almost always depends on the data.

New in version 0.18.

Read more in the User Guide.

Parameters n_components : int, defaults to 1.

The number of mixture components. Depending on the data and the value of the weight_concentration_prior the model can decide to not use all the components by setting some component weights to values very close to zero. The number of effective components is therefore smaller than n_components.

covariance_type : {‘full’, ‘tied’, ‘diag’, ‘spherical’}, defaults to ‘full’

String describing the type of covariance parameters to use. Must be one of:

- 'full' (each component has its own general covariance matrix),
- 'tied' (all components share the same general covariance matrix),
'diag' (each component has its own diagonal covariance matrix),
'spherical' (each component has its own single variance).

tol : float, defaults to 1e-3.

The convergence threshold. EM iterations will stop when the lower bound average gain on the likelihood (of the training data with respect to the model) is below this threshold.

reg_covar : float, defaults to 1e-6.

Non-negative regularization added to the diagonal of covariance. Allows to assure that the covariance matrices are all positive.

max_iter : int, defaults to 100.

The number of EM iterations to perform.

n_init : int, defaults to 1.

The number of initializations to perform. The result with the highest lower bound value on the likelihood is kept.

init_params : {'kmeans', 'random'}, defaults to 'kmeans'.

The method used to initialize the weights, the means and the covariances. Must be one of:

- 'kmeans' : responsibilities are initialized using kmeans.
- 'random' : responsibilities are initialized randomly.

weight_concentration_prior_type : str, defaults to ‘dirichlet_process’.

String describing the type of the weight concentration prior. Must be one of:

- 'dirichlet_process' (using the Stick-breaking representation),
- 'dirichlet_distribution' (can favor more uniform weights).

weight_concentration_prior : float | None, optional.

The dirichlet concentration of each component on the weight distribution (Dirichlet). This is commonly called gamma in the literature. The higher concentration puts more mass in the center and will lead to more components being active, while a lower concentration parameter will lead to more mass at the edge of the mixture weights simplex. The value of the parameter must be greater than 0. If it is None, it’s set to \(1 / n_{\text{components}}\).

mean_precision_prior : float | None, optional.

The precision prior on the mean distribution (Gaussian). Controls the extend to where means can be placed. Smaller values concentrate the means of each clusters around mean_prior. The value of the parameter must be greater than 0. If it is None, it’s set to 1.

mean_prior : array-like, shape (n_features,), optional

The prior on the mean distribution (Gaussian). If it is None, it’s set to the mean of X.

degrees_of_freedom_prior : float | None, optional.

The prior of the number of degrees of freedom on the covariance distributions (Wishart). If it is None, it’s set to n_features.

covariance_prior : float or array-like, optional
The prior on the covariance distribution (Wishart). If it is None, the empirical covariance prior is initialized using the covariance of X. The shape depends on `covariance_type`:

<table>
<thead>
<tr>
<th>Shape</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>(n_features, n_features)</code></td>
<td>if 'full',</td>
</tr>
<tr>
<td><code>(n_features, n_features)</code></td>
<td>if 'tied',</td>
</tr>
<tr>
<td><code>(n_features)</code></td>
<td>if 'diag',</td>
</tr>
<tr>
<td>float</td>
<td>if 'spherical'</td>
</tr>
</tbody>
</table>

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**warm_start**: bool, default to False.

If 'warm_start’ is True, the solution of the last fitting is used as initialization for the next call of fit(). This can speed up convergence when fit is called several time on similar problems.

**verbose**: int, default to 0.

Enable verbose output. If 1 then it prints the current initialization and each iteration step. If greater than 1 then it prints also the log probability and the time needed for each step.

**verbose_interval**: int, default to 10.

Number of iteration done before the next print.
Attributes

- **weights**
  - (array-like, shape (n_components,)) The weights of each mixture component.

- **means_**
  - (array-like, shape (n_components, n_features)) The mean of each mixture component.

- **covariances_**
  - (array-like) The covariance of each mixture component. The shape depends on `covariance_type`:
    - (n_components,) if ‘spherical’,
    - (n_components, n_features) if ‘tied’,
    - (n_components, n_features) if ‘diag’,
    - (n_components, n_features, n_features) if ‘full’

- **precisions_**
  - (array-like) The precision matrices for each component in the mixture. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on `covariance_type`:
    - (n_components,) if ‘spherical’,
    - (n_components, n_features) if ‘tied’,
    - (n_components, n_features) if ‘diag’,
    - (n_components, n_features, n_features) if ‘full’

- **precisions_chol**
  - (array-like) The cholesky decomposition of the precision matrices of each mixture component. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on `covariance_type`:
    - (n_components,) if ‘spherical’,
    - (n_components, n_features) if ‘tied’,
    - (n_components, n_features) if ‘diag’,
    - (n_components, n_features, n_features) if ‘full’

- **converged_**
  - (bool) True when convergence was reached in fit(), False otherwise.

- **n_iter_**
  - (int) Number of step used by the best fit of inference to reach the convergence.

- **lower_bound_**
  - (float) Lower bound value on the likelihood (of the training data with respect to the model) of the best fit of inference.

- **weight_concentration_prior_**
  - (tuple or float) The dirichlet concentration of each component on the weight distribution (Dirichlet). The type depends on `weight_concentration_prior_type`:
    - (float, float) if ‘dirichlet_process’ (Beta parameters),
    - float if ‘dirichlet_distribution’ (Dirichlet parameters).
    The higher concentration puts more mass in the center and will lead to more components being active, while a lower concentration parameter will lead to more mass at the edge of the simplex.

- **weight_concentration_**
  - (array-like, shape (n_components,)) The dirichlet concentration of each component on the weight distribution (Dirichlet).

- **mean_precision_prior**
  - (float) The precision prior on the mean distribution (Gaussian). Controls the extend to where means can be placed. Smaller values concentrate the means of each clusters around `mean_prior`.

- **mean_precision_**
  - (array-like, shape (n_components,)) The precision of each components on the mean distribution (Gaussian).

- **means_prior_**
  - (array-like, shape (n_features,)) The prior on the mean distribution (Gaussian).

- **degrees_of_freedom_prior_**
  - (float) The prior of the number of degrees of freedom on the covariance distributions (Wishart).

- **degrees_of_freedom_**
  - (array-like, shape (n_components,)) The number of degrees of freedom of each components in the model.

- **covariance_prior_**
  - (float or array-like) The prior on the covariance distribution (Wishart). The shape depends on `covariance_type`:
    - (n_features, n_features) if ‘full’,
    - (n_features, n_features) if ‘tied’,
    - (n_components, n_features) if ‘diag’,
    - (n_components, n_features, n_features) if ‘full’

See also:

- **GaussianMixture** Finite Gaussian mixture fit with EM.
Methods

<table>
<thead>
<tr>
<th></th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Estimate model parameters with the EM algorithm.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict the labels for the data samples in X using trained model.</td>
</tr>
<tr>
<td>predict_proba(X)</td>
<td>Predict posterior probability of each component given the data.</td>
</tr>
<tr>
<td>sample([n_samples])</td>
<td>Generate random samples from the fitted Gaussian distribution.</td>
</tr>
<tr>
<td>score(X[, y])</td>
<td>Compute the per-sample average log-likelihood of the given data X.</td>
</tr>
<tr>
<td>score_samples(X)</td>
<td>Compute the weighted log probabilities for each sample.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(n_components=1, covariance_type='full', tol=0.001, reg_covar=1e-06, max_iter=100, n_init=1, init_params='kmeans', weight_concentration_prior=None, weight_concentration_prior_type='dirichlet_process', mean_precision_prior=None, mean_prior=None, degrees_of_freedom_prior=None, covariance_prior=None, random_state=None, warm_start=False, verbose=0, verbose_interval=10)

fit (X, y=None)
Estimate model parameters with the EM algorithm.

The method fit the model n_init times and set the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step for max_iter times until the change of likelihood or lower bound is less than tol, otherwise, a ConvergenceWarning is raised.

Parameters X: array-like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns self

get_params (deep=True)
Get parameters for this estimator.

Parameters deep: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any
Parameter names mapped to their values.

predict (X)
Predict the labels for the data samples in X using trained model.

Parameters X: array-like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.
Returns labels : array, shape (n_samples,)
Component labels.
predict_proba (X)
Predict posterior probability of each component given the data.

Parameters X : array-like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns resp : array, shape (n_samples, n_components)
Returns the probability each Gaussian (state) in the model given each sample.
sample (n_samples=1)
Generate random samples from the fitted Gaussian distribution.

Parameters n_samples : int, optional
Number of samples to generate. Defaults to 1.

Returns X : array, shape (n_samples, n_features)
Randomly generated sample
y : array, shape (nsamples,)
Component labels
score (X, y=None)
Compute the per-sample average log-likelihood of the given data X.

Parameters X : array-like, shape (n_samples, n_dimensions)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns log_likelihood : float
Log likelihood of the Gaussian mixture given X.
score_samples (X)
Compute the weighted log probabilities for each sample.

Parameters X : array-like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns log_prob : array, shape (n_samples,)
Log probabilities of each data point in X.
set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.mixture.BayesianGaussianMixture

- Gaussian Mixture Model Ellipsoids
- Gaussian Mixture Model Sine Curve
Concentration Prior Type Analysis of Variation Bayesian Gaussian Mixture

30.22.2 sklearn.mixture.GaussianMixture

class sklearn.mixture.GaussianMixture(n_components=1, covariance_type='full', tol=0.001, reg_covar=1e-06, max_iter=100, n_init=1, init_params='kmeans', weights_init=None, means_init=None, precisions_init=None, random_state=None, warm_start=False, verbose=0, verbose_interval=10)

Gaussian Mixture.

Representation of a Gaussian mixture model probability distribution. This class allows to estimate the parameters of a Gaussian mixture distribution.

Read more in the User Guide.

New in version 0.18.

Parameters n_components : int, defaults to 1.

   The number of mixture components.

covariance_type : {'full', 'tied', 'diag', 'spherical'},

   defaults to ‘full’.

   String describing the type of covariance parameters to use. Must be one of:

   • 'full' (each component has its own general covariance matrix),
   • 'tied' (all components share the same general covariance matrix),
   • 'diag' (each component has its own diagonal covariance matrix),
   • 'spherical' (each component has its own single variance).

tol : float, defaults to 1e-3.

   The convergence threshold. EM iterations will stop when the lower bound average gain is below this threshold.

reg_covar : float, defaults to 1e-6.

   Non-negative regularization added to the diagonal of covariance. Allows to assure that the covariance matrices are all positive.

max_iter : int, defaults to 100.

   The number of EM iterations to perform.

n_init : int, defaults to 1.

   The number of initializations to perform. The best results are kept.

init_params : {'kmeans', 'random'}, defaults to 'kmeans'.

   The method used to initialize the weights, the means and the precisions. Must be one of:

   • 'kmeans' : responsibilities are initialized using kmeans.
   • 'random' : responsibilities are initialized randomly.

weights_init : array-like, shape (n_components,), optional
The user-provided initial weights, defaults to None. If it None, weights are initialized using the `init_params` method.

**means_init**: array-like, shape (n_components, n_features), optional

The user-provided initial means, defaults to None, If it None, means are initialized using the `init_params` method.

**precisions_init**: array-like, optional.

The user-provided initial precisions (inverse of the covariance matrices), defaults to None. If it None, precisions are initialized using the ‘init_params’ method. The shape depends on ‘covariance_type’:

<table>
<thead>
<tr>
<th>Shape</th>
<th>Covariance Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>(n_components,)</td>
<td>if 'spherical',</td>
</tr>
<tr>
<td>(n_features, n_features)</td>
<td>if 'tied',</td>
</tr>
<tr>
<td>(n_components, n_features)</td>
<td>if 'diag',</td>
</tr>
<tr>
<td>(n_components, n_features, n_features)</td>
<td>if 'full'</td>
</tr>
</tbody>
</table>

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**warm_start**: bool, default to False.

If ‘warm_start’ is True, the solution of the last fitting is used as initialization for the next call of `fit()`. This can speed up convergence when fit is called several time on similar problems.

**verbose**: int, default to 0.

Enable verbose output. If 1 then it prints the current initialization and each iteration step. If greater than 1 then it prints also the log probability and the time needed for each step.

**verbose_interval**: int, default to 10.

Number of iteration done before the next print.
Attributes

- `weights_` (array-like, shape (n_components,)) The weights of each mixture component.
- `means_` (array-like, shape (n_components, n_features)) The mean of each mixture component.
- `covariances_` (array-like) The covariance of each mixture component. The shape depends on `covariance_type`: (n_components,) if ‘spherical’, (n_features, n_features) if ‘tied’, (n_components, n_features) if ‘diag’, (n_components, n_features, n_features) if ‘full’.
- `precisions_` (array-like) The precision matrices for each component in the mixture. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on `covariance_type`: (n_components,) if ‘spherical’, (n_features, n_features) if ‘tied’, (n_components, n_features) if ‘diag’, (n_components, n_features, n_features) if ‘full’.
- `precisions_chol_` (array-like) The cholesky decomposition of the precision matrices of each mixture component. A precision matrix is the inverse of a covariance matrix. A covariance matrix is symmetric positive definite so the mixture of Gaussian can be equivalently parameterized by the precision matrices. Storing the precision matrices instead of the covariance matrices makes it more efficient to compute the log-likelihood of new samples at test time. The shape depends on `covariance_type`: (n_components,) if ‘spherical’, (n_features, n_features) if ‘tied’, (n_components, n_features) if ‘diag’, (n_components, n_features, n_features) if ‘full’.
- `converged_` (bool) True when convergence was reached in fit(), False otherwise.
- `n_iter_` (int) Number of step used by the best fit of EM to reach the convergence.
- `lower_bound_` (float) Log-likelihood of the best fit of EM.

See also:

- `BayesianGaussianMixture` Gaussian mixture model fit with a variational inference.

Methods

- `aiic(X)` Akaike information criterion for the current model on the input X.
- `bic(X)` Bayesian information criterion for the current model on the input X.
- `fit(X[, y])` Estimate model parameters with the EM algorithm.
- `get_params([deep])` Get parameters for this estimator.
- `predict(X)` Predict the labels for the data samples in X using trained model.
- `predict_proba(X)` Predict posterior probability of each component given the data.
- `sample([n_samples])` Generate random samples from the fitted Gaussian distribution.
- `score(X[, y])` Compute the per-sample average log-likelihood of the given data X.
- `score_samples(X)` Compute the weighted log probabilities for each sample.
- `set_params(**params)` Set the parameters of this estimator.
__init__

Parameters:
- **n_components**: integer, default 1
- **covariance_type**: string, default 'full'
- **tol**: float, default 0.001
- **reg_covar**: float, default 1e-06
- **max_iter**: integer, default 100
- **n_init**: integer, default 1
- **init_params**: string, default 'kmeans'
- **weights_init**: array-like, shape (n_components)
- **means_init**: array-like, shape (n_components, n_features)
- **precisions_init**: array-like, shape (n_components, n_features, n_features)
- **random_state**: integer, RandomState instance, or None (default: None)
- **warm_start**: boolean, default False
- **verbose**: integer, default 0
- **verbose_interval**: integer, default 10

aic(X)

Akaike information criterion for the current model on the input X.

Parameters:
- **X**: array of shape (n_samples, n_dimensions)

Returns:
- **aic**: float
  - The lower the better.

bic(X)

Bayesian information criterion for the current model on the input X.

Parameters:
- **X**: array of shape (n_samples, n_dimensions)

Returns:
- **bic**: float
  - The lower the better.

fit(X, y=None)

Estimate model parameters with the EM algorithm.

The method fit the model n_init times and set the parameters with which the model has the largest likelihood or lower bound. Within each trial, the method iterates between E-step and M-step for max_iter times until the change of likelihood or lower bound is less than tol, otherwise, a ConvergenceWarning is raised.

Parameters:
- **X**: array-like, shape (n_samples, n_features)
  - List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns:
- **self**: None

get_params(deep=True)

Get parameters for this estimator.

Parameters:
- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns:
- **params**: mapping of string to any
  - Parameter names mapped to their values.

predict(X)

Predict the labels for the data samples in X using trained model.

Parameters:
- **X**: array-like, shape (n_samples, n_features)
  - List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns:
- **labels**: array, shape (n_samples,)
  - Component labels.

predict_proba(X)

Predict posterior probability of each component given the data.

Parameters:
- **X**: array-like, shape (n_samples, n_features)
  - List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns:
- **resp**: array, shape (n_samples, n_components)
Returns the probability each Gaussian (state) in the model given each sample.

**sample** *(n_samples=1)*
Generate random samples from the fitted Gaussian distribution.

**Parameters**
- **n_samples** : int, optional
  Number of samples to generate. Defaults to 1.

**Returns**
- **X** : array, shape (n_samples, n_features)
  Randomly generated sample
- **y** : array, shape (nsamples,)
  Component labels

**score** *(X, y=None)*
Compute the per-sample average log-likelihood of the given data X.

**Parameters**
- **X** : array-like, shape (n_samples, n_dimensions)
  List of n_features-dimensional data points. Each row corresponds to a single data point.

**Returns**
- **log_likelihood** : float
  Log likelihood of the Gaussian mixture given X.

**score_samples** *(X)*
Compute the weighted log probabilities for each sample.

**Parameters**
- **X** : array-like, shape (n_samples, n_features)
  List of n_features-dimensional data points. Each row corresponds to a single data point.

**Returns**
- **log_prob** : array, shape (n_samples,)
  Log probabilities of each data point in X.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**
- **self**

**Examples using sklearn.mixture.GaussianMixture**

- Comparing different clustering algorithms on toy datasets
- Density Estimation for a Gaussian mixture
- Gaussian Mixture Model Ellipsoids
- Gaussian Mixture Model Selection
- GMM covariances
- Gaussian Mixture Model Sine Curve
30.23 sklearn.model_selection: Model Selection

User guide: See the Cross-validation: evaluating estimator performance, Tuning the hyper-parameters of an estimator and Learning curve sections for further details.

30.23.1 Splitter Classes

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>sklearn.model_selection.GroupKFold</td>
<td>K-fold iterator variant with non-overlapping groups.</td>
</tr>
<tr>
<td>sklearn.model_selection.GroupShuffleSplit</td>
<td>Shuffle-Group(s)-Out cross-validation iterator</td>
</tr>
<tr>
<td>sklearn.model_selection.KFold</td>
<td>K-Folds cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.LeaveOneGroupOut</td>
<td>Leave One Group Out cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.LeavePGroupsOut</td>
<td>Leave P Group(s) Out cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.LeaveOneOut</td>
<td>Leave-One-Out cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.LeavePOut</td>
<td>Leave-P-Out cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.PredefinedSplit</td>
<td>Predefined split cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.RepeatedKFold</td>
<td>Repeated K-Fold cross validator</td>
</tr>
<tr>
<td>sklearn.model_selection.ShuffleSplit</td>
<td>Random permutation cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.StratifiedKFold</td>
<td>Stratified K-Folds cross-validator</td>
</tr>
<tr>
<td>sklearn.model_selection.StratifiedShuffleSplit</td>
<td>Stratified ShuffleSplit cross-validator.</td>
</tr>
<tr>
<td>sklearn.model_selection.TimeSeriesSplit</td>
<td>Time Series cross-validator</td>
</tr>
</tbody>
</table>

**sklearn.model_selection.GroupKFold**

class sklearn.model_selection.GroupKFold(n_splits=3)

K-fold iterator variant with non-overlapping groups.

The same group will not appear in two different folds (the number of distinct groups has to be at least equal to the number of folds).

The folds are approximately balanced in the sense that the number of distinct groups is approximately the same in each fold.

Parameters n_splits : int, default=3

Number of folds. Must be at least 2.

See also:

**LeaveOneGroupOut** For splitting the data according to explicit domain-specific stratification of the dataset.

Examples

```python
>>> from sklearn.model_selection import GroupKFold
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 3, 4])
>>> groups = np.array([0, 0, 2, 2])
>>> group_kfold = GroupKFold(n_splits=2)
>>> group_kfold.get_n_splits(X, y, groups)
```
>>> print(group_kfold)
GroupKFold(n_splits=2)

>>> for train_index, test_index in group_kfold.split(X, y, groups):
    ...
    print("TRAIN:", train_index, "TEST:", test_index)
    ...
    X_train, X_test = X[train_index], X[test_index]
    ...
    y_train, y_test = y[train_index], y[test_index]
    ...
    print(X_train, X_test, y_train, y_test)
    ...
TRAIN: [0 1] TEST: [2 3]
[[1 2]
 [3 4]] [[5 6]
 [7 8]] [1 2] [3 4]
TRAIN: [2 3] TEST: [0 1]
[[5 6]
 [7 8]] [1 2]
 [3 4]] [3 4] [1 2]

Methods

:get_n_splits([X, y, groups]):
Returns the number of splitting iterations in the cross-validator

:split(X, y=None, groups=None):
Generate indices to split data into training and test set.

:__init__(n_splits=3)

:get_n_splits(X=None, y=None, groups=None):
Returns the number of splitting iterations in the cross-validator

Parameters

X : object
    Always ignored, exists for compatibility.

y : object
    Always ignored, exists for compatibility.

groups : object
    Always ignored, exists for compatibility.

Returns

n_splits : int
    Returns the number of splitting iterations in the cross-validator.

:spli t(X=None, y=None, groups=None):
Generate indices to split data into training and test set.

Parameters

X : array-like, shape (n_samples, n_features)
    Training data, where n_samples is the number of samples and n_features is the number of features.

y : array-like, shape (n_samples,)
    The target variable for supervised learning problems.

groups : array-like, with shape (n_samples,), optional
    Group labels for the samples used while splitting the dataset into train/test set.
Returns train : ndarray
    The training set indices for that split.

test : ndarray
    The testing set indices for that split.

Notes

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

sklearn.model_selection.GroupShuffleSplit

class sklearn.model_selection.GroupShuffleSplit(n_splits=5, test_size=’default’, train_size=None, random_state=None)

Shuffle-Group(s)-Out cross-validation iterator

Provides randomized train/test indices to split data according to a third-party provided group. This group information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

The difference between LeavePGroupsOut and GroupShuffleSplit is that the former generates splits using all subsets of size p unique groups, whereas GroupShuffleSplit generates a user-determined number of random test splits, each with a user-determined fraction of unique groups.

For example, a less computationally intensive alternative to LeavePGroupsOut(p=10) would be GroupShuffleSplit(test_size=10, n_splits=100).

Note: The parameters test_size and train_size refer to groups, and not to samples, as in ShuffleSplit.

Parameters n_splits : int (default 5)
    Number of re-shuffling & splitting iterations.

test_size : float, int, None, optional
    If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. By default, the value is set to 0.2. The default will change in version 0.21. It will remain 0.2 only if train_size is unspecified, otherwise it will complement the specified train_size.

train_size : float, int, or None, default is None
    If float, should be between 0.0 and 1.0 and represent the proportion of the groups to include in the train split. If int, represents the absolute number of train groups. If None, the value is automatically set to the complement of the test size.

random_state : int, RandomState instance or None, optional (default=None)
    If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
Methods

### `get_n_splits([X, y, groups])`

Returns the number of splitting iterations in the cross-validator

### `split(X[, y, groups])`

Generate indices to split data into training and test set.

---

**__init__**

`(n_splits=5, test_size='default', train_size=None, random_state=None)`

**get_n_splits**

`(X=None, y=None, groups=None)`

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X**: object
  - Always ignored, exists for compatibility.
- **y**: object
  - Always ignored, exists for compatibility.
- **groups**: object
  - Always ignored, exists for compatibility.

**Returns**

- **n_splits**: int
  - Returns the number of splitting iterations in the cross-validator.

**split**

`(X, y=None, groups=None)`

Generate indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  - Training data, where n_samples is the number of samples and n_features is the number of features.
- **y**: array-like, shape (n_samples,)
  - The target variable for supervised learning problems.
- **groups**: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.

**Returns**

- **train**: ndarray
  - The training set indices for that split.
- **test**: ndarray
  - The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting `random_state` to an integer.

**sklearn.model_selection.KFold**

**class**

`sklearn.model_selection.KFold(n_splits=3, shuffle=False, random_state=None)`

K-Folds cross-validator
Provides train/test indices to split data in train/test sets. Split dataset into k consecutive folds (without shuffling by default).

Each fold is then used once as a validation while the k - 1 remaining folds form the training set.

Read more in the User Guide.

**Parameters**

- **n_splits**: int, default=3
  
  Number of folds. Must be at least 2.

- **shuffle**: boolean, optional
  
  Whether to shuffle the data before splitting into batches.

- **random_state**: int, RandomState instance or None, optional, default=None
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle == True.

See also:

- **StratifiedKFold** Takes group information into account to avoid building folds with imbalanced class distributions (for binary or multiclass classification tasks).

- **GroupKFold** K-fold iterator variant with non-overlapping groups.

- **RepeatedKFold** Repeats K-Fold n times.

Notes

The first $n_samples \% n_splits$ folds have size $n_samples \div n_splits + 1$, other folds have size $n_samples \div n_splits$, where $n_samples$ is the number of samples.

Examples

```python
>>> from sklearn.model_selection import KFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4])
>>> kf = KFold(n_splits=2)
>>> kf.get_n_splits(X)
2
>>> print(kf)
KFold(n_splits=2, random_state=None, shuffle=False)
>>> for train_index, test_index in kf.split(X):
...     print("TRAIN: ", train_index, "TEST: ", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [0 1] TEST: [2 3]
```

Methods
**get_n_splits**([X, y, groups]) Returns the number of splitting iterations in the cross-validator

**split**(X[, y, groups]) Generate indices to split data into training and test set.

__init__(n_splits=3, shuffle=False, random_state=None)

**get_n_splits**(X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

Parameters

- **X**: object
  - Always ignored, exists for compatibility.
- **y**: object
  - Always ignored, exists for compatibility.
- **groups**: object
  - Always ignored, exists for compatibility.

Returns

- **n_splits**: int
  - Returns the number of splitting iterations in the cross-validator.

**split**(X, y=None, groups=None)

Generate indices to split data into training and test set.

Parameters

- **X**: array-like, shape (n_samples, n_features)
  - Training data, where n_samples is the number of samples and n_features is the number of features.
- **y**: array-like, shape (n_samples,)
  - The target variable for supervised learning problems.
- **groups**: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.

Returns

- **train**: ndarray
  - The training set indices for that split.
- **test**: ndarray
  - The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

**Examples using sklearn.model_selection.KFold**

- Feature agglomeration vs. univariate selection
- Gradient Boosting Out-of-Bag estimates
- Cross-validation on diabetes Dataset Exercise
- Nested versus non-nested cross-validation
**Leave One Group Out cross-validator**

Provides train/test indices to split data according to a third-party provided group. This group information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the groups could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

Read more in the *User Guide*.

### Examples

```python
code
>>> from sklearn.model_selection import LeaveOneGroupOut
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 1, 2])
>>> groups = np.array([1, 1, 2, 2])
>>> logo = LeaveOneGroupOut()
>>> logo.get_n_splits(X, y, groups)
2
>>> logo.get_n_splits(groups=groups)  # 'groups' is always required
2
>>> print(logo)
LeaveOneGroupOut()

>>> for train_index, test_index in logo.split(X, y, groups):
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
...     print(X_train, X_test, y_train, y_test)
TRAIN: [2 3] TEST: [0 1]
[[5 6]
 [7 8]] [[1 2]
 [3 4]]
TRAIN: [0 1] TEST: [2 3]
[[1 2]
 [3 4]] [[5 6]
 [7 8]]
```

### Methods

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<td><code>get_n_splits([X, y, groups])</code></td>
<td>Returns the number of splitting iterations in the cross-validator</td>
</tr>
<tr>
<td><code>split(X, y, groups)</code></td>
<td>Generate indices to split data into training and test set.</td>
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</table>

#### __init__ ()

`get_n_splits(X=None, y=None, groups=None)`

Returns the number of splitting iterations in the cross-validator

**Parameters**

- `X`: object, optional

  Always ignored, exists for compatibility.
y : object, optional
   Always ignored, exists for compatibility.

groups : array-like, with shape (n_samples,), optional
   Group labels for the samples used while splitting the dataset into train/test set. This
   ‘groups’ parameter must always be specified to calculate the number of splits, though
   the other parameters can be omitted.

Returns n_splits : int
   Returns the number of splitting iterations in the cross-validator.

split (X, y=None, groups=None)
   Generate indices to split data into training and test set.

   Parameters X : array-like, shape (n_samples, n_features)
      Training data, where n_samples is the number of samples and n_features is the number
      of features.
   y : array-like, of length n_samples
      The target variable for supervised learning problems.
   groups : array-like, with shape (n_samples,), optional
      Group labels for the samples used while splitting the dataset into train/test set.

Returns train : ndarray
   The training set indices for that split.

test : ndarray
   The testing set indices for that split.

Notes

Randomized CV splitters may return different results for each call of split. You can make the results
identical by setting random_state to an integer.

sklearn.model_selection.LeavePGroupsOut

class sklearn.model_selection.LeavePGroupsOut (n_groups)
   Leave P Group(s) Out cross-validator

   Provides train/test indices to split data according to a third-party provided group. This group information can be
   used to encode arbitrary domain specific stratifications of the samples as integers.

   For instance the groups could be the year of collection of the samples and thus allow for cross-validation against
   time-based splits.

   The difference between LeavePGroupsOut and LeaveOneGroupOut is that the former builds the test sets with
   all the samples assigned to \( p \) different values of the groups while the latter uses samples all assigned the same
   groups.

   Read more in the User Guide.

   Parameters n_groups : int
      Number of groups (\( p \)) to leave out in the test split.
See also:

**GroupKFold** K-fold iterator variant with non-overlapping groups.

**Examples**

```python
>>> from sklearn.model_selection import LeavePGroupsOut
>>> X = np.array([[1, 2], [3, 4], [5, 6]])
>>> y = np.array([1, 2, 1])
>>> groups = np.array([1, 2, 3])
>>> lpgo = LeavePGroupsOut(n_groups=2)
>>> lpgo.get_n_splits(X, y, groups)
3
>>> lpgo.get_n_splits(groups=groups)  # 'groups' is always required
3
>>> print(lpgo)
LeavePGroupsOut(n_groups=2)
>>> for train_index, test_index in lpgo.split(X, y, groups):
...   print("TRAIN:", train_index, "TEST:", test_index)
...   X_train, X_test = X[train_index], X[test_index]
...   y_train, y_test = y[train_index], y[test_index]
...   print(X_train, X_test, y_train, y_test)
TRAIN: [2] TEST: [0 1]
[[5 6]] [[1 2]
 [3 4]] [1] [1 2]
TRAIN: [1] TEST: [0 2]
[[3 4]] [[1 2]
 [5 6]] [2] [1 1]
TRAIN: [0] TEST: [1 2]
[[1 2]] [[3 4]
 [5 6]] [1] [2 1]
```

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<td><code>get_n_splits([X, y, groups])</code></td>
<td>Returns the number of splitting iterations in the cross-validator.</td>
</tr>
<tr>
<td><code>split(X[, y, groups])</code></td>
<td>Generate indices to split data into training and test set.</td>
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</table>

**__init__(n_groups)**

- `get_n_splits(X=None, y=None, groups=None)`
  - Returns the number of splitting iterations in the cross-validator.

  **Parameters**
  - **X**: object, optional
    - Always ignored, exists for compatibility.
  - **y**: object, optional
    - Always ignored, exists for compatibility.
  - **groups**: array-like, with shape (n_samples,), optional
    - Group labels for the samples used while splitting the dataset into train/test set. This ‘groups’ parameter must always be specified to calculate the number of splits, though the other parameters can be omitted.
Returns `n_splits` : int

Returns the number of splitting iterations in the cross-validator.

`split` *(X, y=None, groups=None)*

Generate indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  Training data, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, of length n_samples
  
  The target variable for supervised learning problems.

- **groups**: array-like, with shape (n_samples,), optional
  
  Group labels for the samples used while splitting the dataset into train/test set.

**Returns**

- **train**: ndarray
  
  The training set indices for that split.

- **test**: ndarray
  
  The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting `random_state` to an integer.

**sklearn.model_selection.LeaveOneOut**

**class** `sklearn.model_selection.LeaveOneOut`

Leave-One-Out cross-validator

Provides train/test indices to split data in train/test sets. Each sample is used once as a test set (singleton) while the remaining samples form the training set.

**Note:** `LeaveOneOut()` is equivalent to `KFold(n_splits=n)` and `LeavePOut(p=1)` where n is the number of samples.

Due to the high number of test sets (which is the same as the number of samples) this cross-validation method can be very costly. For large datasets one should favor `KFold`, `ShuffleSplit` or `StratifiedKFold`.


**See also:**

- `LeaveOneGroupOut` For splitting the data according to explicit, domain-specific stratification of the dataset.
- `GroupKFold` K-fold iterator variant with non-overlapping groups.

**Examples**
```python
>>> from sklearn.model_selection import LeaveOneOut
>>> X = np.array([[1, 2], [3, 4]])
>>> y = np.array([1, 2])
>>> loo = LeaveOneOut()
>>> loo.get_n_splits(X)
2
>>> print(loo)
LeaveOneOut()
>>> for train_index, test_index in loo.split(X):
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
...     print(X_train, X_test, y_train, y_test)
TRAIN: [1] TEST: [0]
[[3 4]] [[1 2]] [2] [1]
TRAIN: [0] TEST: [1]
[[1 2]] [[3 4]] [1] [2]
```

### Methods

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<td><strong>get_n_splits</strong></td>
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<tr>
<td><strong>split</strong></td>
<td>Generate indices to split data into training and test set.</td>
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</table>

---

**__init__**()

**get_n_splits** *(X, y=None, groups=None)*

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  Training data, where n_samples is the number of samples and n_features is the number of features.

- **y**: object
  
  Always ignored, exists for compatibility.

- **groups**: object
  
  Always ignored, exists for compatibility.

**Returns**

- **n_splits**: int
  
  Returns the number of splitting iterations in the cross-validator.

**split** *(X, y=None, groups=None)*

Generate indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  Training data, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, of length n_samples
  
  The target variable for supervised learning problems.

- **groups**: array-like, with shape (n_samples,), optional
Group labels for the samples used while splitting the dataset into train/test set.

**Returns**

`train` : ndarray
   The training set indices for that split.

`test` : ndarray
   The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting `random_state` to an integer.

**sklearn.model_selection.LeavePOut**

**class** sklearn.model_selection.LeavePOut (p)

Leave-P-Out cross-validator

Provides train/test indices to split data in train/test sets. This results in testing on all distinct samples of size p, while the remaining n - p samples form the training set in each iteration.

Note: LeavePOut (p) is NOT equivalent to KFold(n_splits=n_samples // p) which creates non-overlapping test sets.

Due to the high number of iterations which grows combinatorially with the number of samples this cross-validation method can be very costly. For large datasets one should favor KFold, StratifiedKFold or ShuffleSplit.


**Parameters**

- `p` : int
  Size of the test sets.

**Examples**

```python
>>> from sklearn.model_selection import LeavePOut
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 3, 4])
>>> lpo = LeavePOut(2)
>>> lpo.get_n_splits(X)
6
>>> print(lpo)
LeavePOut(p=2)
>>> for train_index, test_index in lpo.split(X):
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
TRAIN: [0 2] TEST: [1 3]
TRAIN: [0 1] TEST: [2 3]
```
Methods

**get_n_splits**(*X*, *y*, *groups*)
Returns the number of splitting iterations in the cross-validator

**split**(*X*, *y*, *groups*)
Generate indices to split data into training and test set.

__init__(*)

**get_n_splits**(*X*, *y=None*, *groups=None*)
Returns the number of splitting iterations in the cross-validator

*Parameters*

**X**: array-like, shape (n_samples, n_features)
Training data, where n_samples is the number of samples and n_features is the number of features.

**y**: object
Always ignored, exists for compatibility.

**groups**: object
Always ignored, exists for compatibility.

**split**(*X*, *y=None*, *groups=None*)
Generate indices to split data into training and test set.

*Parameters*

**X**: array-like, shape (n_samples, n_features)
Training data, where n_samples is the number of samples and n_features is the number of features.

**y**: array-like, of length n_samples
The target variable for supervised learning problems.

**groups**: array-like, with shape (n_samples,), optional
Group labels for the samples used while splitting the dataset into train/test set.

*Returns*

**train**: ndarray
The training set indices for that split.

**test**: ndarray
The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

**sklearn.model_selection.PredefinedSplit**

class sklearn.model_selection.PredefinedSplit(*test_fold*)
Predefined split cross-validator

Provides train/test indices to split data into train/test sets using a predefined scheme specified by the user with the test_fold parameter.
Parameters **test_fold** : array-like, shape (n_samples,)

The entry test_fold[i] represents the index of the test set that sample i belongs to. It is possible to exclude sample i from any test set (i.e. include sample i in every training set) by setting test_fold[i] equal to -1.

Examples

```python
>>> from sklearn.model_selection import PredefinedSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> test_fold = [0, 1, -1, 1]
>>> ps = PredefinedSplit(test_fold)
>>> ps.get_n_splits()
2
>>> print(ps)
PredefinedSplit(test_fold=array([0, 1, -1, 1]))

>>> for train_index, test_index in ps.split():
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 2 3] TEST: [0]
TRAIN: [0 2] TEST: [1 3]
```

Methods

```
get_n_splits([X, y, groups]) Returns the number of splitting iterations in the cross-validator

split([X, y, groups]) Generate indices to split data into training and test set.

__init__(test_fold)
```

get_n_splits *(X=None, y=None, groups=None)*

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X** : object
  
  Always ignored, exists for compatibility.

- **y** : object
  
  Always ignored, exists for compatibility.

- **groups** : object
  
  Always ignored, exists for compatibility.

**Returns**

- **n_splits** : int
  
  Returns the number of splitting iterations in the cross-validator.

split *(X=None, y=None, groups=None)*

Generate indices to split data into training and test set.

**Parameters**

- **X** : object
Always ignored, exists for compatibility.

y : object
Always ignored, exists for compatibility.

groups : object
Always ignored, exists for compatibility.

Returns

train : ndarray
The training set indices for that split.

test : ndarray
The testing set indices for that split.

sklearn.model_selection.RepeatedKFold

class sklearn.model_selection.RepeatedKFold(n_splits=5, n_repeats=10, random_state=None)

Repeated K-Fold cross validator.
Repeats K-Fold n times with different randomization in each repetition.
Read more in the User Guide.

Parameters

n_splits : int, default=5
Number of folds. Must be at least 2.

n_repeats : int, default=10
Number of times cross-validator needs to be repeated.

random_state : int, RandomState instance or None, optional, default=None
If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

See also:

RepeatedStratifiedKFold Repeates Stratified K-Fold n times.

Examples

```python
>>> from sklearn.model_selection import RepeatedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> rkf = RepeatedKFold(n_splits=2, n_repeats=2, random_state=2652124)
>>> for train_index, test_index in rkf.split(X):
...    print("TRAIN: ", train_index, " TEST: ", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
...    ...
TRAIN: [0 1] TEST: [2 3]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
```
## Methods

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<tr>
<td><code>get_n_splits</code></td>
<td>Returns the number of splitting iterations in the cross-validator</td>
</tr>
<tr>
<td><code>split</code></td>
<td>Generates indices to split data into training and test set.</td>
</tr>
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</table>

### `__init__`(n_splits=5, n_repeats=10, random_state=None)

**get_n_splits**(X=None, y=None, groups=None)

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X**: object
  - Always ignored, exists for compatibility. `np.zeros(n_samples)` may be used as a placeholder.
- **y**: object
  - Always ignored, exists for compatibility. `np.zeros(n_samples)` may be used as a placeholder.
- **groups**: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.

**Returns**

- **n_splits**: int
  - Returns the number of splitting iterations in the cross-validator.

### `split`(X, y=None, groups=None)

Generates indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  - Training data, where n_samples is the number of samples and n_features is the number of features.
- **y**: array-like, of length n_samples
  - The target variable for supervised learning problems.
- **groups**: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.

**Returns**

- **train**: ndarray
  - The training set indices for that split.
- **test**: ndarray
  - The testing set indices for that split.

### `sklearn.model_selection.RepeatedStratifiedKFold`

**class** `sklearn.model_selection.RepeatedStratifiedKFold`(n_splits=5, n_repeats=10, random_state=None)

Repeated Stratified K-Fold cross validator.

- Repeats Stratified K-Fold n times with different randomization in each repetition.
- Read more in the User Guide.
Parameters **n_splits**: int, default=5

Number of folds. Must be at least 2.

**n_repeats**: int, default=10

Number of times cross-validator needs to be repeated.

**random_state**: None, int or RandomState, default=None

Random state to be used to generate random state for each repetition.

See also:

*RepeatedKFold* Repeats K-Fold n times.

Examples

```python
>>> from sklearn.model_selection import RepeatedStratifiedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> rskf = RepeatedStratifiedKFold(n_splits=2, n_repeats=2,
...     random_state=36851234)
>>> for train_index, test_index in rskf.split(X, y):
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
...     print("TRAIN: ", train_index, " TEST: ", test_index)
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [0 2] TEST: [1 3]
```

Methods

*get_n_splits*(X=None, y=None, groups=None) Returns the number of splitting iterations in the cross-validator

*split*(X, y, groups=None) Generates indices to split data into training and test set.

__init__ (n_splits=5, n_repeats=10, random_state=None) Returns the number of splitting iterations in the cross-validator

Parameters **X**: object

Always ignored, exists for compatibility. np.zeros(n_samples) may be used as a placeholder.

**y**: object

Always ignored, exists for compatibility. np.zeros(n_samples) may be used as a placeholder.

**groups**: array-like, with shape (n_samples,), optional

Group labels for the samples used while splitting the dataset into train/test set.
**Returns n_splits : int**

Returns the number of splitting iterations in the cross-validator.

**split (X, y=None, groups=None)**

Generates indices to split data into training and test set.

**Parameters X : array-like, shape (n_samples, n_features)**

Training data, where n_samples is the number of samples and n_features is the number of features.

**y : array-like, of length n_samples**

The target variable for supervised learning problems.

**groups : array-like, with shape (n_samples,), optional**

Group labels for the samples used while splitting the dataset into train/test set.

**Returns train : ndarray**

The training set indices for that split.

**test : ndarray**

The testing set indices for that split.

**sklearn.model_selection.ShuffleSplit**

class sklearn.model_selection.ShuffleSplit (n_splits=10, test_size='default', train_size=None, random_state=None)

Random permutation cross-validator

Yields indices to split data into training and test sets.

Note: contrary to other cross-validation strategies, random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the User Guide.

**Parameters n_splits : int, default 10**

Number of re-shuffling & splitting iterations.

**test_size : float, int, None, default=0.1**

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. By default (the is parameter unspecified), the value is set to 0.1. The default will change in version 0.21. It will remain 0.1 only if train_size is unspecified, otherwise it will complement the specified train_size.

**train_size : float, int, or None, default=None**

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.

**random_state : int, RandomState instance or None, optional (default=None)**

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.
## Examples

```python
>>> from sklearn.model_selection import ShuffleSplit
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 1, 2])
>>> rs = ShuffleSplit(n_splits=3, test_size=.25, random_state=0)
>>> rs.get_n_splits(X)
3
>>> print(rs)
ShuffleSplit(n_splits=3, random_state=0, test_size=0.25, train_size=None)
>>> for train_index, test_index in rs.split(X):
...     print("TRAIN:", train_index, "TEST:", test_index)
...TRAIN: [3 1 0] TEST: [2]
TRAIN: [2 1 3] TEST: [0]
TRAIN: [0 2 1] TEST: [3]
>>> rs = ShuffleSplit(n_splits=3, train_size=0.5, test_size=.25,
...                   random_state=0)
>>> for train_index, test_index in rs.split(X):
...     print("TRAIN:", train_index, "TEST:", test_index)
...TRAIN: [3 1] TEST: [2]
TRAIN: [2 1] TEST: [0]
TRAIN: [0 2] TEST: [3]
```

## Methods

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<tr>
<td><code>get_n_splits(X, y, groups)</code></td>
<td>Returns the number of splitting iterations in the cross-validator</td>
</tr>
<tr>
<td><code>split(X, y, groups)</code></td>
<td>Generate indices to split data into training and test set.</td>
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### `__init__(n_splits=10, test_size='default', train_size=None, random_state=None)`

#### `get_n_splits(X=None, y=None, groups=None)`

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X** : object
  
  Always ignored, exists for compatibility.

- **y** : object
  
  Always ignored, exists for compatibility.

- **groups** : object
  
  Always ignored, exists for compatibility.

**Returns**

- **n_splits** : int
  
  Returns the number of splitting iterations in the cross-validator.

### `split(X=None, y=None, groups=None)`

Generate indices to split data into training and test set.

**Parameters**

- **X** : array-like, shape (n_samples, n_features)
  
  Training data, where n_samples is the number of samples and n_features is the number of features.
y : array-like, shape (n_samples,)
    The target variable for supervised learning problems.
groups : array-like, with shape (n_samples,), optional
    Group labels for the samples used while splitting the dataset into train/test set.

Returns
train : ndarray
    The training set indices for that split.
test : ndarray
    The testing set indices for that split.

Notes
Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

Examples using sklearn.model_selection.ShuffleSplit

- Plotting Learning Curves
- Scaling the regularization parameter for SVCs

sklearn.model_selection.StratifiedKFold

class sklearn.model_selection.StratifiedKFold(n_splits=3, shuffle=False, random_state=None)

Stratified K-Folds cross-validator

Provides train/test indices to split data in train/test sets.

This cross-validation object is a variation of KFold that returns stratified folds. The folds are made by preserving the percentage of samples for each class.

Read more in the User Guide.

Parameters
n_splits : int, default=3
    Number of folds. Must be at least 2.
shuffle : boolean, optional
    Whether to shuffle each stratification of the data before splitting into batches.
random_state : int, RandomState instance or None, optional, default=None
    If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle == True.

See also:

RepeatedStratifiedKFold Repeats Stratified K-Fold n times.
Notes

All the folds have size \( \text{trunc}(n_{\text{samples}} / n_{\text{splits}}) \), the last one has the complementary.

Examples

```python
>>> from sklearn.model_selection import StratifiedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> skf = StratifiedKFold(n_splits=2)
>>> skf.get_n_splits(X, y)
2
>>> print(skf)
StratifiedKFold(n_splits=2, random_state=None, shuffle=False)
>>> for train_index, test_index in skf.split(X, y):
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [0 2] TEST: [1 3]
```

Methods

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<td><code>get_n_splits</code></td>
<td>Returns the number of splitting iterations in the cross-validator.</td>
</tr>
<tr>
<td><code>split</code></td>
<td>Generate indices to split data into training and test set.</td>
</tr>
<tr>
<td><code>__init__</code></td>
<td>(n_splits=3, shuffle=False, random_state=None)</td>
</tr>
<tr>
<td><code>get_n_splits</code></td>
<td>(X=None, y=None, groups=None)</td>
</tr>
<tr>
<td><code>split</code></td>
<td>(X, y, groups=None)</td>
</tr>
</tbody>
</table>

**Parameters**

- **X**: object
  - Always ignored, exists for compatibility.
- **y**: object
  - Always ignored, exists for compatibility.
- **groups**: object
  - Always ignored, exists for compatibility.

**Returns**

- **n_splits**: int
  - Returns the number of splitting iterations in the cross-validator.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  - Training data, where n_samples is the number of samples and n_features is the number of features.
Note that providing \( y \) is sufficient to generate the splits and hence `np.zeros(n_samples)` may be used as a placeholder for \( X \) instead of actual training data.

\[ y : \text{array-like, shape (n_samples,)} \]

The target variable for supervised learning problems. Stratification is done based on the \( y \) labels.

\[ \text{groups} : \text{object} \]

Always ignored, exists for compatibility.

Returns

\[ \text{train} : \text{ndarray} \]

The training set indices for that split.

\[ \text{test} : \text{ndarray} \]

The testing set indices for that split.

Notes

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting `random_state` to an integer.

Examples using `sklearn.model_selection.StratifiedKFold`

- Recursive feature elimination with cross-validation
- Test with permutations the significance of a classification score
- GMM covariances
- Receiver Operating Characteristic (ROC) with cross validation

`sklearn.model_selection.StratifiedShuffleSplit`

class `sklearn.model_selection.StratifiedShuffleSplit`

\[ (n_splits=10, \quad \text{test_size}='\text{default}', \quad \text{train_size}=\text{None}, \quad \text{random_state}=\text{None}) \]

Stratified ShuffleSplit cross-validator

Provides train/test indices to split data in train/test sets.

This cross-validation object is a merge of StratifiedKFold and ShuffleSplit, which returns stratified randomized folds. The folds are made by preserving the percentage of samples for each class.

Note: like the ShuffleSplit strategy, stratified random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the User Guide.

Parameters

\[ \text{n_splits} : \text{int, default 10} \]

Number of re-shuffling & splitting iterations.

\[ \text{test_size} : \text{float, int, None, optional} \]
If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. By default, the value is set to 0.1. The default will change in version 0.21. It will remain 0.1 only if `train_size` is unspecified, otherwise it will complement the specified `train_size`.

**train_size**: float, int, or None, default is None

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

### Examples

```python
>>> from sklearn.model_selection import StratifiedShuffleSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> sss = StratifiedShuffleSplit(n_splits=3, test_size=0.5, random_state=0)
>>> sss.get_n_splits(X, y)
3
>>> print(sss)
StratifiedShuffleSplit(n_splits=3, random_state=0, ...)
>>> for train_index, test_index in sss.split(X, y):
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 2] TEST: [3 0]
TRAIN: [0 2] TEST: [1 3]
TRAIN: [0 2] TEST: [3 1]
```

### Methods

- **get_n_splits**([X, y, groups]): Returns the number of splitting iterations in the cross-validator
- **split**(X, y[, groups]): Generate indices to split data into training and test set.

```python
__init__(n_splits=10, test_size='default', train_size=None, random_state=None)
get_n_splits(X=None, y=None, groups=None)
```

Returns the number of splitting iterations in the cross-validator

**Parameters**

- **X** : object
  
  Always ignored, exists for compatibility.

- **y** : object
  
  Always ignored, exists for compatibility.

- **groups** : object
Always ignored, exists for compatibility.

**Returns**  
**n_splits : int**

Returns the number of splitting iterations in the cross-validator.

**split** (*X*, *y*, *groups=None*)

Generate indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  Training data, where n_samples is the number of samples and n_features is the number of features.
  
  Note that providing *y* is sufficient to generate the splits and hence np.zeros(n_samples) may be used as a placeholder for *X* instead of actual training data.

- **y**: array-like, shape (n_samples,)
  
  The target variable for supervised learning problems. Stratification is done based on the *y* labels.

- **groups**: object
  
  Always ignored, exists for compatibility.

**Returns**

- **train**: ndarray
  
  The training set indices for that split.

- **test**: ndarray
  
  The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

**Examples using sklearn.model_selection.StratifiedShuffleSplit**

- **RBF SVM parameters**

**sklearn.model_selection.TimeSeriesSplit**

**class**  

sklearn.model_selection.TimeSeriesSplit (*n_splits=3*, *max_train_size=None*)

Time Series cross-validator

Provides train/test indices to split time series data samples that are observed at fixed time intervals, in train/test sets. In each split, test indices must be higher than before, and thus shuffling in cross validator is inappropriate.

This cross-validation object is a variation of KFold. In the kth split, it returns first k folds as train set and the (k+1)th fold as test set.

Note that unlike standard cross-validation methods, successive training sets are supersets of those that come before them.

Read more in the User Guide.

**Parameters**

- **n_splits : int, default=3**
Number of splits. Must be at least 1.

\texttt{max_train_size} : int, optional

Maximum size for a single training set.

Notes

The training set has size \(i \times n_{\text{samples}} // (n_{\text{splits}} + 1) + n_{\text{samples}} \% (n_{\text{splits}} + 1)\) in the \(i^{\text{th}}\) split, with a test set of size \(n_{\text{samples}}//(n_{\text{splits}} + 1)\), where \(n_{\text{samples}}\) is the number of samples.

Examples

```python
>>> from sklearn.model_selection import TimeSeriesSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4])
>>> tscv = TimeSeriesSplit(n_splits=3)
>>> print(tscv)
TimeSeriesSplit(max_train_size=None, n_splits=3)
>>> for train_index, test_index in tscv.split(X):
...    print("TRAIN: ", train_index, " TEST: ", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
TRAIN: [0] TEST: [1]
TRAIN: [0 1] TEST: [2]
TRAIN: [0 1 2] TEST: [3]
```

Methods

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<tr>
<td>\texttt{get_n_splits}([X, y, groups])</td>
<td>Returns the number of splitting iterations in the cross-validator</td>
</tr>
<tr>
<td>\texttt{split(X[, y, groups])}</td>
<td>Generate indices to split data into training and test set.</td>
</tr>
</tbody>
</table>

\texttt{__init__} (\texttt{n_splits=3, max_train_size=None})

\texttt{get_n_splits} (\texttt{X=None, y=None, groups=None})

Returns the number of splitting iterations in the cross-validator

**Parameters**

\texttt{X} : object

Always ignored, exists for compatibility.

\texttt{y} : object

Always ignored, exists for compatibility.

\texttt{groups} : object

Always ignored, exists for compatibility.

**Returns**

\texttt{n_splits} : int

Returns the number of splitting iterations in the cross-validator.
split \((X, y=None, groups=None)\)
Generate indices to split data into training and test set.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Training data, where n_samples is the number of samples and n_features is the number of features.
- **y**: array-like, shape (n_samples,)
  Always ignored, exists for compatibility.
- **groups**: array-like, with shape (n_samples,), optional
  Always ignored, exists for compatibility.

**Returns**

- **train**: ndarray
  The training set indices for that split.
- **test**: ndarray
  The testing set indices for that split.

**Notes**

Randomized CV splitters may return different results for each call of split. You can make the results identical by setting random_state to an integer.

### 30.23.2 Splitter Functions

- `model_selection.check_cv([cv, y, classifier])`
  Input checker utility for building a cross-validator
- `model_selection.train_test_split(*arrays, ...)`
  Split arrays or matrices into random train and test subsets

#### `sklearn.model_selection.check_cv`

`sklearn.model_selection.check_cv(cv=3, y=None, classifier=False)`
Input checker utility for building a cross-validator

**Parameters**

- **cv**: int, cross-validation generator or an iterable, optional
  Determines the cross-validation splitting strategy. Possible inputs for cv are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - An object to be used as a cross-validation generator.
  - An iterable yielding train/test splits.

  For integer/None inputs, if classifier is True and y is either binary or multiclass, `StratifiedKFold` is used. In all other cases, `KFold` is used.

  Refer [User Guide](https://scikit-learn.org) for the various cross-validation strategies that can be used here.

- **y**: array-like, optional
  The target variable for supervised learning problems.
classifier : boolean, optional, default False

Whether the task is a classification task, in which case stratified KFold will be used.

Returns checked_cv : a cross-validator instance.

The return value is a cross-validator which generates the train/test splits via the split method.

sklearn.model_selection.train_test_split

**Parameters**

**arrays** : sequence of indexables with same length / shape[0]

Allowed inputs are lists, numpy arrays, scipy-sparse matrices or pandas dataframes.

test_size : float, int, None, optional

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is set to the complement of the train size. The default will change in version 0.21. It will remain 0.25 only if train_size is unspecified, otherwise it will complement the specified train_size.

train_size : float, int, or None, default None

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

shuffle : boolean, optional (default=True)

Whether or not to shuffle the data before splitting. If shuffle=False then stratify must be None.

stratify : array-like or None (default is None)

If not None, data is split in a stratified fashion, using this as the class labels.

Returns splitting : list, length=2 * len(arrays)

List containing train-test split of inputs.

New in version 0.16: If the input is sparse, the output will be a scipy.sparse.csr_matrix. Else, output type is the same as the input type.
Examples

```python
>>> import numpy as np
>>> from sklearn.model_selection import train_test_split
>>> X, y = np.arange(10).reshape((5, 2)), range(5)
>>> X
array([[0, 1],
       [2, 3],
       [4, 5],
       [6, 7],
       [8, 9]])
>>> list(y)
[0, 1, 2, 3, 4]

>>> X_train, X_test, y_train, y_test = train_test_split(...
...     X, y, test_size=0.33, random_state=42)
...
>>> X_train
array([[4, 5],
       [0, 1],
       [6, 7]])
>>> y_train
[2, 0, 3]
>>> X_test
array([[2, 3],
       [8, 9]])
>>> y_test
[1, 4]

>>> train_test_split(y, shuffle=False)
[[0, 1, 2], [3, 4]]
```

Examples using `sklearn.model_selection.train_test_split`

- Faces recognition example using eigenfaces and SVMs
- Prediction Latency
- Probability Calibration curves
- Probability calibration of classifiers
- Classifier comparison
- Comparing random forests and the multi-output meta estimator
- Partial Dependence Plots
- Early stopping of Gradient Boosting
- Feature transformations with ensembles of trees
- Gradient Boosting Out-of-Bag estimates
- Pipeline Anova SVM
- Comparing various online solvers
- MNIST classification using multinomial logistic + L1
Multiclass sparse logistic regression on newsgroups
Parameter estimation using grid search with cross-validation
Confusion matrix
Receiver Operating Characteristic (ROC)
Precision-Recall
Classifier Chain
Restricted Boltzmann Machine features for digit classification
Varying regularization in Multi-layer Perceptron
Using FunctionTransformer to select columns
Importance of Feature Scaling
Understanding the decision tree structure

30.23.3 Hyper-parameter optimizers

model_selection.GridSearchCV(estimator, ...) Exhaustive search over specified parameter values for an estimator.
model_selection.ParameterGrid(param_grid) Grid of parameters with a discrete number of values for each.
model_selection.ParameterSampler(...) Generator on parameters sampled from given distributions.
model_selection.RandomizedSearchCV(...) Randomized search on hyper parameters.

sklearn.model_selection.GridSearchCV

class sklearn.model_selection.GridSearchCV (estimator, param_grid, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', error_score='raise', return_train_score='warn')

Exhaustive search over specified parameter values for an estimator.

Important members are fit, predict.

GridSearchCV implements a “fit” and a “score” method. It also implements “predict”, “predict_proba”, “decision_function”, “transform” and “inverse_transform” if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated grid-search over a parameter grid.

Read more in the User Guide.

Parameters estimator : estimator object.

This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.

param_grid : dict or list of dictionaries

Dictionary with parameters names (string) as keys and lists of parameter settings to try as values, or a list of such dictionaries, in which case the grids spanned by each dic-

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tionary in the list are explored. This enables searching over any sequence of parameter settings.

**scoring** : string, callable, list/tuple, dict or None, default: None

A single string (see The scoring parameter: defining model evaluation rules) or a callable (see Defining your scoring strategy from metric functions) to evaluate the predictions on the test set.

For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See Specifying multiple metrics for evaluation for an example.

If None, the estimator’s default scorer (if available) is used.

**fit_params** : dict, optional

Parameters to pass to the fit method.

Deprecated since version 0.19: fit_params as a constructor argument was deprecated in version 0.19 and will be removed in version 0.21. Pass fit parameters to the fit method instead.

**n_jobs** : int, default=1

Number of jobs to run in parallel.

**pre_dispatch** : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

- None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

**iid** : boolean, default=True

If True, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds.

**cv** : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross validation,
- integer, to specify the number of folds in a (Stratified)KFold,
- An object to be used as a cross-validation generator.
- An iterable yielding train, test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.
refit : boolean, or string, default=True

Refit an estimator using the best found parameters on the whole dataset.

For multiple metric evaluation, this needs to be a string denoting the scorer is used to
find the best parameters for refitting the estimator at the end.

The refitted estimator is made available at the best_estimator_* attribute and per-
mits using predict directly on this GridSearchCV instance.

Also for multiple metric evaluation, the attributes best_index_, best_score_ and
best_parameters_ will only be available if refit is set and all of them will
be determined w.r.t this specific scorer.

See scoring parameter to know more about multiple metric evaluation.

verbose : integer

Controls the verbosity: the higher, the more messages.

error_score : ‘raise’ (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the
error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter
does not affect the refit step, which will always raise the error.

return_train_score : boolean, optional

If False, the cv_results_ attribute will not include training scores.

Current default is 'warn', which behaves as True in addition to raising a warning
when a training score is looked up. That default will be changed to False in 0.21.
Computing training scores is used to get insights on how different parameter settings im-
pact the overfitting/underfitting trade-off. However computing the scores on the training
set can be computationally expensive and is not strictly required to select the parameters
that yield the best generalization performance.
Attributes

**cv_results_** of numpy (masked) ndarrays A dict with keys as column headers and values as columns, that can be imported into a pandas DataFrame. For instance the below given table will be represented by a cv_results_ dict of:

| param_kernel | param_gamma | param_degree | split0_test_score | rank_t | |poly| 1 | - | 2 | 1 | 0.8 | l | 2 | 1 | + | + | + | + | + | + | + | + | 'poly'| l | - | 1 | 3 | 1 | 0.7 | | 4 | 1 | + | + | + | + | + | + | + | + | 1 | 'rbf'| l | 0.1 | l | 0.8 | | 1 | + | + | + | + | + | + | + | + | + | 1 | 'rbf'| l | 0.2 | l | 1 | 0.9 | | 1 | + | + | + | + | + | + | + | + | + | will be represented by a cv_results_ dict of: { 'param_kernel': masked_array(data = ['poly', 'poly', 'rbf', 'rbf'], mask = [False, False, False, False]).  'param_gamma': masked_array(data = [0.1, 0.2, 0.7, 0.7], mask = [False, False, True, True]).  'param_degree': masked_array(data = [2.0, 3.0, -1, -1], mask = [False, False, False, False]).  'split0_test_score': [0.8, 0.7, 0.8, 0.9].  'split1_test_score': [0.82, 0.6, 0.7, 0.78].  'mean_test_score': [0.81, 0.60, 0.75, 0.82].  'std_test_score': [0.02, 0.01, 0.03, 0.03].  'rank_test_score': [2, 4, 3, 1].  'split0_train_score': [0.8, 0.9, 0.7].  'split1_train_score': [0.81, 0.7, 0.8].  'mean_train_score': [0.81, 0.7].  'std_train_score': [0.03, 0.03].  'mean_fit_time': [0.007, 0.06, 0.04, 0.04].  'std_fit_time': [0.007, 0.002, 0.003, 0.005].  'params': [{'kernel': 'poly', 'degree': 2}]. } NOTE The key 'params' is used to store a list of parameter settings dicts for all the parameter candidates. The mean_fit_time, std_fit_time, mean_score_time and std_score_time are all in seconds. For multi-metric evaluation, the scores for all the scorers are available in the cv_results_ dict at the keys ending with that scorer's name ('<scorer_name>') instead of '_score' shown above. ('split0_test_precision', 'mean_precision' etc.)

**best_estimator_** or dict) Estimator that was chosen by the search, i.e. estimator which gave highest score (or smallest loss if specified) on the left out data. Not available if refit=False. See refit parameter for more information on allowed values.

**best_score_** (float) Mean cross-validated score of the best_estimator For multi-metric evaluation, this is present only if refit is specified.

**best_params_** (dict) Parameter setting that gave the best results on the hold out data. For multi-metric evaluation, this is present only if refit is specified.

**best_index_** The index (of the cv_results_ arrays) which corresponds to the best candidate parameter setting. The dict at search.cv_results_['params'][search.best_index_] gives the parameter setting for the best model, that gives the highest mean score (search.best_score_). For multi-metric evaluation, this is present only if refit is specified.

**scorer_** (function or a dict) Scorer function used on the held out data to choose the best parameters for the model. For multi-metric evaluation, this attribute holds the validated scoring dict which maps the scorer key to the scorer callable.

**n_splits** (int) The number of cross-validation splits (folds/iterations).

See also:

* **ParameterGrid** generates all the combinations of a hyperparameter grid.

* **sklearn.model_selection.train_test_split** utility function to split the data into a development set usable for fitting a GridSearchCV instance and an evaluation set for its final evaluation.

* **sklearn.metrics.make_scorer** Make a scorer from a performance metric or loss function.
Notes

The parameters selected are those that maximize the score of the left out data, unless an explicit score is passed in which case it is used instead.

If `n_jobs` was set to a value higher than one, the data is copied for each point in the grid (and not `n_jobs` times). This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set `pre_dispatch`. Then, the memory is copied only `pre_dispatch` many times. A reasonable value for `pre_dispatch` is `2 * n_jobs`.

Examples

```python
>>> from sklearn import svm, datasets
>>> from sklearn.model_selection import GridSearchCV
>>> iris = datasets.load_iris()
>>> parameters = {'kernel':('linear', 'rbf'), 'C':[1, 10]}
>>> svc = svm.SVC()
>>> clf = GridSearchCV(svc, parameters)
>>> clf.fit(iris.data, iris.target)
... GridSearchCV(cv=None, error_score=..., estimator=SVC(C=1.0, cache_size=..., class_weight=..., coef0=...,
... decision_function_shape='ovr', degree=..., gamma=..., kernel='rbf', max_iter=-1, probability=False,
... random_state=None, shrinking=True, tol=...,
... verbose=False),
... fit_params=None, iid=..., n_jobs=1,
... param_grid=..., pre_dispatch=..., refit=..., return_train_score=...,
... scoring=..., verbose=...) >>> sorted(clf.cv_results_.keys()) ...
... ['mean_fit_time', 'mean_score_time', 'mean_test_score',...
... 'mean_train_score', 'param_C', 'param_kernel', 'params',...
... 'rank_test_score', 'split0_test_score',...
... 'split0_train_score', 'split1_test_score', 'split1_train_score',...
... 'split2_test_score', 'split2_train_score',...
... 'std_fit_time', 'std_score_time', 'std_test_score', 'std_train_score']
```

Methods

decision_function(X) Call decision_function on the estimator with the best found parameters.

fit(X, y, groups) Run fit with all sets of parameters.

get_params([deep]) Get parameters for this estimator.

inverse_transform(Xt) Call inverse_transform on the estimator with the best found params.

predict(X) Call predict on the estimator with the best found parameters.

predict_log_proba(X) Call predict_log_proba on the estimator with the best found parameters.

predict_proba(X) Call predict_proba on the estimator with the best found parameters.
Table 30.225 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>score(X[, y])</td>
<td>Returns the score on the given data, if the estimator has been refit.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Call transform on the estimator with the best found parameters.</td>
</tr>
</tbody>
</table>

__init__(estimator, param_grid, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', error_score='raise', return_train_score='warn')

decision_function(X)
Call decision_function on the estimator with the best found parameters.

Parameters X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

fit(X, y=None, groups=None, **fit_params)
Run fit with all sets of parameters.

Parameters X : array-like, shape = [n_samples, n_features]
Training vector, where n_samples is the number of samples and n_features is the number of features.

y : array-like, shape = [n_samples] or [n_samples, n_output], optional
Target relative to X for classification or regression; None for unsupervised learning.

groups : array-like, with shape (n_samples,), optional
Group labels for the samples used while splitting the dataset into train/test set.

**fit_params : dict of string -> object
Parameters passed to the fit method of the estimator

get_params(deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform(Xt)
Call inverse_transform on the estimator with the best found params.

Only available if the underlying estimator implements inverse_transform and refit=True.

Parameters Xt : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

predict(X)
Call predict on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports predict.
Parameters $X$ : indexable, length $n_{\text{samples}}$

Must fulfill the input assumptions of the underlying estimator.

**predict_log_proba** ($X$)

Call predict_log_proba on the estimator with the best found parameters.

Only available if $\text{refit}=\text{True}$ and the underlying estimator supports predict_log_proba.

Parameters $X$ : indexable, length $n_{\text{samples}}$

Must fulfill the input assumptions of the underlying estimator.

**predict_proba** ($X$)

Call predict_proba on the estimator with the best found parameters.

Only available if $\text{refit}=\text{True}$ and the underlying estimator supports predict_proba.

Parameters $X$ : indexable, length $n_{\text{samples}}$

Must fulfill the input assumptions of the underlying estimator.

**score** ($X$, $y$=$\text{None}$)

Returns the score on the given data, if the estimator has been refit.

This uses the score defined by $\text{scoring}$ where provided, and the $\text{best\_estimator\_\_.score}$ method otherwise.

Parameters $X$ : array-like, shape = [n_samples, n_features]

Input data, where $n_{\text{samples}}$ is the number of samples and $n_{\text{features}}$ is the number of features.

$y$ : array-like, shape = [n_samples] or [n_samples, n_output], optional

Target relative to $X$ for classification or regression; None for unsupervised learning.

Returns **score** : float

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form $\text{<component>\_\_<parameter>}$ so that it’s possible to update each component of a nested object.

Returns **self**

**transform** ($X$)

Call transform on the estimator with the best found parameters.

Only available if the underlying estimator supports transform and $\text{refit}=\text{True}$.

Parameters $X$ : indexable, length $n_{\text{samples}}$

Must fulfill the input assumptions of the underlying estimator.

Examples using sklearn.model_selection.GridSearchCV

- Concatenating multiple feature extraction methods
- Pipelining: chaining a PCA and a logistic regression
- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Comparison of kernel ridge regression and SVR
• Faces recognition example using eigenfaces and SVMs
• Feature agglomeration vs. univariate selection
• Shrinkage covariance estimation: LedoitWolf vs OAS and max-likelihood
• Model selection with Probabilistic PCA and Factor Analysis (FA)
• Cross-validation on diabetes Dataset Exercise
• Comparison of kernel ridge and Gaussian process regression
• Parameter estimation using grid search with cross-validation
• Comparing randomized search and grid search for hyperparameter estimation
• Nested versus non-nested cross-validation
• Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV
• Sample pipeline for text feature extraction and evaluation
• Kernel Density Estimation
• Scaling the regularization parameter for SVCs
• RBF SVM parameters

sklearn.model_selection.ParameterGrid

class sklearn.model_selection.ParameterGrid(param_grid)
Grid of parameters with a discrete number of values for each.
Can be used to iterate over parameter value combinations with the Python built-in function iter.
Read more in the User Guide.

Parameters

param_grid : dict of string to sequence, or sequence of such
The parameter grid to explore, as a dictionary mapping estimator parameters to sequences of allowed values.
An empty dict signifies default parameters.
A sequence of dicts signifies a sequence of grids to search, and is useful to avoid exploring parameter combinations that make no sense or have no effect. See the examples below.

See also:
GridSearchCV

Uses class:ParameterGrid to perform a full parallelized parameter search.

Examples

```python
>>> from sklearn.model_selection import ParameterGrid
>>> param_grid = {'a': [1, 2], 'b': [True, False]}
>>> list(ParameterGrid(param_grid)) == (
...     [{'a': 1, 'b': True}, {'a': 1, 'b': False},
...      {'a': 2, 'b': True}, {'a': 2, 'b': False}])
True
```
```python
grid = [{'kernel': 'linear'}, {'kernel': 'rbf', 'gamma': [1, 10]}]
list(ParameterGrid(grid)) == [{'kernel': 'linear'},
...   {'kernel': 'rbf', 'gamma': 1},
...   {'kernel': 'rbf', 'gamma': 10}]
True
ParameterGrid(grid)[1] == {'kernel': 'rbf', 'gamma': 1}
True
```

```python
def __init__(param_grid)

sklearn.model_selection.ParameterSampler

class sklearn.model_selection.ParameterSampler(param_distributions, n_iter, random_state=None)

Generator on parameters sampled from given distributions.
Non-deterministic iterable over random candidate combinations for hyper- parameter search. If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Note that before SciPy 0.16, the scipy.stats.distributions do not accept a custom RNG instance and always use the singleton RNG from numpy.random. Hence setting random_state will not guarantee a deterministic iteration whenever scipy.stats distributions are used to define the parameter search space. Deterministic behavior is however guaranteed from SciPy 0.16 onwards.

Read more in the User Guide.

Parameters

param_distributions : dict

Dictionary where the keys are parameters and values are distributions from which a parameter is to be sampled. Distributions either have to provide a rvs function to sample from them, or can be given as a list of values, where a uniform distribution is assumed.

n_iter : integer

Number of parameter settings that are produced.

random_state : int, RandomState instance or None, optional (default=None)

Pseudo random number generator state used for random uniform sampling from lists of possible values instead of scipy.stats distributions. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

Returns

params : dict of string to any

Yields dictionaries mapping each estimator parameter to as sampled value.

Examples

```python
>>> from sklearn.model_selection import ParameterSampler
>>> from scipy.stats.distributions import expon
>>> import numpy as np
>>> np.random.seed(0)
>>> param_grid = {'a':[1, 2], 'b': expon()}
```
```
>>> param_list = list(ParameterSampler(param_grid, n_iter=4))
>>> rounded_list = [{k: round(v, 6) for k, v in d.items()} for d in param_list]
>>> rounded_list == [{'b': 0.89856, 'a': 1},
...                   {'b': 0.923223, 'a': 1},
...                   {'b': 1.878964, 'a': 2},
...                   {'b': 1.038159, 'a': 2}]
True
```

```
__init__(param_distributions, n_iter, random_state=None)
```

**sklearn.model_selection.RandomizedSearchCV**

```
class sklearn.model_selection.RandomizedSearchCV (estimator, param_distributions, n_iter=10, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', random_state=None, error_score='raise', return_train_score='warn')
```

Randomized search on hyper parameters.

RandomizedSearchCV implements a “fit” and a “score” method. It also implements “predict”, “predict_proba”, “decision_function”, “transform” and “inverse_transform” if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated search over parameter settings.

In contrast to GridSearchCV, not all parameter values are tried out, but rather a fixed number of parameter settings is sampled from the specified distributions. The number of parameter settings that are tried is given by n_iter.

If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Read more in the *User Guide*.

**Parameters**

- **estimator**: estimator object.
  
  A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.

- **param_distributions**: dict
  
  Dictionary with parameters names (string) as keys and distributions or lists of parameters to try. Distributions must provide a rvs method for sampling (such as those from scipy.stats.distributions). If a list is given, it is sampled uniformly.

- **n_iter**: int, default=10
  
  Number of parameter settings that are sampled. n_iter trades off runtime vs quality of the solution.

- **scoring**: string, callable, list/tuple, dict or None, default: None
  
  A single string (see *The scoring parameter: defining model evaluation rules*) or a callable (see *Defining your scoring strategy from metric functions*) to evaluate the predictions on the test set.
For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See *Specifying multiple metrics for evaluation* for an example.

If None, the estimator's default scorer (if available) is used.

**fit_params**: dict, optional

Parameters to pass to the fit method.

Deprecated since version 0.19: *fit_params* as a constructor argument was deprecated in version 0.19 and will be removed in version 0.21. Pass fit parameters to the *fit* method instead.

**n_jobs**: int, default=1

Number of jobs to run in parallel.

**pre_dispatch**: int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

- None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of n_jobs, as in ’2*n_jobs’

**iid**: boolean, default=True

If True, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds.

**cv**: int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross validation,
- integer, to specify the number of folds in a (Stratified)KFold,
- An object to be used as a cross-validation generator.
- An iterable yielding train, test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer *User Guide* for the various cross-validation strategies that can be used here.

**refit**: boolean, or string default=True

Refit an estimator using the best found parameters on the whole dataset.

For multiple metric evaluation, this needs to be a string denoting the scorer that would be used to find the best parameters for refitting the estimator at the end.
The refitted estimator is made available at the `best_estimator_` attribute and permits using `predict` directly on this `RandomizedSearchCV` instance.

Also for multiple metric evaluation, the attributes `best_index_`, `best_score_` and `best_parameters_` will only be available if `refit` is set and all of them will be determined w.r.t this specific scorer.

See `scoring` parameter to know more about multiple metric evaluation.

**verbose** : integer

Controls the verbosity: the higher, the more messages.

**random_state** : int, RandomState instance or None, optional, default=None

Pseudo random number generator state used for random uniform sampling from lists of possible values instead of scipy.stats distributions. If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**error_score** : 'raise' (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to 'raise', the error is raised. If a numeric value is given, `FitFailedWarning` is raised. This parameter does not affect the refit step, which will always raise the error.

**return_train_score** : boolean, optional

If False, the `cv_results_` attribute will not include training scores.

Current default is 'warn', which behaves as True in addition to raising a warning when a training score is looked up. That default will be changed to False in 0.21. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.
cv_results_ of numpy (masked) ndarrays) A dict with keys as column headers and values as columns, that can be imported into a pandas DataFrame. For instance the below given table

<table>
<thead>
<tr>
<th>param_kernel</th>
<th>param_gamma</th>
<th>split0_test_score</th>
<th>...</th>
<th>rank_test_score</th>
</tr>
</thead>
<tbody>
<tr>
<td>'rbf'</td>
<td>0.1</td>
<td>0.8</td>
<td>...</td>
<td>2</td>
</tr>
<tr>
<td>'rbf'</td>
<td>0.2</td>
<td>0.9</td>
<td>...</td>
<td>1</td>
</tr>
</tbody>
</table>

will be represented by a cv_results_dict of:

```python
{ 'param_kernel': masked_array(data = ['rbf', 'rbf', 'rbf'], mask = False),
 'param_gamma': masked_array(data = [0.1, 0.2, 0.3], mask = False),
 'split0_test_score': [0.8, 0.9, 0.7],
 'split1_test_score': [0.82, 0.5, 0.7],
 'mean_test_score': [0.81, 0.7, 0.7],
 'std_test_score': [0.02, 0.03, 0.04],
 'mean_fit_time': [0.73, 0.63, 0.43, 0.49],
 'std_fit_time': [0.01, 0.02, 0.01, 0.01],
 'mean_score_time': [0.007, 0.06, 0.04, 0.04],
 'std_score_time': [0.001, 0.002, 0.003, 0.005],
 'params': [{'kernel': 'rbf', 'gamma': 0.1}, ...]}
```

NOTE The key 'params' is used to store a list of parameter settings dicts for all the parameter candidates. The mean_fit_time, std_fit_time, mean_score_time and std_score_time are all in seconds. For multi-metric evaluation, the scores for all the scorers are available in the cv_results_dict at the keys ending with that scorer's name ('_<scorer_name>') instead of '_score' shown above. ('split0_test_precision', 'mean_train_precision' etc.)

best_estimator_ (or dict) Estimator that was chosen by the search, i.e. estimator which gave highest score (or smallest loss if specified) on the left out data. Not available if refit=False. For multi-metric evaluation, this attribute is present only if refit is specified. See refit parameter for more information on allowed values.

best_score_ (float) Mean cross-validated score of the best_estimator. For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

best_params_ (dict) Parameter setting that gave the best results on the hold out data. For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

best_index_ The index (of the cv_results_ arrays) which corresponds to the best candidate parameter setting. The dict at search.cv_results_['params'][search.best_index_] gives the parameter setting for the best model, that gives the highest mean score (search.best_score_). For multi-metric evaluation, this is not available if refit is False. See refit parameter for more information.

scorer_ (function or a dict) Scorer function used on the held out data to choose the best parameters for the model. For multi-metric evaluation, this attribute holds the validated scoring dict which maps the scorer key to the scorer callable.

n_splits_ (int) The number of cross-validation splits (folds/iterations).

See also:

- GridSearchCV Does exhaustive search over a grid of parameters.
- ParameterSampler A generator over parameter settings, constructed from param_distributions.

Notes

The parameters selected are those that maximize the score of the held-out data, according to the scoring parameter.
If `n_jobs` was set to a value higher than one, the data is copied for each parameter setting (and not `n_jobs` times). This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set `pre_dispatch`. Then, the memory is copied only `pre_dispatch` many times. A reasonable value for `pre_dispatch` is `2 * n_jobs`.

### Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>decision_function(X)</code></td>
<td>Call decision_function on the estimator with the best found parameters.</td>
</tr>
<tr>
<td><code>fit(X[, y, groups])</code></td>
<td>Run fit with all sets of parameters.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>inverse_transform(Xt)</code></td>
<td>Call inverse_transform on the estimator with the best found params.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Call predict on the estimator with the best found parameters.</td>
</tr>
<tr>
<td><code>predict_log_proba(X)</code></td>
<td>Call predict_log_proba on the estimator with the best found parameters.</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Call predict_proba on the estimator with the best found parameters.</td>
</tr>
<tr>
<td><code>score(X[, y])</code></td>
<td>Returns the score on the given data, if the estimator has been refit.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Call transform on the estimator with the best found parameters.</td>
</tr>
</tbody>
</table>

```python
__init__ (estimator, param_distributions, n_iter=10, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', random_state=None, error_score='raise', return_train_score='warn')
```

**decision_function(X)**
Call decision_function on the estimator with the best found parameters.

Only available if `refit=True` and the underlying estimator supports `decision_function`.

**Parameters**
- **X**: indexable, length n_samples
  - Must fulfill the input assumptions of the underlying estimator.

**fit(X, y=None, groups=None, **fit_params)**
Run fit with all sets of parameters.

**Parameters**
- **X**: array-like, shape = [n_samples, n_features]
  - Training vector, where n_samples is the number of samples and n_features is the number of features.
- **y**: array-like, shape = [n_samples] or [n_samples, n_output], optional
  - Target relative to X for classification or regression; None for unsupervised learning.
- **groups**: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.
- **fit_params**: dict of string -> object
  - Parameters passed to the fit method of the estimator.
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform (Xt)
Call inverse_transform on the estimator with the best found params.
Only available if the underlying estimator implements inverse_transform and refit=True.

Parameters Xt : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

predict (X)
Call predict on the estimator with the best found parameters.
Only available if refit=True and the underlying estimator supports predict.

Parameters X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

predict_log_proba (X)
Call predict_log_proba on the estimator with the best found parameters.
Only available if refit=True and the underlying estimator supports predict_log_proba.

Parameters X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

predict_proba (X)
Call predict_proba on the estimator with the best found parameters.
Only available if refit=True and the underlying estimator supports predict_proba.

Parameters X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

score (X, y=None)
Returns the score on the given data, if the estimator has been refit.
This uses the score defined by scoring where provided, and the best_estimator_.score method otherwise.

Parameters X : array-like, shape = [n_samples, n_features]
Input data, where n_samples is the number of samples and n_features is the number of features.
y : array-like, shape = [n_samples] or [n_samples, n_output], optional
Target relative to X for classification or regression; None for unsupervised learning.

Returns score : float

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**transform** *(X)*

Call transform on the estimator with the best found parameters.

Only available if the underlying estimator supports `transform` and `refit=True`.

**Parameters** *X* : indexable, length `n_samples`

Must fulfill the input assumptions of the underlying estimator.

**Examples using sklearn.model_selection.RandomizedSearchCV**

- Comparing randomized search and grid search for hyperparameter estimation

```
model_selection.fit_grid_point(X, y, ...[, ...])
```

**sklearn.model_selection.fit_grid_point**

```
sklearn.model_selection.fit_grid_point(X, y, estimator, parameters, train, test, scorer, verbose, error_score='raise', **fit_params)
```

Run fit on one set of parameters.

**Parameters** *X* : array-like, sparse matrix or list

Input data.

*y* : array-like or None

Targets for input data.

**estimator** : estimator object

A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a `score` function, or `scoring` must be passed.

**parameters** : dict

Parameters to be set on estimator for this grid point.

**train** : ndarray, dtype int or bool

Boolean mask or indices for training set.

**test** : ndarray, dtype int or bool

Boolean mask or indices for test set.

**scorer** : callable or None

The scorer callable object / function must have its signature as `scorer(estimator, X, y)`.

If None the estimator’s default scorer is used.

**verbose** : int
Verbosity level.

**fit_params**: kwargs

Additional parameter passed to the fit function of the estimator.

**error_score**: ‘raise’ (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error.

Returns **score**: float

Score of this parameter setting on given training / test split.

**parameters**: dict

The parameters that have been evaluated.

**n_samples_test**: int

Number of test samples in this split.

### 30.23.4 Model validation

<table>
<thead>
<tr>
<th>Function/Docstring</th>
<th>Description</th>
</tr>
</thead>
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<tr>
<td><code>sklearn.model_selection.cross_validate(estimator, X)</code></td>
<td>Evaluate metric(s) by cross-validation and also record fit/score times.</td>
</tr>
<tr>
<td><code>sklearn.model_selection.cross_val_predict(estimator, X)</code></td>
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<td>Validation curve.</td>
</tr>
</tbody>
</table>

Evaluate metric(s) by cross-validation and also record fit/score times.


**Parameters** **estimator**: estimator object implementing ‘fit’

The object to use to fit the data.

**X**: array-like

The data to fit. Can be for example a list, or an array.

**y**: array-like, optional, default: None

The target variable to try to predict in the case of supervised learning.
groups : array-like, with shape (n_samples,), optional

Group labels for the samples used while splitting the dataset into train/test set.

scoring : string, callable, list/tuple, dict or None, default: None

A single string (see The scoring parameter: defining model evaluation rules) or a callable (see Defining your scoring strategy from metric functions) to evaluate the predictions on the test set.

For evaluating multiple metrics, either give a list of (unique) strings or a dict with names as keys and callables as values.

NOTE that when using custom scorers, each scorer should return a single value. Metric functions returning a list/array of values can be wrapped into multiple scorers that return one value each.

See Specifying multiple metrics for evaluation for an example.

If None, the estimator’s default scorer (if available) is used.

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

• None, to use the default 3-fold cross validation,
• integer, to specify the number of folds in a (Stratified)KFold,
• An object to be used as a cross-validation generator.
• An iterable yielding train, test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

n_jobs : integer, optional

The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

verbose : integer, optional

The verbosity level.

fit_params : dict, optional

Parameters to pass to the fit method of the estimator.

pre_dispatch : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

• None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
• An int, giving the exact number of total jobs that are spawned
• A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

return_train_score : boolean, optional
Whether to include train scores.

Current default is 'warn', which behaves as True in addition to raising a warning when a training score is looked up. That default will be changed to False in 0.21. Computing training scores is used to get insights on how different parameter settings impact the overfitting/underfitting trade-off. However computing the scores on the training set can be computationally expensive and is not strictly required to select the parameters that yield the best generalization performance.

Returns scores : dict of float arrays of shape=(n_splits,)

Array of scores of the estimator for each run of the cross validation.

A dict of arrays containing the score/time arrays for each scorer is returned. The possible keys for this dict are:

test_score The score array for test scores on each cv split.

train_score The score array for train scores on each cv split. This is available only if return_train_score parameter is True.

fit_time The time for fitting the estimator on the train set for each cv split.

score_time The time for scoring the estimator on the test set for each cv split. (Note time for scoring on the train set is not included even if return_train_score is set to True

See also:

sklearn.model_selection.cross_val_score Run cross-validation for single metric evaluation.
sklearn.metrics.make_scorer Make a scorer from a performance metric or loss function.

Examples

```python
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_validate
>>> from sklearn.metrics import confusion_matrix
>>> from sklearn.svm import LinearSVC
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()

Single metric evaluation using cross_validate

```python
>>> cv_results = cross_validate(lasso, X, y, return_train_score=False)
>>> sorted(cv_results.keys())
['fit_time', 'score_time', 'test_score']
>>> cv_results['test_score']
array([ 0.33..., 0.08..., 0.03...])
```

Multiple metric evaluation using cross_validate (please refer the scoring parameter doc for more information)

```python
>>> scores = cross_validate(lasso, X, y, ... scoring=('r2', 'neg_mean_squared_error'))
>>> print(scores['test_neg_mean_squared_error'])
```
```python
>>> print(scores['train_r2'])
[ 0.28... 0.39... 0.22...]
```

```python
sklearn.model_selection.cross_val_predict
```

The function `cross_val_predict` generates cross-validated estimates for each input data point. Read more in the User Guide.

**Parameters**

- `estimator`: estimator object implementing ‘fit’ and ‘predict’
  - The object to use to fit the data.
- `X`: array-like
  - The data to fit. Can be, for example a list, or an array at least 2d.
- `y`: array-like, optional, default: None
  - The target variable to try to predict in the case of supervised learning.
- `groups`: array-like, with shape (n_samples,), optional
  - Group labels for the samples used while splitting the dataset into train/test set.
- `cv`: int, cross-validation generator or an iterable, optional
  - Determines the cross-validation splitting strategy. Possible inputs for cv are:
    - None, to use the default 3-fold cross validation,
    - integer, to specify the number of folds in a (Stratified)KFold,
    - An object to be used as a cross-validation generator.
    - An iterable yielding train, test splits.
  - For integer/None inputs, if the estimator is a classifier and `y` is either binary or multi-class, `StratifiedKFold` is used. In all other cases, `KFold` is used.
- `n_jobs`: integer, optional
  - The number of CPUs to use to do the computation. -1 means ‘all CPUs’.
- `verbose`: integer, optional
  - The verbosity level.
- `fit_params`: dict, optional
  - Parameters to pass to the fit method of the estimator.
- `pre_dispatch`: int, or string, optional
  - Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
• None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
• An int, giving the exact number of total jobs that are spawned
• A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

**method**: string, optional, default: ‘predict’

Invokes the passed method name of the passed estimator. For method=’predict_proba’, the columns correspond to the classes in sorted order.

**Returns** predictions : ndarray

This is the result of calling method

**Notes**

In the case that one or more classes are absent in a training portion, a default score needs to be assigned to all instances for that class if method produces columns per class, as in {‘decision_function’, ‘predict_proba’, ‘predict_log_proba’}. For predict_proba this value is 0. In order to ensure finite output, we approximate negative infinity by the minimum finite float value for the dtype in other cases.

**Examples**

```python
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_val_predict
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> y_pred = cross_val_predict(lasso, X, y)
```

**Examples using sklearn.model_selection.cros_val_predict**

• **Plotting Cross-Validated Predictions**

**sklearn.model_selection.cros_val_score**

```python
sklearn.model_selection.cros_val_score(estimator, X, y=None, groups=None, scoring=None, cv=None, n_jobs=1, verbose=0, fit_params=None, pre_dispatch='2*n_jobs')
```

Evaluate a score by cross-validation

Read more in the **User Guide**.

**Parameters** estimator : estimator object implementing ‘fit’

The object to use to fit the data.

X : array-like

The data to fit. Can be for example a list, or an array.

y : array-like, optional, default: None
The target variable to try to predict in the case of supervised learning.

groups : array-like, with shape (n_samples,), optional
   Group labels for the samples used while splitting the dataset into train/test set.

scoring : string, callable or None, optional, default: None
   A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

cv : int, cross-validation generator or an iterable, optional
   Determines the cross-validation splitting strategy. Possible inputs for cv are:
   • None, to use the default 3-fold cross validation,
   • integer, to specify the number of folds in a (Stratified)KFold,
   • An object to be used as a cross-validation generator.
   • An iterable yielding train, test splits.
   For integer/None inputs, if the estimator is a classifier and y is either binary or multi-class, StratifiedKFold is used. In all other cases, KFold is used.
   Refer User Guide for the various cross-validation strategies that can be used here.

n_jobs : integer, optional
   The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

verbose : integer, optional
   The verbosity level.

fit_params : dict, optional
   Parameters to pass to the fit method of the estimator.

pre_dispatch : int, or string, optional
   Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
   • None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
   • An int, giving the exact number of total jobs that are spawned
   • A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

Returns scores : array of float, shape=(len(list(cv)),)
   Array of scores of the estimator for each run of the cross validation.

See also:

sklearn.model_selection.cross_validate To run cross-validation on multiple metrics and also to return train scores, fit times and score times.

sklearn.metrics.make_scorer Make a scorer from a performance metric or loss function.
Examples

```python
>>> from sklearn import datasets, linear_model
>>> from sklearn.model_selection import cross_val_score

>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> print(cross_val_score(lasso, X, y))
[0.33150734 0.08022311 0.03531764]
```

Examples using `sklearn.model_selection.cross_val_score`

- **Imputing missing values before building an estimator**
- **Model selection with Probabilistic PCA and Factor Analysis (FA)**
- **Cross-validation on Digits Dataset Exercise**
- **Underfitting vs. Overfitting**
- **Nested versus non-nested cross-validation**
- **SVM-Anova: SVM with univariate feature selection**

`sklearn.model_selection.learning_curve`

`sklearn.model_selection.learning_curve` determines cross-validated training and test scores for different training set sizes.

A cross-validation generator splits the whole dataset k times in training and test data. Subsets of the training set with varying sizes will be used to train the estimator and a score for each training subset size and the test set will be computed. Afterwards, the scores will be averaged over all k runs for each training subset size.

Read more in the [User Guide](#).

**Parameters**

- **estimator**: object type that implements the “fit” and “predict” methods
  
  An object of that type which is cloned for each validation.

- **X**: array-like, shape (n_samples, n_features)
  
  Training vector, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, shape (n_samples) or (n_samples, n_features), optional
  
  Target relative to X for classification or regression; None for unsupervised learning.

- **groups**: array-like, with shape (n_samples,), optional
  
  Group labels for the samples used while splitting the dataset into train/test set.

- **train_sizes**: array-like, shape (n_ticks,), dtype float or int
  
  Specifies the percentages orabsolute numbers of training set splits (where n_samples is the number of samples). For example, for 200 samples, [0.1, 0.325, 0.55, 0.775, 1.] would split into 5 sets: 20, 67, 110, 145, 200.
Relative or absolute numbers of training examples that will be used to generate the learning curve. If the dtype is float, it is regarded as a fraction of the maximum size of the training set (that is determined by the selected validation method), i.e. it has to be within (0, 1]. Otherwise it is interpreted as absolute sizes of the training sets. Note that for classification the number of samples usually have to be big enough to contain at least one sample from each class. (default: np.linspace(0.1, 1.0, 5))

**cv**: int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross validation,
- integer, to specify the number of folds in a (Stratified)KFold,
- An object to be used as a cross-validation generator.
- An iterable yielding train, test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multi-class, StratifiedKFold is used. In all other cases, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**scoring**: string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

**exploit_incremental_learning**: boolean, optional, default: False

If the estimator supports incremental learning, this will be used to speed up fitting for different training set sizes.

**n_jobs**: integer, optional

Number of jobs to run in parallel (default 1).

**pre_dispatch**: integer or string, optional

Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like ‘2*n_jobs’.

**verbose**: integer, optional

Controls the verbosity: the higher, the more messages.

**shuffle**: boolean, optional

Whether to shuffle training data before taking prefixes of it based on ‘train_sizes’.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle is True.

**Returns**

**train_sizes_abs**: array, shape = (n_unique_ticks,), dtype int

Numbers of training examples that has been used to generate the learning curve. Note that the number of ticks might be less than n_ticks because duplicate entries will be removed.

**train_scores**: array, shape (n_ticks, n_cv_folds)

Scores on training sets.
**test_scores**: array, shape (n_ticks, n_cv_folds)

Scores on test set.

**Notes**

See [examples/model_selection/plot_learning_curve.py](https://example.com)

**Examples using** `sklearn.model_selection.learning_curve`

- Comparison of kernel ridge regression and SVR
- Plotting Learning Curves

`sklearn.model_selection.permutation_test_score`

`sklearn.model_selection.permutation_test_score` *(estimator, X, y, groups=None, cv=None, n_permutations=100, n_jobs=1, random_state=0, verbose=0, scoring=None)*

Evaluate the significance of a cross-validated score with permutations

Read more in the [User Guide](https://example.com).

**Parameters**

- **estimator**: estimator object implementing 'fit'
  
  The object to use to fit the data.

- **X**: array-like of shape at least 2D
  
  The data to fit.

- **y**: array-like
  
  The target variable to try to predict in the case of supervised learning.

- **groups**: array-like, with shape (n_samples,), optional
  
  Labels to constrain permutation within groups, i.e. y values are permuted among samples with the same group identifier. When not specified, y values are permuted among all samples.

  When a grouped cross-validator is used, the group labels are also passed on to the split method of the cross-validator. The cross-validator uses them for grouping the samples while splitting the dataset into train/test set.

- **scoring**: string, callable or None, optional, default: None
  
  A single string (see [The scoring parameter: defining model evaluation rules](https://example.com)) or a callable (see [Defining your scoring strategy from metric functions](https://example.com)) to evaluate the predictions on the test set.

  If None the estimator’s default scorer, if available, is used.

- **cv**: int, cross-validation generator or an iterable, optional
  
  Determines the cross-validation splitting strategy. Possible inputs for cv are:

  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a *(Stratified)*KFold,
• An object to be used as a cross-validation generator.
• An iterable yielding train, test splits.

For integer/None inputs, if the estimator is a classifier and $y$ is either binary or multi-class, `StratifiedKFold` is used. In all other cases, `KFold` is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**n_permutations** : integer, optional

Number of times to permute $y$.

**n_jobs** : integer, optional

The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

**random_state** : int, RandomState instance or None, optional (default=0)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**verbose** : integer, optional

The verbosity level.

**Returns**

score : float

The true score without permuting targets.

permutation_scores : array, shape (n_permutations,)

The scores obtained for each permutations.

pvalue : float

The p-value, which approximates the probability that the score would be obtained by chance. This is calculated as:

$$(C + 1) / (n_{\text{permutations}} + 1)$$

Where $C$ is the number of permutations whose score $\geq$ the true score.

The best possible p-value is $1 / (n_{\text{permutations}} + 1)$, the worst is 1.0.

**Notes**

This function implements Test 1 in:


**Examples using sklearn.model_selection.permutation_test_score**

• Test with permutations the significance of a classification score
sklearn.model_selection.validation_curve

**sklearn.model_selection.validation_curve**

Validation curve.

Determine training and test scores for varying parameter values.

Compute scores for an estimator with different values of a specified parameter. This is similar to grid search with one parameter. However, this will also compute training scores and is merely a utility for plotting the results.


**Parameters**

- **estimator**: object type that implements the “fit” and “predict” methods
  
  An object of that type which is cloned for each validation.

- **X**: array-like, shape (n_samples, n_features)
  
  Training vector, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, shape (n_samples) or (n_samples, n_features), optional
  
  Target relative to X for classification or regression; None for unsupervised learning.

- **param_name**: string
  
  Name of the parameter that will be varied.

- **param_range**: array-like, shape (n_values,)
  
  The values of the parameter that will be evaluated.

- **groups**: array-like, with shape (n_samples,), optional
  
  Group labels for the samples used while splitting the dataset into train/test set.

- **cv**: int, cross-validation generator or an iterable, optional
  
  Determines the cross-validation splitting strategy. Possible inputs for cv are:
  
  - None, to use the default 3-fold cross validation,
  - integer, to specify the number of folds in a (Stratified)KFold,
  - An object to be used as a cross-validation generator.
  - An iterable yielding train, test splits.
  
  For integer/None inputs, if the estimator is a classifier and y is either binary or multi-class, StratifiedKFold is used. In all other cases, KFold is used.
  
  Refer [User Guide](https://scikit-learn.org/stable/user_guide.html) for the various cross-validation strategies that can be used here.

- **scoring**: string, callable or None, optional, default: None
  
  A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

- **n_jobs**: integer, optional
  
  Number of jobs to run in parallel (default 1).

- **pre_dispatch**: integer or string, optional
Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like ‘2*n_jobs’.

`verbose` : integer, optional

Controls the verbosity: the higher, the more messages.

Returns `train_scores` : array, shape (n_ticks, n_cv_folds)

Scores on training sets.

`test_scores` : array, shape (n_ticks, n_cv_folds)

Scores on test set.

Notes

See *Plotting Validation Curves*

Examples using `sklearn.model_selection.validation_curve`

- *Plotting Validation Curves*

### 30.24 `sklearn.multiclass`: Multiclass and multilabel classification

#### 30.24.1 Multiclass and multilabel classification strategies

This module implements multiclass learning algorithms:

- one-vs-the-rest / one-vs-all
- one-vs-one
- error correcting output codes

The estimators provided in this module are meta-estimators: they require a base estimator to be provided in their constructor. For example, it is possible to use these estimators to turn a binary classifier or a regressor into a multiclass classifier. It is also possible to use these estimators with multiclass estimators in the hope that their accuracy or runtime performance improves.

All classifiers in scikit-learn implement multiclass classification; you only need to use this module if you want to experiment with custom multiclass strategies.

The one-vs-the-rest meta-classifier also implements a `predict_proba` method, so long as such a method is implemented by the base classifier. This method returns probabilities of class membership in both the single label and multilabel case. Note that in the multilabel case, probabilities are the marginal probability that a given sample falls in the given class. As such, in the multilabel case the sum of these probabilities over all possible labels for a given sample will not sum to unity, as they do in the single label case.

User guide: See the *Multiclass and multilabel algorithms* section for further details.

```python
multiclass.OneVsRestClassifier(estimator[, ...])
```

Continued on next page
Table 30.229 – continued from previous page

| sklearn.multiclass.OneVsOneClassifier(estimator[, ...]) | One-vs-one multiclass strategy |
| sklearn.multiclass.OutputCodeClassifier(estimator[, ...]) | (Error-Correcting) Output-Code multiclass strategy |

### 30.24.2 sklearn.multiclass.OneVsRestClassifier

**class** sklearn.multiclass.OneVsRestClassifier (estimator, n_jobs=1)

One-vs-the-rest (OvR) multiclass/multilabel strategy

Also known as one-vs-all, this strategy consists in fitting one classifier per class. For each classifier, the class is fitted against all the other classes. In addition to its computational efficiency (only n_classes classifiers are needed), one advantage of this approach is its interpretability. Since each class is represented by one and one classifier only, it is possible to gain knowledge about the class by inspecting its corresponding classifier. This is the most commonly used strategy for multiclass classification and is a fair default choice.

This strategy can also be used for multilabel learning, where a classifier is used to predict multiple labels for instance, by fitting on a 2-d matrix in which cell [i, j] is 1 if sample i has label j and 0 otherwise.

In the multilabel learning literature, OvR is also known as the binary relevance method.

Read more in the [User Guide](#).

**Parameters**

- **estimator** : estimator object
  An estimator object implementing `fit` and one of `decision_function` or `predict_proba`.

- **n_jobs** : int, optional, default: 1
  The number of jobs to use for the computation. If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.

**Attributes**

- **multilabel_**
  Whether this is a multilabel classifier

- **estimators_**
  (list of n_classes estimators) Estimators used for predictions.

- **classes_**
  (array, shape = [n_classes]) Class labels.

- **label_binarizer_**
  (LabelBinarizer object) Object used to transform multiclass labels to binary labels and vice-versa.

**Methods**

- **decision_function(X)**
  Returns the distance of each sample from the decision boundary for each class.

- **fit(X, y)**
  Fit underlying estimators.

- **get_params([deep])**
  Get parameters for this estimator.

- **partial_fit(X, y[, classes])**
  Partially fit underlying estimators

- **predict(X)**
  Predict multi-class targets using underlying estimators.

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<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tr>
<td>predict_proba</td>
<td>Probability estimates.</td>
</tr>
<tr>
<td>score</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__(estimator, n_jobs=1)
```

**decision_function** *(X)*

Returns the distance of each sample from the decision boundary for each class. This can only be used with estimators which implement the decision_function method.

- **Parameters**
  - `X`: array-like, shape = [n_samples, n_features]

- **Returns**
  - `T`: array-like, shape = [n_samples, n_classes]

```python
fit(X, y)
```

Fit underlying estimators.

- **Parameters**
  - `X`: (sparse) array-like, shape = [n_samples, n_features]
    - Data.
  - `y`: (sparse) array-like, shape = [n_samples, ], [n_samples, n_classes]
    - Multi-class targets. An indicator matrix turns on multilabel classification.

- **Returns**
  - `self`

```python
get_params(deep=True)
```

Get parameters for this estimator.

- **Parameters**
  - `deep`: boolean, optional
    - If True, will return the parameters for this estimator and contained subobjects that are estimators.

- **Returns**
  - `params`: mapping of string to any
    - Parameter names mapped to their values.

```python
multilabel_
```

Whether this is a multilabel classifier

```python
partial_fit(X, y, classes=None)
```

Partially fit underlying estimators

Should be used when memory is inefficient to train all data. Chunks of data can be passed in several iteration.

- **Parameters**
  - `X`: (sparse) array-like, shape = [n_samples, n_features]
    - Data.
  - `y`: (sparse) array-like, shape = [n_samples, ], [n_samples, n_classes]
    - Multi-class targets. An indicator matrix turns on multilabel classification.
  - `classes`: array, shape (n_classes, )
    - Classes across all calls to partial_fit. Can be obtained via `np.unique(y_all)`, where `y_all` is the target vector of the entire dataset. This argument is only required in the first call of partial_fit and can be omitted in the subsequent calls.

- **Returns**
  - `self`
**predict** (*X*)

Predict multi-class targets using underlying estimators.

**Parameters**

- **X**: (sparse) array-like, shape = [n_samples, n_features]
  Data.

**Returns**

- **y**: (sparse) array-like, shape = [n_samples, ], [n_samples, n_classes].
  Predicted multi-class targets.

**predict_proba** (*X*)

Probability estimates.

The returned estimates for all classes are ordered by label of classes.

Note that in the multilabel case, each sample can have any number of labels. This returns the marginal probability that the given sample has the label in question. For example, it is entirely consistent that two labels both have a 90% probability of applying to a given sample.

In the single label multiclass case, the rows of the returned matrix sum to 1.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]

**Returns**

- **T**: (sparse) array-like, shape = [n_samples, n_classes]
  Returns the probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`.

**score** (*X*, *y*, *sample_weight=None*)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)

- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)

- **sample_weight**: array-like, shape = [n_samples], optional

**Returns**

- **score**: float
  Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

**self**

**Examples using sklearn.multiclass.OneVsRestClassifier**

- *Multilabel classification*
- *Receiver Operating Characteristic (ROC)*
30.24.3 sklearn.multiclass.OneVsOneClassifier

class sklearn.multiclass.OneVsOneClassifier (estimator, n_jobs=1)
One-vs-one multiclass strategy

This strategy consists in fitting one classifier per class pair. At prediction time, the class which received
the most votes is selected. Since it requires to fit \( n_{\text{classes}} \times (n_{\text{classes}} - 1) / 2 \) classifiers, this method is usually
slower than one-vs-the-rest, due to its \( O(n_{\text{classes}}^2) \) complexity. However, this method may be advantageous
for algorithms such as kernel algorithms which don’t scale well with \( n_{\text{samples}} \). This is because each individual
learning problem only involves a small subset of the data whereas, with one-vs-the-rest, the complete dataset is
used \( n_{\text{classes}} \) times.

Read more in the User Guide.

Parameters

- **estimator**: estimator object
  An estimator object implementing `fit` and one of `decision_function` or `predict_proba`.

- **n_jobs**: int, optional, default: 1
  The number of jobs to use for the computation. If -1 all CPUs are used. If 1 is given, no
  parallel computing code is used at all, which is useful for debugging. For n_jobs below
  -1, \((n_{\text{cpus}} + 1 + n_{\text{jobs}})\) are used. Thus for n_jobs = -2, all CPUs but one are used.

Attributes

- `estimators_` (list of \( n_{\text{classes}} \times (n_{\text{classes}} - 1) / 2 \) estimators) Estimators used for predictions.
- `classes_` (numpy array of shape \([n_{\text{classes}}]\)) Array containing labels.

Methods

- `decision_function(X)`: Decision function for the OneVsOneClassifier.
- `fit(X, y)`: Fit underlying estimators.
- `get_params([deep])`: Get parameters for this estimator.
- `partial_fit(X, y[, classes])`: Partially fit underlying estimators.
- `predict(X)`: Estimate the best class label for each sample in X.
- `score(X, y[, sample_weight])`: Returns the mean accuracy on the given test data and labels.
- `set_params(**params)`: Set the parameters of this estimator.

__init__ (estimator, n_jobs=1)

decision_function(X)

Decision function for the OneVsOneClassifier.

The decision values for the samples are computed by adding the normalized sum of pair-wise classification
confidence levels to the votes in order to disambiguate between the decision values when the votes for all
the classes are equal leading to a tie.

Parameters

- **X**: array-like, shape = \([n_{\text{samples}}, n_{\text{features}}]\)
Returns $Y$: array-like, shape = [n_samples, n_classes]

```python
fit(X, y)
```
Fit underlying estimators.

Parameters $X$: (sparse) array-like, shape = [n_samples, n_features]
Data.

$y$: array-like, shape = [n_samples]
Multi-class targets.

Returns self

```python
get_params(deep=True)
```
Get parameters for this estimator.

Parameters deep: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any
Parameter names mapped to their values.

```python
partial_fit(X, y, classes=None)
```
Partially fit underlying estimators
Should be used when memory is inefficient to train all data. Chunks of data can be passed in several iteration, where the first call should have an array of all target variables.

Parameters $X$: (sparse) array-like, shape = [n_samples, n_features]
Data.

$y$: array-like, shape = [n_samples]
Multi-class targets.

classes: array, shape (n_classes, )
Classes across all calls to partial_fit. Can be obtained via `np.unique(y_all)`, where $y_{all}$ is the target vector of the entire dataset. This argument is only required in the first call of partial_fit and can be omitted in the subsequent calls.

Returns self

```python
predict(X)
```
Estimate the best class label for each sample in $X$.

This is implemented as `argmax(decision_function(X), axis=1)` which will return the label of the class with most votes by estimators predicting the outcome of a decision for each possible class pair.

Parameters $X$: (sparse) array-like, shape = [n_samples, n_features]
Data.

Returns $y$: numpy array of shape [n_samples]
Predicted multi-class targets.

```python
score(X, y, sample_weight=None)
```
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.
**Parameters** X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

**Returns** score : float

Mean accuracy of self.predict(X) wrt. y.

set_params (**params)**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

30.24.4 sklearn.multiclass.OutputCodeClassifier

class sklearn.multiclass.OutputCodeClassifier(*estimator, code_size=1.5, random_state=None, n_jobs=1)*

(Error-Correcting) Output-Code multiclass strategy

Output-code based strategies consist in representing each class with a binary code (an array of 0s and 1s). At fitting time, one binary classifier per bit in the code book is fitted. At prediction time, the classifiers are used to project new points in the class space and the class closest to the points is chosen. The main advantage of these strategies is that the number of classifiers used can be controlled by the user, either for compressing the model (0 < code_size < 1) or for making the model more robust to errors (code_size > 1). See the documentation for more details.

Read more in the User Guide.

**Parameters** estimator : estimator object

An estimator object implementing `fit` and one of `decision_function` or `predict_proba`.

code_size : float

Percentage of the number of classes to be used to create the code book. A number between 0 and 1 will require fewer classifiers than one-vs-the-rest. A number greater than 1 will require more classifiers than one-vs-the-rest.

random_state : int, RandomState instance or None, optional, default: None

The generator used to initialize the codebook. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

n_jobs : int, optional, default: 1

The number of jobs to use for the computation. If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpu + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used.
Attributes

- **estimators_** *(list of int(n_classes * code_size) estimators)*: Estimators used for predictions.
- **classes_** *(numpy array of shape [n_classes]*)*: Array containing labels.
- **code_book_** *(numpy array of shape [n_classes, code_size]*)*: Binary array containing the code of each class.

References

[R555557], [R556557], [R557557]

Methods

- **fit(X, y)**: Fit underlying estimators.
- **get_params([deep])**: Get parameters for this estimator.
- **predict(X)**: Predict multi-class targets using underlying estimators.
- **score(X, y[, sample_weight])**: Returns the mean accuracy on the given test data and labels.
- **set_params(**params)**: Set the parameters of this estimator.

**__init__**(estimator, code_size=1.5, random_state=None, n_jobs=1)

**fit**(X, y)

Fit underlying estimators.

**Parameters**

- **X**: (sparse) array-like, shape = [n_samples, n_features]
  Data.
- **y**: numpy array of shape [n_samples]
  Multi-class targets.

**Returns**

- **self**

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**predict**(X)

Predict multi-class targets using underlying estimators.

**Parameters**

- **X**: (sparse) array-like, shape = [n_samples, n_features]
  Data.

**Returns**

- **y**: numpy array of shape [n_samples]
  Predicted multi-class targets.
**score** *(X, y, **sample_weight=None]*)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- **score**: float
  Mean accuracy of self.predict(X) wrt. y.

**set_params** *(**params]*)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

---

### 30.25 sklearn.multioutput: Multioutput regression and classification

This module implements multioutput regression and classification.

The estimators provided in this module are meta-estimators: they require a base estimator to be provided in their constructor. The meta-estimator extends single output estimators to multioutput estimators.

**User guide:** See the [Multiclass and multilabel algorithms](https://scikit-learn.org/stable/modules/multiclass.html) section for further details.

| **multioutput.ClassifierChain** *(base_estimator)* | A multi-label model that arranges binary classifiers into a chain. |
| **multioutput.MultiOutputRegressor** *(estimator)* | Multi target regression |
| **multioutput.MultiOutputClassifier** *(estimator)* | Multi target classification |

---

#### 30.25.1 sklearn.multioutput.ClassifierChain

**class sklearn.multioutput.ClassifierChain**(base_estimator, order=None, cv=None, random_state=None)

A multi-label model that arranges binary classifiers into a chain.

Each model makes a prediction in the order specified by the chain using all of the available features provided to the model plus the predictions of models that are earlier in the chain.

**Parameters**

- **base_estimator**: estimator
  
The base estimator from which the classifier chain is built.
**order**: array-like, shape=[n_outputs] or ‘random’, optional

By default the order will be determined by the order of columns in the label matrix Y.:

```python
order = [0, 1, 2, ..., Y.shape[1] - 1]
```

The order of the chain can be explicitly set by providing a list of integers. For example, for a chain of length 5:

```python
order = [1, 3, 2, 4, 0]
```

means that the first model in the chain will make predictions for column 1 in the Y matrix, the second model will make predictions for column 3, etc.

If order is ‘random’ a random ordering will be used.

**cv**: int, cross-validation generator or an iterable, optional (default=None)

Determines whether to use cross validated predictions or true labels for the results of previous estimators in the chain. If cv is None the true labels are used when fitting. Otherwise possible inputs for cv are:

- integer, to specify the number of folds in a (Stratified)KFold,
- An object to be used as a cross-validation generator.
- An iterable yielding train, test splits.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

The random number generator is used to generate random chain orders.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>classes_</code></td>
<td>(list) A list of arrays of length <code>len(estimators_)</code> containing the class labels for each estimator in the chain.</td>
</tr>
<tr>
<td><code>estimators_</code></td>
<td>(list) A list of clones of base_estimator.</td>
</tr>
<tr>
<td><code>order_</code></td>
<td>(list) The order of labels in the classifier chain.</td>
</tr>
</tbody>
</table>

**References**


**Methods**
**decision_function** *(X)*
Evaluate the decision_function of the models in the chain.

**fit** *(X, Y)*
Fit the model to data matrix X and targets Y.

**get_params** *((deep)*)
Get parameters for this estimator.

**predict** *(X)*
Predict on the data matrix X using the ClassifierChain model.

**predict_proba** *(X)*
Predict probability estimates.

**score** *(X, y[, sample_weight]*
Returns the mean accuracy on the given test data and labels.

**set_params** *(**params)*
Set the parameters of this estimator.

---

**__init__** *(base_estimator, order=None, cv=None, random_state=None)*
Evaluate the decision_function of the models in the chain.

**Parameters** *

- **X** : array-like, shape (n_samples, n_features)
- **Y** : array-like, shape (n_samples, n_classes)

**Returns** *

- **Y_decision** : array-like, shape (n_samples, n_classes)
  Returns the decision function of the sample for each model in the chain.

**fit** *(X, Y)*
Fit the model to data matrix X and targets Y.

**Parameters** *

- **X** : {array-like, sparse matrix}, shape (n_samples, n_features)
  The input data.
- **Y** : array-like, shape (n_samples, n_classes)
  The target values.

**Returns** *

- **self** : object
  Returns self.

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters** *

- **deep** : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** *

- **params** : mapping of string to any
  Parameter names mapped to their values.

**predict** *(X)*
Predict on the data matrix X using the ClassifierChain model.

**Parameters** *

- **X** : {array-like, sparse matrix}, shape (n_samples, n_features)
  The input data.

**Returns** *

- **Y_pred** : array-like, shape (n_samples, n_classes)
  The predicted values.

**predict_proba** *(X)*
Predict probability estimates.

**Parameters** *

- **X** : {array-like, sparse matrix}, shape (n_samples, n_features)
Returns **Y_prob** : array-like, shape (n_samples, n_classes)

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

**X** : array-like, shape = (n_samples, n_features)
    Test samples.

**y** : array-like, shape = (n_samples) or (n_samples, n_outputs)
    True labels for X.

**sample_weight** : array-like, shape = [n_samples], optional
    Sample weights.

**Returns**

**score** : float
    Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

**self**

Examples using `sklearn.multioutput.ClassifierChain`

- **Classifier Chain**

### 30.25.2 sklearn.multioutput.MultiOutputRegressor

class **sklearn.multioutput.MultiOutputRegressor** *(estimator, n_jobs=1)*

Multi target regression

This strategy consists of fitting one regressor per target. This is a simple strategy for extending regressors that do not natively support multi-target regression.

**Parameters**

**estimator** : estimator object

An estimator object implementing `fit` and `predict`.

**n_jobs** : int, optional, default=1

The number of jobs to run in parallel for `fit`. If -1, then the number of jobs is set to the number of cores. When individual estimators are fast to train or predict using `n_jobs>1` can result in slower performance due to the overhead of spawning processes.

**Methods**

**fit**(X, y[, sample_weight])

Fit the model to data.

**get_params**(deep)

Get parameters for this estimator.

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<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>partial_fit(X, y[, sample_weight])</td>
<td>Incrementally fit the model to data.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict multi-output variable using a model trained for each target variable.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(estimator, n_jobs=1)

fit (X, y, sample_weight=None)
Fit the model to data. Fit a separate model for each output variable.

Parameters

- **X**: (sparse) array-like, shape (n_samples, n_features)
  Data.
- **y**: (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets. An indicator matrix turns on multilabel estimation.
- **sample_weight**: array-like, shape = (n_samples) or None
  Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

Returns self : object
Returns self.

get_params (deep=True)
Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  Parameter names mapped to their values.

partial_fit (X, y, sample_weight=None)
Incrementally fit the model to data. Fit a separate model for each output variable.

Parameters

- **X**: (sparse) array-like, shape (n_samples, n_features)
  Data.
- **y**: (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets.
- **sample_weight**: array-like, shape = (n_samples) or None
  Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

Returns self : object
Returns self.

predict (X)

Predict multi-output variable using a model trained for each target variable.
**Parameters**

- **X**: (sparse) array-like, shape (n_samples, n_features)
  Data.

- **y**: (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets predicted across multiple predictors. Note: Separate models are generated for each predictor.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $\sum((y_{true} - y_{pred})^2)$ and $v$ is the regression sum of squares $\sum((y_{true} - y_{true.mean})^2)$. Best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Test samples.

- **y**: array-like, shape (n_samples) or (n_samples, n_outputs)
  True values for X.

- **sample_weight**: array-like, shape [n_samples], optional
  Sample weights.

**Returns**

- **score**: float
  $R^2$ of self.predict(X) wrt. y.

**Notes**

$R^2$ is calculated by weighting all the targets equally using `multioutput='uniform_average'`.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**Examples using sklearn.multioutput.MultiOutputRegressor**

- Comparing random forests and the multi-output meta estimator

**30.25.3 sklearn.multioutput.MultiOutputClassifier**

**class** sklearn.multioutput.MultiOutputClassifier(**estimator**, **n_jobs=1**)

Multi target classification

This strategy consists of fitting one classifier per target. This is a simple strategy for extending classifiers that do not natively support multi-target classification

**Parameters**

- **estimator**: estimator object
An estimator object implementing fit, score and predict_proba.

**n_jobs** : int, optional, default=1

The number of jobs to use for the computation. If -1 all CPUs are used. If 1 is given, no parallel computing code is used at all, which is useful for debugging. For n_jobs below -1, (n_cpus + 1 + n_jobs) are used. Thus for n_jobs = -2, all CPUs but one are used. The number of jobs to use for the computation. It does each target variable in y in parallel.

**Attributes**

- **estimators_** (list of n_output estimators) Estimators used for predictions.

**Methods**

- fit(X, y[, sample_weight]) Fit the model to data.
- get_params([deep]) Get parameters for this estimator.
- partial_fit(X, y[, classes, sample_weight]) Incrementally fit the model to data.
- predict(X) Predict multi-output variable using a model trained for each target variable.
- predict_proba(X) Probability estimates.
- score(X, y) Returns the mean accuracy on the given test data and labels.
- set_params(**params) Set the parameters of this estimator.

**init** (estimator, n_jobs=1)

Fit the model to data. Fit a separate model for each output variable.

**Parameters**

- X : (sparse) array-like, shape (n_samples, n_features)
  Data.
- y : (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets. An indicator matrix turns on multilabel estimation.
- sample_weight : array-like, shape = (n_samples) or None
  Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

**Returns**

- self : object
  Returns self.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- params : mapping of string to any
Parameter names mapped to their values.

**partial_fit** (*X, y, classes=None, sample_weight=None*)
Incrementally fit the model to data. Fit a separate model for each output variable.

**Parameters**

- **X**: (sparse) array-like, shape (n_samples, n_features)
  Data.

- **y**: (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets.

- **classes**: list of numpy arrays, shape (n_outputs)
  Each array is unique classes for one output in str/int Can be obtained by via `[np.unique(y[:, i]) for i in range(y.shape[1])]`, where y is the target matrix of the entire dataset. This argument is required for the first call to partial_fit and can be omitted in the subsequent calls. Note that y doesn’t need to contain all labels in classes.

- **sample_weight**: array-like, shape = (n_samples) or None
  Sample weights. If None, then samples are equally weighted. Only supported if the underlying regressor supports sample weights.

**Returns**

- **self**: object
  Returns self.

**predict** (*X*)

Predict multi-output variable using a model trained for each target variable.

**Parameters**

- **X**: (sparse) array-like, shape (n_samples, n_features)
  Data.

**Returns**

- **y**: (sparse) array-like, shape (n_samples, n_outputs)
  Multi-output targets predicted across multiple predictors. Note: Separate models are generated for each predictor.

**predict_proba** (*X*)

Probability estimates. Returns prediction probabilities for each class of each output.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Data

**Returns**

- **p**: array of shape = [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1.
  The class probabilities of the input samples. The order of the classes corresponds to that in the attribute `classes_`.

**score** (*X, y*)

Returns the mean accuracy on the given test data and labels.

**Parameters**

- **X**: array-like, shape [n_samples, n_features]
  Test samples

- **y**: array-like, shape [n_samples, n_outputs]
  True values for X
Returns scores : float
accuracy_score of self.predict(X) versus y

set_params(**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

30.26 sklearn.naive_bayes: Naive Bayes

The sklearn.naive_bayes module implements Naive Bayes algorithms. These are supervised learning methods based on applying Bayes’ theorem with strong (naive) feature independence assumptions.

User guide: See the Naive Bayes section for further details.

| naive_bayes.BernoulliNB([alpha, binarize, ...]) | Naive Bayes classifier for multivariate Bernoulli models. |
| naive_bayes.GaussianNB([priors, var_smoothing]) | Gaussian Naive Bayes (GaussianNB) |
| naive_bayes.MultinomialNB([alpha, ...]) | Naive Bayes classifier for multinomial models |
| naive_bayes.ComplementNB([alpha, fit_prior, ...]) | The Complement Naive Bayes classifier described in Rennie et al. |

30.26.1 sklearn.naive_bayes.BernoulliNB

class sklearn.naive_bayes.BernoulliNB(alpha=1.0,  

binarize=0.0,  

fit_prior=True,  

class_prior=None)

Naive Bayes classifier for multivariate Bernoulli models.

Like MultinomialNB, this classifier is suitable for discrete data. The difference is that while MultinomialNB works with occurrence counts, BernoulliNB is designed for binary/boolean features.

Read more in the User Guide.

Parameters alpha : float, optional (default=1.0)
Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).

binarize : float or None, optional (default=0.0)
Threshold for binarizing (mapping to booleans) of sample features. If None, input is presumed to already consist of binary vectors.

fit_prior : boolean, optional (default=True)
Whether to learn class prior probabilities or not. If false, a uniform prior will be used.

class_prior : array-like, size=[n_classes,], optional (default=None)
Prior probabilities of the classes. If specified the priors are not adjusted according to the data.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
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<tbody>
<tr>
<td><code>class_log_prior</code></td>
<td>array, shape = [n_classes]) Log probability of each class (smoothed).</td>
</tr>
<tr>
<td><code>feature_log_prob</code></td>
<td>array, shape = [n_classes, n_features]) Empirical log probability of features given a class,</td>
</tr>
<tr>
<td><code>class_count</code></td>
<td>array, shape = [n_classes]) Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.</td>
</tr>
<tr>
<td><code>feature_count</code></td>
<td>array, shape = [n_classes, n_features]) Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.</td>
</tr>
</tbody>
</table>

References


Examples

```python
>>> import numpy as np
>>> X = np.random.randint(2, size=(6, 100))
>>> Y = np.array([1, 2, 3, 4, 4, 5])
>>> from sklearn.naive_bayes import BernoulliNB
>>> clf = BernoulliNB()
>>> clf.fit(X, Y)
BernoulliNB(alpha=1.0, binarize=0.0, class_prior=None, fit_prior=True)
>>> print(clf.predict(X[2:3]))
[3]
```

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td><code>fit(X, y[, sample_weight])</code></td>
<td>Fit Naive Bayes classifier according to X, y</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>partial_fit(X, y[, classes, sample_weight])</code></td>
<td>Incremental fit on a batch of samples.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Perform classification on an array of test vectors X.</td>
</tr>
<tr>
<td><code>predict_log_proba(X)</code></td>
<td>Return log-probability estimates for the test vector X.</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Return probability estimates for the test vector X.</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__ (alpha=1.0, binarize=0.0, fit_prior=True, class_prior=None)
fit (X, y, sample_weight=None)
   Fit Naive Bayes classifier according to X, y
```
**Parameters**

- **X**: {array-like, sparse matrix}, shape = [n_samples, n_features]
  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

- **y**: array-like, shape = [n_samples]
  
  Target values.

- **sample_weight**: array-like, shape = [n_samples], (default=None)
  
  Weights applied to individual samples (1. for unweighted).

**Returns**

- **self**: object
  
  Returns self.

**get_params**(deep=True)

Get parameters for this estimator.

- **Parameters**
  
  - **deep**: boolean, optional
    
    If True, will return the parameters for this estimator and contained subobjects that are estimators.

- **Returns**
  
  - **params**: mapping of string to any
    
    Parameter names mapped to their values.

**partial_fit**(X, y, classes=None, sample_weight=None)

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

- **Parameters**
  
  - **X**: {array-like, sparse matrix}, shape = [n_samples, n_features]
    
    Training vectors, where n_samples is the number of samples and n_features is the number of features.

  - **y**: array-like, shape = [n_samples]
    
    Target values.

  - **classes**: array-like, shape = [n_classes] (default=None)
    
    List of all the classes that can possibly appear in the y vector.

    Must be provided at the first call to partial_fit, can be omitted in subsequent calls.

  - **sample_weight**: array-like, shape = [n_samples] (default=None)
    
    Weights applied to individual samples (1. for unweighted).

- **Returns**
  
  - **self**: object
    
    Returns self.

**predict**(X)

Perform classification on an array of test vectors X.

- **Parameters**
  
  - **X**: array-like, shape = [n_samples, n_features]

- **Returns**
  
  - **C**: array, shape = [n_samples]
Predicted target values for X

**predict_log_proba** *(X)*

Return log-probability estimates for the test vector X.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]

**Returns**

- **C**: array-like, shape = [n_samples, n_classes]

Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**predict_proba** *(X)*

Return probability estimates for the test vector X.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]

**Returns**

- **C**: array-like, shape = [n_samples, n_classes]

Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)

- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)

- **sample_weight**: array-like, shape = [n_samples], optional

**Returns**

- **score**: float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

### Examples using sklearn.naive_bayes.BernoulliNB

- Hashing feature transformation using Totally Random Trees
- Classification of text documents using sparse features

### 30.26.2 sklearn.naive_bayes.GaussianNB

**class** *sklearn.naive_bayes.GaussianNB*(**priors=None, var_smoothing=1e-09**)

Gaussian Naive Bayes (GaussianNB)
Can perform online updates to model parameters via `partial_fit` method. For details on algorithm used to update feature means and variance online, see Stanford CS tech report STAN-CS-79-773 by Chan, Golub, and LeVeque:


Read more in the User Guide.

**Parameters**

- **priors**: array-like, shape (n_classes,)
  
  Prior probabilities of the classes. If specified the priors are not adjusted according to the data.

- **var_smoothing**: float, optional (default=1e-9)
  
  Portion of the largest variance of all features that is added to variances for calculation stability.

**Attributes**

- **class_prior_**: (array, shape (n_classes,)) probability of each class.
- **class_count_**: (array, shape (n_classes,)) number of training samples observed in each class.
- **theta_**: (array, shape (n_classes, n_features)) mean of each feature per class.
- **sigma_**: (array, shape (n_classes, n_features)) variance of each feature per class.
- **epsilon_**: (float) absolute additive value to variances.

**Examples**

```python
>>> import numpy as np
d>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])
d>>> Y = np.array([1, 1, 1, 2, 2, 2])
d>>> from sklearn.naive_bayes import GaussianNB
d>>> clf = GaussianNB()
d>>> clf.fit(X, Y)
GaussianNB(priors=None, var_smoothing=1e-09)
d>>> print(clf.predict([[-0.8, -1]]))
[1]
d>>> clf_pf = GaussianNB()
d>>> clf_pf.partial_fit(X, Y, np.unique(Y))
GaussianNB(priors=None, var_smoothing=1e-09)
d>>> print(clf_pf.predict([[-0.8, -1]]))
[1]
```

**Methods**

- **fit(X, y[, sample_weight])**  
  Fit Gaussian Naive Bayes according to X, y.
- **get_params([deep])**  
  Get parameters for this estimator.
- **partial_fit(X, y[, classes, sample_weight])**  
  Incremental fit on a batch of samples.
- **predict(X)**  
  Perform classification on an array of test vectors X.
- **predict_log_proba(X)**  
  Return log-probability estimates for the test vector X.
- **predict_proba(X)**  
  Return probability estimates for the test vector X.
Table 30.240 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

**__init__**(priors=None, var_smoothing=1e-09)

**fit**(X, y, sample_weight=None)

Fit Gaussian Naive Bayes according to X, y

**Parameters**

* X : array-like, shape (n_samples, n_features)
  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

* y : array-like, shape (n_samples,)
  
  Target values.

* sample_weight : array-like, shape (n_samples,), optional (default=None)
  
  Weights applied to individual samples (1. for unweighted).

  New in version 0.17: Gaussian Naive Bayes supports fitting with sample_weight.

**Returns**

* self : object
  
  Returns self.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

* deep : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

* params : mapping of string to any
  
  Parameter names mapped to their values.

**partial_fit**(X, y, classes=None, sample_weight=None)

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance and numerical stability overhead, hence it is better to call partial_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

**Parameters**

* X : array-like, shape (n_samples, n_features)
  
  Training vectors, where n_samples is the number of samples and n_features is the number of features.

* y : array-like, shape (n_samples,)
  
  Target values.

* classes : array-like, shape (n_classes,), optional (default=None)
  
  List of all the classes that can possibly appear in the y vector.

  Must be provided at the first call to partial_fit, can be omitted in subsequent calls.
sample_weight: array-like, shape (n_samples,), optional (default=None)

Weights applied to individual samples (1. for unweighted).

New in version 0.17.

Returns self: object

Returns self.

predict (X)
Perform classification on an array of test vectors X.

Parameters X: array-like, shape = [n_samples, n_features]

Returns C: array, shape = [n_samples]
Predicted target values for X

predict_log_proba (X)
Return log-probability estimates for the test vector X.

Parameters X: array-like, shape = [n_samples, n_features]

Returns C: array-like, shape = [n_samples, n_classes]
Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute classes_.

predict_proba (X)
Return probability estimates for the test vector X.

Parameters X: array-like, shape = [n_samples, n_features]

Returns C: array-like, shape = [n_samples, n_classes]
Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute classes_.

score (X, y, sample_weight=None)
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters X: array-like, shape = (n_samples, n_features)
Test samples.

y: array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

sample_weight: array-like, shape = [n_samples], optional
Sample weights.

Returns score: float
Mean accuracy of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.
Returns self

Examples using sklearn.naive_bayes.GaussianNB

- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Probability calibration of classifiers
- Classifier comparison
- Plot class probabilities calculated by the VotingClassifier
- Plotting Learning Curves
- Importance of Feature Scaling

30.26.3 sklearn.naive_bayes.MultinomialNB

class sklearn.naive_bayes.MultinomialNB(alpha=1.0, fit_prior=True, class_prior=None)

Naive Bayes classifier for multinomial models

The multinomial Naive Bayes classifier is suitable for classification with discrete features (e.g., word counts for text classification). The multinomial distribution normally requires integer feature counts. However, in practice, fractional counts such as tf-idf may also work.

Read more in the User Guide.

Parameters

- **alpha** : float, optional (default=1.0)
  Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).
- **fit_prior** : boolean, optional (default=True)
  Whether to learn class prior probabilities or not. If false, a uniform prior will be used.
- **class_prior** : array-like, size (n_classes,), optional (default=None)
  Prior probabilities of the classes. If specified the priors are not adjusted according to the data.

Attributes

- **class_log_prior_** (array, shape (n_classes,)) Smoothed empirical log probability for each class.
- **intercept_** (property) Mirrors **class_log_prior_** for interpreting MultinomialNB as a linear model.
- **feature_log_prob_** (array, shape (n_classes, n_features)) Empirical log probability of features given a class, P(x_i|y).
- **coef_** (property) Mirrors **feature_log_prob_** for interpreting MultinomialNB as a linear model.
- **class_count_** (array, shape (n_classes,)) Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.
- **feature_count_** (array, shape (n_classes, n_features)) Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.
Notes

For the rationale behind the names `coef_` and `intercept_`, i.e. naive Bayes as a linear classifier, see J. Rennie et al. (2003), Tackling the poor assumptions of naive Bayes text classifiers, ICML.

References


Examples

```python
>>> import numpy as np
>>> X = np.random.randint(5, size=(6, 100))
>>> y = np.array([1, 2, 3, 4, 5, 6])
>>> from sklearn.naive_bayes import MultinomialNB
>>> clf = MultinomialNB()
>>> clf.fit(X, y)
MultinomialNB(alpha=1.0, class_prior=None, fit_prior=True)
>>> print(clf.predict(X[2:3]))
[3]
```

Methods

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<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td><code>fit(X, y[, sample_weight])</code></td>
<td>Fit Naive Bayes classifier according to X, y</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>partial_fit(X, y[, classes, sample_weight])</code></td>
<td>Incremental fit on a batch of samples.</td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Perform classification on an array of test vectors X.</td>
</tr>
<tr>
<td><code>predict_log_proba(X)</code></td>
<td>Return log-probability estimates for the test vector X.</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Return probability estimates for the test vector X.</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__(alpha=1.0, fit_prior=True, class_prior=None)
fit(X, y, sample_weight=None)
```

Fit Naive Bayes classifier according to X, y

**Parameters**

- `X` : array-like, sparse matrix, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of features.
- `y` : array-like, shape = [n_samples]
  - Target values.
- `sample_weight` : array-like, shape = [n_samples], (default=None)
  - Weights applied to individual samples (1. for unweighted).
Returns self:

Returns self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params: mapping of string to any

Parameter names mapped to their values.

partial_fit (X, y, classes=None, sample_weight=None)
Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to
implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial_fit on chunks of data that are
as large as possible (as long as fitting in the memory budget) to hide the overhead.

Parameters X: {array-like, sparse matrix}, shape = [n_samples, n_features]

Training vectors, where n_samples is the number of samples and n_features is the num-
ber of features.

y: array-like, shape = [n_samples]

Target values.

classes: array-like, shape = [n_classes] (default=None)

List of all the classes that can possibly appear in the y vector.

Must be provided at the first call to partial_fit, can be omitted in subsequent calls.

sample_weight: array-like, shape = [n_samples] (default=None)

Weights applied to individual samples (1. for unweighted).

Returns self:

Returns self.

predict (X)
Perform classification on an array of test vectors X.

Parameters X: array-like, shape = [n_samples, n_features]

Returns C: array, shape = [n_samples]

Predicted target values for X.

predict_log_proba (X)
Return log-probability estimates for the test vector X.

Parameters X: array-like, shape = [n_samples, n_features]

Returns C: array-like, shape = [n_samples, n_classes]

Returns the log-probability of the samples for each class in the model. The columns
correspond to the classes in sorted order, as they appear in the attribute classes.
**predict_proba** *(X)*

Return probability estimates for the test vector X.

**Parameters**

  * X : array-like, shape = [n_samples, n_features]

**Returns**

  * C : array-like, shape = [n_samples, n_classes]

Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

  * X : array-like, shape = (n_samples, n_features)
    Test samples.
  * y : array-like, shape = (n_samples) or (n_samples, n_outputs)
    True labels for X.
  * sample_weight : array-like, shape = [n_samples], optional
    Sample weights.

**Returns**

  * score : float
    Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

  * self

---

**Examples using sklearn.naive_bayes.MultinomialNB**

- Out-of-core classification of text documents
- Classification of text documents using sparse features

**30.26.4 sklearn.naive_bayes.ComplementNB**

class sklearn.naive_bayes.ComplementNB *(alpha=1.0, fit_prior=True, class_prior=None, norm=False)*

The Complement Naive Bayes classifier described in Rennie et al. (2003).

The Complement Naive Bayes classifier was designed to correct the “severe assumptions” made by the standard Multinomial Naive Bayes classifier. It is particularly suited for imbalanced data sets.

Read more in the [User Guide](#).

**Parameters**

  * alpha : float, optional (default=1.0)
    Additive (Laplace/Lidstone) smoothing parameter (0 for no smoothing).
  * fit_prior : boolean, optional (default=True)
Only used in edge case with a single class in the training set.

**class_prior** : array-like, size (n_classes,), optional (default=None)

Prior probabilities of the classes. Not used.

**norm** : boolean, optional (default=False)

Whether or not a second normalization of the weights is performed. The default behavior mirrors the implementations found in Mahout and Weka, which do not follow the full algorithm described in Table 9 of the paper.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>class_log_prior_</td>
<td>(array, shape (n_classes,)) Smoothed empirical log probability for each class. Only used in edge case with a single class in the training set.</td>
</tr>
<tr>
<td>feature_log_prob_</td>
<td>(array, shape (n_classes, n_features)) Empirical weights for class complements.</td>
</tr>
<tr>
<td>class_count_</td>
<td>(array, shape (n_classes,)) Number of samples encountered for each class during fitting. This value is weighted by the sample weight when provided.</td>
</tr>
<tr>
<td>feature_count_</td>
<td>(array, shape (n_classes, n_features)) Number of samples encountered for each (class, feature) during fitting. This value is weighted by the sample weight when provided.</td>
</tr>
<tr>
<td>feature_all_</td>
<td>(array, shape (n_features,)) Number of samples encountered for each feature during fitting. This value is weighted by the sample weight when provided.</td>
</tr>
</tbody>
</table>

**References**


**Examples**

```python
>>> from sklearn.naive_bayes import ComplementNB
>>> clf = ComplementNB()
>>> clf.fit(X, y)
ComplementNB(alpha=1.0, class_prior=None, fit_prior=True, norm=False)
>>> clf.predict(X[2:3])
[3]
```

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit Naive Bayes classifier according to X, y</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>partial_fit(X, y[, classes, sample_weight])</td>
<td>Incremental fit on a batch of samples.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Perform classification on an array of test vectors X.</td>
</tr>
<tr>
<td>predict_log_proba(X)</td>
<td>Return log-probability estimates for the test vector X.</td>
</tr>
</tbody>
</table>
Table 30.242 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>predict_proba</code></td>
<td>Return probability estimates for the test vector X.</td>
</tr>
<tr>
<td><code>score</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__ (alpha=1.0, fit_prior=True, class_prior=None, norm=False)
```

```python
fit (X, y, sample_weight=None)
```

Fit Naive Bayes classifier according to X, y

**Parameters**
- X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of features.
- y : array-like, shape = [n_samples]
  - Target values.
- sample_weight : array-like, shape = [n_samples], (default=None)
  - Weights applied to individual samples (1. for unweighted).

**Returns**
- self : object
  - Returns self.

```python
get_params (deep=True)
```

Get parameters for this estimator.

**Parameters**
- deep : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- params : mapping of string to any
  - Parameter names mapped to their values.

```python
partial_fit (X, y, classes=None, sample_weight=None)
```

Incremental fit on a batch of samples.

This method is expected to be called several times consecutively on different chunks of a dataset so as to implement out-of-core or online learning.

This is especially useful when the whole dataset is too big to fit in memory at once.

This method has some performance overhead hence it is better to call partial_fit on chunks of data that are as large as possible (as long as fitting in the memory budget) to hide the overhead.

**Parameters**
- X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training vectors, where n_samples is the number of samples and n_features is the number of features.
- y : array-like, shape = [n_samples]
  - Target values.
- classes : array-like, shape = [n_classes] (default=None)
  - List of all the classes that can possibly appear in the y vector.
  - Must be provided at the first call to partial_fit, can be omitted in subsequent calls.
- sample_weight : array-like, shape = [n_samples] (default=None)
Weights applied to individual samples (1. for unweighted).

**Returns**  
`self` : object

Returns self.

**predict**  
`X`  
Perform classification on an array of test vectors X.

**Parameters**  
`X` : array-like, shape = [n_samples, n_features]

**Returns**  
`C` : array, shape = [n_samples]

Predicted target values for X

**predict_log_proba**  
`X`  
Return log-probability estimates for the test vector X.

**Parameters**  
`X` : array-like, shape = [n_samples, n_features]

**Returns**  
`C` : array-like, shape = [n_samples, n_classes]

Returns the log-probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**predict_proba**  
`X`  
Return probability estimates for the test vector X.

**Parameters**  
`X` : array-like, shape = [n_samples, n_features]

**Returns**  
`C` : array-like, shape = [n_samples, n_classes]

Returns the probability of the samples for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**score**  
`X, y, sample_weight=None`  
Enter the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**  
`X` : array-like, shape = (n_samples, n_features)

Test samples.

`y` : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

`sample_weight` : array-like, shape = [n_samples], optional

Sample weights.

**Returns**  
`score` : float

Mean accuracy of `self.predict(X)` wrt. `y`.

**set_params**  
`**params`  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
`self`
Examples using sklearn.naive_bayes.ComplementNB

- Classification of text documents using sparse features

30.27 sklearn.neighbors: Nearest Neighbors

The sklearn.neighbors module implements the k-nearest neighbors algorithm.

User guide: See the Nearest Neighbors section for further details.

<table>
<thead>
<tr>
<th>neighbors.BallTree</th>
<th>BallTree for fast generalized N-point problems</th>
</tr>
</thead>
<tbody>
<tr>
<td>neighbors.DistanceMetric</td>
<td>DistanceMetric class</td>
</tr>
<tr>
<td>neighbors.KDTree</td>
<td>KDTree for fast generalized N-point problems</td>
</tr>
<tr>
<td>neighbors.KernelDensity([bandwidth, ...])</td>
<td>Kernel Density Estimation</td>
</tr>
<tr>
<td>neighbors.KNeighborsClassifier([...])</td>
<td>Classifier implementing the k-nearest neighbors vote.</td>
</tr>
<tr>
<td>neighbors.KNeighborsRegressor([n_neighbors, ...])</td>
<td>Regression based on k-nearest neighbors.</td>
</tr>
<tr>
<td>neighbors.LocalOutlierFactor([n_neighbors, ...])</td>
<td>Unsupervised Outlier Detection using Local Outlier Factor (LOF)</td>
</tr>
<tr>
<td>neighbors.RadiusNeighborsClassifier([...])</td>
<td>Classifier implementing a vote among neighbors within a given radius</td>
</tr>
<tr>
<td>neighbors.RadiusNeighborsRegressor([radius, ...])</td>
<td>Regression based on neighbors within a fixed radius.</td>
</tr>
<tr>
<td>neighbors.NearestCentroid([metric, ...])</td>
<td>Nearest centroid classifier.</td>
</tr>
<tr>
<td>neighbors.NearestNeighbors([n_neighbors, ...])</td>
<td>Unsupervised learner for implementing neighbor searches.</td>
</tr>
</tbody>
</table>

30.27.1 sklearn.neighbors.BallTree

class sklearn.neighbors.BallTree

BallTree for fast generalized N-point problems

BallTree(X, leaf_size=40, metric='minkowski', **kwargs)

Parameters

X : array-like, shape = [n_samples, n_features]

n_samples is the number of points in the data set, and n_features is the dimension of the parameter space. Note: if X is a C-contiguous array of doubles then data will not be copied. Otherwise, an internal copy will be made.

leaf_size : positive integer (default = 40)

Number of points at which to switch to brute-force. Changing leaf_size will not affect the results of a query, but can significantly impact the speed of a query and the memory required to store the constructed tree. The amount of memory needed to store the tree scales as approximately n_samples / leaf_size. For a specified leaf_size, a leaf node is guaranteed to satisfy leaf_size <= n_points <= 2 * leaf_size, except in the case that n_samples < leaf_size.

metric : string or DistanceMetric object

the distance metric to use for the tree. Default='minkowski' with p=2 (that is, a euclidean metric). See the documentation of the DistanceMetric class for a list of available metrics. ball_tree.valid_metrics gives a list of the metrics which are valid for BallTree.
Additional keywords are passed to the distance metric class.

Attributes

| data | (np.ndarray) The training data |

Examples

Query for k-nearest neighbors

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> dist, ind = tree.query([X[0]], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[ 0.19662693 0.29473397]
```

Pickle and Unpickle a tree. Note that the state of the tree is saved in the pickle operation: the tree needs not be rebuilt upon unpickling.

```python
>>> import numpy as np
>>> import pickle
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> s = pickle.dumps(tree)
>>> tree_copy = pickle.loads(s)
>>> dist, ind = tree_copy.query(X[0], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[ 0.19662693 0.29473397]
```

Query for neighbors within a given radius

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BallTree(X, leaf_size=2)
>>> print(tree.query_radius(X[0], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[0], r=0.3)
>>> print(ind)  # indices of neighbors within distance 0.3
[3 0 1]
```

Compute a gaussian kernel density estimate:

```python
>>> import numpy as np
>>> np.random.seed(1)
>>> X = np.random.random((100, 3))
>>> tree = BallTree(X)
```
```python
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716])
```

Compute a two-point auto-correlation function

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = BallTree(X)
>>> tree.two_point_correlation(X, r)
array([ 30, 62, 278, 580, 820])
```

**Methods**

- `get_arrays`
- `get_n_calls`
- `get_tree_stats`
- `kernel_density`
  - `kernel_density(self, X, h[, kernel, atol, ...])` Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.
- `query`
  - `query(X[, k, return_distance, dualtree, ...])` query the tree for the k nearest neighbors
- `query_radius`
  - `query_radius(self, X, r, count_only = False):`
- `reset_n_calls`
- `two_point_correlation`
  - `two_point_correlation` Compute the two-point correlation function

**__init__**(self, X, h[, kernel, atol, ...])
  Initialize self. See help(type(self)) for accurate signature.

**kernel_density**(self, X, h, kernel='gaussian', atol=0, rtol=1E-8, breadth_first=True, return_log=False)
  Compute the kernel density estimate at points X with the given kernel, using the distance metric specified at tree creation.

  **Parameters**
  - **X**: array_like
    An array of points to query. Last dimension should match dimension of training data.
  - **h**: float
    the bandwidth of the kernel
  - **kernel**: string
    specify the kernel to use. Options are - ‘gaussian’ - ‘tophat’ - ‘epanechnikov’ - ‘exponential’ - ‘linear’ - ‘cosine’ Default is kernel = ‘gaussian’
  - **atol, rtol**: float (default = 0)
    Specify the desired relative and absolute tolerance of the result. If the true result is K_true, then the returned result K_ret satisfies abs(K_true – K_ret) < atol + rtol * K_ret The default is zero (i.e. machine precision) for both.
  - **breadth_first**: boolean (default = False)
    if True, use a breadth-first search. If False (default) use a depth-first search. Breath-first is generally faster for compact kernels and/or high tolerances.
return_log : boolean (default = False)

return the logarithm of the result. This can be more accurate than returning the result itself for narrow kernels.

Returns density : ndarray

The array of (log)-density evaluations, shape = X.shape[:-1]

Examples

Compute a gaussian kernel density estimate:

```python
>>> import numpy as np
>>> np.random.seed(1)
>>> X = np.random.random((100, 3))
>>> tree = BinaryTree(X)
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716 ])
```

query (X, k=1, return_distance=True, dualtree=False, breadth_first=False)

query the tree for the k nearest neighbors

Parameters X : array-like, last dimension self.dim

An array of points to query

k : integer (default = 1)

The number of nearest neighbors to return

return_distance : boolean (default = True)

if True, return a tuple (d, i) of distances and indices if False, return array i

dualtree : boolean (default = False)

if True, use the dual tree formalism for the query: a tree is built for the query points, and the pair of trees is used to efficiently search this space. This can lead to better performance as the number of points grows large.

breadth_first : boolean (default = False)

if True, then query the nodes in a breadth-first manner. Otherwise, query the nodes in a depth-first manner.

sort_results : boolean (default = True)

if True, then distances and indices of each point are sorted on return, so that the first column contains the closest points. Otherwise, neighbors are returned in an arbitrary order.

Returns i : if return_distance == False

(d,i) : if return_distance == True

d : array of doubles - shape: x.shape[:-1] + (k,)

each entry gives the list of distances to the neighbors of the corresponding point

i : array of integers - shape: x.shape[:-1] + (k,)

each entry gives the list of indices of neighbors of the corresponding point
Examples

Query for k-nearest neighbors

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BinaryTree(X, leaf_size=2)
>>> dist, ind = tree.query(X[0], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[ 0. 0.19662693 0.29473397]
```

`query_radius()`

query_radius(self, X, r, count_only = False):

query the tree for neighbors within a radius r

**Parameters**

- `X`: array-like, last dimension self.dim
  
  An array of points to query

- `r`: distance within which neighbors are returned
  
  r can be a single value, or an array of values of shape x.shape[:-1] if different radii are desired for each point.

- `count_only`: boolean (default = False)
  
  if True, return only the count of points within distance r if False, return the indices of all points within distance r. If return_distance==True, setting count_only=True will result in an error.

- `sort_results`: boolean (default = False)
  
  if True, the distances and indices will be sorted before being returned. If False, the results will not be sorted. If return_distance == False, setting sort_results = True will result in an error.

**Returns**

- `count`: if count_only == True
  
  - `ind`: if count_only == False and return_distance == False
  
  - `(ind, dist)`: if count_only == False and return_distance == True

- `count`: array of integers, shape = X.shape[:-1]
  
  each entry gives the number of neighbors within a distance r of the corresponding point.

- `ind`: array of objects, shape = X.shape[:-1]
  
  each element is a numpy integer array listing the indices of neighbors of the corresponding point. Note that unlike the results of a k-neighbors query, the returned neighbors are not sorted by distance by default.

- `dist`: array of objects, shape = X.shape[:-1]
each element is a numpy double array listing the distances corresponding to indices in i.

Examples

Query for neighbors in a given radius

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3)) # 10 points in 3 dimensions
>>> tree = BinaryTree(X, leaf_size=2)
>>> print(tree.query_radius(X[0], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[0], r=0.3)
>>> print(ind) # indices of neighbors within distance 0.3
[3 0 1]
```

two_point_correlation()

Compute the two-point correlation function

**Parameters**

- **X**: array_like
  
  An array of points to query. Last dimension should match dimension of training data.

- **r**: array_like
  
  A one-dimensional array of distances

- **dualtree**: boolean (default = False)
  
  If true, use a dualtree algorithm. Otherwise, use a single-tree algorithm. Dual tree algorithms can have better scaling for large N.

**Returns**

- **counts**: ndarray
  
  counts[i] contains the number of pairs of points with distance less than or equal to r[i]

Examples

Compute the two-point autocorrelation function of X:

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = BinaryTree(X)
>>> tree.two_point_correlation(X, r)
array([ 30, 62, 278, 580, 820])
```

30.27.2 sklearn.neighbors.DistanceMetric
class sklearn.neighbors.DistanceMetric

DistanceMetric class

This class provides a uniform interface to fast distance metric functions. The various metrics can be accessed via the `get_metric` class method and the metric string identifier (see below). For example, to use the Euclidean distance:
Available Metrics The following lists the string metric identifiers and the associated distance metric classes:

### Metrics intended for real-valued vector spaces:

<table>
<thead>
<tr>
<th>identifier</th>
<th>class name</th>
<th>args</th>
<th>distance function</th>
</tr>
</thead>
<tbody>
<tr>
<td>“euclidean”</td>
<td>EuclideanDistance</td>
<td></td>
<td>$\sqrt{\sum((x - y)^2)}$</td>
</tr>
<tr>
<td>“manhattan”</td>
<td>ManhattanDistance</td>
<td></td>
<td>$\sum(</td>
</tr>
<tr>
<td>“chebyshev”</td>
<td>ChebyshevDistance</td>
<td></td>
<td>$\max(</td>
</tr>
<tr>
<td>“minkowski”</td>
<td>MinkowskiDistance</td>
<td>p</td>
<td>$\sum(</td>
</tr>
<tr>
<td>“wminkowski”</td>
<td>WMinkowskiDistance</td>
<td>p, w</td>
<td>$\sum(w *</td>
</tr>
<tr>
<td>“seuclidean”</td>
<td>SEuclideanDistance</td>
<td>V</td>
<td>$\sqrt{\sum((x - y)^2 / V)}$</td>
</tr>
<tr>
<td>“mahalanobis”</td>
<td>MahalanobisDistance</td>
<td>V</td>
<td>$\sqrt{(x - y)' V^{-1} (x - y)}$</td>
</tr>
</tbody>
</table>

### Metrics intended for two-dimensional vector spaces:

Note that the haversine distance metric requires data in the form of [latitude, longitude] and both inputs and outputs are in units of radians.

<table>
<thead>
<tr>
<th>identifier</th>
<th>class name</th>
<th>distance function</th>
</tr>
</thead>
</table>
| “haversine”  | HaversineDistance      | $2 \arcsin(\sqrt{\sin^2(0.5*dx) 
\cdot 
\cos(x1)\cos(x2)\sin^2(0.5*dy)})$ |

### Metrics intended for integer-valued vector spaces:

Though intended for integer-valued vectors, these are also valid metrics in the case of real-valued vectors.

<table>
<thead>
<tr>
<th>identifier</th>
<th>class name</th>
<th>distance function</th>
</tr>
</thead>
<tbody>
<tr>
<td>“hamming”</td>
<td>HammingDistance</td>
<td>$N_{unequal}(x, y) / N_{tot}$</td>
</tr>
<tr>
<td>“canberra”</td>
<td>CanberraDistance</td>
<td>$\sum(</td>
</tr>
<tr>
<td>“braycurtis”</td>
<td>BrayCurtisDistance</td>
<td>$\sum(</td>
</tr>
</tbody>
</table>

### Metrics intended for boolean-valued vector spaces:

Any nonzero entry is evaluated to “True”. In the listings below, the following abbreviations are used:

- N : number of dimensions
- NTT : number of dims in which both values are True
- NTF: number of dims in which the first value is True, second is False
- NFT: number of dims in which the first value is False, second is True
- NFF: number of dims in which both values are False
- NNEQ: number of non-equal dimensions, NNEQ = NTF + NFT
- NNZ: number of nonzero dimensions, NNZ = NTF + NFT + NTT

<table>
<thead>
<tr>
<th>identifier</th>
<th>class name</th>
<th>distance function</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot;jaccard&quot;</td>
<td>JaccardDistance</td>
<td>NNEQ / NNZ</td>
</tr>
<tr>
<td>&quot;matching&quot;</td>
<td>MatchingDistance</td>
<td>NNEQ / N</td>
</tr>
<tr>
<td>&quot;dice&quot;</td>
<td>DiceDistance</td>
<td>NNEQ / (N - NTT) / (NNEQ + N)</td>
</tr>
<tr>
<td>&quot;kulsinski&quot;</td>
<td>KulsinskiDistance</td>
<td>(NNEQ + N - NTT) / (NNEQ + N)</td>
</tr>
<tr>
<td>&quot;rogerstanimoto&quot;</td>
<td>RogersTanimotoDistance</td>
<td>2 * NNEQ / (N + NNEQ)</td>
</tr>
<tr>
<td>&quot;russellrao&quot;</td>
<td>RussellRaoDistance</td>
<td>NNZ / N</td>
</tr>
<tr>
<td>&quot;sokalmichener&quot;</td>
<td>SokalMichenerDistance</td>
<td>2 * NNEQ / (N + NNEQ)</td>
</tr>
<tr>
<td>&quot;sokalsneath&quot;</td>
<td>SokalSneathDistance</td>
<td>NNEQ / (NNEQ + 0.5 * NTT)</td>
</tr>
</tbody>
</table>

**User-defined distance:**

<table>
<thead>
<tr>
<th>identifier</th>
<th>class name</th>
<th>args</th>
<th>func</th>
</tr>
</thead>
<tbody>
<tr>
<td>&quot;pyfunc&quot;</td>
<td>PyFuncDistance</td>
<td></td>
<td>func</td>
</tr>
</tbody>
</table>

Here `func` is a function which takes two one-dimensional numpy arrays, and returns a distance. Note that in order to be used within the BallTree, the distance must be a true metric: i.e. it must satisfy the following properties

1. Non-negativity: \( d(x, y) \geq 0 \)
2. Identity: \( d(x, y) = 0 \) if and only if \( x = y \)
3. Symmetry: \( d(x, y) = d(y, x) \)
4. Triangle Inequality: \( d(x, y) + d(y, z) \geq d(x, z) \)

Because of the Python object overhead involved in calling the python function, this will be fairly slow, but it will have the same scaling as other distances.

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>dist_to_rdist</code></td>
<td>Convert the true distance to the reduced distance.</td>
</tr>
<tr>
<td><code>get_metric</code></td>
<td>Get the given distance metric from the string identifier.</td>
</tr>
<tr>
<td><code>pairwise</code></td>
<td>Compute the pairwise distances between X and Y</td>
</tr>
<tr>
<td><code>rdist_to_dist</code></td>
<td>Convert the Reduced distance to the true distance.</td>
</tr>
</tbody>
</table>

**__init__ ($self$, /, *args, **kwargs)**

Initialize self. See help(type(self)) for accurate signature.

`dist_to_rdist ()`

Convert the true distance to the reduced distance.

The reduced distance, defined for some metrics, is a computationally more efficient measure which preserves the rank of the true distance. For example, in the Euclidean distance metric, the reduced distance is the squared-euclidean distance.
get_metric()  
Get the given distance metric from the string identifier.  
See the docstring of DistanceMetric for a list of available metrics.  

Parameters  
metric : string or class name  
The distance metric to use  

**kwargs  
additional arguments will be passed to the requested metric  

pairwise()  
Compute the pairwise distances between X and Y  
This is a convenience routine for the sake of testing. For many metrics, the utilities in scipy.spatial.distance.cdist and scipy.spatial.distance.pdist will be faster.  

Parameters  
X : array_like  
Array of shape (Nx, D), representing Nx points in D dimensions.  
Y : array_like (optional)  
Array of shape (Ny, D), representing Ny points in D dimensions. If not specified, then Y=X.  

Returns  
——–  
dist : ndarray  
The shape (Nx, Ny) array of pairwise distances between points in X and Y.  

rdist_to_dist()  
Convert the Reduced distance to the true distance.  
The reduced distance, defined for some metrics, is a computationally more efficient measure which preserves the rank of the true distance. For example, in the Euclidean distance metric, the reduced distance is the squared-euclidean distance.  

30.27.3 sklearn.neighbors.KDTree  

class sklearn.neighbors.KDTree  
KDTree for fast generalized N-point problems  
KDTree(X, leaf_size=40, metric='minkowski', **kwargs)  

Parameters  
X : array-like, shape = [n_samples, n_features]  
n_samples is the number of points in the data set, and n_features is the dimension of the parameter space. Note: if X is a C-contiguous array of doubles then data will not be copied. Otherwise, an internal copy will be made.  

leaf_size : positive integer (default = 40)  
Number of points at which to switch to brute-force. Changing leaf_size will not affect the results of a query, but can significantly impact the speed of a query and the memory required to store the constructed tree. The amount of memory needed to store the tree scales as approximately n_samples / leaf_size. For a specified leaf_size, a leaf node is guaranteed to satisfy leaf_size <= n_points <= 2 * leaf_size, except in the case that n_samples < leaf_size.
**metric** : string or DistanceMetric object

the distance metric to use for the tree. Default='minkowski' with p=2 (that is, a euclidean metric). See the documentation of the DistanceMetric class for a list of available metrics. `kd_tree.valid_metrics` gives a list of the metrics which are valid for KDTree.

Additional keywords are passed to the distance metric class.

**Attributes**

| **data** | (np.ndarray) The training data |

**Examples**

Query for k-nearest neighbors

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> dist, ind = tree.query([X[0]], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[0. 0.19662693 0.29473397]
```

Pickle and Unpickle a tree. Note that the state of the tree is saved in the pickle operation: the tree needs not be rebuilt upon unpickling.

```python
>>> import numpy as np
>>> import pickle

>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> s = pickle.dumps(tree)
>>> tree_copy = pickle.loads(s)
>>> dist, ind = tree_copy.query(X[0], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[0. 0.19662693 0.29473397]
```

Query for neighbors within a given radius

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = KDTree(X, leaf_size=2)
>>> print(tree.query_radius(X[0], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[0], r=0.3)
>>> print(ind)  # indices of neighbors within distance 0.3
[3 0 1]
```

Compute a gaussian kernel density estimate:
>>> import numpy as np
>>> np.random.seed(1)
>>> X = np.random.random((100, 3))
>>> tree = KDTree(X)
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716 ])

Compute a two-point auto-correlation function

>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = KDTree(X)
>>> tree.two_point_correlation(X, r)
array([ 30, 62, 278, 580, 820])

Methods

_get_arrays
_get_n_calls
_get_tree_stats
kernel_density(self, X, h[, kernel, atol, . . .]) Compute the kernel density estimate at points X with
the given kernel, using the distance metric specified at
tree creation.

query(X[, k, return_distance, dualtree, . . .]) query the tree for the k nearest neighbors
query_radius(self, X, r, count_only = False):
reset_n_calls

two_point_correlation

Compute the two-point correlation function

__init__($self, /, *args, **kwargs)
Initialize self. See help(type(self)) for accurate signature.

kernel_density($self, X, h, kernel='gaussian', atol=0, rtol=1E-8, breadth_first=True, return_log=False)
Compute the kernel density estimate at points X with the given kernel, using the distance metric specified
at tree creation.

Parameters X : array_like
An array of points to query. Last dimension should match dimension of training data.

h : float
the bandwidth of the kernel

kernel : string
specify the kernel to use. Options are - ‘gaussian’ - ‘tophat’ - ‘epanechnikov’ - ‘exponential’ - ‘linear’ - ‘cosine’ Default is kernel = ‘gaussian’

atol, rtol : float (default = 0)
Specify the desired relative and absolute tolerance of the result. If the true result is
K_true, then the returned result K_ret satisfies abs(K_true - K_ret) < atol + rtol * K_ret The default is zero (i.e. machine precision) for both.
**breadth_first** : boolean (default = False)

    if True, use a breadth-first search. If False (default) use a depth-first search. Breadth-
    first is generally faster for compact kernels and/or high tolerances.

**return_log** : boolean (default = False)

    return the logarithm of the result. This can be more accurate than returning the result
    itself for narrow kernels.

**Returns density** : ndarray

    The array of (log)-density evaluations, shape = X.shape[:-1]

**Examples**

Compute a gaussian kernel density estimate:

```python
>>> import numpy as np
>>> np.random.seed(1)
>>> X = np.random.random((100, 3))
>>> tree = BinaryTree(X)
>>> tree.kernel_density(X[:3], h=0.1, kernel='gaussian')
array([ 6.94114649, 7.83281226, 7.2071716 ])
```

**query** (X, k=1, return_distance=True, dualtree=False, breadth_first=False)

query the tree for the k nearest neighbors

**Parameters X** : array-like, last dimension self.dim

    An array of points to query

**k** : integer (default = 1)

    The number of nearest neighbors to return

**return_distance** : boolean (default = True)

    if True, return a tuple (d, i) of distances and indices if False, return array i

**dualtree** : boolean (default = False)

    if True, use the dual tree formalism for the query: a tree is built for the query points,
    and the pair of trees is used to efficiently search this space. This can lead to better
    performance as the number of points grows large.

**breadth_first** : boolean (default = False)

    if True, then query the nodes in a breadth-first manner. Otherwise, query the nodes in a
    depth-first manner.

**sort_results** : boolean (default = True)

    if True, then distances and indices of each point are sorted on return, so that the first
    column contains the closest points. Otherwise, neighbors are returned in an arbitrary
    order.

**Returns i** : if return_distance == False

    (d,i) : if return_distance == True

    d : array of doubles - shape: x.shape[:-1] + (k,)

    each entry gives the list of distances to the neighbors of the corresponding point
i : array of integers - shape: x.shape[:-1] + (k,)
    each entry gives the list of indices of neighbors of the corresponding point

Examples

Query for k-nearest neighbors

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BinaryTree(X, leaf_size=2)
>>> dist, ind = tree.query(X[0], k=3)
>>> print(ind)  # indices of 3 closest neighbors
[0 3 1]
>>> print(dist)  # distances to 3 closest neighbors
[ 0. 0.19662693 0.29473397]
```

query_radius()

query_radius(self, X, r, count_only = False):
    query the tree for neighbors within a radius r

Parameters

- **X**: array-like, last dimension self.dim
  An array of points to query
- **r**: distance within which neighbors are returned
  r can be a single value, or an array of values of shape x.shape[:-1] if different radii are desired for each point.
- **count_only**: boolean (default = False)
  if True, return only the count of points within distance r If return_distance==True, setting count_only=True will result in an error.
- **sort_results**: boolean (default = False)
  if True, the distances and indices will be sorted before being returned. If False, the results will not be sorted. If return_distance == False, setting sort_results = True will result in an error.

Returns

- **count**: if count_only == True
  - **ind**: if count_only == False and return_distance == False
  - **(ind, dist)**: if count_only == False and return_distance == True
    - **count**: array of integers, shape = X.shape[:-1]
      each entry gives the number of neighbors within a distance r of the corresponding point.
    - **ind**: array of objects, shape = X.shape[:-1]
each element is a numpy integer array listing the indices of neighbors of the corresponding point. Note that unlike the results of a k-neighbors query, the returned neighbors are not sorted by distance by default.

**dist**: array of objects, shape = X.shape[:-1]
each element is a numpy double array listing the distances corresponding to indices in i.

**Examples**

Query for neighbors in a given radius

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((10, 3))  # 10 points in 3 dimensions
>>> tree = BinaryTree(X, leaf_size=2)
>>> print(tree.query_radius(X[0], r=0.3, count_only=True))
3
>>> ind = tree.query_radius(X[0], r=0.3)
>>> print(ind)  # indices of neighbors within distance 0.3
[3 0 1]
```

two_point_correlation()
Compute the two-point correlation function

**Parameters**

- **X**: array_like
  An array of points to query. Last dimension should match dimension of training data.
- **r**: array_like
  A one-dimensional array of distances
- **dualtree**: boolean (default = False)
  If true, use a dualtree algorithm. Otherwise, use a single-tree algorithm. Dual tree algorithms can have better scaling for large N.

**Returns**

- **counts**: ndarray
  counts[i] contains the number of pairs of points with distance less than or equal to r[i]

**Examples**

Compute the two-point autocorrelation function of X:

```python
>>> import numpy as np
>>> np.random.seed(0)
>>> X = np.random.random((30, 3))
>>> r = np.linspace(0, 1, 5)
>>> tree = BinaryTree(X)
>>> tree.two_point_correlation(X, r)
array([ 30,  62,  278,  580,  820])
```
# 30.27.4 sklearn.neighbors.KernelDensity

The class `sklearn.neighbors.KernelDensity` is used for Kernel Density Estimation. It is defined as follows:

```python
KernelDensity(bandwidth=1.0, algorithm='auto', kernel='gaussian', metric='euclidean', atol=0, rtol=0, breadth_first=True, leaf_size=40, metric_params=None)
```

## Parameters

- **bandwidth**: float
  - The bandwidth of the kernel.

- **algorithm**: string
  - The tree algorithm to use. Valid options are ['kd_tree', 'ball_tree', 'auto']. Default is 'auto'.

- **kernel**: string
  - The kernel to use. Valid kernels are ['gaussian', 'tophat', 'epanechnikov', 'exponential', 'linear', 'cosine']. Default is 'gaussian'.

- **metric**: string
  - The distance metric to use. Note that not all metrics are valid with all algorithms. Refer to the documentation of `BallTree` and `KDTree` for a description of available algorithms. Note that the normalization of the density output is correct only for the Euclidean distance metric. Default is 'euclidean'.

- **atol**: float
  - The desired absolute tolerance of the result. A larger tolerance will generally lead to faster execution. Default is 0.

- **rtol**: float
  - The desired relative tolerance of the result. A larger tolerance will generally lead to faster execution. Default is 1E-8.

- **breadth_first**: boolean
  - If true (default), use a breadth-first approach to the problem. Otherwise use a depth-first approach.

- **leaf_size**: int
  - Specify the leaf size of the underlying tree. See `BallTree` or `KDTree` for details. Default is 40.

- **metric_params**: dict
  - Additional parameters to be passed to the tree for use with the metric. For more information, see the documentation of `BallTree` or `KDTree`.

## Methods

- **fit(X[, y])**
  - Fit the Kernel Density model on the data.

- **get_params([deep])**
  - Get parameters for this estimator.

- **sample([n_samples, random_state])**
  - Generate random samples from the model.

- **score(X[, y])**
  - Compute the total log probability under the model.
Table 30.247 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>score_samples</code></td>
<td>Evaluate the density model on the data.</td>
</tr>
<tr>
<td><code>set_params</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__ (bandwidth=1.0, algorithm='auto', kernel='gaussian', metric='euclidean', atol=0, rtol=0, breadth_first=True, leaf_size=40, metric_params=None)
```

```python
fit (X, y=None)
```
- Fit the Kernel Density model on the data.

```python
Parameters

X : array_like, shape (n_samples, n_features)
```
- List of n_features-dimensional data points. Each row corresponds to a single data point.

```python
get_params (deep=True)
```
- Get parameters for this estimator.

```python
Parameters

deep : boolean, optional
```
- If True, will return the parameters for this estimator and contained subobjects that are estimators.

```python
Returns

params : mapping of string to any
```
- Parameter names mapped to their values.

```python
sample (n_samples=1, random_state=None)
```
- Generate random samples from the model.

```python
Parameters

n_samples : int, optional
```
- Number of samples to generate. Defaults to 1.

```python
random_state : int, RandomState instance or None. default to None
```
- If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

```python
Returns

X : array_like, shape (n_samples, n_features)
```
- List of samples.

```python
score (X, y=None)
```
- Compute the total log probability under the model.

```python
Parameters

X : array_like, shape (n_samples, n_features)
```
- List of n_features-dimensional data points. Each row corresponds to a single data point.

```python
Returns

logprob : float
```
- Total log-likelihood of the data in X.

```python
score_samples (X)
```
- Evaluate the density model on the data.

```python
Parameters

X : array_like, shape (n_samples, n_features)
```
- An array of points to query. Last dimension should match dimension of training data (n_features).

```python
Returns

density : ndarray, shape (n_samples,)
```
- The array of log(density) evaluations.
set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

Examples using sklearn.neighbors.KernelDensity

- Kernel Density Estimation
- Kernel Density Estimate of Species Distributions
- Simple 1D Kernel Density Estimation

30.27.5 sklearn.neighbors.KNeighborsClassifier

class sklearn.neighbors.KNeighborsClassifier(n_neighbors=5, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n_jobs=1, **kwargs)

Classifier implementing the k-nearest neighbors vote.

Read more in the User Guide.

Parameters

- n_neighbors : int, optional (default = 5)
  Number of neighbors to use by default for kneighbors queries.

- weights : str or callable, optional (default = 'uniform')
  weight function used in prediction. Possible values:
  - 'uniform': uniform weights. All points in each neighborhood are weighted equally.
  - 'distance': weight points by the inverse of their distance. In this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
  - [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

- algorithm : {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional
  Algorithm used to compute the nearest neighbors:
  - 'ball_tree' will use BallTree
  - 'kd_tree' will use KDTree
  - 'brute' will use a brute-force search.
  - 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

  Note: fitting on sparse input will override the setting of this parameter, using brute force.

- leaf_size : int, optional (default = 30)
Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

\( p \) : integer, optional (default = 2)

Power parameter for the Minkowski metric. When \( p = 1 \), this is equivalent to using manhattan_distance (\( l_1 \)), and euclidean_distance (\( l_2 \)) for \( p = 2 \). For arbitrary \( p \), minkowski_distance (\( l_p \)) is used.

\textbf{metric} : string or callable, default ‘minkowski’

the distance metric to use for the tree. The default metric is minkowski, and with \( p=2 \) is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.

\textbf{metric_params} : dict, optional (default = None)

Additional keyword arguments for the metric function.

\textbf{n_jobs} : int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If \(-1\), then the number of jobs is set to the number of CPU cores. Doesn’t affect \textit{fit} method.

See also:

\texttt{RadiusNeighborsClassifier, KNeighborsRegressor, RadiusNeighborsRegressor, NearestNeighbors}

Notes

See \textit{Nearest Neighbors} in the online documentation for a discussion of the choice of \texttt{algorithm} and \texttt{leaf_size}.

\textbf{Warning:} Regarding the Nearest Neighbors algorithms, if it is found that two neighbors, neighbor \( k+1 \) and \( k \), have identical distances but different labels, the results will depend on the ordering of the training data.


\textbf{Examples}

```python
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import KNeighborsClassifier
>>> neigh = KNeighborsClassifier(n_neighbors=3)
>>> neigh.fit(X, y)
KNeighborsClassifier(...)
>>> print(neigh.predict([[1.1]]))
[0]
>>> print(neigh.predict_proba([[0.9]]))
[[ 0.66666667  0.33333333]]
```
# Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X, y)</code></td>
<td>Fit the model using <code>X</code> as training data and <code>y</code> as target values</td>
</tr>
<tr>
<td><code>get_params()</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>kneighbors()</code></td>
<td>Finds the K-neighbors of a point.</td>
</tr>
<tr>
<td><code>kneighbors_graph()</code></td>
<td>Computes the (weighted) graph of k-Neighbors for points in <code>X</code></td>
</tr>
<tr>
<td><code>predict(X)</code></td>
<td>Predict the class labels for the provided data</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Return probability estimates for the test data <code>X</code>.</td>
</tr>
<tr>
<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__(n_neighbors=5, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n_jobs=1, **kwargs)
```

`fit (X, y)`
Fit the model using `X` as training data and `y` as target values

**Parameters**

`X` : {array-like, sparse matrix, BallTree, KDTree}
Training data. If array or matrix, shape `[n_samples, n_features]`, or `[n_samples, n_samples]` if metric=`'precomputed'`.

`y` : {array-like, sparse matrix}
Target values of shape = `[n_samples]` or `[n_samples, n_outputs]`

```python
get_params(deep=True)
```
Get parameters for this estimator.

**Parameters**

`deep` : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

`params` : mapping of string to any
Parameter names mapped to their values.

```python
kneighbors(X=None, n_neighbors=None, return_distance=True)
```
Finds the K-neighbors of a point.

**Parameters**

`X` : {array-like, sparse matrix, BallTree, KDTree}
The query point or points. If not provided, neighbors of each indexed point are returned.
In this case, the query point is not considered its own neighbor.

`n_neighbors` : int
Number of neighbors to get (default is the value passed to the constructor).

`return_distance` : boolean, optional. Defaults to True.
If False, distances will not be returned

**Returns**

`dist` : array
Array representing the lengths to points, only present if return_distance=True

**ind** : array

Indices of the nearest points in the population matrix.

**Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to [1,1,1]

```python
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[ 0.5]]), array([[2]]...))
```

As you can see, it returns [[0.5]], and [2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

```python
>>> X = [[0., 1., 0.], [1., 0., 1.]]
>>> neigh.kneighbors(X, return_distance=False)
array([[1],
       [2]]...)
```

**kneighbors_graph** *(X=None, n_neighbors=None, mode='connectivity')*

Computes the (weighted) graph of k-Neighbors for points in X

**Parameters**

- **X** : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == ‘precomputed’
  
The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

- **n_neighbors** : int
  
  Number of neighbors for each sample. (default is value passed to the constructor).

- **mode** : {'connectivity', 'distance'}, optional
  
  Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

**Returns**

- **A** : sparse matrix in CSR format, shape = [n_samples, n_samples_fit]

  n_samples_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

**See also:**

- `NearestNeighbors.radius_neighbors_graph`

**Examples**

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
```
```python
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 1.],
       [1., 0., 1.]])
```

### predict \((X)\)

Predict the class labels for the provided data

**Parameters**

- **X**: array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'
  - Test samples.

**Returns**

- **y**: array of shape [n_samples] or [n_samples, n_outputs]
  - Class labels for each data sample.

### predict_proba \((X)\)

Return probability estimates for the test data X.

**Parameters**

- **X**: array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'
  - Test samples.

**Returns**

- **p**: array of shape = [n_samples, n_classes], or a list of n_outputs of such arrays if n_outputs > 1. The class probabilities of the input samples. Classes are ordered by lexicographic order.

### score \((X, y, sample_weight=None)\)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**

- **score**: float
  - Mean accuracy of self.predict(X) wrt. y.

### set_params (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

---

30.27. **sklearn.neighbors**: Nearest Neighbors
Examples using `sklearn.neighbors.KNeighborsClassifier`

- Classifier comparison
- Plot the decision boundaries of a VotingClassifier
- Digits Classification Exercise
- Nearest Neighbors Classification
- Classification of text documents using sparse features

### 30.27.6 `sklearn.neighbors.KNeighborsRegressor`

The target is predicted by local interpolation of the targets associated of the nearest neighbors in the training set.

Read more in the [User Guide](#).

**Parameters**

- **`n_neighbors`**: int, optional (default = 5)
  Number of neighbors to use by default for `kneighbors` queries.

- **`weights`**: str or callable
  weight function used in prediction. Possible values:
  - ‘uniform’: uniform weights. All points in each neighborhood are weighted equally.
  - ‘distance’: weight points by the inverse of their distance. In this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
  - [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

  Uniform weights are used by default.

- **`algorithm`**: {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional
  Algorithm used to compute the nearest neighbors:
  - ‘ball_tree’ will use `BallTree`
  - ‘kd_tree’ will use `KDTree`
  - ‘brute’ will use a brute-force search.
  - ‘auto’ will attempt to decide the most appropriate algorithm based on the values passed to `fit` method.

  Note: fitting on sparse input will override the setting of this parameter, using brute force.

- **`leaf_size`**: int, optional (default = 30)
  Leaf size passed to `BallTree` or `KDTree`. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

- **`p`**: integer, optional (default = 2)
Power parameter for the Minkowski metric. When \( p = 1 \), this is equivalent to using manhattan_distance (\( l_1 \)), and euclidean_distance (\( l_2 \)) for \( p = 2 \). For arbitrary \( p \), minkowski_distance (\( l_p \)) is used.

**metric**: string or callable, default ‘minkowski’

The distance metric to use for the tree. The default metric is minkowski, and with \( p=2 \) is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.

**metric_params**: dict, optional (default = None)

Additional keyword arguments for the metric function.

**n_jobs**: int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores. Doesn’t affect fit method.

See also:

- NearestNeighbors
- RadiusNeighborsRegressor
- KNeighborsClassifier
- RadiusNeighborsClassifier

**Notes**

See Nearest Neighbors in the online documentation for a discussion of the choice of algorithm and leaf_size.

**Warning**: Regarding the Nearest Neighbors algorithms, if it is found that two neighbors, neighbor \( k+1 \) and \( k \), have identical distances but different labels, the results will depend on the ordering of the training data.


**Examples**

```python
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import KNeighborsRegressor
>>> neigh = KNeighborsRegressor(n_neighbors=2)
>>> neigh.fit(X, y)
KNeighborsRegressor(...)
>>> print(neigh.predict([[1.5]]))
[ 0.5]
```

**Methods**

- `fit(X, y)`  
  Fit the model using X as training data and y as target values

- `get_params([deep])`  
  Get parameters for this estimator.

- `kneighbors((X, n_neighbors, return_distance))`  
  Finds the K-neighbors of a point.
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<table>
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<th>Function</th>
<th>Description</th>
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<td>kneighbors_graph</td>
<td>Computes the (weighted) graph of k-Neighbors for points in X</td>
</tr>
<tr>
<td>predict</td>
<td>Predict the target for the provided data</td>
</tr>
<tr>
<td>score</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__ (n_neighbors=5, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, n_jobs=1, **kwargs)

fit (X, y)
Fit the model using X as training data and y as target values

Parameters X : {array-like, sparse matrix, BallTree, KDTree}
Training data. If array or matrix, shape [n_samples, n_features], or [n_samples, n_samples] if metric='precomputed'.

y : {array-like, sparse matrix}
Target values, array of float values, shape = [n_samples] or [n_samples, n_outputs]

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

kneighbors (X=None, n_neighbors=None, return_distance=True)
Finds the K-neighbors of a point.

Returns indices of and distances to the neighbors of each point.

Parameters X : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'
The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

n_neighbors : int
Number of neighbors to get (default is the value passed to the constructor).

return_distance : boolean, optional. Defaults to True.
If False, distances will not be returned

Returns dist : array
Array representing the lengths to points, only present if return_distance=True

ind : array
Indices of the nearest points in the population matrix.
Examples

In the following example, we construct a NeighborsClassifier class from an array representing our data set
and ask who’s the closest point to [1,1,1]

```python
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[ 0.5]]), array([[2]]))
```

As you can see, it returns [[0.5]], and [[2]], which means that the element is at distance 0.5 and is the third
element of samples (indexes start at 0). You can also query for multiple points:

```python
>>> X = [[0., 1., 0.], [1., 0., 1.]]
>>> neigh.kneighbors(X, return_distance=False)
array([[1], [2]])
```

kneighbors_graph (X=None, n_neighbors=None, mode='connectivity')

Computes the (weighted) graph of k-Neighbors for points in X

Parameters:
- X : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == ‘precomputed’
  The query point or points. If not provided, neighbors of each indexed point are returned.
  In this case, the query point is not considered its own neighbor.
- n_neighbors : int
  Number of neighbors for each sample. (default is value passed to the constructor).
  Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones
  and zeros, in ‘distance’ the edges are Euclidean distance between points.

Returns:
- A : sparse matrix in CSR format, shape = [n_samples, n_samples_fit]
  n_samples_fit is the number of samples in the fitted data A[i, j] is assigned the weight
  of edge that connects i to j.

See also:

NearestNeighbors.radius_neighbors_graph

Examples

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 0.],
       [0., 0., 1.]])
```
predict \( (X) \)
Predict the target for the provided data

**Parameters**

- \( X \) : array-like, shape \((n\_query, n\_features)\), or \((n\_query, n\_indexed)\) if \( \text{metric} == \text{‘precomputed’} \)
  - Test samples.

**Returns**

- \( y \) : array of int, shape \([n\_samples]\) or \([n\_samples, n\_outputs]\)
  - Target values

score \((X, y, \text{sample\_weight}=\text{None})\)
Returns the coefficient of determination \( R^2 \) of the prediction.

The coefficient \( R^2 \) is defined as \((1 - \frac{u}{v})\), where \( u \) is the residual sum of squares \(((y\_true - y\_pred) ** 2).\text{sum()}\) and \( v \) is the total sum of squares \(((y\_true - y\_true.mean()) ** 2).\text{sum()}\). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \( y \), disregarding the input features, would get a \( R^2 \) score of 0.0.

**Parameters**

- \( X \) : array-like, shape \((n\_samples, n\_features)\)
  - Test samples.
- \( y \) : array-like, shape \((n\_samples)\) or \((n\_samples, n\_outputs)\)
  - True values for \( X \).
- \( \text{sample\_weight} \) : array-like, shape \([n\_samples]\), optional
  - Sample weights.

**Returns**

- \( \text{score} \) : float
  - \( R^2 \) of \( self.\text{predict}(X) \) wrt. \( y \).

set_params (**params)**
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form \(<\text{component}>.\_<\text{parameter}>\) so that it’s possible to update each component of a nested object.

**Returns**

- \( self \)

**Examples using sklearn.neighbors.KNeighborsRegressor**

- Face completion with a multi-output estimators
- Nearest Neighbors regression

**30.27.7 sklearn.neighbors.LocalOutlierFactor**

**class**

```
sklearn.neighbors.LocalOutlierFactor (n_neighbors=20, algorithm=‘auto’,
leaf_size=30, metric=‘minkowski’, p=2,
metric_params=None, contamination=0.1,
n_jobs=1)
```

Unsupervised Outlier Detection using Local Outlier Factor (LOF)
The anomaly score of each sample is called Local Outlier Factor. It measures the local deviation of density of a given sample with respect to its neighbors. It is local in that the anomaly score depends on how isolated the object is with respect to the surrounding neighborhood. More precisely, locality is given by k-nearest neighbors, whose distance is used to estimate the local density. By comparing the local density of a sample to the local densities of its neighbors, one can identify samples that have a substantially lower density than their neighbors. These are considered outliers.

**Parameters**

**n_neighbors**: int, optional (default=20)
- Number of neighbors to use by default for knn queries. If n_neighbors is larger than the number of samples provided, all samples will be used.

**algorithm**: {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional
- Algorithm used to compute the nearest neighbors:
  - 'ball_tree' will use BallTree
  - 'kd_tree' will use KDTree
  - 'brute' will use a brute-force search.
  - 'auto' will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

**leaf_size**: int, optional (default=30)
- Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

**metric**: string or callable, default='minkowski'
- metric used for the distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.
- If 'precomputed', the training input X is expected to be a distance matrix.
- If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy’s metrics, but is less efficient than passing the metric name as a string.

Valid values for metric are:
- from scikit-learn: ['cityblock', 'cosine', 'euclidean', 'l1', 'l2', 'manhattan']

See the documentation for scipy.spatial.distance for details on these metrics: http://docs.scipy.org/doc/scipy/reference/spatial.distance.html

**p**: integer, optional (default=2)
- Parameter for the Minkowski metric from sklearn.metrics.pairwise.pairwise_distances. When p = 1, this is equivalent to using manhattan_distance (l1), and euclidean_distance (l2) for p = 2. For arbitrary p, minkowski_distance (l_p) is used.

**metric_params**: dict, optional (default=None)
Additional keyword arguments for the metric function.

**contamination** : float in (0., 0.5), optional (default=0.1)

The amount of contamination of the data set, i.e. the proportion of outliers in the data set. When fitting this is used to define the threshold on the decision function.

**n_jobs** : int, optional (default=1)

The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores. Affects only `kneighbors` and `kneighbors_graph` methods.

**Attributes**

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>negative_outlier_factor_</strong></td>
<td>(numpy array, shape (n_samples,)) The opposite LOF of the training samples. The lower, the more abnormal. Inliers tend to have a LOF score close to 1, while outliers tend to have a larger LOF score. The local outlier factor (LOF) of a sample captures its supposed ‘degree of abnormality’. It is the average of the ratio of the local reachability density of a sample and those of its k-nearest neighbors.</td>
</tr>
<tr>
<td><strong>n_neighbors_</strong></td>
<td>(integer) The actual number of neighbors used for <code>kneighbors</code> queries.</td>
</tr>
</tbody>
</table>

**References**

[R185185]

**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Fit the model using X as training data.</td>
</tr>
<tr>
<td><code>fit_predict(X[, y])</code></td>
<td>‘Fits the model to the training set X and returns the labels.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>kneighbors([X, n_neighbors, return_distance])</code></td>
<td>Finds the K-neighbors of a point.</td>
</tr>
<tr>
<td><code>kneighbors_graph([X, n_neighbors, mode])</code></td>
<td>Computes the (weighted) graph of k-Neighbors for points in X.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__ (n_neighbors=20, algorithm='auto', leaf_size=30, metric='minkowski', p=2, metric_params=None, contamination=0.1, n_jobs=1)
```

**fit (X, y=None)**

Fit the model using X as training data.

**Parameters**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>{array-like, sparse matrix, BallTree, KDTree}</td>
</tr>
</tbody>
</table>

Training data. If array or matrix, shape [n_samples, n_features], or [n_samples, n_samples] if metric='precomputed'.

**Returns**

<table>
<thead>
<tr>
<th>Return</th>
<th>Type</th>
</tr>
</thead>
<tbody>
<tr>
<td>self</td>
<td>object</td>
</tr>
</tbody>
</table>

Returns self.

**fit_predict (X, y=None)**

‘Fits the model to the training set X and returns the labels (1 inlier, -1 outlier) on the training set according
to the LOF score and the contamination parameter.

**Parameters**

- **X**: array-like, shape (n_samples, n_features), default=None
  The query sample or samples to compute the Local Outlier Factor w.r.t. to the training samples.

**Returns**

- **is_inlier**: array, shape (n_samples,)
  Returns -1 for anomalies/outliers and 1 for inliers.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**kneighbors** *(X=None, n_neighbors=None, return_distance=True)*

Finds the K-neighbors of a point.

**Returns**

- **dist**: array
  Array representing the lengths to points, only present if return_distance=True
- **ind**: array
  Indices of the nearest points in the population matrix.

**Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to [1,1,1]

```
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]]))
(array([[ 0.5]]), array([2]))
```
As you can see, it returns \([0.5]\), and \([2]\), which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

```python
>>> X = [[0., 1., 0.], [1., 0., 1.]]
>>> neigh.kneighbors(X, return_distance=False)
array([[1],
       [2]])
```

**kneighbors_graph** *(X=None, n_neighbors=None, mode='connectivity')*
Computes the (weighted) graph of k-Neighbors for points in X

- **Parameters**
  - **X** : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == ‘precomputed’
    - The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
  - **n_neighbors** : int
    - Number of neighbors for each sample. (default is value passed to the constructor).
  - **mode** : {'connectivity', 'distance'}, optional
    - Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

- **Returns**
  - **A** : sparse matrix in CSR format, shape = [n_samples, n_samples_fit]
    - n_samples_fit is the number of samples in the fitted data. A[i, j] is assigned the weight of edge that connects i to j.

See also:
- `NearestNeighbors.radius_neighbors_graph`

**Examples**

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 1.],
       [1., 0., 1.]]
```

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

- **Returns** self
Examples using sklearn.neighbors.LocalOutlierFactor

- Outlier detection with several methods.
- Anomaly detection with Local Outlier Factor (LOF)

30.27.8 sklearn.neighbors.RadiusNeighborsClassifier

class sklearn.neighbors.RadiusNeighborsClassifier:

Classifier implementing a vote among neighbors within a given radius

Parameters:
- radius : float, optional (default = 1.0)
  Range of parameter space to use by default for radius_neighbors queries.
- weights : str or callable
  weight function used in prediction. Possible values:
  - ‘uniform’ : uniform weights. All points in each neighborhood are weighted equally.
  - ‘distance’ : weight points by the inverse of their distance. In this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.
  - [callable] : a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

Uniform weights are used by default.
- algorithm : {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional
  Algorithm used to compute the nearest neighbors:
  - ‘ball_tree’ will use BallTree
  - ‘kd_tree’ will use KDTree
  - ‘brute’ will use a brute-force search.
  - ‘auto’ will attempt to decide the most appropriate algorithm based on the values passed to fit method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.
- leaf_size : int, optional (default = 30)
  Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.
- p : integer, optional (default = 2)
  Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan_distance (l1), and euclidean_distance (l2) for p = 2. For arbitrary p, minkowski_distance (l_p) is used.
- metric : string or callable, default ‘minkowski’
the distance metric to use for the tree. The default metric is minkowski, and with p=2
is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.

outlier_label : int, optional (default = None)

Label, which is given for outlier samples (samples with no neighbors on given radius).
If set to None, ValueError is raised, when outlier is detected.

metric_params : dict, optional (default = None)

Additional keyword arguments for the metric function.

See also:
KNeighborsClassifier, RadiusNeighborsRegressor, KNeighborsRegressor, NearestNeighbors

Notes

See Nearest Neighbors in the online documentation for a discussion of the choice of algorithm and leaf_size.


Examples

```python
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import RadiusNeighborsClassifier
>>> neigh = RadiusNeighborsClassifier(radius=1.0)
>>> neigh.fit(X, y)
RadiusNeighborsClassifier(...)
>>> print(neigh.predict([[1.5]]))
[0]
```

Methods

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<tr>
<th>Method</th>
<th>Description</th>
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</thead>
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<tr>
<td>fit(X, y)</td>
<td>Fit the model using X as training data and y as target values</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict the class labels for the provided data</td>
</tr>
<tr>
<td>radius_neighbors([X, radius, return_distance])</td>
<td>Finds the neighbors within a given radius of a point or points.</td>
</tr>
<tr>
<td>radius_neighbors_graph([X, radius, mode])</td>
<td>Computes the (weighted) graph of Neighbors for points in X</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__(radius=1.0, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', outlier_label=None, metric_params=None, **kwargs)
fit(X, y)
```
Fit the model using X as training data and y as target values

**Parameters**

- **X**: {array-like, sparse matrix, BallTree, KDTree}
  - Training data. If array or matrix, shape [n_samples, n_features], or [n_samples, n_samples] if metric='precomputed'.
- **y**: {array-like, sparse matrix}
  - Target values of shape = [n_samples] or [n_samples, n_outputs]

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**predict**(X)

Predict the class labels for the provided data

**Parameters**

- **X**: array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'
  - Test samples.

**Returns**

- **y**: array of shape [n_samples] or [n_samples, n_outputs]
  - Class labels for each data sample.

**radius_neighbors**(X=None, radius=None, return_distance=True)

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size radius around the points of the query array. Points lying on the boundary are included in the results.

The result points are not necessarily sorted by distance to their query point.

**Parameters**

- **X**: array-like, (n_samples, n_features), optional
  - The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.
- **radius**: float
  - Limiting distance of neighbors to return. (default is the value passed to the constructor).
- **return_distance**: boolean, optional. Defaults to True.
  - If False, distances will not be returned

**Returns**

- **dist**: array, shape (n_samples,) of arrays
  - Array representing the distances to each point, only present if return_distance=True. The distance values are computed according to the metric constructor parameter.
- **ind**: array, shape (n_samples,) of arrays
  - An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size radius around the query points.
Notes

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, `radius_neighbors` returns arrays of objects, where each object is a 1D array of indices or distances.

Examples

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to [1, 1, 1]:

```python
>>> import numpy as np

>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]

>>> from sklearn.neighbors import NearestNeighbors

>>> neigh = NearestNeighbors(radius=1.6)

>>> neigh.fit(samples)

NearestNeighbors(algorithm='auto', leaf_size=30, ...)

>>> rng = neigh.radius_neighbors([[1., 1., 1.]])

>>> print(np.asarray(rng[0][0]))

[1.5 0.5]

>>> print(np.asarray(rng[1][0]))

[1 2]
```

The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

`radius_neighbors_graph (X=None, radius=None, mode='connectivity')`

Computes the (weighted) graph of Neighbors for points in X

Neighborhoods are restricted the points at a distance lower than radius.

**Parameters**

- `X`: array-like, shape = [n_samples, n_features], optional
  
The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

- `radius`: float
  
  Radius of neighborhoods. (default is the value passed to the constructor).

- `mode`: {'connectivity', 'distance'}, optional
  
  Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

**Returns**

- `A`: sparse matrix in CSR format, shape = [n_samples, n_samples]
  
  A[i, j] is assigned the weight of edge that connects i to j.

**See also:**

`kneighbors_graph`

**Examples**

```python
>>> X = [[0], [3], [1]]

>>> from sklearn.neighbors import NearestNeighbors

>>> neigh = NearestNeighbors(radius=1.5)
```
```python
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.radius_neighbors_graph(X)
>>> A.toarray()
array([[ 1.,  0.,  1.],
       [ 0.,  1.,  0.],
       [ 1.,  0.,  1.]])
```

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters:
- **X**: array-like, shape = (n_samples, n_features)
  Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  Sample weights.

Returns:
- **score**: float
  Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

Returns:
- **self**: ...

### 30.27.9 sklearn.neighbors.RadiusNeighborsRegressor

**class** sklearn.neighbors.RadiusNeighborsRegressor *(radius=1.0, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, **kwargs)*

Regression based on neighbors within a fixed radius.

The target is predicted by local interpolation of the targets associated of the nearest neighbors in the training set.

Read more in the *User Guide*.

Parameters:
- **radius**: float, optional (default = 1.0)
  Range of parameter space to use by default for radius_neighbors queries.
- **weights**: str or callable
  weight function used in prediction. Possible values:
  - ‘uniform’: uniform weights. All points in each neighborhood are weighted equally.
• 'distance': weight points by the inverse of their distance. In this case, closer neighbors of a query point will have a greater influence than neighbors which are further away.

• [callable]: a user-defined function which accepts an array of distances, and returns an array of the same shape containing the weights.

Uniform weights are used by default.

**algorithm**: {'auto', 'ball_tree', 'kd_tree', 'brute'}, optional

Algorithm used to compute the nearest neighbors:

• 'ball_tree' will use `BallTree`

• 'kd_tree' will use `KDTree`

• 'brute' will use a brute-force search.

• 'auto' will attempt to decide the most appropriate algorithm based on the values passed to `fit` method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

**leaf_size**: int, optional (default = 30)

Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

**p**: integer, optional (default = 2)

Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan_distance (l1), and euclidean_distance (l2) for p = 2. For arbitrary p, minkowski_distance (l_p) is used.

**metric**: string or callable, default 'minkowski'

the distance metric to use for the tree. The default metric is minkowski, and with p=2 is equivalent to the standard Euclidean metric. See the documentation of the DistanceMetric class for a list of available metrics.

**metric_params**: dict, optional (default = None)

Additional keyword arguments for the metric function.

See also:

`NearestNeighbors`, `KNeighborsRegressor`, `KNeighborsClassifier`, `RadiusNeighborsClassifier`

**Notes**

See `Nearest Neighbors` in the online documentation for a discussion of the choice of `algorithm` and `leaf_size`.

Examples

```python
>>> X = [[0], [1], [2], [3]]
>>> y = [0, 0, 1, 1]
>>> from sklearn.neighbors import RadiusNeighborsRegressor
>>> neigh = RadiusNeighborsRegressor(radius=1.0)
>>> neigh.fit(X, y)
RadiusNeighborsRegressor(...)
>>> print(neigh.predict([[1.5]]))
[ 0.5]
```

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<td><code>radius_neighbors([X, radius, return_distance])</code></td>
<td>Finds the neighbors within a given radius of a point or points.</td>
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<td><code>radius_neighbors_graph([X, radius, mode])</code></td>
<td>Computes the (weighted) graph of Neighbors for points in X</td>
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<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
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```python
__init__(radius=1.0, weights='uniform', algorithm='auto', leaf_size=30, p=2, metric='minkowski', metric_params=None, **kwargs)
```
Test samples.

**Returns**  
```
y : array of int, shape = [n_samples] or [n_samples, n_outputs]
```
Target values

**radius_neighbors**  
```
(X=None, radius=None, return_distance=True)
```
Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size `radius` around the points of the query array. Points lying on the boundary are included in the results.

The result points are *not* necessarily sorted by distance to their query point.

**Parameters**  
```
X : array-like, (n_samples, n_features), optional
```
The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

```
radius : float
```
Limiting distance of neighbors to return. (default is the value passed to the constructor).

```
return_distance : boolean, optional. Defaults to True.
```
If False, distances will not be returned

**Returns**  
```
dist : array, shape (n_samples,) of arrays
```
Array representing the distances to each point, only present if `return_distance=True`. The distance values are computed according to the `metric` constructor parameter.

```
ind : array, shape (n_samples,) of arrays
```
An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size `radius` around the query points.

**Notes**

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, `radius_neighbors` returns arrays of objects, where each object is a 1D array of indices or distances.

**Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to `[1, 1, 1]`:

```python
>>> import numpy as np
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.6)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> rng = neigh.radius_neighbors([1., 1., 1.])
>>> print(np.asarray(rng[0][0]))
[ 1.5 0.5]
>>> print(np.asarray(rng[1][0]))
[1 2]
```
The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

`radius_neighbors_graph` \(X=None, \ radius=None, \ mode='connectivity'\)

Computes the (weighted) graph of Neighbors for points in \(X\)

Neighborhoods are restricted the points at a distance lower than \(radius\).

**Parameters**
- \(X\) : array-like, shape = [n_samples, n_features], optional
  - The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

- \(radius\) : float
  - Radius of neighborhoods. (default is the value passed to the constructor).

- \(mode\) : {'connectivity', 'distance'}, optional
  - Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

**Returns**
- \(A\) : sparse matrix in CSR format, shape = [n_samples, n_samples]
  - \(A[i, j]\) is assigned the weight of edge that connects \(i\) to \(j\).

See also:
- `kneighbors_graph`

**Examples**

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.5)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.radius_neighbors_graph(X)
>>> A.toarray()
array([[0., 1., 1.],
        [1., 0., 0.],
        [1., 0., 0.]])
```

`score` \((X, y, \ sample_weight=None)\)

Returns the coefficient of determination \(R^2\) of the prediction.

The coefficient \(R^2\) is defined as \((1 - \frac{u}{v})\), where \(u\) is the residual sum of squares \(((y\_true - y\_pred) ** 2).sum()\) and \(v\) is the total sum of squares \(((y\_true - y\_true.mean()) ** 2).sum()\). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of \(y\), disregarding the input features, would get a \(R^2\) score of 0.0.

**Parameters**
- \(X\) : array-like, shape = (n_samples, n_features)
  - Test samples.

- \(y\) : array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True values for \(X\).

- \(sample\_weight\) : array-like, shape = [n_samples], optional
  - Sample weights.
Returns score : float
R^2 of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it's possible to update each component of a nested object.

Returns self

30.27.10 sklearn.neighbors.NearestCentroid

class sklearn.neighbors.NearestCentroid(metric='euclidean', shrink_threshold=None)
Nearest centroid classifier.

Each class is represented by its centroid, with test samples classified to the class with the nearest centroid.

Read more in the User Guide.

Parameters metric : string, or callable
The metric to use when calculating distance between instances in a feature array. If metric is a string or callable, it must be one of the options allowed by metrics.pairwise.pairwise_distances for its metric parameter. The centroids for the samples corresponding to each class is the point from which the sum of the distances (according to the metric) of all samples that belong to that particular class are minimized. If the “manhattan” metric is provided, this centroid is the median and for all other metrics, the centroid is now set to be the mean.

shrink_threshold : float, optional (default = None)
Threshold for shrinking centroids to remove features.

Attributes

centroids_ (array-like, shape = [n_classes, n_features]) Centroid of each class

See also:

sklearn.neighbors.KNeighborsClassifier nearest neighbors classifier

Notes

When used for text classification with tf-idf vectors, this classifier is also known as the Rocchio classifier.

References

Examples

```python
>>> from sklearn.neighbors.nearest_centroid import NearestCentroid
>>> import numpy as np

>>> X = np.array([[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]])

>>> y = np.array([1, 1, 1, 2, 2, 2])

>>> clf = NearestCentroid()

>>> clf.fit(X, y)
NearestCentroid(metric='euclidean', shrink_threshold=None)

>>> print(clf.predict([[-0.8, -1]]))
[1]
```

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<td>Fit the NearestCentroid model according to the given training data.</td>
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<td><strong>get_params</strong>(deep)</td>
<td>Get parameters for this estimator.</td>
</tr>
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<td><strong>predict</strong>(X)</td>
<td>Perform classification on an array of test vectors X.</td>
</tr>
<tr>
<td><strong>score</strong>(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td><strong>set_params</strong>(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
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</table>

**init**(metric='euclidean', shrink_threshold=None)

**fit**(X, y)

Fit the NearestCentroid model according to the given training data.

**Parameters**

- X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  - Training vector, where n_samples is the number of samples and n_features is the number of features. Note that centroid shrinking cannot be used with sparse matrices.

- y : array, shape = [n_samples]
  - Target values (integers)

**get_params**(deep=**False**)

Get parameters for this estimator.

**Parameters**

- deep : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- params : mapping of string to any
  - Parameter names mapped to their values.

**predict**(X)

Perform classification on an array of test vectors X.

The predicted class C for each sample in X is returned.

**Parameters**

- X : array-like, shape = [n_samples, n_features]

**Returns**

- C : array, shape = [n_samples]
Notes

If the metric constructor parameter is “precomputed”, X is assumed to be the distance matrix between the
data to be predicted and self.centroids_.

score (X, y, sample_weight=None)
Returns the mean accuracy on the given test data and labels.
In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters X : array-like, shape = (n_samples, n_features)
Test samples.
y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.
sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns score : float
Mean accuracy of self.predict(X) wrt. y.

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

Examples using sklearn.neighbors.NearestCentroid

• Nearest Centroid Classification
• Classification of text documents using sparse features

30.27.11 sklearn.neighbors.NearestNeighbors
class sklearn.neighbors.NearestNeighbors (n_neighbors=5, radius=1.0, algorithm='auto', leaf_size=30, metric='minkowski', p=2, metric_params=None, n_jobs=1, **kwargs)
Unsupervised learner for implementing neighbor searches.
Read more in the User Guide.

Parameters n_neighbors : int, optional (default = 5)
Number of neighbors to use by default for kneighbors queries.
radius : float, optional (default = 1.0)
Range of parameter space to use by default for radius_neighbors queries.
Algorithm used to compute the nearest neighbors:
• ‘ball_tree’ will use \textit{BallTree}
• ‘kd_tree’ will use \textit{KDTree}
• ‘brute’ will use a brute-force search.
• ‘auto’ will attempt to decide the most appropriate algorithm based on the values passed to \textit{fit} method.

Note: fitting on sparse input will override the setting of this parameter, using brute force.

\textbf{leaf\textunderscore size} : int, optional (default = 30)

Leaf size passed to BallTree or KDTree. This can affect the speed of the construction and query, as well as the memory required to store the tree. The optimal value depends on the nature of the problem.

\textbf{metric} : string or callable, default ‘minkowski’

metric to use for distance computation. Any metric from scikit-learn or scipy.spatial.distance can be used.

If metric is a callable function, it is called on each pair of instances (rows) and the resulting value recorded. The callable should take two arrays as input and return one value indicating the distance between them. This works for Scipy’s metrics, but is less efficient than passing the metric name as a string.

Distance matrices are not supported.

Valid values for metric are:

• from scikit-learn: ['cityblock', 'cosine', 'euclidean', 'l1', 'l2', 'manhattan']
• from scipy.spatial.distance: ['braycurtis', 'canberra', 'chebyshev', 'correlation', 'dice', 'hamming', 'jaccard', 'kulsinski', 'mahalanobis', 'minkowski', 'rogerstanimoto', 'russellrao', 'seuclidean', 'sokalmichener', 'sokalsneath', 'sqeuclidean', 'yule']

See the documentation for scipy.spatial.distance for details on these metrics.

\textbf{p} : integer, optional (default = 2)

Parameter for the Minkowski metric from sklearn.metrics.pairwise.pairwise_distances. When \( p = 1 \), this is equivalent to using manhattan\_distance (l1), and euclidean\_distance (l2) for \( p = 2 \). For arbitrary \( p \), minkowski\_distance (l\( _p \)) is used.

\textbf{metric\_params} : dict, optional (default = None)

Additional keyword arguments for the metric function.

\textbf{n\_jobs} : int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If \(-1\), then the number of jobs is set to the number of CPU cores. Affects only \textit{kneighbors} and \textit{kneighbors\_graph} methods.

\textbf{See also:}

\textit{KNeighborsClassifier}, \textit{RadiusNeighborsClassifier}, \textit{KNeighborsRegressor}, \textit{RadiusNeighborsRegressor}, \textit{BallTree}
Notes

See Nearest Neighbors in the online documentation for a discussion of the choice of algorithm and leaf_size.


Examples

```python
>>> import numpy as np
>>> from sklearn.neighbors import NearestNeighbors
>>> samples = [[0, 0, 2], [1, 0, 0], [0, 0, 1]]

>>> neigh = NearestNeighbors(2, 0.4)
>>> neigh.fit(samples)
NearestNeighbors(...)

>>> neigh.kneighbors([[0, 0, 1.3]], 2, return_distance=False)
...
array([[2, 0]])...

>>> nbrs = neigh.radius_neighbors([[0, 0, 1.3]], 0.4, return_distance=False)
>>> np.asarray(nbrs[0][0])
array(2)
```

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<td>Get parameters for this estimator.</td>
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<td><code>kneighbors([X, n_neighbors, return_distance])</code></td>
<td>Finds the K-neighbors of a point.</td>
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<td><code>kneighbors_graph([X, n_neighbors, mode])</code></td>
<td>Computes the (weighted) graph of k-Neighbors for points in X.</td>
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<tr>
<td><code>radius_neighbors([X, radius, return_distance])</code></td>
<td>Finds the neighbors within a given radius of a point or points.</td>
</tr>
<tr>
<td><code>radius_neighbors_graph([X, radius, mode])</code></td>
<td>Computes the (weighted) graph of Neighbors for points in X.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
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__init__ (n_neighbors=5, radius=1.0, algorithm='auto', leaf_size=30, metric='minkowski', p=2, metric_params=None, n_jobs=1, **kwargs)

fit (X, y=None)
Fit the model using X as training data

Parameters X : {array-like, sparse matrix, BallTree, KDTree }
Training data. If array or matrix, shape [n_samples, n_features], or [n_samples, n_samples] if metric='precomputed'.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any  
Parameter names mapped to their values.

**kneighbors** *(X=None, n_neighbors=None, return_distance=True)*  
Finds the K-neighbors of a point.

Returns indices of and distances to the neighbors of each point.

**Parameters**  
X : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'  
The query point or points. If not provided, neighbors of each indexed point are returned.  
In this case, the query point is not considered its own neighbor.

n_neighbors : int  
Number of neighbors to get (default is the value passed to the constructor).

return_distance : boolean, optional. Defaults to True.  
If False, distances will not be returned

Returns  
dist : array  
Array representing the lengths to points, only present if return_distance=True

ind : array  
Indices of the nearest points in the population matrix.

**Examples**

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to [1,1,1]

```python
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=1)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> print(neigh.kneighbors([[1., 1., 1.]])
(array([[ 0.5]]), array([[2]]...))
```

As you can see, it returns [[0.5]], and [2]], which means that the element is at distance 0.5 and is the third element of samples (indexes start at 0). You can also query for multiple points:

```python
>>> X = [[0., 1., 0.], [1., 0., 1.]]
>>> neigh.kneighbors(X, return_distance=False)
array([[1]],
      [2]]...)
```

**kneighbors_graph** *(X=None, n_neighbors=None, mode='connectivity')*  
Computes the (weighted) graph of k-Neighbors for points in X

**Parameters**  
X : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == 'precomputed'
The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

\textbf{n_neighbors} : int

Number of neighbors for each sample. (default is value passed to the constructor).

\textbf{mode} : \{'connectivity’, ‘distance’\}, optional

Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

\textbf{Returns} A : sparse matrix in CSR format, shape = [n_samples, n_samples_fit]

n_samples_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

See also:

\textbf{NearestNeighbors.radius_neighbors_graph}

Examples

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 1.],
       [1., 0., 1.]])
```

\textbf{radius_neighbors (X=None, radius=None, return_distance=True)}

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of each point from the dataset lying in a ball with size \textit{radius} around the points of the query array. Points lying on the boundary are included in the results.

The result points are not necessarily sorted by distance to their query point.

\textbf{Parameters} X : array-like, (n_samples, n_features), optional

The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

\textbf{radius} : float

Limiting distance of neighbors to return. (default is the value passed to the constructor).

\textbf{return_distance} : boolean, optional. Defaults to True.

If False, distances will not be returned

\textbf{Returns} dist : array, shape (n_samples,) of arrays

Array representing the distances to each point, only present if return_distance=True. The distance values are computed according to the \textit{metric} constructor parameter.

\textbf{ind} : array, shape (n_samples,) of arrays
An array of arrays of indices of the approximate nearest points from the population matrix that lie within a ball of size radius around the query points.

Notes

Because the number of neighbors of each point is not necessarily equal, the results for multiple query points cannot be fit in a standard data array. For efficiency, radius_neighbors returns arrays of objects, where each object is a 1D array of indices or distances.

Examples

In the following example, we construct a NeighborsClassifier class from an array representing our data set and ask who’s the closest point to [1, 1, 1]:

```python
>>> import numpy as np
>>> samples = [[0., 0., 0.], [0., .5, 0.], [1., 1., .5]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.6)
>>> neigh.fit(samples)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> rng = neigh.radius_neighbors([[1., 1., 1.]])
>>> print(np.asarray(rng[0][0]))
[ 1.5 0.5]
>>> print(np.asarray(rng[1][0]))
[1 2]
```

The first array returned contains the distances to all points which are closer than 1.6, while the second array returned contains their indices. In general, multiple points can be queried at the same time.

radius_neighbors_graph (X=None, radius=None, mode='connectivity')

Computes the (weighted) graph of Neighbors for points in X

Neighborhoods are restricted the points at a distance lower than radius.

Parameters

- **X**: array-like, shape = [n_samples, n_features], optional
  The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

- **radius**: float
  Radius of neighborhoods. (default is the value passed to the constructor).

- **mode**: {‘connectivity’, ‘distance’}, optional
  Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

Returns

- **A**: sparse matrix in CSR format, shape = [n_samples, n_samples]
  A[i, j] is assigned the weight of edge that connects i to j.

See also:

kneighbors_graph
Examples

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.5)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.radius_neighbors_graph(X)
>>> A.toarray()
array([[ 1.,  0.,  1.],
       [ 0.,  1.,  0.],
       [ 1.,  0.,  1.]])
```

```
set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns
self
```

```
neighbors.kneighbors_graph(X, n_neighbors, ...)

Computes the (weighted) graph of k-Neighbors for points in X
```

```
neighbors.radius_neighbors_graph(X, radius)

Computes the (weighted) graph of Neighbors for points in X
```

### 30.27.12 sklearn.neighbors.kneighbors_graph

```
sklearn.neighbors.kneighbors_graph(X, n_neighbors, mode='connectivity', metric='minkowski', p=2, metric_params=None, include_self=False, n_jobs=1)
```

Computes the (weighted) graph of k-Neighbors for points in X

Read more in the User Guide.

**Parameters**

- `X`: array-like or BallTree, shape = [n_samples, n_features]
  Sample data, in the form of a numpy array or a precomputed BallTree.

- `n_neighbors`: int
  Number of neighbors for each sample.

- `mode`: {'connectivity', 'distance'}, optional
  Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, and ‘distance’ will return the distances between neighbors according to the given metric.

- `metric`: string, default ‘minkowski’
  The distance metric used to calculate the k-Neighbors for each sample point. The DistanceMetric class gives a list of available metrics. The default distance is ‘euclidean’ (‘minkowski’ metric with the p param equal to 2.)

- `p`: int, default 2
Power parameter for the Minkowski metric. When $p = 1$, this is equivalent to using manhattan_distance (l1), and euclidean_distance (l2) for $p = 2$. For arbitrary $p$, minkowski_distance ($l_p$) is used.

**metric_params** : dict, optional
additional keyword arguments for the metric function.

**include_self** : bool, default=False.
Whether or not to mark each sample as the first nearest neighbor to itself. If None, then True is used for mode='connectivity' and False for mode='distance' as this will preserve backwards compatibility.

**n_jobs** : int, optional (default = 1)
The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores.

**Returns**
A : sparse matrix in CSR format, shape = [n_samples, n_samples]
A[i, j] is assigned the weight of edge that connects i to j.

See also:

radius_neighbors_graph

**Examples**

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import kneighbors_graph
>>> A = kneighbors_graph(X, 2, mode='connectivity', include_self=True)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 1.],
       [1., 0., 1.]])
```

Examples using sklearn.neighbors.kneighbors_graph

- Agglomerative clustering with and without structure
- Hierarchical clustering: structured vs unstructured ward
- Comparing different clustering algorithms on toy datasets

**30.27.13 sklearn.neighbors.radius_neighbors_graph**

sklearn.neighbors.radius_neighbors_graph(X, radius, mode='connectivity', metric='minkowski', p=2, metric_params=None, include_self=False, n_jobs=1)

Computes the (weighted) graph of Neighbors for points in X
Neighborhoods are restricted the points at a distance lower than radius.
Read more in the User Guide.

**Parameters**

- **X** : array-like or BallTree, shape = [n_samples, n_features]
  Sample data, in the form of a numpy array or a precomputed BallTree.
**radius**: float

Radius of neighborhoods.

**mode**: {'connectivity', 'distance'}, optional

Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, and 'distance' will return the distances between neighbors according to the given metric.

**metric**: string, default 'minkowski'

The distance metric used to calculate the neighbors within a given radius for each sample point. The DistanceMetric class gives a list of available metrics. The default distance is 'euclidean' ('minkowski' metric with the param equal to 2.)

**p**: int, default 2

Power parameter for the Minkowski metric. When p = 1, this is equivalent to using manhattan_distance (l1), and euclidean_distance (l2) for p = 2. For arbitrary p, minkowski_distance (l_p) is used.

**metric_params**: dict, optional

additional keyword arguments for the metric function.

**include_self**: bool, default=False

Whether or not to mark each sample as the first nearest neighbor to itself. If None, then True is used for mode='connectivity' and False for mode='distance' as this will preserve backwards compatibility.

**n_jobs**: int, optional (default = 1)

The number of parallel jobs to run for neighbors search. If -1, then the number of jobs is set to the number of CPU cores.

**Returns**

A : sparse matrix in CSR format, shape = [n_samples, n_samples]

A[i, j] is assigned the weight of edge that connects i to j.

See also:

kneighbors_graph

**Examples**

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import radius_neighbors_graph
>>> A = radius_neighbors_graph(X, 1.5, mode='connectivity', include_self=True)
>>> A.toarray()
array([[1., 0., 1.],
       [0., 1., 0.],
       [1., 0., 1.]])
```

**30.28 sklearn.neural_network: Neural network models**

The `sklearn.neural_network` module includes models based on neural networks.
User guide: See the *Neural network models (supervised)* and *Neural network models (unsupervised)* sections for further details.

```
neural_network.BernoulliRBM([n_components, ...
neural_network.MLPClassifier([...])     Multi-layer Perceptron classifier.
neural_network.MLPRegressor([...])       Multi-layer Perceptron regressor.
```

### 30.28.1 sklearn.neural_network.BernoulliRBM

**class** `sklearn.neural_network.BernoulliRBM(n_components=256, learning_rate=0.1, batch_size=10, n_iter=10, verbose=0, random_state=None)`  
Bernoulli Restricted Boltzmann Machine (RBM).

A Restricted Boltzmann Machine with binary visible units and binary hidden units. Parameters are estimated using Stochastic Maximum Likelihood (SML), also known as Persistent Contrastive Divergence (PCD) [2].

The time complexity of this implementation is $O(d \times 2)$ assuming $d \sim n_{\text{features}} \sim n_{\text{components}}$.

Read more in the *User Guide*.

**Parameters**

- **n_components**: int, optional  
  Number of binary hidden units.

- **learning_rate**: float, optional  
  The learning rate for weight updates. It is *highly* recommended to tune this hyper-parameter. Reasonable values are in the $10^{0 \ldots -3}$ range.

- **batch_size**: int, optional  
  Number of examples per minibatch.

- **n_iter**: int, optional  
  Number of iterations/sweeps over the training dataset to perform during training.

- **verbose**: int, optional  
  The verbosity level. The default, zero, means silent mode.

- **random_state**: integer or numpy.RandomState, optional  
  A random number generator instance to define the state of the random permutations generator. If an integer is given, it fixes the seed. Defaults to the global numpy random number generator.

**Attributes**

- **intercept_hidden**: (array-like, shape (n_components,))  
  Biases of the hidden units.

- **intercept_visible**: (array-like, shape (n_features,))  
  Biases of the visible units.

- **components**: (array-like, shape (n_components, n_features))  
  Weight matrix, where n_features in the number of visible units and n_components is the number of hidden units.
References


Examples

```python
>>> import numpy as np
>>> from sklearn.neural_network import BernoulliRBM

>>> X = np.array([[0, 0, 0], [0, 1, 1], [1, 0, 1], [1, 1, 1]])
>>> model = BernoulliRBM(n_components=2)

>>> model.fit(X)
```

Methods

- `fit(X[, y])`: Fit the model to the data X.
- `fit_transform(X[, y])`: Fit to data, then transform it.
- `get_params([deep])`: Get parameters for this estimator.
- `gibbs(v)`: Perform one Gibbs sampling step.
- `partial_fit(X[, y])`: Fit the model to the data X which should contain a partial segment of the data.
- `score_samples(X)`: Compute the pseudo-likelihood of X.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(X)`: Compute the hidden layer activation probabilities, $P(h=1|v=X)$.

```
__init__(n_components=256, learning_rate=0.1, batch_size=10, n_iter=10, verbose=0, random_state=None)

fit (X, y=None)
Fit the model to the data X.

Parameters X : {array-like, sparse matrix} shape (n_samples, n_features)
   Training data.

Returns self : BernoulliRBM
   The fitted model.

fit_transform (X, y=None, **fit_params)
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]
   Training set.

y : numpy array of shape [n_samples]
Target values.

**Returns X_new**: numpy array of shape [n_samples, n_features_new]

Transformed array.

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  
  Parameter names mapped to their values.

**gibbs** *(v)*
Perform one Gibbs sampling step.

**Parameters**
- **v**: array-like, shape (n_samples, n_features)
  Values of the visible layer to start from.

**Returns**
- **v_new**: array-like, shape (n_samples, n_features)
  Values of the visible layer after one Gibbs step.

**partial_fit** *(X, y=None)*
Fit the model to the data X which should contain a partial segment of the data.

**Parameters**
- **X**: array-like, shape (n_samples, n_features)
  Training data.

**Returns**
- **self**: BernoulliRBM
  
  The fitted model.

**score_samples** *(X)*
Compute the pseudo-likelihood of X.

**Parameters**
- **X**: {array-like, sparse matrix} shape (n_samples, n_features)
  Values of the visible layer. Must be all-boolean (not checked).

**Returns**
- **pseudo_likelihood**: array-like, shape (n_samples,)
  Value of the pseudo-likelihood (proxy for likelihood).

**Notes**

This method is not deterministic: it computes a quantity called the free energy on X, then on a randomly corrupted version of X, and returns the log of the logistic function of the difference.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**
- **self**
**transform** ($X$)
Compute the hidden layer activation probabilities, $P(h=1|v=X)$.

**Parameters**
- **X**: {array-like, sparse matrix} shape (n_samples, n_features)
  
The data to be transformed.

**Returns**
- **h**: array, shape (n_samples, n_components)
  
  Latent representations of the data.

---

**Examples using sklearn.neural_network.BernoulliRBM**

- *Restricted Boltzmann Machine features for digit classification*

---

### 30.28.2 sklearn.neural_network.MLPClassifier

**class sklearn.neural_network.MLPClassifier**(hidden_layer_sizes=(100, ), activation='relu', solver='adam', alpha=0.0001, batch_size='auto', learning_rate='constant', learning_rate_init=0.001, power_t=0.5, max_iter=200, shuffle=True, random_state=None, tol=0.0001, verbose=False, warm_start=False, momentum=0.9, nesterovs_momentum=True, early_stopping=False, validation_fraction=0.1, beta_1=0.9, beta_2=0.999, epsilon=1e-08, n_iter_no_change=10)

Multi-layer Perceptron classifier.

This model optimizes the log-loss function using LBFGS or stochastic gradient descent.

New in version 0.18.

**Parameters**
- **hidden_layer_sizes**: tuple, length = n_layers - 2, default (100,)
  
  The ith element represents the number of neurons in the ith hidden layer.

- **activation**: {'identity', 'logistic', 'tanh', 'relu'}, default 'relu'
  
  Activation function for the hidden layer.
  - 'identity', no-op activation, useful to implement linear bottleneck, returns $f(x) = x$
  - 'logistic', the logistic sigmoid function, returns $f(x) = 1 / (1 + \exp(-x))$.
  - 'tanh', the hyperbolic tan function, returns $f(x) = \tanh(x)$.
  - 'relu', the rectified linear unit function, returns $f(x) = \max(0, x)$

- **solver**: {'lbfgs', 'sgd', 'adam'}, default 'adam'
  
  The solver for weight optimization.
  - 'lbfgs' is an optimizer in the family of quasi-Newton methods.
  - 'sgd' refers to stochastic gradient descent.
  - 'adam' refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba
Note: The default solver ‘adam’ works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, ‘lbfgs’ can converge faster and perform better.

**alpha**: float, optional, default 0.0001

L2 penalty (regularization term) parameter.

**batch_size**: int, optional, default ‘auto’

Size of minibatches for stochastic optimizers. If the solver is ‘lbfgs’, the classifier will not use minibatch. When set to ‘auto’, batch_size=min(200, n_samples)

**learning_rate**: {'constant', 'invscaling', 'adaptive'}, default ‘constant’

Learning rate schedule for weight updates.

- ‘constant’ is a constant learning rate given by ‘learning_rate_init’.
- ‘invscaling’ gradually decreases the learning rate learning_rate at each time step ‘t’ using an inverse scaling exponent of ‘power_t’. effective_learning_rate = learning_rate_init / pow(t, power_t)
- ‘adaptive’ keeps the learning rate constant to ‘learning_rate_init’ as long as training loss keeps decreasing. Each time two consecutive epochs fail to decrease training loss by at least tol, or fail to increase validation score by at least tol if ‘early_stopping’ is on, the current learning rate is divided by 5.

Only used when solver='sgd'.

**learning_rate_init**: double, optional, default 0.001

The initial learning rate used. It controls the step-size in updating the weights. Only used when solver='sgd' or 'adam'.

**power_t**: double, optional, default 0.5

The exponent for inverse scaling learning rate. It is used in updating effective learning rate when the learning_rate is set to ‘invscaling’. Only used when solver='sgd'.

**max_iter**: int, optional, default 200

Maximum number of iterations. The solver iterates until convergence (determined by ‘tol’) or this number of iterations. For stochastic solvers (‘sgd’, ‘adam’), note that this determines the number of epochs (how many times each data point will be used), not the number of gradient steps.

**shuffle**: bool, optional, default True

Whether to shuffle samples in each iteration. Only used when solver='sgd' or 'adam'.

**random_state**: int, RandomState instance or None, optional, default None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**tol**: float, optional, default 1e-4

Tolerance for the optimization. When the loss or score is not improving by at least tol for n_iter_no_change consecutive iterations, unless learning_rate is set to ‘adaptive’, convergence is considered to be reached and training stops.

**verbose**: bool, optional, default False

Whether to print progress messages to stdout.
**warm_start** : bool, optional, default False

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**momentum** : float, default 0.9

Momentum for gradient descent update. Should be between 0 and 1. Only used when solver='sgd'.

**nesterovs_momentum** : boolean, default True

Whether to use Nesterov’s momentum. Only used when solver='sgd' and momentum > 0.

**early_stopping** : bool, default False

Whether to use early stopping to terminate training when validation score is not improving. If set to true, it will automatically set aside 10% of training data as validation and terminate training when validation score is not improving by at least tol for n_iter_no_change consecutive epochs. Only effective when solver='sgd' or 'adam'

**validation_fraction** : float, optional, default 0.1

The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early_stopping is True

**beta_1** : float, optional, default 0.9

Exponential decay rate for estimates of first moment vector in adam, should be in [0, 1). Only used when solver='adam'

**beta_2** : float, optional, default 0.999

Exponential decay rate for estimates of second moment vector in adam, should be in [0, 1). Only used when solver='adam'

**epsilon** : float, optional, default 1e-8

Value for numerical stability in adam. Only used when solver='adam'

**n_iter_no_change** : int, optional, default 10

Maximum number of epochs to not meet tol improvement. Only effective when solver='sgd' or 'adam'

New in version 0.20.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>classes_</td>
<td>(array or list of array of shape (n_classes,)) Class labels for each output.</td>
</tr>
<tr>
<td>loss_</td>
<td>(float) The current loss computed with the loss function.</td>
</tr>
<tr>
<td>coefs_</td>
<td>(list, length n_layers - 1) The ith element in the list represents the weight matrix corresponding to layer i.</td>
</tr>
<tr>
<td>intercepts_</td>
<td>(list, length n_layers - 1) The ith element in the list represents the bias vector corresponding to layer i + 1.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int,) The number of iterations the solver has ran.</td>
</tr>
<tr>
<td>n_layers_</td>
<td>(int) Number of layers.</td>
</tr>
<tr>
<td>n_outputs_</td>
<td>(int) Number of outputs.</td>
</tr>
<tr>
<td>out_activation</td>
<td>(string) Name of the output activation function.</td>
</tr>
</tbody>
</table>
### Notes

MLPClassifier trains iteratively since at each time step the partial derivatives of the loss function with respect to the model parameters are computed to update the parameters.

It can also have a regularization term added to the loss function that shrinks model parameters to prevent over-fitting.

This implementation works with data represented as dense numpy arrays or sparse scipy arrays of floating point values.

### References


### Methods

- **`fit(X, y)`**
  - Fit the model to data matrix X and target(s) y.

- **`get_params([deep])`**
  - Get parameters for this estimator.

- **`predict(X)`**
  - Predict using the multi-layer perceptron classifier.

- **`predict_log_proba(X)`**
  - Return the log of probability estimates.

- **`predict_proba(X)`**
  - Probability estimates.

- **`score(X, y[, sample_weight])`**
  - Returns the mean accuracy on the given test data and labels.

- **`set_params(**params)`**
  - Set the parameters of this estimator.

```python
__init__(hidden_layer_sizes=(100,), activation='relu', solver='adam', alpha=0.0001, batch_size='auto', learning_rate='constant', learning_rate_init=0.001, power_t=0.5, max_iter=200, shuffle=True, random_state=None, tol=0.0001, verbose=False, warm_start=False, momentum=0.9, nesterovs_momentum=True, early_stopping=False, validation_fraction=0.1, beta_1=0.9, beta_2=0.999, epsilon=1e-08, n_iter_no_change=10)
```

**`fit (X, y)`**

Fit the model to data matrix X and target(s) y.

**Parameters**

- **X**: array-like or sparse matrix, shape (n_samples, n_features)
  - The input data.

- **y**: array-like, shape (n_samples,) or (n_samples, n_outputs)
  - The target values (class labels in classification, real numbers in regression).

**Returns**

- **self**: returns a trained MLP model.

**`get_params`**(deep=True)
Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  
  Parameter names mapped to their values.

### partial_fit

Fit the model to data matrix X and target y.

**Parameters**

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  
  The input data.

- **y**: array-like, shape (n_samples,)
  
  The target values.

- **classes**: array, shape (n_classes)
  
  Classes across all calls to partial_fit. Can be obtained via `np.unique(y_all)`, where y_all is the target vector of the entire dataset. This argument is required for the first call to partial_fit and can be omitted in the subsequent calls. Note that y doesn’t need to contain all labels in `classes`.

**Returns**

- **self**: returns a trained MLP model.

### predict

Predict using the multi-layer perceptron classifier

**Parameters**

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  
  The input data.

**Returns**

- **y**: array-like, shape (n_samples,) or (n_samples, n_classes)
  
  The predicted classes.

### predict_log_proba

Return the log of probability estimates.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  
  The input data.

**Returns**

- **log_y_prob**: array-like, shape (n_samples, n_classes)
  
  The predicted log-probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`. Equivalent to log(predict_proba(X))

### predict_proba

Probability estimates.

**Parameters**

- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  
  The input data.

**Returns**

- **y_prob**: array-like, shape (n_samples, n_classes)
  
  The predicted probability of the sample for each class in the model, where classes are ordered as they are in `self.classes_`. 

score(X, y, sample_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters

- **X**: array-like, shape = (n_samples, n_features)
  Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  Sample weights.

Returns **score**: float

Mean accuracy of self.predict(X) wrt. y.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns **self**

Examples using sklearn.neural_network.MLPClassifier

- Classifier comparison
- Visualization of MLP weights on MNIST
- Compare Stochastic learning strategies for MLPClassifier
- Varying regularization in Multi-layer Perceptron

30.28.3 sklearn.neural_network.MLPRegressor

class sklearn.neural_network.MLPRegressor(hidden_layer_sizes=(100, ), activation='relu', solver='adam', alpha=0.0001, batch_size='auto', learning_rate='constant', learning_rate_init=0.001, power_t=0.5, max_iter=200, shuffle=True, random_state=None, tol=0.0001, verbose=False, warm_start=False, momentum=0.9, nesterovs_momentum=True, early_stopping=False, validation_fraction=0.1, beta_1=0.9, beta_2=0.999, epsilon=1e-08, n_iter_no_change=10)

Multi-layer Perceptron regressor.

This model optimizes the squared-loss using LBFGS or stochastic gradient descent.

New in version 0.18.

Parameters **hidden_layer_sizes**: tuple, length = n_layers - 2, default (100,)

The ith element represents the number of neurons in the ith hidden layer.

Activation function for the hidden layer.

- ‘identity’, no-op activation, useful to implement linear bottleneck, returns \( f(x) = x \)
- ‘logistic’, the logistic sigmoid function, returns \( f(x) = 1 / (1 + \exp(-x)) \).
- ‘tanh’, the hyperbolic tan function, returns \( f(x) = \tanh(x) \).
- ‘relu’, the rectified linear unit function, returns \( f(x) = \max(0, x) \)

**solver** : {‘lbfgs’, ‘sgd’, ‘adam’}, default ‘adam’

The solver for weight optimization.

- ‘lbfgs’ is an optimizer in the family of quasi-Newton methods.
- ‘sgd’ refers to stochastic gradient descent.
- ‘adam’ refers to a stochastic gradient-based optimizer proposed by Kingma, Diederik, and Jimmy Ba

Note: The default solver ‘adam’ works pretty well on relatively large datasets (with thousands of training samples or more) in terms of both training time and validation score. For small datasets, however, ‘lbfgs’ can converge faster and perform better.

**alpha** : float, optional, default 0.0001

L2 penalty (regularization term) parameter.

**batch_size** : int, optional, default ‘auto’

Size of minibatches for stochastic optimizers. If the solver is ‘lbfgs’, the classifier will not use minibatch. When set to ‘auto’, \( \text{batch}\_\text{size}=\min(200, n\_\text{samples}) \)

**learning_rate** : {‘constant’, ‘invscaling’, ‘adaptive’}, default ‘constant’

Learning rate schedule for weight updates.

- ‘constant’ is a constant learning rate given by ‘learning_rate_init’.
- ‘invscaling’ gradually decreases the learning rate \( \text{learning}\_\text{rate} \) at each time step ‘t’ using an inverse scaling exponent of ‘power_t’. effective_learning_rate = \( \text{learning}\_\text{rate}\_\text{init} / \text{pow}(t, \text{power}_t) \)
- ‘adaptive’ keeps the learning rate constant to ‘learning_rate_init’ as long as training loss keeps decreasing. Each time two consecutive epochs fail to decrease training loss by at least tol, or fail to increase validation score by at least tol if ‘early_stopping’ is on, the current learning rate is divided by 5.

Only used when solver=’sgd’.

**learning_rate_init** : double, optional, default 0.001

The initial learning rate used. It controls the step-size in updating the weights. Only used when solver=’sgd’ or ‘adam’.

**power_t** : double, optional, default 0.5

The exponent for inverse scaling learning rate. It is used in updating effective learning rate when the learning_rate is set to ‘invscaling’. Only used when solver=’sgd’.

**max_iter** : int, optional, default 200
Maximum number of iterations. The solver iterates until convergence (determined by ‘tol’) or this number of iterations. For stochastic solvers (‘sgd’, ‘adam’), note that this determines the number of epochs (how many times each data point will be used), not the number of gradient steps.

**shuffle**: bool, optional, default True

Whether to shuffle samples in each iteration. Only used when solver=’sgd’ or ‘adam’.

**random_state**: int, RandomState instance or None, optional, default None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**tol**: float, optional, default 1e-4

Tolerance for the optimization. When the loss or score is not improving by at least \( \text{tol} \) for \( \text{n_iter_no_change} \) consecutive iterations, unless learning_rate is set to ‘adaptive’, convergence is considered to be reached and training stops.

**verbose**: bool, optional, default False

Whether to print progress messages to stdout.

**warm_start**: bool, optional, default False

When set to True, reuse the solution of the previous call to fit as initialization, otherwise, just erase the previous solution.

**momentum**: float, default 0.9

Momentum for gradient descent update. Should be between 0 and 1. Only used when solver=’sgd’.

**nesterovs_momentum**: boolean, default True

Whether to use Nesterov’s momentum. Only used when solver=’sgd’ and momentum > 0.

**early_stopping**: bool, default False

Whether to use early stopping to terminate training when validation score is not improving. If set to true, it will automatically set aside 10% of training data as validation and terminate training when validation score is not improving by at least \( \text{tol} \) for \( \text{n_iter_no_change} \) consecutive epochs. Only effective when solver=’sgd’ or ‘adam’

**validation_fraction**: float, optional, default 0.1

The proportion of training data to set aside as validation set for early stopping. Must be between 0 and 1. Only used if early_stopping is True

**beta_1**: float, optional, default 0.9

Exponential decay rate for estimates of first moment vector in adam, should be in \([0, 1)\). Only used when solver=’adam’

**beta_2**: float, optional, default 0.999

Exponential decay rate for estimates of second moment vector in adam, should be in \([0, 1)\). Only used when solver=’adam’

**epsilon**: float, optional, default 1e-8

Value for numerical stability in adam. Only used when solver=’adam’
**n_iter_no_change**: int, optional, default 10

Maximum number of epochs to not meet **tol** improvement. Only effective when **solver='sgd' or 'adam'**

New in version 0.20.

**Attributes**

<table>
<thead>
<tr>
<th>loss_</th>
<th>(float) The current loss computed with the loss function.</th>
</tr>
</thead>
<tbody>
<tr>
<td>coefs_</td>
<td>(list, length n_layers - 1) The ith element in the list represents the weight matrix corresponding to layer i.</td>
</tr>
<tr>
<td>intercepts_</td>
<td>(list, length n_layers - 1) The ith element in the list represents the bias vector corresponding to layer i + 1.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) The number of iterations the solver has ran.</td>
</tr>
<tr>
<td>n_layers_</td>
<td>(int) Number of layers.</td>
</tr>
<tr>
<td>n_outputs_</td>
<td>(int) Number of outputs.</td>
</tr>
<tr>
<td>out_activation</td>
<td>(string) Name of the output activation function.</td>
</tr>
</tbody>
</table>

**Notes**

MLPRegressor trains iteratively since at each time step the partial derivatives of the loss function with respect to the model parameters are computed to update the parameters.

It can also have a regularization term added to the loss function that shrinks model parameters to prevent overfitting.

This implementation works with data represented as dense and sparse numpy arrays of floating point values.

**References**


**Methods**

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<td>fit(X, y)</td>
<td>Fit the model to data matrix X and target(s) y.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the multi-layer perceptron model.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
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</table>
__init__ (hidden_layer_sizes=(100, ), activation='relu', solver='adam', alpha=0.0001, batch_size='auto', learning_rate='constant', learning_rate_init=0.001, power_t=0.5, max_iter=200, shuffle=True, random_state=None, tol=0.0001, verbose=False, warm_start=False, momentum=0.9, nesterovs_momentum=True, early_stopping=False, validation_fraction=0.1, beta_1=0.9, beta_2=0.999, epsilon=1e-08, n_iter_no_change=10)

fit (X, y)
Fit the model to data matrix X and target(s) y.

Parameters
X : array-like or sparse matrix, shape (n_samples, n_features)
The input data.
y : array-like, shape (n_samples,) or (n_samples, n_outputs)
The target values (class labels in classification, real numbers in regression).

Returns
self : returns a trained MLP model.

get_params (deep=True)
Get parameters for this estimator.

Parameters
deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns
params : mapping of string to any
Parameter names mapped to their values.

partial_fit (X, y)
Fit the model to data matrix X and target y.

Parameters
X : {array-like, sparse matrix}, shape (n_samples, n_features)
The input data.
y : array-like, shape (n_samples,)
The target values.

Returns
self : returns a trained MLP model.

predict (X)
Predict using the multi-layer perceptron model.

Parameters
X : {array-like, sparse matrix}, shape (n_samples, n_features)
The input data.

Returns
y : array-like, shape (n_samples, n_outputs)
The predicted values.

score (X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters
X : array-like, shape = (n_samples, n_features)
Test samples.
y : array-like, shape = (n_samples) or (n_samples, n_outputs)
   True values for X.

sample_weight : array-like, shape = [n_samples], optional
   Sample weights.

Returns score : float
   R^2 of self.predict(X) wrt. y.

set_params (**params)
   Set the parameters of this estimator.
   The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
   parameters of the form <component>__<parameter> so that it’s possible to update each component
   of a nested object.

   Returns self

30.29 sklearn.pipeline: Pipeline

The sklearn.pipeline module implements utilities to build a composite estimator, as a chain of transforms and
estimators.

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<th>Concatenates results of multiple transformer objects.</th>
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<td>sklearn.pipeline.Pipeline(steps[, memory])</td>
<td>Pipeline of transforms with a final estimator.</td>
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30.29.1 sklearn.pipeline.FeatureUnion

class sklearn.pipeline.FeatureUnion (transformer_list, n_jobs=1, transformer_weights=None)
   Concatenates results of multiple transformer objects.
   This estimator applies a list of transformer objects in parallel to the input data, then concatenates the results.
   This is useful to combine several feature extraction mechanisms into a single transformer.

   Parameters of the transformers may be set using its name and the parameter name separated by a ‘__’. A
   transformer may be replaced entirely by setting the parameter with its name to another transformer, or removed
   by setting to None.

   Read more in the User Guide.

   Parameters transformer_list : list of (string, transformer) tuples
      List of transformer objects to be applied to the data. The first half of each tuple is the
      name of the transformer.

   n_jobs : int, optional
      Number of jobs to run in parallel (default 1).

   transformer_weights : dict, optional
      Multiplicative weights for features per transformer. Keys are transformer names, values
      the weights.
Methods

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<th>Method</th>
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<td>fit(X[, y])</td>
<td>Fit all transformers using X.</td>
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<tr>
<td>fit_transform(X[, y])</td>
<td>Fit all transformers, transform the data and concatenate results.</td>
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<tr>
<td>get_feature_names()</td>
<td>Get feature names from all transformers.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
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<tr>
<td>set_params(**kwargs)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Transform X separately by each transformer, concatenate results.</td>
</tr>
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</table>

__init__(transformer_list, n_jobs=1, transformer_weights=None)

fit (X, y=None)
Fit all transformers using X.

Parameters:
- **X**: iterable or array-like, depending on transformers
  - Input data, used to fit transformers.
- **y**: array-like, shape (n_samples, . . .), optional
  - Targets for supervised learning.

Returns:
- **self**: FeatureUnion
  - This estimator

fit_transform (X, y=None, **fit_params)
Fit all transformers, transform the data and concatenate results.

Parameters:
- **X**: iterable or array-like, depending on transformers
  - Input data to be transformed.
- **y**: array-like, shape (n_samples, . . .), optional
  - Targets for supervised learning.

Returns:
- **X_t**: array-like or sparse matrix, shape (n_samples, sum_n_components)
  - hstack of results of transformers. sum_n_components is the sum of n_components (output dimension) over transformers.

get_feature_names()
Get feature names from all transformers.

Returns:
- **feature_names**: list of strings
  - Names of the features produced by transform.

get_params (deep=True)
Get parameters for this estimator.

Parameters:
- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns:
- **params**: mapping of string to any
  - Parameter names mapped to their values.
**set_params** (**kwargs)
Set the parameters of this estimator.

Valid parameter keys can be listed with **get_params**.

**Returns**
self

**transform** (**X**)
Transform X separately by each transformer, concatenate results.

**Parameters**
**X** : iterable or array-like, depending on transformers
Input data to be transformed.

**Returns**
**X_t** : array-like or sparse matrix, shape (n_samples, sum_n_components)
hsstack of results of transformers. sum_n_components is the sum of n_components (output dimension) over transformers.

Examples using sklearn.pipeline.FeatureUnion

- Concatenating multiple feature extraction methods
- Feature Union with Heterogeneous Data Sources

### 30.29.2 sklearn.pipeline.Pipeline

**class** sklearn.pipeline.Pipeline (**steps**, memory=None)

Pipeline of transforms with a final estimator.

Sequentially apply a list of transforms and a final estimator. Intermediate steps of the pipeline must be ‘transforms’, that is, they must implement fit and transform methods. The final estimator only needs to implement fit. The transformers in the pipeline can be cached using memory argument.

The purpose of the pipeline is to assemble several steps that can be cross-validated together while setting different parameters. For this, it enables setting parameters of the various steps using their names and the parameter name separated by a ‘__’, as in the example below. A step’s estimator may be replaced entirely by setting the parameter with its name to another estimator, or a transformer removed by setting to None.

Read more in the User Guide.

**Parameters**
**steps** : list
List of (name, transform) tuples (implementing fit/transform) that are chained, in the order in which they are chained, with the last object an estimator.

**memory** : None, str or object with the joblib.Memory interface, optional
Used to cache the fitted transformers of the pipeline. By default, no caching is performed. If a string is given, it is the path to the caching directory. Enabling caching triggers a clone of the transformers before fitting. Therefore, the transformer instance given to the pipeline cannot be inspected directly. Use the attribute named_steps or steps to inspect estimators within the pipeline. Caching the transformers is advantageous when fitting is time consuming.
Attributes

**named_steps**

A dictionary of step name to an estimator. Each estimator can be set using
the names issued. For instance, fit using a k of 10 in the SelectKBest and a parameter 'C' of the svm.

Examples

```python
>>> from sklearn import svm
>>> from sklearn.datasets import samples_generator
>>> from sklearn.feature_selection import SelectKBest
>>> from sklearn.feature_selection import f_regression
>>> from sklearn.pipeline import Pipeline

# generate some data to play with

>>> X, y = samples_generator.make_classification(...
... n_informative=5, n_redundant=0, random_state=42)

# ANOVA SVM-C

>>> anova_filter = SelectKBest(f_regression, k=5)
>>> clf = svm.SVC(kernel='linear')

>>> anova_svm = Pipeline([('anova', anova_filter), ('svc', clf)])

# You can set the parameters using the names issued

# For instance, fit using a k of 10 in the SelectKBest

# and a parameter 'C' of the svm

>>> anova_svm.set_params(anova__k=10, svc__C=.1).fit(X, y)

... Pipeline(memory=None,
    steps=[('anova', SelectKBest(...)),
           ('svc', SVC(...))])

>>> prediction = anova_svm.predict(X)

>>> anova_svm.score(X, y)
0.829...

>>> # getting the selected features chosen by anova_filter

>>> anova_svm.named_steps['anova'].get_support()

array([False, False, True, True, False, False, True, True, False, False,
       True, True, False, False, True, True, False, False, True, False],
      dtype=bool)

>>> # Another way to get selected features chosen by anova_filter

>>> anova_svm.named_steps.anova.get_support()

array([False, False, True, True, False, False, True, True, False, False,
       True, True, False, False, True, True, False, False, True, False],
      dtype=bool)
```

Methods

- **decision_function** *(X)*: Apply transforms, and decision_function of the final estimator.
- **fit**(X[, y]): Fit the model.
- **fit_predict**(X[, y]): Applies fit_predict of last step in pipeline after transforms.
- **fit_transform**(X[, y]): Fit the model and transform with the final estimator.

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<th>Method</th>
<th>Description</th>
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<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
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<tr>
<td><code>predict(X)</code></td>
<td>Apply transforms to the data, and predict with the final estimator.</td>
</tr>
<tr>
<td><code>predict_log_proba(X)</code></td>
<td>Apply transforms, and predict_log_proba of the final estimator.</td>
</tr>
<tr>
<td><code>predict_proba(X)</code></td>
<td>Apply transforms, and predict_proba of the final estimator.</td>
</tr>
<tr>
<td><code>score(X[, y, sample_weight])</code></td>
<td>Apply transforms, and score with the final estimator.</td>
</tr>
<tr>
<td><code>set_params(**kwargs)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(steps, memory=None)

**decision_function** (X)
Apply transforms, and decision_function of the final estimator

**Parameters**
- X : iterable
  Data to predict on. Must fulfill input requirements of first step of the pipeline.

**Returns**
- y_score : array-like, shape = [n_samples, n_classes]

**fit** (X, y=None, **fit_params)
Fit the model
Fit all the transforms one after the other and transform the data, then fit the transformed data using the final estimator.

**Parameters**
- X : iterable
  Training data. Must fulfill input requirements of first step of the pipeline.
- y : iterable, default=None
  Training targets. Must fulfill label requirements for all steps of the pipeline.

**fit_params** : dict of string -> object
Parameters passed to the fit method of each step, where each parameter name is prefixed such that parameter p for step s has key s__p.

**Returns**
- self : Pipeline
  This estimator

**fit_predict** (X, y=None, **fit_params)
Applies fit_predict of last step in pipeline after transforms.
Applies fit_transforms of a pipeline to the data, followed by the fit_predict method of the final estimator in the pipeline. Valid only if the final estimator implements fit_predict.

**Parameters**
- X : iterable
  Training data. Must fulfill input requirements of first step of the pipeline.
- y : iterable, default=None
  Training targets. Must fulfill label requirements for all steps of the pipeline.

**fit_params** : dict of string -> object
Parameters passed to the fit method of each step, where each parameter name is prefixed such that parameter p for step s has key s__p.

**Returns**
- y_pred : array-like
**fit_transform** (*X*, *y=None, **fit_params*)
Fit the model and transform with the final estimator
Fits all the transforms one after the other and transforms the data, then uses fit_transform on transformed data with the final estimator.

**Parameters**
- **X**: iterable
  - Training data. Must fulfill input requirements of first step of the pipeline.
- **y**: iterable, default=None
  - Training targets. Must fulfill label requirements for all steps of the pipeline.
- **fit_params**: dict of string -> object
  - Parameters passed to the `fit` method of each step, where each parameter name is prefixed such that parameter `p` for step `s` has key `s__p`.

**Returns**
- **Xt**: array-like, shape = [n_samples, n_transformed_features]
  - Transformed samples

**get_params** (*deep=True*)
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  - Parameter names mapped to their values.

**inverse_transform**
Apply inverse transformations in reverse order
All estimators in the pipeline must support `inverse_transform`.

**Parameters**
- **Xt**: array-like, shape = [n_samples, n_transformed_features]
  - Data samples, where n_samples is the number of samples and n_features is the number of features. Must fulfill input requirements of last step of pipeline’s `inverse_transform` method.

**Returns**
- **Xt**: array-like, shape = [n_samples, n_features]

**predict** (*X*)
Apply transforms to the data, and predict with the final estimator

**Parameters**
- **X**: iterable
  - Data to predict on. Must fulfill input requirements of first step of the pipeline.

**Returns**
- **y_pred**: array-like

**predict_log_proba** (*X*)
Apply transforms, and predict_log_proba of the final estimator

**Parameters**
- **X**: iterable
  - Data to predict on. Must fulfill input requirements of first step of the pipeline.

**Returns**
- **y_score**: array-like, shape = [n_samples, n_classes]

**predict_proba** (*X*)
Apply transforms, and predict_proba of the final estimator
Parameters X : iterable

Data to predict on. Must fulfill input requirements of first step of the pipeline.

Returns y_proba : array-like, shape = [n_samples, n_classes]

score (X, y=None, sample_weight=None)

Apply transforms, and score with the final estimator

Parameters X : iterable

Data to predict on. Must fulfill input requirements of first step of the pipeline.

y : iterable, default=None

Targets used for scoring. Must fulfill label requirements for all steps of the pipeline.

sample_weight : array-like, default=None

If not None, this argument is passed as sample_weight keyword argument to the score method of the final estimator.

Returns score : float

set_params (**kwargs)

Set the parameters of this estimator.

Valid parameter keys can be listed with get_params().

Returns self

transform

Apply transforms, and transform with the final estimator

This also works where final estimator is None: all prior transformations are applied.

Parameters X : iterable

Data to transform. Must fulfill input requirements of first step of the pipeline.

Returns Xt : array-like, shape = [n_samples, n_transformed_features]

Examples using sklearn.pipeline.Pipeline

• Concatenating multiple feature extraction methods
• Pipelining: chaining a PCA and a logistic regression
• Imputing missing values before building an estimator
• Selecting dimensionality reduction with Pipeline and GridSearchCV
• Feature Union with Heterogeneous Data Sources
• Explicit feature map approximation for RBF kernels
• Feature agglomeration vs. univariate selection
• Underfitting vs. Overfitting
• Sample pipeline for text feature extraction and evaluation
• Restricted Boltzmann Machine features for digit classification
• SVM-Anova: SVM with univariate feature selection
• Classification of text documents using sparse features
pipeline.make_pipeline(*steps, **kwargs) Construct a Pipeline from the given estimators.

pipeline.make_union(*transformers, **kwargs) Construct a FeatureUnion from the given transformers.

30.29.3 sklearn.pipeline.make_pipeline

sklearn.pipeline.make_pipeline(*steps, **kwargs)

Construct a Pipeline from the given estimators.

This is a shorthand for the Pipeline constructor; it does not require, and does not permit, naming the estimators. Instead, their names will be set to the lowercase of their types automatically.

Parameters

*steps : list of estimators,

memory : None, str or object with the joblib.Memory interface, optional

Used to cache the fitted transformers of the pipeline. By default, no caching is performed. If a string is given, it is the path to the caching directory. Enabling caching triggers a clone of the transformers before fitting. Therefore, the transformer instance given to the pipeline cannot be inspected directly. Use the attribute named_steps or steps to inspect estimators within the pipeline. Caching the transformers is advantageous when fitting is time consuming.

Returns

p : Pipeline

Examples

```python
>>> from sklearn.naive_bayes import GaussianNB
>>> from sklearn.preprocessing import StandardScaler

>>> make_pipeline(StandardScaler(), GaussianNB(priors=None))
...
Pipeline(memory=None,
         steps=[('standardscaler',
                 StandardScaler(copy=True, with_mean=True, with_std=True)),
                ('gaussiannb',
                 GaussianNB(priors=None, var_smoothing=1e-09))])
```

Examples using sklearn.pipeline.make_pipeline

- Feature transformations with ensembles of trees
- Pipeline Anova SVM
- Polynomial interpolation
- Robust linear estimator fitting
- Using FunctionTransformer to select columns
- Importance of Feature Scaling
- Clustering text documents using k-means
30.29.4 sklearn.pipeline.make_union

sklearn.pipeline.make_union(*transformers, **kwargs)

Construct a FeatureUnion from the given transformers.

This is a shorthand for the FeatureUnion constructor; it does not require, and does not permit, naming the transformers. Instead, they will be given names automatically based on their types. It also does not allow weighting.

**Parameters**

- *transformers : list of estimators*
  - **n_jobs : int, optional**
    
    Number of jobs to run in parallel (default 1).

**Returns**

- f : FeatureUnion

**Examples**

```python
>>> from sklearn.decomposition import PCA, TruncatedSVD
>>> from sklearn.pipeline import make_union
>>> make_union(PCA(), TruncatedSVD())
FeatureUnion(n_jobs=1,
    transformer_list=[('pca',
        PCA(copy=True, iterated_power='auto',
            n_components=None, random_state=None,
            svd_solver='auto', tol=0.0, whiten=False)),
        ('truncatedsvd',
            TruncatedSVD(algorithm='randomized',
                            n_components=2, n_iter=5,
                            random_state=None, tol=0.0))],
    transformer_weights=None)
```

30.30 sklearn.preprocessing: Preprocessing and Normalization

The sklearn.preprocessing module includes scaling, centering, normalization, binarization and imputation methods.

**User guide:** See the Preprocessing data section for further details.

<table>
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<td>Standardize features by removing the mean and scaling to unit variance.</td>
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### 30.30.1 sklearn.preprocessing.Binarizer

**class** `sklearn.preprocessing.Binarizer(threshold=0.0, copy=True)`

Binarize data (set feature values to 0 or 1) according to a threshold

Values greater than the threshold map to 1, while values less than or equal to the threshold map to 0. With the default threshold of 0, only positive values map to 1.

Binarization is a common operation on text count data where the analyst can decide to only consider the presence or absence of a feature rather than a quantified number of occurrences for instance.

It can also be used as a pre-processing step for estimators that consider boolean random variables (e.g. modelled using the Bernoulli distribution in a Bayesian setting).

Read more in the [User Guide](#).

**Parameters**

- **threshold**: float, optional (0.0 by default)
  
  Feature values below or equal to this are replaced by 0, above it by 1. Threshold may not be less than 0 for operations on sparse matrices.

- **copy**: boolean, optional, default True
  
  set to False to perform inplace binarization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix).

**See also:**

- `binarize` Equivalent function without the estimator API.

**Notes**

If the input is a sparse matrix, only the non-zero values are subject to update by the Binarizer class.

This estimator is stateless (besides constructor parameters), the fit method does nothing but is useful when used in a pipeline.

**Methods**
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<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X[, y, copy])</td>
<td>Binarize each element of X</td>
</tr>
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</table>

**__init__ (threshold=0.0, copy=True)**

**fit (X, y=None)**
Do nothing and return the estimator unchanged

This method is just there to implement the usual API and hence work in pipelines.

Parameters

- **X**: array-like
  - Training set.
- **y**: array-like
  - Target values.

**fit_transform (X, y=None, **fit_params)**

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters

- **X**: array-like
  - numpy array of shape [n_samples, n_features]
  - The data to binarize, element by element. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.
- **y**: array-like
  - Target values.

Returns

- **X_new**: array-like of shape [n_samples, n_features_new]
  - Transformed data.

**get_params (deep=True)**

Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**set_params (**params)**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns

- **self**: estimator

**transform (X, y='deprecated', copy=None)**

Binarize each element of X

Parameters

- **X**: array-like, shape [n_samples, n_features]
  - The data to binarize, element by element. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.
- **y**: array-like
  - Not used.

Returns

- **X**: array-like, shape [n_samples, n_features]
  - Binarized data.

Deprecated since version 0.19: This parameter will be removed in 0.21.
copy : bool
    Copy the input X or not.

30.30.2 sklearn.preprocessing.FunctionTransformer

class sklearn.preprocessing.FunctionTransformer(func=None, inverse_func=None, validate=True, accept_sparse=False, pass_y='deprecated', check_inverse=True, kw_args=None, inv_kw_args=None)

    Constructs a transformer from an arbitrary callable.

    A FunctionTransformer forwards its X (and optionally y) arguments to a user-defined function or function object and returns the result of this function. This is useful for stateless transformations such as taking the log of frequencies, doing custom scaling, etc.

    Note: If a lambda is used as the function, then the resulting transformer will not be pickleable.

    New in version 0.17.

    Read more in the User Guide.

    Parameters func : callable, optional default=None
        The callable to use for the transformation. This will be passed the same arguments as transform, with args and kwargs forwarded. If func is None, then func will be the identity function.

    inverse_func : callable, optional default=None
        The callable to use for the inverse transformation. This will be passed the same arguments as inverse transform, with args and kwargs forwarded. If inverse_func is None, then inverse_func will be the identity function.

    validate : bool, optional default=True
        Indicate that the input X array should be checked before calling func. If validate is false, there will be no input validation. If it is true, then X will be converted to a 2-dimensional NumPy array or sparse matrix. If this conversion is not possible or X contains NaN or infinity, an exception is raised.

    accept_sparse : boolean, optional
        Indicate that func accepts a sparse matrix as input. If validate is False, this has no effect. Otherwise, if accept_sparse is False, sparse matrix inputs will cause an exception to be raised.

    pass_y : bool, optional default=False
        Indicate that transform should forward the y argument to the inner callable.

    check_inverse : bool, default=True
        Whether to check that or func followed by inverse_func leads to the original inputs. It can be used for a sanity check, raising a warning when the condition is not fulfilled.

        New in version 0.20.

    kw_args : dict, optional
        Dictionary of additional keyword arguments to pass to func.
**inv_kw_args** : dict, optional

Dictionary of additional keyword arguments to pass to inverse_func.

## Methods

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<th>Description</th>
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<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
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<tr>
<td><code>inverse_transform(X[, y])</code></td>
<td>Transform X using the inverse function.</td>
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<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X[, y])</code></td>
<td>Transform X using the forward function.</td>
</tr>
</tbody>
</table>

### __init__

```python
(func=None, inverse_func=None, validate=True, accept_sparse=False, pass_y='deprecated', check_inverse=True, kw_args=None, inv_kw_args=None)
```

#### fit (X, y=None)

Fit transformer by checking X.

If `validate` is `True`, X will be checked.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Input array.

**Returns**

- **self**

#### fit_transform (X, y=None, **fit_params)

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  Training set.
- **y**: numpy array of shape [n_samples]
  Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  Transformed array.

#### get_params (deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

#### inverse_transform (X, y='deprecated')

Transform X using the inverse function.

**Parameters**

- **X**: array-like, shape (n_samples, n_features)
  Input array.
y : (ignored)

Returns X_out : array-like, shape (n_samples, n_features)
    Transformed input.

set_params (**params)
    Set the parameters of this estimator.

    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

    Returns self

transform (X, y='deprecated')
    Transform X using the forward function.

    Parameters X : array-like, shape (n_samples, n_features)
        Input array.

    y : (ignored)

    Returns X_out : array-like, shape (n_samples, n_features)
        Transformed input.

Examples using sklearn.preprocessing.FunctionTransformer

• Using FunctionTransformer to select columns

30.30.3 sklearn.preprocessing.Imputer

class sklearn.preprocessing.Imputer(missing_values='NaN', strategy='mean', axis=0, verbose=0, copy=True)
    Imputation transformer for completing missing values.

    Read more in the User Guide.

    Parameters missing_values : integer or “NaN”, optional (default=“NaN”)
        The placeholder for the missing values. All occurrences of missing_values will be imputed. For missing values encoded as np.nan, use the string value “NaN”.

    strategy : string, optional (default=“mean”)
        The imputation strategy.

        • If “mean”, then replace missing values using the mean along the axis.
        • If “median”, then replace missing values using the median along the axis.
        • If “most_frequent”, then replace missing values using the most frequent value along the axis.

    axis : integer, optional (default=0)
        The axis along which to impute.

        • If axis=0, then impute along columns.
**Attributes**

- `statistics_` (array of shape (n_features,)) The imputation fill value for each feature if `axis == 0`.

**Notes**

- When `axis=0`, columns which only contained missing values at `fit` are discarded upon `transform`.
- When `axis=1`, an exception is raised if there are rows for which it is not possible to fill in the missing values (e.g., because they only contain missing values).

**Methods**

- `fit(X[, y])` Fit the imputer on X.
- `fit_transform(X[, y])` Fit to data, then transform it.
- `get_params([deep])` Get parameters for this estimator.
- `set_params(**params)` Set the parameters of this estimator.
- `transform(X)` Impute all missing values in X.

```python
__init__(missing_values='NaN', strategy='mean', axis=0, verbose=0, copy=True)
```

**fit** *(X, y=None)*

Fit the imputer on X.

**Parameters**

- `X` : {array-like, sparse matrix}, shape (n_samples, n_features)
  
  Input data, where `n_samples` is the number of samples and `n_features` is the number of features.

**Returns**

- `self` : Imputer
  
  Returns self.

**fit_transform** *(X, y=None, **fit_params)*

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.
Parameters X : numpy array of shape [n_samples, n_features]
  Training set.

y : numpy array of shape [n_samples]
  Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]
  Transformed array.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
  Parameter names mapped to their values.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Impute all missing values in X.

Parameters X : {array-like, sparse matrix}, shape = [n_samples, n_features]
  The input data to complete.

Examples using sklearn.preprocessing.Imputer

- Imputing missing values before building an estimator

30.30.4 sklearn.preprocessing.KernelCenterer

class sklearn.preprocessing.KernelCenterer
Center a kernel matrix

Let K(x, z) be a kernel defined by phi(x)^T phi(z), where phi is a function mapping x to a Hilbert space. KernelCenterer centers (i.e., normalize to have zero mean) the data without explicitly computing phi(x). It is equivalent to centering phi(x) with sklearn.preprocessing.StandardScaler(with_std=False).

Read more in the User Guide.

Methods

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<td>Fit KernelCenterer</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
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<td><code>get_params()</code></td>
<td>Get parameters for this estimator.</td>
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<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(K[, y, copy])</code></td>
<td>Center kernel matrix.</td>
</tr>
</tbody>
</table>

__init__(self, /, *args, **kwargs)

Initialize self. See help(type(self)) for accurate signature.

`fit(K, y=None)`

Fit KernelCenterer

**Parameters**

- **K**: numpy array of shape [n_samples, n_samples]
  
  Kernel matrix.

**Returns**

- **self**: returns an instance of self.

`fit_transform(X, y=None, **fit_params)`

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  
  Training set.

- **y**: (ignored)

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

`get_params(deep=True)`

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional

  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any

  Parameter names mapped to their values.

`set_params(**params)`

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

`transform(K, y='deprecated', copy=True)`

Center kernel matrix.

**Parameters**

- **K**: numpy array of shape [n_samples1, n_samples2]

  Kernel matrix.

- **y**: (ignored)

  Deprecated since version 0.19: This parameter will be removed in 0.21.

- **copy**: boolean, optional, default True
Set to False to perform inplace computation.

Returns K_new : numpy array of shape [n_samples1, n_samples2]

### 30.30.5 sklearn.preprocessing.LabelBinarizer

class sklearn.preprocessing.LabelBinarizer(neg_label=0, pos_label=1, sparse_output=False)

Binarize labels in a one-vs-all fashion

Several regression and binary classification algorithms are available in the scikit. A simple way to extend these algorithms to the multi-class classification case is to use the so-called one-vs-all scheme.

At learning time, this simply consists in learning one regressor or binary classifier per class. In doing so, one needs to convert multi-class labels to binary labels (belong or does not belong to the class). LabelBinarizer makes this process easy with the transform method.

At prediction time, one assigns the class for which the corresponding model gave the greatest confidence. LabelBinarizer makes this easy with the inverse_transform method.

Read more in the User Guide.

Parameters neg_label : int (default: 0)

Value with which negative labels must be encoded.

pos_label : int (default: 1)

Value with which positive labels must be encoded.

sparse_output : boolean (default: False)

True if the returned array from transform is desired to be in sparse CSR format.

Attributes

<table>
<thead>
<tr>
<th>classes</th>
<th>(array of shape [n_class]) Holds the label for each class.</th>
</tr>
</thead>
<tbody>
<tr>
<td>y_type</td>
<td>(str,) Represents the type of the target data as evaluated by <code>utils.multiclass.type_of_target</code>. Possible types are 'continuous', 'continuous-multioutput', 'binary', 'multiclass', 'multiclass-multioutput', 'multilabel-indicator', and 'unknown'.</td>
</tr>
<tr>
<td>sparse_input</td>
<td>(boolean,) True if the input data to transform is given as a sparse matrix, False otherwise.</td>
</tr>
</tbody>
</table>

See also:

- `label_binarize` function to perform the transform operation of LabelBinarizer with fixed classes.
- `sklearn.preprocessing.OneHotEncoder` encode categorical integer features using a one-hot aka one-of-K scheme.

Examples

```python
>>> from sklearn import preprocessing
>>> lb = preprocessing.LabelBinarizer()
>>> lb.fit([1, 2, 6, 4, 2])
LabelBinarizer(neg_label=0, pos_label=1, sparse_output=False)
>>> lb.classes_
```
array([[1, 2, 4, 6]])
>>> lb.transform([1, 6])
array([[1, 0, 0, 0],
       [0, 0, 0, 1]])

Binary targets transform to a column vector

>>> lb = preprocessing.LabelBinarizer()
>>> lb.fit_transform(['yes', 'no', 'no', 'yes'])
array([[1],
       [0],
       [0],
       [1]])

Passing a 2D matrix for multilabel classification

>>> import numpy as np
>>> lb.fit(np.array([[0, 1, 1], [1, 0, 0]]))
LabelBinarizer(neg_label=0, pos_label=1, sparse_output=False)
>>> lb.classes_
array([0, 1, 2])
>>> lb.transform([[0, 1, 2], [1, 0, 1]])
array([[1, 0, 0],
       [0, 1, 0],
       [0, 0, 1],
       [0, 1, 0]])

Methods

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<td>Fit label binarizer</td>
</tr>
<tr>
<td>fit_transform(y)</td>
<td>Fit label binarizer and transform multi-class labels to binary labels.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>inverse_transform(Y, [threshold])</td>
<td>Transform binary labels back to multi-class labels</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(y)</td>
<td>Transform multi-class labels to binary labels</td>
</tr>
</tbody>
</table>

__init__ (neg_label=0, pos_label=1, sparse_output=False)

**fit** (y)

Fit label binarizer

**Parameters**

- **y**: array of shape [n_samples,] or [n_samples, n_classes]
  - Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification.

**Returns**

- **self**: returns an instance of self.

**fit_transform** (y)

Fit label binarizer and transform multi-class labels to binary labels.

The output of transform is sometimes referred to as the 1-of-K coding scheme.

**Parameters**

- **y**: array or sparse matrix of shape [n_samples,] or [n_samples, n_classes]
Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification. Sparse matrix can be CSR, CSC, COO, DOK, or LIL.

**Returns** $Y$ : array or CSR matrix of shape $[n_{\text{samples}}, n_{\text{classes}}]$

Shape will be $[n_{\text{samples}}, 1]$ for binary problems.

**get_params** *(deep=True)*

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  
  Parameter names mapped to their values.

**inverse_transform** *(Y, threshold=None)*

Transform binary labels back to multi-class labels

**Parameters**

- **Y** : numpy array or sparse matrix with shape $[n_{\text{samples}}, n_{\text{classes}}]$
  
  Target values. All sparse matrices are converted to CSR before inverse transformation.

- **threshold** : float or None
  
  Threshold used in the binary and multi-label cases.
  
  Use 0 when $Y$ contains the output of decision_function (classifier). Use 0.5 when $Y$ contains the output of predict_proba.
  
  If None, the threshold is assumed to be half way between `neg_label` and `pos_label`.

**Returns**

- **y** : numpy array or CSR matrix of shape $[n_{\text{samples}}]$ Target values.

**Notes**

In the case when the binary labels are fractional (probabilistic), inverse_transform chooses the class with the greatest value. Typically, this allows to use the output of a linear model’s decision_function method directly as the input of inverse_transform.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**transform** *(y)*

Transform multi-class labels to binary labels

The output of transform is sometimes referred to by some authors as the 1-of-K coding scheme.

**Parameters**

- **y** : array or sparse matrix of shape $[n_{\text{samples}},]$ or $[n_{\text{samples}}, n_{\text{classes}}]$
  
  Target values. The 2-d matrix should only contain 0 and 1, represents multilabel classification. Sparse matrix can be CSR, CSC, COO, DOK, or LIL.

**Returns**

- **Y** : numpy array or CSR matrix of shape $[n_{\text{samples}}, n_{\text{classes}}]$
  
  Shape will be $[n_{\text{samples}}, 1]$ for binary problems.
30.30.6 sklearn.preprocessing.LabelEncoder

class sklearn.preprocessing.LabelEncoder
    Encode labels with value between 0 and n_classes-1.

    Read more in the User Guide.

    Attributes

    classes_  (array of shape (n_class,)) Holds the label for each class.

    See also:

    sklearn.preprocessing.OneHotEncoder encode categorical integer features using a one-hot aka one-of-K scheme.

    Examples

    LabelEncoder can be used to normalize labels.

    >>> from sklearn import preprocessing
    >>> le = preprocessing.LabelEncoder()
    >>> le.fit([1, 2, 2, 6])
    LabelEncoder()
    >>> le.classes_
    array([1, 2, 6])
    >>> le.transform([1, 1, 2, 6])
    array([0, 0, 1, 2]...)
    >>> le.inverse_transform([0, 0, 1, 2])
    array([1, 1, 2, 6])

    It can also be used to transform non-numerical labels (as long as they are hashable and comparable) to numerical labels.

    >>> le = preprocessing.LabelEncoder()
    >>> le.fit(["paris", "paris", "tokyo", "amsterdam"])
    LabelEncoder()
    >>> list(le.classes_)
    ['amsterdam', 'paris', 'tokyo']
    >>> le.transform(["tokyo", "tokyo", "paris"])
    array([2, 2, 1]...)
    >>> list(le.inverse_transform([2, 2, 1]))
    ['tokyo', 'tokyo', 'paris']

    Methods

    fit(y)  Fit label encoder
    fit_transform(y)  Fit label encoder and return encoded labels
    get_params([deep])  Get parameters for this estimator.
    inverse_transform(y)  Transform labels back to original encoding.
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<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td>set_params</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform</td>
<td>Transform labels to normalized encoding.</td>
</tr>
</tbody>
</table>

```python
__init__($self, /, *args, **kwargs)
Initialize self. See help(type(self)) for accurate signature.
```

```python
fit(y)
Fit label encoder

Parameters y : array-like of shape (n_samples,)
Target values.

Returns self : returns an instance of self.
```

```python
fit_transform(y)
Fit label encoder and return encoded labels

Parameters y : array-like of shape [n_samples]
Target values.

Returns y : array-like of shape [n_samples]
```

```python
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are
estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.
```

```python
inverse_transform(y)
Transform labels back to original encoding.

Parameters y : numpy array of shape [n_samples]
Target values.

Returns y : numpy array of shape [n_samples]
```

```python
set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it's possible to update each component
of a nested object.

Returns self
```

```python
transform(y)
Transform labels to normalized encoding.

Parameters y : array-like of shape [n_samples]
Target values.

Returns y : array-like of shape [n_samples]
```
30.30.7 sklearn.preprocessing.MultiLabelBinarizer

class sklearn.preprocessing.MultiLabelBinarizer (classes=None, sparse_output=False)

Transform between iterable of iterables and a multilabel format

Although a list of sets or tuples is a very intuitive format for multilabel data, it is unwieldy to process. This transformer converts between this intuitive format and the supported multilabel format: a (samples x classes) binary matrix indicating the presence of a class label.

**Parameters**

- **classes**: array-like of shape [n_classes] (optional)
  - Indicates an ordering for the class labels
- **sparse_output**: boolean (default: False),
  - Set to true if output binary array is desired in CSR sparse format

**Attributes**

- **classes_**: (array of labels) A copy of the classes parameter where provided, or otherwise, the sorted set of classes found when fitting.

See also:

- sklearn.preprocessing.OneHotEncoder encode categorical integer features using a one-hot aka one-of-K scheme.

**Examples**

```python
>>> from sklearn.preprocessing import MultiLabelBinarizer
>>> mlb = MultiLabelBinarizer()
>>> mlb.fit_transform([(1, 2), (3,)])
array([[1, 1, 0],
       [0, 0, 1]])
>>> mlb.classes_
array([1, 2, 3])
```

```python
>>> mlb.fit_transform([set(['sci-fi', 'thriller']), set(['comedy'])])
array([[0, 1, 1],
       [1, 0, 0]])
>>> list(mlb.classes_)
['comedy', 'sci-fi', 'thriller']
```

**Methods**

- `fit(y)` Fit the label sets binarizer, storing classes_
- `fit_transform(y)` Fit the label sets binarizer and transform the given label sets
- `get_params([deep])` Get parameters for this estimator.
- `inverse_transform(yt)` Transform the given indicator matrix into label sets

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<table>
<thead>
<tr>
<th>Method</th>
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<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(y)</code></td>
<td>Transform the given label sets.</td>
</tr>
</tbody>
</table>

```python
__init__(classes=None, sparse_output=False)
```

Fit the label sets binarizer, storing `classes_`

Parameters:

- `y` : iterable of iterables
  - A set of labels (any orderable and hashable object) for each sample. If the `classes` parameter is set, `y` will not be iterated.

Returns:

- `self` : returns this MultiLabelBinarizer instance

```python
fit(y)
```

Fit the label sets binarizer.

Parameters:

- `y` : iterable of iterables
  - A set of labels (any orderable and hashable object) for each sample. If the `classes` parameter is set, `y` will not be iterated.

Returns:

- `self` : returns this MultiLabelBinarizer instance

```python
fit_transform(y)
```

Fit the label sets binarizer and transform the given label sets.

Parameters:

- `y` : iterable of iterables
  - A set of labels (any orderable and hashable object) for each sample. If the `classes` parameter is set, `y` will not be iterated.

Returns:

- `y_indicator` : array or CSR matrix, shape (n_samples, n_classes)
  - A matrix such that `y_indicator[i, j] = 1` iff `classes_[j]` is in `y[i]`, and 0 otherwise.

```python
get_params(deep=True)
```

Get parameters for this estimator.

Parameters:

- `deep` : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns:

- `params` : mapping of string to any
  - Parameter names mapped to their values.

```python
inverse_transform(yt)
```

Transform the given indicator matrix into label sets.

Parameters:

- `yt` : array or sparse matrix of shape (n_samples, n_classes)
  - A matrix containing only 1s and 0s.

Returns:

- `y` : list of tuples
  - The set of labels for each sample such that `y[i]` consists of `classes_[j]` for each `yt[i, j] == 1`.

```python
set_params(**params)
```

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

Returns:

- `self`

```python
transform(y)
```

Transform the given label sets.

Parameters:

- `y` : iterable of iterables
A set of labels (any orderable and hashable object) for each sample. If the classes parameter is set, $y$ will not be iterated.

Returns $y_{\text{indicator}}$: array or CSR matrix, shape (n_samples, n_classes)

A matrix such that $y_{\text{indicator}}[i, j] = 1$ iff $\text{classes}_j$ is in $y[i]$, and 0 otherwise.

30.30.8 sklearn.preprocessing.MaxAbsScaler

class sklearn.preprocessing.MaxAbsScaler (copy=True)
Scale each feature by its maximum absolute value.

This estimator scales and translates each feature individually such that the maximal absolute value of each feature in the training set will be 1.0. It does not shift/center the data, and thus does not destroy any sparsity.

This scaler can also be applied to sparse CSR or CSC matrices.

New in version 0.17.

Parameters copy : boolean, optional, default is True

Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

Attributes

scale_ (ndarray, shape (n_features,)) Per feature relative scaling of the data. .. versionadded:: 0.17 scale_ attribute.

max_abs_ (ndarray, shape (n_features,)) Per feature maximum absolute value.

n_samples_seen_ (int) The number of samples processed by the estimator. Will be reset on new calls to fit, but increments across partial_fit calls.

See also:

maxabs_scale Equivalent function without the estimator API.

Notes

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

Methods

fit(X[, y]) Compute the maximum absolute value to be used for later scaling.

fit_transform(X[, y]) Fit to data, then transform it.

get_params([deep]) Get parameters for this estimator.

inverse_transform(X) Scale back the data to the original representation

partial_fit(X[, y]) Online computation of max absolute value of X for later scaling.

set_params(**params) Set the parameters of this estimator.

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<th>Method</th>
<th>Description</th>
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</thead>
<tbody>
<tr>
<td><code>transform(X)</code></td>
<td>Scale the data</td>
</tr>
</tbody>
</table>

__init__ (copy=True)

`fit(X, y=None)`

Compute the maximum absolute value to be used for later scaling.

**Parameters**

- `X`: array-like, sparse matrix, shape [n_samples, n_features]
  
  The data used to compute the per-feature minimum and maximum used for later scaling along the features axis.

`fit_transform(X, y=None, **fit_params)`

Fits transformer to `X` and `y` with optional parameters `fit_params` and returns a transformed version of `X`.

**Parameters**

- `X`: numpy array of shape [n_samples, n_features]
  
  Training set.

- `y`: numpy array of shape [n_samples]
  
  Target values.

**Returns**

- `X_new`: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

get_params (deep=True)

Get parameters for this estimator.

**Parameters**

- `deep`: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- `params`: mapping of string to any
  
  Parameter names mapped to their values.

inverse_transform(X)

Scale back the data to the original representation

**Parameters**

- `X`: array-like, sparse matrix
  
  The data that should be transformed back.

partial_fit(X, y=None)

Online computation of max absolute value of `X` for later scaling. All of `X` is processed as a single batch. This is intended for cases when `fit` is not feasible due to very large number of `n_samples` or because `X` is read from a continuous stream.

**Parameters**

- `X`: array-like, sparse matrix, shape [n_samples, n_features]
  
  The data used to compute the mean and standard deviation used for later scaling along the features axis.

- `y`: Passthrough for Pipeline compatibility.

set_params (**params)

Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

Returns self

**transform** *(X)*
Scale the data

Parameters

**X**: {array-like, sparse matrix}
The data that should be scaled.

Examples using `sklearn.preprocessing.MaxAbsScaler`

- *Compare the effect of different scalers on data with outliers*

### 30.30.9 sklearn.preprocessing.MinMaxScaler

class `sklearn.preprocessing.MinMaxScaler` *(feature_range=(0, 1), copy=True)*

Transforms features by scaling each feature to a given range.

This estimator scales and translates each feature individually such that it is in the given range on the training set, i.e. between zero and one.

The transformation is given by:

$$X_{std} = \frac{X - \text{X.min}(\text{axis}=0)}{\text{X.max}(\text{axis}=0) - \text{X.min}(\text{axis}=0)}$$

$$X_{scaled} = X_{std} \times (\text{max} - \text{min}) + \text{min}$$

where min, max = feature_range.

This transformation is often used as an alternative to zero mean, unit variance scaling.

Read more in the *User Guide*.

Parameters

**feature_range**: tuple (min, max), default=(0, 1)
Desired range of transformed data.

**copy**: boolean, optional, default True
Set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array).

Attributes

| **min_** | (ndarray, shape (n_features,)) Per feature adjustment for minimum. |
| **scale_** | (ndarray, shape (n_features,)) Per feature relative scaling of the data. .. versionadded:: 0.17 |
| **data_min_** | (ndarray, shape (n_features,)) Per feature minimum seen in the data .. versionadded:: 0.17 |
| **data_max_** | (ndarray, shape (n_features,)) Per feature maximum seen in the data .. versionadded:: 0.17 |
| **data_range_** | (ndarray, shape (n_features,)) Per feature range (data_max_ - data_min_) seen in the data .. versionadded:: 0.17 |
See also:

`minmax_scale` Equivalent function without the estimator API.

Notes

For a comparison of the different scalers, transformers, and normalizers, see `examples/preprocessing/plot_all_scaling.py`.

Examples

```python
>>> from sklearn.preprocessing import MinMaxScaler
>>> data = [[-1, 2], [-0.5, 6], [0, 10], [1, 18]]
>>> scaler = MinMaxScaler()
>>> print(scaler.fit(data))
MinMaxScaler(copy=True, feature_range=(0, 1))
>>> print(scaler.data_max_)
[ 1. 18.]
>>> print(scaler.transform(data))
[[ 0. 0.]
 [ 0.25 0.25]
 [ 0.5 0.5]
 [ 1. 1.]]
>>> print(scaler.transform([[2, 2]]))
[[ 1.5 0.]]
```

Methods

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<tr>
<th>Method</th>
<th>Description</th>
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<tbody>
<tr>
<td>fit(X[, y])</td>
<td>Compute the minimum and maximum to be used for later scaling.</td>
</tr>
<tr>
<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>inverse_transform(X)</td>
<td>Undo the scaling of X according to feature_range.</td>
</tr>
<tr>
<td>partial_fit(X[, y])</td>
<td>Online computation of min and max on X for later scaling.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Scaling features of X according to feature_range.</td>
</tr>
</tbody>
</table>

```python
__init__(feature_range=(0, 1), copy=True)
```

```python
fit(X, y=None)
```

Compute the minimum and maximum to be used for later scaling.

**Parameters**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>array-like, shape [n_samples, n_features]</td>
</tr>
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</table>

The data used to compute the per-feature minimum and maximum used for later scaling along the features axis.

```python
fit_transform(X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.
Parameters X : numpy array of shape [n_samples, n_features]
Training set.
y : numpy array of shape [n_samples]
Target values.
Returns X_new : numpy array of shape [n_samples, n_features_new]
Transformed array.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform (X)
Undo the scaling of X according to feature_range.

Parameters X : array-like, shape [n_samples, n_features]
Input data that will be transformed. It cannot be sparse.

partial_fit (X, y=None)
Online computation of min and max on X for later scaling. All of X is processed as a single batch. This is intended for cases when fit is not feasible due to very large number of n_samples or because X is read from a continuous stream.

Parameters X : array-like, shape [n_samples, n_features]
The data used to compute the mean and standard deviation used for later scaling along the features axis.
y : Passthrough for Pipeline compatibility.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Scaling features of X according to feature_range.

Parameters X : array-like, shape [n_samples, n_features]
Input data that will be transformed.

Examples using sklearn.preprocessing.MinMaxScaler

• Compare Stochastic learning strategies for MLPClassifier
• Compare the effect of different scalers on data with outliers
### 30.30.10 sklearn.preprocessing.Normalizer

**class** `sklearn.preprocessing.Normalizer (norm='l2', copy=True)`

Normalize samples individually to unit norm.

Each sample (i.e. each row of the data matrix) with at least one non zero component is rescaled independently of other samples so that its norm (l1 or l2) equals one.

This transformer is able to work both with dense numpy arrays and scipy.sparse matrix (use CSR format if you want to avoid the burden of a copy / conversion).

Scaling inputs to unit norms is a common operation for text classification or clustering for instance. For instance the dot product of two l2-normalized TF-IDF vectors is the cosine similarity of the vectors and is the base similarity metric for the Vector Space Model commonly used by the Information Retrieval community.

Read more in the User Guide.

**Parameters**

- **norm**: ‘l1’, ‘l2’, or ‘max’, optional (‘l2’ by default)
  The norm to use to normalize each non zero sample.

- **copy**: boolean, optional, default True
  set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix).

**See also:**

- `normalize` Equivalent function without the estimator API.

**Notes**

This estimator is stateless (besides constructor parameters), the fit method does nothing but is useful when used in a pipeline.

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

**Methods**

- `fit(X[, y])` Do nothing and return the estimator unchanged

- `fit_transform(X[, y])` Fit to data, then transform it.

- `get_params([deep])` Get parameters for this estimator.

- `set_params(**params)` Set the parameters of this estimator.

- `transform(X[, y, copy])` Scale each non zero row of X to unit norm

- `__init__ (norm='l2', copy=True)`

- `fit (X, y=None)`
  Do nothing and return the estimator unchanged
  
  This method is just there to implement the usual API and hence work in pipelines.

  - **Parameters**
    - `X`: array-like

- `fit_transform (X, y=None, **fit_params)`
  Fit to data, then transform it.
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  - Training set.
- **y**: numpy array of shape [n_samples]
  - Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  - Transformed array.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**set_params**(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**

**transform**(X, y=’deprecated’, copy=None)

Scale each non zero row of X to unit norm

**Parameters**

- **X**: {array-like, sparse matrix}, shape [n_samples, n_features]
  - The data to normalize, row by row. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.
- **y**: (ignored)
  - Deprecated since version 0.19: This parameter will be removed in 0.21.
- **copy**: bool, optional (default: None)
  - Copy the input X or not.

**Examples using sklearn.preprocessing.Normalizer**

- Compare the effect of different scalers on data with outliers
- Clustering text documents using k-means

**30.30.11 sklearn.preprocessing.OneHotEncoder**

Encode categorical integer features using a one-hot aka one-of-K scheme.

```python
class sklearn.preprocessing.OneHotEncoder(n_values='auto', categorical_features='all', dtype=<class 'numpy.float64'>, sparse=True, handle_unknown='error')
```
The input to this transformer should be a matrix of integers, denoting the values taken on by categorical (discrete) features. The output will be a sparse matrix where each column corresponds to one possible value of one feature. It is assumed that input features take on values in the range [0, n_values).

This encoding is needed for feeding categorical data to many scikit-learn estimators, notably linear models and SVMs with the standard kernels.

Note: a one-hot encoding of y labels should use a LabelBinarizer instead.

Read more in the User Guide.

**Parameters**

- `n_values` : ‘auto’, int or array of ints
  
  Number of values per feature.
  
  - ‘auto’ : determine value range from training data.
  
  - int [number of categorical values per feature.] Each feature value should be in range(n_values)
  
  - array [n_values[i] is the number of categorical values in] X[:, i]. Each feature value should be in range(n_values[i])

- `categorical_features` : “all” or array of indices or mask
  
  Specify what features are treated as categorical.
  
  - ‘all’ (default): All features are treated as categorical.
  
  - array of indices: Array of categorical feature indices.
  
  - mask: Array of length n_features and with dtype=bool.

Non-categorical features are always stacked to the right of the matrix.

- `dtype` : number type, default=np.float
  
  Desired dtype of output.

- `sparse` : boolean, default=True
  
  Will return sparse matrix if set True else will return an array.

- `handle_unknown` : str, ‘error’ or ‘ignore’
  
  Whether to raise an error or ignore if a unknown categorical feature is present during transform.

**Attributes**

- `active_features_` : (array) Indices for active features, meaning values that actually occur in the training set. Only available when n_values is ‘auto’.

- `feature_indices_` : (array of shape (n_features,)) Indices to feature ranges. Feature i in the original data is mapped to features from feature_indices_[i] to feature_indices_[i+1] (and then potentially masked by active_features_ afterwards)

- `n_values_` : (array of shape (n_features,)) Maximum number of values per feature.

**See also:**

- `sklearn.feature_extraction.DictVectorizer` performs a one-hot encoding of dictionary items (also handles string-valued features).
**sklearn.feature_extraction.FeatureHasher** performs an approximate one-hot encoding of dictionary items or strings.

**sklearn.preprocessing.LabelBinarizer** binarizes labels in a one-vs-all fashion.

**sklearn.preprocessing.MultiLabelBinarizer** transforms between iterable of iterables and a multilabel format, e.g. a (samples x classes) binary matrix indicating the presence of a class label.

**sklearn.preprocessing.LabelEncoder** encodes labels with values between 0 and n_classes-1.

### Examples

Given a dataset with three features and four samples, we let the encoder find the maximum value per feature and transform the data to a binary one-hot encoding.

```python
>>> from sklearn.preprocessing import OneHotEncoder

>>> enc = OneHotEncoder()
>>> enc.fit([[0, 0, 3], [1, 1, 0], [0, 2, 1], [1, 0, 2]])
OneHotEncoder(categorical_features='all', dtype=<... 'numpy.float64'>,
     handle_unknown='error', n_values='auto', sparse=True)

>>> enc.n_values_
array([2, 3, 4])

>>> enc.feature_indices_
array([0, 2, 5, 9])

>>> enc.transform([[0, 1, 1]]).toarray()
array([[ 1., 0., 0., 1., 0., 0., 1., 0., 0.]])
```

### Methods

- **fit(X[, y])**  
  Fit OneHotEncoder to X.

- **fit_transform(X[, y])**  
  Fit OneHotEncoder to X, then transform X.  
  Equivalent to self.fit(X).transform(X), but more convenient and more efficient. See fit for the parameters, transform for the return value.

- **get_params([deep])**  
  Get parameters for this estimator.

- **set_params(**params)**  
  Set the parameters of this estimator.

- **transform(X)**  
  Transform X using one-hot encoding.

**__init__**(n_values='auto', categorical_features='all', dtype=<class 'numpy.float64'>, sparse=True, handle_unknown='error')

- **fit (X, y=None)**  
  Fit OneHotEncoder to X.

  **Parameters**  
  X : array-like, shape [n_samples, n_feature]

  Input array of type int.

  **Returns**  
  self

- **fit_transform (X, y=None)**  
  Fit OneHotEncoder to X, then transform X.

  Equivalent to self.fit(X).transform(X), but more convenient and more efficient. See fit for the parameters, transform for the return value.

  **Parameters**  
  X : array-like, shape [n_samples, n_feature]

  Input array of type int.
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

transform (X)
Transform X using one-hot encoding.

Parameters X : array-like, shape [n_samples, n_features]
Input array of type int.

Returns X_out : sparse matrix if sparse=True else a 2-d array, dtype=int
Transformed input.

Examples using sklearn.preprocessing.OneHotEncoder

• Feature transformations with ensembles of trees

30.30.12 sklearn.preprocessing.PolynomialFeatures

class sklearn.preprocessing.PolynomialFeatures (degree=2, interaction_only=False, include_bias=True)
Generate polynomial and interaction features.

Generate a new feature matrix consisting of all polynomial combinations of the features with degree less than or equal to the specified degree. For example, if an input sample is two dimensional and of the form [a, b], the degree-2 polynomial features are [1, a, b, a^2, ab, b^2].

Parameters degree : integer
The degree of the polynomial features. Default = 2.

interaction_only : boolean, default = False
If true, only interaction features are produced: features that are products of at most degree distinct input features (so not x[1] ** 2, x[0] * x[2] ** 3, etc.).

include_bias : boolean
If True (default), then include a bias column, the feature in which all polynomial powers are zero (i.e. a column of ones - acts as an intercept term in a linear model).
Attributes

<table>
<thead>
<tr>
<th>powers_</th>
<th>(array, shape (n_output_features, n_input_features)) powers_[i, j] is the exponent of the jth input in the ith output.</th>
</tr>
</thead>
<tbody>
<tr>
<td>n_input_features</td>
<td>The total number of input features.</td>
</tr>
<tr>
<td>n_output_features</td>
<td>The total number of polynomial output features. The number of output features is computed by iterating over all suitably sized combinations of input features.</td>
</tr>
</tbody>
</table>

Notes

Be aware that the number of features in the output array scales polynomially in the number of features of the input array, and exponentially in the degree. High degrees can cause overfitting.

See examples/linear_model/plot_polynomial_interpolation.py

Examples

```python
>>> X = np.arange(6).reshape(3, 2)
>>> X
array([[0, 1],
       [2, 3],
       [4, 5]])
>>> poly = PolynomialFeatures(2)
>>> poly.fit_transform(X)
array([[ 1., 0., 1., 0., 0., 1.],
       [ 1., 2., 3., 4., 6., 9.],
       [ 1., 4., 5., 16., 20., 25.]])
>>> poly = PolynomialFeatures(interaction_only=True)
>>> poly.fit_transform(X)
array([[ 1., 0., 1., 0.],
       [ 1., 2., 3., 6.],
       [ 1., 4., 5., 20.]])
```

Methods

- `fit(X[, y])`: Compute number of output features.
- `fit_transform(X[, y])`: Fit to data, then transform it.
- `get_feature_names([input_features])`: Return feature names for output features
- `get_params([deep])`: Get parameters for this estimator.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(X)`: Transform data to polynomial features

```python
__init__(degree=2, interaction_only=False, include_bias=True)

fit(X, y=None)
    Compute number of output features.
    Parameters X : array-like, shape (n_samples, n_features)
    The data.
```

1948 Chapter 30. API Reference
Returns self: instance

**fit_transform** *(X, y=None, **fit_params)*
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  Training set.

- **y**: numpy array of shape [n_samples]
  Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  Transformed array.

**get_feature_names** *(input_features=None)*
Return feature names for output features

**Parameters**

- **input_features**: list of string, length n_features, optional
  String names for input features if available. By default, “x0”, “x1”, . . . “xn_features” is used.

**Returns**

- **output_feature_names**: list of string, length n_output_features

**get_params** *(deep=True)*
Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  Parameter names mapped to their values.

**set_params** *(**params)*
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**transform** *(X)*
Transform data to polynomial features

**Parameters**

- **X**: array-like, shape [n_samples, n_features]
  The data to transform, row by row.

**Returns**

- **XP**: np.ndarray shape [n_samples, NP]
  The matrix of features, where NP is the number of polynomial features generated from the combination of inputs.

**Examples using sklearn.preprocessing.PolynomialFeatures**

- **Polynomial interpolation**
30.30.13 sklearn.preprocessing.QuantileTransformer

```python
class sklearn.preprocessing.QuantileTransformer (n_quantiles=1000, output_distribution='uniform', ignore_implicit_zeros=False, subsample=100000, random_state=None, copy=True)
```

Transform features using quantiles information.

This method transforms the features to follow a uniform or a normal distribution. Therefore, for a given feature, this transformation tends to spread out the most frequent values. It also reduces the impact of (marginal) outliers: this is therefore a robust preprocessing scheme.

The transformation is applied on each feature independently. The cumulative density function of a feature is used to project the original values. Features values of new/unseen data that fall below or above the fitted range will be mapped to the bounds of the output distribution. Note that this transform is non-linear. It may distort linear correlations between variables measured at the same scale but renders variables measured at different scales more directly comparable.

Read more in the User Guide.

**Parameters**

- `n_quantiles` : int, optional (default=1000)
  
  Number of quantiles to be computed. It corresponds to the number of landmarks used to discretize the cumulative density function.

- `output_distribution` : str, optional (default='uniform')
  
  Marginal distribution for the transformed data. The choices are ‘uniform’ (default) or ‘normal’.

- `ignore_implicit_zeros` : bool, optional (default=False)
  
  Only applies to sparse matrices. If True, the sparse entries of the matrix are discarded to compute the quantile statistics. If False, these entries are treated as zeros.

- `subsample` : int, optional (default=1e5)
  
  Maximum number of samples used to estimate the quantiles for computational efficiency. Note that the subsampling procedure may differ for value-identical sparse and dense matrices.

- `random_state` : int, RandomState instance or None, optional (default=None)
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Note that this is used by subsampling and smoothing noise.

- `copy` : boolean, optional, (default=True)
  
  Set to False to perform inplace transformation and avoid a copy (if the input is already a numpy array).
Attributes

| quantiles_ | (ndarray, shape (n_quantiles, n_features)) The values corresponding the quantiles of reference. |
| references_ | (ndarray, shape(n_quantiles, )) Quantiles of references. |

See also:

quantile_transform  Equivalent function without the estimator API.
StandardScaler  perform standardization that is faster, but less robust to outliers.
RobustScaler  perform robust standardization that removes the influence of outliers but does not put outliers and inliers on the same scale.

Notes

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

Examples

```python
>>> import numpy as np
>>> from sklearn.preprocessing import QuantileTransformer
>>> rng = np.random.RandomState(0)
>>> X = np.sort(rng.normal(loc=0.5, scale=0.25, size=(25, 1)), axis=0)
>>> qt = QuantileTransformer(n_quantiles=10, random_state=0)
>>> qt.fit_transform(X)
array([[...]])
```

Methods

- `fit(X[, y])`: Compute the quantiles used for transforming.
- `fit_transform(X[, y])`: Fit to data, then transform it.
- `get_params([deep])`: Get parameters for this estimator.
- `inverse_transform(X)`: Back-projection to the original space.
- `set_params(**params)`: Set the parameters of this estimator.
- `transform(X)`: Feature-wise transformation of the data.

```
__init__(n_quantiles=1000, output_distribution='uniform', ignore_implicit_zeros=False, subsample=100000, random_state=None, copy=True)

fit(X, y=None)
Compute the quantiles used for transforming.

Parameters X : ndarray or sparse matrix, shape (n_samples, n_features)
The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore_implicit_zeros is False.
```
Returns self: object

Returns self

**fit_transform** *(X, y=None, **fit_params)*
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters

- **X**: numpy array of shape [n_samples, n_features]
  - Training set.
- **y**: numpy array of shape [n_samples]
  - Target values.

Returns

- **X_new**: numpy array of shape [n_samples, n_features_new]
  - Transformed array.

**get_params** *(deep=True)*
Get parameters for this estimator.

Parameters

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns

- **params**: mapping of string to any
  - Parameter names mapped to their values.

**inverse_transform** *(X)*
Back-projection to the original space.

Parameters

- **X**: ndarray or sparse matrix, shape (n_samples, n_features)
  - The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore_implicit_zeros is False.

Returns

- **Xt**: ndarray or sparse matrix, shape (n_samples, n_features)
  - The projected data.

**set_params** *(**params)*
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns

- **self**

**transform** *(X)*
Feature-wise transformation of the data.

Parameters

- **X**: ndarray or sparse matrix, shape (n_samples, n_features)
  - The data used to scale along the features axis. If a sparse matrix is provided, it will be converted into a sparse csc_matrix. Additionally, the sparse matrix needs to be nonnegative if ignore_implicit_zeros is False.

Returns

- **Xt**: ndarray or sparse matrix, shape (n_samples, n_features)
  - The projected data.
Examples using `sklearn.preprocessing.QuantileTransformer`

- Compare the effect of different scalers on data with outliers

### 30.30.14 sklearn.preprocessing.RobustScaler

**class sklearn.preprocessing.RobustScaler**

```python
class sklearn.preprocessing.RobustScaler(with_centering=True, with_scaling=True, quantile_range=(25.0, 75.0), copy=True)
```

Scale features using statistics that are robust to outliers.

This Scaler removes the median and scales the data according to the quantile range (defaults to IQR: Interquartile Range). The IQR is the range between the 1st quartile (25th quantile) and the 3rd quartile (75th quantile).

Centering and scaling happen independently on each feature (or each sample, depending on the `axis` argument) by computing the relevant statistics on the samples in the training set. Median and interquartile range are then stored to be used on later data using the `transform` method.

Standardization of a dataset is a common requirement for many machine learning estimators. Typically this is done by removing the mean and scaling to unit variance. However, outliers can often influence the sample mean / variance in a negative way. In such cases, the median and the interquartile range often give better results.

New in version 0.17.

Read more in the *User Guide*.

**Parameters**

- `with_centering` : boolean, True by default
  
  If True, center the data before scaling. This will cause `transform` to raise an exception when attempted on sparse matrices, because centering them entails building a dense matrix which in common use cases is likely to be too large to fit in memory.

- `with_scaling` : boolean, True by default
  
  If True, scale the data to interquartile range.

- `quantile_range` : tuple (q_min, q_max), 0.0 < q_min < q_max < 100.0
  
  Default: (25.0, 75.0) = (1st quantile, 3rd quantile) = IQR Quantile range used to calculate `scale_`.
  
  New in version 0.18.

- `copy` : boolean, optional, default is True
  
  If False, try to avoid a copy and do inplace scaling instead. This is not guaranteed to always work inplace; e.g. if the data is not a NumPy array or scipy.sparse CSR matrix, a copy may still be returned.

**Attributes**

<table>
<thead>
<tr>
<th>attribute</th>
<th>description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>center_</code></td>
<td>(array of floats) The median value for each feature in the training set.</td>
</tr>
<tr>
<td><code>scale_</code></td>
<td>(array of floats) The (scaled) interquartile range for each feature in the training set. .. versionadded:: 0.17 <code>scale_</code> attribute.</td>
</tr>
</tbody>
</table>

**See also:**

- `robust_scale` Equivalent function without the estimator API.
sklearn.decomposition.PCA Further removes the linear correlation across features with `whiten=True`.

**Notes**

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.


**Methods**

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>fit(X[, y])</code></td>
<td>Compute the median and quantiles to be used for scaling.</td>
</tr>
<tr>
<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>inverse_transform(X)</code></td>
<td>Scale back the data to the original representation</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Center and scale the data.</td>
</tr>
</tbody>
</table>

**__init__** *(with_centering=True, with_scaling=True, quantile_range=(25.0, 75.0), copy=True)*

**fit** *(X, y=None)*

Compute the median and quantiles to be used for scaling.

**Parameters**

- **X**: array-like, shape [n_samples, n_features]
  - The data used to compute the median and quantiles used for later scaling along the features axis.

**fit_transform** *(X, y=None, **fit_params)*

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  - Training set.
- **y**: numpy array of shape [n_samples]
  - Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  - Transformed array.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
  - Parameter names mapped to their values.
inverse_transform(X)
    Scale back the data to the original representation

    Parameters X : array-like
        The data used to scale along the specified axis.

set_params(**params)
    Set the parameters of this estimator.

    The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
    parameters of the form <component>__<parameter> so that it's possible to update each component
    of a nested object.

    Returns self

transform(X)
    Center and scale the data.

    Can be called on sparse input, provided that RobustScaler has been fitted to dense input and
    with_centering=False.

    Parameters X : {array-like, sparse matrix}
        The data used to scale along the specified axis.

Examples using sklearn.preprocessing.RobustScaler

- Compare the effect of different scalers on data with outliers

30.30.15 sklearn.preprocessing.StandardScaler

class sklearn.preprocessing.StandardScaler(copy=True, with_mean=True, with_std=True)
    Standardize features by removing the mean and scaling to unit variance

    Centering and scaling happen independently on each feature by computing the relevant statistics on the samples
    in the training set. Mean and standard deviation are then stored to be used on later data using the transform
    method.

    Standardization of a dataset is a common requirement for many machine learning estimators: they might behave
    badly if the individual feature do not more or less look like standard normally distributed data (e.g. Gaussian
    with 0 mean and unit variance).

    For instance many elements used in the objective function of a learning algorithm (such as the RBF kernel of
    Support Vector Machines or the L1 and L2 regularizers of linear models) assume that all features are centered
    around 0 and have variance in the same order. If a feature has a variance that is orders of magnitude larger
    that others, it might dominate the objective function and make the estimator unable to learn from other features
    correctly as expected.

    This scaler can also be applied to sparse CSR or CSC matrices by passing with_mean=False to avoid breaking
    the sparsity structure of the data.

    Read more in the User Guide.

    Parameters copy : boolean, optional, default True
        If False, try to avoid a copy and do inplace scaling instead. This is not guaranteed to
        always work inplace; e.g. if the data is not a NumPy array or scipy.sparse CSR matrix,
        a copy may still be returned.

        with_mean : boolean, True by default
If True, center the data before scaling. This does not work (and will raise an exception) when attempted on sparse matrices, because centering them entails building a dense matrix which in common use cases is likely to be too large to fit in memory.

**with_std**: boolean, True by default

If True, scale the data to unit variance (or equivalently, unit standard deviation).

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>scale_</code></td>
<td>(ndarray, shape (n_features,)) Per feature relative scaling of the data. .. versionadded:: 0.17</td>
</tr>
<tr>
<td><code>mean_</code></td>
<td>(array of floats with shape [n_features]) The mean value for each feature in the training set.</td>
</tr>
<tr>
<td><code>var_</code></td>
<td>(array of floats with shape [n_features]) The variance for each feature in the training set. Used to compute <code>scale_</code>.</td>
</tr>
<tr>
<td><code>n_samples_seen_</code></td>
<td>The number of samples processed by the estimator. Will be reset on new calls to fit, but increments across <code>partial_fit</code> calls.</td>
</tr>
</tbody>
</table>

### See also:

- **scale**: Equivalent function without the estimator API.
- **sklearn.decomposition.PCA**: Further removes the linear correlation across features with ‘whiten=True’.

### Notes

For a comparison of the different scalers, transformers, and normalizers, see `examples/preprocessing/plot_all_scaling.py`.

### Examples

```python
>>> from sklearn.preprocessing import StandardScaler
>>> data = [[0, 0], [0, 0], [1, 1], [1, 1]]
>>> scaler = StandardScaler()
>>> print(scaler.fit(data))
StandardScaler(copy=True, with_mean=True, with_std=True)
>>> print(scaler.mean_)
[ 0.5 0.5]
>>> print(scaler.transform(data))
[[-1. -1.]
 [-1. -1.]
 [ 1.  1.]
 [ 1.  1.]]
>>> print(scaler.transform([[2, 2]]))
[[ 3.  3.]]
```

### Methods
fit(X, y)
Compute the mean and std to be used for later scaling.

fit_transform(X, y)
Fit to data, then transform it.

get_params([deep])
Get parameters for this estimator.

inverse_transform(X[, copy])
Scale back the data to the original representation

partial_fit(X[, y])
Online computation of mean and std on X for later scaling.

set_params(**params)
Set the parameters of this estimator.

transform(X[, y, copy])
Perform standardization by centering and scaling

__init__(copy=True, with_mean=True, with_std=True)
Compute the mean and std to be used for later scaling.

Parameters X : {array-like, sparse matrix}, shape [n_samples, n_features]
The data used to compute the mean and standard deviation used for later scaling along
the features axis.

y : Passthrough for Pipeline compatibility.

fit_transform(X, y=\text{None}, **fit_params)
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]
Training set.

y : numpy array of shape [n_samples]
Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]
Transformed array.

get_params(deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

inverse_transform(X, copy=\text{None})
Scale back the data to the original representation

Parameters X : array-like, shape [n_samples, n_features]
The data used to scale along the features axis.

copy : bool, optional (default: \text{None})
Copy the input X or not.

Returns X_tr : array-like, shape [n_samples, n_features]
Transformed array.
**partial_fit** *(X, y=None)*

Online computation of mean and std on X for later scaling. All of X is processed as a single batch. This is intended for cases when *fit* is not feasible due to very large number of *n_samples* or because X is read from a continuous stream.

The algorithm for incremental mean and std is given in Equation 1.5a,b in Chan, Tony F., Gene H. Golub, and Randall J. LeVeque. “Algorithms for computing the sample variance: Analysis and recommendations.” The American Statistician 37.3 (1983): 242-247:

Parameters

- **X**: {array-like, sparse matrix}, shape [n_samples, n_features]
  
  The data used to compute the mean and standard deviation used for later scaling along the features axis.

- **y**: Passthrough for Pipeline compatibility.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns

- **self**

**transform** *(X, y='deprecated', copy=None)*

Perform standardization by centering and scaling

Parameters

- **X**: array-like, shape [n_samples, n_features]
  
  The data used to scale along the features axis.

- **y**: (ignored)
  
  Deprecated since version 0.19: This parameter will be removed in 0.21.

- **copy**: bool, optional (default: None)
  
  Copy the input X or not.

Examples using sklearn.preprocessing.StandardScaler

- Prediction Latency
- Classifier comparison
- Demo of DBSCAN clustering algorithm
- Comparing different clustering algorithms on toy datasets
- MNIST classification using multinomial logistic + L1
- L1 Penalty and Sparsity in Logistic Regression
- Varying regularization in Multi-layer Perceptron
- Importance of Feature Scaling
- Compare the effect of different scalers on data with outliers
- RBF SVM parameters

**preprocessing.add_dummy_feature** *(X[, value])*  
Augment dataset with an additional dummy feature.

Continued on next page
Table 30.280 – continued from previous page

<table>
<thead>
<tr>
<th>Function</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>preprocessing.binarize(X[, threshold, copy])</code></td>
<td>Boolean thresholding of array-like or scipy.sparse matrix</td>
</tr>
<tr>
<td><code>preprocessing.label_binarize(y, classes[...])</code></td>
<td>Binarize labels in a one-vs-all fashion</td>
</tr>
<tr>
<td><code>preprocessing.maxabs_scale(X[, axis, copy])</code></td>
<td>Scale each feature to the [-1, 1] range without breaking the sparsity.</td>
</tr>
<tr>
<td><code>preprocessing.minmax_scale(X[, ...])</code></td>
<td>Transforms features by scaling each feature to a given range.</td>
</tr>
<tr>
<td><code>preprocessing.normalize(X[, norm, axis, ...])</code></td>
<td>Scale input vectors individually to unit norm (vector length).</td>
</tr>
<tr>
<td><code>preprocessing.quantile_transform(X[, axis,...])</code></td>
<td>Transform features using quantiles information.</td>
</tr>
<tr>
<td><code>preprocessing.robust_scale(X[, axis,...])</code></td>
<td>Standardize a dataset along any axis</td>
</tr>
<tr>
<td><code>preprocessing.scale(X[, axis, with_mean,...])</code></td>
<td>Standardize a dataset along any axis</td>
</tr>
</tbody>
</table>

### 30.30.16 sklearn.preprocessing.add_dummy_feature

`sklearn.preprocessing.add_dummy_feature(X, value=1.0)`

Augment dataset with an additional dummy feature.

This is useful for fitting an intercept term with implementations which cannot otherwise fit it directly.

**Parameters**

- **X**: [array-like, sparse matrix], shape [n_samples, n_features]
  
  Data.

- **value**: float
  
  Value to use for the dummy feature.

**Returns**

- **X**: [array, sparse matrix], shape [n_samples, n_features + 1]
  
  Same data with dummy feature added as first column.

### Examples

```python
>>> from sklearn.preprocessing import add_dummy_feature
>>> add_dummy_feature([[0, 1], [1, 0]])
array([[ 1., 0., 1.],
       [ 1., 1., 0.]])
```

### 30.30.17 sklearn.preprocessing.binarize

`sklearn.preprocessing.binarize(X, threshold=0.0, copy=True)`

Boolean thresholding of array-like or scipy.sparse matrix

Read more in the [User Guide](https://www.example.com).

**Parameters**

- **X**: [array-like, sparse matrix], shape [n_samples, n_features]
  
  The data to binarize, element by element. scipy.sparse matrices should be in CSR or CSC format to avoid an un-necessary copy.

- **threshold**: float, optional (0.0 by default)
  
  Feature values below or equal to this are replaced by 0, above it by 1. Threshold may not be less than 0 for operations on sparse matrices.
**copy**: boolean, optional, default True

set to False to perform inplace binarization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR / CSC matrix and if axis is 1).

See also:

**Binarizer** Performs binarization using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

### 30.30.18 sklearn.preprocessing.label_binarize

```python
sklearn.preprocessing.label_binarize(y, classes, neg_label=0, pos_label=1, sparse_output=False)
```

Binarize labels in a one-vs-all fashion

Several regression and binary classification algorithms are available in the scikit. A simple way to extend these algorithms to the multi-class classification case is to use the so-called one-vs-all scheme.

This function makes it possible to compute this transformation for a fixed set of class labels known ahead of time.

**Parameters**

- `y` : array-like
  Sequence of integer labels or multilabel data to encode.
- `classes` : array-like of shape [n_classes]
  Uniquely holds the label for each class.
- `neg_label` : int (default: 0)
  Value with which negative labels must be encoded.
- `pos_label` : int (default: 1)
  Value with which positive labels must be encoded.
- `sparse_output` : boolean (default: False),
  Set to true if output binary array is desired in CSR sparse format

**Returns**

- `Y` : numpy array or CSR matrix of shape [n_samples, n_classes]
  Shape will be [n_samples, 1] for binary problems.

See also:

**LabelBinarizer** class used to wrap the functionality of label_binarize and allow for fitting to classes independently of the transform operation

**Examples**

```python
>>> from sklearn.preprocessing import label_binarize
>>> label_binarize([1, 6], classes=[1, 2, 4, 6])
array([[1, 0, 0, 0],
       [0, 0, 0, 1]])
```

The class ordering is preserved:
```python
>>> label_binarize([1, 6], classes=[1, 6, 4, 2])
array([[1, 0, 0, 0],
       [0, 1, 0, 0]])
```

Binary targets transform to a column vector

```python
>>> label_binarize(['yes', 'no', 'no', 'yes'], classes=['no', 'yes'])
array([[1],
       [0],
       [0],
       [1]])
```

Examples using `sklearn.preprocessing.label_binarize`

- Receiver Operating Characteristic (ROC)
- Precision-Recall

30.30.19 sklearn.preprocessing.maxabs_scale

`sklearn.preprocessing.maxabs_scale(X, axis=0, copy=True)`
Scale each feature to the [-1, 1] range without breaking the sparsity.

This estimator scales each feature individually such that the maximal absolute value of each feature in the training set will be 1.0.

This scaler can also be applied to sparse CSR or CSC matrices.

**Parameters**

- `X`: array-like, shape (n_samples, n_features)
  The data.
- `axis`: int (0 by default)
  axis used to scale along. If 0, independently scale each feature, otherwise (if 1) scale each sample.
- `copy`: boolean, optional, default is True
  Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

**See also:**

- `MaxAbsScaler` Performs scaling to the [-1, 1] range using the “Transformer” API (e.g. as part of a pre-processing `sklearn.pipeline.Pipeline`).

**Notes**

For a comparison of the different scalers, transformers, and normalizers, see `examples/preprocessing/plot_all_scaling.py`. 
30.30.20 sklearn.preprocessing.minmax_scale

sklearn.preprocessing.minmax_scale(X, feature_range=(0, 1), axis=0, copy=True)

Transforms features by scaling each feature to a given range.

This estimator scales and translates each feature individually such that it is in the given range on the training set, i.e. between zero and one.

The transformation is given by:

\[
X_{\text{std}} = \frac{X - \text{X.min}(\text{axis}=0)}{\text{X.max}(\text{axis}=0) - \text{X.min}(\text{axis}=0)}
\]

\[
X_{\text{scaled}} = X_{\text{std}} \times (\text{max} - \text{min}) + \text{min}
\]

where min, max = feature_range.

This transformation is often used as an alternative to zero mean, unit variance scaling.

Read more in the User Guide.

New in version 0.17: minmax_scale function interface to sklearn.preprocessing.MinMaxScaler.

Parameters

- **X**: array-like, shape (n_samples, n_features)
  The data.
- **feature_range**: tuple (min, max), default=(0, 1)
  Desired range of transformed data.
- **axis**: int (0 by default)
  Axis used to scale along. If 0, independently scale each feature, otherwise (if 1) scale each sample.
- **copy**: boolean, optional, default is True
  Set to False to perform inplace scaling and avoid a copy (if the input is already a numpy array).

See also:

MinMaxScaler Performs scaling to a given range using the “Transformer” API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

Notes

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

Examples using sklearn.preprocessing.minmax_scale

- Compare the effect of different scalers on data with outliers

30.30.21 sklearn.preprocessing.normalize

sklearn.preprocessing.normalize(X, norm='l2', axis=1, copy=True, return_norm=False)

Scale input vectors individually to unit norm (vector length).

Read more in the User Guide.
Parameters

\( \textbf{X} \) : \{array-like, sparse matrix\}, shape \([\text{n}\_\text{samples}, \text{n}\_\text{features}]\)

The data to normalize, element by element. scipy.sparse matrices should be in CSR format to avoid an un-necessary copy.

\textbf{norm} : ‘l1’, ‘l2’, or ‘max’, optional (‘l2’ by default)

The norm to use to normalize each non zero sample (or each non-zero feature if axis is 0).

\textbf{axis} : 0 or 1, optional (1 by default)

axis used to normalize the data along. If 1, independently normalize each sample, otherwise (if 0) normalize each feature.

\textbf{copy} : boolean, optional, default True

set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix and if axis is 1).

\textbf{return\_norm} : boolean, default False

whether to return the computed norms

Returns

\( \textbf{X} \) : \{array-like, sparse matrix\}, shape \([\text{n}\_\text{samples}, \text{n}\_\text{features}]\)

Normalized input X.

\textbf{norms} : array, shape \([\text{n}\_\text{samples}]\) if axis=1 else \([\text{n}\_\text{features}]\)

An array of norms along given axis for X. When X is sparse, a NotImplementedError will be raised for norm ‘l1’ or ‘l2’.

\textbf{See also:}

\textit{Normalizer} Performs normalization using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

\textbf{Notes}

For a comparison of the different scalers, transformers, and normalizers, see \texttt{examples/preprocessing/plot\_all\_scaling.py}.

30.30.22 \texttt{sklearn.preprocessing.quantile\_transform}

\texttt{sklearn.preprocessing.quantile\_transform}(X, axis=0, n\_quantiles=1000, output\_distribution='uniform', ignore\_implicit\_zeros=False, subsample=100000, random\_state=None, copy=False)

Transform features using quantiles information.

This method transforms the features to follow a uniform or a normal distribution. Therefore, for a given feature, this transformation tends to spread out the most frequent values. It also reduces the impact of (marginal) outliers: this is therefore a robust preprocessing scheme.

The transformation is applied on each feature independently. The cumulative density function of a feature is used to project the original values. Features values of new/unseen data that fall below or above the fitted range will be mapped to the bounds of the output distribution. Note that this transform is non-linear. It may distort linear correlations between variables measured at the same scale but renders variables measured at different scales more directly comparable.
Read more in the *User Guide*.

**Parameters**

- **X** : array-like, sparse matrix
  The data to transform.
- **axis** : int, (default=0)
  Axis used to compute the means and standard deviations along. If 0, transform each feature, otherwise (if 1) transform each sample.
- **n_quantiles** : int, optional (default=1000)
  Number of quantiles to be computed. It corresponds to the number of landmarks used to discretize the cumulative density function.
- **output_distribution** : str, optional (default='uniform')
  Marginal distribution for the transformed data. The choices are 'uniform' (default) or 'normal'.
- **ignore_implicit_zeros** : bool, optional (default=False)
  Only applies to sparse matrices. If True, the sparse entries of the matrix are discarded to compute the quantile statistics. If False, these entries are treated as zeros.
- **subsample** : int, optional (default=1e5)
  Maximum number of samples used to estimate the quantiles for computational efficiency. Note that the subsampling procedure may differ for value-identical sparse and dense matrices.
- **random_state** : int, RandomState instance or None, optional (default=None)
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Note that this is used by subsampling and smoothing noise.
- **copy** : boolean, optional, (default=True)
  Set to False to perform inplace transformation and avoid a copy (if the input is already a numpy array).

**Attributes**

- **quantiles_**
  (ndarray, shape (n_quantiles, n_features)) The values corresponding the quantiles of reference.
- **references_**
  (ndarray, shape(n_quantiles, )) Quantiles of references.

**See also:**

- **QuantileTransformer** Performs quantile-based scaling using the Transformer API (e.g. as part of a preprocessing `sklearn.pipeline.Pipeline`).
- **scale** perform standardization that is faster, but less robust to outliers.
- **robust_scale** perform robust standardization that removes the influence of outliers but does not put outliers and inliers on the same scale.
Notes

For a comparison of the different scalers, transformers, and normalizers, see `examples/preprocessing/plot_all_scaling.py`.

Examples

```python
>>> import numpy as np
>>> from sklearn.preprocessing import quantile_transform
>>> rng = np.random.RandomState(0)
>>> X = np.sort(rng.normal(loc=0.5, scale=0.25, size=(25, 1)), axis=0)
>>> quantile_transform(X, n_quantiles=10, random_state=0)
... array([...])
```

30.30.23 sklearn.preprocessing.robust_scale

`sklearn.preprocessing.robust_scale` (X, axis=0, with_centering=True, with_scaling=True, quantile_range=(25.0, 75.0), copy=True)

Standardize a dataset along any axis.

Center to the median and component wise scale according to the interquartile range.

Read more in the `User Guide`.

Parameters

- **X**: array-like
  - The data to center and scale.

- **axis**: int (0 by default)
  - axis used to compute the medians and IQR along. If 0, independently scale each feature, otherwise (if 1) scale each sample.

- **with_centering**: boolean, True by default
  - If True, center the data before scaling.

- **with_scaling**: boolean, True by default
  - If True, scale the data to unit variance (or equivalently, unit standard deviation).

- **quantile_range**: tuple (q_min, q_max), 0.0 < q_min < q_max < 100.0
  - Default: (25.0, 75.0) = (1st quantile, 3rd quantile) = IQR Quantile range used to calculate scale_.
  - New in version 0.18.

- **copy**: boolean, optional, default is True
  - set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSR matrix and if axis is 1).

See also:

- `RobustScaler` Performs centering and scaling using the `Transformer API` (e.g. as part of a preprocessing `sklearn.pipeline.Pipeline`).
Notes

This implementation will refuse to center scipy.sparse matrices since it would make them non-sparse and would potentially crash the program with memory exhaustion problems.

Instead the caller is expected to either set explicitly with_centering=False (in that case, only variance scaling will be performed on the features of the CSR matrix) or to call X.toarray() if he/she expects the materialized dense array to fit in memory.

To avoid memory copy the caller should pass a CSR matrix.

For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

30.30.24 sklearn.preprocessing.scale

sklearn.preprocessing.scale(X, axis=0, with_mean=True, with_std=True, copy=True)

Standardize a dataset along any axis

Center to the mean and component wise scale to unit variance.

Read more in the User Guide.

Parameters X : {array-like, sparse matrix}
The data to center and scale.

axis : int (0 by default)
axis used to compute the means and standard deviations along. If 0, independently standardize each feature, otherwise (if 1) standardize each sample.

with_mean : boolean, True by default
If True, center the data before scaling.

with_std : boolean, True by default
If True, scale the data to unit variance (or equivalently, unit standard deviation).

copy : boolean, optional, default True
set to False to perform inplace row normalization and avoid a copy (if the input is already a numpy array or a scipy.sparse CSC matrix and if axis is 1).

See also:

StandardScaler Performs scaling to unit variance using the Transformer API (e.g. as part of a preprocessing sklearn.pipeline.Pipeline).

Notes

This implementation will refuse to center scipy.sparse matrices since it would make them non-sparse and would potentially crash the program with memory exhaustion problems.

Instead the caller is expected to either set explicitly with_mean=False (in that case, only variance scaling will be performed on the features of the CSC matrix) or to call X.toarray() if he/she expects the materialized dense array to fit in memory.

To avoid memory copy the caller should pass a CSC matrix.
For a comparison of the different scalers, transformers, and normalizers, see examples/preprocessing/plot_all_scaling.py.

Examples using sklearn.preprocessing.scale

- A demo of K-Means clustering on the handwritten digits data

30.31 sklearn.random_projection: Random projection

Random Projection transformers

Random Projections are a simple and computationally efficient way to reduce the dimensionality of the data by trading a controlled amount of accuracy (as additional variance) for faster processing times and smaller model sizes.

The dimensions and distribution of Random Projections matrices are controlled so as to preserve the pairwise distances between any two samples of the dataset.

The main theoretical result behind the efficiency of random projection is the Johnson-Lindenstrauss lemma (quoting Wikipedia):

In mathematics, the Johnson-Lindenstrauss lemma is a result concerning low-distortion embeddings of points from high-dimensional into low-dimensional Euclidean space. The lemma states that a small set of points in a high-dimensional space can be embedded into a space of much lower dimension in such a way that distances between the points are nearly preserved. The map used for the embedding is at least Lipschitz, and can even be taken to be an orthogonal projection.

User guide: See the Random Projection section for further details.

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<tr>
<td>random_projection.</td>
<td>SparseRandomProjection([...])</td>
<td>Reduce dimensionality through sparse random projection</td>
</tr>
</tbody>
</table>

30.31.1 sklearn.random_projection.GaussianRandomProjection

class sklearn.random_projection.GaussianRandomProjection(n_components='auto', eps=0.1, random_state=None)

Reduce dimensionality through Gaussian random projection

The components of the random matrix are drawn from N(0, 1 / n_components).

Read more in the User Guide.

Parameters n_components : int or ‘auto’, optional (default = ‘auto’)

Dimensionality of the target projection space.

n_components can be automatically adjusted according to the number of samples in the dataset and the bound given by the Johnson-Lindenstrauss lemma. In that case the quality of the embedding is controlled by the eps parameter.

It should be noted that Johnson-Lindenstrauss lemma can yield very conservative estimated of the required number of components as it makes no assumption on the structure of the dataset.
eps : strictly positive float, optional (default=0.1)
Parameter to control the quality of the embedding according to the Johnson-
Lindenstrauss lemma when n_components is set to ‘auto’.
Smaller values lead to better embedding and higher number of dimensions
(n_components) in the target projection space.

random_state : int, RandomState instance or None, optional (default=None)
Control the pseudo random number generator used to generate the matrix at fit time.
If int, random_state is the seed used by the random number generator; If RandomState
instance, random_state is the random number generator; If None, the random number
generator is the RandomState instance used by np.random.

Attributes

<table>
<thead>
<tr>
<th>n_components_</th>
<th>(int) Concrete number of components computed when n_components=”auto”.</th>
</tr>
</thead>
<tbody>
<tr>
<td>components_</td>
<td>(numpy array of shape [n_components, n_features]) Random matrix used for the projection.</td>
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See also:
SparseRandomProjection

Methods

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<td>fit_transform(X[, y])</td>
<td>Fit to data, then transform it.</td>
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<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
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<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Project the data by using matrix product with the random matrix</td>
</tr>
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</table>

__init__ (n_components='auto', eps=0.1, random_state=None)

fit (X, y=None)
Generate a sparse random projection matrix

Parameters X : numpy array or scipy.sparse of shape [n_samples, n_features]
Training set: only the shape is used to find optimal random matrix dimensions based on
the theory referenced in the afore mentioned papers.

y : is not used: placeholder to allow for usage in a Pipeline.

Returns self

fit_transform (X, y=None, **fit_params)
Fit to data, then transform it.
Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]
Training set.
y : numpy array of shape [n_samples]

   Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]

   Transformed array.

get_params (deep=True)

   Get parameters for this estimator.

Parameters deep : boolean, optional

   If True, will return the parameters for this estimator and contained subobjects that are
   estimators.

Returns params : mapping of string to any

   Parameter names mapped to their values.

set_params (**params)

   Set the parameters of this estimator.

   The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
   parameters of the form <component>__<parameter> so that it's possible to update each component
   of a nested object.

Returns self

transform (X)

   Project the data by using matrix product with the random matrix

Parameters X : numpy array or scipy.sparse of shape [n_samples, n_features]

   The input data to project into a smaller dimensional space.

Returns X_new : numpy array or scipy sparse of shape [n_samples, n_components]

   Projected array.

30.31.2 sklearn.random_projection.SparseRandomProjection

class sklearn.random_projection.SparseRandomProjection (n_components='auto',
   density='auto', eps=0.1,
   dense_output=False, random_state=None)

Reduce dimensionality through sparse random projection

Sparse random matrix is an alternative to dense random projection matrix that guarantees similar embedding
quality while being much more memory efficient and allowing faster computation of the projected data.

If we note $s = 1 / \text{density}$ the components of the random matrix are drawn from:

- $-\sqrt{s} / \sqrt{n\_components}$ with probability $1 / 2s$
- $0$ with probability $1 - 1 / s$
- $+\sqrt{s} / \sqrt{n\_components}$ with probability $1 / 2s$

Read more in the User Guide.

Parameters n_components : int or ‘auto’, optional (default = ‘auto’)

Dimensionality of the target projection space.

n_components can be automatically adjusted according to the number of samples in the dataset and the bound given by the Johnson-Lindenstrauss lemma. In that case the quality of the embedding is controlled by the \( \text{eps} \) parameter.

It should be noted that Johnson-Lindenstrauss lemma can yield very conservative estimated of the required number of components as it makes no assumption on the structure of the dataset.

**density** : float in range \([0, 1]\), optional (default=’auto’)

Ratio of non-zero component in the random projection matrix.

If density = ‘auto’, the value is set to the minimum density as recommended by Ping Li et al.: \( 1 / \sqrt{n\text{features}} \).

Use density = 1 / 3.0 if you want to reproduce the results from Achlioptas, 2001.

**eps** : strictly positive float, optional, (default=0.1)

Parameter to control the quality of the embedding according to the Johnson-Lindenstrauss lemma when n_components is set to ‘auto’.

Smaller values lead to better embedding and higher number of dimensions (n_components) in the target projection space.

**dense_output** : boolean, optional (default=False)

If True, ensure that the output of the random projection is a dense numpy array even if the input and random projection matrix are both sparse. In practice, if the number of components is small the number of zero components in the projected data will be very small and it will be more CPU and memory efficient to use a dense representation.

If False, the projected data uses a sparse representation if the input is sparse.

**random_state** : int, RandomState instance or None, optional (default=None)

Control the pseudo random number generator used to generate the matrix at fit time. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by \textit{np.random}.

**Attributes**

<table>
<thead>
<tr>
<th>n_components</th>
<th>(int) Concrete number of components computed when n_components=&quot;auto&quot;.</th>
</tr>
</thead>
<tbody>
<tr>
<td>components_</td>
<td>(CSR matrix with shape [n_components, n_features]) Random matrix used for the projection.</td>
</tr>
<tr>
<td>density_</td>
<td>(float in range 0.0 - 1.0) Concrete density computed from when density = “auto”.</td>
</tr>
</tbody>
</table>

**See also:**

\textit{GaussianRandomProjection}  

**References**

[R187188],[R188188]
Methods

<table>
<thead>
<tr>
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</tr>
<tr>
<td><code>fit_transform(X[, y])</code></td>
<td>Fit to data, then transform it.</td>
</tr>
<tr>
<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Project the data by using matrix product with the random matrix</td>
</tr>
</tbody>
</table>

```
__init__(n_components='auto', density='auto', eps=0.1, dense_output=False, random_state=None)
```

```
fit (X, y=None)
Generate a sparse random projection matrix

Parameters X : numpy array or scipy.sparse of shape [n_samples, n_features]

Training set: only the shape is used to find optimal random matrix dimensions based on
the theory referenced in the afore mentioned papers.

y : is not used: placeholder to allow for usage in a Pipeline.

Returns self
```

```
fit_transform (X, y=None, **fit_params)
Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

Parameters X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

Returns X_new : numpy array of shape [n_samples, n_features_new]

Transformed array.
```

```
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.
```

```
set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self
```

```
transform (X)
Project the data by using matrix product with the random matrix
```

**Parameters** X : numpy array or scipy.sparse of shape [n_samples, n_features]

The input data to project into a smaller dimensional space.

**Returns** X_new : numpy array or scipy sparse of shape [n_samples, n_components]

Projected array.

**Examples using** sklearn.random_projection.SparseRandomProjection

- The Johnson-Lindenstrauss bound for embedding with random projections
- Manifold learning on handwritten digits: Locally Linear Embedding, Isomap...

```python
random_projection.
johnson_lindenstrauss_min_dim(...)
```

### 30.31.3 sklearn.random_projection.johnson_lindenstrauss_min_dim

**sklearn.random_projection.johnson_lindenstrauss_min_dim** (n_samples, eps=0.1)

Find a ‘safe’ number of components to randomly project to

The distortion introduced by a random projection \( p \) only changes the distance between two points by a factor \((1 + \varepsilon)\) in an euclidean space with good probability. The projection \( p \) is an eps-embedding as defined by:

\[
(1 - \varepsilon) \|u - v\|^2 < \|p(u) - p(v)\|^2 < (1 + \varepsilon) \|u - v\|^2
\]

Where \( u \) and \( v \) are any rows taken from a dataset of shape \([n\_samples, n\_features]\), \( \varepsilon \) is in \([0, 1]\) and \( p \) is a projection by a random Gaussian \( \mathcal{N}(0, 1) \) matrix with shape \([n\_components, n\_features]\) (or a sparse Achlioptas matrix).

The minimum number of components to guarantee the eps-embedding is given by:

\[
n\_components \geq 4 \log(n\_samples) / (\varepsilon^2 / 2 - \varepsilon^3 / 3)
\]

Note that the number of dimensions is independent of the original number of features but instead depends on the size of the dataset: the larger the dataset, the higher is the minimal dimensionality of an eps-embedding.

Read more in the **User Guide**.

**Parameters**

- **n_samples** : int or numpy array of int greater than 0,
  
  Number of samples. If an array is given, it will compute a safe number of components array-wise.

- **eps** : float or numpy array of float in \([0, 1]\), optional (default=0.1)
  
  Maximum distortion rate as defined by the Johnson-Lindenstrauss lemma. If an array is given, it will compute a safe number of components array-wise.

**Returns**

- **n_components** : int or numpy array of int,
  
  The minimal number of components to guarantee with good probability an eps-embedding with n_samples.

**References**

[R191192],[R192192]
Examples

```python
>>> johnson_lindenstrauss_min_dim(1e6, eps=0.5)
663
```

```python
>>> johnson_lindenstrauss_min_dim(1e6, eps=[0.5, 0.1, 0.01])
array([ 663, 11841, 1112658])
```

```python
>>> johnson_lindenstrauss_min_dim([1e4, 1e5, 1e6], eps=0.1)
array([ 7894, 9868, 11841])
```

Examples using `sklearn.random_projection.johnson_lindenstrauss_min_dim`

- The Johnson-Lindenstrauss bound for embedding with random projections

### 30.32 sklearn.semi_supervised Semi-Supervised Learning

The `sklearn.semi_supervised` module implements semi-supervised learning algorithms. These algorithms utilized small amounts of labeled data and large amounts of unlabeled data for classification tasks. This module includes Label Propagation.

**User guide:** See the Semi-Supervised section for further details.

### 30.32.1 sklearn.semi_supervised.LabelPropagation

**class** `sklearn.semi_supervised.LabelPropagation(kernel='rbf', gamma=20, n_neighbors=7, alpha=None, max_iter=1000, tol=0.001, n_jobs=1)`

Label Propagation classifier

Read more in the *User Guide*.

**Parameters**

- **kernel** : {'knn', 'rbf', callable}  
  String identifier for kernel function to use or the kernel function itself. Only ‘rbf’ and ‘knn’ strings are valid inputs. The function passed should take two inputs, each of shape [n_samples, n_features], and return a [n_samples, n_samples] shaped weight matrix.

- **gamma** : float  
  Parameter for rbf kernel

- **n_neighbors** : integer > 0  
  Parameter for knn kernel

- **alpha** : float  
  Clamping factor.
Deprecation since version 0.19: This parameter will be removed in 0.21. ‘alpha’ is fixed to zero in ‘LabelPropagation’.

**max_iter**: integer

Change maximum number of iterations allowed

**tol**: float

Convergence tolerance: threshold to consider the system at steady state

**n_jobs**: int, optional (default = 1)

The number of parallel jobs to run. If -1, then the number of jobs is set to the number of CPU cores.

**Attributes**

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>X_</td>
<td>(array, shape = [n_samples, n_features]) Input array.</td>
</tr>
<tr>
<td>classes_</td>
<td>(array, shape = [n_classes]) The distinct labels used in classifying instances.</td>
</tr>
<tr>
<td>label_distributions_</td>
<td>(array, shape = [n_samples, n_classes]) Categorical distribution for each item.</td>
</tr>
<tr>
<td>transduction_</td>
<td>(array, shape = [n_samples]) Label assigned to each item via the transduction.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Number of iterations run.</td>
</tr>
</tbody>
</table>

**See also:**

*LabelSpreading* Alternate label propagation strategy more robust to noise

**References**


**Examples**

```python
>>> from sklearn import datasets
>>> from sklearn.semi_supervised import LabelPropagation
>>> label_prop_model = LabelPropagation()
>>> iris = datasets.load_iris()
>>> rng = np.random.RandomState(42)
>>> random_unlabeled_points = rng.rand(len(iris.target)) < 0.3
>>> labels = np.copy(iris.target)
>>> labels[random_unlabeled_points] = -1
>>> label_prop_model.fit(iris.data, labels)
... LabelPropagation(...)
```

**Methods**
fit(X, y)
get_params([deep])
predict(X)
predict_proba(X)
score(X, y[, sample_weight])
set_params(**params)

__init__(kernel='rbf', gamma=20, n_neighbors=7, alpha=None, max_iter=1000, tol=0.001, n_jobs=1)

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X)
Performs inductive inference across the model.

Parameters X : array_like, shape = [n_samples, n_features]
Returns y : array_like, shape = [n_samples]
Predictions for input data

predict_proba (X)
Predict probability for each possible outcome.

Parameters X : array_like, shape = [n_samples, n_features]

Returns probabilities : array, shape = [n_samples, n_classes]
Normalized probability distributions across class labels

score (X, y, sample_weight=None)
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

Parameters X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for X.

sample_weight : array-like, shape = [n_samples], optional
Sample weights.

Returns score : float
Mean accuracy of self.predict(X) wrt. y.
set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form `<component>__<parameter>` so that it’s possible to update each component
of a nested object.

Returns: self

30.32.2 sklearn.semi_supervised.LabelSpreading
class sklearn.semi_supervised.LabelSpreading(kernel='rbf', gamma=20, n_neighbors=7, alpha=0.2, max_iter=30, tol=0.001, n_jobs=1)
LabelSpreading model for semi-supervised learning
This model is similar to the basic Label Propagation algorithm, but uses affinity matrix based on the normalized
graph Laplacian and soft clamping across the labels.
Read more in the User Guide.

Parameters:

- **kernel**: {'knn', 'rbf', callable}
  String identifier for kernel function to use or the kernel function itself. Only ‘rbf’ and
  ‘knn’ strings are valid inputs. The function passed should take two inputs, each of shape
  [n_samples, n_features], and return a [n_samples, n_samples] shaped weight matrix

- **gamma**: float
  parameter for rbf kernel

- **n_neighbors**: integer > 0
  parameter for knn kernel

- **alpha**: float
  Clamping factor. A value in [0, 1] that specifies the relative amount that an instance
  should adopt the information from its neighbors as opposed to its initial label. alpha=0
  means keeping the initial label information; alpha=1 means replacing all initial infor-
  mation.

- **max_iter**: integer
  maximum number of iterations allowed

- **tol**: float
  Convergence tolerance: threshold to consider the system at steady state

- **n_jobs**: int, optional (default = 1)
  The number of parallel jobs to run. If -1, then the number of jobs is set to the number
  of CPU cores.

Attributes:

<table>
<thead>
<tr>
<th>X_</th>
<th>(array, shape = [n_samples, n_features]) Input array.</th>
</tr>
</thead>
<tbody>
<tr>
<td>classes</td>
<td>(array, shape = [n_classes]) The distinct labels used in classifying instances.</td>
</tr>
<tr>
<td>label_distributions_</td>
<td>(array, shape = [n_samples, n_classes]) Categorical distribution for each item.</td>
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<td>(array, shape = [n_samples]) Label assigned to each item via the transduction.</td>
</tr>
<tr>
<td>n_iter_</td>
<td>(int) Number of iterations run.</td>
</tr>
</tbody>
</table>
See also:

**LabelPropagation** Unregularized graph based semi-supervised learning

References


Examples

```python
>>> from sklearn import datasets
>>> from sklearn.semi_supervised import LabelSpreading
>>> label_prop_model = LabelSpreading()
>>> iris = datasets.load_iris()
>>> rng = np.random.RandomState(42)
>>> random_unlabeled_points = rng.rand(len(iris.target)) < 0.3
>>> labels = np.copy(iris.target)
>>> labels[random_unlabeled_points] = -1
>>> label_prop_model.fit(iris.data, labels)
... LabelSpreading(...)
```

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
</table>
| `fit(X, y)` | Fit a semi-supervised label propagation model based on the graph.
| `get_params([deep])` | Get parameters for this estimator.
| `predict(X)` | Performs inductive inference across the model.
| `predict_proba(X)` | Predict probability for each possible outcome.
| `score(X, y[, sample_weight])` | Returns the mean accuracy on the given test data and labels.
| `set_params(**params)` | Set the parameters of this estimator.

__init__ (kernel='rbf', gamma=20, n_neighbors=7, alpha=0.2, max_iter=30, tol=0.001, n_jobs=1)

**fit** (X, y)

Fit a semi-supervised label propagation model based on the graph.

All the input data is provided matrix X (labeled and unlabeled) and corresponding label matrix y with a dedicated marker value for unlabeled samples.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  A [n_samples by n_features] size matrix will be created from this.

- **y**: array-like, shape = [n_samples]
  
  A [n_samples by n_samples] size matrix will be created from this.

**Returns**

- **self**: returns an instance of self.

**get_params** (deep=True)

Get parameters for this estimator.
Parameters  

**deep**: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**  

**params**: mapping of string to any

Parameter names mapped to their values.

**predict** *(X)*

Performs inductive inference across the model.

**Parameters**  

*X*: array_like, shape = [n_samples, n_features]

**Returns**  

*y*: array_like, shape = [n_samples]

Predictions for input data

**predict_proba** *(X)*

Predict probability for each possible outcome.

Compute the probability estimates for each single sample in X and each possible outcome seen during training (categorical distribution).

**Parameters**  

*X*: array_like, shape = [n_samples, n_features]

**Returns**  

*probabilities*: array, shape = [n_samples, n_classes]

Normalized probability distributions across class labels

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**  

*X*: array-like, shape = (n_samples, n_features)

Test samples.

*y*: array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

*sample_weight*: array-like, shape = [n_samples], optional

Sample weights.

**Returns**  

*score*: float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  

self

**Examples using sklearn.semi_supervised.LabelSpreading**

- Decision boundary of label propagation versus SVM on the Iris dataset
- Label Propagation learning a complex structure
30.33 sklearn.svm: Support Vector Machines

The sklearn.svm module includes Support Vector Machine algorithms.

User guide: See the Support Vector Machines section for further details.

30.33.1 Estimators

<table>
<thead>
<tr>
<th>sklearn.svm.LinearSVC([penalty, loss, dual, tol, C, ...])</th>
<th>Linear Support Vector Classification.</th>
</tr>
</thead>
<tbody>
<tr>
<td>sklearn.svm.LinearSVR([epsilon, tol, C, loss, ...])</td>
<td>Linear Support Vector Regression.</td>
</tr>
<tr>
<td>sklearn.svm.NuSVC([nu, kernel, degree, gamma, ...])</td>
<td>Nu-Support Vector Classification.</td>
</tr>
<tr>
<td>sklearn.svm.NuSVR([nu, C, kernel, degree, gamma, ...])</td>
<td>Nu Support Vector Regression.</td>
</tr>
<tr>
<td>sklearn.svm.OneClassSVM([kernel, degree, gamma, ...])</td>
<td>Unsupervised Outlier Detection.</td>
</tr>
<tr>
<td>sklearn.svm.SVC([C, kernel, degree, gamma, coef0, ...])</td>
<td>C-Support Vector Classification.</td>
</tr>
<tr>
<td>sklearn.svm.SVR([kernel, degree, gamma, coef0, ...])</td>
<td>Epsilon-Support Vector Regression.</td>
</tr>
</tbody>
</table>

sklearn.svm.LinearSVC

class sklearn.svm.LinearSVC (penalty='l2', loss='squared_hinge', dual=True, tol=0.0001, C=1.0, multi_class='ovr', fit_intercept=True, intercept_scaling=1, class_weight=None, verbose=0, random_state=None, max_iter=1000)

Linear Support Vector Classification.

Similar to SVC with parameter kernel='linear', but implemented in terms of liblinear rather than libsvm, so it has more flexibility in the choice of penalties and loss functions and should scale better to large numbers of samples.

This class supports both dense and sparse input and the multiclass support is handled according to a one-vs-the-rest scheme.

Read more in the User Guide.

Parameters

penalty : string, ‘l1’ or ‘l2’ (default='l2')

Specifies the norm used in the penalization. The ‘l2’ penalty is the standard used in SVC. The ‘l1’ leads to coef_ vectors that are sparse.

loss : string, ‘hinge’ or ‘squared_hinge’ (default='squared_hinge')

Specifies the loss function. ‘hinge’ is the standard SVM loss (used e.g. by the SVC class) while ‘squared_hinge’ is the square of the hinge loss.

dual : bool, (default=True)

Select the algorithm to either solve the dual or primal optimization problem. Prefer dual=False when n_samples > n_features.

tol : float, optional (default=1e-4)

Tolerance for stopping criteria.

C : float, optional (default=1.0)

Penalty parameter C of the error term.
**multi_class** : string, ‘ovr’ or ‘crammer_singer’ (default=’ovr’)

Determines the multi-class strategy if y contains more than two classes. "ovr" trains n_classes one-vs-rest classifiers, while "crammer_singer" optimizes a joint objective over all classes. While `crammer_singer` is interesting from a theoretical perspective as it is consistent, it is seldom used in practice as it rarely leads to better accuracy and is more expensive to compute. If "crammer_singer" is chosen, the options loss, penalty and dual will be ignored.

**fit_intercept** : boolean, optional (default=True)

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (i.e. data is expected to be already centered).

**intercept_scaling** : float, optional (default=1)

When `self.fit_intercept` is True, instance vector x becomes [x, self.intercept_scaling], i.e. a “synthetic” feature with constant value equals to intercept_scaling is appended to the instance vector. The intercept becomes intercept_scaling * synthetic feature weight. Note! the synthetic feature weight is subject to l1/l2 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept_scaling has to be increased.

**class_weight** : {dict, ‘balanced’}, optional

Set the parameter C of class i to `class_weight[i]*C` for SVC. If not given, all classes are supposed to have weight one. The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as `n_samples / (n_classes * np.bincount(y))`

**verbose** : int, (default=0)

Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in liblinear that, if enabled, may not work properly in a multithreaded context.

**random_state** : int, RandomState instance or None, optional (default=None)

The seed of the pseudo random number generator to use when shuffling the data for the dual coordinate descent (if `dual=True`). When `dual=False` the underlying implementation of LinearSVC is not random and `random_state` has no effect on the results. If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**max_iter** : int, (default=1000)

The maximum number of iterations to be run.

### Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>coef</strong></td>
<td>(array, shape = [n_features] if n_classes == 2 else [n_classes, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. <code>coef_</code> is a readonly property derived from <code>raw_coef_</code> that follows the internal memory layout of liblinear.</td>
</tr>
<tr>
<td><strong>intercept</strong></td>
<td>(array, shape = [1] if n_classes == 2 else [n_classes]) Constants in decision function.</td>
</tr>
</tbody>
</table>
See also:

**SVC** Implementation of Support Vector Machine classifier using libsvm: the kernel can be non-linear but its SMO algorithm does not scale to large number of samples as LinearSVC does. Furthermore SVC multi-class mode is implemented using one vs one scheme while LinearSVC uses one vs the rest. It is possible to implement one vs the rest with SVC by using the `sklearn.multiclass.OneVsRestClassifier` wrapper. Finally SVC can fit dense data without memory copy if the input is C-contiguous. Sparse data will still incur memory copy though.

**sklearn.linear_model.SGDClassifier** SGDClassifier can optimize the same cost function as LinearSVC by adjusting the penalty and loss parameters. In addition it requires less memory, allows incremental (online) learning, and implements various loss functions and regularization regimes.

**Notes**

The underlying C implementation uses a random number generator to select features when fitting the model. It is thus not uncommon to have slightly different results for the same input data. If that happens, try with a smaller `tol` parameter.

The underlying implementation, liblinear, uses a sparse internal representation for the data that will incur a memory copy.

Predict output may not match that of standalone liblinear in certain cases. See differences from liblinear in the narrative documentation.

**References**

LIBLINEAR: A Library for Large Linear Classification

**Examples**

```python
>>> from sklearn.svm import LinearSVC
>>> from sklearn.datasets import make_classification
>>> X, y = make_classification(n_features=4, random_state=0)
>>> clf = LinearSVC(random_state=0)
>>> clf.fit(X, y)
LinearSVC(C=1.0, class_weight=None, dual=True, fit_intercept=True,
         intercept_scaling=1, loss='squared_hinge', max_iter=1000,
         multi_class='ovr', penalty='l2', random_state=0, tol=0.0001,
         verbose=0)
>>> print(clf.coef_)
[[ 0.08551385 0.39414796 0.49847831 0.37513797]]
>>> print(clf.intercept_)
[ 0.28418066]
>>> print(clf.predict([[0, 0, 0, 0]]))
[1]
```

**Methods**

`decision_function(X)` Predict confidence scores for samples.
Table 30.289 – continued from previous page

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>densify()</td>
<td>Convert coefficient matrix to dense array format.</td>
</tr>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit the model according to the given training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict class labels for samples in X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>sparsify()</td>
<td>Convert coefficient matrix to sparse format.</td>
</tr>
</tbody>
</table>

`__init__`(penalty='l2', loss='squared_hinge', dual=True, tol=0.0001, C=1.0, multi_class='ovr', fit_intercept=True, intercept_scaling=1, class_weight=None, verbose=0, random_state=None, max_iter=1000)

**decision_function** *(X)*

Predict confidence scores for samples.

Parameters:
- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Samples.

Returns:
- array, shape=(n_samples,) if n_classes == 2 else (n_samples, n_classes)
  - Confidence scores per (sample, class) combination. In the binary case, confidence score for self.classes_[1] where >0 means this class would be predicted.

**densify()**

Convert coefficient matrix to dense array format.

Converts the `coef_` member (back) to a `numpy.ndarray`. This is the default format of `coef_` and is required for fitting, so calling this method is only required on models that have previously been sparsified; otherwise, it is a no-op.

Returns:
- **self**: estimator

**fit**(X, y, sample_weight=None)

Fit the model according to the given training data.

Parameters:
- **X**: {array-like, sparse matrix}, shape = (n_samples, n_features)
  - Training vector, where n_samples in the number of samples and n_features is the number of features.
- **y**: array-like, shape = [n_samples]
  - Target vector relative to X
- **sample_weight**: array-like, shape = [n_samples], optional
  - Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

Returns:
- **self**: object
  - Returns self.

**get_params**(deep=True)

Get parameters for this estimator.

Parameters:
- **deep**: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**predict** *(X)*

Predict class labels for samples in X.

**Parameters**

X : {array-like, sparse matrix}, shape = [n_samples, n_features]

Samples.

**Returns**

C : array, shape = [n_samples]

Predicted class label per sample.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

X : array-like, shape = (n_samples, n_features)

Test samples.

y : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

sample_weight : array-like, shape = [n_samples], optional

Sample weights.

**Returns**

score : float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

self

**sparsify** ()

Convert coefficient matrix to sparse format.

Converts the coef_ member to a scipy.sparse matrix, which for L1-regularized models can be much more memory- and storage-efficient than the usual numpy.ndarray representation.

The intercept_ member is not converted.

**Returns**

self : estimator

**Notes**

For non-sparse models, i.e. when there are not many zeros in coef_, this may actually increase memory usage, so use this method with care. A rule of thumb is that the number of zero elements, which can be computed with `(coef_ == 0).sum()`, must be more than 50% for this to provide significant benefits.
After calling this method, further fitting with the partial_fit method (if any) will not work until you call densify.

Examples using sklearn.svm.LinearSVC

- Selecting dimensionality reduction with Pipeline and GridSearchCV
- Explicit feature map approximation for RBF kernels
- Comparison of Calibration of Classifiers
- Probability Calibration curves
- Precision-Recall
- Plot different SVM classifiers in the iris dataset
- Scaling the regularization parameter for SVCs
- Classification of text documents using sparse features

sklearn.svm.LinearSVR

class sklearn.svm.LinearSVR(epsilon=0.0, tol=0.0001, C=1.0, loss='epsilon_insensitive',
fit_intercept=True, intercept_scaling=1.0, dual=True, verbose=0,
random_state=None, max_iter=1000)

Linear Support Vector Regression.

Similar to SVR with parameter kernel='linear', but implemented in terms of liblinear rather than libsvm, so it has more flexibility in the choice of penalties and loss functions and should scale better to large numbers of samples.

This class supports both dense and sparse input.

Read more in the User Guide.

Parameters

- **C**: float, optional (default=1.0)
  Penalty parameter C of the error term. The penalty is a squared l2 penalty. The bigger this parameter, the less regularization is used.

- **loss**: string, ‘epsilon_insensitive’ or ‘squared_epsilon_insensitive’ (default=’epsilon_insensitive’)
  Specifies the loss function. ‘l1’ is the epsilon-insensitive loss (standard SVR) while ‘l2’ is the squared epsilon-insensitive loss.

- **epsilon**: float, optional (default=0.1)
  Epsilon parameter in the epsilon-insensitive loss function. Note that the value of this parameter depends on the scale of the target variable y. If unsure, set epsilon=0.

- **dual**: bool, (default=True)
  Select the algorithm to either solve the dual or primal optimization problem. Prefer dual=False when n_samples > n_features.

- **tol**: float, optional (default=1e-4)
  Tolerance for stopping criteria.

- **fit_intercept**: boolean, optional (default=True)
Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (i.e. data is expected to be already centered).

**intercept_scaling**: float, optional (default=1)

When self.fit_intercept is True, instance vector x becomes [x, self.intercept_scaling], i.e. a “synthetic” feature with constant value equals to intercept_scaling is appended to the instance vector. The intercept becomes intercept_scaling * synthetic feature weight

Note! the synthetic feature weight is subject to l1/l2 regularization as all other features. To lessen the effect of regularization on synthetic feature weight (and therefore on the intercept) intercept_scaling has to be increased.

**verbose**: int, (default=0)

Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in liblinear that, if enabled, may not work properly in a multithreaded context.

**random_state**: int, RandomState instance or None, optional (default=None)

The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**max_iter**: int, (default=1000)

The maximum number of iterations to be run.

**Attributes**

- **coef_** (array, shape = [n_features] if n_classes == 2 else [n_classes, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is a readonly property derived from raw_coef_ that follows the internal memory layout of liblinear.

- **intercept_** (array, shape = [1] if n_classes == 2 else [n_classes]) Constants in decision function.

**See also:**

**LinearSVC** Implementation of Support Vector Machine classifier using the same library as this class (liblinear).

**SVR** Implementation of Support Vector Machine regression using libsvm: the kernel can be non-linear but its SMO algorithm does not scale to large number of samples as LinearSVC does.

**sklearn.linear_model.SGDRegressor** SGDRegressor can optimize the same cost function as LinearSVR by adjusting the penalty and loss parameters. In addition it requires less memory, allows incremental (online) learning, and implements various loss functions and regularization regimes.

**Examples**

```python
>>> from sklearn.svm import LinearSVR
>>> from sklearn.datasets import make_regression
>>> X, y = make_regression(n_features=4, random_state=0)
>>> regr = LinearSVR(random_state=0)
>>> regr.fit(X, y)
```

---

30.33. **sklearn.svm**: Support Vector Machines
LinearSVR(C=1.0, dual=True, epsilon=0.0, fit_intercept=True,
    intercept_scaling=1.0, loss='epsilon_insensitive', max_iter=1000,
    random_state=0, tol=0.0001, verbose=0)

>>> print(regr.coef_)
[ 16.35750999  26.91499923  42.30652207  60.47843124]

>>> print(regr.intercept_)
[ -4.29756543]

>>> print(regr.predict([[0, 0, 0, 0]]))
[ -4.29756543]

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit the model according to the given training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict using the linear model</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the coefficient of determination $R^2$ of the prediction.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(epsilon=0.0, tol=0.0001, C=1.0, loss='epsilon_insensitive', fit_intercept=True, intercept_scaling=1.0, dual=True, verbose=0, random_state=None, max_iter=1000)

fit(X, y, sample_weight=None)

Fit the model according to the given training data.

Parameters
X : {array-like, sparse matrix}, shape = [n_samples, n_features]
   Training vector, where n_samples is the number of samples and n_features is the number of features.

y : array-like, shape = [n_samples]
   Target vector relative to X

sample_weight : array-like, shape = [n_samples], optional
   Array of weights that are assigned to individual samples. If not provided, then each sample is given unit weight.

Returns
self : object
   Returns self.

get_params(deep=True)

Get parameters for this estimator.

Parameters
depth : boolean, optional
   If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns
params : mapping of string to any
   Parameter names mapped to their values.

predict(X)

Predict using the linear model

Parameters
X : {array-like, sparse matrix}, shape = (n_samples, n_features)
Samples.

**Returns**

- `C` : array, shape = (n_samples,)
  Returns predicted values.

**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares ($(y_{true} - y_{pred}) ** 2).sum()$ and $v$ is the total sum of squares ($(y_{true} - y_{true}.mean()) ** 2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

- `X` : array-like, shape = (n_samples, n_features)
  Test samples.
- `y` : array-like, shape = (n_samples) or (n_samples, n_outputs)
  True values for $X$.
- `sample_weight` : array-like, shape = [n_samples], optional
  Sample weights.

**Returns**

- `score` : float
  $R^2$ of self.predict($X$) wrt. $y$.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- `self`

**sklearn.svm.NuSVC**

**class** `sklearn.svm.NuSVC` *(nu=0.5, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', random_state=None)*

Nu-Support Vector Classification.

Similar to SVC but uses a parameter to control the number of support vectors.

The implementation is based on libsvm.

Read more in the [User Guide](#).

**Parameters**

- `nu` : float, optional (default=0.5)
  An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1].
- `kernel` : string, optional (default='rbf')
  Specifies the kernel type to be used in the algorithm. It must be one of ‘linear’, ‘poly’, ‘rbf’, ‘sigmoid’, ‘precomputed’ or a callable. If none is given, ‘rbf’ will be used. If a callable is given it is used to precompute the kernel matrix.
- `degree` : int, optional (default=3)

30.33. **sklearn.svm**: Support Vector Machines 1987
Degree of the polynomial kernel function (`poly`). Ignored by all other kernels.

**gamma** : float, optional (default=`'auto'`)

Kernel coefficient for `rbf`, `poly` and `sigmoid`. If gamma is `auto` then $1/n\_features$ will be used instead.

**coef0** : float, optional (default=0.0)

Independent term in kernel function. It is only significant in `poly` and `sigmoid`.

**probability** : boolean, optional (default=False)

Whether to enable probability estimates. This must be enabled prior to calling `fit`, and will slow down that method.

**shrinking** : boolean, optional (default=True)

Whether to use the shrinking heuristic.

**tol** : float, optional (default=1e-3)

Tolerance for stopping criterion.

**cache_size** : float, optional

Specify the size of the kernel cache (in MB).

**class_weight** : {dict, ‘balanced’}, optional

Set the parameter $C$ of class $i$ to $\text{class_weight}[i]*C$ for SVC. If not given, all classes are supposed to have weight one. The “balanced” mode uses the values of $y$ to automatically adjust weights inversely proportional to class frequencies as $n\_\text{samples} / (n\_\text{classes} * \text{np.bincount}(y))$.

**verbose** : bool, default: False

Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsvm that, if enabled, may not work properly in a multithreaded context.

**max_iter** : int, optional (default=-1)

Hard limit on iterations within solver, or -1 for no limit.

**decision_function_shape** : ‘ovo’, ‘ovr’, default=’ovr’

Whether to return a one-vs-rest (‘ovo’) decision function of shape (n_samples, n_classes) as all other classifiers, or the original one-vs-one (‘ovr’) decision function of libsvm which has shape (n_samples, n_classes * (n_classes - 1) / 2).

Changed in version 0.19: `decision_function_shape` is ‘ovr’ by default.

New in version 0.17: `decision_function_shape='ovr'` is recommended.

Changed in version 0.17: Deprecated `decision_function_shape='ovo'` and None.

**random_state** : int, RandomState instance or None, optional (default=None)

The seed of the pseudo random number generator used when shuffling the data for probability estimates. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`. 
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>support_</td>
<td>(array-like, shape = [n_SV]) Indices of support vectors.</td>
</tr>
<tr>
<td>support_vectors_</td>
<td>(array-like, shape = [n_SV, n_features]) Support vectors.</td>
</tr>
<tr>
<td>n_support_</td>
<td>(array-like, dtype=int32, shape = [n_class]) Number of support vectors for each class.</td>
</tr>
<tr>
<td>dual_coef_</td>
<td>(array, shape = [n_class-1, n_SV]) Coefficients of the support vector in the decision function. For multiclass, coefficient for all 1-vs-1 classifiers. The layout of the coefficients in the multiclass case is somewhat non-trivial. See the section about multi-class classification in the SVM section of the User Guide for details.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape = [n_class-1, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is readonly property derived from dual_coef_ and support_vectors_.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [n_class * (n_class-1) / 2]) Constants in decision function.</td>
</tr>
</tbody>
</table>

See also:

SVC  Support Vector Machine for classification using libsvm.

LinearSVC  Scalable linear Support Vector Machine for classification using liblinear.

Examples

```python
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [1, 1], [2, 1]])
>>> y = np.array([1, 1, 2, 2])
>>> from sklearn.svm import NuSVC
>>> clf = NuSVC()
>>> clf.fit(X, y)
NuSVC(cache_size=200, class_weight=None, coef0=0.0,
     decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
     max_iter=-1, nu=0.5, probability=False, random_state=None,
     shrinking=True, tol=0.001, verbose=False)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>decision_function(X)</td>
<td>Distance of the samples X to the separating hyperplane.</td>
</tr>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit the SVM model according to the given training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Perform classification on samples in X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>
__init__(nu=0.5, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', random_state=None)

decision_function(X)
   Distance of the samples X to the separating hyperplane.
   Parameters X : array-like, shape (n_samples, n_features)
   Returns X : array-like, shape (n_samples, n_classes * (n_classes-1) / 2)
      Returns the decision function of the sample for each class in the model. If decision_function_shape='ovr', the shape is (n_samples, n_classes)

fit(X, y, sample_weight=None)
   Fit the SVM model according to the given training data.
   Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
      Training vectors, where n_samples is the number of samples and n_features is the number of features. For kernel="precomputed", the expected shape of X is (n_samples, n_samples).
   y : array-like, shape (n_samples,)
      Target values (class labels in classification, real numbers in regression)
   sample_weight : array-like, shape (n_samples,)
      Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.
   Returns self : object
      Returns self.

Notes

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr_matrix, X and/or y may be copied.
If X is a dense array, then the other methods will not support sparse matrices as input.

get_params(deep=True)
   Get parameters for this estimator.
   Parameters deep : boolean, optional
      If True, will return the parameters for this estimator and contained subobjects that are estimators.
   Returns params : mapping of string to any
      Parameter names mapped to their values.

predict(X)
   Perform classification on samples in X.
   For an one-class model, +1 or -1 is returned.
   Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
      For kernel="precomputed", the expected shape of X is [n_samples_test, n_samples_train]
Returns \texttt{y_pred} : array, shape (n_samples,)
Class labels for samples in X.

\texttt{predict_log_proba}
Compute log probabilities of possible outcomes for samples in X.
The model need to have probability information computed at training time: fit with attribute \texttt{probability}
set to True.

\textbf{Parameters} \texttt{X} : array-like, shape (n_samples, n_features)
For kernel="precomputed", the expected shape of \texttt{X} is [n_samples_test, n_samples_train]

\textbf{Returns} \texttt{T} : array-like, shape (n_samples, n_classes)
Returns the log-probabilities of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute \texttt{classes}.

\textbf{Notes}
The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

\texttt{predict_proba}
Compute probabilities of possible outcomes for samples in X.
The model need to have probability information computed at training time: fit with attribute \texttt{probability}
set to True.

\textbf{Parameters} \texttt{X} : array-like, shape (n_samples, n_features)
For kernel="precomputed", the expected shape of \texttt{X} is [n_samples_test, n_samples_train]

\textbf{Returns} \texttt{T} : array-like, shape (n_samples, n_classes)
Returns the probability of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute \texttt{classes}.

\textbf{Notes}
The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

\textbf{score} \texttt{(X, y, sample_weight=None)}
Returns the mean accuracy on the given test data and labels.
In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

\textbf{Parameters} \texttt{X} : array-like, shape = (n_samples, n_features)
Test samples.

\texttt{y} : array-like, shape = (n_samples) or (n_samples, n_outputs)
True labels for \texttt{X}.

\textbf{sample_weight} : array-like, shape = [n_samples], optional
Sample weights.

**Returns**  
`score` : float
Mean accuracy of `self.predict(X)` wrt. `y`.

**set_params** (**params**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
`self`

**Examples using sklearn.svm.NuSVC**

- Non-linear SVM

**sklearn.svm.NuSVR**

class sklearn.svm.NuSVR (nu=0.5, C=1.0, kernel=’rbf’, degree=3, gamma=’auto’, coef0=0.0, shrinking=True, tol=0.001, cache_size=200, verbose=False, max_iter=-1)

Nu Support Vector Regression.

Similar to NuSVC, for regression, uses a parameter nu to control the number of support vectors. However, unlike NuSVC, where nu replaces C, here nu replaces the parameter epsilon of epsilon-SVR.

The implementation is based on libsvm.

Read more in the User Guide.

**Parameters**

- `C` : float, optional (default=1.0)
  Penalty parameter C of the error term.

- `nu` : float, optional
  An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1]. By default 0.5 will be taken.

- `kernel` : string, optional (default=’rbf’)
  Specifies the kernel type to be used in the algorithm. It must be one of ‘linear’, ‘poly’, ‘rbf’, ‘sigmoid’, ‘precomputed’ or a callable. If none is given, ‘rbf’ will be used. If a callable is given it is used to precompute the kernel matrix.

- `degree` : int, optional (default=3)
  Degree of the polynomial kernel function (‘poly’). Ignored by all other kernels.

- `gamma` : float, optional (default=’auto’)
  Kernel coefficient for ‘rbf’, ‘poly’ and ‘sigmoid’. If gamma is ‘auto’ then 1/n_features will be used instead.

- `coef0` : float, optional (default=0.0)
  Independent term in kernel function. It is only significant in ‘poly’ and ‘sigmoid’.

- `shrinking` : boolean, optional (default=True)
  Whether to use the shrinking heuristic.
tol : float, optional (default=1e-3)
    Tolerance for stopping criterion.

cache_size : float, optional
    Specify the size of the kernel cache (in MB).

verbose : bool, default: False
    Enable verbose output. Note that this setting takes advantage of a per-process runtime
    setting in libsvm that, if enabled, may not work properly in a multithreaded context.

max_iter : int, optional (default=-1)
    Hard limit on iterations within solver, or -1 for no limit.

Attributes

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<th>description</th>
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<tbody>
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<td>support_</td>
<td>(array-like, shape = [n_SV]) Indices of support vectors.</td>
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<tr>
<td>support_vectors_</td>
<td>(array-like, shape = [nSV, n_features]) Support vectors.</td>
</tr>
<tr>
<td>dual_coef_</td>
<td>(array, shape = [1, n_SV]) Coefficients of the support vector in the decision function.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape = [1, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is readonly property derived from dual_coef_ and support_vectors_.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [1]) Constants in decision function.</td>
</tr>
</tbody>
</table>

See also:

**NuSVC** Support Vector Machine for classification implemented with libsvm with a parameter to control the number of support vectors.

**SVR** epsilon Support Vector Machine for regression implemented with libsvm.

Examples

```python
>>> from sklearn.svm import NuSVR
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> np.random.seed(0)
>>> y = np.random.randn(n_samples)
>>> X = np.random.randn(n_samples, n_features)
>>> clf = NuSVR(C=1.0, nu=0.1)
>>> clf.fit(X, y)
```

Methods
**fit**(X, y[, sample_weight])
Fit the SVM model according to the given training data.

**get_params**(deep)
Get parameters for this estimator.

**predict**(X)
Perform regression on samples in X.

**score***(X, y[, sample_weight])
Returns the coefficient of determination $R^2$ of the prediction.

**set_params**(**params)**
Set the parameters of this estimator.

**__init__**(nu=0.5, C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, tol=0.001, cache_size=200, verbose=False, max_iter=-1)

**fit**(X, y, sample_weight=None)
Fit the SVM model according to the given training data.

**Parameters**
- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  Training vectors, where n_samples is the number of samples and n_features is the number of features. For kernel="precomputed", the expected shape of X is (n_samples, n_samples).
- **y**: array-like, shape (n_samples,)
  Target values (class labels in classification, real numbers in regression)
- **sample_weight**: array-like, shape (n_samples,)
  Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

**Returns**
- **self**: object
  Returns self.

**Notes**
If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr_matrix, X and/or y may be copied.
If X is a dense array, then the other methods will not support sparse matrices as input.

**get_params**(deep=True)
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any
  Parameter names mapped to their values.

**predict**(X)
Perform regression on samples in X.
For an one-class model, +1 (inlier) or -1 (outlier) is returned.

**Parameters**
- **X**: {array-like, sparse matrix}, shape (n_samples, n_features)
  For kernel="precomputed", the expected shape of X is (n_samples_test, n_samples_train).

**Returns**
- **y_pred**: array, shape (n_samples,)
**score** *(X, y, sample_weight=None)*

Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  
  Test samples.

- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  
  True values for X.

- **sample_weight**: array-like, shape = [n_samples], optional
  
  Sample weights.

**Returns**

- **score**: float
  
  R^2 of self.predict(X) wrt. y.

**set_params** *(**params)**

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

**Examples using sklearn.svm.NuSVR**

- **Model Complexity Influence**

**sklearn.svm.OneClassSVM**

---

**class** sklearn.svm.OneClassSVM *(kernel='rbf', degree=3, gamma='auto', coef0=0.0, tol=0.001, nu=0.5, shrinking=True, cache_size=200, verbose=False, max_iter=-1, random_state=None)*

Unsupervised Outlier Detection.

Estimate the support of a high-dimensional distribution.

The implementation is based on libsvm.

Read more in the *User Guide*.

**Parameters**

- **kernel**: string, optional (default='rbf')

  Specifies the kernel type to be used in the algorithm. It must be one of ‘linear’, ‘poly’, ‘rbf’, ‘sigmoid’, ‘precomputed’ or a callable. If none is given, ‘rbf’ will be used. If a callable is given it is used to precompute the kernel matrix.

- **nu**: float, optional

  An upper bound on the fraction of training errors and a lower bound of the fraction of support vectors. Should be in the interval (0, 1]. By default 0.5 will be taken.

- **degree**: int, optional (default=3)
Degree of the polynomial kernel function (‘poly’). Ignored by all other kernels.

**gamma**: float, optional (default=’auto’)

Kernel coefficient for ‘rbf’, ‘poly’ and ‘sigmoid’. If gamma is ‘auto’ then 1/n_features will be used instead.

**coef0**: float, optional (default=0.0)

Independent term in kernel function. It is only significant in ‘poly’ and ‘sigmoid’.

**tol**: float, optional

Tolerance for stopping criterion.

**shrinking**: boolean, optional

Whether to use the shrinking heuristic.

**cache_size**: float, optional

Specify the size of the kernel cache (in MB).

**verbose**: bool, default: False

Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsvm that, if enabled, may not work properly in a multithreaded context.

**max_iter**: int, optional (default=-1)

Hard limit on iterations within solver, or -1 for no limit.

**random_state**: int, RandomState instance or None, optional (default=None)

Ignored.

Deprecated since version 0.20: random_state has been deprecated in 0.20 and will be removed in 0.22.

### Attributes

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<td>(array-like, shape = [nSV, n_features]) Support vectors.</td>
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<td>dual_coef_</td>
<td>(array, shape = [1, n_SV]) Coefficients of the support vectors in the decision function.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape = [1, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is readonly property derived from dual_coef_ and support_vectors_</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [1,]) Constant in the decision function.</td>
</tr>
</tbody>
</table>

### Methods

<table>
<thead>
<tr>
<th>Method</th>
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<tbody>
<tr>
<td>decision_function(X)</td>
<td>Signed distance to the separating hyperplane.</td>
</tr>
<tr>
<td>fit(X, y, sample_weight)</td>
<td>Detects the soft boundary of the set of samples X.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
</tbody>
</table>
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<table>
<thead>
<tr>
<th>Method</th>
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<tbody>
<tr>
<td><strong>predict</strong></td>
<td>Perform classification on samples in X.</td>
</tr>
<tr>
<td><strong>set_params</strong></td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

```python
__init__ (kernel=’rbf’, degree=3, gamma=’auto’, coef0=0.0, tol=0.001, nu=0.5, shrinking=True, cache_size=200, verbose=False, max_iter=-1, random_state=None)
```

**decision_function** (X)
Signed distance to the separating hyperplane.

- **Parameters** X : array-like, shape (n_samples, n_features)
- **Returns** X : array-like, shape (n_samples,)

**fit** (X=None, y=None, sample_weight=None, **params)
Detects the soft boundary of the set of samples X.

- **Parameters** X : array-like, shape (n_samples, n_features)
  - Set of samples, where n_samples is the number of samples and n_features is the number of features.
- sample_weight : array-like, shape (n_samples,)
  - Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.
- **Returns** self : object
  - Returns self.

**Notes**
If X is not a C-ordered contiguous array it is copied.

**get_params** (deep=True)
Get parameters for this estimator.

- **Parameters** deep : boolean, optional
  - If True, will return the parameters for this estimator and contained subobjects that are estimators.
- **Returns** params : mapping of string to any
  - Parameter names mapped to their values.

**predict** (X)
Perform classification on samples in X.

- For an one-class model, +1 or -1 is returned.
- **Parameters** X : array-like, shape (n_samples, n_features)
  - For kernel=”precomputed”, the expected shape of X is [n_samples_test, n_samples_train]
- **Returns** y_pred : array, shape (n_samples,)
  - Class labels for samples in X.
**set_params** (**params**)  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**  
self

**Examples using sklearn.svm.OneClassSVM**

- Outlier detection on a real data set
- Species distribution modeling
- Libsvm GUI
- Outlier detection with several methods.
- One-class SVM with non-linear kernel (RBF)

**sklearn.svm.SVC**

class sklearn.svm.SVC(C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', random_state=None)

C-Support Vector Classification.

The implementation is based on libsvm. The fit time complexity is more than quadratic with the number of samples which makes it hard to scale to dataset with more than a couple of 10000 samples.

The multiclass support is handled according to a one-vs-one scheme.

For details on the precise mathematical formulation of the provided kernel functions and how `gamma`, `coef0` and `degree` affect each other, see the corresponding section in the narrative documentation: **Kernel functions**.

Read more in the User Guide.

**Parameters**

- **C** : float, optional (default=1.0)  
  Penalty parameter C of the error term.

- **kernel** : string, optional (default='rbf')  
  Specifies the kernel type to be used in the algorithm. It must be one of ‘linear’, ‘poly’, ‘rbf’, ‘sigmoid’, ‘precomputed’ or a callable. If none is given, ‘rbf’ will be used. If a callable is given it is used to pre-compute the kernel matrix from data matrices; that matrix should be an array of shape (n_samples, n_samples).

- **degree** : int, optional (default=3)  
  Degree of the polynomial kernel function (‘poly’). Ignored by all other kernels.

- **gamma** : float, optional (default='auto')  
  Kernel coefficient for ‘rbf’, ‘poly’ and ‘sigmoid’. If gamma is ‘auto’ then 1/n_features will be used instead.

- **coef0** : float, optional (default=0.0)  
  Independent term in kernel function. It is only significant in ‘poly’ and ‘sigmoid’.

- **probability** : boolean, optional (default=False)
Whether to enable probability estimates. This must be enabled prior to calling `fit`, and will slow down that method.

**shrinking**: boolean, optional (default=True)
Whether to use the shrinking heuristic.

**tol**: float, optional (default=1e-3)
Tolerance for stopping criterion.

**cache_size**: float, optional
Specify the size of the kernel cache (in MB).

**class_weight**: {dict, ‘balanced’}, optional
Set the parameter C of class i to class_weight[i] * C for SVC. If not given, all classes are supposed to have weight one. The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as n_samples / (n_classes * np.bincount(y))

**verbose**: bool, default: False
Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsvm that, if enabled, may not work properly in a multithreaded context.

**max_iter**: int, optional (default=-1)
Hard limit on iterations within solver, or -1 for no limit.

**decision_function_shape**: ‘ovo’, ‘ovr’, default='ovr'
Whether to return a one-vs-rest (‘ovr’) decision function of shape (n_samples, n_classes) as all other classifiers, or the original one-vs-one (‘ovo’) decision function of libsvm which has shape (n_samples, n_classes * (n_classes - 1) / 2).

Changed in version 0.19: decision_function_shape is ‘ovr’ by default.

New in version 0.17: decision_function_shape=’ovr’ is recommended.

Changed in version 0.17: Deprecated decision_function_shape='ovo' and None.

**random_state**: int, RandomState instance or None, optional (default=None)
The seed of the pseudo random number generator used when shuffling the data for probability estimates. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.
Attributes

<table>
<thead>
<tr>
<th>Attribute</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>support_</td>
<td>(array-like, shape = [n_SV]) Indices of support vectors.</td>
</tr>
<tr>
<td>support_vectors_</td>
<td>(array-like, shape = [n_SV, n_features]) Support vectors.</td>
</tr>
<tr>
<td>n_support</td>
<td>(array-like, dtype=int32, shape = [n_class]) Number of support vectors for each class.</td>
</tr>
<tr>
<td>dual_coef_</td>
<td>(array, shape = [n_class-1, n_SV]) Coefficients of the support vector in the decision function. For multiclass, coefficient for all 1-vs-1 classifiers. The layout of the coefficients in the multiclass case is somewhat non-trivial. See the section about multi-class classification in the SVM section of the User Guide for details.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape = [n_class-1, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is a readonly property derived from dual_coef_ and support_vectors_.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [n_class * (n_class-1) / 2]) Constants in decision function.</td>
</tr>
</tbody>
</table>

See also:

SVR Support Vector Machine for Regression implemented using libsvm.

LinearSVC Scalable Linear Support Vector Machine for classification implemented using liblinear. Check the See also section of LinearSVC for more comparison element.

Examples

```python
>>> import numpy as np
>>> X = np.array([[-1, -1], [-2, -1], [1, 1], [2, 1]])
>>> y = np.array([1, 1, 2, 2])
>>> from sklearn.svm import SVC
>>> clf = SVC()
>>> clf.fit(X, y)
SVC(C=1.0, cache_size=200, class_weight=None, coef0=0.0, 
decision_function_shape='ovr', degree=3, gamma='auto', kernel='rbf',
max_iter=-1, probability=False, random_state=None, shrinking=True,
tol=0.001, verbose=False)
>>> print(clf.predict([[-0.8, -1]]))
[1]
```

Methods

<table>
<thead>
<tr>
<th>Method</th>
<th>Description</th>
</tr>
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<tbody>
<tr>
<td>decision_function(X)</td>
<td>Distance of the samples X to the separating hyperplane.</td>
</tr>
<tr>
<td>fit(X, y[, sample_weight])</td>
<td>Fit the SVM model according to the given training data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Perform classification on samples in X.</td>
</tr>
<tr>
<td>score(X, y[, sample_weight])</td>
<td>Returns the mean accuracy on the given test data and labels.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>
__init__ (C=1.0, kernel='rbf', degree=3, gamma='auto', coef0=0.0, shrinking=True, probability=False, tol=0.001, cache_size=200, class_weight=None, verbose=False, max_iter=-1, decision_function_shape='ovr', random_state=None)

decision_function (X)
Distance of the samples X to the separating hyperplane.

Parameters X : array-like, shape (n_samples, n_features)

Returns X : array-like, shape (n_samples, n_classes * (n_classes-1) / 2)
Returns the decision function of the sample for each class in the model. If decision_function_shape='ovr', the shape is (n_samples, n_classes)

fit (X, y, sample_weight=None)
Fit the SVM model according to the given training data.

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
Training vectors, where n_samples is the number of samples and n_features is the number of features. For kernel="precomputed", the expected shape of X is (n_samples, n_samples).

y : array-like, shape (n_samples,)
Target values (class labels in classification, real numbers in regression)

sample_weight : array-like, shape (n_samples,)
Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

Returns self : object
Returns self.

Notes
If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr_matrix, X and/or y may be copied.
If X is a dense array, then the other methods will not support sparse matrices as input.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X)
Perform classification on samples in X.
For an one-class model, +1 or -1 is returned.

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
For kernel="precomputed", the expected shape of X is [n_samples_test, n_samples_train]
**Returns**  
`y_pred` : array, shape (n_samples,)  
Class labels for samples in X.

**predict_log_proba**  
Compute log probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute `probability` set to True.

**Parameters**  
`X` : array-like, shape (n_samples, n_features)

For kernel="precomputed", the expected shape of X is [n_samples_test, n_samples_train]

**Returns**  
`T` : array-like, shape (n_samples, n_classes)

Returns the log-probabilities of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**Notes**  
The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

**predict_proba**  
Compute probabilities of possible outcomes for samples in X.

The model need to have probability information computed at training time: fit with attribute `probability` set to True.

**Parameters**  
`X` : array-like, shape (n_samples, n_features)

For kernel="precomputed", the expected shape of X is [n_samples_test, n_samples_train]

**Returns**  
`T` : array-like, shape (n_samples, n_classes)

Returns the probability of the sample for each class in the model. The columns correspond to the classes in sorted order, as they appear in the attribute `classes_`.

**Notes**  
The probability model is created using cross validation, so the results can be slightly different than those obtained by predict. Also, it will produce meaningless results on very small datasets.

**score**  
`(X, y, sample_weight=None)`  
Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**  
`X` : array-like, shape = (n_samples, n_features)

Test samples.

`y` : array-like, shape = (n_samples) or (n_samples, n_outputs)

True labels for X.

`sample_weight` : array-like, shape = [n_samples], optional
Sample weights.

**Returns** score : float

Mean accuracy of self.predict(X) wrt. y.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

---

**Examples using sklearn.svm.SVC**

- Concatenating multiple feature extraction methods
- Multilabel classification
- Feature Union with Heterogeneous Data Sources
- Explicit feature map approximation for RBF kernels
- Faces recognition example using eigenfaces and SVMs
- Libsvm GUI
- Recognizing hand-written digits
- Plot classification probability
- Classifier comparison
- Plot the decision boundaries of a VotingClassifier
- Cross-validation on Digits Dataset Exercise
- SVM Exercise
- Recursive feature elimination
- Pipeline Anova SVM
- Recursive feature elimination with cross-validation
- Test with permutations the significance of a classification score
- Univariate Feature Selection
- Plotting Validation Curves
- Parameter estimation using grid search with cross-validation
- Receiver Operating Characteristic (ROC) with cross validation
- Confusion matrix
- Nested versus non-nested cross-validation
- Receiver Operating Characteristic (ROC)
- Plotting Learning Curves
- Decision boundary of label propagation versus SVM on the Iris dataset
- SVM: Maximum margin separating hyperplane
Epsilon-Support Vector Regression. The free parameters in the model are C and epsilon.
The implementation is based on libsvm.
Read more in the User Guide.

Parameters

- **C** : float, optional (default=1.0)
  Penalty parameter C of the error term.

- **epsilon** : float, optional (default=0.1)
  Epsilon in the epsilon-SVR model. It specifies the epsilon-tube within which no penalty is associated in the training loss function with points predicted within a distance epsilon from the actual value.

- **kernel** : string, optional (default='rbf')
  Specifies the kernel type to be used in the algorithm. It must be one of ‘linear’, ‘poly’, ‘rbf’, ‘sigmoid’, ‘precomputed’ or a callable. If none is given, ‘rbf’ will be used. If a callable is given it is used to precompute the kernel matrix.

- **degree** : int, optional (default=3)
  Degree of the polynomial kernel function (‘poly’). Ignored by all other kernels.

- **gamma** : float, optional (default=‘auto’)
  Kernel coefficient for ‘rbf’, ‘poly’ and ‘sigmoid’. If gamma is ‘auto’ then 1/n_features will be used instead.

- **coef0** : float, optional (default=0.0)
  Independent term in kernel function. It is only significant in ‘poly’ and ‘sigmoid’.

- **shrinking** : boolean, optional (default=True)
  Whether to use the shrinking heuristic.

- **tol** : float, optional (default=1e-3)
  Tolerance for stopping criterion.

- **cache_size** : float, optional
Specify the size of the kernel cache (in MB).

verbose : bool, default: False

Enable verbose output. Note that this setting takes advantage of a per-process runtime setting in libsvm that, if enabled, may not work properly in a multithreaded context.

max_iter : int, optional (default=-1)

Hard limit on iterations within solver, or -1 for no limit.

Attributes

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<th>Description</th>
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<td>support_</td>
<td>(array-like, shape = [n_SV]) Indices of support vectors.</td>
</tr>
<tr>
<td>support_vectors_</td>
<td>(array-like, shape = [nSV, n_features]) Support vectors.</td>
</tr>
<tr>
<td>dual_coef_</td>
<td>(array, shape = [1, n_SV]) Coefficients of the support vector in the decision function.</td>
</tr>
<tr>
<td>coef_</td>
<td>(array, shape = [1, n_features]) Weights assigned to the features (coefficients in the primal problem). This is only available in the case of a linear kernel. coef_ is readonly property derived from dual_coef_ and support_vectors_.</td>
</tr>
<tr>
<td>intercept_</td>
<td>(array, shape = [1]) Constants in decision function.</td>
</tr>
<tr>
<td>sample_weight</td>
<td>(array-like, shape = [n_samples]) Individual weights for each sample</td>
</tr>
</tbody>
</table>

See also:

NuSVR  Support Vector Machine for regression implemented using libsvm using a parameter to control the number of support vectors.

LinearSVR  Scalable Linear Support Vector Machine for regression implemented using liblinear.

Examples

```python
>>> from sklearn.svm import SVR
>>> import numpy as np
>>> n_samples, n_features = 10, 5
>>> np.random.seed(0)
>>> y = np.random.randn(n_samples)
>>> X = np.random.randn(n_samples, n_features)
>>> clf = SVR(C=1.0, epsilon=0.2)
>>> clf.fit(X, y)
SVR(C=1.0, cache_size=200, coef0=0.0, degree=3, epsilon=0.2, gamma='auto',
    kernel='rbf', max_iter=-1, shrinking=True, tol=0.001, verbose=False)
```

Methods

- `fit(X, y[, sample_weight])`: Fit the SVM model according to the given training data.
- `get_params([deep])`: Get parameters for this estimator.

Continued on next page
predict(X)  Perform regression on samples in X.

score(X, y[, sample_weight])  Returns the coefficient of determination $R^2$ of the prediction.

set_params(**params)  Set the parameters of this estimator.

__init__ (kernel='rbf', degree=3, gamma='auto', coef0=0.0, tol=0.001, C=1.0, epsilon=0.1, shrinking=True, cache_size=200, verbose=False, max_iter=-1)

fit (X, y, sample_weight=None)
Fit the SVM model according to the given training data.

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
Training vectors, where n_samples is the number of samples and n_features is the number of features. For kernel="precomputed", the expected shape of X is (n_samples, n_samples).

y : array-like, shape (n_samples,)
Target values (class labels in classification, real numbers in regression)

sample_weight : array-like, shape (n_samples,)
Per-sample weights. Rescale C per sample. Higher weights force the classifier to put more emphasis on these points.

Returns self : object
Returns self.

Notes

If X and y are not C-ordered and contiguous arrays of np.float64 and X is not a scipy.sparse.csr_matrix, X and/or y may be copied.

If X is a dense array, then the other methods will not support sparse matrices as input.

generate (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X)
Perform regression on samples in X.

For an one-class model, +1 (inlier) or -1 (outlier) is returned.

Parameters X : {array-like, sparse matrix}, shape (n_samples, n_features)
For kernel="precomputed", the expected shape of X is (n_samples_test, n_samples_train).

Returns y_pred : array, shape (n_samples,)
**score** *(X, y, **sample_weight=None)**

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred}) ** 2).sum()$ and $v$ is the total sum of squares $((y_{true} - y_{true.mean()}) ** 2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True values for $X$.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**

- **score**: float
  - $R^2$ of self.predict(X) wrt. $y$.

**set_params** (**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns**

- **self**

---

**Examples using sklearn.svm.SVR**

- *Comparison of kernel ridge regression and SVR*
- *Prediction Latency*
- *Support Vector Regression (SVR) using linear and non-linear kernels*

```python
from sklearn.svm import SVR

# example of SVR using linear and non-linear kernels

# example of SVR using linear and non-linear kernels
```

---

**sklearn.svm.l1_min_c**

**sklearn.svm.l1_min_c** *(X, y[, loss, fit_intercept, ...])*

Return the lowest bound for C such that for C in (l1_min_C, infinity) the model is guaranteed not to be empty.

This value is valid if class_weight parameter in fit() is not set.

**Parameters**

- **X**: array-like or sparse matrix, shape = [n_samples, n_features]
  - Training vector, where n_samples in the number of samples and n_features is the number of features.
- **y**: array, shape = [n_samples]
  - Target vector relative to $X$
loss : {'squared_hinge', 'log'}, default ‘squared_hinge’

Specifies the loss function. With ‘squared_hinge’ it is the squared hinge loss (a.k.a. L2 loss). With 'log' it is the loss of logistic regression models. ‘l2’ is accepted as an alias for ‘squared_hinge’, for backward compatibility reasons, but should not be used in new code.

fit_intercept : bool, default: True

Specifies if the intercept should be fitted by the model. It must match the fit() method parameter.

intercept_scaling : float, default: 1

when fit_intercept is True, instance vector x becomes [x, intercept_scaling], i.e. a “synthetic” feature with constant value equals to intercept_scaling is appended to the instance vector. It must match the fit() method parameter.

Returns l1_min_c : float

minimum value for C

Examples using sklearn.svm.l1_min_c

• Path with L1- Logistic Regression

30.33.2 Low-level methods

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<td>Binding of the cross-validation routine (low-level routine)</td>
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<td>svm.libsvm.decision_function</td>
<td>Predict margin (libsvm name for this is predict_values)</td>
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<tr>
<td>svm.libsvm.fit</td>
<td>Train the model using libsvm (low-level method)</td>
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<tr>
<td>svm.libsvm.predict</td>
<td>Predict target values of X given a model (low-level method)</td>
</tr>
<tr>
<td>svm.libsvm.predict_proba</td>
<td>Predict probabilities</td>
</tr>
</tbody>
</table>

sklearn.svm.libsvm.cross_validation

sklearn.svm.libsvm.cross_validation()

Binding of the cross-validation routine (low-level routine)

Parameters

- `X` : array-like, dtype=float, size=[n_samples, n_features]
- `Y` : array, dtype=float, size=[n_samples]
- `svm_type` : {0, 1, 2, 3, 4}
  Type of SVM: C SVC, nu SVC, one class, epsilon SVR, nu SVR
- `kernel` : {'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}
  Kernel to use in the model: linear, polynomial, RBF, sigmoid or precomputed.
- `degree` : int
  Degree of the polynomial kernel (only relevant if kernel is set to polynomial)
- `gamma` : float
Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

**coef0**: float

Independent parameter in poly/sigmoid kernel.

**tol**: float

Stopping criteria.

**C**: float

C parameter in C-Support Vector Classification

**nu**: float

Cache size

**random_seed**: int, optional

Seed for the random number generator used for probability estimates. 0 by default.

**Returns**

**target**: array, float

**sklearn.svm.libsvm.decision_function**

**sklearn.svm.libsvm.decision_function()**

Predict margin (libsvm name for this is predict_values)

We have to reconstruct model and parameters to make sure we stay in sync with the python object.

**sklearn.svm.libsvm.fit**

**sklearn.svm.libsvm.fit()**

Train the model using libsvm (low-level method)

**Parameters**

**X**: array-like, dtype=float64, size=[n_samples, n_features]

**Y**: array, dtype=float64, size=[n_samples]

**target vector**

**svm_type**: {0, 1, 2, 3, 4}, optional

Type of SVM: C_SVC, NuSVC, OneClassSVM, EpsilonSVR or NuSVR respectively. 0 by default.

**kernel**: {'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}, optional

Kernel to use in the model: linear, polynomial, RBF, sigmoid or precomputed. ‘rbf’ by default.

**degree**: int32, optional

Degree of the polynomial kernel (only relevant if kernel is set to polynomial), 3 by default.

**gamma**: float64, optional

Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

**coef0**: float64, optional

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2009
Independent parameter in poly/sigmoid kernel. 0 by default.

**tol**: float64, optional

Numeric stopping criterion (WRITEME). 1e-3 by default.

**C**: float64, optional

C parameter in C-Support Vector Classification. 1 by default.

**nu**: float64, optional

0.5 by default.

**epsilon**: double, optional

0.1 by default.

**class_weight**: array, dtype float64, shape (n_classes,), optional

np.empty(0) by default.

**sample_weight**: array, dtype float64, shape (n_samples,), optional

np.empty(0) by default.

**shrinking**: int, optional

1 by default.

**probability**: int, optional

0 by default.

**cache_size**: float64, optional

Cache size for gram matrix columns (in megabytes). 100 by default.

**max_iter**: int (-1 for no limit), optional.

Stop solver after this many iterations regardless of accuracy (XXX Currently there is no API to know whether this kicked in.) -1 by default.

**random_seed**: int, optional

Seed for the random number generator used for probability estimates. 0 by default.

Returns **support**: array, shape=[n_support]

index of support vectors

**support_vectors**: array, shape=[n_support, n_features]

support vectors (equivalent to X[support]). Will return an empty array in the case of precomputed kernel.

**n_class_SV**: array

number of support vectors in each class.

**sv_coef**: array

coefficients of support vectors in decision function.

**intercept**: array

intercept in decision function

**probA, probB**: array

probability estimates, empty array for probability=False
sklearn.svm.libsvm.predict

sklearn.svm.libsvm.predict()  
Predict target values of X given a model (low-level method)

Parameters  
X : array-like, dtype=float, size=[n_samples, n_features]

svm_type : {0, 1, 2, 3, 4}
Type of SVM: C SVC, nu SVC, one class, epsilon SVR, nu SVR

kernel : {'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}
Type of kernel.

degree : int
Degree of the polynomial kernel.

gamma : float
Gamma parameter in rbf, poly and sigmoid kernels. Ignored by other kernels. 0.1 by default.

coeff : float
Independent parameter in poly/sigmoid kernel.

Returns  
dec_values : array
predicted values.

sklearn.svm.libsvm.predict_proba

sklearn.svm.libsvm.predict_proba()  
Predict probabilities

svm_model stores all parameters needed to predict a given value.
For speed, all real work is done at the C level in function copy_predict (libsvm_helper.c).
We have to reconstruct model and parameters to make sure we stay in sync with the python object.
See sklearn.svm.predict for a complete list of parameters.

Parameters  
X : array-like, dtype=float

kernel : {'linear', 'rbf', 'poly', 'sigmoid', 'precomputed'}

Returns  
dec_values : array
predicted values.

30.34 sklearn.tree: Decision Trees

The sklearn.tree module includes decision tree-based models for classification and regression.

User guide: See the Decision Trees section for further details.

tree.DecisionTreeClassifier([criterion, ...])  A decision tree classifier.
tree.DecisionTreeRegressor([criterion, ...])  A decision tree regressor.
Table 30.298 – continued from previous page

<table>
<thead>
<tr>
<th>Class</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>tree.ExtraTreeClassifier([criterion,...])</td>
<td>An extremely randomized tree classifier.</td>
</tr>
<tr>
<td>tree.ExtraTreeRegressor([criterion,...])</td>
<td>An extremely randomized tree regressor.</td>
</tr>
</tbody>
</table>

### 30.34.1 sklearn.tree.DecisionTreeClassifier

```python
class sklearn.tree.DecisionTreeClassifier(criterion='gini', splitter='best', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features=None, random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, class_weight=None, presort=False)
```

A decision tree classifier.

Read more in the User Guide.

**Parameters**

- **criterion** : string, optional (default=’gini’)
  
The function to measure the quality of a split. Supported criteria are “gini” for the Gini impurity and “entropy” for the information gain.

- **splitter** : string, optional (default=’best’)
  
The strategy used to choose the split at each node. Supported strategies are “best” to choose the best split and “random” to choose the best random split.

- **max_depth** : int or None, optional (default=None)
  
The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min_samples_split samples.

- **min_samples_split** : int, float, optional (default=2)
  
The minimum number of samples required to split an internal node:
  
  - If int, then consider min_samples_split as the minimum number.
  - If float, then min_samples_split is a percentage and \(\text{ceil}(\text{min_samples_split} \times n_{\text{samples}})\) are the minimum number of samples for each split.
  
  Changed in version 0.18: Added float values for percentages.

- **min_samples_leaf** : int, float, optional (default=1)
  
The minimum number of samples required to be at a leaf node:
  
  - If int, then consider min_samples_leaf as the minimum number.
  - If float, then min_samples_leaf is a percentage and \(\text{ceil}(\text{min_samples_leaf} \times n_{\text{samples}})\) are the minimum number of samples for each node.
  
  Changed in version 0.18: Added float values for percentages.

- **min_weight_fraction_leaf** : float, optional (default=0.)
  
The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

- **max_features** : int, float, string or None, optional (default=None)
  
Keywords that can be used to specify features (e.g. “auto” to let the best be chosen).

- **random_state** : int, RandomState instance or None, optional (default=None)
  
Control the randomness of the split.

- **max_leaf_nodes** : int or None, optional (default=None)
  
The限制 maximum number of leaves in the tree. If None, then no limit is imposed.

- **class_weight** : dict or list of dicts, optional (default=None)
  
The strategy to compute class weights (e.g., frequency). The default is None.

- **presort** : bool, optional (default=False)
  
Whether to presort the data to speed up the construction of leaf nodes. The algorithm requires O(n^2) in general to build all leaf nodes. By pre-sorting the data, it can achieve O(n log(n)) complexity.

---

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The number of features to consider when looking for the best split:

- If int, then consider \textit{max\_features} features at each split.
- If float, then \textit{max\_features} is a percentage and \textit{int(max\_features * n\_features)} features are considered at each split.
- If “auto”, then \textit{max\_features} = \textit{sqrt(n\_features)}.
- If “sqrt”, then \textit{max\_features} = \textit{sqrt(n\_features)}.
- If “log2”, then \textit{max\_features} = \textit{log2(n\_features)}.
- If None, then \textit{max\_features} = \textit{n\_features}.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than \textit{max\_features} features.

\textbf{random\_state} : int, RandomState instance or None, optional (default=None)

If int, random\_state is the seed used by the random number generator; If RandomState instance, random\_state is the random number generator; If None, the random number generator is the RandomState instance used by \textit{np.random}.

\textbf{max\_leaf\_nodes} : int or None, optional (default=None)

Grow a tree with \textit{max\_leaf\_nodes} in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

\textbf{min\_impurity\_decrease} : float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
N_t / N * (\text{impurity} - \frac{N_{t\_R}}{N_t} \times \text{right\_impurity} - \frac{N_{t\_L}}{N_t} \times \text{left\_impurity})
\]

where \(N\) is the total number of samples, \(N_t\) is the number of samples at the current node, \(N_{t\_L}\) is the number of samples in the left child, and \(N_{t\_R}\) is the number of samples in the right child.

\(N, N_{t\_L}, N_{t\_R}\) and \(N_{t\_R}\) all refer to the weighted sum, if \textit{sample\_weight} is passed.

New in version 0.19.

\textbf{min\_impurity\_split} : float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: \textit{min\_impurity\_split} has been deprecated in favor of \textit{min\_impurity\_decrease} in 0.19 and will be removed in 0.21. Use \textit{min\_impurity\_decrease} instead.

\textbf{class\_weight} : dict, list of dicts, “balanced” or None, default=None

Weights associated with classes in the form \{\textit{class\_label}: \textit{weight}\}. If not given, all classes are supposed to have weight one. For multi-output problems, a list of dicts can be provided in the same order as the columns of \(y\).
Note that for multioutput (including multilabel) weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be \([[0: 1, 1: 1], [0: 1, 1: 5], [0: 1, 1: 1], [0: 1, 1: 1]]\) instead of [[1:1], [2:5], [3:1], [4:1]].

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as \(\frac{n_{\text{samples}}}{(n_{\text{classes}} \times \text{np.bincount}(y))}\)

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with sample_weight (passed through the fit method) if sample_weight is specified.

**presort**: bool, optional (default=False)

Whether to presort the data to speed up the finding of best splits in fitting. For the default settings of a decision tree on large datasets, setting this to true may slow down the training process. When using either a smaller dataset or a restricted depth, this may speed up the training.

### Attributes

**feature_importances_**: Return the feature importances.

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>classes_</td>
<td>(array of shape = [n_classes] or a list of such arrays) The classes labels (single output problem), or a list of arrays of class labels (multi-output problem).</td>
</tr>
<tr>
<td>max_features</td>
<td>(int) The inferred value of max_features.</td>
</tr>
<tr>
<td>n_classes</td>
<td>(int or list) The number of classes (for single output problems), or a list containing the number of classes for each output (for multi-output problems).</td>
</tr>
<tr>
<td>n_features</td>
<td>(int) The number of features when fit is performed.</td>
</tr>
<tr>
<td>n_outputs</td>
<td>(int) The number of outputs when fit is performed.</td>
</tr>
<tr>
<td>tree_</td>
<td>(Tree object) The underlying Tree object.</td>
</tr>
</tbody>
</table>

**See also:**

`DecisionTreeRegressor`

### Notes

The default values for the parameters controlling the size of the trees (e.g. `max_depth`, `min_samples_leaf`, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and `max_features=n_features`, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, `random_state` has to be fixed.
References

[R195198], [R196198], [R197198], [R198198]

Examples

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn.model_selection import cross_val_score
>>> from sklearn.tree import DecisionTreeClassifier

>>> clf = DecisionTreeClassifier(random_state=0)
>>> iris = load_iris()
>>> cross_val_score(clf, iris.data, iris.target, cv=10)
... 
... array([ 1.0, 0.93..., 0.86..., 0.93..., 0.93..., 0.93..., 0.93..., 1.0, 0.93..., 1.0])
```

Methods

```
apply(X[, check_input]) Returns the index of the leaf that each sample is predicted as.
decision_path(X[, check_input]) Return the decision path in the tree
fit(X, y[, sample_weight, check_input,...]) Build a decision tree classifier from the training set (X, y).
get_params([deep]) Get parameters for this estimator.
predict(X[, check_input]) Predict class or regression value for X.
predict_log_proba(X) Predict class log-probabilities of the input samples X.
predict_proba(X[, check_input]) Predict class probabilities of the input samples X.
score(X, y[, sample_weight]) Returns the mean accuracy on the given test data and labels.
set_params(**params) Set the parameters of this estimator.
```

```
__init__(criterion='gini', splitter='best', max_depth=None, min_samples_split=2,
         min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features=None,
         random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0,
         min_impurity_split=None, class_weight=None, presort=False)

apply(X, check_input=True)
    Returns the index of the leaf that each sample is predicted as.

    New in version 0.17.

    Parameters X : array_like or sparse matrix, shape = [n_samples, n_features]
        The input samples. Internally, it will be converted to dtype=np.float32 and
        if a sparse matrix is provided to a sparse csr_matrix.

    check_input : boolean, (default=True)
        Allow to bypass several input checking. Don’t use this parameter unless you
        know what you do.

    Returns X_leaves : array_like, shape = [n_samples,]
```

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For each datapoint $x$ in $X$, return the index of the leaf $x$ ends up in. Leaves are numbered within $[0; \text{self.tree_.node_count})$, possibly with gaps in the numbering.

**decision_path** ($X$, *check_input=True*)

Return the decision path in the tree

New in version 0.18.

**Parameters**

$X$ : array_like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to $\text{dtype=np.float32}$ and if a sparse matrix is provided to a sparse $\text{csr_matrix}$.

*check_input* : boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**

indicator : sparse csr array, shape = [n_samples, n_nodes]

Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**feature_importances_**

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

**Returns**

feature_importances_ : array, shape = [n_features]

**fit** ($X$, $y$, *sample_weight=None, check_input=True, X_idx_sorted=None*)

Build a decision tree classifier from the training set ($X$, $y$).

**Parameters**

$X$ : array-like or sparse matrix, shape = [n_samples, n_features]

The training input samples. Internally, it will be converted to $\text{dtype=np.float32}$ and if a sparse matrix is provided to a sparse $\text{csc_matrix}$.

$y$ : array-like, shape = [n_samples] or [n_samples, n_outputs]

The target values (class labels) as integers or strings.

*sample_weight* : array-like, shape = [n_samples] or None

Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. Splits are also ignored if they would result in any single class carrying a negative weight in either child node.

*check_input* : boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

*X_idx_sorted* : array-like, shape = [n_samples, n_features], optional

The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don’t use this parameter unless you know what to do.

**Returns**

self : object

Returns self.
get_params (deep=True)
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X, check_input=True)
Predict class or regression value for X.
For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

check_input : boolean, (default=True)
Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

Returns y : array of shape = [n_samples] or [n_samples, n_outputs]
The predicted classes, or the predict values.

predict_log_proba (X)
Predict class log-probabilities of the input samples X.

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

Returns p : array of shape = [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1. The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute classes._

predict_proba (X, check_input=True)
Predict class probabilities of the input samples X.
The predicted class probability is the fraction of samples of the same class in a leaf.

check_input [boolean, (default=True)] Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

check_input : bool
Run check_array on X.

Returns p : array of shape = [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes._
score(X, y, sample_weight=None)

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  
  Test samples.

- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  
  True labels for X.

- **sample_weight**: array-like, shape = [n_samples], optional
  
  Sample weights.

**Returns**

- **score**: float
  
  Mean accuracy of self.predict(X) wrt. y.

set_params(**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**

---

**Examples using sklearn.tree.DecisionTreeClassifier**

- *Classifier comparison*
- *Plot the decision boundaries of a VotingClassifier*
- *Two-class AdaBoost*
- *Discrete versus Real AdaBoost*
- *Multi-class AdaBoosted Decision Trees*
- *Plot the decision surfaces of ensembles of trees on the iris dataset*
- *Demonstration of multi-metric evaluation on cross_val_score and GridSearchCV*
- *Plot the decision surface of a decision tree on the iris dataset*
- *Understanding the decision tree structure*

---

**30.34.2 sklearn.tree.DecisionTreeRegressor**

**class sklearn.tree.DecisionTreeRegressor**(criterion='mse', splitter='best', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features=None, random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, presort=False)

A decision tree regressor.

Read more in the User Guide.

**Parameters**

- **criterion**: string, optional (default="mse")
The function to measure the quality of a split. Supported criteria are “mse” for the mean squared error, which is equal to variance reduction as feature selection criterion and minimizes the L2 loss using the mean of each terminal node, “friedman_mse”, which uses mean squared error with Friedman’s improvement score for potential splits, and “mae” for the mean absolute error, which minimizes the L1 loss using the median of each terminal node.

New in version 0.18: Mean Absolute Error (MAE) criterion.

**splitter**: string, optional (default=“best”)

The strategy used to choose the split at each node. Supported strategies are “best” to choose the best split and “random” to choose the best random split.

**max_depth**: int or None, optional (default=None)

The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than min_samples_split samples.

**min_samples_split**: int, float, optional (default=2)

The minimum number of samples required to split an internal node:

- If int, then consider min_samples_split as the minimum number.
- If float, then min_samples_split is a percentage and ceil(min_samples_split * n_samples) are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider min_samples_leaf as the minimum number.
- If float, then min_samples_leaf is a percentage and ceil(min_samples_leaf * n_samples) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

**max_features**: int, float, string or None, optional (default=None)

The number of features to consider when looking for the best split:

- If int, then consider max_features features at each split.
- If float, then max_features is a percentage and int(max_features * n_features) features are considered at each split.
- If “auto”, then max_features=n_features.
- If “sqrt”, then max_features=sqrt(n_features).
- If “log2”, then max_features=log2(n_features).
- If None, then max_features=n_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max_features features.
**random_state**: int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**max_leaf_nodes**: int or None, optional (default=None)

Grow a tree with max_leaf_nodes in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_t}{N} \times \left( \text{impurity} - \frac{N_{t,R}}{N_t} \times \text{right_impurity} - \frac{N_{t,L}}{N_t} \times \text{left_impurity} \right)
\]

where \( N \) is the total number of samples, \( N_t \) is the number of samples at the current node, \( N_{t,L} \) is the number of samples in the left child, and \( N_{t,R} \) is the number of samples in the right child.

\( N, N_t, N_{t,R} \) and \( N_{t,L} \) all refer to the weighted sum, if sample_weight is passed.

New in version 0.19.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min_impurity_split has been deprecated in favor of min_impurity_decrease in 0.19 and will be removed in 0.21. Use min_impurity_decrease instead.

**presort**: bool, optional (default=False)

Whether to presort the data to speed up the finding of best splits in fitting. For the default settings of a decision tree on large datasets, setting this to true may slow down the training. When using either a smaller dataset or a restricted depth, this may speed up the training.

**Attributes**

- `feature_importances_`: Return the feature importances.
- `max_features_`: (int,) The inferred value of max_features.
- `n_features_`: (int) The number of features when fit is performed.
- `n_outputs_`: (int) The number of outputs when fit is performed.
- `tree_`: (Tree object) The underlying Tree object.

**See also:**

`DecisionTreeClassifier`
Notes

The default values for the parameters controlling the size of the trees (e.g. max_depth, min_samples_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

The features are always randomly permuted at each split. Therefore, the best found split may vary, even with the same training data and max_features=n_features, if the improvement of the criterion is identical for several splits enumerated during the search of the best split. To obtain a deterministic behaviour during fitting, random_state has to be fixed.

References

[R203206], [R204206], [R205206], [R206206]

Examples

```python
>>> from sklearn.datasets import load_boston
>>> from sklearn.model_selection import cross_val_score
>>> from sklearn.tree import DecisionTreeRegressor

>>> boston = load_boston()
>>> regressor = DecisionTreeRegressor(random_state=0)
>>> cross_val_score(regressor, boston.data, boston.target, cv=10)
...  ...  
array([ 0.61..., 0.57..., -0.34..., 0.41..., 0.75..., 0.07..., 0.29..., 0.33..., -1.42..., -1.77...])
```

Methods

- `apply(X[, check_input])`: Returns the index of the leaf that each sample is predicted as. New in version 0.17.
- `decision_path(X[, check_input])`: Return the decision path in the tree.
- `fit(X, y[, sample_weight, check_input, ...])`: Build a decision tree regressor from the training set (X, y).
- `get_params([deep])`: Get parameters for this estimator.
- `predict(X[, check_input])`: Predict class or regression value for X.
- `score(X, y[, sample_weight])`: Returns the coefficient of determination R^2 of the prediction.
- `set_params(**params)`: Set the parameters of this estimator.

```python
__init__(criterion='mse', splitter='best', max_depth=None, min_samples_split=2,
         min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features=None,
         random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0,
         min_impurity_split=None, presort=False)

apply(X, check_input=True)

    Returns the index of the leaf that each sample is predicted as.

New in version 0.17.
```
Parameters **X**: array_like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**check_input**: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns X_leaves**: array_like, shape = [n_samples,]

For each datapoint x in X, return the index of the leaf x ends up in. Leaves are numbered within [0; self.tree_.node_count), possibly with gaps in the numbering.

**decision_path** *(X, check_input=True)*

Return the decision path in the tree

New in version 0.18.

Parameters **X**: array_like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**check_input**: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns indicator**: sparse csr array, shape = [n_samples, n_nodes]

Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**feature_importances_**

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

**Returns feature_importances_**: array, shape = [n_features]

**fit**(X, y, sample_weight=None, check_input=True, X_idx_sorted=None)

Build a decision tree regressor from the training set (X, y).

Parameters **X**: array-like or sparse matrix, shape = [n_samples, n_features]

The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc_matrix.

**y**: array-like, shape = [n_samples] or [n_samples, n_outputs]

The target values (real numbers). Use dtype=np.float64 and order='C' for maximum efficiency.

**sample_weight**: array-like, shape = [n_samples] or None

Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node.

**check_input**: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.
X_idx_sorted: array-like, shape = [n_samples, n_features], optional

The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don’t use this parameter unless you know what to do.

Returns self: object

Returns self.

get_params (deep=True)
Get parameters for this estimator.

Parameters deep: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params: mapping of string to any

Parameter names mapped to their values.

predict (X, check_input=True)
Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

Parameters X: array-like or sparse matrix of shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

check_input: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

Returns y: array of shape = [n_samples] or [n_samples, n_outputs]

The predicted classes, or the predict values.

score (X, y, sample_weight=None)
Returns the coefficient of determination R^2 of the prediction.

The coefficient R^2 is defined as (1 - u/v), where u is the residual sum of squares ((y_true - y_pred) ** 2).sum() and v is the total sum of squares ((y_true - y_true.mean()) ** 2).sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a R^2 score of 0.0.

Parameters X: array-like, shape = (n_samples, n_features)

Test samples.

y: array-like, shape = (n_samples) or (n_samples, n_outputs)

True values for X.

sample_weight: array-like, shape = [n_samples], optional

Sample weights.

Returns score: float

R^2 of self.predict(X) wrt. y.
set_params (**params)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

Examples using `sklearn.tree.DecisionTreeRegressor`

- Decision Tree Regression with AdaBoost
- Single estimator versus bagging: bias-variance decomposition
- Decision Tree Regression
- Multi-output Decision Tree Regression

30.34.3 `sklearn.tree.ExtraTreeClassifier`

```python
class sklearn.tree.ExtraTreeClassifier (criterion='gini', splitter='random', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, class_weight=None)
```

An extremely randomized tree classifier.

Extra-trees differ from classic decision trees in the way they are built. When looking for the best split to separate the samples of a node into two groups, random splits are drawn for each of the `max_features` randomly selected features and the best split among those is chosen. When `max_features` is set 1, this amounts to building a totally random decision tree.

Warning: Extra-trees should only be used within ensemble methods.

Read more in the User Guide.

**Parameters**

- **criterion**: string, optional (default=”gini”)
  The function to measure the quality of a split. Supported criteria are “gini” for the Gini impurity and “entropy” for the information gain.

- **splitter**: string, optional (default=”best”)
  The strategy used to choose the split at each node. Supported strategies are “best” to choose the best split and “random” to choose the best random split.

- **max_depth**: int or None, optional (default=None)
  The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than `min_samples_split` samples.

- **min_samples_split**: int, float, optional (default=2)
  The minimum number of samples required to split an internal node:
  - If int, then consider `min_samples_split` as the minimum number.
  - If float, then `min_samples_split` is a percentage and `ceil(min_samples_split * n_samples)` are the minimum number of samples for each split.
Changed in version 0.18: Added float values for percentages.

**min_samples_leaf**: int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider \texttt{min_samples_leaf} as the minimum number.
- If float, then \texttt{min_samples_leaf} is a percentage and \( \text{ceil}(\text{min_samples_leaf} \times \text{n_samples}) \) are the minimum number of samples for each node.

Changed in version 0.18: Added float values for percentages.

**min_weight_fraction_leaf**: float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when \texttt{sample_weight} is not provided.

**max_features**: int, float, string or None, optional (default=None)

The number of features to consider when looking for the best split:

- If int, then consider \texttt{max_features} features at each split.
- If float, then \texttt{max_features} is a percentage and \( \text{int}(\text{max_features} \times \text{n_features}) \) features are considered at each split.
- If “auto”, then \texttt{max_features} is \( \sqrt{\text{n_features}} \).
- If “sqrt”, then \texttt{max_features} is \( \sqrt{\text{n_features}} \).
- If “log2”, then \texttt{max_features} is \( \log_2(\text{n_features}) \).
- If None, then \texttt{max_features} is \( \text{n_features} \).

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than \texttt{max_features} features.

**random_state**: int, RandomState instance or None, optional (default=None)

If int, \texttt{random_state} is the seed used by the random number generator; If RandomState instance, \texttt{random_state} is the random number generator; If None, the random number generator is the RandomState instance used by \texttt{np.random}.

**max_leaf_nodes**: int or None, optional (default=None)

Grow a tree with \texttt{max_leaf_nodes} in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**min_impurity_decrease**: float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_t}{N} \times (\text{impurity} - \frac{N_{t,R}}{N_t} \times \text{right_impurity} - \frac{N_{t,L}}{N_t} \times \text{left_impurity})
\]

where \( N \) is the total number of samples, \( N_{t} \) is the number of samples at the current node, \( N_{t,L} \) is the number of samples in the left child, and \( N_{t,R} \) is the number of samples in the right child.
N, N_t, N_t_R and N_t_L all refer to the weighted sum, if sample_weight is passed.

New in version 0.19.

**min_impurity_split**: float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min_impurity_split has been deprecated in favor of min_impurity_decrease in 0.19 and will be removed in 0.21. Use min_impurity_decrease instead.

**class_weight**: dict, list of dicts, “balanced” or None, default=None

Weights associated with classes in the form {class_label: weight}. If not given, all classes are supposed to have weight one. For multi-output problems, a list of dicts can be provided in the same order as the columns of y.

Note that for multilabel classification, weights should be defined for each class of every column in its own dict. For example, for four-class multilabel classification weights should be [{0: 1, 1: 1}, {0: 1, 1: 5}, {0: 1, 1: 1}, {0: 1, 1: 1}] instead of [{1:1}, {2:5}, {3:1}, {4:1}].

The “balanced” mode uses the values of y to automatically adjust weights inversely proportional to class frequencies in the input data as n_samples / (n_classes * np.bincount(y))

For multi-output, the weights of each column of y will be multiplied.

Note that these weights will be multiplied with sample_weight (passed through the fit method) if sample_weight is specified.

Attributes

**feature_importances_**: Return the feature importances.

See also:

*ExtraTreeRegressor*, *ExtraTreesClassifier*, *ExtraTreesRegressor*

Notes

The default values for the parameters controlling the size of the trees (e.g. max_depth, min_samples_leaf, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

References

[R589589]
### Methods

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**__init__**(criterion='gini', splitter='random', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', random_state=None, max_leaf_nodes=None, min_impurity_decrease=0.0, min_impurity_split=None, class_weight=None)

**apply** *(X, check_input=True)*

Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

**Parameters**
- **X**: array_like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

- **check_input** : boolean, (default=True)
  
  Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**
- **X_leaves** : array_like, shape = [n_samples,]
  
  For each datapoint x in X, return the index of the leaf x ends up in. Leaves are numbered within [0; self.tree_.node_count), possibly with gaps in the numbering.

**decision_path** *(X, check_input=True)*

Return the decision path in the tree

New in version 0.18.

**Parameters**
- **X** : array_like or sparse matrix, shape = [n_samples, n_features]
  
The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

- **check_input** : boolean, (default=True)

  Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**
- **indicator** : sparse csr array, shape = [n_samples, n_nodes]

  Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.
**feature_importances_**

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

Returns feature_importances_ : array, shape = [n_features]

**fit** (X, y, sample_weight=None, check_input=True, X_idx_sorted=None)

Build a decision tree classifier from the training set (X, y).

Parameters X : array-like or sparse matrix, shape = [n_samples, n_features]

The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc_matrix.

y : array-like, shape = [n_samples] or [n_samples, n_outputs]

The target values (class labels) as integers or strings.

sample_weight : array-like, shape = [n_samples] or None

Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node. Splits are also ignored if they would result in any single class carrying a negative weight in either child node.

check_input : boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

X_idx_sorted : array-like, shape = [n_samples, n_features], optional

The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don’t use this parameter unless you know what to do.

Returns self : object

Returns self.

**get_params** (deep=True)

Get parameters for this estimator.

Parameters deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any

Parameter names mapped to their values.

**predict** (X, check_input=True)

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

Parameters X : array-like or sparse matrix of shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

check_input : boolean, (default=True)
Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**

- **y**: array of shape = [n_samples] or [n_samples, n_outputs]
  - The predicted classes, or the predict values.

**predict_log_proba** *(X)*

Predict class log-probabilities of the input samples X.

**Parameters**

- **X**: array-like or sparse matrix of shape = [n_samples, n_features]
  - The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**Returns**

- **p**: array of shape = [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1. The class log-probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**predict_proba** *(X, check_input=True)*

Predict class probabilities of the input samples X.

The predicted class probability is the fraction of samples of the same class in a leaf.

**check_input** [boolean, (default=True)] Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Parameters**

- **X**: array-like or sparse matrix of shape = [n_samples, n_features]
  - The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

- **check_input**: bool
  - Run check_array on X.

**Returns**

- **p**: array of shape = [n_samples, n_classes], or a list of n_outputs such arrays if n_outputs > 1. The class probabilities of the input samples. The order of the classes corresponds to that in the attribute classes_.

**score** *(X, y, sample_weight=None)*

Returns the mean accuracy on the given test data and labels.

In multi-label classification, this is the subset accuracy which is a harsh metric since you require for each sample that each label set be correctly predicted.

**Parameters**

- **X**: array-like, shape = (n_samples, n_features)
  - Test samples.
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
  - True labels for X.
- **sample_weight**: array-like, shape = [n_samples], optional
  - Sample weights.

**Returns**

- **score**: float
  - Mean accuracy of self.predict(X) wrt. y.
**set_params**(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

### 30.34.4 sklearn.tree.ExtraTreeRegressor

class sklearn.tree.ExtraTreeRegressor(**criterion='mse', splitter='random', max_depth=None, min_samples_split=2, min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto', random_state=None, min_impurity_decrease=0.0, min_impurity_split=None, max_leaf_nodes=None)

An extremely randomized tree regressor.

Extra-trees differ from classic decision trees in the way they are built. When looking for the best split to separate the samples of a node into two groups, random splits are drawn for each of the `max_features` randomly selected features and the best split among those is chosen. When `max_features` is set 1, this amounts to building a totally random decision tree.

Warning: Extra-trees should only be used within ensemble methods.

Read more in the User Guide.

**Parameters**

criterion : string, optional (default=”mse”)

The function to measure the quality of a split. Supported criteria are “mse” for the mean squared error, which is equal to variance reduction as feature selection criterion, and “mae” for the mean absolute error.

New in version 0.18: Mean Absolute Error (MAE) criterion.

splitter : string, optional (default=”best”)

The strategy used to choose the split at each node. Supported strategies are “best” to choose the best split and “random” to choose the best random split.

max_depth : int or None, optional (default=None)

The maximum depth of the tree. If None, then nodes are expanded until all leaves are pure or until all leaves contain less than `min_samples_split` samples.

min_samples_split : int, float, optional (default=2)

The minimum number of samples required to split an internal node:

- If int, then consider `min_samples_split` as the minimum number.
- If float, then `min_samples_split` is a percentage and `ceil(min_samples_split * n_samples)` are the minimum number of samples for each split.

Changed in version 0.18: Added float values for percentages.

min_samples_leaf : int, float, optional (default=1)

The minimum number of samples required to be at a leaf node:

- If int, then consider `min_samples_leaf` as the minimum number.
- If float, then `min_samples_leaf` is a percentage and `ceil(min_samples_leaf * n_samples)` are the minimum number of samples for each node.
min_weight_fraction_leaf : float, optional (default=0.)

The minimum weighted fraction of the sum total of weights (of all the input samples) required to be at a leaf node. Samples have equal weight when sample_weight is not provided.

max_features : int, float, string or None, optional (default=None)

The number of features to consider when looking for the best split:
- If int, then consider max_features features at each split.
- If float, then max_features is a percentage and \( \text{int}(\text{max_features} \times \text{n_features}) \) features are considered at each split.
- If “auto”, then max_features=n_features.
- If “sqrt”, then max_features=sqrt(n_features).
- If “log2”, then max_features=log2(n_features).
- If None, then max_features=n_features.

Note: the search for a split does not stop until at least one valid partition of the node samples is found, even if it requires to effectively inspect more than max_features features.

random_state : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

min_impurity_decrease : float, optional (default=0.)

A node will be split if this split induces a decrease of the impurity greater than or equal to this value.

The weighted impurity decrease equation is the following:

\[
\frac{N_n}{N} \left( \text{impurity} - \frac{N_n \times \text{right_impurity}}{N_n} - \frac{N_n \times \text{left_impurity}}{N_n} \right)
\]

where \( N \) is the total number of samples, \( N_n \) is the number of samples at the current node, \( N_n \times \text{left_impurity} \) is the number of samples in the left child, and \( N_n \times \text{right_impurity} \) is the number of samples in the right child.

\( N, N_n, N_n \times \text{left_impurity} \) and \( N_n \times \text{right_impurity} \) all refer to the weighted sum, if sample_weight is passed.

New in version 0.19.

min_impurity_split : float,

Threshold for early stopping in tree growth. A node will split if its impurity is above the threshold, otherwise it is a leaf.

Deprecated since version 0.19: min_impurity_split has been deprecated in favor of min_impurity_decrease in 0.19 and will be removed in 0.21. Use min_impurity_decrease instead.

max_leaf_nodes : int or None, optional (default=None)
Grow a tree with `max_leaf_nodes` in best-first fashion. Best nodes are defined as relative reduction in impurity. If None then unlimited number of leaf nodes.

**Attributes**

- `feature_importances_` Return the feature importances.

**See also:**

`ExtraTreeClassifier`, `ExtraTreesClassifier`, `ExtraTreesRegressor`

**Notes**

The default values for the parameters controlling the size of the trees (e.g. `max_depth`, `min_samples_leaf`, etc.) lead to fully grown and unpruned trees which can potentially be very large on some data sets. To reduce memory consumption, the complexity and size of the trees should be controlled by setting those parameter values.

**References**

[R591591]

**Methods**

- `apply(X[, check_input])` Returns the index of the leaf that each sample is predicted as.
- `decision_path(X[, check_input])` Return the decision path in the tree
- `fit(X, y[, sample_weight, check_input, ...])` Build a decision tree regressor from the training set (X, y).
- `get_params([deep])` Get parameters for this estimator.
- `predict(X[, check_input])` Predict class or regression value for X.
- `score(X, y[, sample_weight])` Returns the coefficient of determination $R^2$ of the prediction.
- `set_params(**params)` Set the parameters of this estimator.

```python
__init__(criterion='mse', splitter='random', max_depth=None, min_samples_split=2,
         min_samples_leaf=1, min_weight_fraction_leaf=0.0, max_features='auto',
         random_state=None, min_impurity_decrease=0.0, min_impurity_split=None,
         max_leaf_nodes=None)
```

- `apply(X, check_input=True)` Returns the index of the leaf that each sample is predicted as.

New in version 0.17.

**Parameters**

- `X` : array_like or sparse matrix, shape = [n_samples, n_features]

  The input samples. Internally, it will be converted to `dtype=np.float32` and if a sparse matrix is provided to a sparse `csr_matrix`.

- `check_input` : boolean, (default=True)
Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**

**X_leaves**: array_like, shape = [n_samples,]

For each datapoint x in X, return the index of the leaf x ends up in. Leaves are numbered within [0; self.tree_.node_count), possibly with gaps in the numbering.

**decision_path** *(X, check_input=True)*

Return the decision path in the tree

New in version 0.18.

**Parameters**

**X**: array_like or sparse matrix, shape = [n_samples, n_features]

The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.

**check_input**: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**Returns**

**indicator**: sparse csr array, shape = [n_samples, n_nodes]

Return a node indicator matrix where non zero elements indicates that the samples goes through the nodes.

**feature_importances_**

Return the feature importances.

The importance of a feature is computed as the (normalized) total reduction of the criterion brought by that feature. It is also known as the Gini importance.

**Returns**

**feature_importances_**: array, shape = [n_features]

**fit** *(X, y, sample_weight=None, check_input=True, X_idx_sorted=None)*

Build a decision tree regressor from the training set (X, y).

**Parameters**

**X**: array-like or sparse matrix, shape = [n_samples, n_features]

The training input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csc_matrix.

**y**: array-like, shape = [n_samples] or [n_samples, n_outputs]

The target values (real numbers). Use dtype=np.float64 and order='C' for maximum efficiency.

**sample_weight**: array-like, shape = [n_samples] or None

Sample weights. If None, then samples are equally weighted. Splits that would create child nodes with net zero or negative weight are ignored while searching for a split in each node.

**check_input**: boolean, (default=True)

Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

**X_idx_sorted**: array-like, shape = [n_samples, n_features], optional

The indexes of the sorted training input samples. If many tree are grown on the same dataset, this allows the ordering to be cached between trees. If None, the data will be sorted here. Don’t use this parameter unless you know what to do.
**get_params**(deep=True)

Get parameters for this estimator.

- **Parameters**
  - **deep**: boolean, optional
    - If True, will return the parameters for this estimator and contained subobjects that are estimators.

- **Returns**
  - **params**: mapping of string to any
    - Parameter names mapped to their values.

**predict**(X, check_input=True)

Predict class or regression value for X.

For a classification model, the predicted class for each sample in X is returned. For a regression model, the predicted value based on X is returned.

- **Parameters**
  - **X**: array-like or sparse matrix of shape = [n_samples, n_features]
    - The input samples. Internally, it will be converted to dtype=np.float32 and if a sparse matrix is provided to a sparse csr_matrix.
  - **check_input**: boolean, (default=True)
    - Allow to bypass several input checking. Don’t use this parameter unless you know what you do.

- **Returns**
  - **y**: array of shape = [n_samples] or [n_samples, n_outputs]
    - The predicted classes, or the predict values.

**score**(X, y, sample_weight=None)

Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $((y_{true} - y_{pred})**2).sum()$ and $v$ is the total sum of squares $((y_{true} - y_{true}.mean())**2).sum()$. The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of y, disregarding the input features, would get a $R^2$ score of 0.0.

- **Parameters**
  - **X**: array-like, shape = (n_samples, n_features)
    - Test samples.
  - **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)
    - True values for X.
  - **sample_weight**: array-like, shape = [n_samples], optional
    - Sample weights.

- **Returns**
  - **score**: float
    - $R^2$ of self.predict(X) wrt. y.

**set_params**(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>_<parameter>` so that it’s possible to update each component of a nested object.
Returns

```
tree.export_graphviz(decision_tree[, ....])
```

Export a decision tree in DOT format.

### 30.34.5 sklearn.tree.export_graphviz

The function `sklearn.tree.export_graphviz` exports a decision tree in DOT format.

This function generates a GraphViz representation of the decision tree, which is then written into `out_file`. Once exported, graphical renderings can be generated using, for example:

```
$ dot -Tps tree.dot -o tree.ps  (PostScript format)
$ dot -Tpng tree.dot -o tree.png  (PNG format)
```

The sample counts that are shown are weighted with any `sample_weight` that might be present.

Read more in the User Guide.

**Parameters**

- `decision_tree`: decision tree regressor or classifier
  - The decision tree to be exported to GraphViz.

- `out_file`: file object or string, optional (default='tree.dot')
  - Handle or name of the output file. If `None`, the result is returned as a string. This will be the default from version 0.20.

- `max_depth`: int, optional (default=None)
  - The maximum depth of the representation. If `None`, the tree is fully generated.

- `feature_names`: list of strings, optional (default=None)
  - Names of each of the features.

- `class_names`: list of strings, bool or None, optional (default=None)
  - Names of each of the target classes in ascending numerical order. Only relevant for classification and not supported for multi-output. If `True`, shows a symbolic representation of the class name.

- `label`: {'all', 'root', 'none'}, optional (default='all')
  - Whether to show informative labels for impurity, etc. Options include ‘all’ to show at every node, ‘root’ to show only at the top root node, or ‘none’ to not show at any node.

- `filled`: bool, optional (default=False)
  - When set to `True`, paint nodes to indicate majority class for classification, extremity of values for regression, or purity of node for multi-output.

- `leaves_parallel`: bool, optional (default=False)
  - When set to `True`, draw all leaf nodes at the bottom of the tree.

- `impurity`: bool, optional (default=True)
  - When set to `True`, show the impurity at each node.
node_ids : bool, optional (default=False)

  When set to True, show the ID number on each node.

proportion : bool, optional (default=False)

  When set to True, change the display of ‘values’ and/or ‘samples’ to be proportions and percentages respectively.

rotate : bool, optional (default=False)

  When set to True, orient tree left to right rather than top-down.

rounded : bool, optional (default=False)

  When set to True, draw node boxes with rounded corners and use Helvetica fonts instead of Times-Roman.

special_characters : bool, optional (default=False)

  When set to False, ignore special characters for PostScript compatibility.

precision : int, optional (default=3)

  Number of digits of precision for floating point in the values of impurity, threshold and value attributes of each node.

Returns  dot_data : string

  String representation of the input tree in GraphViz dot format. Only returned if out_file is None.

  New in version 0.18.

Examples

```python
>>> from sklearn.datasets import load_iris
>>> from sklearn import tree

>>> clf = tree.DecisionTreeClassifier()
>>> iris = load_iris()

>>> clf = clf.fit(iris.data, iris.target)

...  tree.export_graphviz(clf, out_file='tree.dot')
```

30.35 sklearn.utils: Utilities

The sklearn.utils module includes various utilities.

Developer guide: See the Utilities for Developers page for further details.

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### 30.35.1 sklearn.utils.as_float_array

`sklearn.utils.as_float_array(X, copy=True, force_all_finite=True)`

Converts an array-like to an array of floats.

The new dtype will be np.float32 or np.float64, depending on the original type. The function can create a copy or modify the argument depending on the argument copy.

**Parameters**

- **X**: array-like, sparse matrix
- **copy**: bool, optional
  - If True, a copy of X will be created. If False, a copy may still be returned if X’s dtype is not a floating point type.
- **force_all_finite**: boolean (default=True)
  - Whether to raise an error on np.inf and np.nan in X.

**Returns**

- **XT**: array, sparse matrix
An array of type np.float

### 30.35.2 sklearn.utils.assert_all_finite

```
assert_all_finite(X)
```

Throw a ValueError if X contains NaN or infinity.

**Parameters**
- **X**: array or sparse matrix

### 30.35.3 sklearn.utils.check_X_y

```
check_X_y(X, y, accept_sparse=False, dtype='numeric', order=None,
          copy=False, force_all_finite=True, ensure_2d=True, allow_nd=False,
          multi_output=False, ensure_min_samples=1, ensure_min_features=1,
          y_numeric=False, warn_on_dtype=False, estimator=None)
```

Input validation for standard estimators.

Checks X and y for consistent length, enforces X 2d and y 1d. Standard input checks are only applied to y, such as checking that y does not have np.nan or np.inf targets. For multi-label y, set multi_output=True to allow 2d and sparse y. If the dttype of X is object, attempt converting to float, raising on failure.

**Parameters**
- **X**: nd-array, list or sparse matrix
  - Input data.
- **y**: nd-array, list or sparse matrix
  - Labels.
- **accept_sparse**: string, boolean or list of string (default=False)
  - String[s] representing allowed sparse matrix formats, such as ‘csc’, ‘csr’, etc. If the input is sparse but not in the allowed format, it will be converted to the first listed format. True allows the input to be any format. False means that a sparse matrix input will raise an error.
  - Deprecation: Passing ‘None’ to parameter accept_sparse in methods is deprecated in version 0.19 “and will be removed in 0.21. Use accept_sparse=False instead.
- **dtype**: string, type, list of types or None (default=’numeric’)
  - Data type of result. If None, the dttype of the input is preserved. If “numeric”, dtype is preserved unless array.dtype is object. If dtype is a list of types, conversion on the first type is only performed if the dttype of the input is not in the list.
- **order**: ‘F’, ‘C’ or None (default=None)
  - Whether an array will be forced to be fortran or c-style.
- **copy**: boolean (default=False)
  - Whether a forced copy will be triggered. If copy=False, a copy might be triggered by a conversion.
- **force_all_finite**: boolean (default=True)
  - Whether to raise an error on np.inf and np.nan in X. This parameter does not influence whether y can have np.inf or np.nan values.
- **ensure_2d**: boolean (default=True)
Whether to make X at least 2d.

**allow_nd** : boolean (default=False)

Whether to allow X.ndim > 2.

**multi_output** : boolean (default=False)

Whether to allow 2-d y (array or sparse matrix). If false, y will be validated as a vector. y cannot have np.nan or np.inf values if multi_output=True.

**ensure_min_samples** : int (default=1)

Make sure that X has a minimum number of samples in its first axis (rows for a 2D array).

**ensure_min_features** : int (default=1)

Make sure that the 2D array has some minimum number of features (columns). The default value of 1 rejects empty datasets. This check is only enforced when X has effectively 2 dimensions or is originally 1D and ensure_2d is True. Setting to 0 disables this check.

**y_numeric** : boolean (default=False)

Whether to ensure that y has a numeric type. If dtype of y is object, it is converted to float64. Should only be used for regression algorithms.

**warn_on_dtype** : boolean (default=False)

Raise DataConversionWarning if the dtype of the input data structure does not match the requested dtype, causing a memory copy.

**estimator** : str or estimator instance (default=None)

If passed, include the name of the estimator in warning messages.

**Returns**

**X_converted** : object

The converted and validated X.

**y_converted** : object

The converted and validated y.

### 30.35.4 sklearn.utils.check_array

**sklearn.utils.check_array** *(array, accept_sparse=False, dtype='numeric', order=None, copy=False, force_all_finite=True, ensure_2d=True, allow_nd=False, ensure_min_samples=1, ensure_min_features=1, warn_on_dtype=False, estimator=None)*

Input validation on an array, list, sparse matrix or similar.

By default, the input is converted to an at least 2D numpy array. If the dtype of the array is object, attempt converting to float, raising on failure.

**Parameters**

**array** : object

Input object to check / convert.

**accept_sparse** : string, boolean or list/tuple of strings (default=False)

String[s] representing allowed sparse matrix formats, such as ‘csc’, ‘csr’, etc. If the input is sparse but not in the allowed format, it will be converted to the first listed...
format. True allows the input to be any format. False means that a sparse matrix input will raise an error.

Deprecation since version 0.19: Passing ‘None’ to parameter accept_sparse in methods is deprecated in version 0.19 “and will be removed in 0.21. Use accept_sparse=False instead.

**dtype**: string, type, list of types or None (default=’numeric’)

Data type of result. If None, the dtype of the input is preserved. If “numeric”, dtype is preserved unless array.dtype is object. If dtype is a list of types, conversion on the first type is only performed if the dtype of the input is not in the list.

**order**: ‘F’, ‘C’ or None (default=None)

Whether an array will be forced to be fortran or c-style. When order is None (default), then if copy=False, nothing is ensured about the memory layout of the output array; otherwise (copy=True) the memory layout of the returned array is kept as close as possible to the original array.

**copy**: boolean (default=False)

Whether a forced copy will be triggered. If copy=False, a copy might be triggered by a conversion.

**force_all_finite**: boolean (default=True)

Whether to raise an error on np.inf and np.nan in X.

**ensure_2d**: boolean (default=True)

Whether to raise a value error if X is not 2d.

**allow_nd**: boolean (default=False)

Whether to allow X.ndim > 2.

**ensure_min_samples**: int (default=1)

Make sure that the array has a minimum number of samples in its first axis (rows for a 2D array). Setting to 0 disables this check.

**ensure_min_features**: int (default=1)

Make sure that the 2D array has some minimum number of features (columns). The default value of 1 rejects empty datasets. This check is only enforced when the input data has effectively 2 dimensions or is originally 1D and ensure_2d is True. Setting to 0 disables this check.

**warn_on_dtype**: boolean (default=False)

Raise DataConversionWarning if the dtype of the input data structure does not match the requested dtype, causing a memory copy.

**estimator**: str or estimator instance (default=None)

If passed, include the name of the estimator in warning messages.

Returns **X_converted**: object

The converted and validated X.
30.35.5 sklearn.utils.check_consistent_length

sklearn.utils.check_consistent_length (*arrays)
Check that all arrays have consistent first dimensions.
Checks whether all objects in arrays have the same shape or length.

Parameters *arrays : list or tuple of input objects.
Objects that will be checked for consistent length.

30.35.6 sklearn.utils.check_random_state

sklearn.utils.check_random_state (seed)
Turn seed into a np.random.RandomState instance

Parameters seed : None | int | instance of RandomState
    If seed is None, return the RandomState singleton used by np.random. If seed is an int,
    return a new RandomState instance seeded with seed. If seed is already a RandomState
    instance, return it. Otherwise raise ValueError.

Examples using sklearn.utils.check_random_state

• Isotonic Regression
• Face completion with a multi-output estimators
• Empirical evaluation of the impact of k-means initialization
• MNIST classification using multinomial logistic + L1
• Manifold Learning methods on a severed sphere
• Scaling the regularization parameter for SVCs

30.35.7 sklearn.utils.class_weight.compute_class_weight

sklearn.utils.class_weight.compute_class_weight (class_weight, classes, y)
Estimate class weights for unbalanced datasets.

Parameters class_weight : dict, ‘balanced’ or None
    If ‘balanced’, class weights will be given by n_samples / (n_classes * np.
    bincount(y)). If a dictionary is given, keys are classes and values are correspond-
    ing class weights. If None is given, the class weights will be uniform.

classes : ndarray
    Array of the classes occurring in the data, as given by np.unique(y_org) with
    y_org the original class labels.

y : array-like, shape (n_samples,)
    Array of original class labels per sample;

Returns class_weight_vect : ndarray, shape (n_classes,)
    Array with class_weight_vect[i] the weight for i-th class
30.35.8 sklearn.utils.class_weight.compute_sample_weight

sklearn.utils.class_weight.compute_sample_weight(class_weight, y, indices=None)

Estimate sample weights by class for unbalanced datasets.

Parameters:
- class_weight : dict, list of dicts, “balanced”, or None, optional
  Weights associated with classes in the form `class_label: weight`. If not
given, all classes are supposed to have weight one. For multi-output problems, a list of
dicts can be provided in the same order as the columns of `y`.

  Note that for multioutput (including multilabel) weights should be defined for each class
  of every column in its own dict. For example, for four-class multilabel classification
  weights should be `[0: 1, 1: 1], [0: 1, 1: 5], [0: 1, 1: 1], [0: 1, 1: 1]]` instead of
  `[1:1], [2:5], [3:1], [4:1]`.

  The “balanced” mode uses the values of `y` to automatically adjust weights inversely
  proportional to class frequencies in the input data: `n_samples / (n_classes * np.bincount(y))`.

  For multi-output, the weights of each column of `y` will be multiplied.

- y : array-like, shape = [n_samples] or [n_samples, n_outputs]
  Array of original class labels per sample.

- indices : array-like, shape (n_subsample,), or None
  Array of indices to be used in a subsample. Can be of length less than n_samples in the
  case of a subsample, or equal to n_samples in the case of a bootstrap subsample with
  repeated indices. If None, the sample weight will be calculated over the full sample.
  Only “balanced” is supported for `class_weight` if this is provided.

Returns:
- sample_weight_vect : ndarray, shape (n_samples,)
  Array with sample weights as applied to the original `y`.

30.35.9 sklearn.utils.estimator_checks.check_estimator

sklearn.utils.estimator_checks.check_estimator(Estimator)

Check if estimator adheres to scikit-learn conventions.

This estimator will run an extensive test-suite for input validation, shapes, etc. Additional tests for classifiers,
regressors, clustering or transformers will be run if the Estimator class inherits from the corresponding mixin
from sklearn.base.

This test can be applied to classes or instances. Classes currently have some additional tests that related to
construction, while passing instances allows the testing of multiple options.

Parameters:
- estimator : estimator object or class
  Estimator to check. Estimator is a class object or instance.
30.35.10 sklearn.utils.extmath.safe_sparse_dot

`sklearn.utils.extmath.safe_sparse_dot(a, b, dense_output=False)`

Dot product that handle the sparse matrix case correctly

Uses BLAS GEMM as replacement for numpy.dot where possible to avoid unnecessary copies.

**Parameters**
- `a`: array or sparse matrix
- `b`: array or sparse matrix
- `dense_output`: boolean, default False

When False, either `a` or `b` being sparse will yield sparse output. When True, output will always be an array.

**Returns**
- `dot_product`: array or sparse matrix
  - sparse if `a` or `b` is sparse and `dense_output=False`.

30.35.11 sklearn.utils.indexable

`sklearn.utils.indexable(*iterables)`

Make arrays indexable for cross-validation.

Checks consistent length, passes through None, and ensures that everything can be indexed by converting sparse matrices to csr and converting non-interable objects to arrays.

**Parameters**
- `*iterables`: lists, dataframes, arrays, sparse matrices

List of objects to ensure sliceability.

30.35.12 sklearn.utils.resample

`sklearn.utils.resample(*arrays, **options)`

Resample arrays or sparse matrices in a consistent way

The default strategy implements one step of the bootstrapping procedure.

**Parameters**
- `*arrays`: sequence of indexable data-structures
  - Indexable data-structures can be arrays, lists, dataframes or scipy sparse matrices with consistent first dimension.
- `replace`: boolean, True by default
  - Implements resampling with replacement. If False, this will implement (sliced) random permutations.
- `n_samples`: int, None by default
  - Number of samples to generate. If left to None this is automatically set to the first dimension of the arrays. If replace is False it should not be larger than the length of arrays.
- `random_state`: int, RandomState instance or None, optional (default=None)
  - The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

---

30.35. sklearn.utils: Utilities
Returns **resampled_arrays** : sequence of indexable data-structures

Sequence of resampled views of the collections. The original arrays are not impacted.

See also:

`sckearn.utils.shuffle`

**Examples**

It is possible to mix sparse and dense arrays in the same run:

```python
>>> X = np.array([[1., 0.], [2., 1.], [0., 0.]])
>>> y = np.array([0, 1, 2])

>>> from scipy.sparse import coo_matrix
>>> X_sparse = coo_matrix(X)

>>> from sklearn.utils import resample

>>> X, X_sparse, y = resample(X, X_sparse, y, random_state=0)

>>> X
array([[ 1., 0.],
       [ 2., 1.],
       [ 1., 0.]])

>>> X_sparse
<3x2 sparse matrix of type '<... 'numpy.float64'>'
   with 4 stored elements in Compressed Sparse Row format>

>>> X_sparse.toarray()
array([[ 1., 0.],
       [ 2., 1.],
       [ 1., 0.]])

>>> y
array([0, 1, 0])

>>> resample(y, n_samples=2, random_state=0)
array([0, 1])
```

### 30.35.13 sklearn.utils.safe_indexing

**sklearn.utils.safe_indexing** *(X, indices)*

Return items or rows from X using indices.

Allows simple indexing of lists or arrays.

**Parameters**

  Data from which to sample rows or items.

- **indices** : array-like of int
  Indices according to which X will be subsampled.

**Returns**

- **subset**
  Subset of X on first axis
Notes

CSR, CSC, and LIL sparse matrices are supported. COO sparse matrices are not supported.

30.35.14 sklearn.utils.shuffle

**sklearn.utils.shuffle(**arrays, **options**)

Shuffle arrays or sparse matrices in a consistent way

This is a convenience alias to resample(*arrays, replace=False) to do random permutations of the collections.

Parameters

- **arrays**: sequence of indexable data-structures
  
  Indexable data-structures can be arrays, lists, dataframes or scipy sparse matrices with consistent first dimension.

- **random_state**: int, RandomState instance or None, optional (default=None)
  
  The seed of the pseudo random number generator to use when shuffling the data. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

- **n_samples**: int, None by default
  
  Number of samples to generate. If left to None this is automatically set to the first dimension of the arrays.

Returns

- **shuffled_arrays**: sequence of indexable data-structures
  
  Sequence of shuffled views of the collections. The original arrays are not impacted.

See also:

sklearn.utils.resample

Examples

It is possible to mix sparse and dense arrays in the same run:

```python
>>> X = np.array([[1., 0.], [2., 1.], [0., 0.]])
>>> y = np.array([0, 1, 2])

>>> from scipy.sparse import coo_matrix
>>> X_sparse = coo_matrix(X)

>>> from sklearn.utils import shuffle

>>> X, X_sparse, y = shuffle(X, X_sparse, y, random_state=0)

>>> X
array([[ 0., 0.],
       [ 2., 1.],
       [ 1., 0.]])

>>> X_sparse
<3x2 sparse matrix of type '<... 'numpy.float64'>'
  with 3 stored elements in Compressed Sparse Row format>

>>> X_sparse.toarray()
```
array([[ 0.,  0.],
       [ 2.,  1.],
       [ 1.,  0.]])

```python
>>> y
array([2, 1, 0])

>>> shuffle(y, n_samples=2, random_state=0)
array([0, 1])
```

Examples using `sklearn.utils.shuffle`

- Model Complexity Influence
- Prediction Latency
- Color Quantization using K-Means
- Empirical evaluation of the impact of k-means initialization
- Gradient Boosting regression

### 30.35.15 sklearn.utils.sparsefuncs.incr_mean_variance_axis

`sklearn.utils.sparsefuncs.incr_mean_variance_axis(X, axis, last_mean, last_var, last_n)`

Compute incremental mean and variance along an axis on a CSR or CSC matrix.

last_mean, last_var are the statistics computed at the last step by this function. Both must be initialized to 0-arrays of the proper size, i.e. the number of features in X. last_n is the number of samples encountered until now.

**Parameters**

- **X**: CSR or CSC sparse matrix, shape (n_samples, n_features)
- **axis**: int (either 0 or 1)
- **last_mean**: float array with shape (n_features,)
- **last_var**: float array with shape (n_features,)
- **last_n**: int

**Returns**

- **means**: float array with shape (n_features,)
- **variances**: float array with shape (n_features,)
- **n**: int

Updated feature-wise means.
Updated feature-wise variances.
Updated number of seen samples.
30.35.16 sklearn.utils.sparsefuncs.inplace_column_scale

sklearn.utils.sparsefuncs.inplace_column_scale(X, scale)

Inplace column scaling of a CSC/CSR matrix.

Scale each feature of the data matrix by multiplying with specific scale provided by the caller assuming a (n_samples, n_features) shape.

Parameters X : CSC or CSR matrix with shape (n_samples, n_features)

Matrix to normalize using the variance of the features.

scale : float array with shape (n_features,)

Array of precomputed feature-wise values to use for scaling.

30.35.17 sklearn.utils.sparsefuncs.inplace_row_scale

sklearn.utils.sparsefuncs.inplace_row_scale(X, scale)

Inplace row scaling of a CSR or CSC matrix.

Scale each row of the data matrix by multiplying with specific scale provided by the caller assuming a (n_samples, n_features) shape.

Parameters X : CSR or CSC sparse matrix, shape (n_samples, n_features)

Matrix to be scaled.

scale : float array with shape (n_features,)

Array of precomputed sample-wise values to use for scaling.

30.35.18 sklearn.utils.sparsefuncs.inplace_swap_row

sklearn.utils.sparsefuncs.inplace_swap_row(X, m, n)

Swaps two rows of a CSC/CSR matrix in-place.

Parameters X : CSR or CSC sparse matrix, shape=(n_samples, n_features)

Matrix whose two rows are to be swapped.

m : int

Index of the row of X to be swapped.

n : int

Index of the row of X to be swapped.

30.35.19 sklearn.utils.sparsefuncs.inplace_swap_column

sklearn.utils.sparsefuncs.inplace_swap_column(X, m, n)

Swaps two columns of a CSC/CSR matrix in-place.

Parameters X : CSR or CSC sparse matrix, shape=(n_samples, n_features)

Matrix whose two columns are to be swapped.

m : int

Index of the column of X to be swapped.
n : int

Index of the column of X to be swapped.

30.35.20 sklearn.utils.sparsefuncs.mean_variance_axis

sklearn.utils.sparsefuncs.mean_variance_axis(X, axis)

Compute mean and variance along an axis on a CSR or CSC matrix

Parameters X : CSR or CSC sparse matrix, shape (n_samples, n_features)

Input data.

axis : int (either 0 or 1)

Axis along which the axis should be computed.

Returns means : float array with shape (n_features,)

Feature-wise means

variances : float array with shape (n_features,)

Feature-wise variances

30.35.21 sklearn.utils.validation.check_is_fitted

sklearn.utils.validation.check_is_fitted(estimator, attributes, msg=None, all_or_any=<built-in function all>)

Perform is_fitted validation for estimator.

Checks if the estimator is fitted by verifying the presence of “all_or_any” of the passed attributes and raises a
NotFittedError with the given message.

Parameters estimator : estimator instance.

estimator instance for which the check is performed.

attributes : attribute name(s) given as string or a list/tuple of strings

Eg.: ["coef_", "estimator_", ...], "coef_"

msg : string

The default error message is, “This %(name)s instance is not fitted yet. Call ‘fit’ with
appropriate arguments before using this method.”

For custom messages if “%(name)s” is present in the message string, it is substituted
for the estimator name.

Eg. : “Estimator, %(name)s, must be fitted before sparsifying”.

all_or_any : callable, {all, any}, default all

Specify whether all or any of the given attributes must exist.

Returns None

Raises NotFittedError

If the attributes are not found.
30.35.22 sklearn.utils.validation.check_memory

`sklearn.utils.validation.check_memory(memory)`

Check that memory is joblib.Memory-like.

joblib.Memory-like means that memory can be converted into a sklearn.externals.joblib.Memory instance (typically a str denoting the cachedir) or has the same interface (has a cache method).

**Parameters**
- `memory`: None, str or object with the joblib.Memory interface

**Returns**
- `memory`: object with the joblib.Memory interface

**Raises**
- `ValueError` if `memory` is not joblib.Memory-like.

30.35.23 sklearn.utils.validation.check_symmetric

`sklearn.utils.validation.check_symmetric(array, tol=1e-10, raise_warning=True, raise_exception=False)`

Make sure that array is 2D, square and symmetric.

If the array is not symmetric, then a symmetrized version is returned. Optionally, a warning or exception is raised if the matrix is not symmetric.

**Parameters**
- `array`: nd-array or sparse matrix
- `tol`: float
  - Absolute tolerance for equivalence of arrays. Default = 1E-10.
- `raise_warning`: boolean (default=True)
  - If True then raise a warning if conversion is required.
- `raise_exception`: boolean (default=False)
  - If True then raise an exception if array is not symmetric.

**Returns**
- `array_sym`: ndarray or sparse matrix
  - Symmetrized version of the input array, i.e. the average of array and array.transpose().
  - If sparse, then duplicate entries are first summed and zeros are eliminated.

30.35.24 sklearn.utils.validation.column_or_1d

`sklearn.utils.validation.column_or_1d(y, warn=False)`

Ravel column or 1d numpy array, else raises an error

**Parameters**
- `y`: array-like
- `warn`: boolean, default False
  - To control display of warnings.

**Returns**
- `y`: array
30.35.25 sklearn.utils.validation.has_fit_parameter

sklearn.utils.validation.has_fit_parameter(estimator, parameter)
Checks whether the estimator’s fit method supports the given parameter.

Parameters estimator : object
An estimator to inspect.

parameter : str
The searched parameter.

Returns is_parameter : bool
Whether the parameter was found to be a named parameter of the estimator’s fit method.

Examples

```python
>>> from sklearn.svm import SVC
>>> has_fit_parameter(SVC(), "sample_weight")
True
```

30.36 Recently deprecated

30.36.1 To be removed in 0.21

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sklearn.linear_model.RandomizedLasso

Warning: DEPRECATED

class sklearn.linear_model.RandomizedLasso(*args, **kwargs)
Randomized Lasso.

Randomized Lasso works by subsampling the training data and computing a Lasso estimate where the penalty of a random subset of coefficients has been scaled. By performing this double randomization several times, the method assigns high scores to features that are repeatedly selected across randomizations. This is known as stability selection. In short, features selected more often are considered good features.

Parameters alpha : float, ‘aic’, or ‘bic’, optional
The regularization parameter alpha parameter in the Lasso. Warning: this is not the alpha parameter in the stability selection article which is scaling.

scaling : float, optional
The s parameter used to randomly scale the penalty of different features. Should be between 0 and 1.

**sample_fraction** : float, optional

The fraction of samples to be used in each randomized design. Should be between 0 and 1. If 1, all samples are used.

**n_resampling** : int, optional

Number of randomized models.

**selection_threshold** : float, optional

The score above which features should be selected.

**fit_intercept** : boolean, optional

Whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**verbose** : boolean or integer, optional

Sets the verbosity amount

**normalize** : boolean, optional, default True

If True, the regressors X will be normalized before regression. This parameter is ignored when fit_intercept is set to False. When the regressors are normalized, note that this makes the hyperparameters learned more robust and almost independent of the number of samples. The same property is not valid for standardized data. However, if you wish to standardize, please use preprocessing.StandardScaler before calling fit on an estimator with normalize=False.

**precompute** : True | False | ‘auto’ | array-like

Whether to use a precomputed Gram matrix to speed up calculations. If set to ‘auto’ let us decide. The Gram matrix can also be passed as argument, but it will be used only for the selection of parameter alpha, if alpha is ‘aic’ or ‘bic’.

**max_iter** : integer, optional

Maximum number of iterations to perform in the Lars algorithm.

**eps** : float, optional

The machine-precision regularization in the computation of the Cholesky diagonal factors. Increase this for very ill-conditioned systems. Unlike the ‘tol’ parameter in some iterative optimization-based algorithms, this parameter does not control the tolerance of the optimization.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**n_jobs** : integer, optional

Number of CPUs to use during the resampling. If ‘-1’, use all the CPUs

**pre_dispatch** : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
• None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
• An int, giving the exact number of total jobs that are spawned
• A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

memory : None, str or object with the joblib.Memory interface, optional (default=None)

Used for internal caching. By default, no caching is done. If a string is given, it is the path to the caching directory.

Attributes

| scores_ | (array, shape = [n_features]) Feature scores between 0 and 1. |
| all_scores_ | (array, shape = [n_features, n_reg_parameter]) Feature scores between 0 and 1 for all values of the regularization parameter. The reference article suggests scores_ is the max of all_scores_. |

See also:

RandomizedLogisticRegression, Lasso, ElasticNet

References


Examples

```python
>>> from sklearn.linear_model import RandomizedLasso
>>> randomized_lasso = RandomizedLasso()
```

Methods

| fit(X, y) | Fit the model using X, y as training data. |
| fit_transform(X[, y]) | Fit to data, then transform it. |
| get_params([deep]) | Get parameters for this estimator. |
| get_support([indices]) | Get a mask, or integer index, of the features selected |
| inverse_transform(X) | Reverse the transformation operation |
| set_params(**params) | Set the parameters of this estimator. |
| transform(X) | Reduce X to the selected features. |

```python
__init__(*args, **kwargs)
```

DEPRECATED: The class RandomizedLasso is deprecated in 0.19 and will be removed in 0.21.

```python
fit (X, y)
```

Fit the model using X, y as training data.

Parameters X : array-like, shape = [n_samples, n_features]
Training data.

\textbf{y} : array-like, shape = [n_samples]

Target values. Will be cast to X’s dtype if necessary

\textbf{Returns} \ self : object

Returns an instance of self.

\textbf{fit\_transform} (X, y=None, **\textit{fit\_params})

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

\textbf{Parameters} X : numpy array of shape [n_samples, n_features]

Training set.

y : numpy array of shape [n_samples]

Target values.

\textbf{Returns} X\_new : numpy array of shape [n_samples, n_features\_new]

Transformed array.

\textbf{get\_params} (\textit{deep}=True)

Get parameters for this estimator.

\textbf{Parameters} \ deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

\textbf{Returns} \ params : mapping of string to any

Parameter names mapped to their values.

\textbf{get\_support} (\textit{indices}=False)

Get a mask, or integer index, of the features selected

\textbf{Parameters} \ indices : boolean (default False)

If True, the return value will be an array of integers, rather than a boolean mask.

\textbf{Returns} \ support : array

An index that selects the retained features from a feature vector. If \textit{indices} is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If \textit{indices} is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

\textbf{inverse\_transform} (X)

Reverse the transformation operation

\textbf{Parameters} X : array of shape [n_samples, n\_selected\_features]

The input samples.

\textbf{Returns} X\_r : array of shape [n_samples, n\_original\_features]

X with columns of zeros inserted where features would have been removed by \textit{transform}.

\textbf{set\_params} (**\textit{params})

Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform** *(X)*
Reduce X to the selected features.

**Parameters**

`X` : array of shape [n_samples, n_features]
The input samples.

**Returns**

`X_r` : array of shape [n_samples, n_selected_features]
The input samples with only the selected features.

**sklearn.linear_model.RandomizedLogisticRegression**

**Warning:** DEPRECATED

```python
class sklearn.linear_model.RandomizedLogisticRegression(*args, **kwargs)

Randomized Logistic Regression

Randomized Logistic Regression works by subsampling the training data and fitting a L1-penalized LogisticRegression model where the penalty of a random subset of coefficients has been scaled. By performing this double randomization several times, the method assigns high scores to features that are repeatedly selected across randomizations. This is known as stability selection. In short, features selected more often are considered good features.

**Parameters**

`C` : float or array-like of shape [n_reg_parameter], optional, default=1

The regularization parameter C in the LogisticRegression. When C is an array, fit will take each regularization parameter in C one by one for LogisticRegression and store results for each one in all_scores_, where columns and rows represent corresponding reg_parameters and features.

`scaling` : float, optional, default=0.5

The s parameter used to randomly scale the penalty of different features. Should be between 0 and 1.

`sample_fraction` : float, optional, default=0.75

The fraction of samples to be used in each randomized design. Should be between 0 and 1. If 1, all samples are used.

`n_resampling` : int, optional, default=200

Number of randomized models.

`selection_threshold` : float, optional, default=0.25

The score above which features should be selected.

`tol` : float, optional, default=1e-3

tolerance for stopping criteria of LogisticRegression

`fit_intercept` : boolean, optional, default=True
```

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whether to calculate the intercept for this model. If set to false, no intercept will be used in calculations (e.g. data is expected to be already centered).

**verbose** : boolean or integer, optional

Sets the verbosity amount

**normalize** : boolean, optional, default True

If True, the regressors X will be normalized before regression. This parameter is ignored when `fit_intercept` is set to False. When the regressors are normalized, note that this makes the hyperparameters learnt more robust and almost independent of the number of samples. The same property is not valid for standardized data. However, if you wish to standardize, please use `preprocessing.StandardScaler` before calling `fit` on an estimator with `normalize=False`.

**random_state** : int, RandomState instance or None, optional (default=None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**n_jobs** : integer, optional

Number of CPUs to use during the resampling. If `-1`, use all the CPUs

**pre_dispatch** : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

- None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of `n_jobs`, as in `2*n_jobs`

**memory** : None, str or object with the joblib.Memory interface, optional (default=None)

Used for internal caching. By default, no caching is done. If a string is given, it is the path to the caching directory.

**Attributes**

| scores | (array, shape = [n_features]) Feature scores between 0 and 1. |
| all_scores | (array, shape = [n_features, n_reg_parameter]) Feature scores between 0 and 1 for all values of the regularization parameter. The reference article suggests `scores_` is the max of `all_scores_`. |

**See also:**

RandomizedLasso, LogisticRegression

**References**

Examples

```python
>>> from sklearn.linear_model import RandomizedLogisticRegression
>>> randomized_logistic = RandomizedLogisticRegression()
```

Methods

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</tr>
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<td><code>get_params([deep])</code></td>
<td>Get parameters for this estimator.</td>
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<td><code>get_support([indices])</code></td>
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<td><code>inverse_transform(X)</code></td>
<td>Reverse the transformation operation</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td><code>transform(X)</code></td>
<td>Reduce X to the selected features.</td>
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</tbody>
</table>

```python
__init__(*args, **kwargs)
```

DEPRECATED: The class RandomizedLogisticRegression is deprecated in 0.19 and will be removed in 0.21.

```python
fit (X, y)
```

Fit the model using X, y as training data.

**Parameters**

- **X**: array-like, shape = [n_samples, n_features]
  
  Training data.

- **y**: array-like, shape = [n_samples]
  
  Target values. Will be cast to X’s dtype if necessary

**Returns**

- **self**: object
  
  Returns an instance of self.

```python
fit_transform (X, y=None, **fit_params)
```

Fit to data, then transform it.

Fits transformer to X and y with optional parameters fit_params and returns a transformed version of X.

**Parameters**

- **X**: numpy array of shape [n_samples, n_features]
  
  Training set.

- **y**: numpy array of shape [n_samples]
  
  Target values.

**Returns**

- **X_new**: numpy array of shape [n_samples, n_features_new]
  
  Transformed array.

```python
get_params (deep=True)
```

Get parameters for this estimator.

**Parameters**

- **deep**: boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params**: mapping of string to any
Parameter names mapped to their values.

**get_support**(indices=False)

Get a mask, or integer index, of the features selected

**Parameters**

- **indices**: boolean (default False)
  
  If True, the return value will be an array of integers, rather than a boolean mask.

**Returns**

- **support**: array
  
  An index that selects the retained features from a feature vector. If `indices` is False, this is a boolean array of shape [# input features], in which an element is True iff its corresponding feature is selected for retention. If `indices` is True, this is an integer array of shape [# output features] whose values are indices into the input feature vector.

**inverse_transform**(X)

Reverse the transformation operation

**Parameters**

- **X**: array of shape [n_samples, n_selected_features]
  
  The input samples.

**Returns**

- **X_r**: array of shape [n_samples, n_original_features]
  
  X with columns of zeros inserted where features would have been removed by `transform`.

**set_params**(**params**)

Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns**

- **self**: 

**transform**(X)

Reduce X to the selected features.

**Parameters**

- **X**: array of shape [n_samples, n_features]
  
  The input samples.

**Returns**

- **X_r**: array of shape [n_samples, n_selected_features]
  
  The input samples with only the selected features.

**sklearn.neighbors.LSHForest**

**Warning**: DEPRECATED

**class** `sklearn.neighbors.LSHForest` *(n_estimators=10, radius=1.0, n_candidates=50, n_neighbors=5, min_hash_match=4, radius_cutoff_ratio=0.9, random_state=None)*

Performs approximate nearest neighbor search using LSH forest.

**LSH Forest**: Locality Sensitive Hashing forest [1] is an alternative method for vanilla approximate nearest neighbor search methods. LSH forest data structure has been implemented using sorted arrays and binary search and 32 bit fixed-length hashes. Random projection is used as the hash family which approximates cosine distance.
The cosine distance is defined as $1 - \text{cosine_similarity}$: the lowest value is 0 (identical point) but it is bounded above by 2 for the farthest points. Its value does not depend on the norm of the vector points but only on their relative angles.

**Parameters**

- **n_estimators**: int (default = 10)
  
  Number of trees in the LSH Forest.

- **radius**: float, optional (default = 1.0)
  
  Radius from the data point to its neighbors. This is the parameter space to use by default for the `radius_neighbors` queries.

- **n_candidates**: int (default = 50)
  
  Minimum number of candidates evaluated per estimator, assuming enough items meet the `min_hash_match` constraint.

- **n_neighbors**: int (default = 5)
  
  Number of neighbors to be returned from query function when it is not provided to the `kneighbors` method.

- **min_hash_match**: int (default = 4)
  
  Lowest hash length to be searched when candidate selection is performed for nearest neighbors.

- **radius_cutoff_ratio**: float, optional (default = 0.9)
  
  A value ranges from 0 to 1. Radius neighbors will be searched until the ratio between total neighbors within the radius and the total candidates becomes less than this value unless it is terminated by hash length reaching `min_hash_match`.

- **random_state**: int, RandomState instance or None, optional (default= None)
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**Attributes**

- **hash_functions**: (GaussianRandomProjectionHash objects) Hash function $g(p, x)$ for a tree is an array of 32 randomly generated float arrays with the same dimension as the data set. This array is stored in GaussianRandomProjectionHash object and can be obtained from `components_` attribute.

- **trees_**: (array, shape (n_estimators, n_samples)) Each tree (corresponding to a hash function) contains an array of sorted hashed values. The array representation may change in future versions.

- **original_indices_**: (array, shape (n_estimators, n_samples)) Original indices of sorted hashed values in the fitted index.

**References**

[R561561]
Examples

```python
>>> from sklearn.neighbors import LSHForest

>>> X_train = [[5, 5, 2], [21, 5, 5], [1, 1, 1], [8, 9, 1], [6, 10, 2]]
>>> X_test = [[9, 1, 6], [3, 1, 10], [7, 10, 3]]
>>> lshf = LSHForest(random_state=42)
>>> lshf.fit(X_train)
LSHForest(min_hash_match=4, n_candidates=50, n_estimators=10,
            n_neighbors=5, radius=1.0, radius_cutoff_ratio=0.9,
            random_state=42)
>>> distances, indices = lshf.kneighbors(X_test, n_neighbors=2)
>>> distances
array([[0.069..., 0.149...],
       [0.229..., 0.481...],
       [0.004..., 0.014...]])
>>> indices
array([[1, 2],
       [2, 0],
       [4, 0]])
```

Methods

```python
fit(X[, y])          Fit the LSH forest on the data.
get_params([deep])   Get parameters for this estimator.
kneighbors(X[, n_neighbors, return_distance]) Returns n_neighbors of approximate nearest neighbors.
kneighbors_graph([X, n_neighbors, mode]) Computes the (weighted) graph of k-Neighbors for points in X
partial_fit(X[, y]) Inserts new data into the already fitted LSH Forest.
radius_neighbors(X[, radius, return_distance]) Finds the neighbors within a given radius of a point or points.
radius_neighbors_graph([X, radius, mode]) Computes the (weighted) graph of Neighbors for points in X
set_params(**params) Set the parameters of this estimator.
```

```python
__init__(n_estimators=10, radius=1.0, n_candidates=50, n_neighbors=5, min_hash_match=4, radius_cutoff_ratio=0.9, random_state=None)

fit (X, y=None)
    Fit the LSH forest on the data.

    This creates binary hashes of input data points by getting the dot product of input points and hash_function then transforming the projection into a binary string array based on the sign (positive/negative) of the projection. A sorted array of binary hashes is created.

    Parameters X : array_like or sparse (CSR) matrix, shape (n_samples, n_features)

    List of n_features-dimensional data points. Each row corresponds to a single data point.

    Returns self : object

    Returns self.

get_params (deep=True)
    Get parameters for this estimator.
```
**Parameters** deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns** params : mapping of string to any

Parameter names mapped to their values.

**kneighbors** *(X, n_neighbors=None, return_distance=True)*

Returns n_neighbors of approximate nearest neighbors.

**Parameters** X : array_like or sparse (CSR) matrix, shape (n_samples, n_features)

List of n_features-dimensional data points. Each row corresponds to a single query.

n_neighbors : int, optional (default = None)

Number of neighbors required. If not provided, this will return the number specified at the initialization.

return_distance : boolean, optional (default = True)

Returns the distances of neighbors if set to True.

**Returns** dist : array, shape (n_samples, n_neighbors)

Array representing the cosine distances to each point, only present if return_distance=True.

ind : array, shape (n_samples, n_neighbors)

Indices of the approximate nearest points in the population matrix.

**kneighbors_graph** *(X=None, n_neighbors=None, mode='connectivity')*

Computes the (weighted) graph of k-Neighbors for points in X

**Parameters** X : array-like, shape (n_query, n_features), or (n_query, n_indexed) if metric == ‘precomputed’

The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

n_neighbors : int

Number of neighbors for each sample. (default is value passed to the constructor).

mode : {'connectivity', 'distance'}, optional

Type of returned matrix: ‘connectivity’ will return the connectivity matrix with ones and zeros, in ‘distance’ the edges are Euclidean distance between points.

**Returns** A : sparse matrix in CSR format, shape = [n_samples, n_samples_fit]

n_samples_fit is the number of samples in the fitted data A[i, j] is assigned the weight of edge that connects i to j.

See also:

*NearestNeighbors.radius_neighbors_graph*

**Examples**
```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(n_neighbors=2)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.kneighbors_graph(X)
>>> A.toarray()
array([[ 1., 0., 1.],
       [ 0., 1., 1.],
       [ 1., 0., 1.]])
```

**partial_fit** (*X*, *y=None*)

Inserts new data into the already fitted LSH Forest. Cost is proportional to new total size, so additions should be batched.

**Parameters**

**X** : array_like or sparse (CSR) matrix, shape (n_samples, n_features)

New data point to be inserted into the LSH Forest.

**radius_neighbors** (*X*, *radius=None*, *return_distance=True*)

Finds the neighbors within a given radius of a point or points.

Return the indices and distances of some points from the dataset lying in a ball with size radius around the points of the query array. Points lying on the boundary are included in the results.

The result points are not necessarily sorted by distance to their query point.

LSH Forest being an approximate method, some true neighbors from the indexed dataset might be missing from the results.

**Parameters**

**X** : array_like or sparse (CSR) matrix, shape (n_samples, n_features)

List of n_features-dimensional data points. Each row corresponds to a single query.

**radius** : float

Limiting distance of neighbors to return. (default is the value passed to the constructor).

**return_distance** : boolean, optional (default = False)

Returns the distances of neighbors if set to True.

**Returns**

**dist** : array, shape (n_samples,) of arrays

Each element is an array representing the cosine distances to some points found within radius of the respective query. Only present if return_distance=True.

**ind** : array, shape (n_samples,) of arrays

Each element is an array of indices for neighbors within radius of the respective query.

**radius_neighbors_graph** (*X=None*, *radius=None*, *mode='connectivity'*)

Computes the (weighted) graph of Neighbors for points in X

Neighborhoods are restricted the points at a distance lower than radius.

**Parameters**

**X** : array-like, shape = [n_samples, n_features], optional

The query point or points. If not provided, neighbors of each indexed point are returned. In this case, the query point is not considered its own neighbor.

**radius** : float

Radius of neighborhoods. (default is the value passed to the constructor).

30.36. Recently deprecated
mode : {'connectivity', 'distance'}, optional

Type of returned matrix: 'connectivity' will return the connectivity matrix with ones and zeros, in 'distance' the edges are Euclidean distance between points.

Returns A : sparse matrix in CSR format, shape = [n_samples, n_samples]

A[i, j] is assigned the weight of edge that connects i to j.

See also:

kneighbors_graph

Examples

```python
>>> X = [[0], [3], [1]]
>>> from sklearn.neighbors import NearestNeighbors
>>> neigh = NearestNeighbors(radius=1.5)
>>> neigh.fit(X)
NearestNeighbors(algorithm='auto', leaf_size=30, ...)
>>> A = neigh.radius_neighbors_graph(X)
>>> A.toarray()
array([[ 1., 0., 1.],
       [ 0., 1., 0.],
       [ 1., 0., 1.]])
```

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

Returns self

30.36.2 To be removed in 0.20

- `cross_validation.KFold(n[, n_folds, ...])` K-Folds cross validation iterator.
- `cross_validation.LabelKFold(labels[, n_folds])` K-fold iterator variant with non-overlapping labels.
- `cross_validation.LeaveOneLabelOut(labels)` Leave-One-Label_Out cross-validation iterator
- `cross_validation.LeaveOneOut(n)` Leave-One-Out cross validation iterator.
- `cross_validation.LeavePOut(n, p)` Leave-P-Out cross validation iterator
- `cross_validation.LeavePLabelOut(labels, p)` Leave-P-Label_Out cross-validation iterator
- `cross_validation.LabelShuffleSplit(labels[,...])` Shuffle-Labels-Out cross-validation iterator
- `cross_validation.ShuffleSplit(n[, n_iter,...])` Random permutation cross-validation iterator.
- `cross_validation.StratifiedKFold(y[,...])` Stratified K-Folds cross validation iterator
- `cross_validation.StratifiedShuffleSplit(y[Stratified ShuffleSplit cross validation iterator
- `cross_validation.PredefinedSplit(test_fold)` Predefined split cross validation iterator
- `decomposition.RandomizedPCA(*args, **kwargs)` Principal component analysis (PCA) using randomized SVD

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### sklearn.cross_validation.KFold

**Warning:** DEPRECATED

**class** `sklearn.cross_validation.KFold(n, n_folds=3, shuffle=False, random_state=None)`

K-Folds cross validation iterator.

- **Deprecated since version 0.18:** This module will be removed in 0.20. Use `sklearn.model_selection.KFold` instead.

Provides train/test indices to split data in train test sets. Split dataset into k consecutive folds (without shuffling by default).

Each fold is then used as a validation set once while the k - 1 remaining fold(s) form the training set.

Read more in the User Guide.

**Parameters**

- `n`: int
  - Total number of elements.

- `n_folds`: int, default=3
  - Number of folds. Must be at least 2.

- `shuffle`: boolean, optional
  - Whether to shuffle the data before splitting into batches.

- `random_state`: int, RandomState instance or None, optional, default=None
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`. Used when `shuffle == True`.

**See also:**

- `StratifiedKFold`, `folds`, `classification`  
- `LabelKFold` K-fold iterator variant with non-overlapping labels.
Notes

The first n \% n_folds folds have size n // n_folds + 1, other folds have size n // n_folds.

Examples

```python
>>> from sklearn.cross_validation import KFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([1, 2, 3, 4])
>>> kf = KFold(4, n_folds=2)
>>> len(kf)
2
>>> print(kf)
sklearn.cross_validation.KFold(n=4, n_folds=2, shuffle=False, random_state=None)
>>> for train_index, test_index in kf:
...    print("TRAIN: \{\}", train_index, "TEST: \{\}", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [0 1] TEST: [2 3]
```

__init__ (n, n_folds=3, shuffle=False, random_state=None)

**sklearn.cross_validation.LabelKFold**

**Warning:** DEPRECATED

**class sklearn.cross_validation.LabelKFold (labels, n_folds=3)**

K-fold iterator variant with non-overlapping labels.

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.GroupKFold instead.

The same label will not appear in two different folds (the number of distinct labels has to be at least equal to the number of folds).

The folds are approximately balanced in the sense that the number of distinct labels is approximately the same in each fold.

New in version 0.17.

**Parameters**

**labels** : array-like with shape (n_samples, )

Contains a label for each sample. The folds are built so that the same label does not appear in two different folds.

**n_folds** : int, default=3

Number of folds. Must be at least 2.

**See also:**

LeaveOneLabelOut, domain-specific
Examples

```python
>>> from sklearn.cross_validation import LabelKFold
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 3, 4])
>>> labels = np.array([0, 0, 2, 2])
>>> label_kfold = LabelKFold(labels, n_folds=2)
>>> len(label_kfold)
2
>>> print(label_kfold)
sklearn.cross_validation.LabelKFold(n_labels=4, n_folds=2)
>>> for train_index, test_index in label_kfold:
...    print("TRAIN:", train_index, "TEST:", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
...    print(X_train, X_test, y_train, y_test)
...TRAIN: [0 1] TEST: [2 3]
[[1 2]
 [3 4]] [[5 6]
 [7 8]]
TRAIN: [2 3] TEST: [0 1]
[[5 6]
 [7 8]] [[1 2]
 [3 4]]
```

__init__(labels, n_folds=3)

sklearn.cross_validation.LeaveOneLabelOut

**Warning:** DEPRECATED

class sklearn.cross_validation.LeaveOneLabelOut (labels)
Leave-One-Label_Out cross-validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.LeaveOneGroupOut instead.

Provides train/test indices to split data according to a third-party provided label. This label information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the labels could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

Read more in the User Guide.

Parameters labels : array-like of int with shape (n_samples,)

Arbitrary domain-specific stratification of the data to be used to draw the splits.

See also:

 LabelKFold K-fold iterator variant with non-overlapping labels.
Examples

```python
>>> from sklearn import cross_validation
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
>>> y = np.array([1, 2, 1, 2])
>>> labels = np.array([1, 1, 2, 2])
>>> lol = cross_validation.LeaveOneLabelOut(labels)
>>> len(lol)
2
>>> print(lol)
sklearn.cross_validation.LeaveOneLabelOut(labels=[1 1 2 2])
>>> for train_index, test_index in lol:
...    print("TRAIN:", train_index, "TEST:", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
...    print(X_train, X_test, y_train, y_test)
TRAIN: [2 3] TEST: [0 1]
[[5 6]
 [7 8]] [[1 2]
 [3 4]] [1 2] [1 2]
TRAIN: [0 1] TEST: [2 3]
[[1 2]
 [3 4]] [[5 6]
 [7 8]] [1 2] [1 2]
```

__init__(labels)

**sklearn.cross_validation.LeaveOneOut**

**Warning**: DEPRECATED

class sklearn.cross_validation.LeaveOneOut(n)
Leaves-One-Out cross validation iterator.

Deprecation since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.LeaveOneOut instead.

Provides train/test indices to split data in train test sets. Each sample is used once as a test set (singleton) while the remaining samples form the training set.

Note: LeaveOneOut(n) is equivalent to KFold(n, n_folds=n) and LeavePOut(n, p=1).

Due to the high number of test sets (which is the same as the number of samples) this cross validation method can be very costly. For large datasets one should favor KFold, StratifiedKFold or ShuffleSplit.

Read more in the User Guide.

**Parameters**

- **n**: int
  Total number of elements in dataset.

**See also**

- LeaveOneLabelOut, domain-specific
Examples

```python
>>> from sklearn import cross_validation
>>> X = np.array([[1, 2], [3, 4]])
>>> y = np.array([1, 2])
>>> loo = cross_validation.LeaveOneOut(2)
>>> print(loo)
sklearn.cross_validation.LeaveOneOut(n=2)
>>> for train_index, test_index in loo:
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
...     print(X_train, X_test, y_train, y_test)
TRAIN: [1] TEST: [0]
[[3 4]] [[1 2]] [2] [1]
TRAIN: [0] TEST: [1]
[[1 2]] [[3 4]] [1] [2]
```

`__init__`(n)

**sklearn.cross_validation.LeavePOut**

**Warning:** DEPRECATED

class sklearn.cross_validation.LeavePOut(n, p) Leave-P-Out cross validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.LeavePOut instead.

Provides train/test indices to split data in train test sets. This results in testing on all distinct samples of size p, while the remaining n - p samples form the training set in each iteration.

**Note:** LeavePOut(n, p) is NOT equivalent to KFold(n, n_folds=n // p) which creates non-overlapping test sets.

Due to the high number of iterations which grows combinatorically with the number of samples this cross validation method can be very costly. For large datasets one should favor KFold, StratifiedKFold or ShuffleSplit.

Read more in the User Guide.

**Parameters**

n : int
    Total number of elements in dataset.

p : int
    Size of the test sets.

**Examples**

```python
>>> from sklearn import cross_validation
>>> X = np.array([[1, 2], [3, 4], [5, 6], [7, 8]])
```
```python
>>> y = np.array([1, 2, 3, 4])
>>> lpo = cross_validation.LeavePOut(4, 2)
>>> len(lpo)
6
>>> print(lpo)
sklearn.cross_validation.LeavePOut(n=4, p=2)

>>> for train_index, test_index in lpo:
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [2 3] TEST: [0 1]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [1 2] TEST: [0 3]
TRAIN: [0 3] TEST: [1 2]
TRAIN: [0 2] TEST: [1 3]
TRAIN: [0 1] TEST: [2 3]
```

__init__(n, p)

`sklearn.cross_validation.LeavePLabelOut`

**Warning:** DEPRECATED

```python
class sklearn.cross_validation.LeavePLabelOut(labels, p)
Leaves P Label Out cross-validation iterator

Deprecation since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.LeavePGroupsOut instead.

Provides train/test indices to split data according to a third-party provided label. This label information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the labels could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

The difference between LeavePLabelOut and LeaveOneLabelOut is that the former builds the test sets with all the samples assigned to \( p \) different values of the labels while the latter uses samples all assigned the same labels.


**Parameters**

- `labels` : array-like of int with shape (n_samples,)
  
  Arbitrary domain-specific stratification of the data to be used to draw the splits.

- `p` : int
  
  Number of samples to leave out in the test split.

**See also**

- `LabelKFold` K-fold iterator variant with non-overlapping labels.

**Examples**
```python
>>> from sklearn import cross_validation
>>> X = np.array([[1, 2], [3, 4], [5, 6]])
>>> y = np.array([1, 2, 1])
>>> labels = np.array([1, 2, 3])
>>> lpl = cross_validation.LeavePLabelOut(labels, p=2)
>>> len(lpl)
3
>>> print(lpl)
sklearn.cross_validation.LeavePLabelOut(labels=[1 2 3], p=2)
>>> for train_index, test_index in lpl:
...    print("TRAIN:", train_index, "TEST:", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
...    print(X_train, X_test, y_train, y_test)
TRAIN: [2] TEST: [0 1]
[[5 6]] [[1 2]
 [3 4]] [1] [2]
TRAIN: [1] TEST: [0 2]
[[3 4]] [[1 2]
 [5 6]] [2] [1]
TRAIN: [0] TEST: [1 2]
[[1 2]] [[3 4]
 [5 6]] [1] [2 1]
```

```
__init__(labels, p)

sklearn.cross_validation.LabelShuffleSplit

Warning: DEPRECATED

class sklearn.cross_validation.LabelShuffleSplit (labels, n_iter=5, test_size=0.2, train_size=None, random_state=None)

Shuffle-Labels-Out cross-validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.GroupShuffleSplit instead.

Provides randomized train/test indices to split data according to a third-party provided label. This label information can be used to encode arbitrary domain specific stratifications of the samples as integers.

For instance the labels could be the year of collection of the samples and thus allow for cross-validation against time-based splits.

The difference between LeavePLabelOut and LabelShuffleSplit is that the former generates splits using all subsets of size \(p\) unique labels, whereas LabelShuffleSplit generates a user-determined number of random test splits, each with a user-determined fraction of unique labels.

For example, a less computationally intensive alternative to `LeavePLabelOut(labels, p=10)` would be `LabelShuffleSplit(labels, test_size=10, n_iter=100)`.

Note: The parameters `test_size` and `train_size` refer to labels, and not to samples, as in ShuffleSplit.

New in version 0.17.

Parameters labels : array, [n_samples]

Labels of samples

30.36. Recently deprecated
**n_iter** : int (default 5)

Number of re-shuffling and splitting iterations.

**test_size** : float (default 0.2), int, or None

If float, should be between 0.0 and 1.0 and represent the proportion of the labels to include in the test split. If int, represents the absolute number of test labels. If None, the value is automatically set to the complement of the train size.

**train_size** : float, int, or None (default is None)

If float, should be between 0.0 and 1.0 and represent the proportion of the labels to include in the train split. If int, represents the absolute number of train labels. If None, the value is automatically set to the complement of the test size.

**random_state** : int, RandomState instance or None, optional (default None)

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

```
__init__(labels, n_iter=5, test_size=0.2, train_size=None, random_state=None)
```

**sklearn.cross_validation.ShuffleSplit**

---

**Warning:** DEPRECATED

```
class sklearn.cross_validation.ShuffleSplit (n, n_iter=10, test_size=0.1, train_size=None, random_state=None)
```

Random permutation cross-validation iterator.

Depreciated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.ShuffleSplit` instead.

Yields indices to split data into training and test sets.

Note: contrary to other cross-validation strategies, random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the [User Guide](#).

**Parameters**

**n** : int

Total number of elements in the dataset.

**n_iter** : int (default 10)

Number of re-shuffling & splitting iterations.

**test_size** : float (default 0.1), int, or None

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is automatically set to the complement of the train size.

**train_size** : float, int, or None (default is None)

If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.
random_state : int, RandomState instance or None, optional (default None)

If int, random_state is the seed used by the random number generator; If RandomState
instance, random_state is the random number generator; If None, the random number
generator is the RandomState instance used by np.random.

Examples

```python
>>> from sklearn import cross_validation
>>> rs = cross_validation.ShuffleSplit(4, n_iter=3,
...    test_size=.25, random_state=0)
>>> len(rs)
3
>>> print(rs)
ShuffleSplit(4, n_iter=3, test_size=0.25, ...)
>>> for train_index, test_index in rs:
...    print("TRAIN:", train_index, "TEST:", test_index)
...    TRAIN: [3 1 0] TEST: [2]
    TRAIN: [2 1 3] TEST: [0]
    TRAIN: [0 2 1] TEST: [3]
```

__init__(n, n_iter=10, test_size=0.1, train_size=None, random_state=None)

sklearn.cross_validation.StratifiedKFold

Warning: DEPRECATED

class sklearn.cross_validation.StratifiedKFold(y, n_folds=3, shuffle=False, random_state=None)

Stratified K-Folds cross validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.StratifiedKFold instead.

Provides train/test indices to split data in train test sets.

This cross-validation object is a variation of KFold that returns stratified folds. The folds are made by preserving the percentage of samples for each class.

Read more in the User Guide.

Parameters y : array-like, [n_samples]

Samples to split in K folds.
**n_folds**: int, default=3

Number of folds. Must be at least 2.

**shuffle**: boolean, optional

Whether to shuffle each stratification of the data before splitting into batches.

**random_state**: int, RandomState instance or None, optional, default=None

If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random. Used when shuffle == True.

See also:

*LabelKFold* K-fold iterator variant with non-overlapping labels.

### Notes

All the folds have size trunc(n_samples / n_folds), the last one has the complementary.

### Examples

```python
>>> from sklearn.cross_validation import StratifiedKFold
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> skf = StratifiedKFold(y, n_folds=2)
>>> len(skf)
2
>>> for train_index, test_index in skf:
...     print("TRAIN:", train_index, "TEST:", test_index)
...     X_train, X_test = X[train_index], X[test_index]
...     y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 3] TEST: [0 2]
TRAIN: [0 2] TEST: [1 3]
```

**__init__**(y, n_folds=3, shuffle=False, random_state=None)

### sklearn.cross_validation.StratifiedShuffleSplit

**Warning**: DEPRECATED

**class sklearn.cross_validation.StratifiedShuffleSplit**(y, n_iter=10, test_size=0.1, train_size=None, random_state=None)

Stratified ShuffleSplit cross validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.StratifiedShuffleSplit` instead.
Provides train/test indices to split data in train test sets.

This cross-validation object is a merge of StratifiedKFold and ShuffleSplit, which returns stratified randomized folds. The folds are made by preserving the percentage of samples for each class.

Note: like the ShuffleSplit strategy, stratified random splits do not guarantee that all folds will be different, although this is still very likely for sizeable datasets.

Read more in the User Guide.

**Parameters**

- y : array, [n_samples]
  - Labels of samples.
- n_iter : int (default 10)
  - Number of re-shuffling & splitting iterations.
- test_size : float (default 0.1), int, or None
  - If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is automatically set to the complement of the train size.
- train_size : float, int, or None (default is None)
  - If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.
- random_state : int, RandomState instance or None, optional (default None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.

**Examples**

```python
>>> from sklearn.cross_validation import StratifiedShuffleSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> sss = StratifiedShuffleSplit(y, 3, test_size=0.5, random_state=0)
>>> len(sss)
3
>>> print(sss)
StratifiedShuffleSplit(labels=[0 0 1 1], n_iter=3, ...)
```

The method `__init__` is recently deprecated.

```python
>>> __init__(y, n_iter=10, test_size=0.1, train_size=None, random_state=None)
```
**sklearn.cross_validation.PredefinedSplit**

Warning: DEPRECATED

class sklearn.cross_validation.PredefinedSplit(test_fold)

Predefined split cross validation iterator

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.PredefinedSplit instead.

Splits the data into training/test set folds according to a predefined scheme. Each sample can be assigned to at most one test set fold, as specified by the user through the test_fold parameter.

Read more in the User Guide.

Parameters test_fold : “array-like, shape (n_samples,)

  test_fold[i] gives the test set fold of sample i. A value of -1 indicates that the corresponding sample is not part of any test set folds, but will instead always be put into the training fold.

Examples

```python
>>> from sklearn.cross_validation import PredefinedSplit
>>> X = np.array([[1, 2], [3, 4], [1, 2], [3, 4]])
>>> y = np.array([0, 0, 1, 1])
>>> ps = PredefinedSplit(test_fold=[0, 1, -1, 1])
>>> len(ps)
2
>>> print(ps)
sklearn.cross_validation.PredefinedSplit(test_fold=[ 0 1 -1 1])
>>> for train_index, test_index in ps:
...    print("TRAIN: ", train_index, "TEST: ", test_index)
...    X_train, X_test = X[train_index], X[test_index]
...    y_train, y_test = y[train_index], y[test_index]
TRAIN: [1 3] TEST: [0]
TRAIN: [0 2] TEST: [1 3]
```

**sklearn.decomposition.RandomizedPCA**

Warning: DEPRECATED

class sklearn.decomposition.RandomizedPCA (*args, **kwargs)

Principal component analysis (PCA) using randomized SVD

Deprecated since version 0.18: This class will be removed in 0.20. Use PCA with parameter svd_solver `randomized` instead. The new implementation DOES NOT store whitening components. Apply transform to get them.

Linear dimensionality reduction using approximated Singular Value Decomposition of the data and keeping only the most significant singular vectors to project the data to a lower dimensional space.
Read more in the *User Guide*.

**Parameters**

- **n_components**: int, optional
  
  Maximum number of components to keep. When not given or None, this is set to n_features (the second dimension of the training data).

- **copy**: bool
  
  If False, data passed to fit are overwritten and running fit(X).transform(X) will not yield the expected results, use fit_transform(X) instead.

- **iterated_power**: int, default=2
  
  Number of iterations for the power method.

  Changed in version 0.18.

- **whiten**: bool, optional
  
  When True (False by default) the components_ vectors are multiplied by the square root of (n_samples) and divided by the singular values to ensure uncorrelated outputs with unit component-wise variances.

  Whitening will remove some information from the transformed signal (the relative variance scales of the components) but can sometime improve the predictive accuracy of the downstream estimators by making their data respect some hard-wired assumptions.

- **random_state**: int, RandomState instance or None, optional, default=None
  
  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

**Attributes**

- **components_**: (array, shape (n_components, n_features)) Components with maximum variance.

- **explained_variance_ratio_**: (array, shape (n_components,)) Percentage of variance explained by each of the selected components. If k is not set then all components are stored and the sum of explained variances is equal to 1.0.

- **singular_values_**: (array, shape (n_components,)) The singular values corresponding to each of the selected components. The singular values are equal to the 2-norms of the n_components variables in the lower-dimensional space.

- **mean_**: (array, shape (n_features,)) Per-feature empirical mean, estimated from the training set.

**See also:**

- PCA
- TruncatedSVD

**References**

[Halko2009358360], [MRT358360]
Examples

```python
>>> import numpy as np
>>> from sklearn.decomposition import RandomizedPCA
>>> X = np.array([[[-1, -1], [-2, -1], [-3, -2], [1, 1], [2, 1], [3, 2]]])
>>> pca = RandomizedPCA(n_components=2)
>>> pca.fit(X)
RandomizedPCA(copy=True, iterated_power=2, n_components=2, random_state=None, whiten=False)
>>> print(pca.explained_variance_ratio_)
[ 0.99244... 0.00755...]
>>> print(pca.singular_values_)
[ 6.30061... 0.54980...]
```

Methods

```python
fit(X[, y])
Fit the model with X by extracting the first principal components.

fit_transform(X[, y])
Fit the model with X and apply the dimensionality reduction on X.

get_params([deep])
Get parameters for this estimator.

inverse_transform(X)
Transform data back to its original space.

set_params(**params)
Set the parameters of this estimator.

transform(X)
Apply dimensionality reduction on X.
```

```python
__init__(*args, **kwargs)
DEPRECATED: RandomizedPCA was deprecated in 0.18 and will be removed in 0.20. Use PCA(svd_solver='randomized') instead. The new implementation DOES NOT store whiten components_. Apply transform to get them.

fit(X, y=None)
Fit the model with X by extracting the first principal components.

Parameters

X : array-like, shape (n_samples, n_features)
Training data, where n_samples in the number of samples and n_features is the number of features.

y : Ignored

Returns

self : object
Returns the instance itself.

fit_transform(X, y=None)
Fit the model with X and apply the dimensionality reduction on X.

Parameters

X : array-like, shape (n_samples, n_features)
New data, where n_samples in the number of samples and n_features is the number of features.

y : Ignored

Returns

X_new : array-like, shape (n_samples, n_components)
```
get_params (deep=True)
Get parameters for this estimator.

Parameters  
  deep : boolean, optional
  If True, will return the parameters for this estimator and contained subobjects that are
  estimators.

Returns  
  params : mapping of string to any
  Parameter names mapped to their values.

inverse_transform (X)
Transform data back to its original space.

Returns an array X_original whose transform would be X.

Parameters  
  X : array-like, shape (n_samples, n_components)
  New data, where n_samples in the number of samples and n_components is the number
  of components.

Returns  
  X_original array-like, shape (n_samples, n_features)

Notes
If whitening is enabled, inverse_transform does not compute the exact inverse operation of transform.

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
parameters of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns  
  self

transform (X)
Apply dimensionality reduction on X.

X is projected on the first principal components previous extracted from a training set.

Parameters  
  X : array-like, shape (n_samples, n_features)
  New data, where n_samples in the number of samples and n_features is the number
  of features.

Returns  
  X_new : array-like, shape (n_samples, n_components)

sklearn.gaussian_process.GaussianProcess

Warning: DEPRECATED

class  
  sklearn.gaussian_process.GaussianProcess(*args, **kwargs)
  The legacy Gaussian Process model class.

  Deprecated since version 0.18: This class will be removed in 0.20. Use the GaussianProcessRegressor
  instead.

  Read more in the User Guide.
Parameters `regr`: string or callable, optional

A regression function returning an array of outputs of the linear regression functional basis. The number of observations `n_samples` should be greater than the size `p` of this basis. Default assumes a simple constant regression trend. Available built-in regression models are:

'constant', 'linear', 'quadratic'

`corr`: string or callable, optional

A stationary autocorrelation function returning the autocorrelation between two points `x` and `x'`. Default assumes a squared-exponential autocorrelation model. Built-in correlation models are:

'absolute_exponential', 'squared_exponential',
'generalized_exponential', 'cubic', 'linear'

`beta0`: double array_like, optional

The regression weight vector to perform Ordinary Kriging (OK). Default assumes Universal Kriging (UK) so that the vector `beta` of regression weights is estimated using the maximum likelihood principle.

`storage_mode`: string, optional

A string specifying whether the Cholesky decomposition of the correlation matrix should be stored in the class (storage_mode = 'full') or not (storage_mode = 'light'). Default assumes storage_mode = 'full', so that the Cholesky decomposition of the correlation matrix is stored. This might be a useful parameter when one is not interested in the MSE and only plan to estimate the BLUP, for which the correlation matrix is not required.

`verbose`: boolean, optional

A boolean specifying the verbose level. Default is verbose = False.

`theta0`: double array_like, optional

An array with shape (n_features, ) or (1, ). The parameters in the autocorrelation model. If thetaL and thetaU are also specified, theta0 is considered as the starting point for the maximum likelihood estimation of the best set of parameters. Default assumes isotropic autocorrelation model with theta0 = 1e-1.

`thetaL`: double array_like, optional

An array with shape matching theta0's. Lower bound on the autocorrelation parameters for maximum likelihood estimation. Default is None, so that it skips maximum likelihood estimation and it uses theta0.

`thetaU`: double array_like, optional

An array with shape matching theta0's. Upper bound on the autocorrelation parameters for maximum likelihood estimation. Default is None, so that it skips maximum likelihood estimation and it uses theta0.

`normalize`: boolean, optional

Input X and observations y are centered and reduced wrt means and standard deviations estimated from the `n_samples` observations provided. Default is normalize = True so that data is normalized to ease maximum likelihood estimation.

`nugget`: double or ndarray, optional
Introduce a nugget effect to allow smooth predictions from noisy data. If nugget is
an ndarray, it must be the same length as the number of data points used for the fit.
The nugget is added to the diagonal of the assumed training covariance; in this way
it acts as a Tikhonov regularization in the problem. In the special case of the squared
exponential correlation function, the nugget mathematically represents the variance of
the input values. Default assumes a nugget close to machine precision for the sake of
robustness (nugget = 10. * MACHINE_EPSILON).

**optimizer** : string, optional

A string specifying the optimization algorithm to be used. Default uses ‘fmin_cobyla’
algorithm from scipy.optimize. Available optimizers are:

```
'fmin_cobyla', 'Welch'
```

‘Welch’ optimizer is due to Welch et al., see reference [WBSWM1992426428]. It
consists in iterating over several one-dimensional optimizations instead of running one
single multi-dimensional optimization.

**random_start** : int, optional

The number of times the Maximum Likelihood Estimation should be performed from a
random starting point. The first MLE always uses the specified starting point (theta0),
the next starting points are picked at random according to an exponential distribution
(log-uniform on [thetaL, thetaU]). Default does not use random starting point (ran-
dom_start = 1).

**random_state** : int, RandomState instance or None, optional (default=None)

The generator used to shuffle the sequence of coordinates of theta in the Welch opti-
mizer. If int, random_state is the seed used by the random number generator; If Ran-
domState instance, random_state is the random number generator; If None, the random
number generator is the RandomState instance used by np.random.

**Attributes**

| theta_          | (array) Specified theta OR the best set of autocorrelation parameters (the sought
            | maximizer of the reduced likelihood function). |
|-----------------|-------------------------------------------------|
| reduced_        | (array) The optimal reduced likelihood function value. |
| likelihood_value_ |                                                |

**Notes**

The presentation implementation is based on a translation of the DACE Matlab toolbox, see reference
[NLNS2002426428].

**References**

[NLNS2002426428], [WBSWM1992426428]
Examples

```python
>>> import numpy as np
>>> from sklearn.gaussian_process import GaussianProcess
>>> X = np.array([[1., 3., 5., 6., 7., 8.]]).T
>>> y = (X * np.sin(X)).ravel()
>>> gp = GaussianProcess(theta0=0.1, thetaL=.001, thetaU=1.)
>>> gp.fit(X, y)
GaussianProcess(beta0=None...
```

Methods

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<td>The Gaussian Process model fitting method.</td>
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<td><code>get_params(deep)</code></td>
<td>Get parameters for this estimator.</td>
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<td><code>predict(X[, eval_MSE, batch_size])</code></td>
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<td><code>score(X, y[, sample_weight])</code></td>
<td>Returns the coefficient of determination R^2 of the prediction.</td>
</tr>
<tr>
<td><code>set_params(**params)</code></td>
<td>Set the parameters of this estimator.</td>
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```python
__init__(*args, **kwargs)

DEPRECATED: GaussianProcess was deprecated in version 0.18 and will be removed in 0.20. Use the GaussianProcessRegressor instead.
```

```python
fit (X, y)

The Gaussian Process model fitting method.

Parameters

- **X**: double array_like
  An array with shape (n_samples, n_features) with the input at which observations were made.

- **y**: double array_like
  An array with shape (n_samples,) or shape (n_samples, n_targets) with the observations of the output to be predicted.

Returns **gp**: self
A fitted Gaussian Process model object awaiting data to perform predictions.

get_params (deep=True)
Get parameters for this estimator.

Parameters **deep**: boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns **params**: mapping of string to any
Parameter names mapped to their values.
predict \((X, eval\_MSE=False, batch\_size=None)\)
This function evaluates the Gaussian Process model at \(x\).

**Parameters**

\(X\) : array-like
An array with shape \((n\_eval, n\_features)\) giving the point(s) at which the prediction(s) should be made.

\(eval\_MSE\) : boolean, optional
A boolean specifying whether the Mean Squared Error should be evaluated or not. Default assumes \(evalMSE = False\) and evaluates only the BLUP (mean prediction).

\(batch\_size\) : integer, optional
An integer giving the maximum number of points that can be evaluated simultaneously (depending on the available memory). Default is None so that all given points are evaluated at the same time.

**Returns**

\(y\) : array-like, shape \((n\_samples, )\) or \((n\_samples, n\_targets)\)
An array with shape \((n\_eval, )\) if the Gaussian Process was trained on an array of shape \((n\_samples, )\) or an array with shape \((n\_eval, n\_targets)\) if the Gaussian Process was trained on an array of shape \((n\_samples, n\_targets)\) with the Best Linear Unbiased Prediction at \(x\).

\(MSE\) : array-like, optional (if \(eval\_MSE == True\) )
An array with shape \((n\_eval, )\) or \((n\_eval, n\_targets)\) as with \(y\), with the Mean Squared Error at \(x\).

reduced_likelihood_function \((\theta=None)\)
This function determines the BLUP parameters and evaluates the reduced likelihood function for the given autocorrelation parameters \(\theta\).

Maximizing this function wrt the autocorrelation parameters \(\theta\) is equivalent to maximizing the likelihood of the assumed joint Gaussian distribution of the observations \(y\) evaluated onto the design of experiments \(X\).

**Parameters**

\(\theta\) : array-like, optional
An array containing the autocorrelation parameters at which the Gaussian Process model parameters should be determined. Default uses the built-in autocorrelation parameters (ie \(\theta = self.\theta\_\)).

**Returns**

\(reduced\_likelihood\_function\_value\) : double
The value of the reduced likelihood function associated to the given autocorrelation parameters \(\theta\).

\(par\) : dict
A dictionary containing the requested Gaussian Process model parameters:

- \(\texttt{sigma2}\) is the Gaussian Process variance.
- \(\texttt{beta}\) is the generalized least-squares regression weights for Universal Kriging or given beta0 for Ordinary Kriging.
- \(\texttt{gamma}\) is the Gaussian Process weights.
- \(\texttt{C}\) is the Cholesky decomposition of the correlation matrix [R].
- \(\texttt{Ft}\) is the solution of the linear equation system [R] x Ft = F
- \(\texttt{G}\) is the QR decomposition of the matrix Ft.
**score** *(X, y, sample_weight=None)*  
Returns the coefficient of determination $R^2$ of the prediction.

The coefficient $R^2$ is defined as $(1 - u/v)$, where $u$ is the residual sum of squares $(y_{true} - y_{pred})^2$.sum() and $v$ is the total sum of squares $(y_{true} - y_{true}.mean())^2$.sum(). The best possible score is 1.0 and it can be negative (because the model can be arbitrarily worse). A constant model that always predicts the expected value of $y$, disregarding the input features, would get a $R^2$ score of 0.0.

**Parameters**  
- **X**: array-like, shape = (n_samples, n_features)  
  Test samples.  
- **y**: array-like, shape = (n_samples) or (n_samples, n_outputs)  
  True values for X.  
- **sample_weight**: array-like, shape = [n_samples], optional  
  Sample weights.

**Returns** **score**: float  
$R^2$ of self.predict(X) wrt. $y$.

**set_params** *(**params)**  
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** **self**

---

**sklearn.grid_search.ParameterGrid**

---

**Warning**: DEPRECATED

**class** **sklearn.grid_search.ParameterGrid**(param_grid)  
Grid of parameters with a discrete number of values for each.

Deprecated since version 0.18: This module will be removed in 0.20. Use **sklearn.model_selection.ParameterGrid** instead.

Can be used to iterate over parameter value combinations with the Python built-in function `iter`.

Read more in the **User Guide**.

**Parameters** **param_grid**: dict of string to sequence, or sequence of such  

The parameter grid to explore, as a dictionary mapping estimator parameters to sequences of allowed values.

An empty dict signifies default parameters.

A sequence of dicts signifies a sequence of grids to search, and is useful to avoid exploring parameter combinations that make no sense or have no effect. See the examples below.

**See also**:

**GridSearchCV** uses **ParameterGrid** to perform a full parallelized parameter search.
Examples

```python
>>> from sklearn.grid_search import ParameterGrid
>>> param_grid = {'a': [1, 2], 'b': [True, False]}
>>> list(ParameterGrid(param_grid)) == (
...     [{'a': 1, 'b': True}, {'a': 1, 'b': False},
...     {'a': 2, 'b': True}, {'a': 2, 'b': False}])
True

>>> grid = [{'kernel': ['linear']}, {'kernel': ['rbf'], 'gamma': [1, 10]}]
>>> list(ParameterGrid(grid)) == [{'kernel': 'linear'},
...     {'kernel': 'rbf', 'gamma': 1},
...     {'kernel': 'rbf', 'gamma': 10}]
True

>>> ParameterGrid(grid)[1] == {'kernel': 'rbf', 'gamma': 1}
True
```

```
__init__(param_grid)
```

### sklearn.grid_search.ParameterSampler

**Warning:** DEPRECATED

```python
class sklearn.grid_search.ParameterSampler(param_distributions, n_iter, random_state=None)
```

Generator on parameters sampled from given distributions.

Deprecated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.ParameterSampler` instead.

Non-deterministic iterable over random candidate combinations for hyperparameter search. If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Note that as of SciPy 0.12, the `scipy.stats.distributions` do not accept a custom RNG instance and always use the singleton RNG from `numpy.random`. Hence setting `random_state` will not guarantee a deterministic iteration whenever `scipy.stats` distributions are used to define the parameter search space.

Read more in the [User Guide](https://scikit-learn.org/stable/).

**Parameters**

- **`param_distributions`**: dict
  
  Dictionary where the keys are parameters and values are distributions from which a parameter is to be sampled. Distributions either have to provide a `rvs` function to sample from them, or can be given as a list of values, where a uniform distribution is assumed.

- **`n_iter`**: integer

  Number of parameter settings that are produced.

- **`random_state`**: int, RandomState instance or None, optional (default=None)

  Pseudo random number generator state used for random uniform sampling from lists of possible values instead of `scipy.stats` distributions. If int, `random_state` is the seed used by the random number generator; If RandomState instance, `random_state` is the random state of the RandomState instance; if None, the random state of `numpy.random` is used.
number generator; If None, the random number generator is the RandomState instance used by \texttt{np.random}.

**Returns** \texttt{params} : dict of string to any

**Yields** dictionaries mapping each estimator parameter to as sampled value.

### Examples

```python
>>> from sklearn.grid_search import ParameterSampler
>>> from scipy.stats.distributions import expon
>>> import numpy as np

>>> np.random.seed(0)
>>> param_grid = {'a':[1, 2], 'b': expon()}
>>> param_list = list(ParameterSampler(param_grid, n_iter=4))
>>> rounded_list = [{k: round(v, 6) for (k, v) in d.items()} for d in param_list]
>>> rounded_list == [{'b': 0.89856, 'a': 1},
...                   {'b': 0.923223, 'a': 1},
...                   {'b': 1.878964, 'a': 2},
...                   {'b': 1.038159, 'a': 2}]
True
```

__init__ (param_distributions, n_iter, random_state=None)

### sklearn.grid_search.GridSearchCV

**Warning:** DEPRECATED

**class** sklearn.grid_search.GridSearchCV (estimator, param_grid, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', error_score='raise')

Exhaustive search over specified parameter values for an estimator.

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.GridSearchCV instead.

Important members are fit, predict.

GridSearchCV implements a “fit” and a “score” method. It also implements “predict”, “predict_proba”, “decision_function”, “transform” and “inverse_transform” if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated grid-search over a parameter grid.

Read more in the User Guide.

**Parameters**

- **estimator** : estimator object.
  
  A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a score function, or scoring must be passed.

- **param_grid** : dict or list of dictionaries
Dictionary with parameters names (string) as keys and lists of parameter settings to try as values, or a list of such dictionaries, in which case the grids spanned by each dictionary in the list are explored. This enables searching over any sequence of parameter settings.

**scoring** : string, callable or None, default=None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y). If None, the `score` method of the estimator is used.

**fit_params** : dict, optional

Parameters to pass to the fit method.

**n_jobs** : int, default: 1

The maximum number of estimators fit in parallel.

- If -1 all CPUs are used.
- If 1 is given, no parallel computing code is used at all, which is useful for debugging.
- For n_jobs below -1, (n_cpus + n_jobs + 1) are used. For example, with n_jobs = -2 all CPUs but one are used.

Changed in version 0.17: Upgraded to joblib 0.9.3.

**pre_dispatch** : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

- None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

**iid** : boolean, default=True

If True, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds.

**cv** : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, `sklearn.model_selection.StratifiedKFold` is used. In all other cases, `sklearn.model_selection.KFold` is used.

Refer User Guide for the various cross-validation strategies that can be used here.

**refit** : boolean, default=True

30.36. Recently deprecated
Refit the best estimator with the entire dataset. If “False”, it is impossible to make predictions using this GridSearchCV instance after fitting.

**verbose** : integer

Controls the verbosity: the higher, the more messages.

**error_score** : ‘raise’ (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error.

### Attributes

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<th>Attribute</th>
<th>Description</th>
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<td><strong>grid_scores</strong></td>
<td>(of named tuples) Contains scores for all parameter combinations in param_grid. Each entry corresponds to one parameter setting. Each named tuple has the attributes: * parameters, a dict of parameter settings * mean_validation_score, the mean score over the cross-validation folds * cv_validation_scores, the list of scores for each fold</td>
</tr>
<tr>
<td><strong>best_estimator</strong></td>
<td>Estimator that was chosen by the search, i.e. estimator which gave highest score (or smallest loss if specified) on the left out data. Not available if refit=False.</td>
</tr>
<tr>
<td><strong>best_score</strong></td>
<td>Score of best_estimator on the left out data.</td>
</tr>
<tr>
<td><strong>best_params</strong></td>
<td>Parameter setting that gave the best results on the hold out data.</td>
</tr>
<tr>
<td><strong>scorer</strong></td>
<td>(function) Scorer function used on the hold out data to choose the best parameters for the model.</td>
</tr>
</tbody>
</table>

See also:

* **ParameterGrid** generates all the combinations of a hyperparameter grid.
* **sklearn.cross_validation.train_test_split** utility function to split the data into a development set usable for fitting a GridSearchCV instance and an evaluation set for its final evaluation.
* **sklearn.metrics.make_scorer** Make a scorer from a performance metric or loss function.

### Notes

The parameters selected are those that maximize the score of the left out data, unless an explicit score is passed in which case it is used instead.

If n_jobs was set to a value higher than one, the data is copied for each point in the grid (and not n_jobs times).

This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set pre_dispatch. Then, the memory is copied only pre_dispatch many times. A reasonable value for pre_dispatch is 2 * n_jobs.

### Examples

```python
>>> from sklearn import svm, grid_search, datasets
>>> iris = datasets.load_iris()
>>> parameters = {'kernel':('linear', 'rbf'), 'C':[1, 10]}
>>> svr = svm.SVC()
>>> clf = grid_search.GridSearchCV(svr, parameters)
>>> clf.fit(iris.data, iris.target)
```
GridSearchCV(cv=None, error_score=..., estimator=SVC(C=1.0, cache_size=..., class_weight=..., coef0=..., decision_function_shape='ovr', degree=..., gamma=..., kernel='rbf', max_iter=-1, probability=False, random_state=None, shrinking=True, tol=..., verbose=False), fit_params={}, iid=..., n_jobs=1, param_grid=..., pre_dispatch=..., refit=..., scoring=..., verbose=...)

Methods

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<th>Method</th>
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<td>decision_function(X)</td>
<td>Call decision_function on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>fit(X, y=None)</td>
<td>Run fit with all sets of parameters.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>inverse_transform(Xt)</td>
<td>Call inverse_transform on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Call predict on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>predict_log_proba(X)</td>
<td>Call predict_log_proba on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>predict_proba(X)</td>
<td>Call predict_proba on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>score(X, y=None)</td>
<td>Returns the score on the given data, if the estimator has been refit.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Call transform on the estimator with the best found parameters.</td>
</tr>
</tbody>
</table>

__init__ (estimator, param_grid, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2 * n_jobs', error_score='raise')

decision_function (X)
Call decision_function on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports decision_function.

Parameters X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

fit (X, y=None)
Run fit with all sets of parameters.

Parameters X : array-like, shape = [n_samples, n_features]
Training vector, where n_samples is the number of samples and n_features is the number of features.

y : array-like, shape = [n_samples] or [n_samples, n_output], optional
Target relative to X for classification or regression; None for unsupervised learning.

get_params (deep=True)
Get parameters for this estimator.
Parameters deep : boolean, optional
    If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
    Parameter names mapped to their values.

inverse_transform(Xt)
    Call inverse_transform on the estimator with the best found parameters.
    Only available if the underlying estimator implements inverse_transform and refit=True.
    Parameters Xt : indexable, length n_samples
        Must fulfill the input assumptions of the underlying estimator.

predict(X)
    Call predict on the estimator with the best found parameters.
    Only available if refit=True and the underlying estimator supports predict.
    Parameters X : indexable, length n_samples
        Must fulfill the input assumptions of the underlying estimator.

predict_log_proba(X)
    Call predict_log_proba on the estimator with the best found parameters.
    Only available if refit=True and the underlying estimator supports predict_log_proba.
    Parameters X : indexable, length n_samples
        Must fulfill the input assumptions of the underlying estimator.

predict_proba(X)
    Call predict_proba on the estimator with the best found parameters.
    Only available if refit=True and the underlying estimator supports predict_proba.
    Parameters X : indexable, length n_samples
        Must fulfill the input assumptions of the underlying estimator.

score(X, y=None)
    Returns the score on the given data, if the estimator has been refit.
    This uses the score defined by scoring where provided, and the best_estimator_.score method otherwise.
    Parameters X : array-like, shape = [n_samples, n_features]
        Input data, where n_samples is the number of samples and n_features is the number of features.
    y : array-like, shape = [n_samples] or [n_samples, n_output], optional
        Target relative to X for classification or regression; None for unsupervised learning.
    Returns score : float

Notes

• The long-standing behavior of this method changed in version 0.16.
• It no longer uses the metric provided by `estimator.score` if the `scoring` parameter was set when fitting.

**set_params(**`params`**)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

**Returns** self

**transform**(X)
Call transform on the estimator with the best found parameters.

Only available if the underlying estimator supports `transform` and `refit=True`.

**Parameters** X : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

**sklearn.grid_search.RandomizedSearchCV**

**Warning:** DEPRECATED

**class** `sklearn.grid_search.RandomizedSearchCV`(estimator, param_distributions, n_iter=10, scoring=None, fit_params=None, n_jobs=1, iid=True, refit=True, cv=None, verbose=0, pre_dispatch='2*n_jobs', random_state=None, error_score='raise')

Randomized search on hyper parameters.

Deprecated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.RandomizedSearchCV` instead.

RandomizedSearchCV implements a “fit” and a “score” method. It also implements “predict”, “predict_proba”, “decision_function”, “transform” and “inverse_transform” if they are implemented in the estimator used.

The parameters of the estimator used to apply these methods are optimized by cross-validated search over parameter settings.

In contrast to GridSearchCV, not all parameter values are tried out, but rather a fixed number of parameter settings is sampled from the specified distributions. The number of parameter settings that are tried is given by `n_iter`.

If all parameters are presented as a list, sampling without replacement is performed. If at least one parameter is given as a distribution, sampling with replacement is used. It is highly recommended to use continuous distributions for continuous parameters.

Read more in the User Guide.

**Parameters**

`estimator` : estimator object.

A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a `score` function, or `scoring` must be passed.

`param_distributions` : dict
Dictionary with parameters names (string) as keys and distributions or lists of parameters to try. Distributions must provide a \texttt{rvs} method for sampling (such as those from scipy.stats.distributions). If a list is given, it is sampled uniformly.

\textbf{\texttt{n_iter}} : int, default=10

Number of parameter settings that are sampled. \texttt{n_iter} trades off runtime vs quality of the solution.

\textbf{\texttt{scoring}} : string, callable or None, default=None

A string (see model evaluation documentation) or a scorer callable object / function with signature \texttt{scorer(estimator, X, y)}. If None, the \texttt{score} method of the estimator is used.

\textbf{\texttt{fit_params}} : dict, optional

Parameters to pass to the fit method.

\textbf{\texttt{n_jobs}}: int, default: 1 :

The maximum number of estimators fit in parallel.

- If -1 all CPUs are used.
- If 1 is given, no parallel computing code is used at all, which is useful for debugging.
- For \texttt{n_jobs} below -1, \((\texttt{n_cpus} + \texttt{n_jobs} + 1)\) are used. For example, with \texttt{n_jobs} = -2 all CPUs but one are used.

\textbf{\texttt{pre_dispatch}} : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

- None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of \texttt{n_jobs}, as in ‘2*\texttt{n_jobs}’

\textbf{\texttt{iid}} : boolean, default=True

If True, the data is assumed to be identically distributed across the folds, and the loss minimized is the total loss per sample, and not the mean loss across the folds.

\textbf{\texttt{cv}} : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for \texttt{cv} are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if the estimator is a classifier and \texttt{y} is either binary or multiclass, \texttt{sklearn.model_selection.StratifiedKFold} is used. In all other cases, \texttt{sklearn.model_selection.KFold} is used.

Refer \textit{User Guide} for the various cross-validation strategies that can be used here.
refit : boolean, default=True

Refit the best estimator with the entire dataset. If “False”, it is impossible to make predictions using this RandomizedSearchCV instance after fitting.

verbose : integer

Controls the verbosity: the higher, the more messages.

random_state : int, RandomState instance or None, optional, default=None

Pseudo random number generator state used for random uniform sampling from lists of possible values instead of scipy.stats distributions. If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

error_score : ‘raise’ (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error.

Attributes

grid_scores_ (list of named tuples) Contains scores for all parameter combinations in param_grid. Each entry corresponds to one parameter setting. Each named tuple has the attributes: * parameters, a dict of parameter settings * mean_validation_score, the mean score over the cross-validation folds * cv_validation_scores, the list of scores for each fold

best_estimator_ (estimator) Estimator that was chosen by the search, i.e. estimator which gave highest score (or smallest loss if specified) on the left out data. Not available if refit=False.

best_score_ (float) Score of best_estimator on the left out data.

best_params_ Parameter setting that gave the best results on the hold out data.

See also:

GridSearchCV Does exhaustive search over a grid of parameters.

ParameterSampler A generator over parameter settings, constructed from param_distributions.

Notes

The parameters selected are those that maximize the score of the held-out data, according to the scoring parameter.

If n_jobs was set to a value higher than one, the data is copied for each parameter setting (and not n_jobs times). This is done for efficiency reasons if individual jobs take very little time, but may raise errors if the dataset is large and not enough memory is available. A workaround in this case is to set pre_dispatch. Then, the memory is copied only pre_dispatch many times. A reasonable value for pre_dispatch is 2*n_jobs.

Methods

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<td>fit(X[, y])</td>
<td>Run fit on the estimator with randomly drawn parameters.</td>
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<tr>
<td>get_params([deep])</td>
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<td>Call inverse_transform on the estimator with the best found parameters.</td>
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<td>Call predict_log_proba on the estimator with the best found parameters.</td>
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<td>predict_proba(X)</td>
<td>Call predict_proba on the estimator with the best found parameters.</td>
</tr>
<tr>
<td>score(X[, y])</td>
<td>Returns the score on the given data, if the estimator has been refit.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
<tr>
<td>transform(X)</td>
<td>Call transform on the estimator with the best found parameters.</td>
</tr>
</tbody>
</table>

#### __init__

```
__init__(estimator, param_distributions, n_iter=10, scoring=None, fit_params=None, n_jobs=1,
         iid=True, refit=True, cv=None, pre_dispatch='2*n_jobs', random_state=None,
         error_score='raise')
```

**decision_function** (X)

Call decision_function on the estimator with the best found parameters.

Only available if refit=True and the underlying estimator supports decision_function.

**Parameters**

- **X** : indexable, length n_samples
  
  Must fulfill the input assumptions of the underlying estimator.

**fit** (X, y=None)

Run fit on the estimator with randomly drawn parameters.

**Parameters**

- **X** : array-like, shape = [n_samples, n_features]
  
  Training vector, where n_samples in the number of samples and n_features is the number of features.

- **y** : array-like, shape = [n_samples] or [n_samples, n_output], optional
  
  Target relative to X for classification or regression; None for unsupervised learning.

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**

- **deep** : boolean, optional
  
  If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**

- **params** : mapping of string to any
  
  Parameter names mapped to their values.

**inverse_transform** (Xt)

Call inverse_transform on the estimator with the best found parameters.

Only available if the underlying estimator implements inverse_transform and refit=True.
Parameters $X_t$ : indexable, length $n_{samples}$

- Must fulfill the input assumptions of the underlying estimator.

```
predict ($X$)
```

- Call predict on the estimator with the best found parameters.
- Only available if refit=True and the underlying estimator supports predict.

```
Parameters $X$ : indexable, length $n_{samples}$
```

- Must fulfill the input assumptions of the underlying estimator.

```
predict_log_proba ($X$)
```

- Call predict_log_proba on the estimator with the best found parameters.
- Only available if refit=True and the underlying estimator supports predict_log_proba.

```
Parameters $X$ : indexable, length $n_{samples}$
```

- Must fulfill the input assumptions of the underlying estimator.

```
predict_proba ($X$)
```

- Call predict_proba on the estimator with the best found parameters.
- Only available if refit=True and the underlying estimator supports predict_proba.

```
Parameters $X$ : indexable, length $n_{samples}$
```

- Must fulfill the input assumptions of the underlying estimator.

```
score ($X$, $y=None$)
```

- Returns the score on the given data, if the estimator has been refit.
- This uses the score defined by scoring where provided, and the best_estimator_.score method otherwise.

```
Parameters $X$ : array-like, shape = [n_{samples}, n_{features}]
```

- Input data, where n_samples is the number of samples and n_features is the number of features.

```
y : array-like, shape = [n_{samples}] or [n_{samples}, n_{output}], optional
```

- Target relative to $X$ for classification or regression; None for unsupervised learning.

```
Returns score : float
```

Notes

- The long-standing behavior of this method changed in version 0.16.
- It no longer uses the metric provided by estimator.score if the scoring parameter was set when fitting.

```
set_params (**params)
```

- Set the parameters of this estimator.
- The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it’s possible to update each component of a nested object.

```
Returns self
```
transform($X$)
Call transform on the estimator with the best found parameters.
Only available if the underlying estimator supports transform and refit=True.

Parameters $X$ : indexable, length n_samples
Must fulfill the input assumptions of the underlying estimator.

sklearn.mixture.DPGMM

Warning: DEPRECATED

class sklearn.mixture.DPGMM(*args, **kwargs)
Dirichlet Process Gaussian Mixture Models

Deprecated since version 0.18: This class will be removed in 0.20.
Use sklearn.mixture.BayesianGaussianMixture with parameter
weight_concentration_prior_type='dirichlet_process' instead.

Methods

aic($X$) Akaike information criterion for the current model fit and the proposed data.
bic($X$) Bayesian information criterion for the current model fit and the proposed data.
fit($X$, $y$) Estimate model parameters with the EM algorithm.
fit_predict($X$, $y$) Fit and then predict labels for data.
get_params([deep]) Get parameters for this estimator.
lower_bound($X$, $z$) returns a lower bound on model evidence based on $X$ and membership
predict($X$) Predict label for data.
predict_proba($X$) Predict posterior probability of data under each Gaussian in the model.
sample([n_samples, random_state]) Generate random samples from the model.
score($X$, $y$) Compute the log probability under the model.
score_samples($X$) Return the likelihood of the data under the model.
set_params(**params) Set the parameters of this estimator.

__init__(*args, **kwargs)
DEPRECATED: The DPGMM class is not working correctly and it’s better to use sklearn.mixture.BayesianGaussianMixture class with parameter weight_concentration_prior_type='dirichlet_process' instead. DPGMM is deprecated in 0.18 and will be removed in 0.20.

aic($X$) Akaike information criterion for the current model fit and the proposed data.

Parameters $X$ : array of shape(n_samples, n_dimensions)

Returns aic : float (the lower the better)
bic($X$)
Bayesian information criterion for the current model fit and the proposed data.

**Parameters**  
X : array of shape(n_samples, n_dimensions)

**Returns**  
bic : float (the lower the better)

**fit**(X, y=None)

Estimate model parameters with the EM algorithm.

A initialization step is performed before entering the expectation-maximization (EM) algorithm. If you want to avoid this step, set the keyword argument init_params to the empty string ‘’ when creating the GMM object. Likewise, if you would like just to do an initialization, set n_iter=0.

**Parameters**  
X : array_like, shape (n, n_features)

**Returns**  
self

**fit_predict**(X, y=None)

Fit and then predict labels for data.

Warning: Due to the final maximization step in the EM algorithm, with low iterations the prediction may not be 100% accurate.

New in version 0.17: fit_predict method in Gaussian Mixture Model.

**Parameters**  
X : array-like, shape = [n_samples, n_features]

**Returns**  
C : array, shape = [n_samples,] component memberships

**get_params**(deep=True)

Get parameters for this estimator.

**Parameters**  
deep : boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**  
params : mapping of string to any

Parameter names mapped to their values.

**lower_bound**(X, z)

returns a lower bound on model evidence based on X and membership

**predict**(X)

Predict label for data.

**Parameters**  
X : array-like, shape = [n_samples, n_features]

**Returns**  
C : array, shape = [n_samples,] component memberships

**predict_proba**(X)

Predict posterior probability of data under each Gaussian in the model.

**Parameters**  
X : array-like, shape = [n_samples, n_features]

**Returns**  
responsibilities : array-like, shape = [n_samples, n_components]

Returns the probability of the sample for each Gaussian (state) in the model.

**sample**(n_samples=1, random_state=None)

Generate random samples from the model.

**Parameters**  
n_samples : int, optional

Number of samples to generate. Defaults to 1.

30.36. Recently deprecated
Returns X : array_like, shape (n_samples, n_features)
    List of samples

score(X, y=None)
Compute the log probability under the model.

Parameters X : array_like, shape (n_samples, n_features)
    List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
    Log probabilities of each data point in X

score_samples(X)
Return the likelihood of the data under the model.

Compute the bound on log probability of X under the model and return the posterior distribution (responsibilities) of each mixture component for each element of X.

This is done by computing the parameters for the mean-field of z for each observation.

Parameters X : array_like, shape (n_samples, n_features)
    List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
    Log probabilities of each data point in X
responsibilities : array_like, shape (n_samples, n_components)
    Posterior probabilities of each mixture component for each observation

set_params(**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form <component>__<parameter> so that it’s possible to update each component of a nested object.

Returns self

sklearn.mixture.GMM

Warning: DEPRECATED

class sklearn.mixture.GMM(*args, **kwargs)
Legacy Gaussian Mixture Model

Deprecated since version 0.18: This class will be removed in 0.20. Use sklearn.mixture.GaussianMixture instead.

Methods

aic(X)
Akaike information criterion for the current model fit and the proposed data.

Continued on next page
bic(X)  Bayesian information criterion for the current model fit and the proposed data.

fit(X[, y])  Estimate model parameters with the EM algorithm.

fit_predict(X[, y])  Fit and then predict labels for data.

get_params([deep])  Get parameters for this estimator.

predict(X)  Predict label for data.

predict_proba(X)  Predict posterior probability of data under each Gaussian in the model.

sample([n_samples, random_state])  Generate random samples from the model.

score(X[, y])  Compute the log probability under the model.

score_samples(X)  Return the per-sample likelihood of the data under the model.

set_params(**params)  Set the parameters of this estimator.

__init__(*args, **kwargs)
DEPRECATED: The class GMM is deprecated in 0.18 and will be removed in 0.20. Use class Gaussian-Mixture instead.

aic(X)  Akaike information criterion for the current model fit and the proposed data.

Parameters X : array of shape(n_samples, n_dimensions)

Returns aic : float (the lower the better)

bic(X)  Bayesian information criterion for the current model fit and the proposed data.

Parameters X : array of shape(n_samples, n_dimensions)

Returns bic : float (the lower the better)

fit(X, y=None)  Estimate model parameters with the EM algorithm.

A initialization step is performed before entering the expectation-maximization (EM) algorithm. If you want to avoid this step, set the keyword argument init_params to the empty string '' when creating the GMM object. Likewise, if you would like just to do an initialization, set n_iter=0.

Parameters X : array_like, shape = [n_samples, n_features]

List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns self

fit_predict(X, y=None)  Fit and then predict labels for data.

Warning: Due to the final maximization step in the EM algorithm, with low iterations the prediction may not be 100% accurate.

New in version 0.17: fit_predict method in Gaussian Mixture Model.

Parameters X : array-like, shape = [n_samples, n_features]

Returns C : array, shape = (n_samples,) component memberships

generate_sample([n_samples, random_state])
Get parameters for this estimator.

Parameters deep : boolean, optional
If True, will return the parameters for this estimator and contained subobjects that are estimators.

Returns params : mapping of string to any
Parameter names mapped to their values.

predict (X)
Predict label for data.

Parameters X : array-like, shape = [n_samples, n_features]

Returns C : array, shape = (n_samples,) component memberships

predict_proba (X)
Predict posterior probability of data under each Gaussian in the model.

Parameters X : array-like, shape = [n_samples, n_features]

Returns responsibilities : array-like, shape = (n_samples, n_components)
Returns the probability of the sample for each Gaussian (state) in the model.

sample (n_samples=1, random_state=None)
Generate random samples from the model.

Parameters n_samples : int, optional
   Number of samples to generate. Defaults to 1.

Returns X : array_like, shape (n_samples, n_features)
List of samples

score (X, y=None)
Compute the log probability under the model.

Parameters X : array_like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
Log probabilities of each data point in X

score_samples (X)
Return the per-sample likelihood of the data under the model.
Compute the log probability of X under the model and return the posterior distribution (responsibilities) of each mixture component for each element of X.

Parameters X : array_like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
Log probabilities of each data point in X.
responsibilities : array_like, shape (n_samples, n_components)
Posterior probabilities of each mixture component for each observation

set_params (**params)
Set the parameters of this estimator.
The method works on simple estimators as well as on nested objects (such as pipelines). The latter have parameters of the form `<component>__<parameter>` so that it's possible to update each component of a nested object.

**Returns** self

**sklearn.mixture.VBGMM**

### Warning: DEPRECATED

**class** sklearn.mixture.VBGMM(*args, **kwargs)**

Variational Inference for the Gaussian Mixture Model

Deprecated since version 0.18: This class will be removed in 0.20.

Use **sklearn.mixture.BayesianGaussianMixture** with parameter weight_concentration_prior_type='dirichlet_distribution' instead.

Variational inference for a Gaussian mixture model probability distribution. This class allows for easy and efficient inference of an approximate posterior distribution over the parameters of a Gaussian mixture model with a fixed number of components.

Initialization is with normally-distributed means and identity covariance, for proper convergence.

Read more in the **User Guide**.

**Parameters**

- **n_components**: int, default 1
  Number of mixture components.

- **covariance_type**: string, default 'diag'
  String describing the type of covariance parameters to use. Must be one of ‘spherical’, ‘tied’, ‘diag’, ‘full’.

- **alpha**: float, default 1
  Real number representing the concentration parameter of the dirichlet distribution. Intuitively, the higher the value of alpha the more likely the variational mixture of Gaussians model will use all components it can.

- **tol**: float, default 1e-3
  Convergence threshold.

- **n_iter**: int, default 10
  Maximum number of iterations to perform before convergence.

- **params**: string, default ‘wmc’
  Controls which parameters are updated in the training process. Can contain any combination of ‘w’ for weights, ‘m’ for means, and ‘c’ for covars.

- **init_params**: string, default ‘wmc’
  Controls which parameters are updated in the initialization process. Can contain any combination of ‘w’ for weights, ‘m’ for means, and ‘c’ for covars. Defaults to ‘wmc’.

- **verbose**: int, default 0
  Controls output verbosity.
Attributes

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<tr>
<td>covariance_type</td>
<td>(string) String describing the type of covariance parameters used by the DP-GMM. Must be one of 'spherical', 'tied', 'diag', 'full'.</td>
</tr>
<tr>
<td>n_features</td>
<td>Dimensionality of the Gaussians.</td>
</tr>
<tr>
<td>n_components</td>
<td>Number of mixture components.</td>
</tr>
<tr>
<td>weights</td>
<td>(array, shape (n_components,)) Mixing weights for each mixture component.</td>
</tr>
<tr>
<td>means</td>
<td>(array, shape (n_components, n_features)) Mean parameters for each mixture component.</td>
</tr>
<tr>
<td>precs_</td>
<td>(array) Precision (inverse covariance) parameters for each mixture component. The shape depends on covariance_type:: (n_components, 'n_features') if 'spherical', (n_features, n_features) if 'tied', (n_components, n_features) if 'diag', (n_components, n_features, n_features) if 'full'</td>
</tr>
<tr>
<td>converged_</td>
<td>(bool) True when convergence was reached in fit(), False otherwise.</td>
</tr>
</tbody>
</table>

See also:

**GMM** Finite Gaussian mixture model fit with EM

**DPGMM** Infinite Gaussian mixture model, using the dirichlet process, fit with a variational algorithm

Methods

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<td>Akaike information criterion for the current model fit and the proposed data.</td>
</tr>
<tr>
<td>bic(X)</td>
<td>Bayesian information criterion for the current model fit and the proposed data.</td>
</tr>
<tr>
<td>fit(X[, y])</td>
<td>Estimate model parameters with the EM algorithm.</td>
</tr>
<tr>
<td>fit_predict(X[, y])</td>
<td>Fit and then predict labels for data.</td>
</tr>
<tr>
<td>get_params([deep])</td>
<td>Get parameters for this estimator.</td>
</tr>
<tr>
<td>lower_bound(X, z)</td>
<td>Returns a lower bound on model evidence based on X and membership.</td>
</tr>
<tr>
<td>predict(X)</td>
<td>Predict label for data.</td>
</tr>
<tr>
<td>predict_proba(X)</td>
<td>Predict posterior probability of data under each Gaussian in the model.</td>
</tr>
<tr>
<td>sample([n_samples, random_state])</td>
<td>Generate random samples from the model.</td>
</tr>
<tr>
<td>score(X[, y])</td>
<td>Compute the log probability under the model.</td>
</tr>
<tr>
<td>score_samples(X)</td>
<td>Return the likelihood of the data under the model.</td>
</tr>
<tr>
<td>set_params(**params)</td>
<td>Set the parameters of this estimator.</td>
</tr>
</tbody>
</table>

__init__(**args, **kwargs)

DEPRECATED: The VBGMM class is not working correctly and it’s better to use sklearn.mixture.BayesianGaussianMixture class with parameter weight_concentration_prior_type=’dirichlet_distribution’ instead. VBGMM is deprecated in 0.18 and will be removed in 0.20.

aic(X)

Akaike information criterion for the current model fit and the proposed data.

Parameters X : array of shape(n_samples, n_dimensions)

Returns aic : float (the lower the better)
**bic**
Bayesian information criterion for the current model fit and the proposed data.

**Parameters**
- **X**: array of shape(n_samples, n_dimensions)

**Returns**
- **bic**: float (the lower the better)

**fit**
Estimate model parameters with the EM algorithm.

A initialization step is performed before entering the expectation-maximization (EM) algorithm. If you want to avoid this step, set the keyword argument init_params to the empty string '' when creating the GMM object. Likewise, if you would like just to do an initialization, set n_iter=0.

**Parameters**
- **X**: array_like, shape (n, n_features)

**Returns**
- **self**

**fit_predict**
Fit and then predict labels for data.

Warning: Due to the final maximization step in the EM algorithm, with low iterations the prediction may not be 100% accurate.

New in version 0.17: fit_predict method in Gaussian Mixture Model.

**Parameters**
- **X**: array-like, shape = [n_samples, n_features]

**Returns**
- **C**: array, shape = (n_samples,) component memberships

**get_params**
Get parameters for this estimator.

**Parameters**
- **deep**: boolean, optional

If True, will return the parameters for this estimator and contained subobjects that are estimators.

**Returns**
- **params**: mapping of string to any

Parameter names mapped to their values.

**lower_bound**
returns a lower bound on model evidence based on X and membership

**predict**
Predict label for data.

**Parameters**
- **X**: array-like, shape = [n_samples, n_features]

**Returns**
- **C**: array, shape = (n_samples,) component memberships

**predict_proba**
Predict posterior probability of data under each Gaussian in the model.

**Parameters**
- **X**: array-like, shape = [n_samples, n_features]

**Returns**
- **responsibilities**: array-like, shape = (n_samples, n_components)

Returns the probability of the sample for each Gaussian (state) in the model.

**sample**
Generate random samples from the model.

**Parameters**
- **n_samples**: int, optional

30.36. Recently deprecated
Number of samples to generate. Defaults to 1.

Returns X : array_like, shape (n_samples, n_features)

List of samples

score (X, y=None)
Compute the log probability under the model.

Parameters X : array_like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
Log probabilities of each data point in X

score_samples (X)
Return the likelihood of the data under the model.

Compute the bound on log probability of X under the model and return the posterior distribution (respon-
sibilities) of each mixture component for each element of X.

This is done by computing the parameters for the mean-field of z for each observation.

Parameters X : array_like, shape (n_samples, n_features)
List of n_features-dimensional data points. Each row corresponds to a single data point.

Returns logprob : array_like, shape (n_samples,)
Log probabilities of each data point in X

responsibilities : array_like, shape (n_samples, n_components)
Posterior probabilities of each mixture component for each observation

set_params (**params)
Set the parameters of this estimator.

The method works on simple estimators as well as on nested objects (such as pipelines). The latter have
data of the form <component>__<parameter> so that it’s possible to update each component
of a nested object.

Returns self

cross_validation.check_cv(cv[, X, y, classifier])
Input checker utility for building a CV in a user friendly
way.

cross_validation.cross_val_predict(estimator, Generate cross-validated estimates for each input data point
X)

cross_validation.cross_val_score(estimator, Evaluate a score by cross-validation
X)

cross_validation.permutation_test_score(...) Evaluate the significance of a cross-validated score with
permutations

cross_validation.train_test_split(*arrays, Split arrays or matrices into random train and test subsets
...

grid_search.fit_grid_point(X, y, estimator, Run fit on one set of parameters.
...

learning_curve.learning_curve(estimator, Learning curve.
X, y)

learning_curve.validation_curve(validator, Validation curve.
sklearn.cross_validation.check_cv

Warning: DEPRECATED

sklearn.cross_validation.check_cv(cv=X=None, y=None, classifier=False)
Input checker utility for building a CV in a user friendly way.

Deprecated since version 0.18: This module will be removed in 0.20. Use \texttt{sklearn.model_selection.check_cv} instead.

Parameters cv: int, cross-validation generator or an iterable, optional
Determines the cross-validation splitting strategy. Possible inputs for \texttt{cv} are:

- None, to use the default 3-fold cross-validation,
- integer, to specify the number of folds.
- An object to be used as a cross-validation generator.
- An iterable yielding train/test splits.

For integer/None inputs, if classifier is True and \texttt{y} is binary or multiclass, \texttt{StratifiedKFold} is used. In all other cases, \texttt{KFold} is used.

Refer \textit{User Guide} for the various cross-validation strategies that can be used here.

\texttt{X}: array-like
The data the cross-val object will be applied on.

\texttt{y}: array-like
The target variable for a supervised learning problem.

\texttt{classifier}: boolean optional
Whether the task is a classification task, in which case stratified \texttt{KFold} will be used.

Returns \texttt{checked_cv}: a cross-validation generator instance.

The return value is guaranteed to be a \texttt{cv} generator instance, whatever the input type.

sklearn.cross_validation.cross_val_predict

Warning: DEPRECATED

sklearn.cross_validation.cross_val_predict(estimator, X, y=None, cv=None, n_jobs=1, verbose=0, fit_params=None, pre_dispatch='2*n_jobs')
Generate cross-validated estimates for each input data point

Deprecated since version 0.18: This module will be removed in 0.20. Use \texttt{sklearn.model_selection.cross_val_predict} instead.

Read more in the \textit{User Guide}.

Parameters estimator: estimator object implementing ‘fit’ and ‘predict’
The object to use to fit the data.
X : array-like

The data to fit. Can be, for example a list, or an array at least 2d.

y : array-like, optional, default: None

The target variable to try to predict in the case of supervised learning.

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

• None, to use the default 3-fold cross-validation,
• integer, to specify the number of folds.
• An object to be used as a cross-validation generator.
• An iterable yielding train/test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multi-class, StratifiedKFold is used. In all other cases, KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

n_jobs : integer, optional

The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

verbose : integer, optional

The verbosity level.

fit_params : dict, optional

Parameters to pass to the fit method of the estimator.

pre_dispatch : int, or string, optional

Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:

• None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs
• An int, giving the exact number of total jobs that are spawned
• A string, giving an expression as a function of n_jobs, as in ‘2*n_jobs’

Returns preds : ndarray

This is the result of calling ‘predict’

Examples

```python
>>> from sklearn import datasets, linear_model
>>> from sklearn.cross_validation import cross_val_predict
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> y_pred = cross_val_predict(lasso, X, y)
```
**sklearn.cross_validation.cross_val_score**

**Warning**: DEPRECATED

`sklearn.cross_validation.cross_val_score(estimator, X, y=None, scoring=None, cv=None, n_jobs=1, verbose=0, fit_params=None, pre_dispatch='2*n_jobs')`

Evaluate a score by cross-validation

Deprecated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.cross_val_score` instead.

Read more in the User Guide.

**Parameters**

- **estimator**: estimator object implementing 'fit'
  
  The object to use to fit the data.

- **X**: array-like
  
  The data to fit. Can be, for example a list, or an array at least 2d.

- **y**: array-like, optional, default: None
  
  The target variable to try to predict in the case of supervised learning.

- **scoring**: string, callable or None, optional, default: None
  
  A string (see model evaluation documentation) or a scorer callable object / function with signature `scorer(estimator, X, y)`.

- **cv**: int, cross-validation generator or an iterable, optional
  
  Determines the cross-validation splitting strategy. Possible inputs for cv are:
  
  - None, to use the default 3-fold cross-validation,
  
  - integer, to specify the number of folds.
  
  - An object to be used as a cross-validation generator.
  
  - An iterable yielding train/test splits.
  
  For integer/None inputs, if the estimator is a classifier and y is either binary or multi-class, `StratifiedKFold` is used. In all other cases, `KFold` is used.
  
  Refer User Guide for the various cross-validation strategies that can be used here.

- **n_jobs**: integer, optional
  
  The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

- **verbose**: integer, optional
  
  The verbosity level.

- **fit_params**: dict, optional
  
  Parameters to pass to the fit method of the estimator.

- **pre_dispatch**: int, or string, optional
  
  Controls the number of jobs that get dispatched during parallel execution. Reducing this number can be useful to avoid an explosion of memory consumption when more jobs get dispatched than CPUs can process. This parameter can be:
None, in which case all the jobs are immediately created and spawned. Use this for lightweight and fast-running jobs, to avoid delays due to on-demand spawning of the jobs.

- An int, giving the exact number of total jobs that are spawned
- A string, giving an expression as a function of n_jobs, as in '2*n_jobs'

Returns scores : array of float, shape=(len(list(cv)),)

Array of scores of the estimator for each run of the cross validation.

See also:

sklearn.metrics.make_scorer Make a scorer from a performance metric or loss function.

Examples

```python
>>> from sklearn import datasets, linear_model
>>> from sklearn.cross_validation import cross_val_score
>>> diabetes = datasets.load_diabetes()
>>> X = diabetes.data[:150]
>>> y = diabetes.target[:150]
>>> lasso = linear_model.Lasso()
>>> print(cross_val_score(lasso, X, y))
[ 0.33150734 0.08022311 0.03531764]
```

sklearn.cross_validation.permutation_test_score

Warning: DEPRECATED

sklearn.cross_validation.permutation_test_score(estimator, X, y, cv=None, n_permutations=100, n_jobs=1, labels=None, random_state=0, verbose=0, scoring=None)

Evaluate the significance of a cross-validated score with permutations

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.permutation_test_score instead.

Read more in the User Guide.

Parameters estimator : estimator object implementing 'fit'

The object to use to fit the data.

X : array-like of shape at least 2D

The data to fit.

y : array-like

The target variable to try to predict in the case of supervised learning.

scoring : string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).
cv : int, cross-validation generator or an iterable, optional

  Determines the cross-validation splitting strategy. Possible inputs for cv are:
  • None, to use the default 3-fold cross-validation,
  • integer, to specify the number of folds.
  • An object to be used as a cross-validation generator.
  • An iterable yielding train/test splits.

  For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, StratifiedKFold is used. In all other cases, KFold is used.

  Refer User Guide for the various cross-validation strategies that can be used here.

n_permutations : integer, optional

  Number of times to permute y.

n_jobs : integer, optional

  The number of CPUs to use to do the computation. -1 means ‘all CPUs’.

labels : array-like of shape [n_samples] (optional)

  Labels constrain the permutation among groups of samples with a same label.

random_state : int, RandomState instance or None, optional (default=0)

  If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by np.random.

verbose : integer, optional

  The verbosity level.

Returns score : float

  The true score without permuting targets.

permutation_scores : array, shape (n_permutations,)

  The scores obtained for each permutations.

pvalue : float

  The p-value, which approximates the probability that the score would be obtained by chance. This is calculated as:

  \[(C + 1) / (n_permutations + 1)\]

  Where C is the number of permutations whose score \(\geq\) the true score.

  The best possible p-value is \(1/(n_permutations + 1)\), the worst is 1.0.

Notes

This function implements Test 1 in:


30.36. Recently deprecated
**sklearn.cross_validation.train_test_split**

*Warning: DEPRECATED*

**sklearn.cross_validation.train_test_split(*arrays, **options)**

Split arrays or matrices into random train and test subsets

Deprecated since version 0.18: This module will be removed in 0.20. Use `sklearn.model_selection.train_test_split` instead.

Quick utility that wraps input validation and `next(iter(ShuffleSplit(n_samples)))` and application to input data into a single call for splitting (and optionally subsampling) data in a oneliner.

Read more in the User Guide.

**Parameters**

- **arrays**: sequence of indexables with same length / shape[0]
  - Allowed inputs are lists, numpy arrays, scipy-sparse matrices or pandas dataframes.
- **test_size**: float, int, or None (default is None)
  - If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the test split. If int, represents the absolute number of test samples. If None, the value is automatically set to the complement of the train size. If train size is also None, test size is set to 0.25.
- **train_size**: float, int, or None (default is None)
  - If float, should be between 0.0 and 1.0 and represent the proportion of the dataset to include in the train split. If int, represents the absolute number of train samples. If None, the value is automatically set to the complement of the test size.
- **random_state**: int, RandomState instance or None, optional (default=None)
  - If int, random_state is the seed used by the random number generator; If RandomState instance, random_state is the random number generator; If None, the random number generator is the RandomState instance used by `np.random`.
- **stratify**: array-like or None (default is None)
  - If not None, data is split in a stratified fashion, using this as the labels array.

**Returns**

- **splitting**: list, length = 2 * len(arrays),
  - List containing train-test split of inputs.

New in version 0.16: If the input is sparse, the output will be a `scipy.sparse.csr_matrix`. Else, output type is the same as the input type.

**Examples**

```python
>>> import numpy as np
>>> from sklearn.cross_validation import train_test_split
>>> X, y = np.arange(10).reshape((5, 2)), range(5)
>>> X
array([(0, 1),
       [2, 3],
       [4, 5],...)```
>>> list(y)
[0, 1, 2, 3, 4]

>>> X_train, X_test, y_train, y_test = train_test_split(...
... X, y, test_size=0.33, random_state=42)
...
>>> X_train
array([[4, 5],
       [0, 1],
       [6, 7]])
>>> y_train
[2, 0, 3]
>>> X_test
array([[2, 3],
       [8, 9]])
>>> y_test
[1, 4]

**sklearn.grid_search.fit_grid_point**

---

**Warning**: DEPRECATED

sklearn.grid_search.**fit_grid_point** (X, y, estimator, parameters, train, test, scorer, verbose, error_score='raise', **fit_params)

Run fit on one set of parameters.

Deprecated since version 0.18: This module will be removed in 0.20. Use **sklearn.model_selection.fit_grid_point** instead.

**Parameters**

- **X**: array-like, sparse matrix or list
  
  Input data.
  
  - **y**: array-like or None
    
    Targets for input data.
  
  - **estimator**: estimator object
    
    A object of that type is instantiated for each grid point. This is assumed to implement the scikit-learn estimator interface. Either estimator needs to provide a `score` function, or `scoring` must be passed.
  
  - **parameters**: dict
    
    Parameters to be set on estimator for this grid point.
  
  - **train**: ndarray, dtype int or bool
    
    Boolean mask or indices for training set.
  
  - **test**: ndarray, dtype int or bool
    
    Boolean mask or indices for test set.
  
  - **scorer**: callable or None
If provided must be a scorer callable object / function with signature

caller(estimator, X, y).

verbose : int
Verbosity level.

**fit_params : kwargs

Additional parameter passed to the fit function of the estimator.

error_score : ‘raise’ (default) or numeric
Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the
error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter
does not affect the refit step, which will always raise the error.

Returns score : float
Score of this parameter setting on given training / test split.

parameters : dict
The parameters that have been evaluated.

n_samples_test : int
Number of test samples in this split.

sklearn.learning_curve.learning_curve

**Warning: DEPRECATED**

sklearn.learning_curve.learning_curve(estimator, X, y, train_sizes=arrray([ 0.1, 0.33,
0.55, 0.78, 1. ]), cv=None, scoring=None,
exploit_incremental_learning=False, n_jobs=1,
pre_dispatch=’all’, verbose=0, error_score=’raise’)

Learning curve.

Deprecated since version 0.18: This module will be removed in 0.20. Use sklearn.model_selection.
learning_curve instead.

Determines cross-validated training and test scores for different training set sizes.

A cross-validation generator splits the whole dataset k times in training and test data. Subsets of the training set
with varying sizes will be used to train the estimator and a score for each training subset size and the test set
will be computed. Afterwards, the scores will be averaged over all k runs for each training subset size.

Read more in the User Guide.

Parameters estimator : object type that implements the “fit” and “predict” methods

An object of that type which is cloned for each validation.

X : array-like, shape (n_samples, n_features)
Training vector, where n_samples is the number of samples and n_features is the number
of features.

y : array-like, shape (n_samples) or (n_samples, n_features), optional
Target relative to X for classification or regression; None for unsupervised learning.
train_sizes : array-like, shape (n_ticks,), dtype float or int

Relative or absolute numbers of training examples that will be used to generate the learning curve. If the dtype is float, it is regarded as a fraction of the maximum size of the training set (that is determined by the selected validation method), i.e. it has to be within (0, 1]. Otherwise it is interpreted as absolute sizes of the training sets. Note that for classification the number of samples usually have to be big enough to contain at least one sample from each class. (default: np.linspace(0.1, 1.0, 5))

cv : int, cross-validation generator or an iterable, optional

Determines the cross-validation splitting strategy. Possible inputs for cv are:

• None, to use the default 3-fold cross-validation,
• integer, to specify the number of folds.
• An object to be used as a cross-validation generator.
• An iterable yielding train/test splits.

For integer/None inputs, if the estimator is a classifier and y is either binary or multiclass, sklearn.model_selection.StratifiedKFold is used. In all other cases, sklearn.model_selection.KFold is used.

Refer User Guide for the various cross-validation strategies that can be used here.

scoring : string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature scorer(estimator, X, y).

exploit_incremental_learning : boolean, optional, default: False

If the estimator supports incremental learning, this will be used to speed up fitting for different training set sizes.

n_jobs : integer, optional

Number of jobs to run in parallel (default 1).

pre_dispatch : integer or string, optional

Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like ‘2*n_jobs’.

verbose : integer, optional

Controls the verbosity: the higher, the more messages.

error_score : ‘raise’ (default) or numeric

Value to assign to the score if an error occurs in estimator fitting. If set to ‘raise’, the error is raised. If a numeric value is given, FitFailedWarning is raised. This parameter does not affect the refit step, which will always raise the error.

Returns train_sizes_abs : array, shape = (n_unique_ticks,), dtype int

Numbers of training examples that has been used to generate the learning curve. Note that the number of ticks might be less than n_ticks because duplicate entries will be removed.

train_scores : array, shape (n_ticks, n_cv_folds)

Scores on training sets.

test_scores : array, shape (n_ticks, n_cv_folds)

30.36. Recently deprecated
Scores on test set.

**Notes**

See examples/model_selection/plot_learning_curve.py

```python
sklearn.learning_curve.validation_curve
```

**Warning: DEPRECATED**

Determine training and test scores for varying parameter values.

Compute scores for an estimator with different values of a specified parameter. This is similar to grid search with one parameter. However, this will also compute training scores and is merely a utility for plotting the results.

Read more in the User Guide.

**Parameters**

- `estimator`: object type that implements the “fit” and “predict” methods
  An object of that type which is cloned for each validation.

- `X`: array-like, shape (n_samples, n_features)
  Training vector, where n_samples is the number of samples and n_features is the number of features.

- `y`: array-like, shape (n_samples) or (n_samples, n_features), optional
  Target relative to X for classification or regression; None for unsupervised learning.

- `param_name`: string
  Name of the parameter that will be varied.

- `param_range`: array-like, shape (n_values,)
  The values of the parameter that will be evaluated.

- `cv`: int, cross-validation generator or an iterable, optional
  Determines the cross-validation splitting strategy. Possible inputs for `cv` are:
  - None, to use the default 3-fold cross-validation,
  - integer, to specify the number of folds.
  - An object to be used as a cross-validation generator.
  - An iterable yielding train/test splits.
For integer/None inputs, if the estimator is a classifier and \( y \) is either binary or multiclass, \( \textit{sklearn.model_selection.StratifiedKFold} \) is used. In all other cases, \( \textit{sklearn.model_selection.KFold} \) is used.

Refer \textit{User Guide} for the various cross-validation strategies that can be used here.

**scoring** : string, callable or None, optional, default: None

A string (see model evaluation documentation) or a scorer callable object / function with signature \( \text{scorer}(\text{estimator}, X, y) \).

**n_jobs** : integer, optional

Number of jobs to run in parallel (default 1).

**pre_dispatch** : integer or string, optional

Number of predispatched jobs for parallel execution (default is all). The option can reduce the allocated memory. The string can be an expression like ‘2*n_jobs’.

**verbose** : integer, optional

Controls the verbosity: the higher, the more messages.

Returns **train_scores** : array, shape (n_ticks, n_cv_folds)

Scores on training sets.

**test_scores** : array, shape (n_ticks, n_cv_folds)

Scores on test set.

**Notes**

See \textit{examples/model_selection/plot_validation_curve.py}
31.1 Contributing

This project is a community effort, and everyone is welcome to contribute.

The project is hosted on https://github.com/scikit-learn/scikit-learn

Scikit-learn is somewhat selective when it comes to adding new algorithms, and the best way to contribute and to help the project is to start working on known issues. See Issues for New Contributors to get started.

Our community, our values

We are a community based on openness and friendly, didactic, discussions.

We aspire to treat everybody equally, and value their contributions.

Decisions are made based on technical merit and consensus.

Code is not the only way to help the project. Reviewing pull requests, answering questions to help others on mailing lists or issues, organizing and teaching tutorials, working on the website, improving the documentation, are all priceless contributions.

We abide by the principles of openness, respect, and consideration of others of the Python Software Foundation: https://www.python.org/psf/codeofconduct/

31.1.1 Submitting a bug report

In case you experience issues using this package, do not hesitate to submit a ticket to the Bug Tracker. You are also welcome to post feature requests or pull requests.

31.1.2 Ways to contribute

There are many ways to contribute to scikit-learn, with the most common ones being contribution of code or documentation to the project. Improving the documentation is no less important than improving the library itself. If you find a typo in the documentation, or have made improvements, do not hesitate to send an email to the mailing list or preferably submit a GitHub pull request. Full documentation can be found under the doc/ directory.
But there are many other ways to help. In particular answering queries on the issue tracker, investigating bugs, and reviewing other developers’ pull requests are very valuable contributions that decrease the burden on the project maintainers.

Another way to contribute is to report issues you’re facing, and give a “thumbs up” on issues that others reported and that are relevant to you. It also helps us if you spread the word: reference the project from your blog and articles, link to it from your website, or simply say “I use it”:

### 31.1.3 Retrieving the latest code

We use Git for version control and GitHub for hosting our main repository.

You can check out the latest sources with the command:

```
git clone git://github.com/scikit-learn/scikit-learn.git
```

or if you have write privileges:

```
git clone git@github.com:scikit-learn/scikit-learn.git
```

If you run the development version, it is cumbersome to reinstall the package each time you update the sources. It is thus preferred that you add the scikit-learn directory to your PYTHONPATH and build the extension in place:

```
python setup.py build_ext --inplace
```

Another option is to install the package in editable mode if you change your code a lot and do not want to have to reinstall every time. This basically builds the extension in place and creates a link to the development directory (see the pip docs):

```
pip install --editable .
```

**Note:** This is fundamentally similar to using the command `python setup.py develop` (see the setuptools docs). It is however preferred to use pip.

**Note:** If you decide to do an editable install you have to rerun:

```
python setup.py build_ext --inplace
```

every time the source code of a compiled extension is changed (for instance when switching branches or pulling changes from upstream).

On Unix-like systems, you can simply type `make` in the top-level folder to build in-place and launch all the tests. Have a look at the `Makefile` for additional utilities.

### 31.1.4 Contributing code

**Note:** To avoid duplicating work, it is highly advised that you contact the developers on the mailing list before starting work on a non-trivial feature.

[https://mail.python.org/mailman/listinfo/scikit-learn](https://mail.python.org/mailman/listinfo/scikit-learn)
How to contribute

The preferred way to contribute to scikit-learn is to fork the main repository on GitHub, then submit a “pull request” (PR):

1. Create an account on GitHub if you do not already have one.
2. Fork the project repository: click on the ‘Fork’ button near the top of the page. This creates a copy of the code under your account on the GitHub server. For more details on how to fork a repository see this guide.
3. Clone this copy to your local disk:

   ```sh
   $ git clone git@github.com:YourLogin/scikit-learn.git
   ```

4. Create a branch to hold your changes:

   ```sh
   $ git checkout -b my-feature
   ```

   and start making changes. Never work in the master branch!

5. Work on this copy, on your computer, using Git to do the version control. When you’re done editing, do:

   ```sh
   $ git add modified_files
   $ git commit
   ```

   to record your changes in Git, then push them to GitHub with:

   ```sh
   $ git push -u origin my-feature
   ```

Finally, follow these instructions to create a pull request from your fork. This will send an email to the committers. You may want to consider sending an email to the mailing list for more visibility.

**Note:** In the above setup, your origin remote repository points to YourLogin/scikit-learn.git. If you wish to fetch/merge from the main repository instead of your forked one, you will need to add another remote to use instead of origin. If we choose the name upstream for it, the command will be:

```sh
$ git remote add upstream https://github.com/scikit-learn/scikit-learn.git
```

If any of the above seems like magic to you, then look up the Git documentation and the Git development workflow on the web.

If some conflicts arise between your branch and the master branch, you need to merge master. The command will be:

```sh
$ git merge master
```

with master being synchronized with the upstream.

Subsequently, you need to solve the conflicts. You can refer to the Git documentation related to resolving merge conflict using the command line.

**Note:** In the past, the policy to resolve conflicts was to rebase your branch on master. GitHub interface deals with merging master better than in the past.
Contributing pull requests

It is recommended to check that your contribution complies with the following rules before submitting a pull request:

- Follow the coding-guidelines (see below). To make sure that your PR does not add PEP8 violations you can run 
  ./build_tools/travis/flake8_diff.sh or make flake8-diff on a Unix-like system.

- When applicable, use the validation tools and other code in the sklearn.utils submodule. A list of utility
  routines available for developers can be found in the Utilities for Developers page.

- Give your pull request a helpful title that summarises what your contribution does. In some cases “Fix <ISSUE
  TITLE>” is enough. “Fix #<ISSUE NUMBER>” is not enough.

- Often pull requests resolve one or more other issues (or pull requests). If merging your pull request means that
  some other issues/PRs should be closed, you should use keywords to create link to them (e.g., Fixes #1234;
  multiple issues/PRs are allowed as long as each one is preceded by a keyword). Upon merging, those issues/PRs
  will automatically be closed by GitHub. If your pull request is simply related to some other issues/PRs, create a
  link to them without using the keywords (e.g., See also #1234).

- All public methods should have informative docstrings with sample usage presented as doctests when appropriate.

- Please prefix the title of your pull request with [MRG] if the contribution is complete and should be subjected
to a detailed review. Two core developers will review your code and change the prefix of the pull request to
[MRG + 1] and [MRG + 2] on approval, making it eligible for merging. An incomplete contribution –
where you expect to do more work before receiving a full review – should be prefixed [WIP] (to indicate
a work in progress) and changed to [MRG] when it matures. WIPs may be useful to: indicate you are working on
something to avoid duplicated work, request broad review of functionality or API, or seek collaborators. WIPs
often benefit from the inclusion of a task list in the PR description.

- All other tests pass when everything is rebuilt from scratch. On Unix-like systems, check with (from the toplevel
  source folder):

  $ make

- When adding additional functionality, provide at least one example script in the examples/ folder. Have
  a look at other examples for reference. Examples should demonstrate why the new functionality is useful in
  practice and, if possible, compare it to other methods available in scikit-learn.

- Documentation and high-coverage tests are necessary for enhancements to be accepted. Bug-fixes or new features
  should be provided with non-regression tests. These tests verify the correct behavior of the fix or feature.
  In this manner, further modifications on the code base are granted to be consistent with the desired behavior. For
  the case of bug fixes, at the time of the PR, the non-regression tests should fail for the code base in the master
  branch and pass for the PR code.

- At least one paragraph of narrative documentation with links to references in the literature (with PDF links when possible) and the example. For more details on writing and building the documentation, see the Documentation
  section. 

You can also check for common programming errors with the following tools:

- Code with a good unittest coverage (at least 90%, better 100%), check with:

  $ pip install nose coverage
  $ nosetests --with-coverage path/to/tests_for_package

  see also Testing and improving test coverage

- No pyflakes warnings, check with:
$ pip install pyflakes
$ pyflakes path/to/module.py

- No PEP8 warnings, check with:

  $ pip install pep8
  $ pep8 path/to/module.py

- AutoPEP8 can help you fix some of the easy redundant errors:

  $ pip install autopep8
  $ autopep8 path/to/pep8.py

Bonus points for contributions that include a performance analysis with a benchmark script and profiling output (please report on the mailing list or on the GitHub wiki).

Also check out the *How to optimize for speed* guide for more details on profiling and Cython optimizations.

**Note:** The current state of the scikit-learn code base is not compliant with all of those guidelines, but we expect that enforcing those constraints on all new contributions will get the overall code base quality in the right direction.

**Note:** For two very well documented and more detailed guides on development workflow, please pay a visit to the *Scipy Development Workflow - and the Astropy Workflow for Developers* sections.

### Continuous Integration (CI)

- Travis is used for testing on Linux platforms
- Appveyor is used for testing on Windows platforms
- CircleCI is used to build the docs for viewing

Please note that if one of the following markers appear in the latest commit message, the following actions are taken.

<table>
<thead>
<tr>
<th>Commit Message Marker</th>
<th>Action Taken by CI</th>
</tr>
</thead>
<tbody>
<tr>
<td><code>[ci skip]</code></td>
<td>CI is skipped completely</td>
</tr>
<tr>
<td><code>[doc skip]</code></td>
<td>Docs are not built</td>
</tr>
<tr>
<td><code>[doc quick]</code></td>
<td>Docs built, but excludes example gallery plots</td>
</tr>
<tr>
<td><code>[doc build]</code></td>
<td>Docs built including example gallery plots</td>
</tr>
</tbody>
</table>

### Filing Bugs

We use GitHub issues to track all bugs and feature requests; feel free to open an issue if you have found a bug or wish to see a feature implemented.

It is recommended to check that your issue complies with the following rules before submitting:

- Verify that your issue is not being currently addressed by other issues or pull requests.
- If you are submitting an algorithm or feature request, please verify that the algorithm fulfills our new algorithm requirements.
• Please ensure all code snippets and error messages are formatted in appropriate code blocks. See Creating and highlighting code blocks.

• Please include your operating system type and version number, as well as your Python, scikit-learn, numpy, and scipy versions. This information can be found by running the following code snippet:

```python
import platform; print(platform.platform())
import sys; print("Python", sys.version)
import numpy; print("NumPy", numpy.__version__)
import scipy; print("SciPy", scipy.__version__)
import sklearn; print("Scikit-Learn", sklearn.__version__)
```

• Please be specific about what estimators and/or functions are involved and the shape of the data, as appropriate; please include a reproducible code snippet or link to a gist. If an exception is raised, please provide the traceback.

### Issues for New Contributors

New contributors should look for the following tags when looking for issues. We strongly recommend that new contributors tackle “easy” issues first: this helps the contributor become familiar with the contribution workflow, and for the core devs to become acquainted with the contributor; besides which, we frequently underestimate how easy an issue is to solve!

**good first issue tag**

A great way to start contributing to scikit-learn is to pick an item from the list of good first issues in the issue tracker. Resolving these issues allow you to start contributing to the project without much prior knowledge. If you have already contributed to scikit-learn, you should look at Easy issues instead.

**Easy tag**

Another great way to contribute to scikit-learn is to pick an item from the list of Easy issues in the issue tracker. Your assistance in this area will be greatly appreciated by the more experienced developers as it helps free up their time to concentrate on other issues.

**help wanted tag**

We often use the help wanted tag to mark issues regardless of difficulty. Additionally, we use the help wanted tag to mark Pull Requests which have been abandoned by their original contributor and are available for someone to pick up where the original contributor left off. The list of issues with the help wanted tag can be found [here](#).

Note that not all issues which need contributors will have this tag.

### Documentation

We are glad to accept any sort of documentation: function docstrings, reStructuredText documents (like this one), tutorials, etc. reStructuredText documents live in the source code repository under the doc/ directory.

You can edit the documentation using any text editor, and then generate the HTML output by typing `make html` from the doc/ directory. Alternatively, `make html-noplot` can be used to quickly generate the documentation without
the example gallery. The resulting HTML files will be placed in _build/html/ and are viewable in a web browser. See the README file in the doc/ directory for more information.

For building the documentation, you will need **sphinx**, **matplotlib** and **pillow**.

**When you are writing documentation**, it is important to keep a good compromise between mathematical and algorithmic details, and give intuition to the reader on what the algorithm does.

Basically, to elaborate on the above, it is best to always start with a small paragraph with a hand-waving explanation of what the method does to the data. Then, it is very helpful to point out why the feature is useful and when it should be used - the latter also including “big O” \(O(g(n))\) complexities of the algorithm, as opposed to just rules of thumb, as the latter can be very machine-dependent. If those complexities are not available, then rules of thumb may be provided instead.

Secondly, a generated figure from an example (as mentioned in the previous paragraph) should then be included to further provide some intuition.

Next, one or two small code examples to show its use can be added.

Next, any math and equations, followed by references, can be added to further the documentation. Not starting the documentation with the maths makes it more friendly towards users that are just interested in what the feature will do, as opposed to how it works “under the hood”.

You may also be asked to show your changes when it’s built. When you create a pull request or make changes in an existing one modifying the docs, CircleCI automatically builds them. Thus, you can easily view your changes in the built artifacts using the following URL:

http://scikit-learn.org/circle?{BUILD_NUMBER}

We attempt to assemble a more precise set of changed files in the documentation at:

http://scikit-learn.org/circle?{BUILD_NUMBER}/_changed.html

Note: When you visit the details page of the CircleCI tests, you can find your BUILD_NUMBER mentioned as ‘build #’ which is different from your pull request number, which is presented as ‘pull/#’.

Finally, follow the formatting rules below to make it consistently good:

- Add “See also” in docstrings for related classes/functions.
- “See also” in docstrings should be one line per reference, with a colon and an explanation, for example:

```
See also
--------
SelectKBest : Select features based on the k highest scores.
SelectFpr : Select features based on a false positive rate test.
```

- For unwritten formatting rules, try to follow existing good works:
  
  - For “References” in docstrings, see the Silhouette Coefficient (sklearn.metrics.silhouette_score).

**Warning: Sphinx version**

While we do our best to have the documentation build under as many versions of Sphinx as possible, the different versions tend to behave slightly differently. To get the best results, you should use the same version as the one we used on CircleCI. Look at this github search to know the exact version.
Testing and improving test coverage

High-quality unit testing is a corner-stone of the scikit-learn development process. For this purpose, we use the nose package. The tests are functions appropriately named, located in tests subdirectories, that check the validity of the algorithms and the different options of the code.

The full scikit-learn tests can be run using ‘make’ in the root folder. Alternatively, running ‘nosetests’ in a folder will run all the tests of the corresponding subpackages.

We expect code coverage of new features to be at least around 90%.

Note: Workflow to improve test coverage

To test code coverage, you need to install the coverage package in addition to nose.

1. Run ‘make test-coverage’. The output lists for each file the line numbers that are not tested.
2. Find a low hanging fruit, looking at which lines are not tested, write or adapt a test specifically for these lines.
3. Loop.

Developers web site

More information can be found on the developer’s wiki.

Issue Tracker Tags

All issues and pull requests on the GitHub issue tracker should have (at least) one of the following tags:

- **Bug / Crash** Something is happening that clearly shouldn’t happen. Wrong results as well as unexpected errors from estimators go here.
- **Cleanup / Enhancement** Improving performance, usability, consistency.
- **Documentation** Missing, incorrect or sub-standard documentations and examples.
- **New Feature** Feature requests and pull requests implementing a new feature.

There are four other tags to help new contributors:

- **good first issue** This issue is ideal for a first contribution to scikit-learn. Ask for help if the formulation is unclear. If you have already contributed to scikit-learn, look at Easy issues instead.
- **Easy** This issue can be tackled without much prior experience.
- **Moderate** Might need some knowledge of machine learning or the package, but is still approachable for someone new to the project.
- **help wanted** This tag marks an issue which currently lacks a contributor or a PR that needs another contributor to take over the work. These issues can range in difficulty, and may not be approachable for new contributors. Note that not all issues which need contributors will have this tag.

### 31.1.5 Coding guidelines

The following are some guidelines on how new code should be written. Of course, there are special cases and there will be exceptions to these rules. However, following these rules when submitting new code makes the review easier so new code can be integrated in less time.
Uniformly formatted code makes it easier to share code ownership. The scikit-learn project tries to closely follow the official Python guidelines detailed in PEP8 that detail how code should be formatted and indented. Please read it and follow it.

In addition, we add the following guidelines:

- Use underscores to separate words in non class names: n_samples rather than nsamples.
- Avoid multiple statements on one line. Prefer a line return after a control flow statement (if/for).
- Use relative imports for references inside scikit-learn.
- Unit tests are an exception to the previous rule; they should use absolute imports, exactly as client code would. A corollary is that, if sklearn.foo exports a class or function that is implemented in sklearn.foo.bar.baz, the test should import it from sklearn.foo.
- Please don’t use import * in any case. It is considered harmful by the official Python recommendations. It makes the code harder to read as the origin of symbols is no longer explicitly referenced, but most important, it prevents using a static analysis tool like pyflakes to automatically find bugs in scikit-learn.
- Use the numpy docstring standard in all your docstrings.

A good example of code that we like can be found here.

**Input validation**

The module sklearn.utils contains various functions for doing input validation and conversion. Sometimes, np.asarray suffices for validation; do not use np.asanyarray or np.atleast_2d, since those let NumPy’s np.matrix through, which has a different API (e.g., * means dot product on np.matrix, but Hadamard product on np.ndarray).

In other cases, be sure to call check_array on any array-like argument passed to a scikit-learn API function. The exact parameters to use depends mainly on whether and which scipy.sparse matrices must be accepted.

For more information, refer to the Utilities for Developers page.

**Random Numbers**

If your code depends on a random number generator, do not use numpy.random.random() or similar routines. To ensure repeatability in error checking, the routine should accept a keyword random_state and use this to construct a numpy.random.RandomState object. See sklearn.utils.check_random_state in Utilities for Developers.

Here’s a simple example of code using some of the above guidelines:

```python
from sklearn.utils import check_array, check_random_state

def choose_random_sample(X, random_state=0):
    """
    Choose a random point from X
    
    Parameters
    ----------
    X : array-like, shape = (n_samples, n_features)
        array representing the data
    random_state : RandomState or an int seed (0 by default)
        A random number generator instance to define the state of the
        random permutations generator.
    """
```

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If you use randomness in an estimator instead of a freestanding function, some additional guidelines apply.

First off, the estimator should take a random_state argument to its __init__ with a default value of None. It should store that argument’s value, unmodified, in an attribute random_state. fit can call check_random_state on that attribute to get an actual random number generator. If, for some reason, randomness is needed after fit, the RNG should be stored in an attribute random_state_. The following example should make this clear:

```python
class GaussianNoise(BaseEstimator, TransformerMixin):
    """This estimator ignores its input and returns random Gaussian noise.
    It also does not adhere to all scikit-learn conventions,
    but showcases how to handle randomness."
    
    def __init__(self, n_components=100, random_state=None):
        self.random_state = random_state

        # the arguments are ignored anyway, so we make them optional
        def fit(self, X=None, y=None):
            self.random_state_ = check_random_state(self.random_state)

        def transform(self, X):
            n_samples = X.shape[0]
            return self.random_state_.randn(n_samples, n_components)
```

The reason for this setup is reproducibility: when an estimator is fit twice to the same data, it should produce an identical model both times, hence the validation in fit, not __init__.

**Deprecation**

If any publicly accessible method, function, attribute or parameter is renamed, we still support the old one for two releases and issue a deprecation warning when it is called/passed/accessed. E.g., if the function zero_one is renamed to zero_one_loss, we add the decorator deprecated (from sklearn.utils) to zero_one and call zero_one_loss from that function:

```python
from ..utils import deprecated

def zero_one_loss(y_true, y_pred, normalize=True):
    # actual implementation
    pass

@deprecated("Function 'zero_one' was renamed to 'zero_one_loss' "
            "in version 0.13 and will be removed in release 0.15. "
            "Default behavior is changed from 'normalize=False' to "
            "'normalize=True'")
```
def zero_one(y_true, y_pred, normalize=False):
    return zero_one_loss(y_true, y_pred, normalize)

If an attribute is to be deprecated, use the decorator deprecated on a property. E.g., renaming an attribute labels_ to classes_ can be done as:

@property
@deprecated("Attribute labels_ was deprecated in version 0.13 and "
           "will be removed in 0.15. Use 'classes_' instead")
def labels_(self):
    return self.classes_

If a parameter has to be deprecated, use DeprecationWarning appropriately. In the following example, k is deprecated and renamed to n_clusters:

import warnings
def example_function(n_clusters=8, k=None):
    if k is not None:
        warnings.warn("'k' was renamed to n_clusters in version 0.13 and "
                      "will be removed in 0.15.", DeprecationWarning)
    n_clusters = k

As in these examples, the warning message should always give both the version in which the deprecation happened and the version in which the old behavior will be removed. If the deprecation happened in version 0.x-dev, the message should say deprecation occurred in version 0.x and the removal will be in 0.(x+2). For example, if the deprecation happened in version 0.18-dev, the message should say it happened in version 0.18 and the old behavior will be removed in version 0.20.

In addition, a deprecation note should be added in the docstring, recalling the same information as the deprecation warning as explained above. Use the .. deprecated:: directive:

.. deprecated:: 0.13
    `k` was renamed to `n_clusters` in version 0.13 and will be removed in 0.15.

Python versions supported

All scikit-learn code should work unchanged in both Python 2.7 and 3.4 or newer. Since Python 3.x is not backwards compatible, that may require changes to code and it certainly requires testing on both 2.7 and 3.4 or newer.

For most numerical algorithms, Python 3.x support is easy: just remember that print is a function and integer division is written `/`. String handling has been overhauled, though, as have parts of the Python standard library. The six package helps with cross-compatibility and is included in scikit-learn as sklearn.externals.six.

31.1.6 Code Review Guidelines

Reviewing code contributed to the project as PRs is a crucial component of scikit-learn development. We encourage anyone to start reviewing code of other developers. The code review process is often highly educational for everybody involved. This is particularly appropriate if it is a feature you would like to use, and so can respond critically about whether the PR meets your needs. While each pull request needs to be signed off by two core developers, you can speed up this process by providing your feedback.

Here are a few important aspects that need to be covered in any code review, from high-level questions to a more detailed check-list.

31.1. Contributing
• Do we want this in the library? Is it likely to be used? Do you, as a scikit-learn user, like the change and intend to use it? Is it in the scope of scikit-learn? Will the cost of maintaining a new feature be worth its benefits?

• Is the code consistent with the API of scikit-learn? Are public functions/classes/parameters well named and intuitively designed?

• Are all public functions/classes and their parameters, return types, and stored attributes named according to scikit-learn conventions and documented clearly?

• Is any new functionality described in the user-guide and illustrated with examples?

• Is every public function/class tested? Are a reasonable set of parameters, their values, value types, and combinations tested? Do the tests validate that the code is correct, i.e. doing what the documentation says it does? If the change is a bug-fix, is a non-regression test included? Look at this to get started with testing in Python.

• Do the tests pass in the continuous integration build? If appropriate, help the contributor understand why tests failed.

• Do the tests cover every line of code (see the coverage report in the build log)? If not, are the lines missing coverage good exceptions?

• Is the code easy to read and low on redundancy? Should variable names be improved for clarity or consistency? Should comments be added? Should comments be removed as unhelpful or extraneous?

• Could the code easily be rewritten to run much more efficiently for relevant settings?

• Is the code backwards compatible with previous versions? (or is a deprecation cycle necessary?)

• Will the new code add any dependencies on other libraries? (this is unlikely to be accepted)

• Does the documentation render properly (see the Documentation section for more details), and are the plots instructive?

31.1.7 APIs of scikit-learn objects

To have a uniform API, we try to have a common basic API for all the objects. In addition, to avoid the proliferation of framework code, we try to adopt simple conventions and limit to a minimum the number of methods an object must implement.

Different objects

The main objects in scikit-learn are (one class can implement multiple interfaces):

**Estimator** The base object, implements a fit method to learn from data, either:

```
estimator = obj.fit(data, targets)
```

or:

```
estimator = obj.fit(data)
```

**Predictor** For supervised learning, or some unsupervised problems, implements:

```
prediction = obj.predict(data)
```

Classification algorithms usually also offer a way to quantify certainty of a prediction, either using decision_function or predict_proba:
probabiliity = obj.predict_proba(data)

**Transformer** For filtering or modifying the data, in a supervised or unsupervised way, implements:

new_data = obj.transform(data)

When fitting and transforming can be performed much more efficiently together than separately, implements:

new_data = obj.fit_transform(data)

**Model** A model that can give a **goodness of fit** measure or a likelihood of unseen data, implements (higher is better):

score = obj.score(data)

---

**Estimators**

The API has one predominant object: the estimator. A estimator is an object that fits a model based on some training data and is capable of inferring some properties on new data. It can be, for instance, a classifier or a regressor. All estimators implement the fit method:

```python
estimator.fit(X, y)
```

All built-in estimators also have a `set_params` method, which sets data-independent parameters (overriding previous parameter values passed to `__init__`).

All estimators in the main scikit-learn codebase should inherit from `sklearn.base.BaseEstimator`.

---

**Instantiation**

This concerns the creation of an object. The object’s `__init__` method might accept constants as arguments that determine the estimator’s behavior (like the C constant in SVMs). It should not, however, take the actual training data as an argument, as this is left to the `fit()` method:

```python
clf2 = SVC(C=2.3)
clf3 = SVC([[1, 2], [2, 3]], [-1, 1]) # WRONG!
```

The arguments accepted by `__init__` should all be keyword arguments with a default value. In other words, a user should be able to instantiate an estimator without passing any arguments to it. The arguments should all correspond to hyperparameters describing the model or the optimisation problem the estimator tries to solve. These initial arguments (or parameters) are always remembered by the estimator. Also note that they should not be documented under the “Attributes” section, but rather under the “Parameters” section for that estimator.

In addition, **every keyword argument accepted by `__init__` should correspond to an attribute on the instance**. Scikit-learn relies on this to find the relevant attributes to set on an estimator when doing model selection.

To summarize, an `__init__` should look like:

```python
def __init__(self, param1=1, param2=2):
    self.param1 = param1
    self.param2 = param2
```

There should be no logic, not even input validation, and the parameters should not be changed. The corresponding logic should be put where the parameters are used, typically in `fit`. The following is wrong:

---

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def __init__(self, param1=1, param2=2, param3=3):
    # WRONG: parameters should not be modified
    if param1 > 1:
        param2 += 1
    self.param1 = param1
    # WRONG: the object's attributes should have exactly the name of
    # the argument in the constructor
    self.param3 = param2

The reason for postponing the validation is that the same validation would have to be performed in `set_params`, which is used in algorithms like `GridSearchCV`.

**Fitting**

The next thing you will probably want to do is to estimate some parameters in the model. This is implemented in the `fit()` method.

The `fit()` method takes the training data as arguments, which can be one array in the case of unsupervised learning, or two arrays in the case of supervised learning.

Note that the model is fitted using X and y, but the object holds no reference to X and y. There are, however, some exceptions to this, as in the case of precomputed kernels where this data must be stored for use by the predict method.

### Parameters

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>X</td>
<td>array-like, with shape = [N, D], where N is the number of samples and D is the number of features.</td>
</tr>
<tr>
<td>y</td>
<td>array, with shape = [N], where N is the number of samples.</td>
</tr>
<tr>
<td>kwargs</td>
<td>optional data-dependent parameters.</td>
</tr>
</tbody>
</table>

`X.shape[0]` should be the same as `y.shape[0]`. If this requisite is not met, an exception of type `ValueError` should be raised.

`y` might be ignored in the case of unsupervised learning. However, to make it possible to use the estimator as part of a pipeline that can mix both supervised and unsupervised transformers, even unsupervised estimators need to accept a `y=None` keyword argument in the second position that is just ignored by the estimator. For the same reason, `fit_predict`, `fit_transform`, `score` and `partial_fit` methods need to accept a `y` argument in the second place if they are implemented.

The method should return the object (`self`). This pattern is useful to be able to implement quick one liners in an IPython session such as:

```python
y_predicted = SVC(C=100).fit(X_train, y_train).predict(X_test)
```

Depending on the nature of the algorithm, `fit` can sometimes also accept additional keywords arguments. However, any parameter that can have a value assigned prior to having access to the data should be an `__init__` keyword argument. **Fit parameters should be restricted to directly data dependent variables.** For instance a Gram matrix or an affinity matrix which are precomputed from the data matrix `X` are data dependent. A tolerance stopping criterion `tol` is not directly data dependent (although the optimal value according to some scoring function probably is).

**Estimated Attributes**

Attributes that have been estimated from the data must always have a name ending with trailing underscore, for example the coefficients of some regression estimator would be stored in a `coef_` attribute after `fit` has been called.
The last-mentioned attributes are expected to be overridden when you call `fit` a second time without taking any previous value into account: **fit should be idempotent**.

### Optional Arguments

In iterative algorithms, the number of iterations should be specified by an integer called `n_iter`.

#### 31.1.8 Rolling your own estimator

If you want to implement a new estimator that is scikit-learn-compatible, whether it is just for you or for contributing it to scikit-learn, there are several internals of scikit-learn that you should be aware of in addition to the scikit-learn API outlined above. You can check whether your estimator adheres to the scikit-learn interface and standards by running `utils.estimator_checks.check_estimator` on the class:

```python
>>> from sklearn.utils.estimator_checks import check_estimator
>>> from sklearn.svm import LinearSVC
>>> check_estimator(LinearSVC)  # passes
```

The main motivation to make a class compatible to the scikit-learn estimator interface might be that you want to use it together with model evaluation and selection tools such as `model_selection.GridSearchCV` and `pipeline.Pipeline`.

Before detailing the required interface below, we describe two ways to achieve the correct interface more easily.

### Project template:

We provide a [project template](#) which helps in the creation of Python packages containing scikit-learn compatible estimators. It provides:

- an initial git repository with Python package directory structure
- a template of a scikit-learn estimator
- an initial test suite including use of `check_estimator`
- directory structures and scripts to compile documentation and example galleries
- scripts to manage continuous integration (testing on Linux and Windows)
- instructions from getting started to publishing on PyPi

### BaseEstimator and mixins:

We tend to use use “duck typing”, so building an estimator which follows the API suffices for compatibility, without needing to inherit from or even import any scikit-learn classes.

However, if a dependency on scikit-learn is acceptable in your code, you can prevent a lot of boilerplate code by deriving a class from `BaseEstimator` and optionally the mixin classes in `sklearn.base`. For example, below is a custom classifier, with more examples included in the scikit-learn-contrib project template.
>>> import numpy as np
>>> from sklearn.base import BaseEstimator, ClassifierMixin
>>> from sklearn.utils.validation import check_X_y, check_array, check_is_fitted
>>> from sklearn.utils.multiclass import unique_labels
>>> from sklearn.metrics import euclidean_distances

class TemplateClassifier(BaseEstimator, ClassifierMixin):
    def __init__(self, demo_param='demo'):
        self.demo_param = demo_param

    def fit(self, X, y):
        # Check that X and y have correct shape
        X, y = check_X_y(X, y)
        # Store the classes seen during fit
        self.classes_ = unique_labels(y)

        self.X_ = X
        self.y_ = y
        # Return the classifier
        return self

    def predict(self, X):
        # Check if fit had been called
        check_is_fitted(self, ['X_', 'y_'])

        # Input validation
        X = check_array(X)

        closest = np.argmin(euclidean_distances(X, self.X_), axis=1)
        return self.y_[closest]

get_params and set_params

All scikit-learn estimators have get_params and set_params functions. The get_params function takes no arguments and returns a dict of the __init__ parameters of the estimator, together with their values. It must take one keyword argument, deep, which receives a boolean value that determines whether the method should return the parameters of sub-estimators (for most estimators, this can be ignored). The default value for deep should be true.

The set_params on the other hand takes as input a dict of the form 'parameter': value and sets the parameter of the estimator using this dict. Return value must be estimator itself.

While the get_params mechanism is not essential (see Cloning below), the set_params function is necessary as it is used to set parameters during grid searches.

The easiest way to implement these functions, and to get a sensible __repr__ method, is to inherit from sklearn.base.BaseEstimator. If you do not want to make your code dependent on scikit-learn, the easiest way to implement the interface is:

def get_params(self, deep=True):
    # suppose this estimator has parameters "alpha" and "recursive"
    return {'alpha': self.alpha, 'recursive': self.recursive}
def set_params(self, **parameters):
    for parameter, value in parameters.items():
**Parameters and init**

As `model_selection.GridSearchCV` uses `set_params` to apply parameter setting to estimators, it is essential that calling `set_params` has the same effect as setting parameters using the `__init__` method. The easiest and recommended way to accomplish this is to **not do any parameter validation in `__init__`**. All logic behind estimator parameters, like translating string arguments into functions, should be done in `fit`.

Also it is expected that parameters with trailing `_` are **not to be set inside the `__init__` method**. All and only the public attributes set by `fit` have a trailing `_`. As a result the existence of parameters with trailing `_` is used to check if the estimator has been fitted.

**Cloning**

For use with the `model_selection` module, an estimator must support the `base.clone` function to replicate an estimator. This can be done by providing a `get_params` method. If `get_params` is present, then `clone(estimator)` will be an instance of `type(estimator)` on which `set_params` has been called with clones of the result of `estimator.get_params()`.

Objects that do not provide this method will be deep-copied (using the Python standard function `copy.deepcopy`) if `safe=False` is passed to `clone`.

**Pipeline compatibility**

For an estimator to be usable together with `pipeline.Pipeline` in any but the last step, it needs to provide a `fit` or `fit_transform` function. To be able to evaluate the pipeline on any data but the training set, it also needs to provide a `transform` function. There are no special requirements for the last step in a pipeline, except that it has a `fit` function. All `fit` and `fit_transform` functions must take arguments `X, y`, even if `y` is not used. Similarly, for `score` to be usable, the last step of the pipeline needs to have a `score` function that accepts an optional `y`.

**Estimator types**

Some common functionality depends on the kind of estimator passed. For example, cross-validation in `model_selection.GridSearchCV` and `model_selection.cross_val_score` defaults to being stratified when used on a classifier, but not otherwise. Similarly, scorers for average precision that take a continuous prediction need to call `decision_function` for classifiers, but `predict` for regressors. This distinction between classifiers and regressors is implemented using the `_estimator_type` attribute, which takes a string value. It should be "classifier" for classifiers and "regressor" for regressors and "clusterer" for clustering methods, to work as expected. Inheriting from `ClassifierMixin`, `RegressorMixin` or `ClusterMixin` will set the attribute automatically.

**Working notes**

For unresolved issues, TODOs, and remarks on ongoing work, developers are advised to maintain notes on the GitHub wiki.
Specific models

Classifiers should accept \( y \) (target) arguments to `fit` that are sequences (lists, arrays) of either strings or integers. They should not assume that the class labels are a contiguous range of integers; instead, they should store a list of classes in a `classes_` attribute or property. The order of class labels in this attribute should match the order in which `predict_proba`, `predict_log_proba` and `decision_function` return their values. The easiest way to achieve this is to put:

```
self.classes_, y = np.unique(y, return_inverse=True)
```

in `fit`. This returns a new \( y \) that contains class indexes, rather than labels, in the range \([0, n\_classes)\).

A classifier's `predict` method should return arrays containing class labels from `classes_`. In a classifier that implements `decision_function`, this can be achieved with:

```python
def predict(self, X):
    D = self.decision_function(X)
    return self.classes_[np.argmax(D, axis=1)]
```

In linear models, coefficients are stored in an array called `coef_`, and the independent term is stored in `intercept_`. `sklearn.linear_model.base` contains a few base classes and mixins that implement common linear model patterns.

The `sklearn.utils.multiclass` module contains useful functions for working with multiclass and multilabel problems.

31.2 Developers' Tips and Tricks

31.2.1 Productivity and sanity-preserving tips

In this section we gather some useful advice and tools that may increase your quality-of-life when reviewing pull requests, running unit tests, and so forth. Some of these tricks consist of userscripts that require a browser extension such as TamperMonkey or GreaseMonkey; to set up userscripts you must have one of these extensions installed, enabled and running. We provide userscripts as GitHub gists; to install them, click on the “Raw” button on the gist page.

**Viewing the rendered HTML documentation for a pull request**

We use CircleCI to build the HTML documentation for every pull request. To access that documentation, we provide a redirect as described in the documentation section of the contributor guide. Instead of typing the address by hand, we provide a userscript that adds a button to every PR. After installing the userscript, navigate to any GitHub PR; a new button labeled “See CircleCI doc for this PR” should appear in the top-right area.

**Folding and unfolding outdated diffs on pull requests**

GitHub hides discussions on PRs when the corresponding lines of code have been changed in the mean while. This userscript provides a button to unfold all such hidden discussions at once, so you can catch up.

**Checking out pull requests as remote-tracking branches**

In your local fork, add to your `.git/config`, under the `[remote "upstream"]` heading, the line:
You may then use `git checkout pr/PR_NUMBER` to navigate to the code of the pull-request with the given number. (Read more in this gist.)

**Display code coverage in pull requests**

To overlay the code coverage reports generated by the CodeCov continuous integration, consider this browser extension. The coverage of each line will be displayed as a color background behind the line number.

**Useful pytest aliases and flags**

We recommend using pytest to run unit tests. When a unit tests fail, the following tricks can make debugging easier:

1. The command line argument `pytest -l` instructs pytest to print the local variables when a failure occurs.
2. The argument `pytest --pdb` drops into the Python debugger on failure. To instead drop into the rich IPython debugger `ipdb`, you may set up a shell alias to:
   ```bash
   pytest --pdbcls=IPython.terminal.debugger:TerminalPdb --capture no
   ```

**31.2.2 Debugging memory errors in Cython with valgrind**

While python/numpy’s built-in memory management is relatively robust, it can lead to performance penalties for some routines. For this reason, much of the high-performance code in scikit-learn in written in cython. This performance gain comes with a tradeoff, however: it is very easy for memory bugs to crop up in cython code, especially in situations where that code relies heavily on pointer arithmetic.

Memory errors can manifest themselves a number of ways. The easiest ones to debug are often segmentation faults and related glibc errors. Uninitialized variables can lead to unexpected behavior that is difficult to track down. A very useful tool when debugging these sorts of errors is **valgrind**.

Valgrind is a command-line tool that can trace memory errors in a variety of code. Follow these steps:

1. Install `valgrind` on your system.
2. Download the python valgrind suppression file: `valgrind-python.supp`.
3. Follow the directions in the `README.valgrind` file to customize your python suppressions. If you don’t, you will have spurious output coming related to the python interpreter instead of your own code.
4. Run `valgrind` as follows:
   ```bash
   $> valgrind --suppressions=valgrind-python.supp python my_test_script.py
   ```

The result will be a list of all the memory-related errors, which reference lines in the C-code generated by cython from your .pyx file. If you examine the referenced lines in the .c file, you will see comments which indicate the corresponding location in your .pyx source file. Hopefully the output will give you clues as to the source of your memory error.

For more information on valgrind and the array of options it has, see the tutorials and documentation on the valgrind web site.
31.3 Utilities for Developers

Scikit-learn contains a number of utilities to help with development. These are located in `sklearn.utils`, and include tools in a number of categories. All the following functions and classes are in the module `sklearn.utils`.

**Warning:** These utilities are meant to be used internally within the scikit-learn package. They are not guaranteed to be stable between versions of scikit-learn. Backports, in particular, will be removed as the scikit-learn dependencies evolve.

### 31.3.1 Validation Tools

These are tools used to check and validate input. When you write a function which accepts arrays, matrices, or sparse matrices as arguments, the following should be used when applicable.

- **assert_all_finite**: Throw an error if array contains NaNs or Infs.
- **as_float_array**: convert input to an array of floats. If a sparse matrix is passed, a sparse matrix will be returned.
- **check_array**: convert input to 2d array, raise error on sparse matrices. Allowed sparse matrix formats can be given optionally, as well as allowing 1d or nd arrays. Calls `assert_all_finite` by default.
- **check_X_y**: check that X and y have consistent length, calls check_array on X, and column_or_1d on y. For multilabel classification or multitarget regression, specify multi_output=True, in which case check_array will be called on y.
- **indexable**: check that all input arrays have consistent length and can be sliced or indexed using safe_index. This is used to validate input for cross-validation.
- **validation.check_memory** checks that input is `joblib.Memory`-like, which means that it can be converted into a `sklearn.externals.joblib.Memory` instance (typically a str denoting the cachedir) or has the same interface.

If your code relies on a random number generator, it should never use functions like `numpy.random.random` or `numpy.random.normal`. This approach can lead to repeatability issues in unit tests. Instead, a `numpy.random.RandomState` object should be used, which is built from a `random_state` argument passed to the class or function. The function `check_random_state`, below, can then be used to create a random number generator object.

- **check_random_state**: create a `numpy.random.RandomState` object from a parameter `random_state`.
  - If `random_state` is `None` or `numpy.random`, then a randomly-initialized `RandomState` object is returned.
  - If `random_state` is an integer, then it is used to seed a new `RandomState` object.
  - If `random_state` is a `RandomState` object, then it is passed through.

For example:

```python
>>> from sklearn.utils import check_random_state
>>> random_state = 0
>>> random_state = check_random_state(random_state)
>>> random_state.rand(4)
array([[ 0.5488135 , 0.71518937, 0.60276338, 0.54488318]])
```

When developing your own scikit-learn compatible estimator, the following helpers are available.
• **validation.check_is_fitted**: check that the estimator has been fitted before calling `transform`, `predict`, or similar methods. This helper allows to raise a standardized error message across estimator.

• **validation.has_fit_parameter**: check that a given parameter is supported in the `fit` method of a given estimator.

### 31.3.2 Efficient Linear Algebra & Array Operations

• **extmath.randomized_range_finder**: construct an orthonormal matrix whose range approximates the range of the input. This is used in `extmath.randomized_svd`, below.

• **extmath.randomized_svd**: compute the k-truncated randomized SVD. This algorithm finds the exact truncated singular values decomposition using randomization to speed up the computations. It is particularly fast on large matrices on which you wish to extract only a small number of components.

• **arrayfuncs.cholesky_delete**: (used in `sklearn.linear_model.least_angle.lars_path`) Remove an item from a cholesky factorization.

• **arrayfuncs.min_pos**: (used in `sklearn.linear_model.least_angle`) Find the minimum of the positive values within an array.

• **extmath.fast_logdet**: efficiently compute the log of the determinant of a matrix.

• **extmath.density**: efficiently compute the density of a sparse vector

• **extmath.safe_sparse_dot**: dot product which will correctly handle `scipy.sparse` inputs. If the inputs are dense, it is equivalent to `numpy.dot`.

• **extmath.weighted_mode**: an extension of `scipy.stats.mode` which allows each item to have a real-valued weight.

• **resample**: Resample arrays or sparse matrices in a consistent way. used in `shuffle`, below.

• **shuffle**: Shuffle arrays or sparse matrices in a consistent way. Used in `sklearn.cluster.k_means`.

### 31.3.3 Efficient Random Sampling

• **random.sample_without_replacement**: implements efficient algorithms for sampling `n_samples` integers from a population of size `n_population` without replacement.

### 31.3.4 Efficient Routines for Sparse Matrices

The `sklearn.utils.sparsefuncs` cython module hosts compiled extensions to efficiently process `scipy.sparse` data.

• **sparsefuncs.mean_variance_axis**: compute the means and variances along a specified axis of a CSR matrix. Used for normalizing the tolerance stopping criterion in `sklearn.cluster.k_means_.KMeans`.

• **sparsefuncs.inplace_csr_row_normalize_l1** and **sparsefuncs.inplace_csr_row_normalize_l2**: can be used to normalize individual sparse samples to unit L1 or L2 norm as done in `sklearn.preprocessing.Normalizer`.

• **sparsefuncs.inplace_csr_column_scale**: can be used to multiply the columns of a CSR matrix by a constant scale (one scale per column). Used for scaling features to unit standard deviation in `sklearn.preprocessing.StandardScaler`. 

### 31.3. Utilities for Developers
31.3.5 Graph Routines

- `graph.single_source_shortest_path_length`: (not currently used in scikit-learn) Return the shortest path from a single source to all connected nodes on a graph. Code is adapted from networkx. If this is ever needed again, it would be far faster to use a single iteration of Dijkstra’s algorithm from `graph_shortest_path`.

- `graph_shortest_path.graph_shortest_path`: (used in `sklearn.manifold.Isomap`) Return the shortest path between all pairs of connected points on a directed or undirected graph. Both the Floyd-Warshall algorithm and Dijkstra’s algorithm are available. The algorithm is most efficient when the connectivity matrix is a `scipy.sparse.csr_matrix`.

Benchmarking

- `bench.total_seconds` (back-ported from `timedelta.total_seconds` in Python 2.7). Used in benchmarks/bench_glm.py.

31.3.6 Testing Functions

- `testing.assert_in`, `testing.assert_not_in`: Assertions for container membership. Designed for forward compatibility with Nose 1.0.

- `testing.assert_raise_message`: Assertions for checking the error raise message.

- `testing.mock_mldata_urlopen`: Mocks the urlopen function to fake requests to mldata.org. Used in tests of `sklearn.datasets`.

- `testing.all_estimators`: returns a list of all estimators in scikit-learn to test for consistent behavior and interfaces.

31.3.7 Multiclass and multilabel utility function

- `multiclass.is_multilabel`: Helper function to check if the task is a multi-label classification one.

- `multiclass.is_label_indicator_matrix`: Helper function to check if a classification output is in label indicator matrix format.

- `multiclass.unique_labels`: Helper function to extract an ordered array of unique labels from different formats of target.

31.3.8 Helper Functions

- `gen_even_slices`: generator to create n-packs of slices going up to n. Used in `sklearn.decomposition.dict_learning` and `sklearn.cluster.k_means`.

- `safe_mask`: Helper function to convert a mask to the format expected by the numpy array or scipy sparse matrix on which to use it (sparse matrices support integer indices only while numpy arrays support both boolean masks and integer indices).

- `safe_sqr`: Helper function for unified squaring (`**2`) of array-likes, matrices and sparse matrices.
31.3.9 Hash Functions

- **murmurhash3_32** provides a python wrapper for the MurmurHash3_x86_32 C++ non cryptographic hash function. This hash function is suitable for implementing lookup tables, Bloom filters, Count Min Sketch, feature hashing and implicitly defined sparse random projections:

```python
>>> from sklearn.utils import murmurhash3_32
>>> murmurhash3_32("some feature", seed=0) == -384616559
True
>>> murmurhash3_32("some feature", seed=0, positive=True) == 3910350737
True
```

The sklearn.utils.murmurhash module can also be “cimported” from other cython modules so as to benefit from the high performance of MurmurHash while skipping the overhead of the Python interpreter.

31.3.10 Warnings and Exceptions

- **deprecated**: Decorator to mark a function or class as deprecated.
- **sklearn.exceptions.ConvergenceWarning**: Custom warning to catch convergence problems. Used in sklearn.covariance.graph_lasso.

31.4 How to optimize for speed

The following gives some practical guidelines to help you write efficient code for the scikit-learn project.

**Note:** While it is always useful to profile your code so as to check performance assumptions, it is also highly recommended to review the literature to ensure that the implemented algorithm is the state of the art for the task before investing into costly implementation optimization.

Times and times, hours of efforts invested in optimizing complicated implementation details have been rendered irrelevant by the subsequent discovery of simple algorithmic tricks, or by using another algorithm altogether that is better suited to the problem.

The section A sample algorithmic trick: warm restarts for cross validation gives an example of such a trick.

31.4.1 Python, Cython or C/C++?

In general, the scikit-learn project emphasizes the readability of the source code to make it easy for the project users to dive into the source code so as to understand how the algorithm behaves on their data but also for ease of maintainability (by the developers).

When implementing a new algorithm is thus recommended to start implementing it in Python using Numpy and Scipy by taking care of avoiding looping code using the vectorized idioms of those libraries. In practice this means trying to replace any nested for loops by calls to equivalent Numpy array methods. The goal is to avoid the CPU wasting time in the Python interpreter rather than crunching numbers to fit your statistical model. It’s generally a good idea to consider NumPy and SciPy performance tips: http://scipy.github.io/old-wiki/pages/PerformanceTips

Sometimes however an algorithm cannot be expressed efficiently in simple vectorized Numpy code. In this case, the recommended strategy is the following:
1. **Profile** the Python implementation to find the main bottleneck and isolate it in a dedicated module level function. This function will be reimplemented as a compiled extension module.

2. If there exists a well maintained BSD or MIT C/C++ implementation of the same algorithm that is not too big, you can write a **Cython wrapper** for it and include a copy of the source code of the library in the scikit-learn source tree: this strategy is used for the classes `svm.LinearSVC`, `svm.SVC` and `linear_model.LogisticRegression` (wrappers for liblinear and libsvm).

3. Otherwise, write an optimized version of your Python function using **Cython** directly. This strategy is used for the `linear_model.ElasticNet` and `linear_model.SGDClassifier` classes for instance.

4. **Move the Python version of the function in the tests** and use it to check that the results of the compiled extension are consistent with the gold standard, easy to debug Python version.

5. Once the code is optimized (not simple bottleneck spottable by profiling), check whether it is possible to have coarse grained parallelism that is amenable to multi-processing by using the `joblib.Parallel` class.

When using Cython, use either

```
$ python setup.py build_ext -i $ python setup.py install
```

to generate C files. You are responsible for adding `.c/.cpp` extensions along with build parameters in each submodule `setup.py`.

C/C++ generated files are embedded in distributed stable packages. The goal is to make it possible to install scikit-learn stable version on any machine with Python, Numpy, Scipy and C/C++ compiler.

### 31.4.2 Profiling Python code

In order to profile Python code we recommend to write a script that loads and prepare you data and then use the IPython integrated profiler for interactively exploring the relevant part for the code.

Suppose we want to profile the Non Negative Matrix Factorization module of the scikit. Let us setup a new IPython session and load the digits dataset and as in the Recognizing hand-written digits example:

```python
In [1]: from sklearn.decomposition import NMF
In [2]: from sklearn.datasets import load_digits
In [3]: X = load_digits().data
```

Before starting the profiling session and engaging in tentative optimization iterations, it is important to measure the total execution time of the function we want to optimize without any kind of profiler overhead and save it somewhere for later reference:

```
In [4]: %%timeit NMF(n_components=16, tol=1e-2).fit(X)
1 loops, best of 3: 1.7 s per loop
```

To have a look at the overall performance profile using the `%prun` magic command:

```
In [5]: %prun -l nmf.py NMF(n_components=16, tol=1e-2).fit(X)
14496 function calls in 1.682 CPU seconds

Ordered by: internal time
List reduced from 90 to 9 due to restriction '<nmf.py>'

ncalls  tottime  percall  cumtime  percall filename:lineno(function)
      36   0.609s   0.017s   1.499s   0.042s nmf.py:151(_nls_subproblem)
    1263   0.157s   0.000s   0.157s   0.000s nmf.py:18(_pos)
```

...
The `tottime` column is the most interesting: it gives to total time spent executing the code of a given function ignoring the time spent in executing the sub-functions. The real total time (local code + sub-function calls) is given by the `cumtime` column.

Note the use of the `-l nmf.py` that restricts the output to lines that contains the “nmf.py” string. This is useful to have a quick look at the hotspot of the nmf Python module it-self ignoring anything else.

Here is the beginning of the output of the same command without the `-l nmf.py` filter:

```bash
In [5] %prun NMF(n_components=16, tol=1e-2).fit(X)
16159 function calls in 1.840 CPU seconds
Ordered by: internal time
ncalls  tottime  percall  cumtime  percall filename:lineno(function)
2833  0.653  0.000   0.653  0.000 {numpy.core._dotblas.dot}
46    0.651  0.014  1.636  0.036 nmf.py:151(_nls_subproblem)
1397  0.171  0.000   0.171  0.000 nmf.py:18(_pos)
2780  0.167  0.000   0.167  0.000 {method 'sum' of 'numpy.ndarray'→}
2  0.064  0.032  1.840  0.920 nmf.py:352(fit_transform)
1542  0.043  0.000   0.043  0.000 {method 'flatten' of 'numpy.ndarray'→}
  1  0.019  0.000   0.019  0.000 {method 'all' of 'numpy.ndarray'→}
  2  0.010  0.005   0.010  0.005 {numpy.linalg.lapack_lite.dgesdd}
748  0.009  0.000   0.065  0.065 nmf.py:28(norm)
...
```

The above results show that the execution is largely dominated by dot products operations (delegated to blas). Hence there is probably no huge gain to expect by rewriting this code in Cython or C/C++: in this case out of the 1.7s total execution time, almost 0.7s are spent in compiled code we can consider optimal. By rewriting the rest of the Python code and assuming we could achieve a 1000% boost on this portion (which is highly unlikely given the shallowness of the Python loops), we would not gain more than a 2.4x speed-up globally.

Hence major improvements can only be achieved by **algorithmic improvements** in this particular example (e.g. trying to find operation that are both costly and useless to avoid computing then rather than trying to optimize their implementation).

It is however still interesting to check what’s happening inside the `_nls_subproblem` function which is the hotspot if we only consider Python code: it takes around 100% of the accumulated time of the module. In order to better understand the profile of this specific function, let us install `line_profiler` and wire it to IPython:

```bash
$ pip install line_profiler
```

- Under IPython 0.13+, first create a configuration profile:

```bash
$ ipython profile create
```
Then register the line_profiler extension in ~/.ipython/profile_default/ipython_config.py:

c.TerminalIPythonApp.extensions.append('line_profiler')
c.InteractiveShellApp.extensions.append('line_profiler')

This will register the %lprun magic command in the IPython terminal application and the other frontends such as qtconsole and notebook.

Now restart IPython and let us use this new toy:

```python
In [1]: from sklearn.datasets import load_digits
In [2]: from sklearn.decomposition.nmf import _nls_subproblem, NMF
In [3]: X = load_digits().data
In [4]: %lprun -f _nls_subproblem NMF(n_components=16, tol=1e-2).fit(X)
```

Timer unit: 1e-06 s

File: sklearn/decomposition/nmf.py
Function: _nls_subproblem at line 137
Total time: 1.73153 s

<table>
<thead>
<tr>
<th>Line</th>
<th>Hits</th>
<th>Time</th>
<th>Per Hit</th>
<th>% Time</th>
<th>Line Contents</th>
</tr>
</thead>
</table>
| 137  | def _nls_subproblem(V, W, H_init, tol, max_iter):
| 138  | """Non-negative least square solver"
| 170  | if (H_init < 0).any():
| 171  | raise ValueError("Negative values in H_init passed to NLS solver.")
| 172  | for n_iter in xrange(1, max_iter):
| 182  | grad = np.dot(WtW, H) - WtV
| 183  | proj_gradient = norm(grad[np.logical_or(grad < 0, H > 0)])
| 184  | if proj_gradient < tol:
| 185  | break
| 186  | for inner_iter in xrange(1,)
| 187  | Hn = H - alpha * grad
| 188  | dQd = np.sum(np.dot(WtW, d))
| 189  | dQd = np.sum(np.dot(WtW, d))
```
By looking at the top values of the % Time column it is really easy to pin-point the most expensive expressions that would deserve additional care.

### 31.4.3 Memory usage profiling

You can analyze in detail the memory usage of any Python code with the help of `memory_profiler`. First, install the latest version:

```bash
$ pip install -U memory_profiler
```

Then, setup the magics in a manner similar to `line_profiler`.

- **Under IPython 0.11+**, first create a configuration profile:

  ```bash
  $ ipython profile create
  ```

  Then register the extension in `~/.ipython/profile_default/ipython_config.py` alongside the line profiler:

  ```python
  c.TerminalIPythonApp.extensions.append('memory_profiler')
  c.InteractiveShellApp.extensions.append('memory_profiler')
  ```

  This will register the `%memit` and `%mprun` magic commands in the IPython terminal application and the other frontends such as qtconsole and notebook.

  `%mprun` is useful to examine, line-by-line, the memory usage of key functions in your program. It is very similar to `%lprun`, discussed in the previous section. For example, from the `memory_profiler` examples directory:

  ```python
  In [1]: from example import my_func
  In [2]: %mprun -f my_func my_func()
  Filename: example.py
  Line #    Mem usage      Increment  Line Contents
  ==================================================
  3         5.97 MB      0.00 MB  @profile
  4         7.64 MB      1.67 MB  def my_func():
  5         13.61 MB     152.59 MB  a = [1] * (10 ** 6)
  6         166.20 MB    152.59 MB  b = [2] * (2 * 10 ** 7)
  7         13.61 MB     -152.59 MB  del b
  8         13.61 MB      0.00 MB  return a
  ```

  Another useful magic that `memory_profiler` defines is `%memit`, which is analogous to `%timeit`. It can be used as follows:

  ```python
  In [1]: import numpy as np
  In [2]: %memit np.zeros(1e7)
  maximum of 3: 76.402344 MB per loop
  ```

  For more details, see the docstrings of the magics, using `%memit?` and `%mprun?`. 

31.4.4 Performance tips for the Cython developer

If profiling of the Python code reveals that the Python interpreter overhead is larger by one order of magnitude or more than the cost of the actual numerical computation (e.g. for loops over vector components, nested evaluation of conditional expression, scalar arithmetic...), it is probably adequate to extract the hotspot portion of the code as a standalone function in a .pyx file, add static type declarations and then use Cython to generate a C program suitable to be compiled as a Python extension module.

The official documentation available at http://docs.cython.org/ contains a tutorial and reference guide for developing such a module. In the following we will just highlight a couple of tricks that we found important in practice on the existing cython codebase in the scikit-learn project.

TODO: html report, type declarations, bound checks, division by zero checks, memory alignment, direct blas calls...

- https://www.youtube.com/watch?v=gMvkiQ-gOW8

31.4.5 Profiling compiled extensions

When working with compiled extensions (written in C/C++ with a wrapper or directly as Cython extension), the default Python profiler is useless: we need a dedicated tool to introspect what’s happening inside the compiled extension itself.

Using yep and google-perftools

Easy profiling without special compilation options use yep:

- https://pypi.python.org/pypi/yep
- http://fa.bianp.net/blog/2011/a-profiler-for-python-extensions

Note: google-perftools provides a nice ‘line by line’ report mode that can be triggered with the --lines option. However this does not seem to work correctly at the time of writing. This issue can be tracked on the project issue tracker.

Using gprof

In order to profile compiled Python extensions one could use gprof after having recompiled the project with gcc -pg and using the python-dbq variant of the interpreter on debian / ubuntu: however this approach requires to also have numpy and scipy recompiled with -pg which is rather complicated to get working.

Fortunately there exist two alternative profilers that don’t require you to recompile everything.

Using valgrind / callgrind / kcachegrind

TODO
31.4.6 Multi-core parallelism using joblib.Parallel

TODO: give a simple teaser example here.

Checkout the official joblib documentation:

- https://pythonhosted.org/joblib

31.4.7 A sample algorithmic trick: warm restarts for cross validation

TODO: demonstrate the warm restart tricks for cross validation of linear regression with Coordinate Descent.

31.5 Advanced installation instructions

There are different ways to get scikit-learn installed:

- Install the version of scikit-learn provided by your operating system or Python distribution. This is the quickest option for those who have operating systems that distribute scikit-learn.
- Install an official release. This is the best approach for users who want a stable version number and aren’t concerned about running a slightly older version of scikit-learn.
- Install the latest development version. This is best for users who want the latest-and-greatest features and aren’t afraid of running brand-new code.

Note: If you wish to contribute to the project, you need to install the latest development version.

31.5.1 Installing an official release

Scikit-learn requires:

- Python (>= 2.7 or >= 3.3),
- NumPy (>= 1.8.2),
- SciPy (>= 0.13.3).

Mac OSX

Scikit-learn and its dependencies are all available as wheel packages for OSX:

```
pip install -U numpy scipy scikit-learn
```

Linux

At this time scikit-learn does not provide official binary packages for Linux so you have to build from source if you want the latest version. If you don’t need the newest version, consider using your package manager to install scikit-learn. It is usually the easiest way, but might not provide the newest version.
Installing build dependencies

Installing from source requires you to have installed the scikit-learn runtime dependencies, Python development headers and a working C/C++ compiler. Under Debian-based operating systems, which include Ubuntu, if you have Python 2 you can install all these requirements by issuing:

```bash
sudo apt-get install build-essential python-dev python-setuptools \
    python-numpy python-scipy \
    libatlas-dev libatlas3gf-base
```

If you have Python 3:

```bash
sudo apt-get install build-essential python3-dev python3-setuptools \
    python3-numpy python3-scipy \
    libatlas-dev libatlas3gf-base
```

On recent Debian and Ubuntu (e.g. Ubuntu 13.04 or later) make sure that ATLAS is used to provide the implementation of the BLAS and LAPACK linear algebra routines:

```bash
sudo update-alternatives --set libblas.so.3 /usr/lib/atlas-base/atlas/libblas.so.3
sudo update-alternatives --set liblapack.so.3 /usr/lib/atlas-base/atlas/liblapack.so.3
```

**Note:** In order to build the documentation and run the example code contains in this documentation you will need matplotlib:

```bash
sudo apt-get install python-matplotlib
```

**Note:** The above installs the ATLAS implementation of BLAS (the Basic Linear Algebra Subprograms library). Ubuntu 11.10 and later, and recent (testing) versions of Debian, offer an alternative implementation called OpenBLAS. Using OpenBLAS can give speedups in some scikit-learn modules, but can freeze joblib/multiprocessing prior to OpenBLAS version 0.2.8-4, so using it is not recommended unless you know what you’re doing.

If you do want to use OpenBLAS, then replacing ATLAS only requires a couple of commands. ATLAS has to be removed, otherwise NumPy may not work:

```bash
sudo apt-get remove libatlas3gf-base libatlas-dev
sudo apt-get install libopenblas-dev
sudo update-alternatives --set libblas.so.3 /usr/lib/openblas-base/libopenblas.so.0
sudo update-alternatives --set liblapack.so.3 /usr/lib/lapack/liblapack.so.3
```

On Red Hat and clones (e.g. CentOS), install the dependencies using:

```bash
sudo yum -y install gcc gcc-c++ numpy python-devel scipy
```
### Building scikit-learn with pip

This is usually the fastest way to install or upgrade to the latest stable release:

```bash
pip install --user --install-option="--prefix=" -U scikit-learn
```

The `--user` flag asks pip to install scikit-learn in the `$HOME/.local` folder therefore not requiring root permission. This flag should make pip ignore any old version of scikit-learn previously installed on the system while benefiting from system packages for numpy and scipy. Those dependencies can be long and complex to build correctly from source.

The `--install-option="--prefix="` flag is only required if Python has a `distutils.cfg` configuration with a predefined `prefix=` entry.

### From source package

download the source package from pypi, unpack the sources and cd into the source directory.

This packages uses distutils, which is the default way of installing python modules. The install command is:

```bash
python setup.py install
```

or alternatively (also from within the scikit-learn source folder):

```bash
pip install .
```

**Warning:** Packages installed with the `python setup.py install` command cannot be uninstalled nor upgraded by `pip` later. To properly uninstall scikit-learn in that case it is necessary to delete the `sklearn` folder from your Python `site-packages` directory.

### Windows

First, you need to install numpy and scipy from their own official installers.

Wheel packages (.whl files) for scikit-learn from pypi can be installed with the `pip` utility. Open a console and type the following to install or upgrade scikit-learn to the latest stable release:

```bash
pip install -U scikit-learn
```

If there are no binary packages matching your python, version you might to try to install scikit-learn and its dependencies from christoph gohlke unofficial windows installers or from a python distribution instead.

### 31.5.2 Third party distributions of scikit-learn

Some third-party distributions are now providing versions of scikit-learn integrated with their package-management systems.

These can make installation and upgrading much easier for users since the integration includes the ability to automatically install dependencies (numpy, scipy) that scikit-learn requires.

The following is an incomplete list of python and os distributions that provide their own version of scikit-learn.
MacPorts for Mac OSX

The MacPorts package is named py<XY>-scikits-learn, where XY denotes the Python version. It can be installed by typing the following command:

```
sudo port install py26-scikit-learn
```
or:

```
sudo port install py27-scikit-learn
```

Arch Linux

Arch Linux’s package is provided through the official repositories as python-scikit-learn for Python 3 and python2-scikit-learn for Python 2. It can be installed by typing the following command:

```
# pacman -S python-scikit-learn
```
or:

```
# pacman -S python2-scikit-learn
```
depending on the version of Python you use.

NetBSD

scikit-learn is available via pkgsrc-wip:

```
http://pkgsrc.se/wip/py-scikit_learn
```

Fedora

The Fedora package is called python-scikit-learn for the Python 2 version and python3-scikit-learn for the Python 3 version. Both versions can be installed using yum:

```
$ sudo yum install python-scikit-learn
```
or:

```
$ sudo yum install python3-scikit-learn
```

Building on windows

To build scikit-learn on Windows you need a working C/C++ compiler in addition to numpy, scipy and setuptools.

Picking the right compiler depends on the version of Python (2 or 3) and the architecture of the Python interpreter, 32-bit or 64-bit. You can check the Python version by running the following in cmd or powershell console:

```
python --version
```
and the architecture with:
The above commands assume that you have the Python installation folder in your PATH environment variable.

### 32-bit Python

For 32-bit python it is possible use the standalone installers for Microsoft visual C++ express 2008 for Python 2 or Microsoft Visual C++ Express 2010 for Python 3.

Once installed you should be able to build scikit-learn without any particular configuration by running the following command in the scikit-learn folder:

```
python setup.py install
```

### 64-bit Python

For the 64-bit architecture, you either need the full Visual Studio or the free Windows SDKs that can be downloaded from the links below.

The Windows SDKs include the MSVC compilers both for 32 and 64-bit architectures. They come as a GRMSDKX_EN_DVD.iso file that can be mounted as a new drive with a setup.exe installer in it.

- For Python 2 you need SDK v7.0: MS Windows SDK for Windows 7 and .NET Framework 3.5 SP1
- For Python 3 you need SDK v7.1: MS Windows SDK for Windows 7 and .NET Framework 4

Both SDKs can be installed in parallel on the same host. To use the Windows SDKs, you need to setup the environment of a cmd console launched with the following flags (at least for SDK v7.0):

```cmd
/E:ON /V:ON
```

Then configure the build environment with:

```cmd
SET DISTUTILS_USE_SDK=1
SET MSSdk=1
"C:\Program Files\Microsoft SDKs\Windows\v7.0\Setup\WindowsSdkVer.exe" -q -version:v7.0
"C:\Program Files\Microsoft SDKs\Windows\v7.0\Bin\SetEnv.cmd" /x64 /release
```

Finally you can build scikit-learn in the same cmd console:

```
python setup.py install
```

Replace v7.0 by the v7.1 in the above commands to do the same for Python 3 instead of Python 2.

Replace /x64 by /x86 to build for 32-bit Python instead of 64-bit Python.

### Building binary packages and installers

The .whl package and .exe installers can be built with:

```
pip install wheel
python setup.py bdist_wheel bdist_wininst -b doc/logos/scikit-learn-logo.bmp
```

The resulting packages are generated in the `dist/` folder.
Using an alternative compiler

It is possible to use MinGW (a port of GCC to Windows OS) as an alternative to MSVC for 32-bit Python. Not that extensions built with mingw32 can be redistributed as reusable packages as they depend on GCC runtime libraries typically not installed on end-users environment.

To force the use of a particular compiler, pass the --compiler flag to the build step:

```
python setup.py build --compiler=my_compiler install
```

where my_compiler should be one of mingw32 or msvc.

31.5.3 Bleeding Edge

See section Retrieving the latest code on how to get the development version. Then follow the previous instructions to build from source depending on your platform. You will also require Cython >=0.23 in order to build the development version.

31.5.4 Testing

Testing scikit-learn once installed

Testing requires having the nose library. After installation, the package can be tested by executing from outside the source directory:

```
$ nosetests -v sklearn
```

Under Windows, it is recommended to use the following command (adjust the path to the python.exe program) as using the nosetests.exe program can badly interact with tests that use multiprocessing:

```
C:\Python34\python.exe -c "import nose; nose.main()" -v sklearn
```

This should give you a lot of output (and some warnings) but eventually should finish with a message similar to:

```
Ran 3246 tests in 260.618s
OK (SKIP=20)
```

Otherwise, please consider posting an issue into the bug tracker or to the Mailing List including the traceback of the individual failures and errors. Please include your operating system, your version of NumPy, SciPy and scikit-learn, and how you installed scikit-learn.

Testing scikit-learn from within the source folder

Scikit-learn can also be tested without having the package installed. For this you must compile the sources inplace from the source directory:

```
python setup.py build_ext --inplace
```

Test can now be run using nosetests:

```
nosetests -v sklearn/
```

This is automated by the commands:
You can also install a symlink named `site-packages/scikit-learn.egg-link` to the development folder of scikit-learn with:

```
pip install --editable .
```

### 31.6 Maintainer / core-developer information

For more information see https://github.com/scikit-learn/scikit-learn/wiki/How-to-make-a-release

#### 31.6.1 Making a release

1. Update docs:
   - edit the doc/whats_new.rst file to add release title and commit statistics. You can retrieve commit statistics with:
     ```
     $ git shortlog -ns 0.998..
     ```
   - edit the doc/conf.py to increase the version number
   - edit the doc/themes/scikit-learn/layout.html to change the `News` entry of the front page.

2. Update the version number in sklearn/__init__.py, the `__version__` variable

3. Create the tag and push it:

   ```
   $ git tag 0.999
   $ git push origin --tags
   ```

4. create tarballs:
   - Wipe clean your repo:
     ```
     $ git clean -xfd
     ```
   - Register and upload on PyPI:
     ```
     $ python setup.py sdist register upload
     ```

5. Push the documentation to the website (see README in doc folder)

6. Build binaries using dedicated CI servers by updating the git submodule reference to the new scikit-learn tag of the release at:

   https://github.com/MacPython/scikit-learn-wheels

   Once the CI has completed successfully, collect the generated binary wheel packages and upload them to PyPI by running the following commands in the scikit-learn source folder (checked out at the release tag):

   ```
   $ python setup.py sdist register upload
   ```
$ pip install -U wheelhouse_uploader
$ python setup.py sdist fetch_artifacts upload_all

7. FOR FINAL RELEASE: Update the release date in What’s New


[R14] Obtaining calibrated probability estimates from decision trees and naive Bayesian classifiers, B. Zadrozny & C. Elkan, ICML 2001


[R44] Predicting Good Probabilities with Supervised Learning, A. Niculescu-Mizil & R. Caruana, ICML 2005


[R411414] Mutual Information on Wikipedia.


[R97100] Mutual Information on Wikipedia.


[R105106] Peter J. Huber, Elvezio M. Ronchetti, Robust Statistics Concomitant scale estimates, pg 172


[R109111] https://en.wikipedia.org/wiki/RANSAC


[R116117] Wikipedia entry on the Least-angle regression

[R117117] Wikipedia entry on the Lasso


[R528529] Wikipedia entry for the F1-score

[R529529] Discriminative Methods for Multi-labeled Classification Advances in Knowledge Discovery and Data Mining (2004), pp. 22-30 by Shantanu Godbole, Sunita Sarawagi

[R535535] Wikipedia entry for the Receiver operating characteristic

[R167167] Wikipedia entry for the Receiver operating characteristic

[R165165] Wikipedia entry on the Coefficient of determination


[R140140] Wikipedia entry for the Adjusted Mutual Information


[wk142144] https://en.wikipedia.org/wiki/Rand_index#Adjusted_Rand_index


[R500500] Wikipedia entry for the Fowlkes-Mallows Index


[R174174] Wikipedia entry on the Silhouette Coefficient


[R170170] Wikipedia entry on the Silhouette Coefficient


[MRT358360] A randomized algorithm for the decomposition of matrices Per-Gunnar Martinsson, Vladimir Rokhlin and Mark Tygert


Symbols

___call___ (sklearn.gaussian_process.kernels.CompoundKernel method), 1523
___call___ (sklearn.gaussian_process.kernels.ConstantKernel method), 1525
___call___ (sklearn.gaussian_process.kernels.DotProduct method), 1527
___call___ (sklearn.gaussian_process.kernels.ExpSineSquared method), 1530
___call___ (sklearn.gaussian_process.kernels.Exponentiation method), 1532
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__init__ (sklearn.base.ClusterMixin method), 1208
__init__ (sklearn.base.DensityMixin method), 1209
__init__ (sklearn.base.RegressorMixin method), 1209
__init__ (sklearn.base.TransformerMixin method), 1209
__init__ (sklearn.calibration.CalibratedClassifierCV method), 1213
__init__ (sklearn.cluster.AffinityPropagation method), 1217
__init__ (sklearn.cluster.AgglomerativeClustering method), 1219
__init__ (sklearn.cluster.Birch method), 1222
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